The Innovation Premium to Soft Skills in Low-Skilled Occupations*

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Abstract

We use matched employee-employer data from the UK to analyze the wage premium to working in an innovative firm. We find that firms that are more R&D intensive pay higher wages on average, and this is particularly true for workers in *some* low-skilled occupations. We develop a simple model where complementarity between workers in high-skilled occupations and workers in *some* low-skilled occupations increases with the firm's innovativeness. The model yields additional predictions about training, tenure and outsource which we show empirical support for in the data.

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1 Introduction

This paper has come out of a surprise empirical finding. It is not only workers in highskilled occupations that benefit from higher wage premia from working in more innovative firms, as predicted by the literature on skill-biased technical change, but the average worker in low-skilled occupations also obtains a significant wage premium from working in a more innovative firm, see Figure 1.



Figure 1: Average wage of workers in low-skilled occupations

Notes: Authors' calculations based on 104,318 observations in matched ASHE-BERD data; see Appendix A. The figure plots the average log of hourly wage at each age from 18 to 64 for workers in low-skilled occupations (see Appendix A.2.3). The dashed curve is for workers in firms that do not report R&D expenditure, the solid curve for workers in firms are firm that report positive R&D expenditure; see Appendix A.1. 95% confident intervals are included.

Our contribution in this paper is twofold. First, we use matched employer-employee data from the UK, augmented with information on R&D expenditures, to show that the wage premium from working in a more R&D intensive firm, relative to working in a less R&D intensive firm, is indeed positive and larger for workers in *some* low-skilled occupations. Second, we propose an explanation to rationalize this finding. In a nutshell: (i) workers productivity depends upon both hard skills and soft skills; (ii) more innovative firms exhibit a higher degree of complementarity between workers in high-skilled occupation and those workers in low-skilled occupation that have a high levels of soft skills; (iii) hard skills are largely observable whereas soft skills are less easy to detect *ex-ante*, and soft skills form a larger proportion of the abilities of workers in low-skilled occupations. Thus workers in low-skilled occupation command higher bargaining power in more innovative

firms (compared to similar workers in less innovative firms), since it is harder for such firms to replace these workers in low-skilled occupations with high soft skills.

We then test the assumptions and additional predictions of the model, in particular: (i) in more innovative firms workers in low-skilled occupations exhibit on average a higher degree of complementarity with employees in high-skilled occupations, than in less innovative firms; (ii) there is a wage premium to working in a more innovative firm for workers in low-skilled occupations, which increases with the complementarity between their quality and the quality of workers in high-skilled occupations; (iii) workers in low-skilled occupations should have longer tenure in more innovative firms than in less innovative firms; (iv) a more innovative firm will invest more in training its workers in low-skilled occupations than a non innovative firm; (v) a more innovative firm should outsource a higher fraction of tasks which involve lower complementarity between workers in high and low-skilled occupations.

The literature has established that there is considerable wage inequality between seemingly similar workers that is correlated with the firm that they work for (e.g. Abowd et al., 1999, Card et al., 2016). Less is known about what drives these differences, particularly for workers in low-skilled occupations. We highlight one channel, the importance of technology and the structure of production. The literature has been relatively silent as to why some firms pay higher wages than others for workers that appear similar. In a competitive labor market we would expect wages for similar workers to be the same across firms; heterogeneity in firm level technology might influence who is hired, but not the wages of any specific worker, since wages are taken as given by the firm. However, wages might deviate from marginal cost in imperfectly competitive markets. From the endogenous growth literature (e.g. see Romer, 1990; and Aghion and Howitt, 1992), where innovation-led growth is motivated by the prospect of rents, it seems that innovation would be a prime candidate, and recent papers show the effect of innovation on income inequality (e.g. Aghion et al., 2018; and Akcigit et al., 2017). Here we focus on the relationship between the wages of workers and the R&D intensity of the firms they work for.

Our findings are consistent with skill-biased technical change. Technology and innovation in our framework will increase the relative earnings of high-skilled workers in the overall economy. The underlying idea we develop is that workers in higher-skilled occupations typically have observable qualifications, and their market value is primarily determined by their education and accumulated reputation which are easily observable and verifiable. A firm can replace a worker in a high-skilled occupation by another similar worker with limited downside risk, because their quality is observable. In contrast, the key qualities of workers in *some* low-skilled occupations are soft skills (non-cognitive) and can be difficult to observe or develop, so difficult to replace.¹

As an example, think of a worker in a low-skilled occupation, for example a maintenance worker, a personal assistant or a sales telephonist, who shows outstanding initiative and reliability. These attributes may be difficult to measure and verify, yet they allow the worker to perform tasks which complement the tasks performed by high-skilled employees within the firm in the sense that mistakes by the worker in the low-skilled occupation can be damaging to the firm's overall performance.

Our work relates to several strands of literature. First, there is the literature on wage inequality and skill-biased technical change (e.g. see Acemoglu, 2002; Goldin and Katz, 2010, Acemoglu and Autor, 2011, Krusell et al., 2000). As already alluded to, our finding that the premium to working in more innovative firms is higher for workers in low-skilled occupations, is not at odds with the view that technical change has become increasingly skill-biased over the past thirty five years. Indeed, we find that more innovative firms outsource a higher fraction of workers in some low-skilled occupations. As technology advances, workers in high-skilled occupations do better overall because there is an increasing demand for this type of workers, but workers in some low-skilled occupations. Akerman et al. (2015) study the impact of the adoption of broadband internet on wages, they find that overall workers in low skill occupations and the tasks they do remain valuable.

Second, there is the labour and wage literature (Gibbons and Katz, 1992; Groshen, 1991 and Abowd et al., 1999 among others), which emphasises that firm heterogeneity plays a large role in explaining wage differences across workers; however, there is little consensus in explaining which features of the firm account for such variation. For example, Card et al. (2016) assume that firm heterogeneity arises through TFP, but do not model what drives these differences in TFP. Other studies report a link between productivity and wage policy (Cahuc et al., 2006 and Barth et al., 2016 among others) and Song et al. (2015) consistently find that "between firm inequality" accounts for the majority of the total increase in income inequality between 1981 and 2013 in the US. A recent trend of this literature is to link the aggregate dispersions in wages to productivity dispersion across firms (Barth et al., 2016, Dunne et al., 2004). Matched worker-employee data are often used (see Card et al., 2016 for

¹In our model the soft skills of workers in low-skilled occupations are largely unknown to the firm at the point of hiring or they require that the firm invest in training. Our model is not therefore a simple matching set up, and tenure increases the premium for workers in low-skilled occupations more in more innovative firms.

a review) to investigate whether this correlation represents differences in workers selected into different firms, or the same type of worker being paid a different wage depending on the firm they work in. Abowd et al. (1999) pioneered the use of the two-way fixed effect model (firm and worker fixed effects) to study the effect on wages when a worker moves between firms. In a related literature that seeks to measure rent-sharing elasticities, Card et al. (2016) report that, "most studies that control for worker heterogeneity find wage-productivity elasticities in the range 0.05-0.15.". We contribute to this literature by bringing innovation into the picture, and by analysing the relationship between innovation, wages and occupation across firms.

