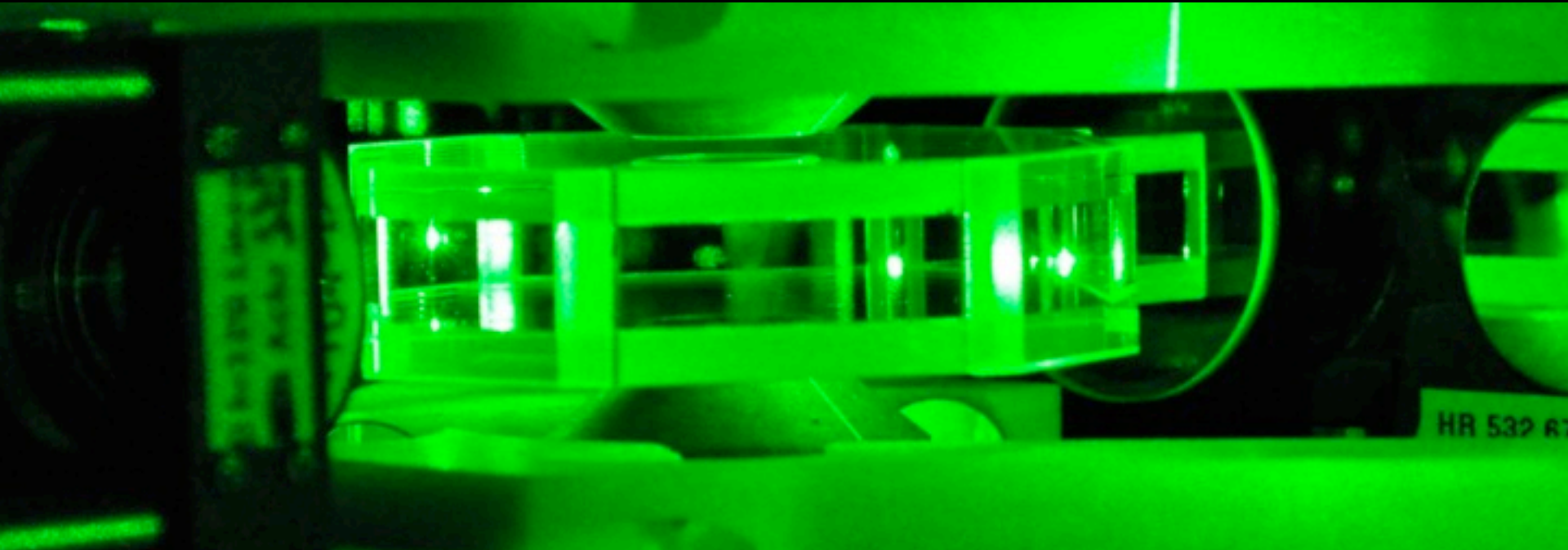


# Transport experiments with ultracold Fermions



J.P. Brantut, J. Meineke, D. Stadler, S. Krinner, D. Husmann, S. Häusler, T. Esslinger

Institute for Quantum Electronics  
ETH Zürich

# Cold atoms and condensed matter physics

	Cold Fermionic atoms	Electrons in a solid
Density	$10^{12} \text{ cm}^{-3}$	$10^{22} \text{ cm}^{-3}$ (Metals)

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Interparticle spacing:  $1 \mu\text{m}$

*Wavelength of atomic wave functions is in the optical domain  
-> optical lattices, microscopic disorder, etc*

# Cold atoms and condensed matter physics

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Density	$10^{12} \text{ cm}^{-3}$	$10^{22} \text{ cm}^{-3}$ (Metals)
Mass	6 (Li), 40 (K)	$5.4 \cdot 10^{-4}$

Interparticle spacing:  $1 \mu\text{m}$

Fermi temperature:  $1 \mu\text{K}$

*Requires laser cooling + evaporation*

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Temperature	100 nK	10 mK

Temperature range :  $\frac{T}{T_F} \sim 0.1$

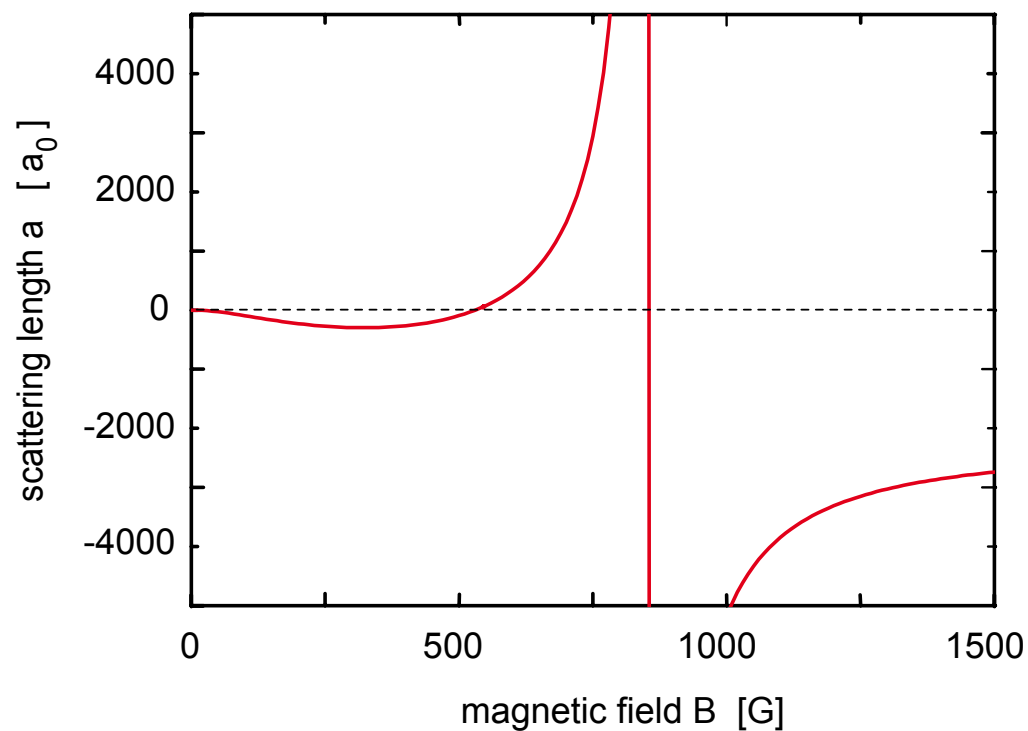
*Requires laser cooling + evaporation (+ new ideas ?)*

# Cold atoms and condensed matter physics

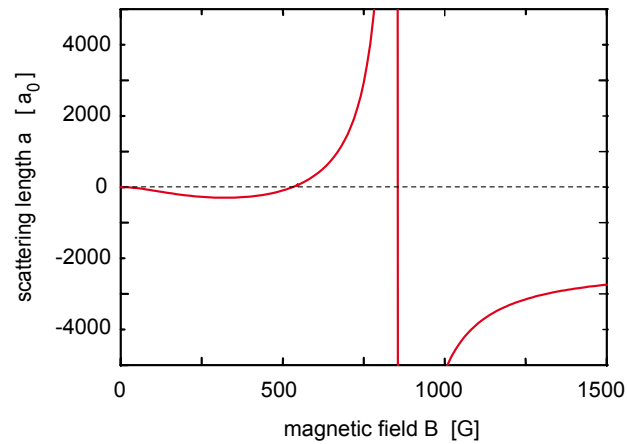
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# Feshbach resonances

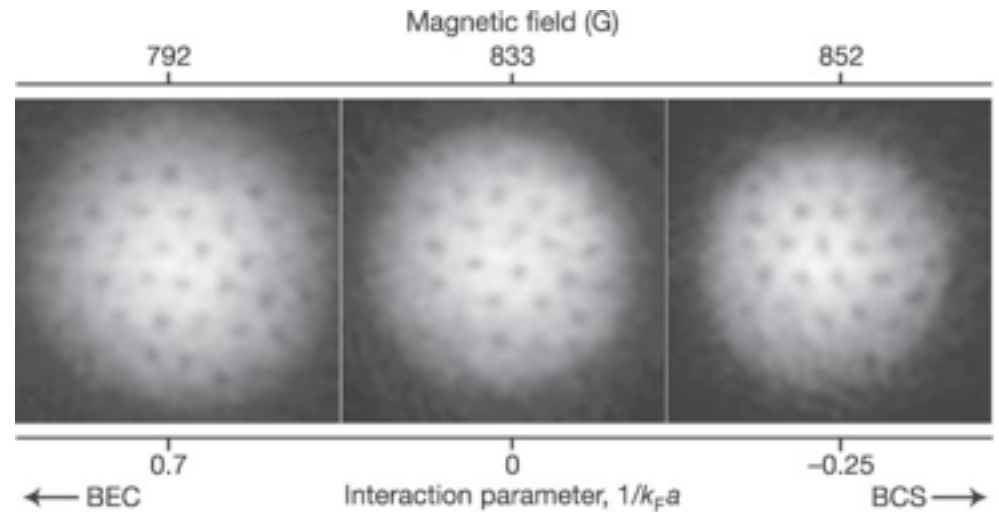
*Use the internal structure of atoms to manipulate scattering*



# Feshbach resonances



Superfluidity emerges at low temperatures



M. Zwierlein *et al*, Nature **435**, 1047 (2005)



# Cold atoms and condensed matter physics

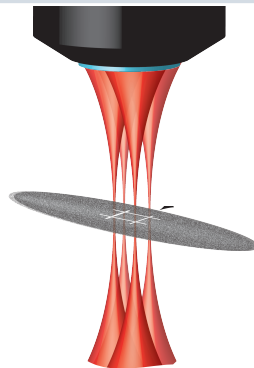
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*K. Ensslin, ETH*

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Probing	Imaging, spectroscopy	AC/DC characteristics, response functions...

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# From materials to devices

*Material*

e<sup>-</sup> gas

atoms

# From materials to devices

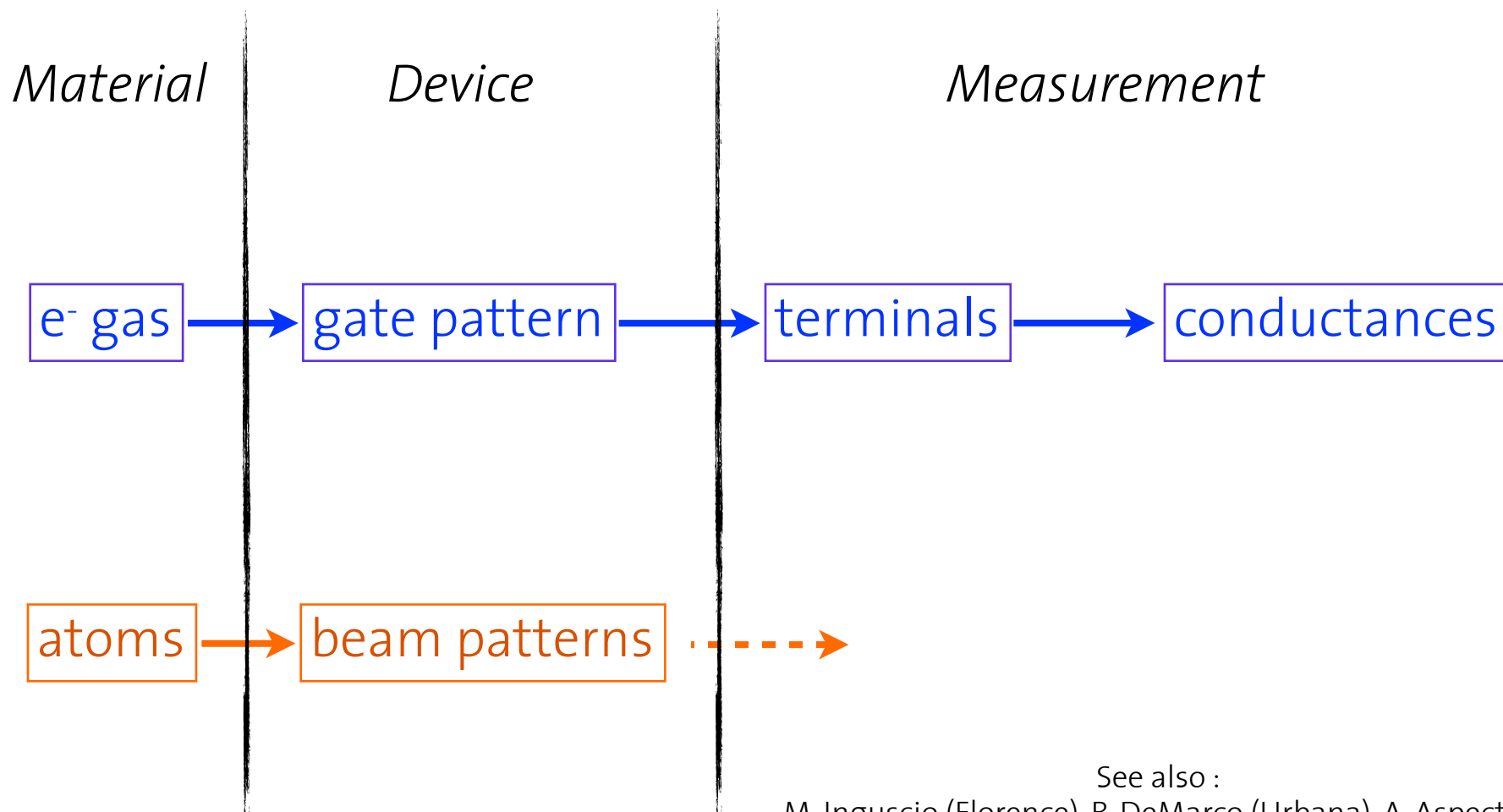
*Material*

*Device*

e<sup>-</sup> gas → gate pattern

atoms → beam patterns

# From materials to devices



See also :  
M. Inguscio (Florence), B. DeMarco (Urbana), A. Aspect (Palaiseau), I. Bloch (Munich), C. Chin (Chicago)...

- Experimental setup
  - Two terminals Landauer configuration
  - Strongly attractive interactions: superfluids
  - Disordered superfluids
  
- Thermoelectric transport

*Theory : Charles Grenier, Corinna Kollath and Antoine Georges*

  - Ballistic channel
  - Disordered channel : ballistic to diffusive crossover
  - Efficiency of heat to work conversion
  
