## Transport of entropy in cuprates

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### Transport of entropy in cuprates Orsay 1995–2000; Paris 2000–2007



**Hervé Aubin** [1994–1997;2004–2007]



**Cigdem Capan** [1999-2002]



Saco Nakamae [2000-2002]



[2001-2004]



Alexandre Pourret [2004–2007]



**Cyril Proust** 

Toulouse 2002 présent

### Contents

- I. Thermal conductivity
- Heat transport in conventional and unconventional superconductors
- Sub-kelvin thermal conductivity as a probe of gap structure

### II. Nernst effect

Sources of Nernst signal

- superconducting vortices
- short-lived Cooper pairs
- Normal quasi-particles

### Heat and charge current in a solid

$$\vec{J}_{e} = \sigma \vec{E} - \alpha \vec{\nabla} T$$
$$\vec{J}_{Q} = \alpha T \vec{E} - \kappa \vec{\nabla} T$$



Only components in red will be treated in this talk!



### Thermal conductivity of superconductors

- Above T<sub>c</sub> both mobile electrons and phonons carry heat.
- Below T<sub>c</sub>, mobile electrons condensate in a macroscopic quantum state: electronic heat carriers vanish!
- A superconductor can be assimilated to a thermal insulator!

### Conventional superconductors

- Electron thermal conductivity decreases exponentially
- Phonon thermal conductivity increases due to a diminished electron scattering



### Unconventional superconductors

- The order parameter of the is less symmetric than the Fermi surface.
- The gap function may vanish along particular orientations (nodes).
- Nodal quasi-particles can carry heat!

# Effect of an unconventional superconducting transition on thermal transport

• The electronic thermal transport does NOT decrease exponentially

• It can even increase below  $T_c$ , due to an increase in the electronic mean-free-path

## Scattering events are restricted in an unconventional superconductor



s-wave d-wave

### Heat conduction in high-T<sub>c</sub> superconductors

Aubin at al., 1997



The increase in thermal conductivity below T<sub>c</sub> is due to electrons!

Heat conduction in high-T<sub>c</sub> superconductors





Angular-dependent thermal conductivity reveals angular position of gap minima!

### Heat conduction in high-Tc superconductors

Sutherland at al., 2003



Cleaner systems show larger enhancement below T<sub>c</sub>

## In the zero temperature limit

Mean-free-path of both electrons and phonons attains its maximum value, then  $\kappa_{ph\,\propto}\,T^3$  (phonons are bosons)  $\kappa_e^{}\propto T$  (electrons are fermions)

In principle, one can separate the two contributions!



### Example



A residual normal fluid at zero temperature!



FIG. 1. *a*-axis thermal conductivity of the two YBa<sub>2</sub>Cu<sub>3</sub>O<sub>y</sub> crystals, one superconducting (y = 6.9; circles) and one insulating (y = 6.0; triangles). Main panel:  $\kappa/T$  vs  $T^2$ ; lines are fits to  $a + bT^2$  for T < 0.15 K. Inset:  $\kappa/T$  vs T.

### Universal thermal conductivity

• In a d-wave superconductor  $\kappa_0$  is expected to be independent of impurity concentration



These two cancel out!

 $\kappa = 1/3 C v l$ 

### A TALE OF TWO VELOCITIES! (Durst, Lee '99)

An anisotropic Dirac cone



Excitation spectrum in the vicinity of a node:  $E(k) = (\epsilon_k^2 + \Delta_k^2)^{1/2}$  $= (v_F^2 k_1^2 + v_2^2 k_2^2)^{1/2}$ 

$$\kappa_{00}/T = (nk_{B}^{2}/3\hbar) (v_{F}/v_{2})$$

Fermi velocity : $v_F = d\epsilon_k/dk_1$ Gap velocity:  $v_2 = d\Delta_k/dk_2$ 

## Residual quasi-particle conductivity in optimally-doped cuprates



## Experimental observation of universal thermal conductivity

(Taillefer et al., 1997)





FIG. 2. *a*-axis thermal conductivity of the four Zn-doped crystals, plotted as  $\kappa/T$  vs T.

FIG. 3. Residual linear term vs scattering rate for the four crystals of YBa<sub>2</sub>(Cu<sub>1-x</sub>Zn<sub>x</sub>)<sub>3</sub>O<sub>6.9</sub>; the dashed line indicates a constant at 0.19 mW K<sup>-2</sup> cm<sup>-1</sup>. Inset: same, but with corrected values (see text); the solid line is a least-squares fit.