Third, two recent papers use individual fiscal data merged with patent data respectively in the US and in Finland to look at the individual returns from innovation to the inventors and to their co-workers in the US (Kline et al., 2017) and Finland (Aghion et al., 2018). Both papers find significant returns to innovation, most of which accrue to other employees or stakeholders within the inventor's firm.² We contribute to this literature by focusing on the comparison between workers in high-skilled and some low-skilled occupations in more versus less innovative firms, and on how innovativeness affects the degree of complementarity between workers in high-skilled and low-skilled occupations.

Finally, we draw on the literature on wage inequality and the organization of the firm (e.g. see Kremer, 1993, Kremer and Maskin, 1996, Garicano, 2000 and Garicano and Rossi-Hansberg, 2006). We contribute to this literature by linking wage inequality, the organization of the firm, and its degree of innovativeness.

The structure of rest of the paper is as follows. In Section 2 we present our data and empirical methodology, and establish that more innovative firms pay higher wages to observationally similar workers, particularly in low-skilled occupations. In Section 3 we develop a model to account for these findings and derive additional predictions from this model. In Section 4 we test these additional predictions and discuss the robustness of our main findings, in particular showing that workers in low-skilled occupations that get a wage premia from working in innovative firms work in occupations where soft skills are important. Section 5 collects our concluding remarks.

 $^{^{2}}$ Kline et al. (2017) find that workers capture 29 cents of every dollar of patent-induced operating surplus. Aghion et al. (2018) find that inventors get only 7.9% of the total gains, entrepreneurs get over 44.5% of the total gains and blue-collar workers get about 25.7% of the gains.

2 Wage premia for working in an innovative firm

In this section we describe our data and empirical approach to establish that more innovative firms pay higher wages to observationally similar workers, particularly in low-skilled occupations.

2.1 Data

We use novel matched employer-employee data for the UK that also contains information on R&D expenditure for the period 2004 to 2015. The employee data come from the Annual Survey of Hours and Earnings (ASHE), which is a random sample of 1% of the UK working population. We match this to the Business Expenditure on Research and Development (BERD) survey, which is a census for firms with 400+ employees. The data are longitudinal, we follow the same workers over time, and is recorded at the establishment level, with information on which establishments are part of the same firm. We focus on private companies (excluding the public sector, charities, etc) that have 400 or more employees. We use information on 186,000 employees who work in around 7,370 firms, giving us a total of 626,722 observations. Further details on the data are given in Appendix A.

We classify occupations by the average required skill level based on qualifications, see details in Appendix A.2.3. We distinguish low-skilled occupations, which are those that require on minimal formal education and training, intermediate-skilled occupations, which typically require the equivalent of a high-school education and include trades, specialist clerical, associate professionals, and high-skilled occupations, which typically included advance training or a university degree and include engineers and managers.

2.2 Wage premia

There are significant differences in the wages paid to workers in innovative firms compared to those working in non-innovative firms at all ages and even after controlling for a range of observable worker and firm characteristics. Figure 2 shows that the average wage of workers increases with the firm's R&D intensity; average wages are around 150% higher in the most R&D intensive firms compared to firms that do no R&D.³ This result echoes those of Van Reenen (1996), who showed that innovative firms pay higher wages on average, using information on public listed UK firms. Another way to see this is by looking at the

³This is (exp(3.2) - exp(2.287))/exp(2.287) = 1.49.

share of workers that work in a firm that does any R&D across the wage distribution; this increases from just over 20% for workers at the bottom of the wage distribution, to over 55% after the 80^{th} percentile of the distribution (see Figure A4 in Appendix A.5).



Figure 2: Wages and R&D intensity

Notes: This figure plots the average value of the log hourly wages against R&D intensity. The x-axis shows the average value of R&D intensity for each quantile of R&D intensity of the firm, with 20 quantiles and an additional one indicating zero R&D as quantile 0. Wages are defined in Appendix A.2.2. R&D intensity is defined in Appendix A.1.

Workers in more R&D intensive firms might have different characteristics to those working in less R&D intensive firms. Table 1 shows that they are indeed more likely to be male, work full-time and have longer tenure within the firm. R&D firms also differ from non-R&D firms in that they are larger (have a larger workforce), all of which might affect the wages of workers in these firms. In Appendix A we give further descriptive statistics of the key variables.

	Innovative firm		Current R&D firm	
	Yes	No	Yes	No
Employment	2 784	2 213	2 543	2,365
Hourly Wage (£)	15.8	12.5	16.1	12.9
Share of Male (%)	68	56	70	57
Share of full-time	90	76	92	77
Workers in high-skilled occupations (%)	30	18	31	19
Workers in low-skilled occupations (%)	51	65	50	63
Age	40.4	38.1	41.1	38.3
Tenure	8.8	5.7	9.5	5.9
Workers	72,718	113,181	52,617	135,551
Firms	2,332	5032	1,877	5,939
Firms-years	12,871	25,481	8,542	29,810
Worker-firm-year	263,447	363,275	162,764	463,958

Table 1: Comparison of R&D and non R&D firms

Notes: Innovative firms are those that report any R&D expenditure over the period, current R&D firms are those that report a positive amount of R&D expenditure in that period. Employment is the average number of workers in the firm over all years. Wages are defined in Appendix A.2.2. Skill level is defined in Appendix A.2.3.

To investigate whether these correlations hold up to controlling for other individual and firm characteristics we estimate the following relationship:

$$ln(w_{ijkft}) = \beta_1 \tilde{R}_{ft} + \beta_2 f(A_i, T_{ift}, FT_{ift}, S_{ift}) + \gamma_i + \eta_t + e_{ijkft},$$
(1)

where *i* indexes individual, *j* occupation, *k* labor market, *f* firm and *t* years; w_{ijkft} is the hourly wage, and $\tilde{R}_{ft} = ln(1 + R_{ft})$ is R&D intensity.⁴ A_i is the age of the worker, T_{ift} is the workers tenure (length of time working in the firm), FT_{ift} is an indicator of whether the job is full-time (as opposed to part-time), and S_{ft} is number of employees in the firm. η_t represent common time effects. Finally, e_{ijkft} captures remaining idiosyncratic time varying unobservables.

Table 2 presents our estimates of equation (1). In Column (1) we include only labour market (defined as a travel to work area; there are around 240 such areas in the UK, see

⁴R&D expenditure divided by number of employees, we use $ln(1+R_{ft})$ to accommodate values of zero in firms that do not do any R&D; it is almost always equal to $ln(R_{ft})$ given the magnitude of R&D expenditure, so we can interpret β_7 as the elasticity of wage with respect to R&D intensity. In Section 4.6 we show robustness of our results to alternative functional forms and alternative measures of R&D.

Appendix A.3) and time effects. The coefficient estimate of 0.029 suggest that workers in the most R&D intensive firms earn nearly 50% more than workers in firms that do no R&D,⁵ controlling for these characteristics accounts for a substantial part of the differences we saw in the raw data.

In section 4 below we introduce a second form of skills "soft skills" that are less easy to measure and therefore less verifiable. We argue that these are valuable to R&D firms and also form a larger proportion of the potential skill bundle of workers in low skill occupations. Before developing the model and results with soft skills we first provide evidence that more innovative firms pay higher wages to observationally similar workers, particularly those in low-skilled occupations.