- Outlook
  - Lithography for cold atoms

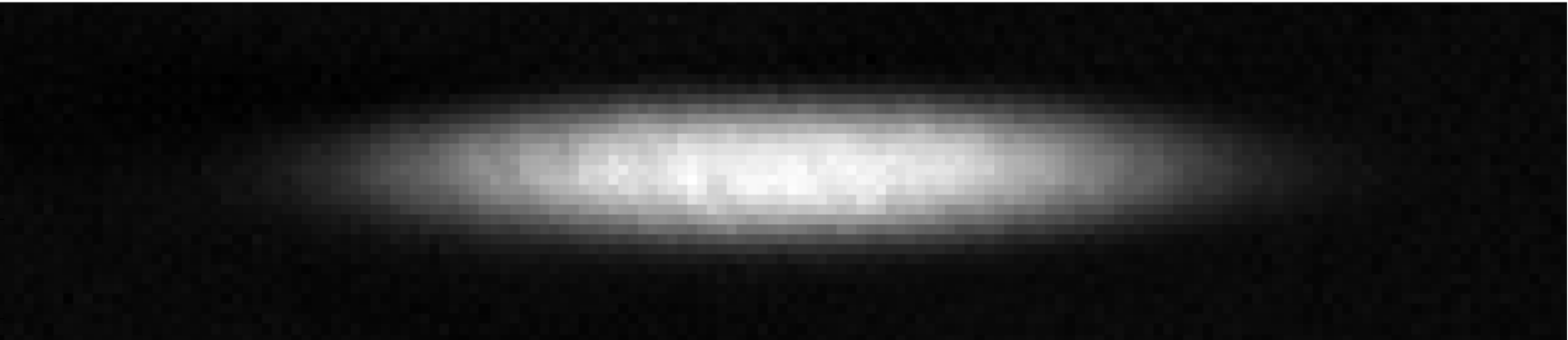


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# Two-terminals setup

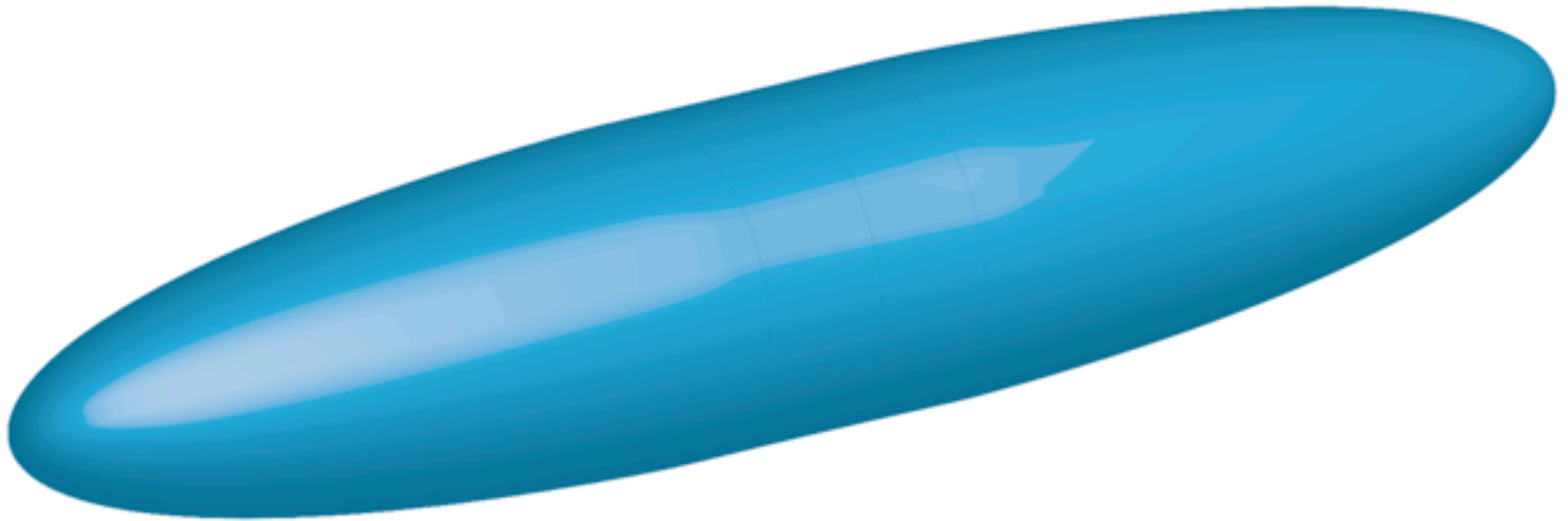


$10^5$   ${}^6\text{Li}$  atoms

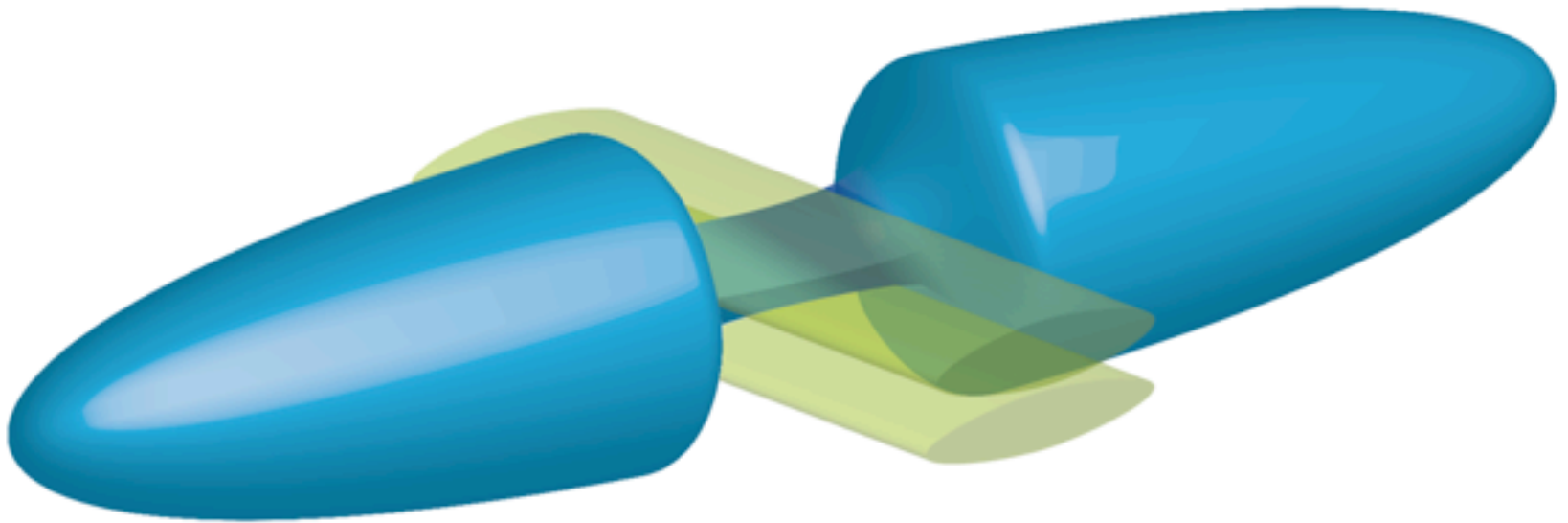
$$T \sim 0.2 T_F$$

$$T_F = 930 \text{ nK}$$

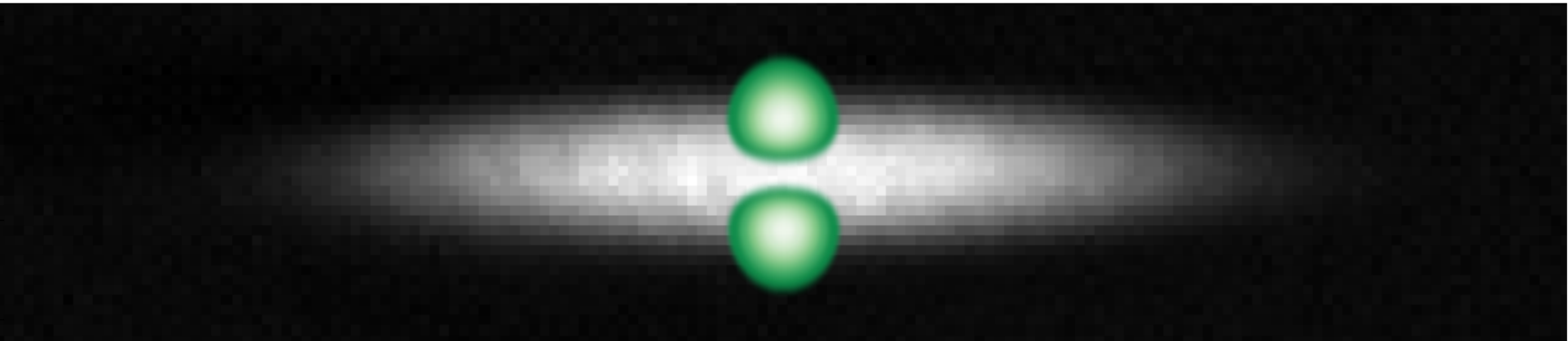
# Two-terminals setup



# Two-terminals setup



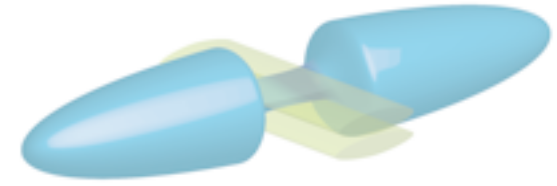
# Two-terminals setup



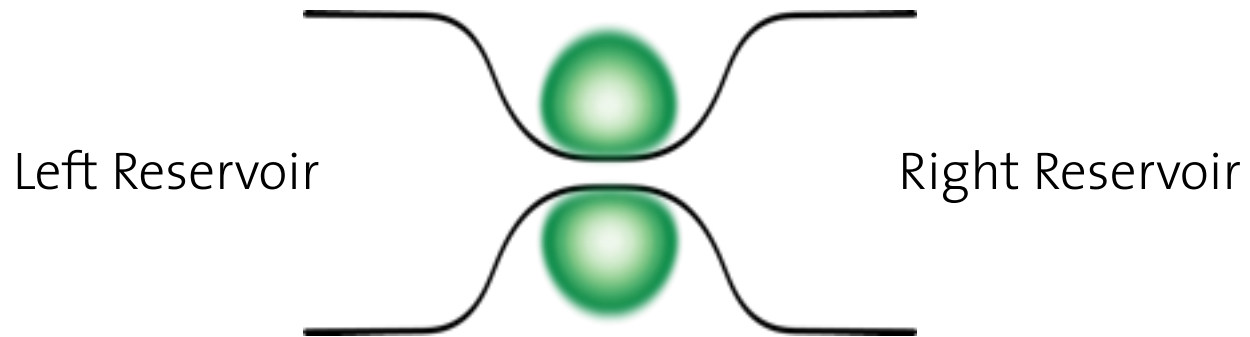
Repulsive  $TEM_{01}$  laser beam on the center of the cloud

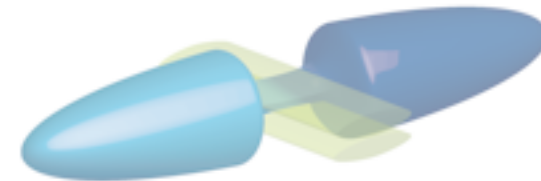
Trap frequency up to 11 kHz

Creates a narrow multimode, *ballistic* channel

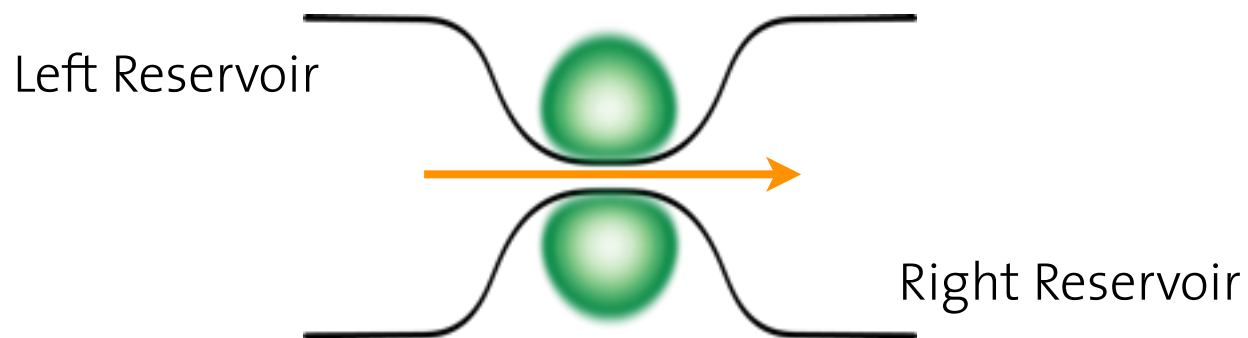


# Two-terminals setup



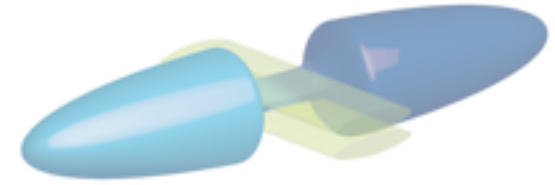


# Two-terminals setup



$$N_{\text{Left}} > N_{\text{Right}}$$

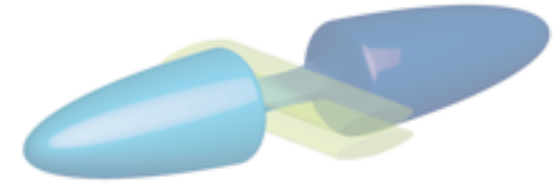
# Linear response



*Ohm's Law*  
channel

$$I_N = G \cdot \Delta\mu$$





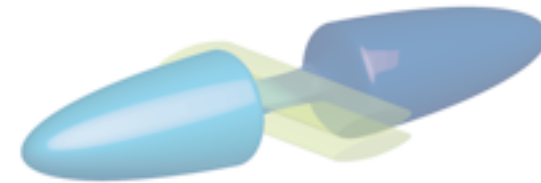
# Linear response

*Ohm's Law*  
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*Thermodynamic relations*  
Reservoirs

$$\Delta\mu = \frac{1}{\kappa} \Delta N$$



# Linear response

*Ohm's Law*  
**channel**

$$I_N = G \cdot \Delta\mu$$

*Thermodynamic relations*  
**Reservoirs**

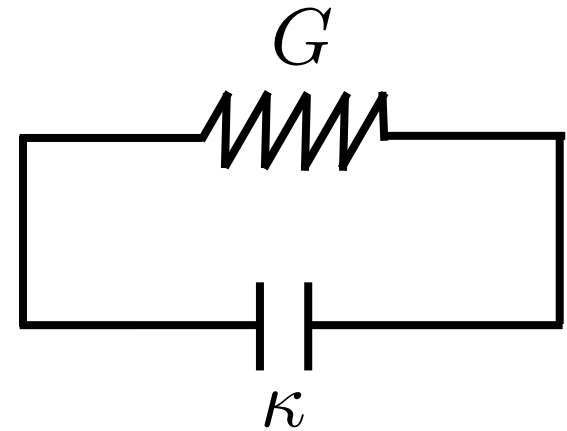
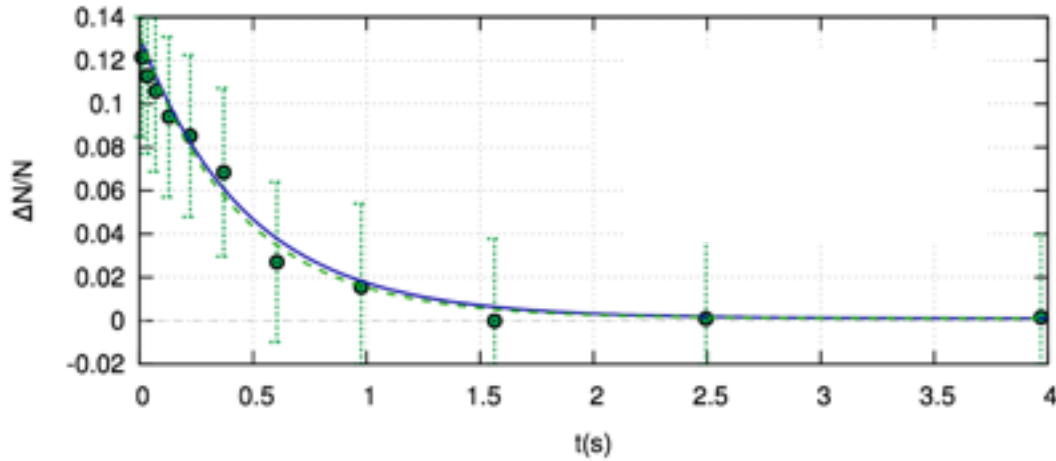
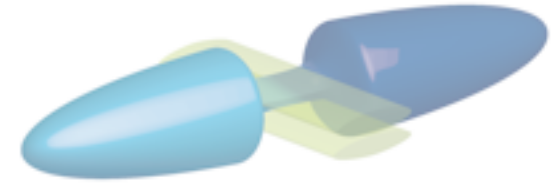
$$\Delta\mu = \frac{1}{\kappa} \Delta N$$

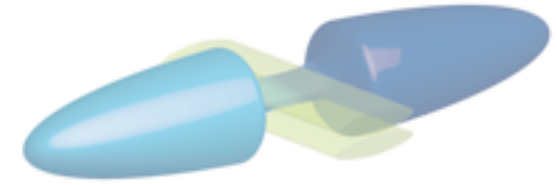
*Continuity equation*

$$I_N = \dot{\Delta N}$$

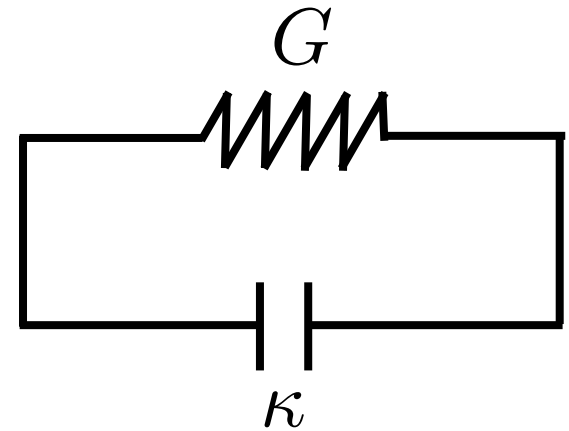
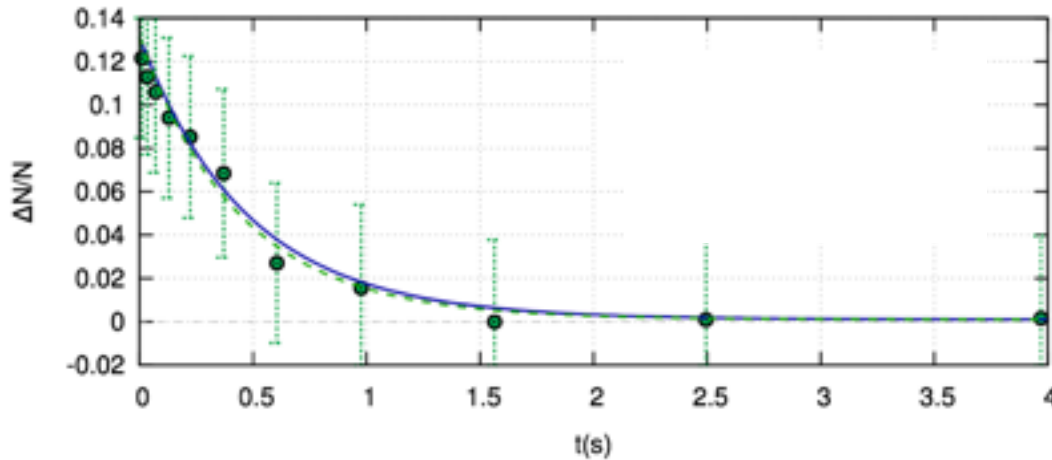
$$\dot{\Delta N} = \frac{G}{\kappa} \Delta N$$

# Atomic flow through the channel



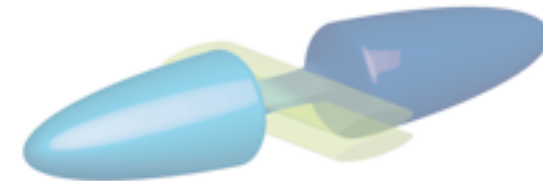


# Atomic flow through the channel

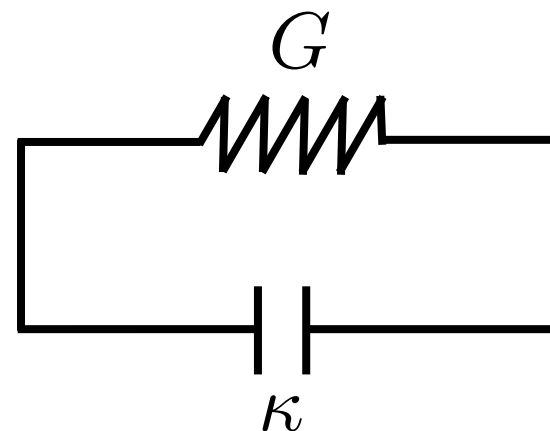
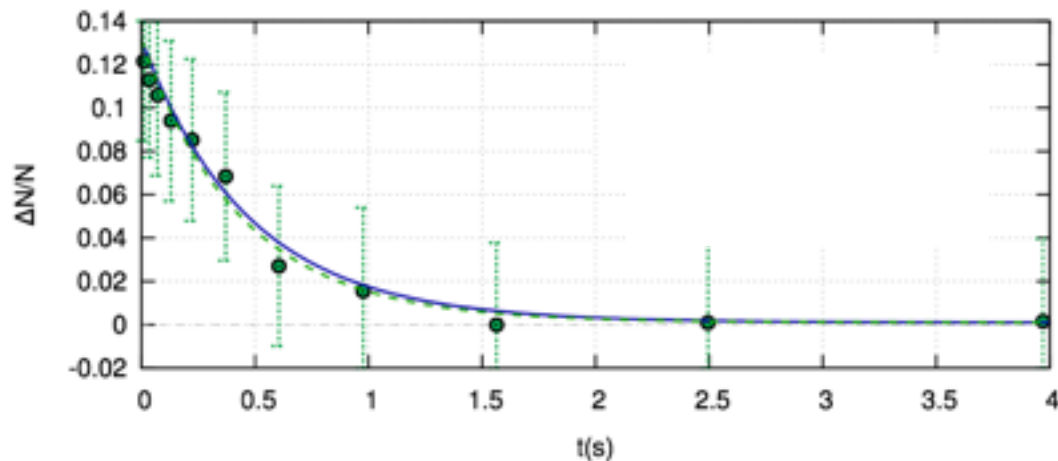


Ballistic channel :

$$\kappa/G = 481(30) \text{ ms} \quad \textit{Experimental fit}$$



# Atomic flow through the channel



Ballistic channel :