A 30-fold decrease in mean-free-path in Zn-doped YBCO leaves  $\kappa_0$  unchanged

## The magnitude of the linear term is barely affected by the introduction of defects!



Nakamae et al., 2001

Evolution of the residual thermal conductivity with doping



Suggesting an enhancement of  $v_F/v_2$  with increasing doping!

### Assuming that $\kappa/T$ is inversely proportional to the superconducting





The interpretation is ambigous on the underdoped side!

But the nodal structure evolves with doping!

∆₀ (meV)

### Nernst effect

- In presence of a thermal gradient, electrons produce an electric field.
- Seebeck and Nernst effect refer to the longitudinal and the transverse components of this field.



$$N[=S_{xy} = e_y = e_N] = \frac{-E_y}{\nabla_x T} \qquad [v = \frac{-E_y}{B_z \nabla_x}]$$

### Nernst effect in the vortex state



A superconducting vortex is:

- A quantum of magnetic flux
- An entropy reservoir
- A topological defect

- Thermal force on the vortex :  $F=-S_{\phi} \nabla T (S_{\phi}: vortex entropy)$
- The vortex moves
- The movement leads to a transverse voltage: E<sub>y</sub>=v<sub>x</sub> B<sub>z</sub>

### Nernst effect in optimally-doped YBCO



FIG. 3. Resistivity  $\rho$  (a) and normalized Nernst electric field  $E_{y}/\nabla_{x} T$  (b) versus temperature for an epitaxial, *c*-axis-oriented YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7-8</sub> film at different magnetic fields applied parallel to the *c* axis of the film.

The Nernst coefficient is finite only in the vortex liquid state!

(Ri, et al. 1994)

### A positive Nernst signal survives above $\rm T_{c}$

Wang, Li and Ong, 2006



The fluctuating tail is longer in the underdoped regime

## Vortex-like excitations in the normal state of the underdoped cuprates?



A finite Nernst signal in a wide temperature range above T<sub>c</sub>

## Preformed Cooper pairs in the pseudogap state?

### Importance of phase fluctuations in superconductors with small superfluid density

#### V. J. Emery<sup>\*</sup> & S. A. Kivelson<sup>†</sup>

\* Department of Physics, Brookhaven National Laboratory, Upton, New York 11973, USA
† Department of Physics, University of California at Los Angeles, Los Angeles, California 90095, USA

Nature 1995

Two distinct temperature scales for superconductivity:

 $T^{\star}$  as the onset of phase fluctuating Cooper pairs ?  $T_{\rm c}$  as the onset of Phase coherence?



## The Nernst response of normal electrons

### Nernst effect in a single-band metal

Absence of charge current leads to a counterflow of hot and cold electrons:

$$J_Q \neq 0$$
;  $J_e = 0$ ;  $E_y = 0$ 



In an ideally simple metal, the Nernst effect vanishes! (« Sondheimer cancellation », 1948) In real metals Nernst coefficient can be large!



### Close-up on Sondheimer cancellation

$$\vec{J}_{e} = \sigma \vec{E} - \alpha \vec{\nabla} T$$
$$\vec{J}_{Q} = \alpha T \vec{E} - \kappa \vec{\nabla} T$$

$$J_e = 0 \qquad \qquad N = \frac{E_y}{\nabla_x T} = \frac{\alpha_{xy}\sigma_{xx} - \alpha_{xx}\sigma_{xy}}{\sigma_{xx}^2 + \sigma_{xy}^2}$$

Boltzmann picture: 
$$\overline{\alpha} = \frac{\pi^2}{3} \frac{k_B^2 T}{e} \frac{\partial \overline{\sigma}}{\partial \epsilon} \Big|_{\epsilon_F} \longrightarrow N = \frac{\pi^2}{3} \frac{k_B^2 T}{e} \frac{\partial \Theta_H}{\partial \epsilon} \Big|_{\epsilon_F}$$

If the Hall angle,  $\Theta_H$ , does not depend on the position of the Fermi level, then the Nernst signal vanishes!

### Recipe for a large diffusive Nernst response:

$$N = \frac{\pi^2}{3} \frac{k_B^2 T}{e} \frac{\partial \Theta_H}{\partial \epsilon} |_{\epsilon_F} \qquad \qquad \nu \sim (\pi^2/3) \ k_B^2 T/e \ \mu \ / \ E_F$$



## Quantum oscillations and the Fermi surface in an underdoped high-T<sub>c</sub> superconductor

Nicolas Doiron-Leyraud<sup>1</sup>, Cyril Proust<sup>2</sup>, David LeBoeuf<sup>1</sup>, Julien Levallois<sup>2</sup>, Jean-Baptiste Bonnemaison<sup>1</sup>, Ruixing Liang<sup>3,4</sup>, D. A. Bonn<sup>3,4</sup>, W. N. Hardy<sup>3,4</sup> & Louis Taillefer<sup>1,4</sup>