In column (2) of Table 2 we add occupation effects at the two-digit level (25 occupations). This reduces the coefficient on R&D intensity by about half, the coefficient estimate of 0.016 suggest that workers in the most R&D intensive firms earn around 24% more than workers in firms that do no R&D.⁶

In column (3) we add worker effects (γ_i). These are included to capture permanent unobserved attributes that workers carry across firms. These are important and control for selection on unobserved permanent individual characteristics. Higher quality workers might select into higher quality firms. Identification is achieved through individuals who move jobs between firms that do more or less R&D, and individuals working in firms that increase or decrease their R&D intensity. This specification accounts for endogenous selection and matching based on the individual effect (γ_i). We drop occupation and labour market effects as we do not observe many workers who move across occupations or labour markets. This specification reduces the coefficient on R&D intensity to 0.006, which implies that workers in the most R&D intensive firms earn around 8% more than workers in firms that do no R&D.⁷ Compared to the estimates in column (3) the estimates without worker effects considerably over-estimate the impact of R&D intensity on wages.

Figure 3 showed that workers in low-skilled occupations earned higher wages on average in innovative firms; is that true for workers in high- and intermediate-skill occupations? Figure 3 shows that the within-skill group variance of wages across firms is relatively more important for workers in low-skilled occupations than workers in high- or intermediate-

⁵This is (exp(predicted wage at $max(\tilde{R}_{ft})$) minus exp(predicted wage at $min(\tilde{R}_{ft})$))/exp(predicted wage at $min(\tilde{R}_{ft})$)=(exp(2.678)-exp(2.287))/exp(2.287)=0.48, where the predictions use the coefficient estimates from column (1) of Table 2.

⁶As footnote 5, using the coefficient estimates from column (2) of Table 2: $(\exp(2.506) - \exp(2.287))/\exp(2.287) = 0.24$.

⁷As footnote 5, using the coefficient estimates from column (3) of Table 2: $(\exp(2.368) - \exp(2.287))/\exp(2.287) = 0.08$.

Dependent variable: $ln(w_{ijkfi})$							
	(1)	(2)	(3)	(4)	(5)	(6)	(7)
Skill level	All	All	All	Low	Med	High	All
~							
R_{ft}	0.029***	0.016***	0.006***	0.007***	0.003***	-0.000	0.002***
	(0.002)	(0.001)	(0.001)	(0.001)	(0.001)	(0.001)	(0.001)
×med skill							0.002***
1 1 111							(0.001)
×IOW-SK111							0.006***
Age	0.058***	0.034***					(0.001)
1150	(0.003)	(0.002)					
Age Squared	-0.001***	-0.000***	-0.001***	-0.000***	-0.001***	-0.001***	-0.001***
81	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)
Tenure	0.023***	0.015***	0.008***	0.009***	0.006***	0.001	0.007***
	(0.001)	(0.001)	(0.000)	(0.001)	(0.001)	(0.001)	(0.000)
Tenure Squared	-0.000***	-0.000***	-0.000***	-0.000***	-0.000***	0.000	-0.000***
	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)
Firm Size	-0.032***	-0.010***	-0.008***	-0.005**	0.002	0.004	-0.006***
	(0.006)	(0.004)	(0.002)	(0.002)	(0.003)	(0.002)	(0.002)
Gender	0.156***	0.143***					
	(0.006)	(0.004)					
Full-Time	0.244***	0.070***	0.004	-0.011*	-0.089***	-0.109***	-0.004
	(0.014)	(0.007)	(0.005)	(0.006)	(0.014)	(0.014)	(0.005)
low-skill							-0.15/***
mod abill							(0.006)
med-skin							-0.073^{+++}
							(0.004)
Occupation-year	\checkmark						
Geo-Occupation-year		\checkmark					
Individual			\checkmark	\checkmark	\checkmark	\checkmark	\checkmark
Year			\checkmark	\checkmark	\checkmark	\checkmark	\checkmark
R^2	0.385	0.624	0.887	0.774	0.851	0.885	0.889
Observations	626,210	626,210	626,210	407,341	104,318	114,535	626,210

Table 2: Relationship between wages and R&D intensity

Notes: The dependent variable is log of wage which is defined in Appendix A.2.2. $\tilde{R}_{ft} = ln(1 + R_{ft})$. Other covariates definitions are given in Table A7. Column 1 includes year-labour market fixed effects, column 2 includes year-labour market-occupation effects, column 3-7 include year and individual fixed effects. The specifications in column 3-7 can't identify Age and the Gender dummy because of additive worker and year fixed effects. Heteroskedasticity robust standard errors clustered at the firm level are reported in parenthesis. ***, ** and * respectively indicate 0.01, 0.05 and 0.1 levels of significance.

skill occupations. Workers in higher skill occupations earn the highest wages, and these wages are on average similar across firms that are more or less R&D intensive. In contrast, workers in low-skilled occupations earn substantially more if they work in a firm that has higher R&D intensity. The wage gradient with respect to R&D intensity is largest for workers in low-skilled occupations.

Figure 3: Average wage of workers in high- and intermediate-skilled occupations



Notes: This figure plots the average log of hourly wage at each age from 18 to 64 for workers in different skill level occupation. The dashed curve is for workers in non-innovative firms, the solid curve for workers in innovative firms. Innovative firms are firm that report at least £1 in R&D expenditures over the period. 95% confident intervals are included.

In order to see if the wage premium shown in Figures 1 and 3 are robust to controlling for other difference in workers and firms we separately workers by skill level of their occupation. Column (4) of Table 2 shows low-skilled occupations, column (5) intermediateskilled occupations and column (6) high-skilled occupations. The positive coefficient on R&D intensity holds for low and intermediate-skill categories and is strongest for the lowskilled occupations. In column (7) we pool all skill levels and allow the intercept and coefficient on R&D intensity to vary with the skill level. The premium is higher for workers in intermediate and low-skilled occupations.

The estimates in column (7) suggest that on average workers in low-skilled occupations in the most R&D intensive firms earn 12% more than workers in firms that do no R&D,⁸ for workers in intermediate-skilled occupations they earn 6% more and for workers in high-skilled occupations 3% more, once we condition on worker effects and other observables.

Of course highly innovative firms also hire fewer workers in low-skilled occupations. Table A9 in the Appendix shows that moving from the least to the most R&D intensive firm increases the share of workers in high-skilled occupations from 13.7% to 53.8%.

The finding that the premium to working in a more innovative firm is larger for workers in low-skilled occupations may, at first sight, look somewhat counter-intuitive and at odds with the literature on skill-biased technical change. In the next section we show how this finding can be rationalized. More specifically, we propose a model in which a firm's inno-

⁸As footnote 5, using the coefficient estimates from column 4 of Table 2: $(\exp(2.174) - \exp(2.065))/\exp(2.065) = 0.12$.

vativeness is reflected in the degree of complementarity between workers in low-skill and high-skilled occupations.