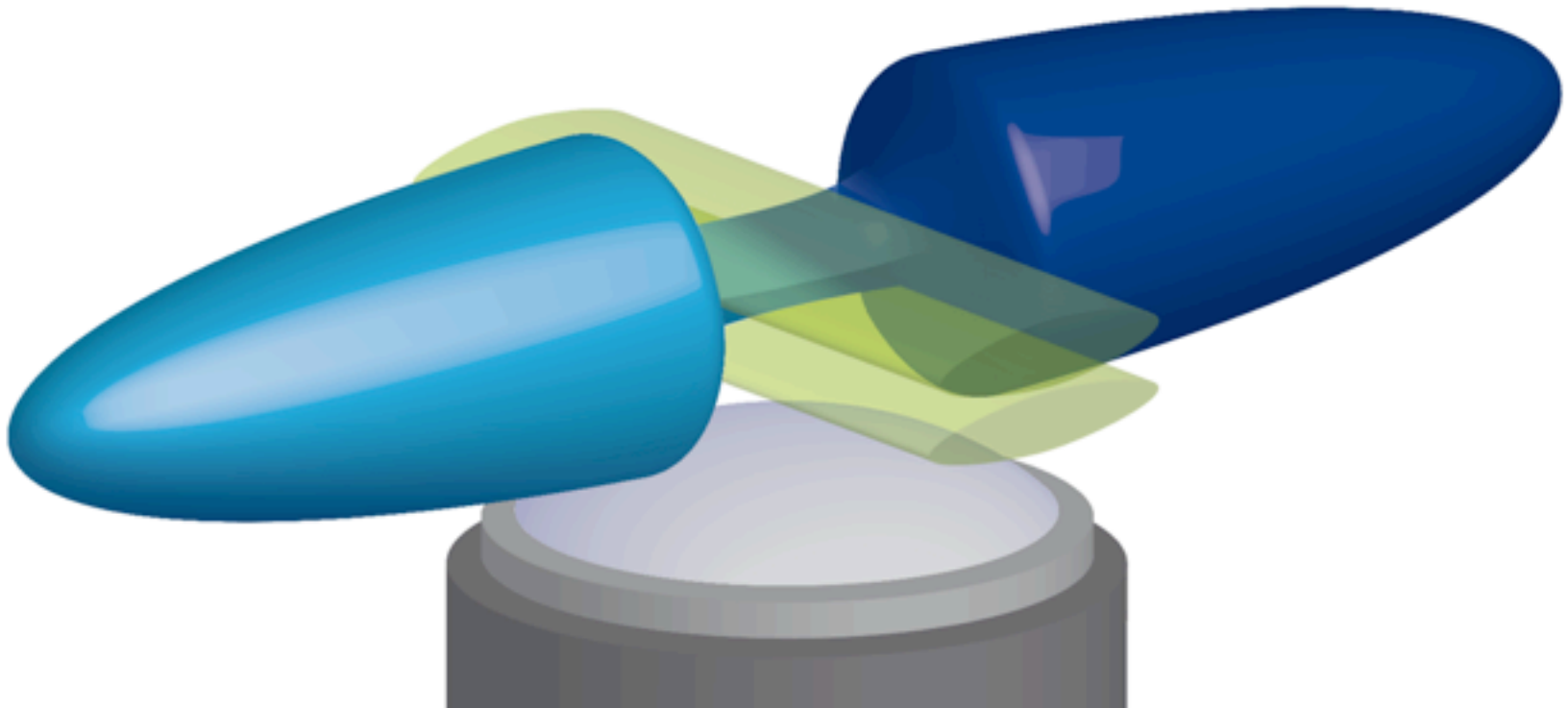
$$\kappa/G = 481(30) \text{ ms}$$

*Experimental fit*

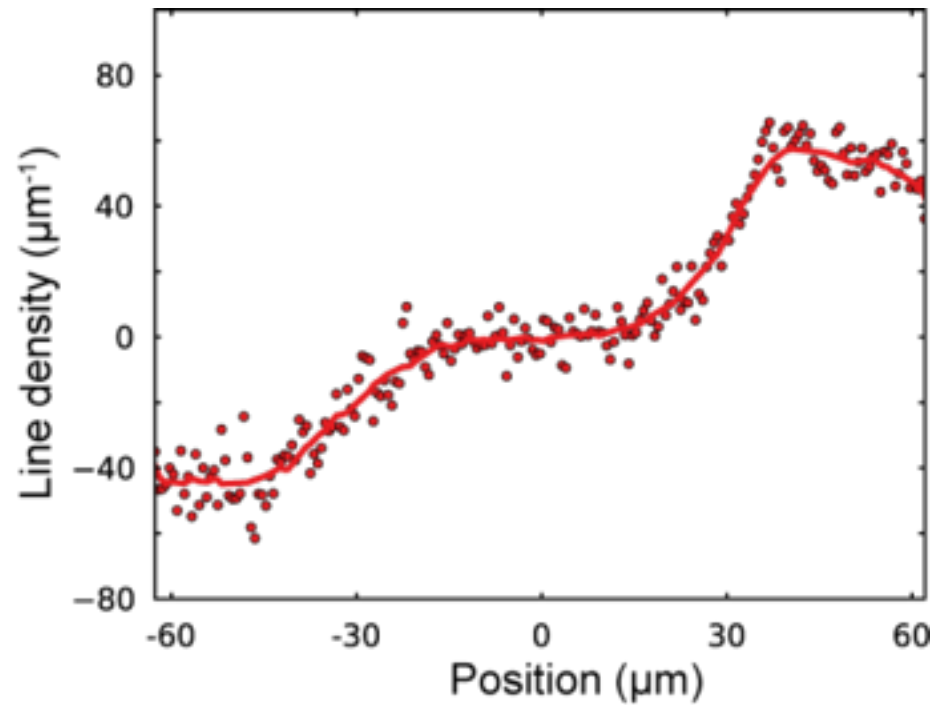
$$\kappa/G = 450(30) \text{ ms}$$

*Landauer-Büttiker + ideal reservoirs*

# Where does the voltage drop ?

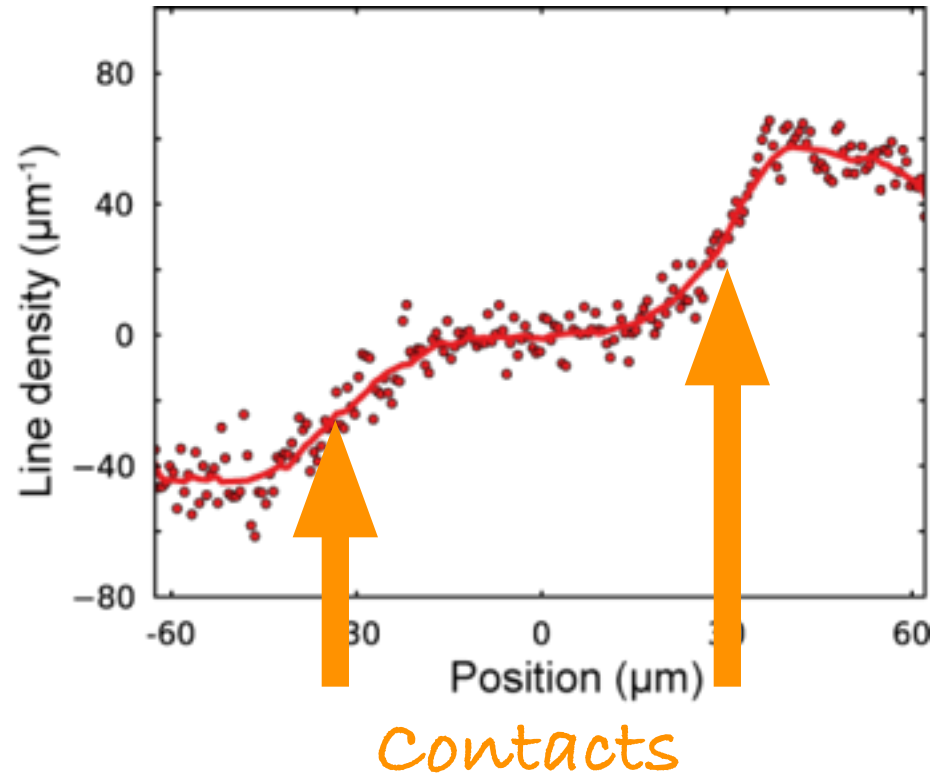


# Where does the voltage drop ?



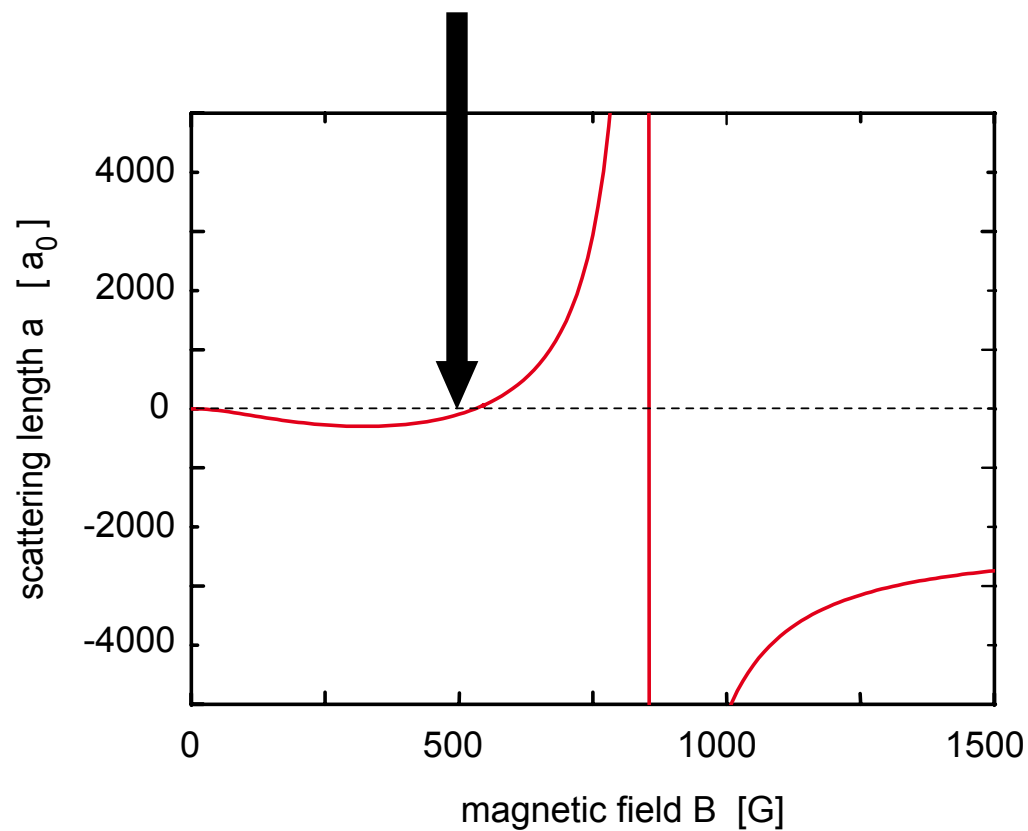


# Where does the voltage drop ?

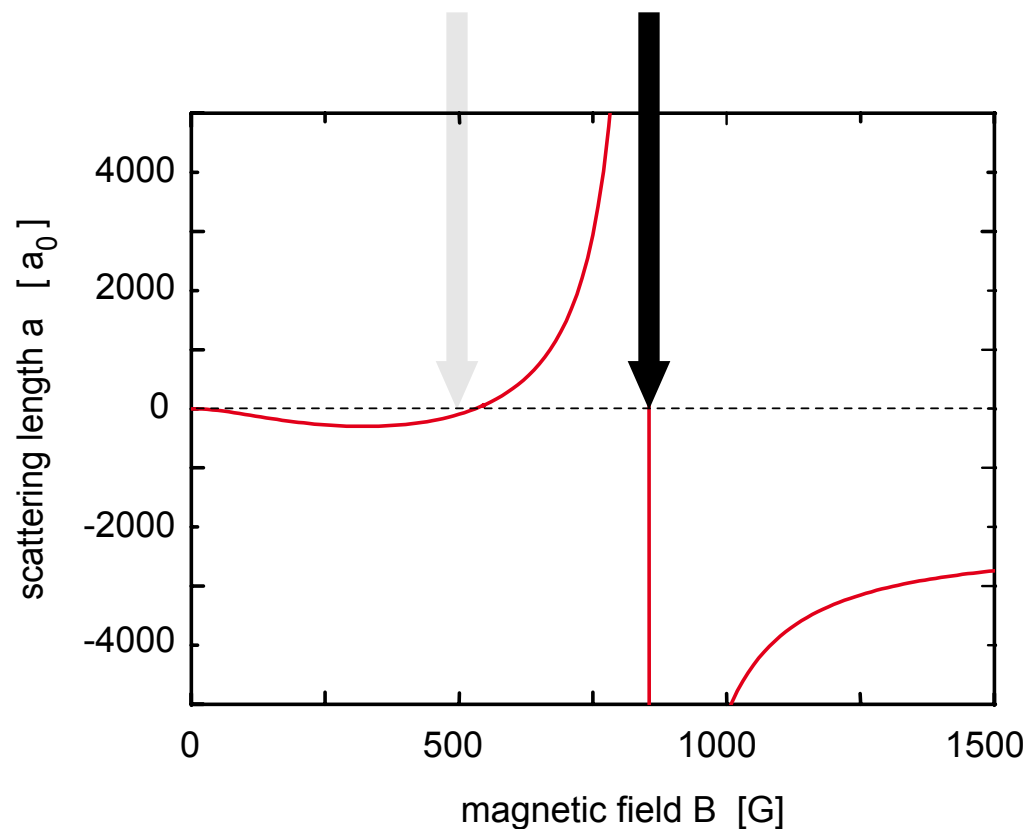




# Resistance of cold atom systems : interactions

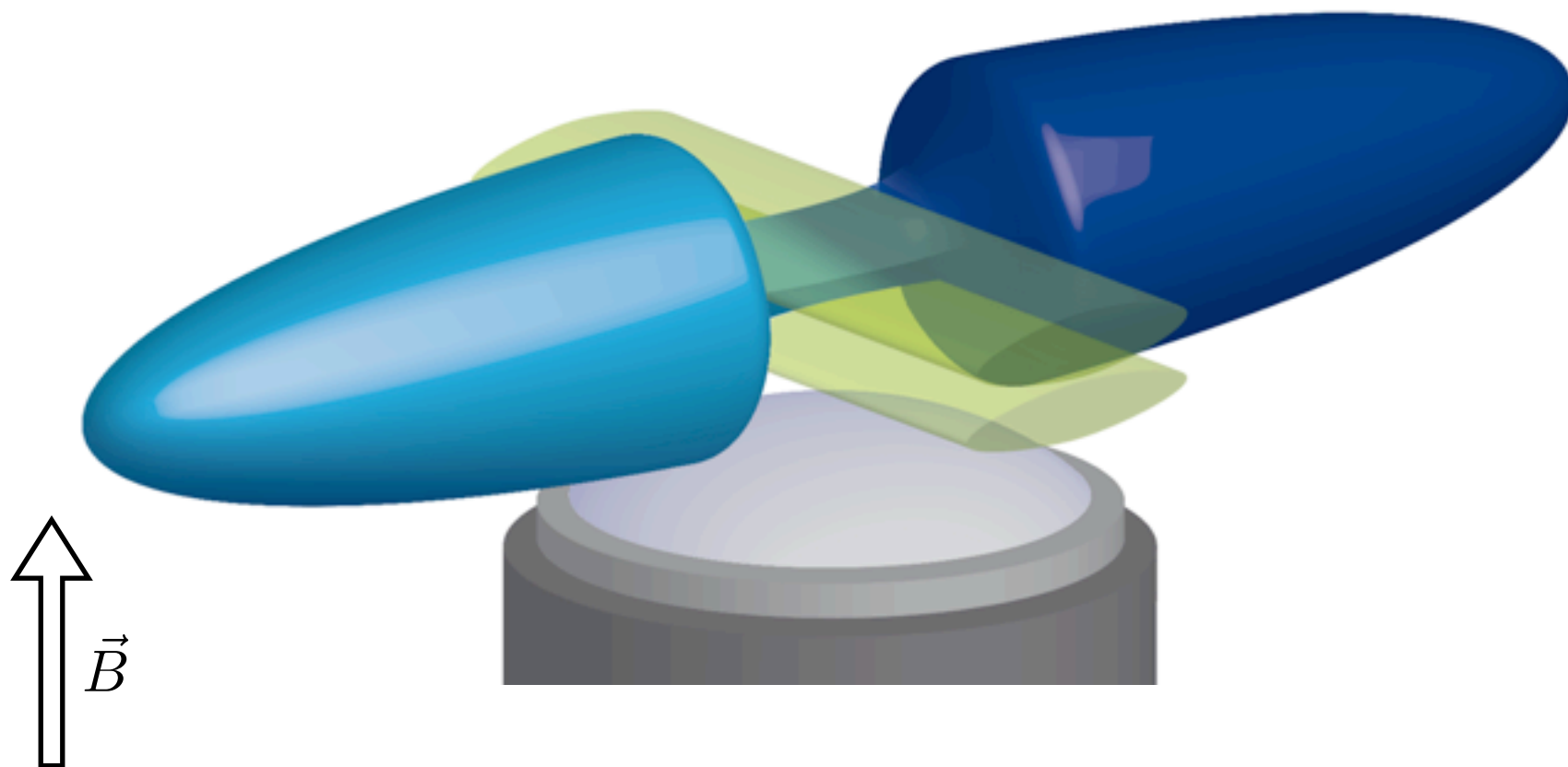


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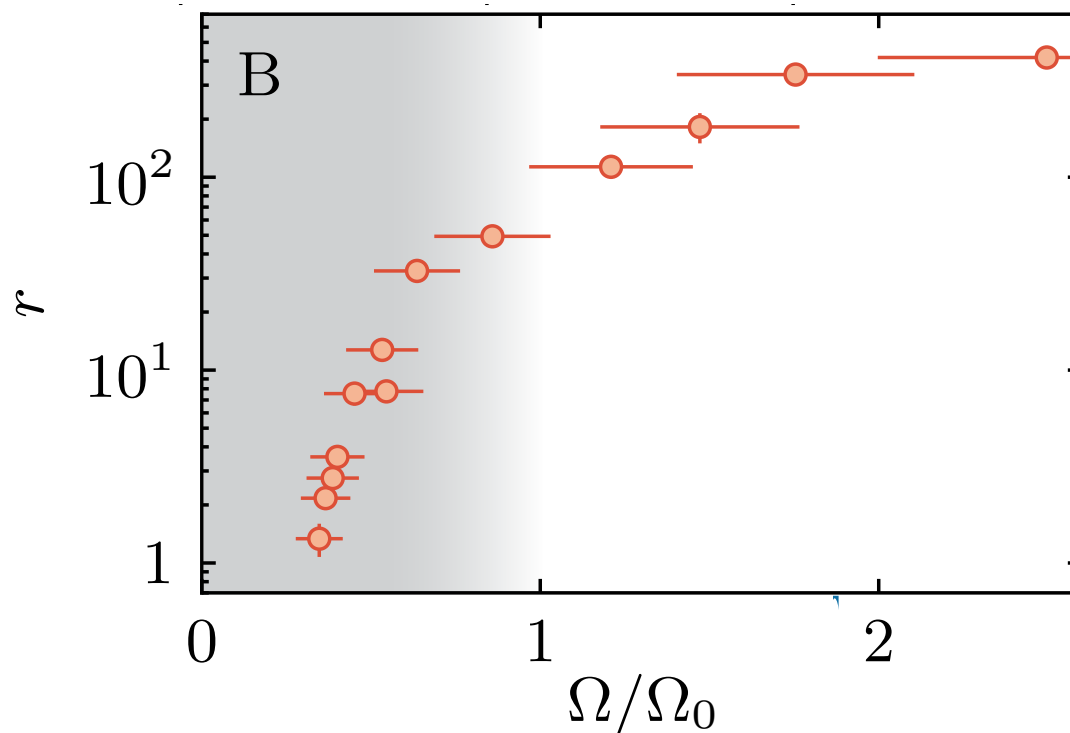