### **Electron pockets in the Fermi surface of hole-doped high-T<sub>c</sub> superconductors**

David LeBoeuf<sup>1</sup>, Nicolas Doiron-Leyraud<sup>1</sup>, Julien Levallois<sup>2</sup>, R. Daou<sup>1</sup>, J.-B. Bonnemaison<sup>1</sup>, N. E. Hussey<sup>3</sup>, L. Balicas<sup>4</sup>, B. J. Ramshaw<sup>5</sup>, Ruixing Liang<sup>5,6</sup>, D. A. Bonn<sup>5,6</sup>, W. N. Hardy<sup>5,6</sup>, S. Adachi<sup>7</sup>, Cyril Proust<sup>2</sup> & Louis Taillefer<sup>1,6</sup>

### The Nernst coefficient in YBCO



The background signal is negative!

The small electron pocket is the source of a negative Nernst signal in YBCO!



### Broken rotational symmetry in the pseudogap phase of a high-T<sub>c</sub> superconductor Na<sup>-</sup>

Nature 2010

R. Daou<sup>1</sup><sup>†</sup>, J. Chang<sup>1</sup>, David LeBoeuf<sup>1</sup>, Olivier Cyr-Choinière<sup>1</sup>, Francis Laliberté<sup>1</sup>, Nicolas Doiron-Leyraud<sup>1</sup>, B. J. Ramshaw<sup>2</sup>, Ruixing Liang<sup>2,3</sup>, D. A. Bonn<sup>2,3</sup>, W. N. Hardy<sup>2,3</sup> & Louis Taillefer<sup>1,3</sup>



The negative Nernst signal in YBCO emerges below T\* !!!????

### Broken rotational symmetry in the pseudogap phase of a high-T<sub>c</sub> superconductor Nature 2010

R. Daou<sup>1</sup><sup>†</sup>, J. Chang<sup>1</sup>, David LeBoeuf<sup>1</sup>, Olivier Cyr-Choinière<sup>1</sup>, Francis Laliberté<sup>1</sup>, Nicolas Doiron-Leyraud<sup>1</sup>, B. J. Ramshaw<sup>2</sup>, Ruixing Liang<sup>2,3</sup>, D. A. Bonn<sup>2,3</sup>, W. N. Hardy<sup>2,3</sup> & Louis Taillefer<sup>1,3</sup>



The Nernst response is extremely anisotropic in the pseudogap state!

Nernst effect due to Gaussian fluctuations of the amplitude of the superconducting order parameter (Usshishkin, Sondhi & Huse, 2002)



## In two dimensions, the coherence length is the unique parameter!

### Nernst effect in a conventional superconductor



### Surviving deep in to the normal state!

#### LETTERS

## Observation of the Nernst signal generated by fluctuating Cooper pairs

### A. POURRET<sup>1</sup>, H. AUBIN<sup>1</sup>\*, J. LESUEUR<sup>1</sup>, C. A. MARRACHE-KIKUCHI<sup>2</sup>, L. BERGÉ<sup>2</sup>, L. DUMOULIN<sup>2</sup> AND K. BEHNIA<sup>1</sup>\*

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## The Nernst signal of the normal electrons is negligible!

Pourret et al. 2006



## Comparison with theory

Experiment:



### The ghost critical field



Nb<sub>0.15</sub>Si<sub>0.85</sub>

Pourret et al. 2006

## Back to cuprates: upper critical field and the ghost critical field

Wang et al., 2006





The upper critical field?

### A brief summary

The Nernst signal in cuprates can come from:

- Normal quasi-particles:
- The negative Nernst signal in YBCO is generated by Fermi surface reconstruction
- Gaussian fluctuations:

Source of a positive Nernst signal above T<sub>c</sub> in any superconductor

Is there still room for phase fluctuations?

## Questions

### Is there any additional temperature scale associated with superconductivity? Probably, no!

• Why the sign of the Nernst signal in YBCO differ from other cuprates?

Chains? Stripe commensurability?

### Stripes?

#### Electrical Resistivity Anisotropy from Self-Organized One Dimensionality in High-Temperature Superconductors

Yoichi Ando, Kouji Segawa, Seiki Komiya, and A. N. Lavrov Central Research Institute of Electric Power Industry, Komae, Tokyo 201-8511, Japan (Received 31 July 2001; published 19 March 2002)





On peut traduire T et B en longueurs correspondantes! Même pour T »Tc la supraconductivité est la source du signal Nernst !