3 A Model

In this section we propose an explanation for the fact we showed in the previous section: namely, that the premium to working in more innovative firms, is higher for workers in low-skilled occupations than for those in high-skilled occupations. The idea of the model can be summarized as follows: (i) workers productivity depends upon both, hard skills and soft skills; (ii) more innovative firms exhibit a higher degree of complementarity between workers in high- and low-skilled occupations. A key feature of the model is that hard skills are largely observable (e.g. those are typically more educated employees, whose market value is largely determined by their education and accumulated reputation), whereas soft skills are less easy to detect *ex-ante* or require more training. Moreover, soft skills account for a larger fraction of workers' overall abilities for workers in low-skilled occupations than for workers in high-skilled occupations. Workers in low-skilled occupations with relatively high soft skills draw bargaining power for two reasons. First from the fact that they are more complementary to workers in high-skilled occupations. Second from the fact that it is hard for the firm to find alternative workers in low-skilled occupations with relatively high soft skills right away: instead, firms need time to find or train workers to get equal levels of soft skills. As a result, workers in low-skilled occupations with high soft skills will command a higher wage in more innovative firms. If we further assume that the firm's output suffers more from replacing a worker in a low-skilled occupation with high soft skill than from replacing a worker in a high-skilled occupation, then the wage differential between workers in low-skilled occupations in more versus less innovative firms will be higher than the wage differential between workers in high-skilled occupations in more versus less innovative firms. We now proceed to formalize our argument.

3.1 Model setup

Production function

We consider a representative firm which we model as a two-layer hierarchy with workers in high and low-skilled occupations. For simplicity we assume that there is one high-skilled occupation employee who monitors a continuum of tasks, each of which is performed by a different low-skilled occupation worker. Tasks are ranked according to the degree of complementarity $\lambda \in [0, 1]$ between high and low-skilled occupation workers. If Q denotes the overall quality of the employee in the high-skilled occupation, and $q = q(\lambda)$ denotes the overall quality of the worker in low-skilled occupation on task λ , then the output produced on that task is assumed to be determined by the following "partially O'Ring" production function (see Kremer, 1993 and Kremer and Maskin, 1996):

$$f(\lambda, q, Q) = \lambda q Q + (1 - \lambda) (q + Q).$$

The value $\lambda = 0$ corresponds to full substitutability between the qualities of the employees in the high and the low-skilled occupations. The value $\lambda = 1$ corresponds to the case where the qualities of the employees in the high and low-skilled occupations are fully complementary.

The firm's total output is then taken to be a weighted sum of the outputs on the individual tasks. Formally, if $\phi(\lambda)$ denotes the weight function on tasks, which we allow to vary with the degree of innovativeness z of the firm, we denote the firm's aggregate production by:

$$F(\vec{q}, Q) = \int_0^1 f(\lambda, q(\lambda), Q) \phi(\lambda, z) d\lambda.$$

where:

$$\vec{q} = (q(\lambda))_{\lambda \in [0,1]}$$
 and $\int_0^1 \phi(\lambda, z) d\lambda = 1.$

Wage negotiation

For each task λ , the firm engages in separate wage negotiations with the high- and lowskilled occupation workers on that task. This negotiation leads to the equilibrium wage $w_q(\lambda)$ for the worker in the low-skilled occupation and to w_Q for the worker in the highskilled occupation. We denote by β^L (resp. β^H) the fraction of the firm's net surplus that accrues to the worker in the low-skilled occupation (resp. high-skilled occupation) where we assume: $\beta^L \leq \beta^H < 1$.

Wages within the firm are determined by Nash bargaining following Stole and Zwiebel (1996). In this bargaining, the firm has the opportunity of replacing the high-skilled occupation employee - whose quality is Q - by an outside high-skilled employee with ex ante expected quality Q_L . Similarly, on each task λ , the firm has the outside option of replacing the worker in the low-skilled occupation on that task - this worker has quality $q(\lambda)$ and is

paid wage $w_q(\lambda)$ - by an outside worker with reservation quality q_L and reservation wage w_L .⁹

We assume that it is easier for the firm to find a substitute for employee in the highskilled occupation than in the low-skilled occupation. The underlying idea is that soft skills account for a higher share of the overall quality for a low-skilled occupation worker than for a high-skilled occupation worker, and that soft skills are harder to detect *ex-ante* or to generate via training than hard skill. Formally, this leads us to assume that:

$$Q - Q_L < q(\lambda) - q_L,$$

for all λ , where we also assume that $Q > Q_L >> q(\lambda) > q_L > 1$.

Substitute workers in low-skilled and high-skilled occupations are paid wages w_L and w_H respectively, which we assume to be exogenous. Similarly, the low- and high-skilled occupations incumbent workers have outside option \bar{w}^L and \bar{w}^H , which are also exogenous. We assume: $w_L < w_H$ and $\bar{w}^L << \bar{w}^H$.

The firm's total wage bill is then equal to

$$W(\vec{q}) = \int_0^1 w_q(\lambda) d\lambda + w_Q,$$

Training and profits

The firm's *ex post* profit is equal to:

$$\tilde{\Pi}(\vec{q}) \equiv F(\vec{q}) - W(\vec{q}).$$

We assume that prior to wage negotiation, the firm can learn about or train the lowskilled occupation worker on each task λ , so that the expected quality of the worker moves up from q_L to some higher quality level $q(\lambda)$ at a quadratic cost. The firm's *ex ante* training investment will seek to maximize:

$$\tilde{\Pi}(\vec{q}) - \int_0^1 C(\lambda) \left(q(\lambda) - q_L\right)^2 d\lambda,$$

with respect to $\vec{q} = (q(\lambda))_{\lambda}$.

⁹An alternative interpretation is that absent a wage agreement the low-skilled occupation worker chooses to underperform at quality level q_L .

Innovativeness and complementarity

We shall assume that more innovative firms display higher average complementarity between high and low-skilled occupation qualities across tasks. More formally, we assume that

$$\mathbb{E}_{\phi}\left(\lambda,z\right) = \int_{0}^{1} \lambda \phi(\lambda,z) d\lambda$$

increases with the innovativeness measure z.

Here are two tractable cases which will allow us to nicely develop our intuitions:

Example 1. Suppose that $\phi(\lambda, z) = (z + 1)\lambda^z$. In that case we have:

$$\mathbb{E}_{\phi}\left[\lambda\right] = 1 - \frac{1}{z+2},$$

which increases with the innovation intensity z.

Example 2. An even simpler case which we shall refer to as the "toy case", is where $\phi(\lambda, z)$ is equal to 1 only for $\lambda = \lambda_z \equiv \frac{z}{z_{max}}$ (where z_{max} denotes the maximum value z can take) and to zero for $\lambda \neq \lambda_z$. In that case:

$$\mathbb{E}_{\phi}\left[\lambda\right] = \frac{z}{z_{max}},$$

which again increases with the innovation intensity z.

3.2 Solving the model

To simplify the analysis we henceforth assume that the bargaining surplus is split equally between the firm and each worker ($\beta_H = \beta_L = 1$) and that the training cost parameter *C* is independent of the task.

3.2.1 The toy case

Here we consider the toy case where $\phi(\lambda, z) = 1$ if $\lambda = \lambda_z$ and 0 otherwise. In this case, the firm with innovativeness level z has only one task $\lambda = \lambda_z$ performed (other tasks are irrelevant to the firm since they have no impact on its production).

Equilibrium low-skilled occupation wages The firm's net surplus from employing a worker with quality q in a low-skilled occupation on the unique task λ_z , is equal to:

$$S^F = [\lambda_z Q + (1 - \lambda_z)](q - q_L) - w_q + w_L.$$

The surplus of the worker in low-skilled occupation on that task is equal to

$$S^{LS} = w_q - \bar{w}^L,$$

where \bar{w}^L is the worker's outside option.