Strongly attractive Fermi gases : pairing and superfluidity

# Resistance of cold atom systems : interactions

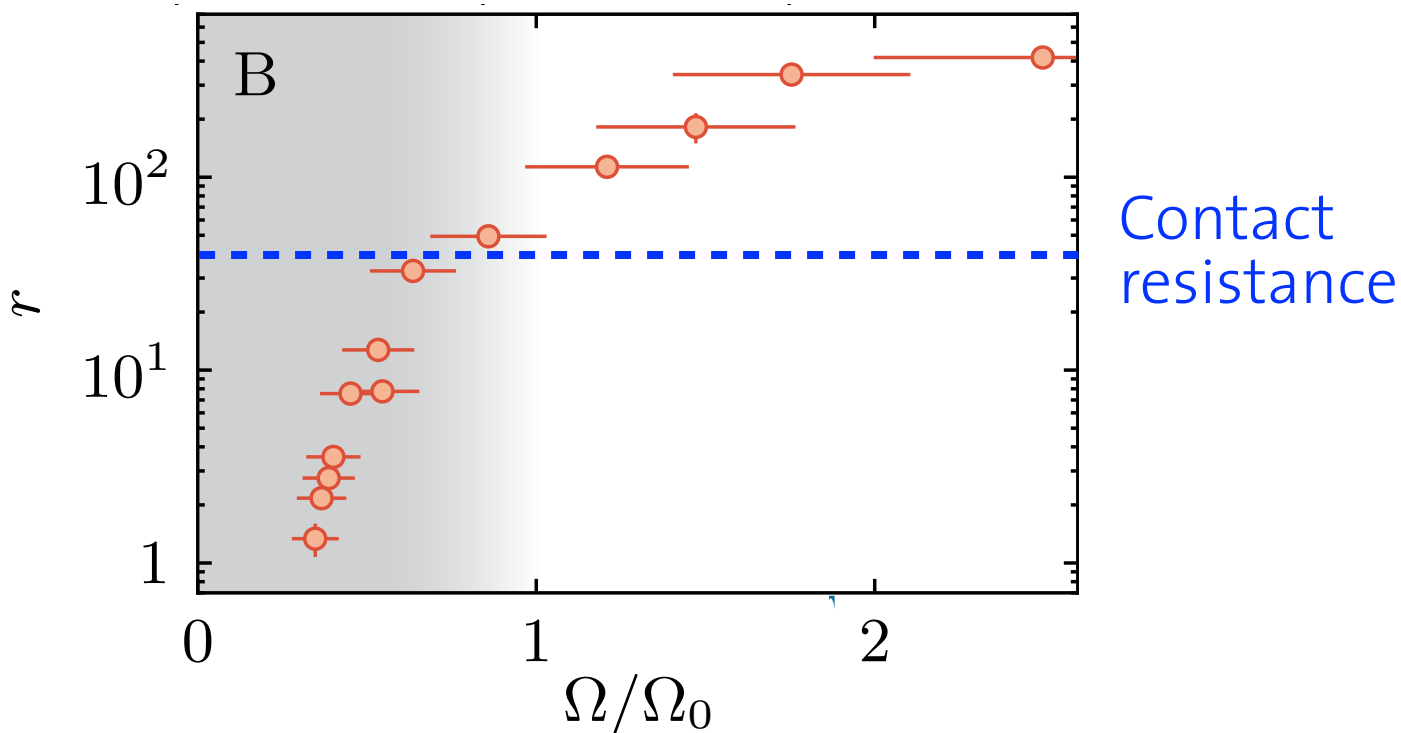


# Resistance of cold atom systems : interactions



Strongly attractive Fermi gases : pairing and superfluidity

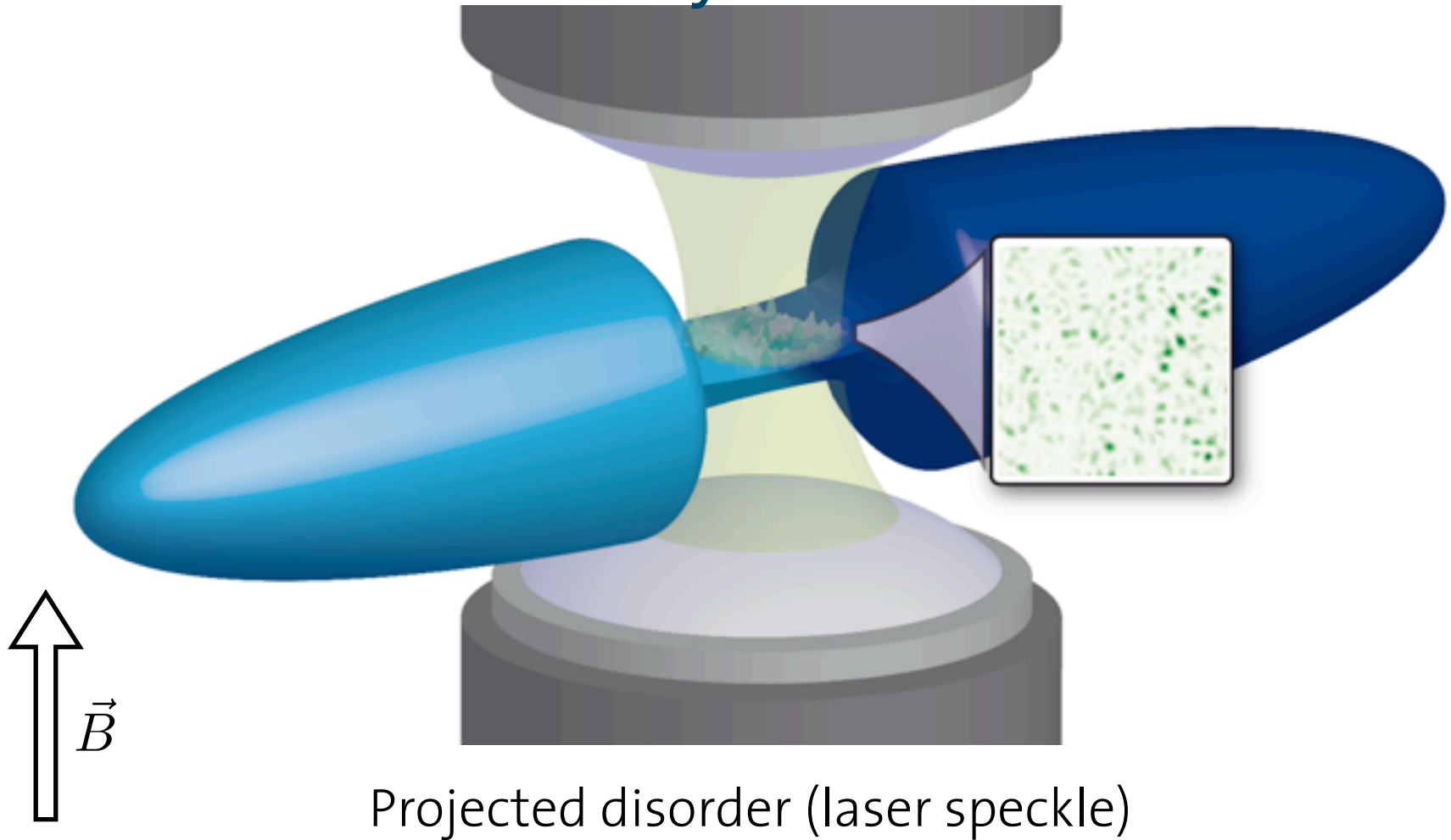
# Resistance of cold atom systems : interactions



Strongly attractive Fermi gases : pairing and superfluidity

# Resistance of cold atom systems : disorder

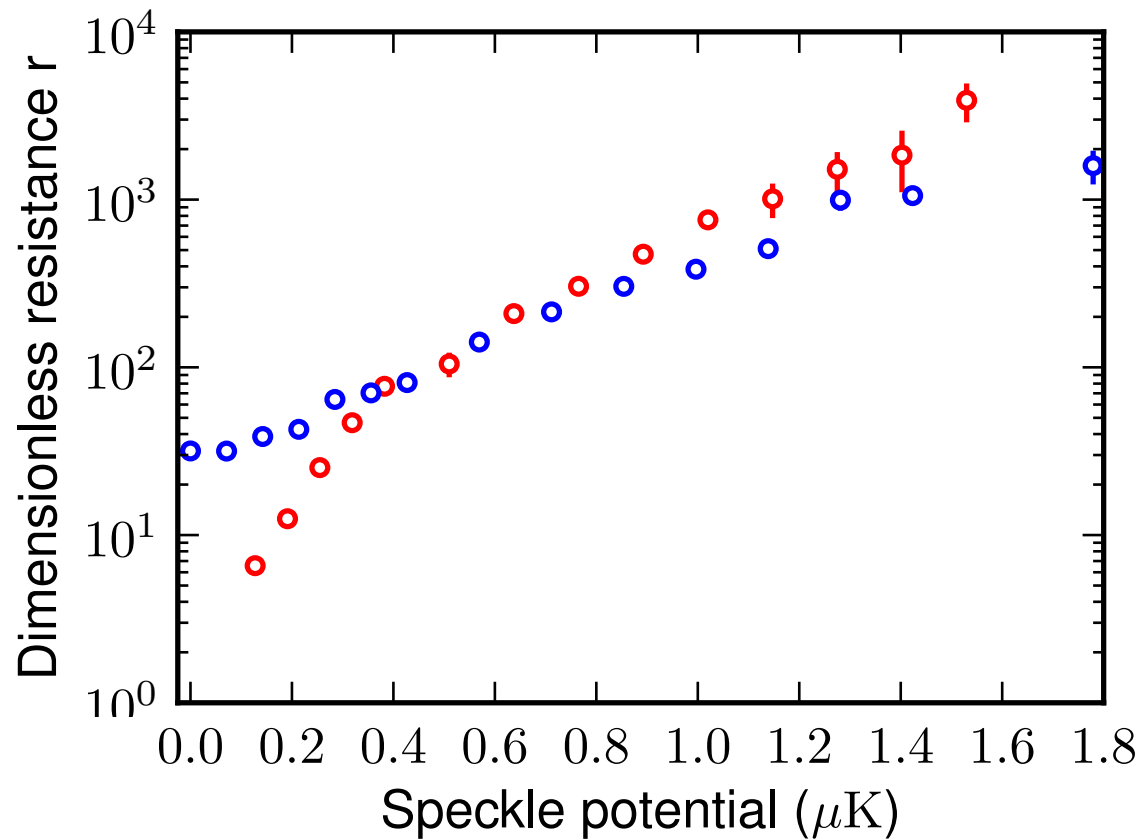
# Resistance of cold atom systems : disorder



Projected disorder (laser speckle)

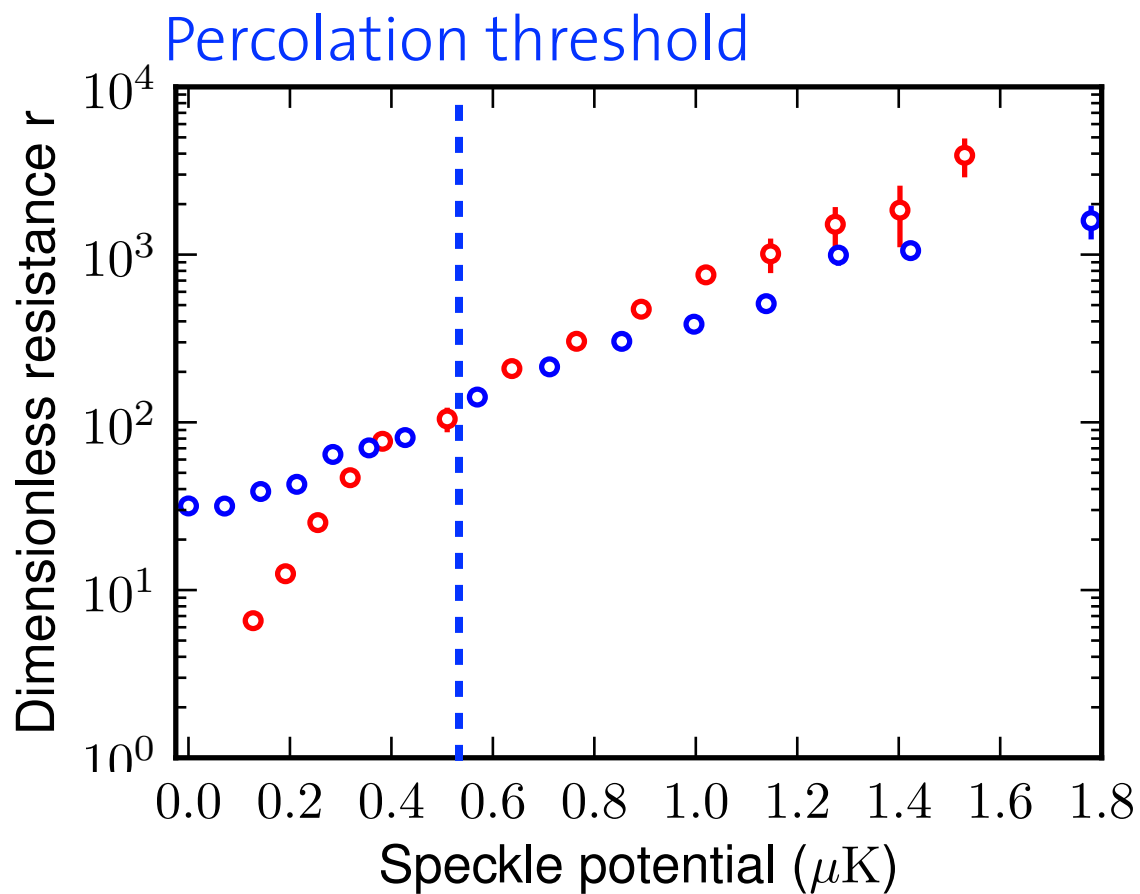
See also : M. Inguscio (Florence), B. DeMarco (Urbana), A. Aspect (Palaiseau), S. Rolston (NIST)

# Resistance of cold atom systems : disorder

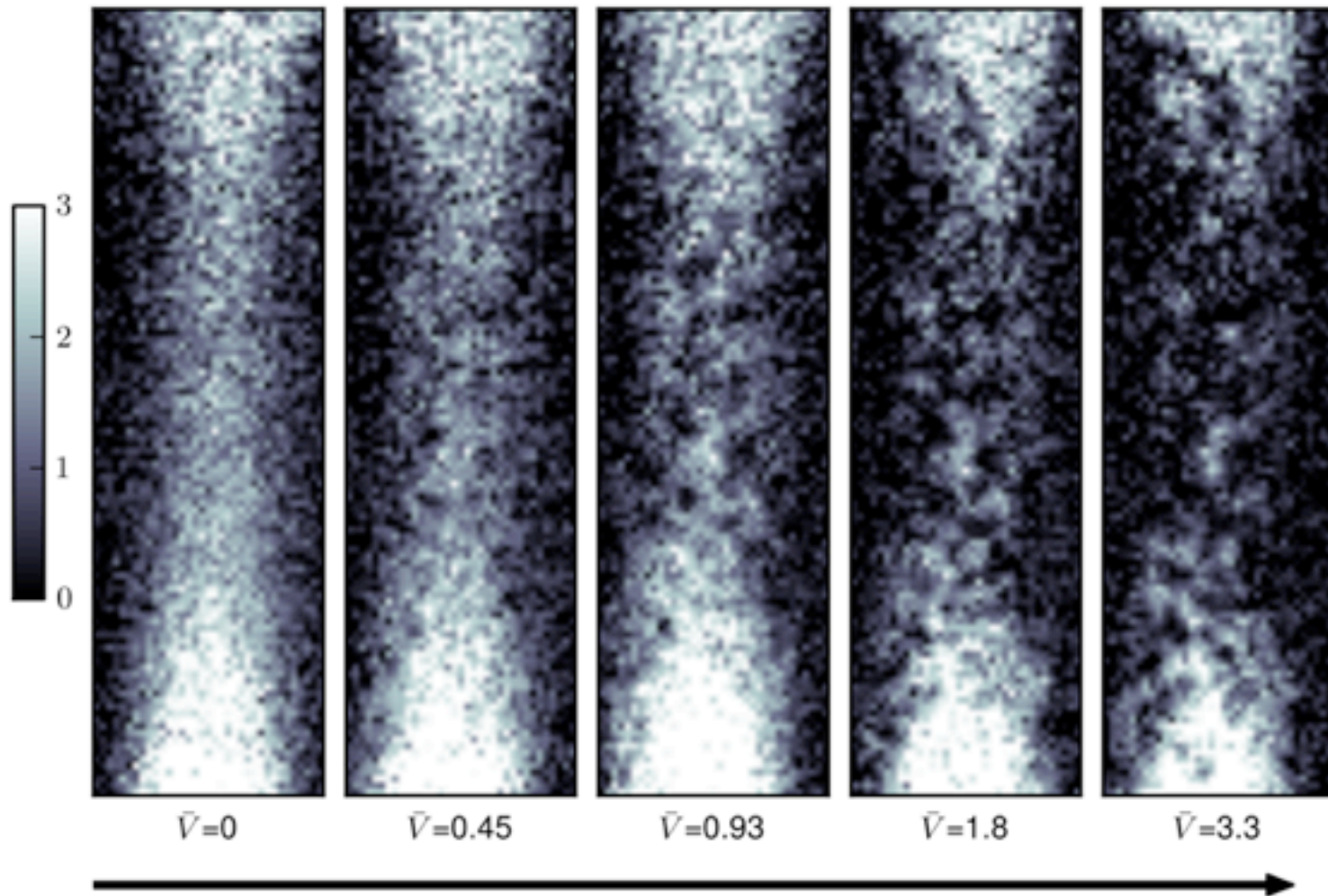




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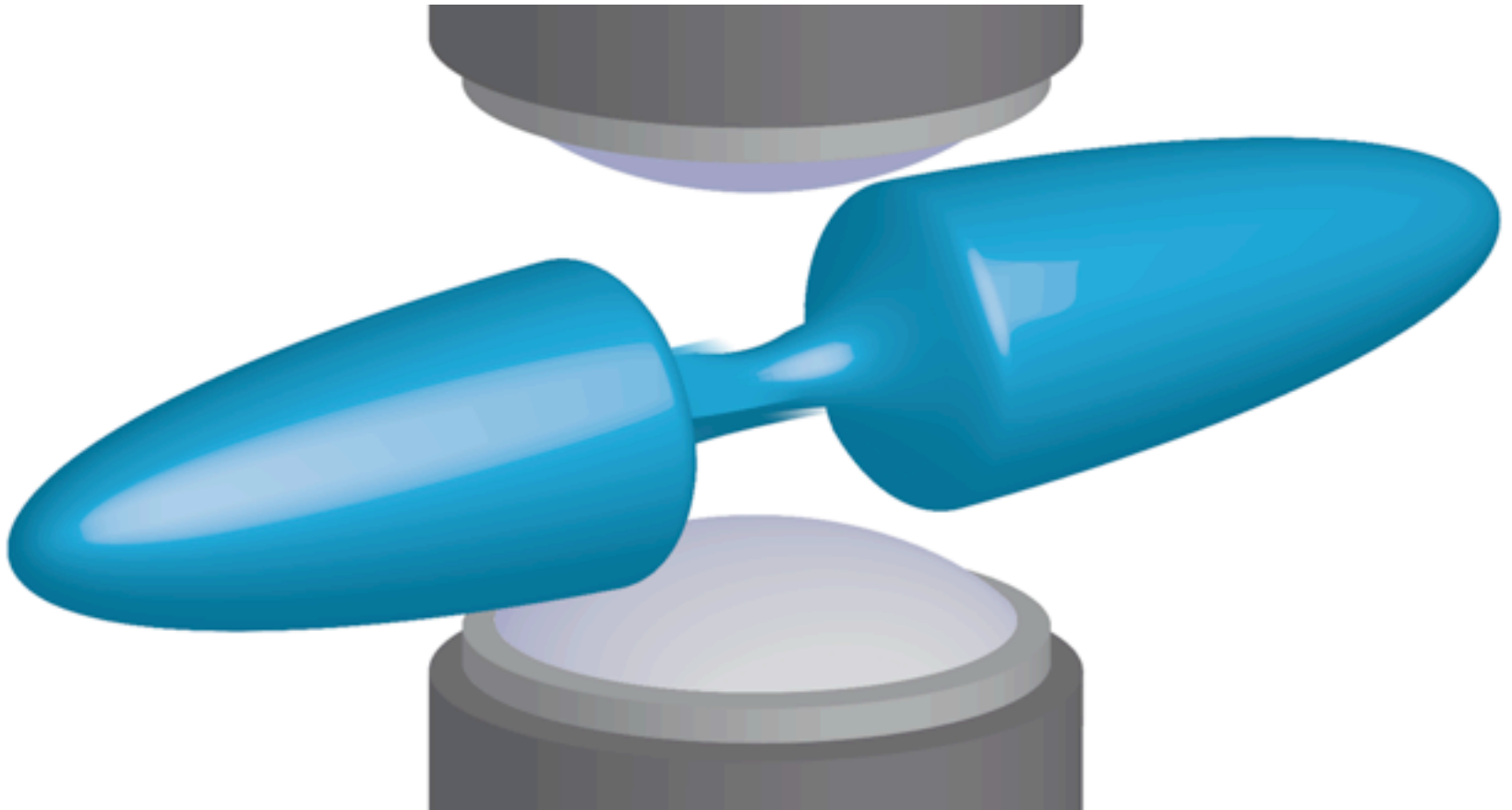
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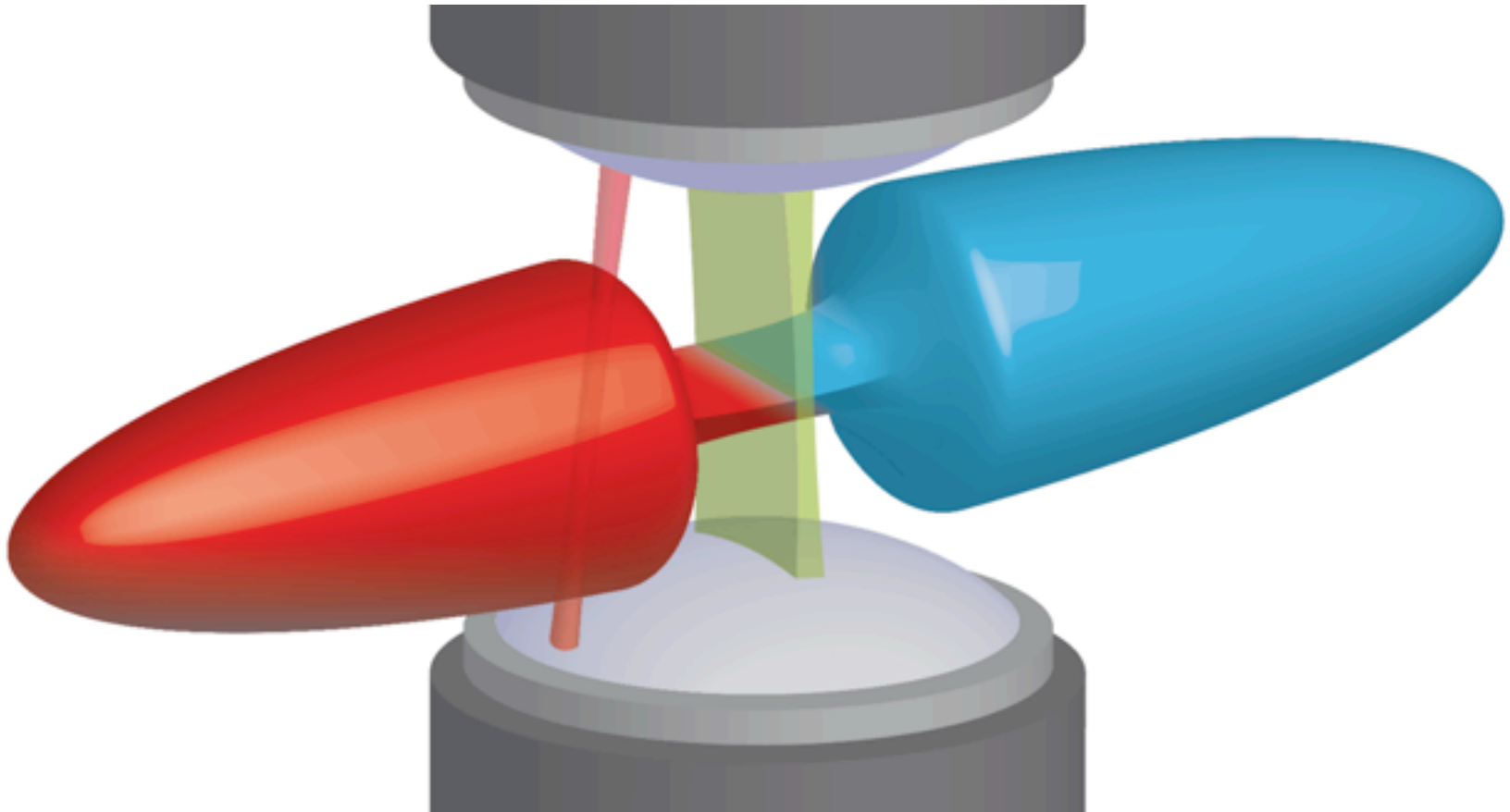


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  - Strongly attractive interactions: superfluids
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- Thermoelectric transport

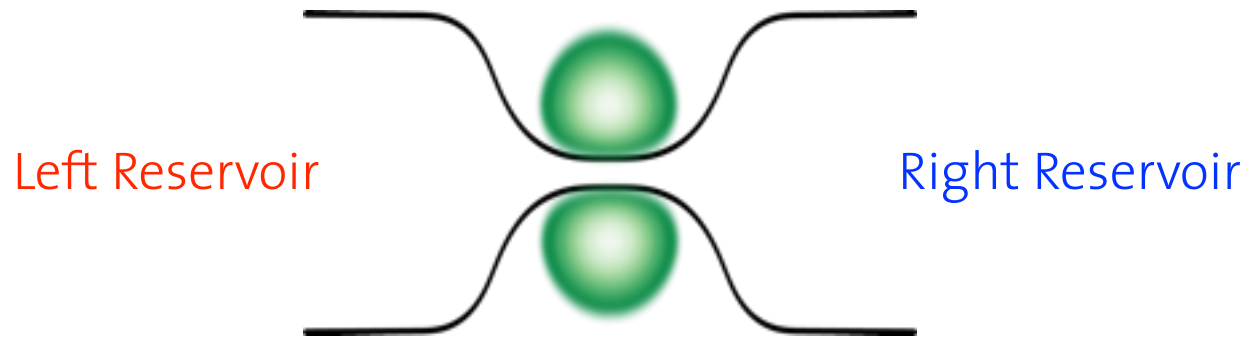
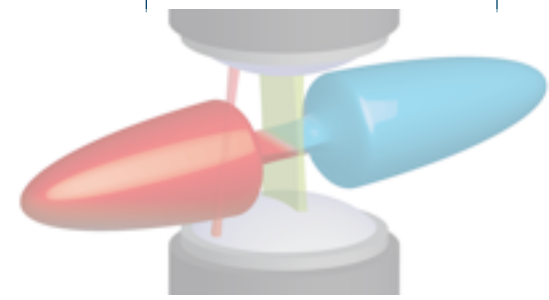
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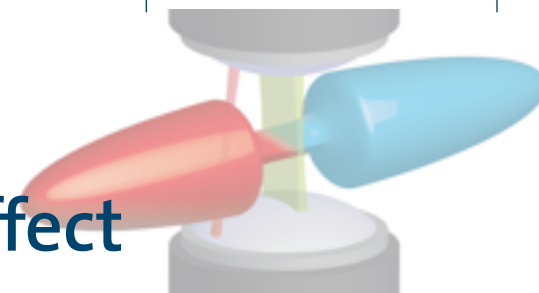




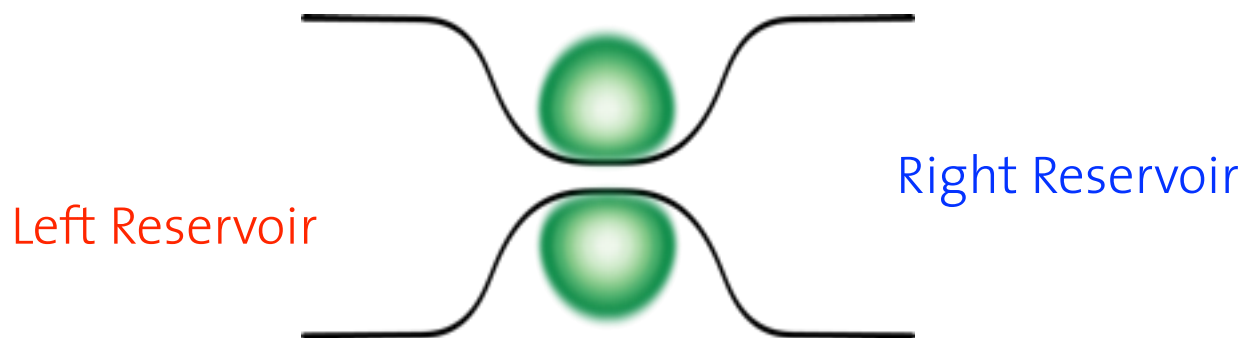
# Temperature bias



$$T_{\text{Left}} > T_{\text{Right}}$$



# Temperature bias : a thermodynamic effect

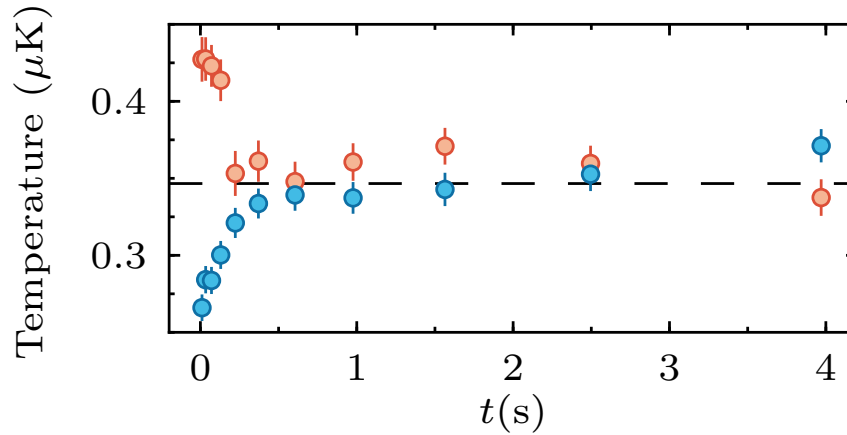
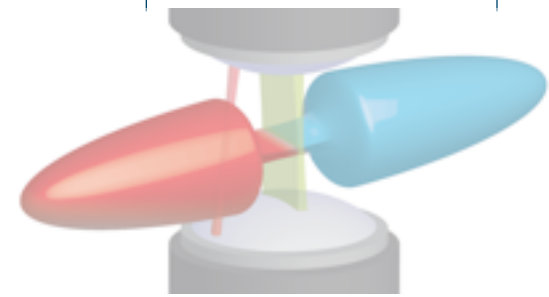


$$T_{\text{Left}} > T_{\text{Right}}$$

$$\mu_{\text{Left}} < \mu_{\text{Right}}$$

negative potential bias

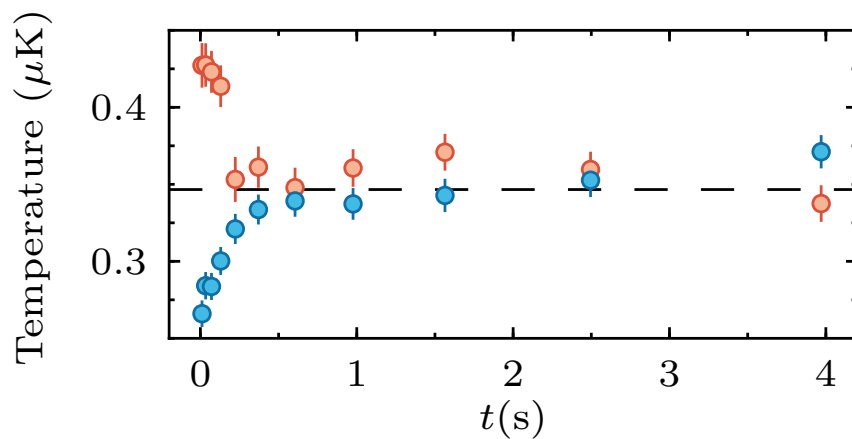
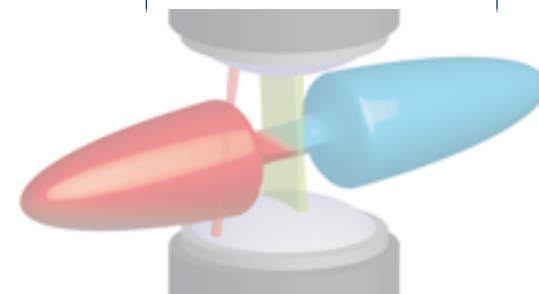
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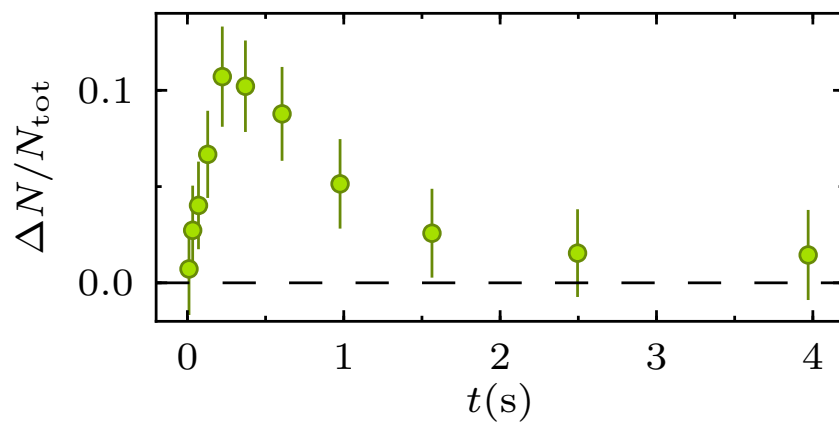
Entropy flow from  
hot to cold



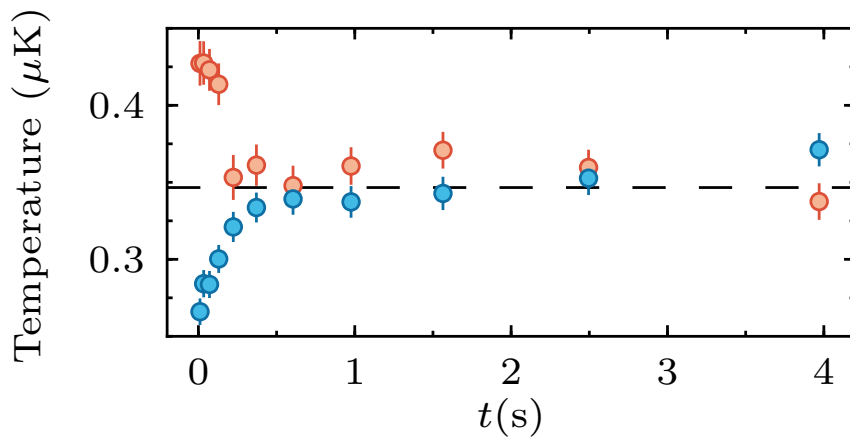
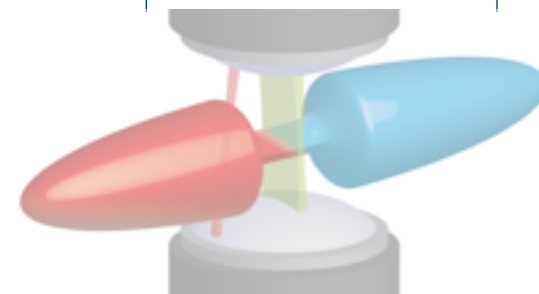
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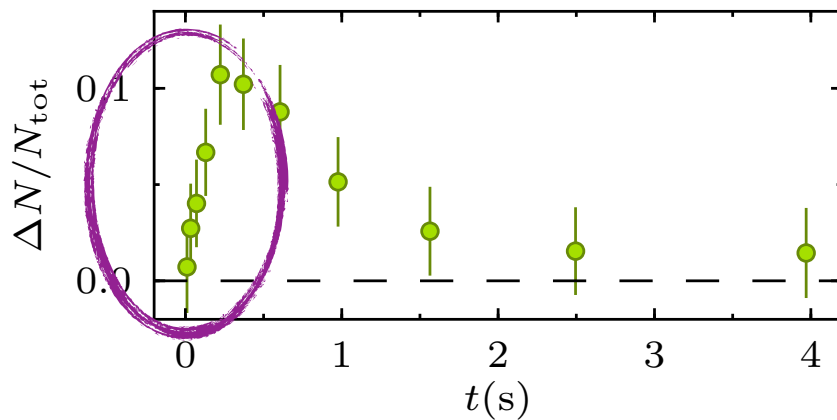
Entropy flow from hot to cold



# Temperature bias

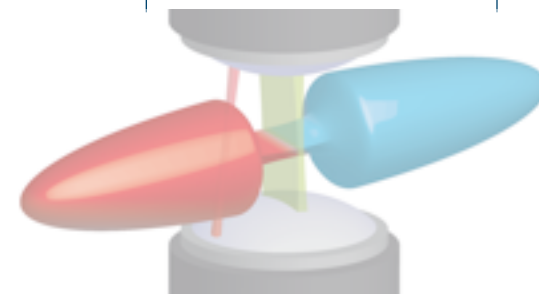


Entropy flow from hot to cold

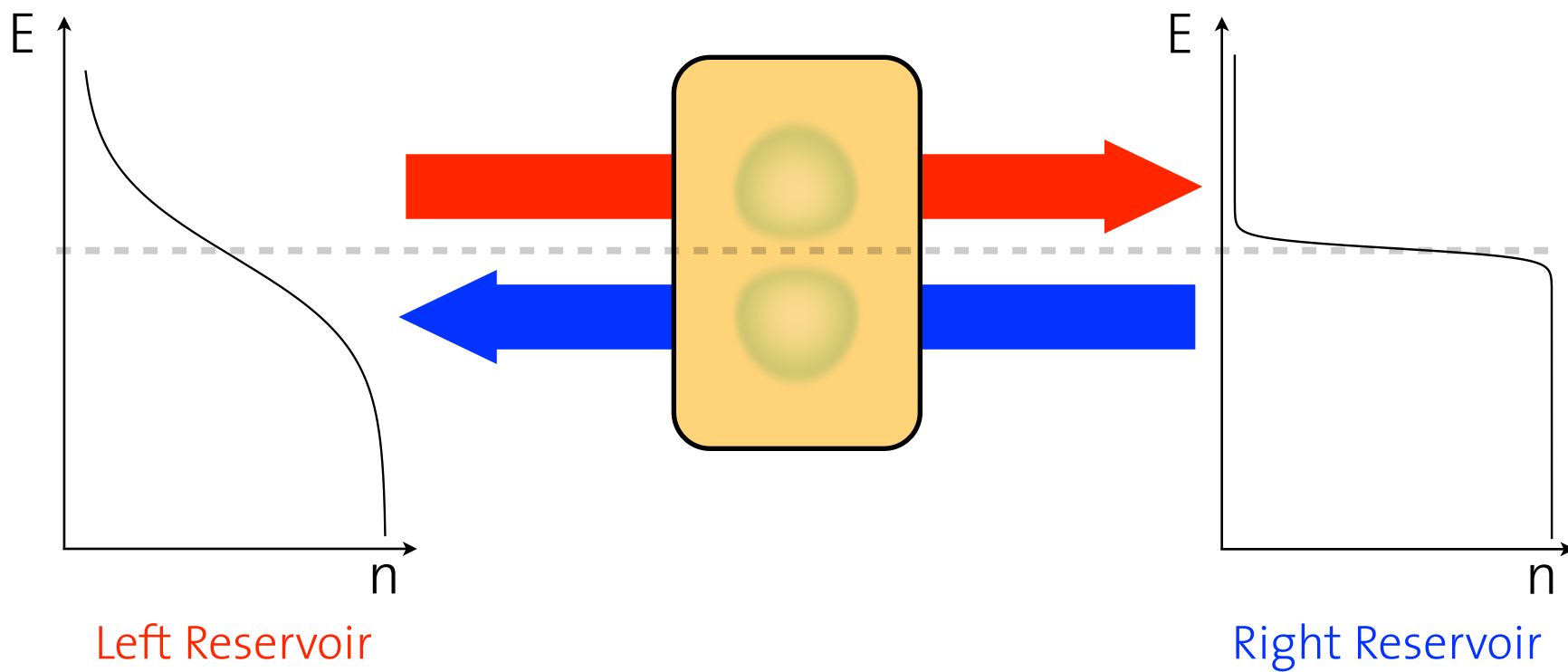


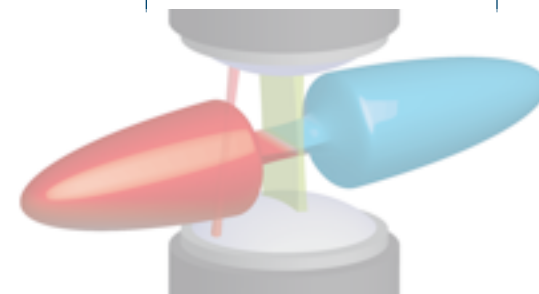
Particle flow from hot to cold

...flows against the potential bias...