Since we assume $\beta_L = 1$, the equilibrium wage of the worker in the low-skilled occupation on the unique task λ_z is defined by equalizing the two surplus:

$$w_q(\lambda_z, q, Q) = \frac{q - q_L}{2} \left(\lambda_z(Q - 1) + 1\right) + \frac{w_L + \bar{w}^L}{2}$$
(2)

Equilibrium high-skilled occupation wage Replicating the same argument for the worker in the high-skilled occupation, we obtain the following expression for the equilibrium wage of the high occupation employee:

$$w_{Q}(\lambda_{z}, q, Q) = \frac{Q - Q_{L}}{2} \left(\lambda_{z}(q - 1) + 1\right) + \frac{w_{H} + \bar{w}^{H}}{2}$$
(3)

Optimal training decision Having determined the equilibrium wages w_Q and w_q for given q, Q and z, we now move back and consider the firm's optimal choice of qualities $(q^*(\lambda_z) = q^*, Q^*)$, where we impose

$$q^* \in [q_L, \overline{q}]; Q^* \in [Q_L, \overline{Q}].$$

Then the firm chooses (q^*, Q^*) by solving:

$$(q^*, Q^*) = \underset{q_L < q < \overline{q} \ Q_L < Q < \overline{Q}}{\operatorname{argmax}} \left\{ f(\lambda_z, q, Q) - w_Q(\lambda_z, q, Q) - w_q(\lambda_z, q, Q) - C(q - q_L)^2 \right\}$$

With respect to Q, the problem is linear which leads to the corner solution $Q^* = \overline{Q}$. With respect to q, the problem is concave so that by first order condition we obtain:

$$q^*(\lambda_z) = q_L + \frac{1}{4C} \left[\lambda_z (Q_L - 1) + 1 \right],$$

where we implicitly assume that this value if lower than \overline{q} .¹⁰ Note that q^* is increasing with λ_z , and therefore with z: that is, the optimal level of training of a worker in a low-skilled occupation is higher in a more innovative firm.

¹⁰A sufficient condition is that $\overline{q} > q_L + \frac{Q_L}{4C}$. Note that we must have $Q_L >> \overline{q}$, which is true as long as training costs are large enough.

Innovativeness and high versus low-skilled occupation wages The equilibrium wage of the worker in the low-skilled occupation on task z, up to a constant, is equal to:

$$w_q(z) \equiv w_q(\lambda_z, q^*(\lambda_z), Q^*)$$

and similarly, the equilibrium wage of the worker in the high-skilled occupation on task z, up to a constant, is equal to:

$$w_Q(z) \equiv w_Q(\lambda_z, q^*(\lambda_z), Q^*).$$

We have the following results:

Proposition 1. The premium to working in a more innovative task-firm is higher for workers in low-skilled occupations than for workers in the high-skilled occupations:

$$\frac{dw_q(z)}{dz} > \frac{dw_Q(z)}{dz}$$

Proof. See Appendix B.1

The proposition immediately results from the fact that in more innovative firms the complementarity is higher between the worker in the high-skilled occupation and low-skilled occupation workers with training (or with high soft skill), and that the optimal training of workers in low-skilled occupations is higher in more innovative firms so that replacing the current worker in the low-skilled occupation by an outside worker has a more negative impact for such a firm.

3.2.2 The general case

We now consider the case where the firm covers a whole range of tasks with a continuous density distribution $\phi(\lambda, z)$ over tasks λ . We assume that $\phi(\lambda, z)$ is increasing in both λ and the innovativeness level z. We then show the following result:

Proposition 2. The average premium across tasks to working in more innovative firms, is higher for workers in low-skilled occupations than for workers in high-skilled occupations:

$$\frac{d\overline{w}_q}{dz} > \frac{d\overline{w}_Q}{dz}$$

Proof. See Appendix B.2

3.2.3 Outsourcing

Assume that the firm is subject to an overall time constraint (or "limited attention" constraint) for training or screening. Formally:

$$\int_0^1 \left(q(\lambda) - q_L\right) d\lambda \le T,$$

so that ex ante the firm maximizes

$$\tilde{\Pi}(\vec{q}) - \int_0^1 C(\lambda) \left(q(\lambda) - q_L\right)^2 d\lambda$$

subject to that constraint:

Then if the above time constraint is binding, for sufficiently low λ it is optimal for the firm to fix $q^*(\lambda) = q_L$, which we interpret as outsourcing the corresponding task. The following proposition, establishes that the cutoff value of λ below which the firm outsources tasks, increases with the firm's degree of innovativeness z.

Proposition 3. There exists a cutoff value $\overline{\lambda}(z)$ such that for all tasks $\lambda \leq \overline{\lambda}(z)$, then $q^*(\lambda) = q_L$: in other words all tasks $\lambda \leq \overline{\lambda}(z)$ are outsourced. Moreover, we have

$$\frac{d\bar{\lambda}(z)}{dz} > 0.$$

That is, more frontier firms outsource a higher fraction of tasks.

Proof. See Appendix B.3

In the case where $\phi(\lambda, z) = \lambda^z(z+1)$, it is possible to find tractable formula that defines $\overline{\lambda}$ for integer values of *z* (see Appendix B.3). Figure 4 shows the cases *z* = 0, 1 and 2.

3.3 Testing the model

In the next section we shall test the following assumptions and predictions of the above model. Here we list the corresponding facts or conjectures:

Fact 1: In more innovative firms workers in low-skilled occupation exhibit on average a higher degree of complementarity with high-skilled occupation employees, than in less innovative firms.

Fact 2: There is a wage premium to working in a more innovative firm for workers in low-skilled occupation, which is driven by the complementarity between their quality and the quality of workers in high-skilled occupation.

Figure 4: $\overline{\lambda}$ as a function of z



Fact 3: Workers in low-skilled occupations should have longer tenure in more innovative firms than in less innovative firms, as more time and money is invested in getting them from q_L to q^* .

Fact 4: A more innovative firm will invest more in training its low occupation workers than a non innovative firm. This is captured by the fact that $q - q_L$ is an increasing function of z in the model.

Fact 5: A more innovative firm will outsource a higher fraction of tasks which involve lower complementarity between workers in high and low-skilled occupations.

We now confront these facts/conjectures to the data.

4 Empirical evidence

The model relies on the distinction between hard-skills and soft-skills. Hard-skills are reasonably easy to observe, for example, by formal qualifications. Soft-skills are more difficult to observe, both for us as researchers and for employers. In our model what drives the returns to working in an R&D firm for workers in low-skilled occupations is that *some* have soft-skills and these are important for the firm. By their nature these soft-skills are difficult to observe and measure.¹¹

¹¹It is important to note that we do not argue that the *absolute* importance of soft-skills is higher for workers in low-skilled occupations. Our model is predicated on the idea that these soft-skills are *relatively* more

4.1 Measuring complementarity λ

To test the predictions and assumptions of the model, it is useful to find a measure for λ . We do so by working at the occupation level using the O*NET data. The O*NET data provides detailed information on the characteristics of occupations based on surveys of workers and experts in the US (more detailed are given in Appendix A.6). We work at the 3 digit SOC 2010 occupation level.