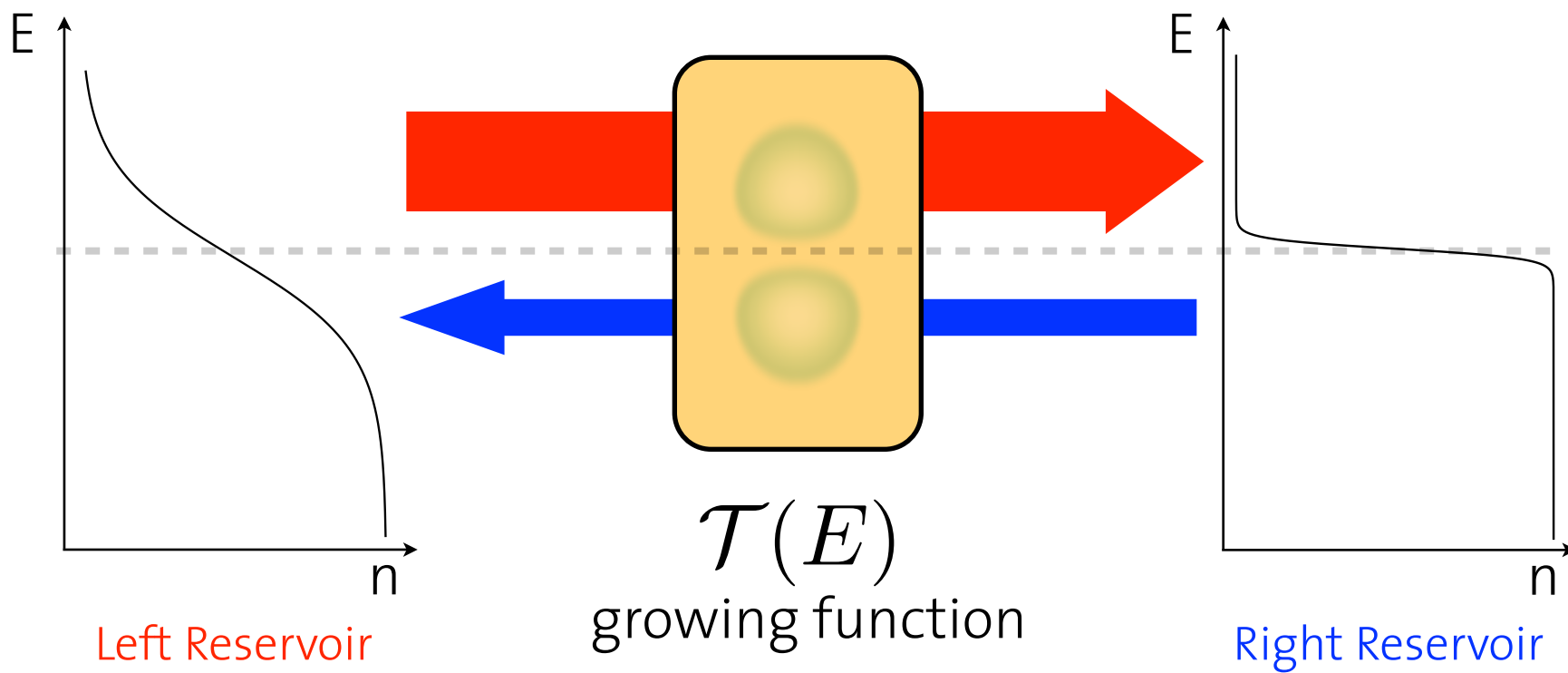


# Intrinsic thermoelectric effect

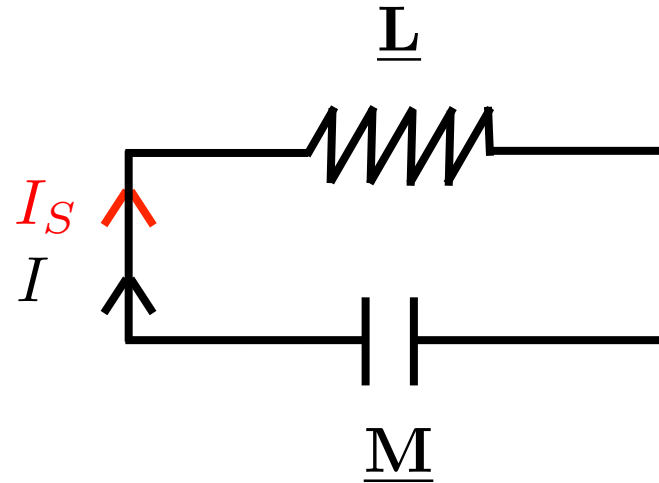


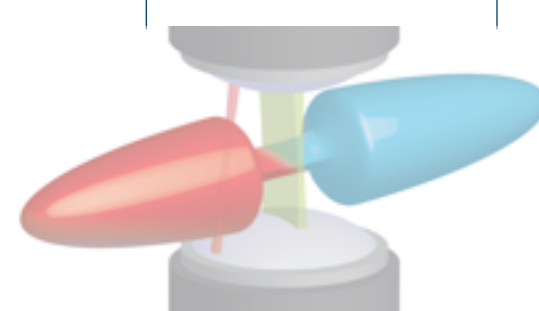


# Intrinsic thermoelectric effect

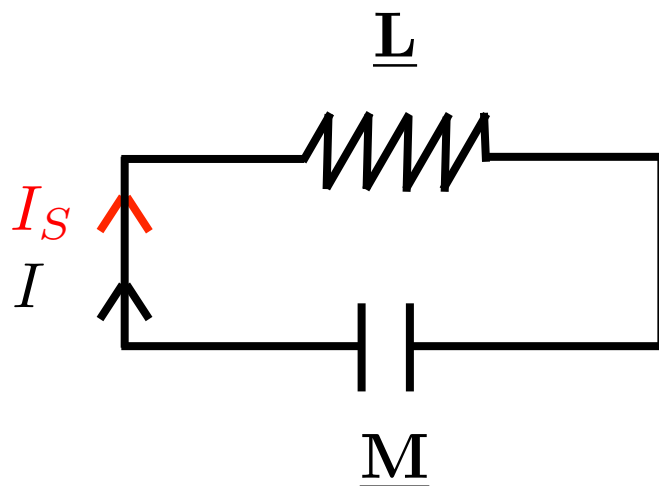


# Thermoelectric capacitor description





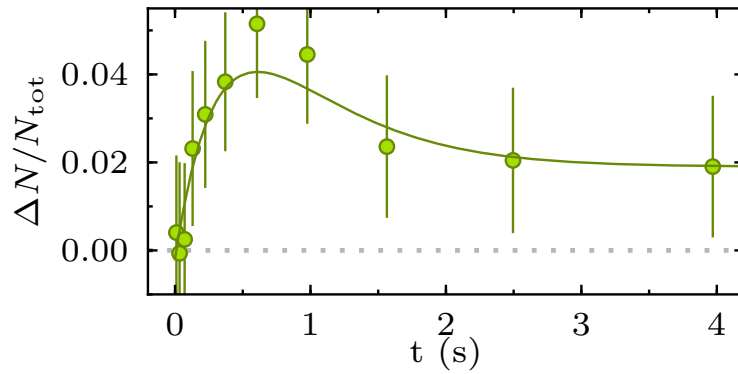
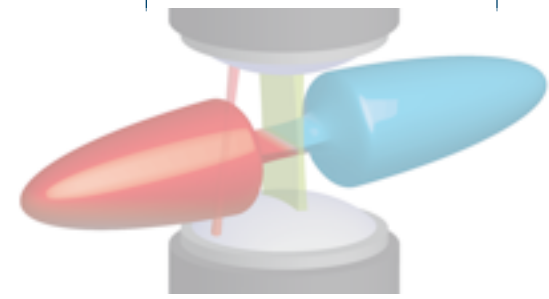
# Thermoelectric capacitor description



$$\tau_0 \frac{d}{dt} \begin{pmatrix} \Delta N \\ \Delta T \end{pmatrix} = -\underline{\Lambda} \begin{pmatrix} \Delta N \\ \Delta T \end{pmatrix}$$

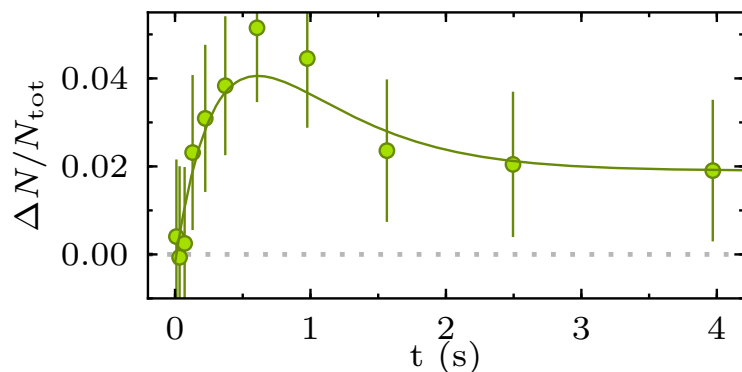
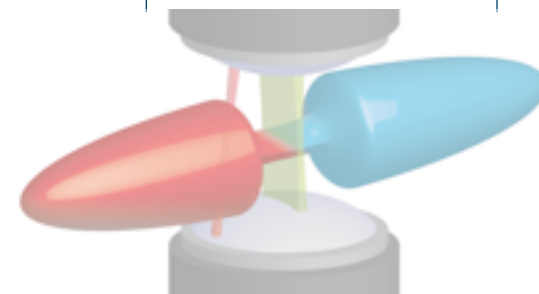
Provides a fitting procedure to extract resistance and thermopower

# Ballistic channels



Trap frequency in the channel : 9.3 kHz

# Ballistic channels

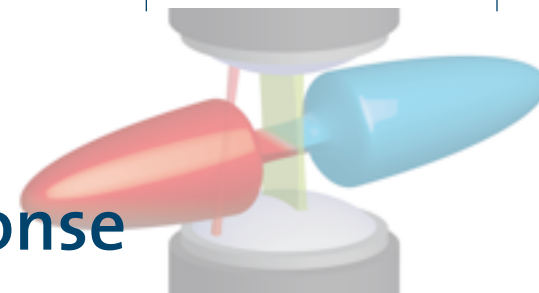


Trap frequency in the channel : 9.3 kHz

Trapped ideal Fermi gas  
+  
Landauer-Büttiker formula

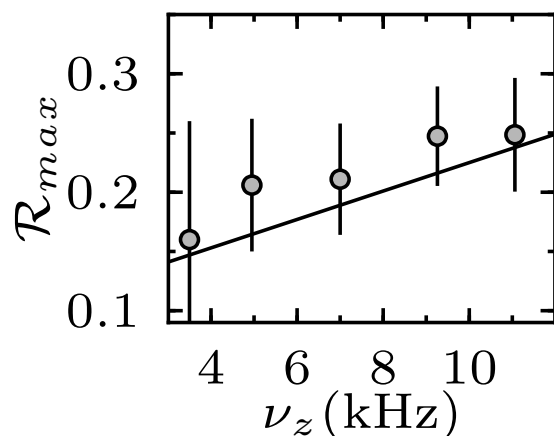
*No adjustable parameter*





# Ballistic channels : thermoelectric response

Normalized atom number difference as a response to the temperature bias



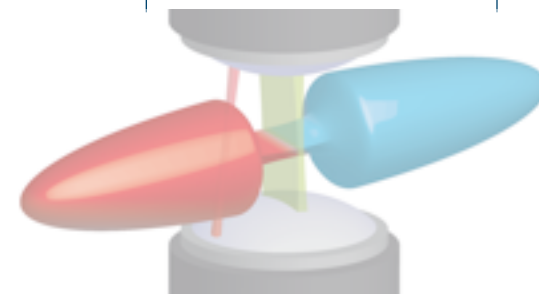
$$\mathcal{R} = \frac{(\Delta N/N_{\text{tot}})}{(\Delta T_0/T_F)}$$

Increasing confinement:

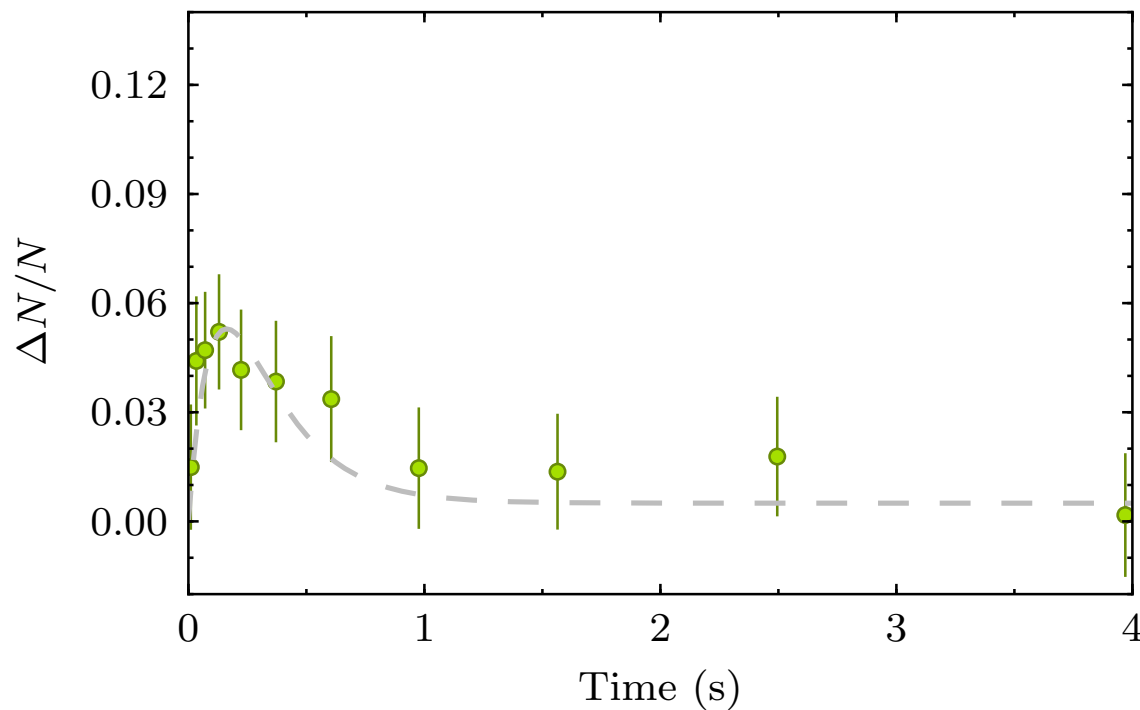
- decreases the conductance
- increases the thermoelectric response