In our model we denote the level of complementarity between workers in high and low-skilled occupations of each task by $\lambda \in [0, 1]$. The O*NET data contain a number of questions that are related to the idea of complementarity that is captured by λ . We select 7 dimensions that we believe are most relevant for our purposes and aggregate into a single score using principle components analysis. Workers are surveyed and asked to grade each dimensions from 1 (this dimension is not relevant to this occupation) to 5 (this dimension is very relevant to this occupation). We run a principal component analysis eigen decomposition and consider the first eigen axis as our measure of complementarity λ ; this explains more than 57% of the total variance. Table 3 presents these 7 dimensions and their relative importance in the definition of λ .

important for workers in low hard-skill occupations, but they are still lower than for high-skilled occupation workers in absolute. Consider, for example, the pay of a researcher. The average researcher will also have high soft-skills. However, their pay we be largely determined by the university they graduated from, and their track record of publication and invention; soft-skills will be relatively unimportant for their pay. In contrast, an administrative assistant might have less soft-skills on average, but these will form an important part of their value to the researcher, and thus to the firm, and so be influential in their pay. These will also be difficult to observe, but will be revealed over time.

O*NET Dimension	Weight
How important is being very exact of highly accurate in performing the	0.1191
job?	
How serious would be the result usually be if the worker made a mistake	0.3377
that was not readily correctable?	
What results do your decisions usually have on other people or the image	0.4395
or reputation or financial resources of your employer?	
How important is it to work with others in a group or team in this job?	0.3736
How responsible is the worker for work outcomes and results of other	0.4004
workers?	
How important is it to coordinate or lead others in accomplishing work	0.4425
activities in this job?	
How important is the following skill for your job: "Adjusting actions in	0.4278
relation to others' action"?	

Table 3: O*NET dimensions contributing to λ

Notes: Results from a Principal Component Analysis of the seven dimension taken from O*NET at the occupation level. The weight correspond to the decomposition of the first axis.

We standardized our resulting measure so that λ is always between 0 and 1. On average, low-skilled occupation employees work in task with a λ of 0.41, with a standard deviation of 0.17. In what follows, we shall refer to high lambda occupations as occupations in the top 33% of lambda, and similarly to low lambda occupations as occupations in the bottom 33%. Following this terminology, 55% of workers are in low lambda occupations (224,552 out of 410,198) and 12% (49,888) in a high lambda occupation.

4.2 Workers in high-lambda low-skilled occupations are more essential in more innovative firms

In this section, we first show that more innovative firms have a higher share of low-skilled occupations that are associated with a high value of λ . In particular, Figure 5 shows that the share of high lambda occupations among low-skilled occupations essentially increases with the firm's R&D intensity, which vindicated our first conjecture (Fact 1). This share increases from around 11% for no R&D firms to around one third for the most innovative firms.

In line with our model, we expect workers in these high lambda low skill occupations to have a higher wage in more innovative firms. This is indeed what Figure 6(a) hints at. Namely, Figure 6(a) shows a clear positive correlation between the log of hourly wage and our measure of λ , the average level of complementarity of tasks in the firm, for innovative





Notes: This Figure reports the average share of workers in high lambda occupations among low-skilled occupation workers against the average level of R&D intensity of the firm for 20 percentiles of the R&D intensity distribution, and for non innovative firms.

firms. Doing the same exercise but replacing the logarithm of hourly wage by the tenure in the firm also yields a positive correlation, as presented in Figure 6(b).

In the next section, we provide more detailed evidence that the premium of low-skilled occupation workers from working in more innovative firms increases with both λ and tenure.

4.3 Wage premium to workers in low-skilled occupation from working in more innovative firms and its relationship to λ and tenure

Highly innovative firms hire fewer workers in low-skilled occupations. Table A9 in the Appendix shows that comparing the least to the most R&D intensive firm increases the share of workers in high-skilled occupations from 13.7% to 53.8%. Here we want to move the focus away from workers in high-skilled occupations and highlight workers in low-skilled occupations. Our aim is to assess whether there is a return to soft skills for such workers and whether this return increases the more R&D intensive is the firm.

Suppose the level of soft skills for individual *i* is represented by ψ_i . To allow for the value of soft skills to differ across firms depending on their R&D intensity we augment

Figure 6: Hourly wage and tenure against lambda for low-skilled occupation workers in innovative firms



Notes: This Figure reports the average log of hourly wage (left-hand side figure) and tenure in years (right-hand side figure) for workers in low-skilled occupations against the average level λ . Aggregates are done for 50 bins of equal size based on the value of λ . The sample is restricted to innovative firms.

wage equation (1) and write

$$ln(w_{ijkft}) = \beta_1 \tilde{R}_{ft} + \beta_2 f(A_i, T_{ift}, FT_{ift}, S_{ift}) + \gamma_i + \eta_t + \phi_j(R_{ft}, T_{ift}, \psi_i) + e_{ijkft}$$
(4)

where the new term $\phi_j(R_{ft}, T_{ift}, \psi_i)$ measures the return for worker *i* in occupation *j* with soft skills ψ_i , and with tenure *T* in firm of R&D intensity R_{ft} . As before *i* indexes individual, *j* occupation, *k* labor market, *f* firm and *t* years.

The dependence on tenure reflects the fact that soft skills are, by definition, not easily verifiable. The firm (and the worker) have to learn about them. Moreover, as emphasised in the theoretical discussion, this lack of easy verification places such workers in innovative firms in a stronger bargaining position, at least as their soft skills are revealed. Resulting in a premium for soft skills that increases for workers in innovative intensive firms as their soft skills are revealed and their bargaining position is enhanced. This is precisely what the term $\phi_i(R_{ft}, T_{ift}, \psi_i)$ is designed to capture.

In this framework with two dimensions of worker heterogeneity (γ_i and ψ_i) the γ_i term identifies the average of the unobserved component in the soft skills term for each worker over the period of observation. This leads to us underestimating the impact of soft-skills. We would like to instead to condition on the level of skills of the worker at entry into our sample period, rather than on an average worker effect. To account for this our preferred specification is one in which we replace γ_i by a measurement of the initial condition in the wage variable. This pre-sample measurement will reflect the worker's initial skill level and is not influenced by the evolution of the soft skills term during the observation period.

		(-)	(2)
Dependent variable: $ln(w_{ijkft})$	(1)	(2)	(3)
Tenure (years):	< 10 years	15	20
	0.045444	0.040/1////	0.045 th the
R&D firm	0.045***	0.048***	0.045***
	(0.003)	(0.003)	(0.004)
×med-lambda	0.016***	0.016***	0.021***
	(0.005)	(0.006)	(0.006)
×high-lambda	0.062***	0.046***	0.035***
	(0.008)	(0.010)	(0.012)
Tenure	0.021***	0.021***	0.013***
	(0.001)	(0.001)	(0.002)
Tenure Squared	-0.001***	-0.001***	0.001**
	(0.000)	(0.000)	(0.000)
Tenure \times med-lambda	-0.000	0.000	0.002
	(0.000)	(0.001)	(0.001)
Tenure \times high-lambda	0.005***	0.004***	0.001
-	(0.001)	(0.001)	(0.002)
R&D firm ×Tenure ×med-lambda	0.002**	0.002	-0.000
	(0.001)	(0.001)	(0.002)
R&D firm ×Tenure ×high-lambda	0.001	0.006***	0.012***
6	(0.001)	(0.002)	(0.004)
Tenure \times RDfirm	-0.000	-0.001	0.001
	(0.000)	(0.001)	(0.001)
Med lambda	0.059***	0.061***	0.061***
	(0.003)	(0.001)	(0.001)
High lambda	0.071***	0.079***	0.001)
Thigh fulliouu	(0.005)	(0.005)	(0.006)
Δge	0.013***	0.015***	0.016***
nge -	(0,000)	(0.013)	(0.001)
A ge Squared	0.000)	0.001)	0.001)
Age Squared	-0.000	-0.000	-0.000
Firm Size	0.010***	(0.000)	0.000)
1 IIIII Size	$-0.010^{-0.01}$	-0.010	-0.009***
Candan	(0.001)	(0.001)	(0.001)
Gender	(0.002^{+++})	(0.001^{+++})	$(0.03)^{+++}$
Eull Time	(0.002)	(0.002)	(0.002)
run-mne	0.093***	(0.002)	0.105***
F 'ad	(0.002)	(0.002)	(0.002)
First year wage	0.381***	0.334***	0.291***
	(0.009)	(0.009)	(0.008)
Fixed Effects			
Labour market	\checkmark	\checkmark	\checkmark
Year	\checkmark	\checkmark	\checkmark
R^2	0.445	0.394	0.345
Observations	301,100	253,348	185,556

Table 4: R&D and hourly wages low-skilled occupations

Notes: The dependent variable, log of wage, is defined in Appendix A.2.2. The main regressor, R&D firm, is a dummy variable equal to 1 if the firm is reporting any positive expenditure in R&D. Other covariates definitions are given in Table A7. Ordinary Least Square regression including travel to work area times year fixed effects. Heteroskedasticity robust standard errors clustered at the firm level are computed to indicate the level of significance: ***, ** and * for 0.01, 0.05 and 0.1 levels of significance.

Table 4 presents supporting evidence for our story. The columns relate to different sample based on tenure. The first column is for tenure < 10 years, then 15 and then 20. The three way interaction term, R&D firm ×Tenure ×high-lambda, shows that there is a wage premium to working in a more innovative firm for workers in low-skilled occupations, when these occupations are high lambda (suggesting it is driven by a complementarity). This is increasing in tenure, and more so in the earlier years.

Our model predicts that workers in low-skilled occupation should have longer tenure in more innovative firms, as more time and money is required to get them to the position where they can achieving their full potential. This is indeed what we see from Figure 7.



Figure 7: Tenure, by occupation and R&D intensity

Notes: Vertical axis shows the average of the number of year spent in the firm. Horizontal axis shows average value of R&D intensity for each quantile of R&D intensity of the firm, with 20 quantiles and an additional one indicating zero R&D as quantile 0. The bottom curve shows mean tenure for workers in low-skilled occupations and the top line for workers in high-skilled occupations (see section A.2.3). 95% confident intervals are included.

As suggested by the theoretical model, a firm may use on the job training to help reveal, and even develop, soft skills. Something that we also confirm below.

4.4 Training of workers in low-skilled occupations is higher in more R&D intensive firms

We find evidence in support of our prediction (Fact 4) that more innovative firms invest more in training their workes in low-skilled occupations. Unfortunately, we do not have direct information on the spending in training by the firms and we do not know if a worker was actually trained. We thus come back to our occupation level results, exploiting two additional questions about the duration of training on-site or on-the-job. Table 5 reports the share of workers that are in occupation associated with different level of training: none, up to 6 months, between 6 months and a year and more than a year. What Table 5 shows in columns 1 to 4 is that in the highest R&D intensive firms, from 14.3% to 16.2% of workers in low-skilled occupations report having received training for more than one year, whereas only 6.4% to 7.2% of workers in low-skilled occupations report having received training for more than one year in no-R&D firms.¹²

All these results are in line with the assumptions of our model, namely that: (i) workers in low-skilled occupations are dedicated to tasks that involve more complementarity with other tasks in more R&D intensive firms (in other words, we vindicate the link between λ and the firm's innovativeness); (ii) workers in low-skilled occupations in more R&D intensive firms have a higher need to develop firm-specific skills than they do in less R&D intensive firms and therefore they are in higher need to be trained (this is captured by the difference $q - q_L$ which increases with λ in our model).

¹²Columns 5 to 8 of Table 5 shows that this trend, that more innovative firms have a higher share of workers in occupations that are associated with longer training, is not driven by a size effect.

	Tercile of R&D intensity				
	None	Low	Middle	High	
	(1)	(2)	(3)	(4)	
On-site or in-plant					
None	20.4	20.1	18.6	18.4	
Up to 6 months	65.7	64.5	59.9	54.5	
6 months - 1 year	7.6	8.2	10.8	12.8	
A year or more	6.3	7.3	10.7	14.2	
On-the-job					
None	10.2	10.1	9.4	9.1	
Up to 6 months	74.9	73.1	66.3	60.0	
6 months - 1 year	7.8	8.7	12.4	14.8	
A year or more	7.1	8.2	11.9	16.1	

Table 5: On the job and on-site training for low skill occupations

Notes: R&D firms are split in three groups of equal size based on the value of their R&D expenditure per employee. Data are taken from O*NET and report the share of workers in low-skilled occupations reporting having been trained for different durations whether on-site or on-the job.

4.5 Outsourcing

Our model predicts that more innovative firms tend to outsource a higher fraction of tasks than less innovative firms, in particular those tasks with lower complementarity (associated with a small λ in the model). The previous results using O*Net data have already shown that innovative firms put more weight in low-skilled occupations that are associated with longer training and larger consequences in case of error. Unfortunately, it is not easy to directly measure outsourcing in our data for at least two reasons. First because outsourced workers do not necessary appear in the ASHE data, and even if they do, they won't be link to the firm that use their service. Second because we conjecture that most of the outsourcing occurred before 2004, which prevent us from following workers in low-skilled occupations that are outsourced from innovative firms as in Goldschmidt and Schmieder (2017). We therefore proceed indirectly.

We start from the idea that all firms need the same share of cleaners which can be arguably seen as a low λ task. The only reason this share is lower than average in more innovative firms is because of the outsourcing of cleaners by those firms. In Figure 8, we plot the share of cleaners among all workers in low-skilled occupations against R&D intensity in the left-hand side panel and against total employment in the right-hand side

panel. This graph clearly shows that innovative firms outsource more their cleaners than non innovative firms, and here again, this is not a size effect.



Figure 8: Share of workers in low-skilled occupations that are cleaners

Notes: The y-axis shows the share of cleaners over the total number of workers in low-skilled occupations. The x-axis shows the average value of R&D intensity for each quantile of R&D intensity of the firm, with 20 quantiles and an additional one indicating zero R&D as quantile 0 (left-hand side panel) and the average value of employment for each quantile of employment of the firm with 20 quantiles (right-hand side panel).

4.6 Robustness

In this section we show that our main results are robust to a number of potential robustness concerns. First, we show that our results are robust to including firm effects, as in AKM. Second, we show that the relationship between wages and R&D is not driven by firm size. Third, we show that bonus income and other measures of wages do not drive our results. Four, we show that alternative functions of R&D yield qualitatively similar results. Finally, we check robustness to firms with exceptionally high R&D and also to different definitions of skill level.