# Ballistic to diffusive crossover

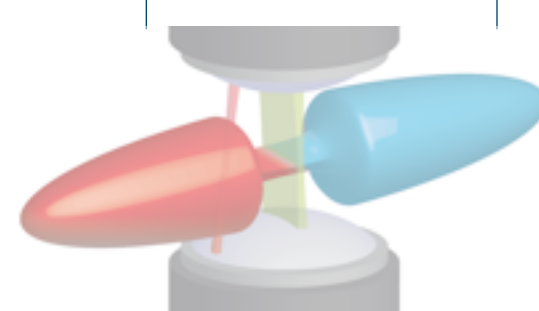




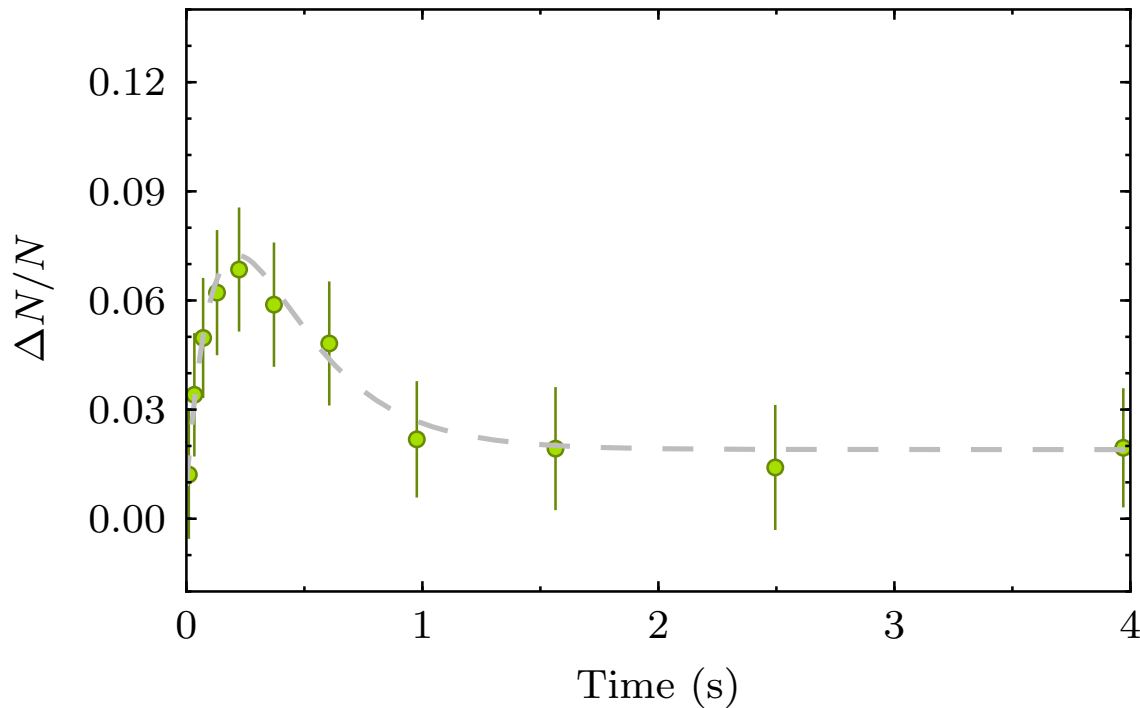
# Ballistic to diffusive crossover



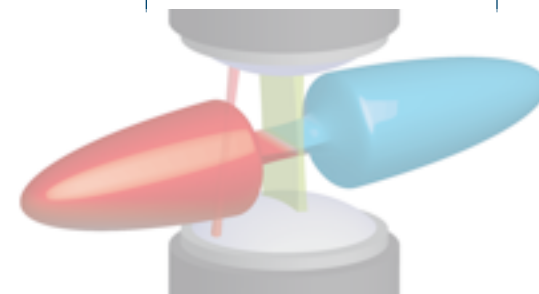
Disorder strength =  $0.13 \mu\text{K}$



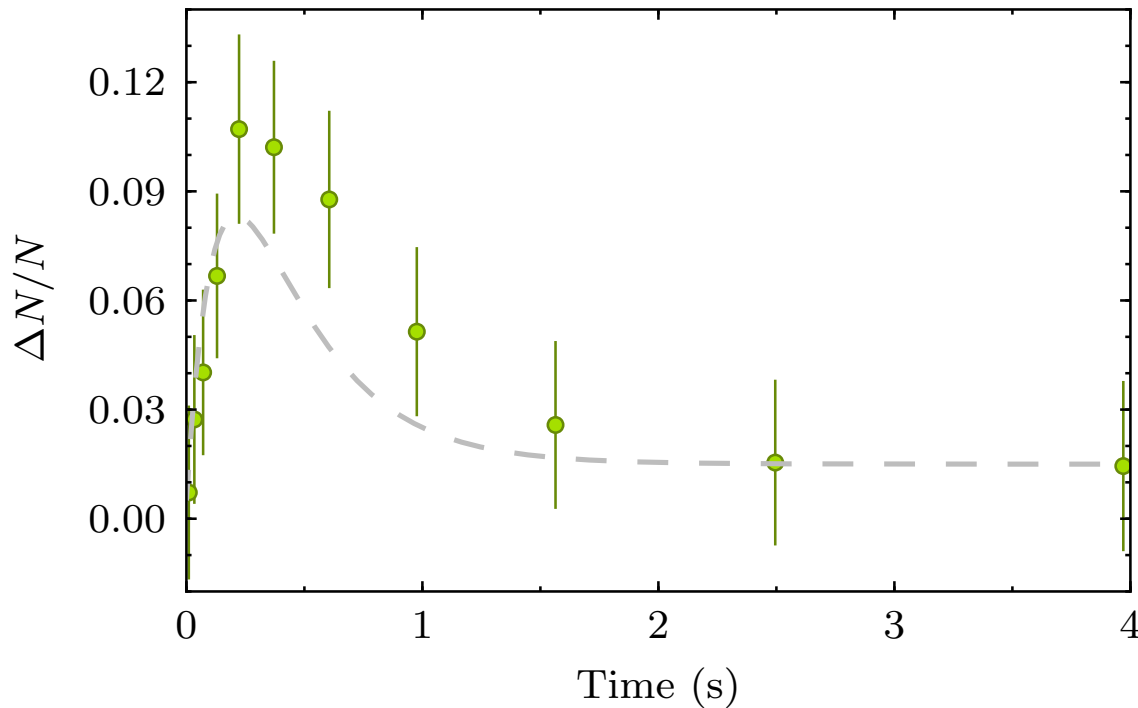
# Ballistic to diffusive crossover



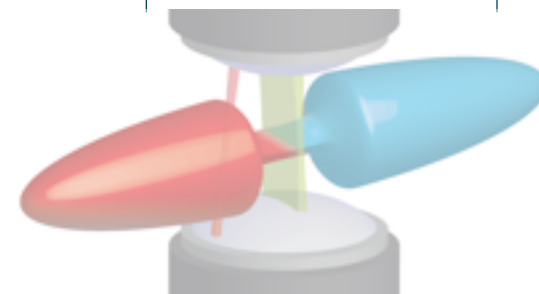
Disorder strength =  $0.26 \mu\text{K}$



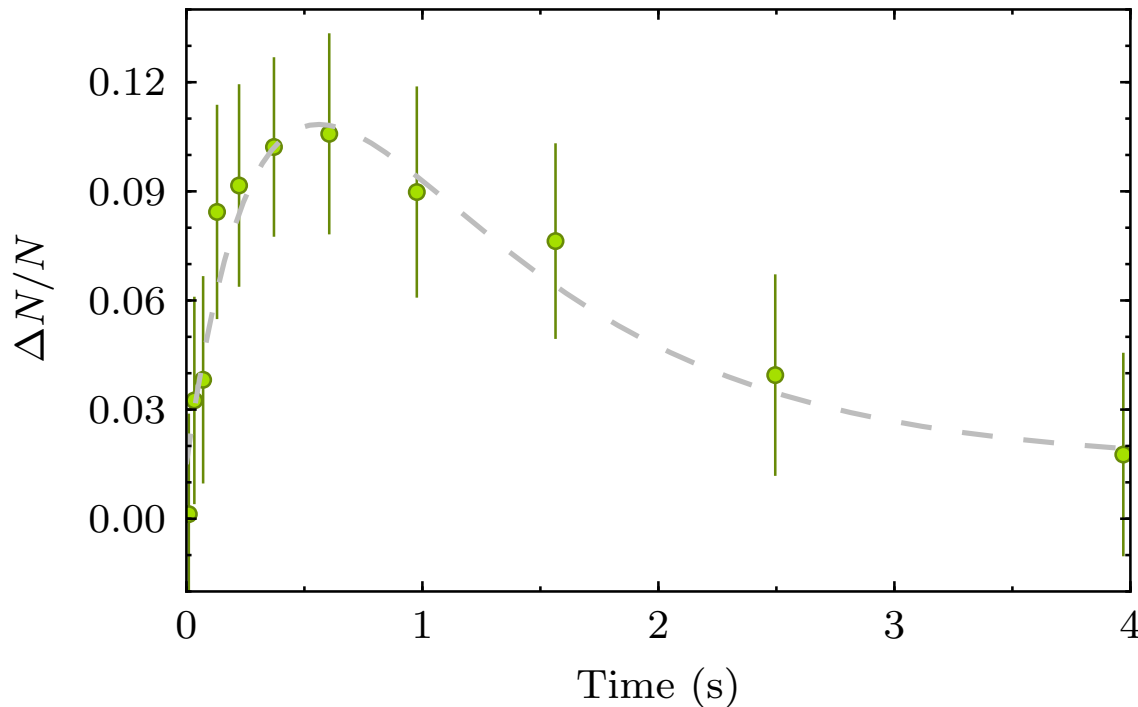
# Ballistic to diffusive crossover



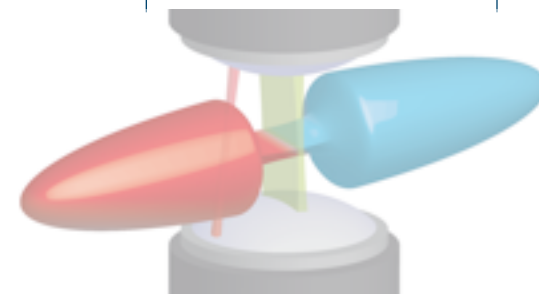
Disorder strength =  $0.54 \mu\text{K}$



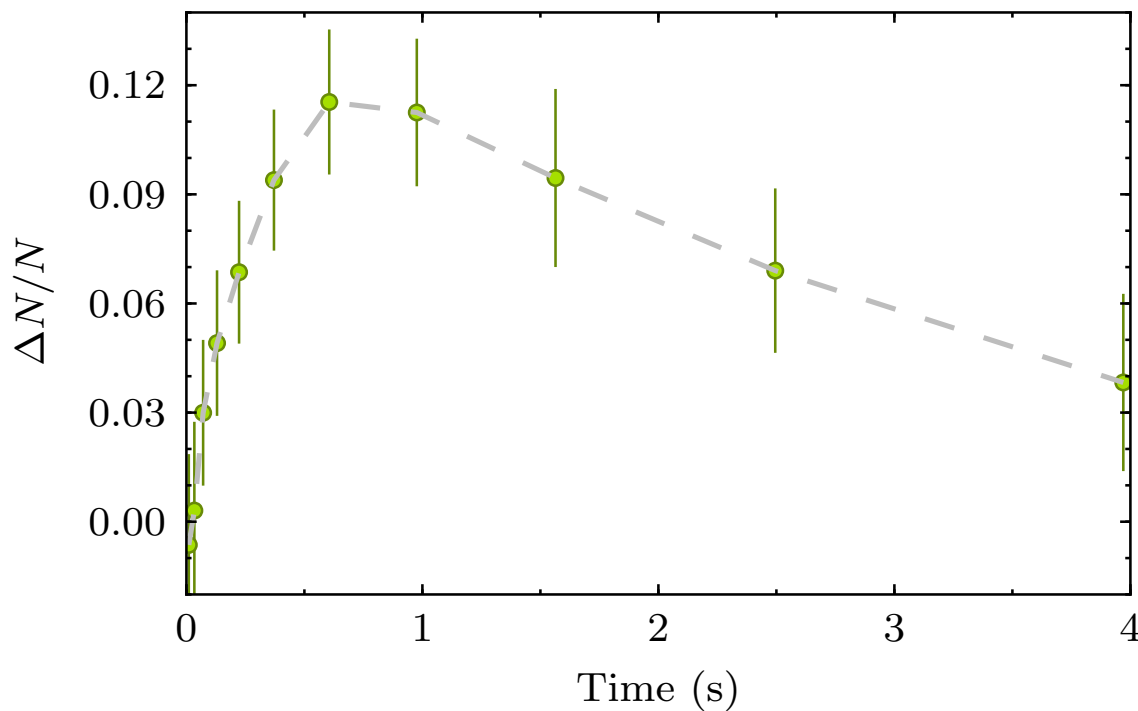
# Ballistic to diffusive crossover



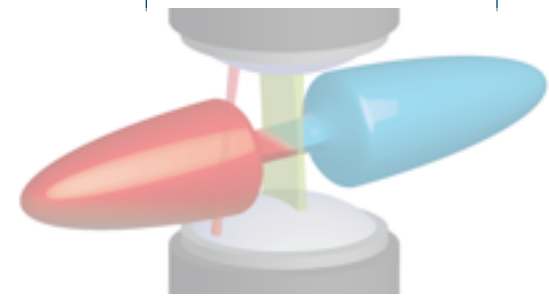
Disorder strength =  $0.81 \mu\text{K}$



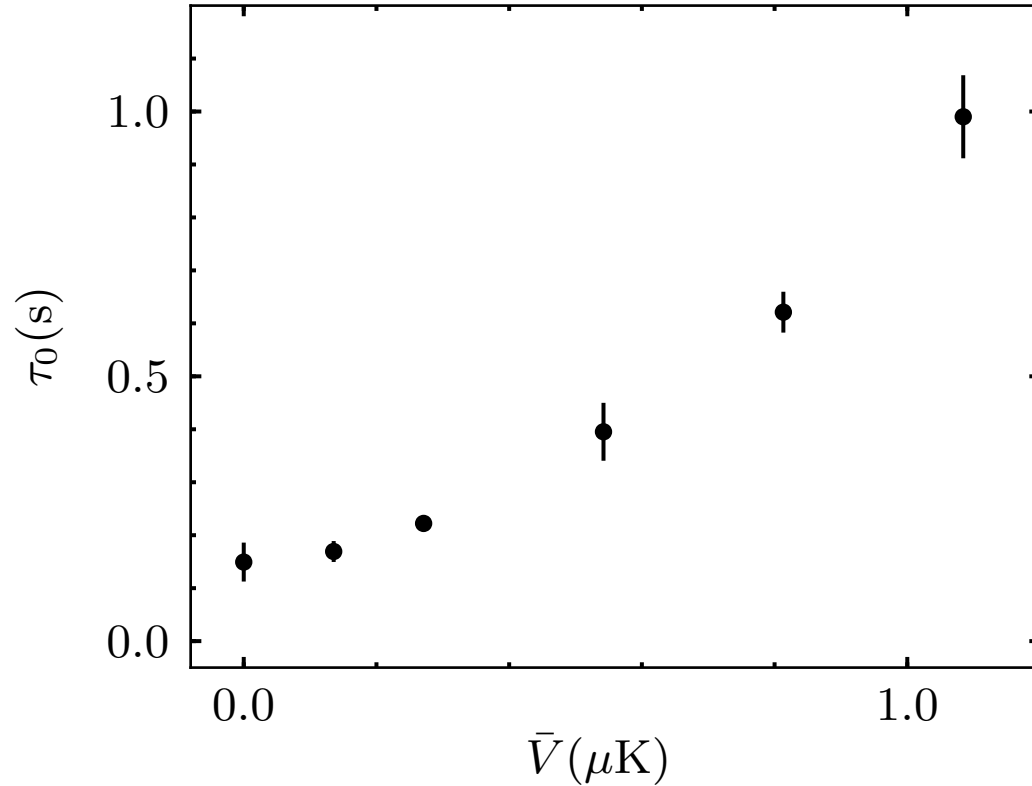
# Ballistic to diffusive crossover



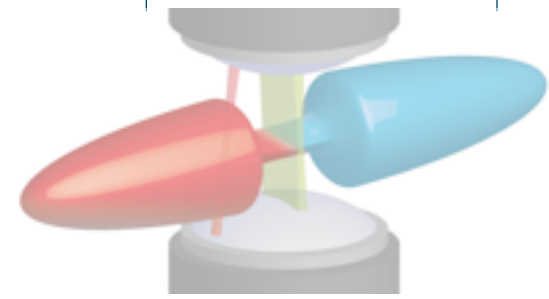
Disorder strength =  $1.08 \mu\text{K}$



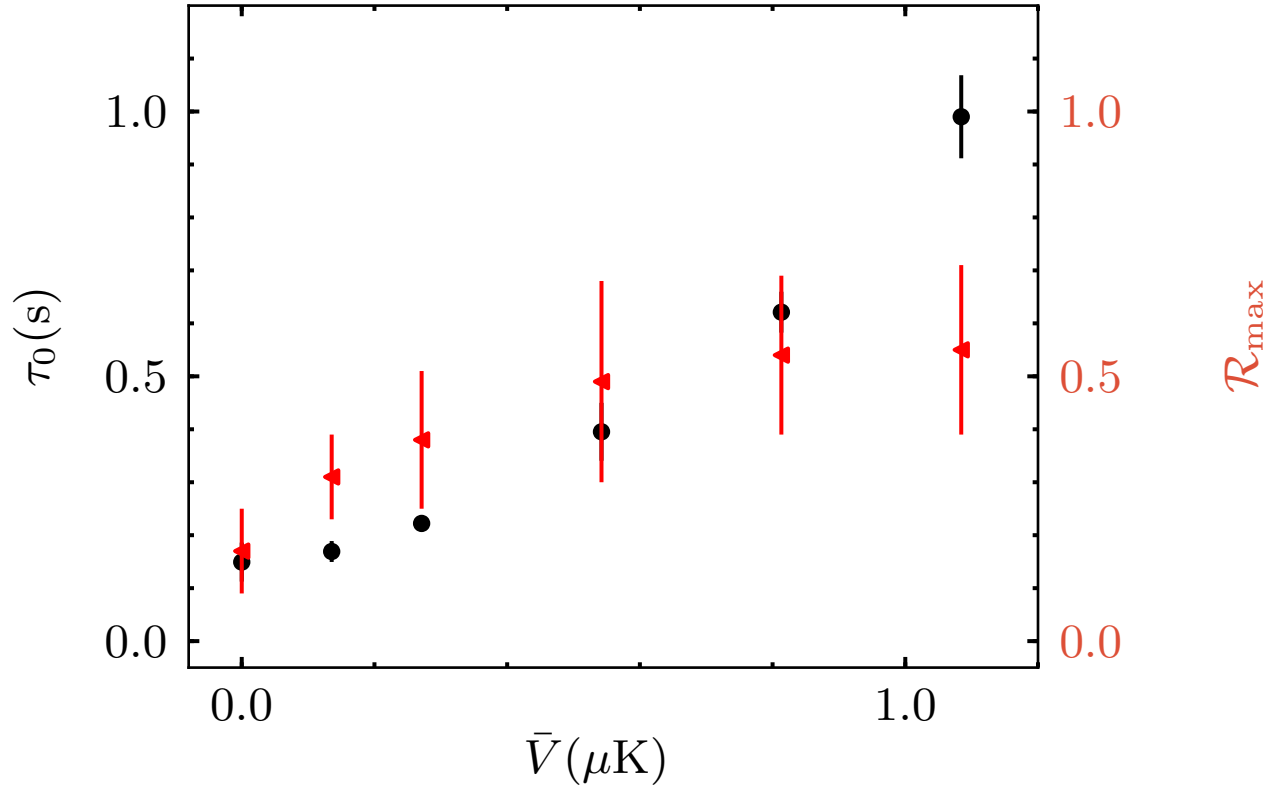
# Ballistic to diffusive crossover



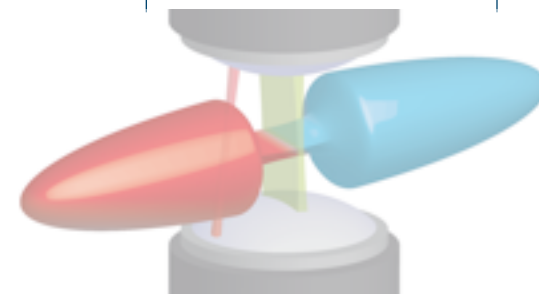




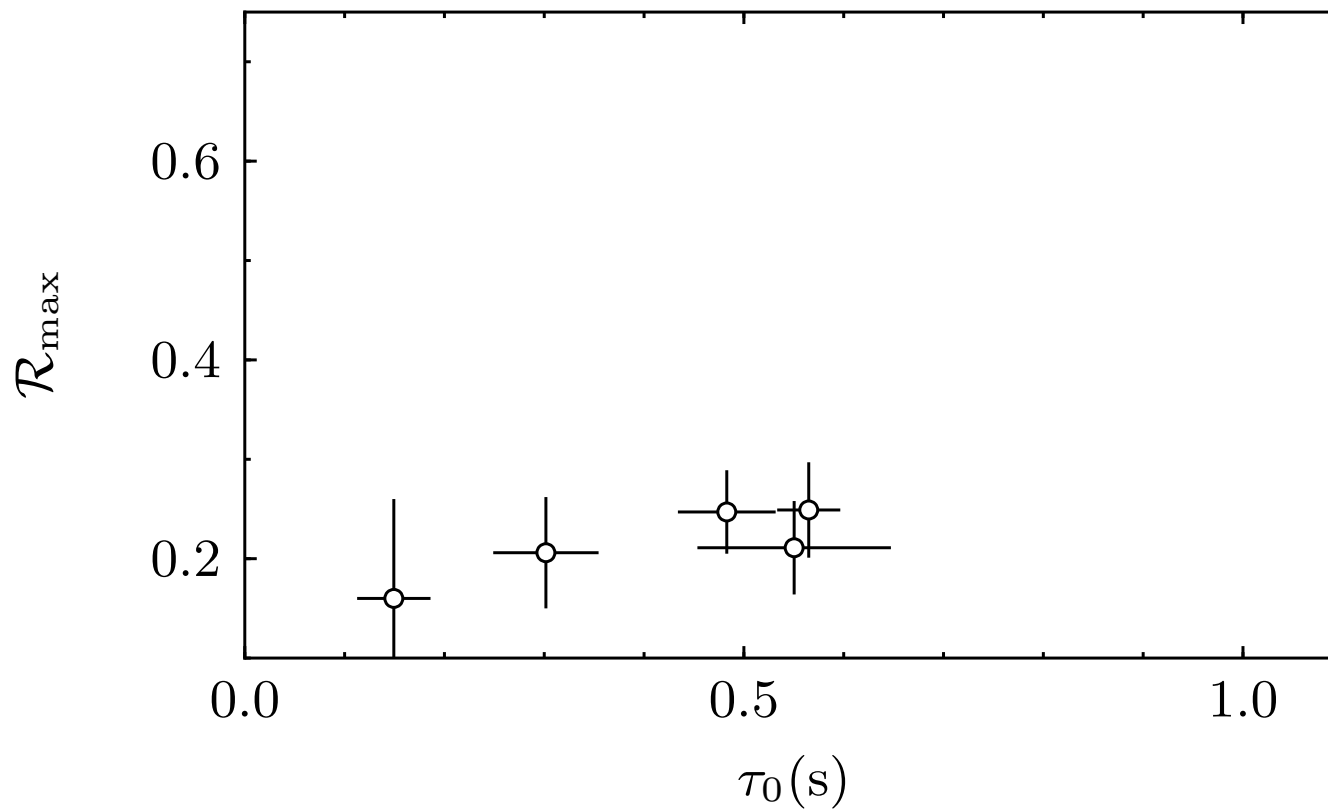
# Ballistic to diffusive crossover

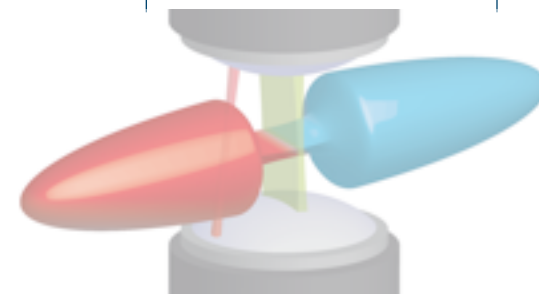


Increase thermoelectric response at the expense of a decrease of conductance

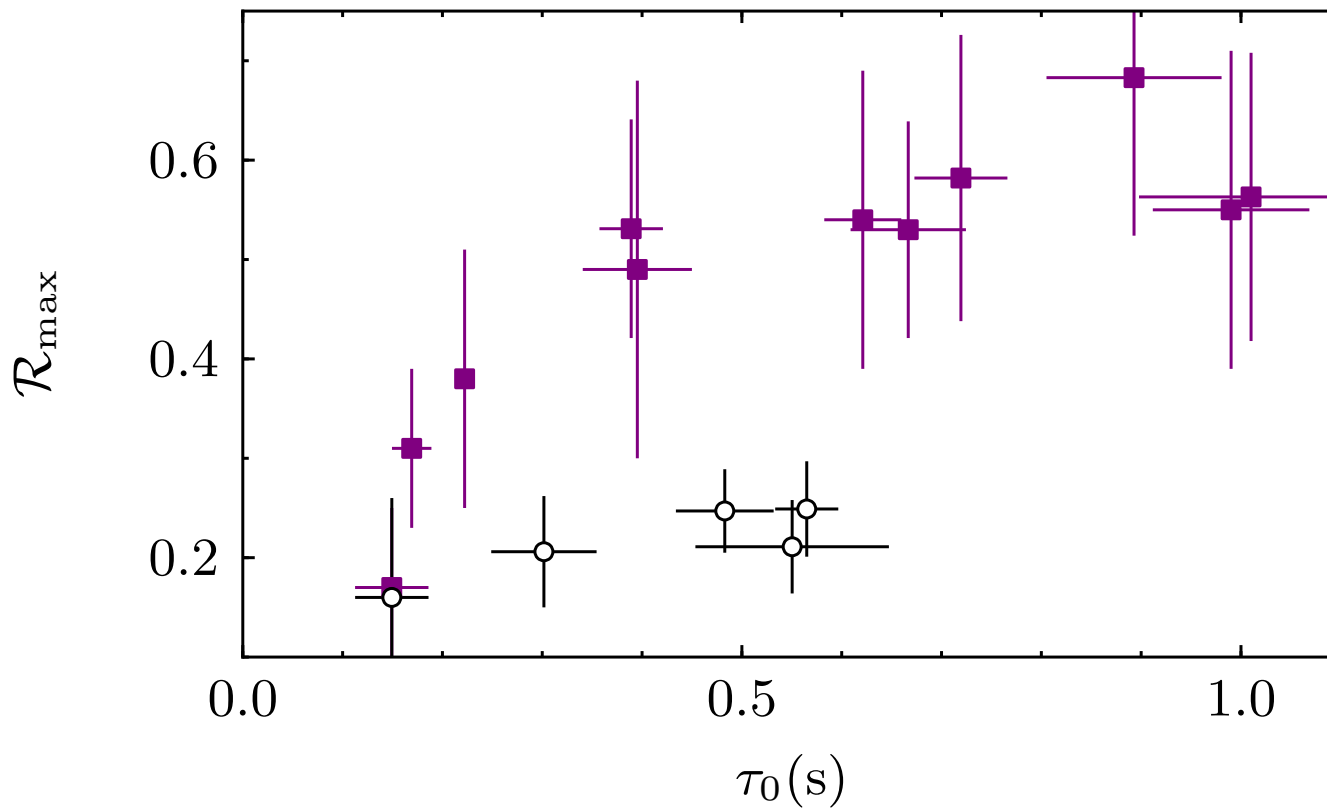


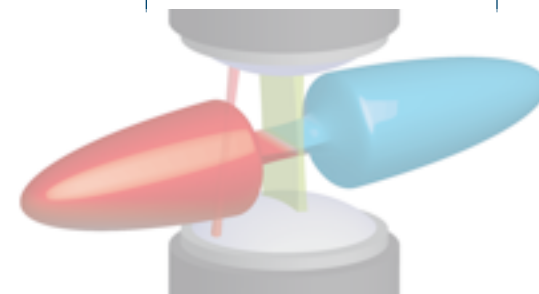
# Thermopower / Resistance tradeoff



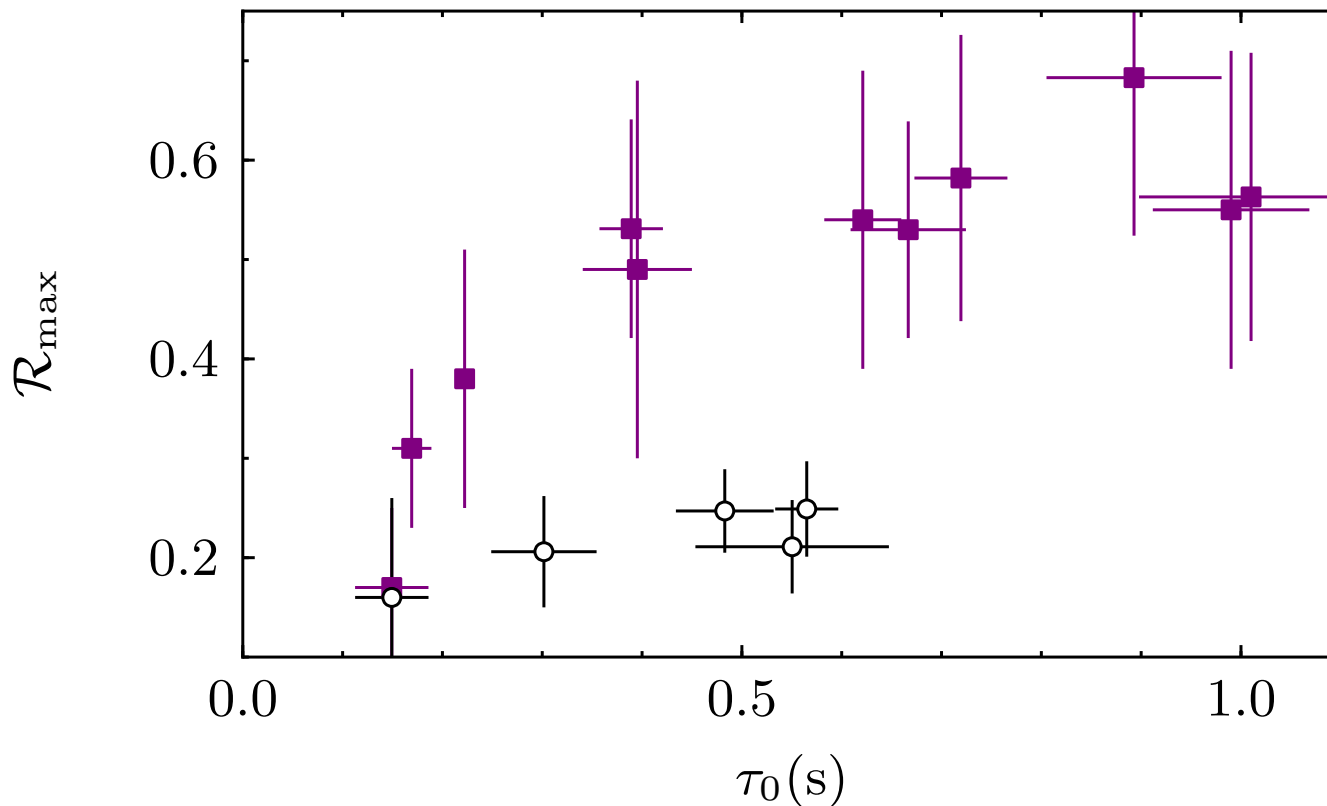


# Thermopower / Resistance tradeoff



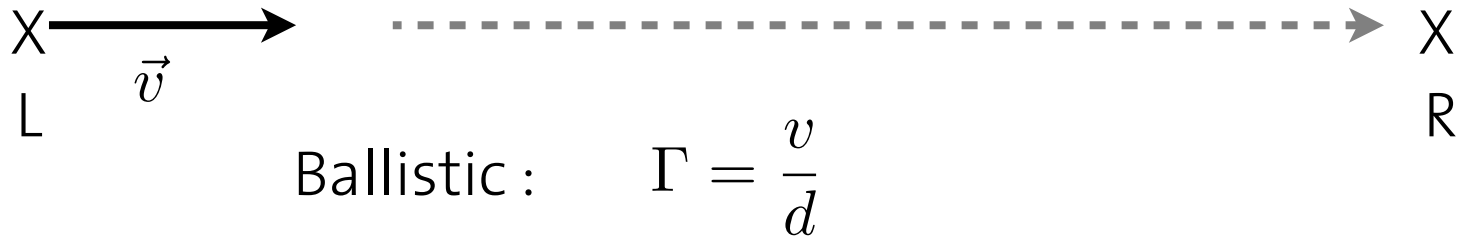


# Thermopower / Resistance tradeoff

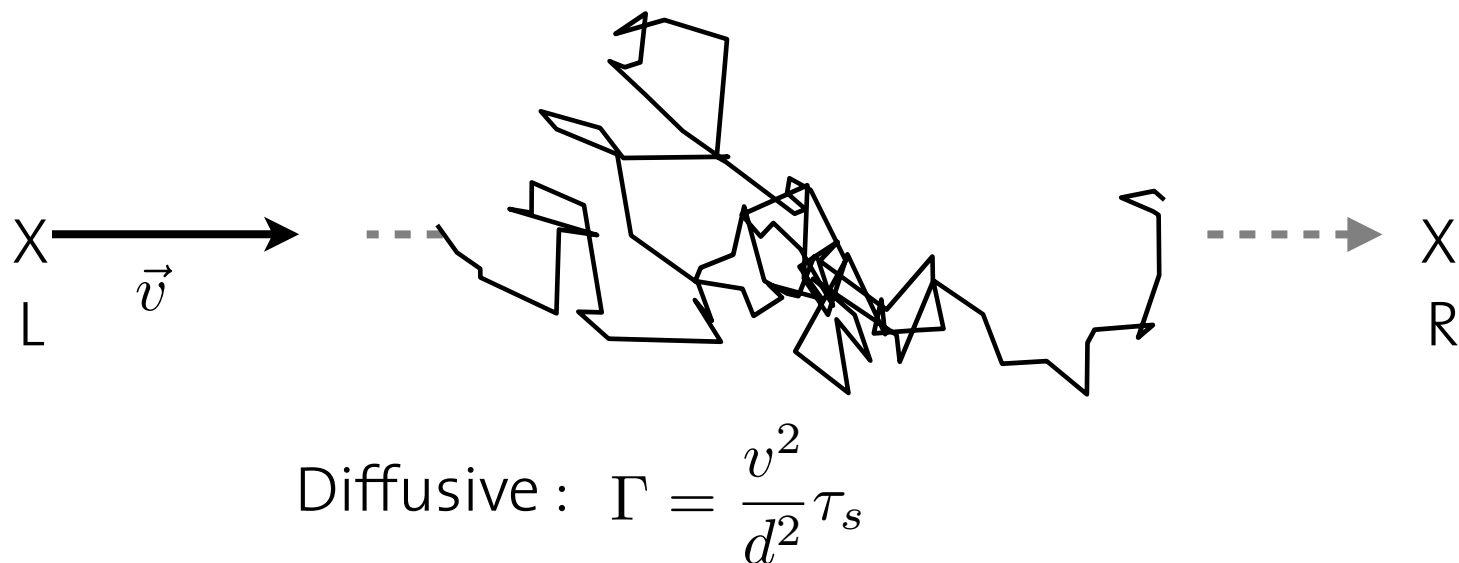
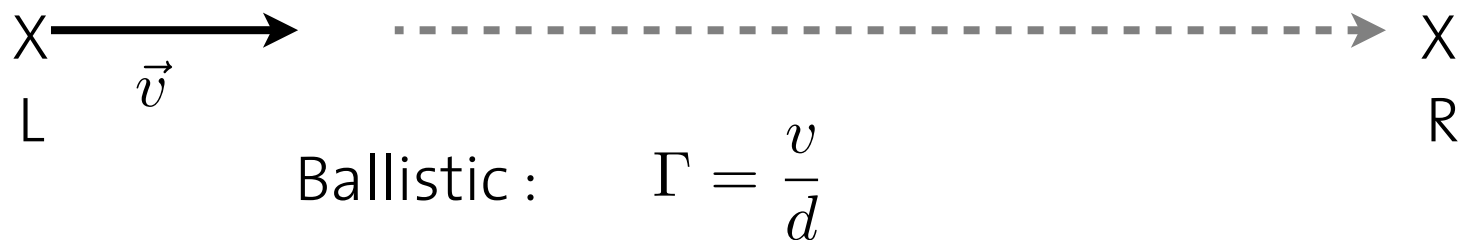


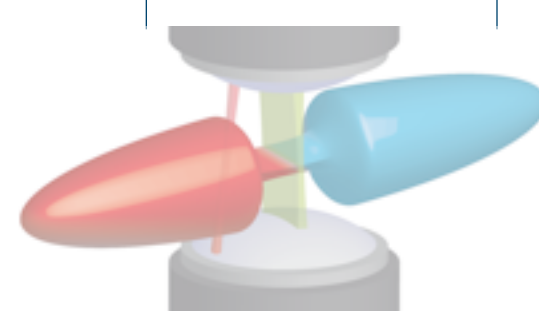
Transmission has a larger dependence on energy in the diffusive case

# Energy dependance of transmission



# Energy dependance of transmission



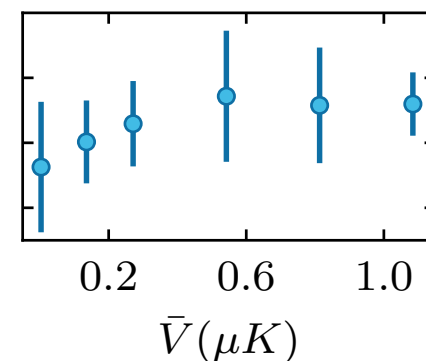
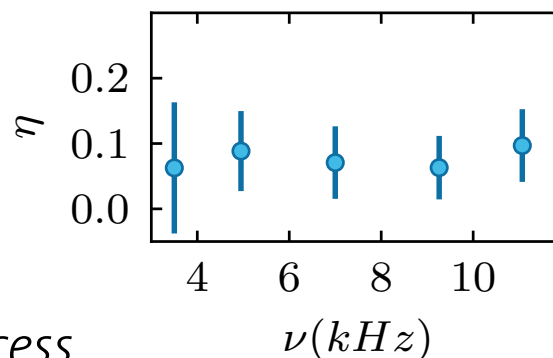


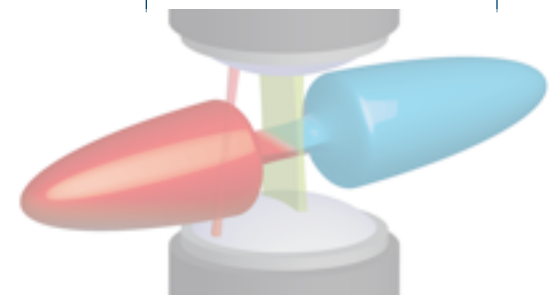
## Efficiency and Power

Thermoelectricity drives current against the potential difference

$$\eta = \frac{W}{Q_{\text{irr}}} = \frac{\int I_N \Delta\mu dt}{\int I_S \Delta T dt}$$

*efficiency relative to a reversible process*

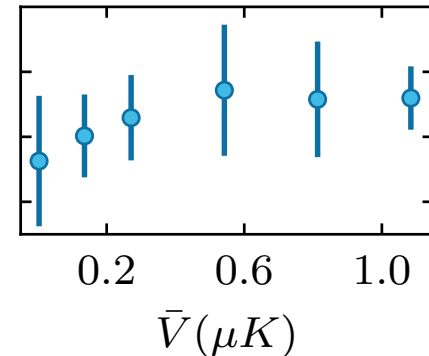
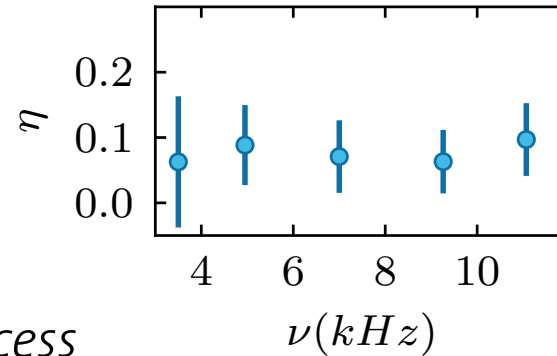




# Efficiency and Power

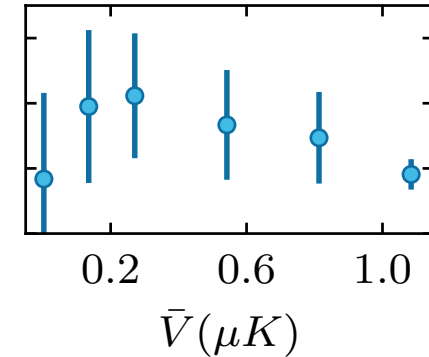
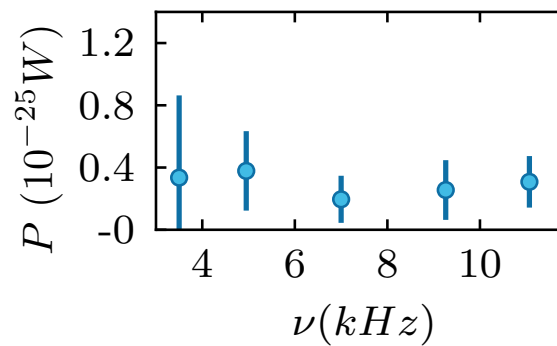
Thermoelectricity drives current against the potential difference

$$\eta = \frac{W}{Q_{\text{irr}}} = \frac{\int I_N \Delta\mu dt}{\int I_S \Delta T dt}$$



*efficiency relative to a reversible process*

$$P = \frac{W}{\tau_0}$$



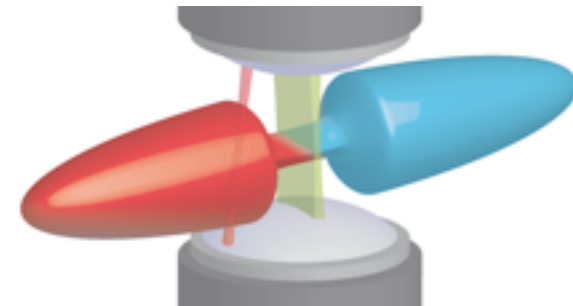
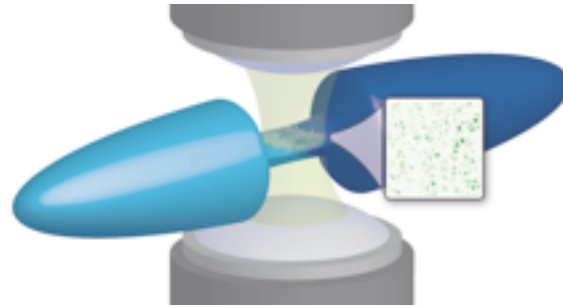
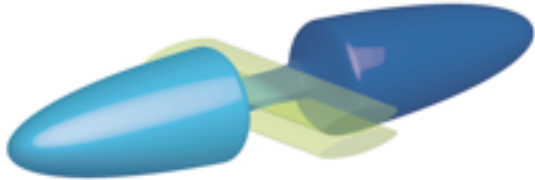
*average power for the “cycle”*

see also E.L.Hazlett *et al*, arXiv 1306.4018



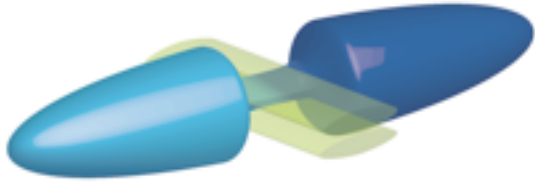
- Experimental setup
  - Two terminals Landauer configuration
  - Strongly attractive interactions: superfluids
  - Disordered superfluids
- Thermoelectric transport
  - Ballistic channel
  - Disordered channel : ballistic to diffusive crossover
  - Efficiency of heat to work conversion
- Outlook
  - Lithography for cold atoms

# Conclusion

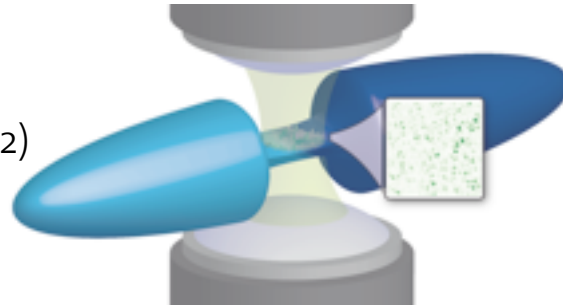


Transport properties of cold Fermions with tunable interactions / disorder / dimensionality

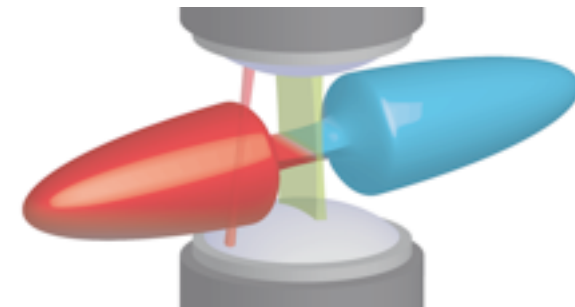
# Conclusion



J.P. Brantut *et al*, Science **337**, 1069 (2012)  
D. Stadler *et al*, Nature **491**, 736 (2012)



S. Krinner *et al*, PRL. **110**, 100601 (2013)  
S. Krinner *et al*, arXiv:1311:5174 (2013)



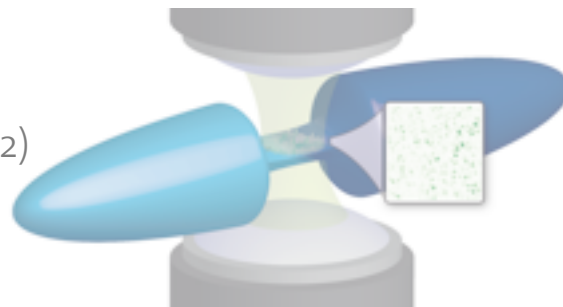
J.P. Brantut *et al*, Science **342**, 713 (2013)

Transport properties of cold Fermions with tunable  
interactions / disorder / dimensionality

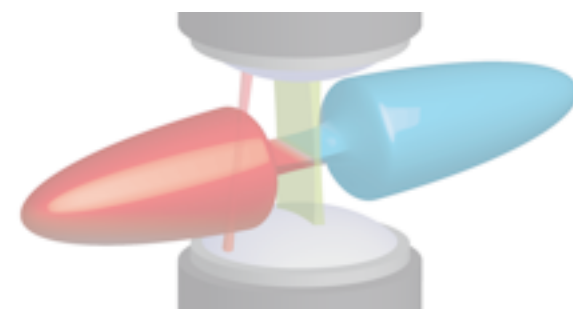
# Conclusion



J.P. Brantut *et al*, *Science* **337**, 1069 (2012)  
D. Stadler *et al*, *Nature* **491**, 736 (2012)



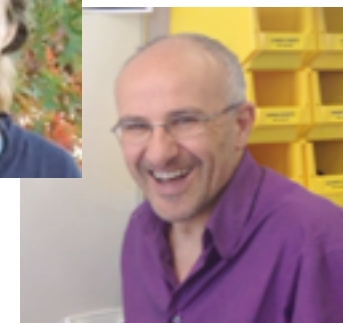
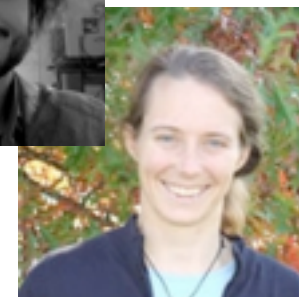
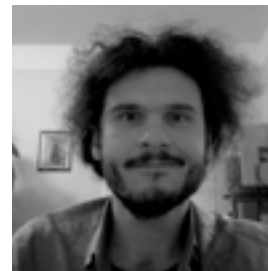
S. Krinner *et al*, *PRL*. **110**, 100601 (2013)  
S. Krinner *et al*, *arXiv:1311:5174* (2013)



J.P. Brantut *et al*, *Science* **342**, 713 (2013)

Transport properties of cold Fermions with tunable  
interactions / disorder / dimensionality

Towards quantum simulation of mesoscopic devices



*Experiment:* (ETH Zürich)  
S. Krinner      D. Husmann  
J.P. Brantut,    S. Haüsler  
J. Meineke      M. Lebrat  
D. Stadler  
T. Esslinger

*Theory of thermoelectricity :*  
C. Grenier (Ecole Polytechnique)  
C. Kollath (University of Bonn)  
A. Georges (College de France)

*Discussions :*

*T. Giamarchi, J. Blatter, W. Zwirger, L. Pollet, T. Bourdel, D. Shahar, V. Shenoy, V. Josse, P. Lugan, C. Mueller, S. Pilati, M. Mueller, T. Ihn, Y. Imry, D. Shepelyanski*