4.6.1 R&D and firm effect

In our main analysis we did not control for potential unobservable firm factors. In Table 6 we include firm effect. R&D remains positive and statistically significant. Here identification comes off changes in wages in firms that increase or decrease their R&D intensity. The full impact of R&D here is the coefficient on R&D plus the effect of R&D on the firm effect. We obtain an estimate of this from an auxiliary regression. We recover the firm fixed effect from the estimates in column (3) and regress this on R&D intensity and a year

Table 6: Relationship between wages and R&D intensity						
	Deper	dent variable: <i>ln</i> ((w_{ijkft})			
	(1)	(2)	(3)			
ln R&D int	0.006***	0.001***	0.001***			
Age Squared	-0.001***	-0.001***	-0.000***			
Tenure	0.008***	0.015***	0.008***			
Tenure Squared	-0.000***	-0.000***	-0.000***			
Firm Size	-0.008***	-0.031***	-0.001			
Full-Time	0.004	0.142***	-0.023***			
Age	(0.003)	0.045***	(0.002)			
Gender		0.155***				
		(0.005)				
Fixed Effects						
Individual	\checkmark		\checkmark			
Firm Year	\checkmark	\checkmark	\checkmark			
R^2	0.887	0.561	0.895			

fixed effect. The estimated coefficient, estimated over 37000 observations, is 0.0153 with standard error 0.00034.

Notes: 626,206 observations. The dependent variable is log of wage which is defined in Appendix A.2.2. $\tilde{R}_{ft} = ln(1 + R_{ft})$. Other covariates definitions are given in Table A7. Column 1 replicates column 3 in Table **??** and includes year and individual effects. Column 2 includes firm and year effects. Column 3 includes worker, firm and year effects. Heteroskedasticity robust standard errors clustered at the firm level (column 1) or individual levels (columns 2 and 3) are reported in parenthesis. ***, ** and * respectively indicate 0.01, 0.05 and 0.1 levels of significance.

We recover the estimate firm and individual fixed effects using the estimates in column (3) of Table 6. Figure 9 shows that they are positively correlated for workers in low-skilled occupations. Each dot in the graph is the mean effect in the relevant centiles (we split firms into 100 bins of equal size, with around 66 observations per bins) and take the average of worker fixed effects within each bin.



Figure 9: Correlation between firm and individual effects, by skill

Notes: The x-axis shows the average firm fixed effect in each centile. The y-axis shows the average individual fixed effect in each centile. Centiles are 100 equal sized bins by firm fixed effect.

These estimates suffer from a potential incidental parameter bias. We can use the Jacknife method of Dhaene and Jochmans (2015). The estimator is based on split-sample estimation where, within each firm, the stayers and movers (out of the firm) are split into two random subsamples of equal sizes. The bias-corrected estimate is equal to two times the full-sample estimate minus twice the mean of the two split-sample estimates. We then compare the coefficient with the one obtained with the whole sample.

With one draw, the corrected coefficient of innovation is 0.0010115 which we can compare with 0.0011998, the coefficient of the model with all the data. In terms of predictive effect of innovation, comparing the predicted wage with this model for the maximum value of innovation versus the smallest value, we get a 1.36% increase with the corrected coefficient and a 1.61% with the uncorrected coefficient. Note that this is only the direct effect of innovation to which we need to add the indirect effect through the fixed effect.

Figure 10 compares the firm fixed effects, first between the two subsamples and then by comparing the corrected fixed effect and the uncorrected.





Notes: Panel (a) shows the estimated firm fixed effects from two independent samples of the data. Panel (b) shows the uncorrected fixed effect estimated from column (3) of Table 6 with the corrected fixed effect.

4.6.2 Firm size

Our empirical results estimate a negative elasticity of wage with respect to the size of the firm. However, the fact that larger firms pay higher wage is a well established fact in the labour literature (see among other Oi and Idson, 1999). This negative effect actually stems from the fact that we are focusing on large firms while the premium from working in a firm with more employees is essentially captured by relatively small firms as shown in Figure 11. Moreover, in Table 10 that we discuss further below, we see that when we estimate the effect of R&D on wage, using the whole ASHE sample (that is, without restricting to large firms), we find a positive and significant coefficient of the logarithm of total employment on wage.





Notes: Vertical axis shows the average of the logarithm of hourly wage by firm. Horizontal axis shows the average value of employment for each quantile of employment of the firm, with 20 quantiles. The left-hand side panel considers all firms that are in ASHE whereas the right-hand side panel only considers firms over 400 employees and corresponds to our final sample.

4.6.3 Bonus income and other measures of wage or income

A first concern is that high-skilled workers may receive a large part of their wage in the form of lump-sum bonuses at the end of the year and that these bonuses are not well captured by measures of weekly wages. This would particularly be an issue if workers in high-skilled occupations receive larger bonuses in more R&D intensive firms. In Table 7 we show that using average annual wages instead of average weekly wages and including or excluding incentive payments does not affect our results.

More generally, how are our results affected by the definition of income that we use? In our baseline results, we have chosen to use the wages measured in the week that the survey is collected. As explained in Appendix A.2.2, the numerator includes a fixed salary and additional variable earnings (incentive, overtime and other pay). Here, we test the sensitivity to our main result to using other measures of wages. Results are presented in Table 7 when the usual set of control variables are included and individual and year fixed effects are added. Column 1 uses the baseline measure (logarithm of total earning per hours) as a reference. Column 2 uses the same measure but restricting to fixed salary and excluding overtime. Column 3 uses the total weekly earnings and column 4 and 5 use total annual earnings including (resp. excluding) bonuses. One concern with our results is that high-skilled occupation workers receive most of their earnings from incentive paid at the end of the year and hence not well captured by our baseline measure of wages (based

on a standard week in April). This could potentially drive our result if in turns, highskilled occupation workers receive a larger share of their earnings as incentive in innovative firms. In fact, the average share of bonus in annual earnings is 8.8% for non R&D firms against 6.5% for non R&D firms. Finally, comparing column 4 and 5 of Table 7 shows no substantial differences when bonus are included or excluded.

	Dependent variable: $ln(w_{ijkft})$					
Income	Total hourly	Fixed hourly	Total pay	Fixed pay		
	pay	pay	(Inc.			
	(1)	(2)	(3)	(4)		
-						
$ln(R_{ft}+1)$	0.002***	0.002***	0.006***	0.005***		
	(0.001)	(0.001)	(0.001)	(0.001)		
\times med skill	0.002***	0.002**	0.001	0.000		
	(0.001)	(0.001)	(0.002)	(0.002)		
\times low-skill	0.006***	0.005***	0.011***	0.011***		
	(0.001)	(0.001)	(0.002)	(0.002)		
Age Sq.	-0.001***	-0.001***	-0.001***	-0.001***		
	(0.000)	(0.000)	(0.000)	(0.000)		
Tenure	0.007***	0.006***	0.068***	0.066***		
	(0.000)	(0.000)	(0.003)	(0.003)		
Tenure Squared	-0.000***	-0.000***	-0.002***	-0.002***		
-	(0.000)	(0.000)	(0.000)	(0.000)		
Firm Size	-0.006***	-0.009***	-0.024***	-0.022***		
	(0.002)	(0.001)	(0.005)	(0.005)		
Full-Time	-0.004	0.009	0.493***	0.489***		
	(0.005)	(0.006)	(0.014)	(0.014)		
low-skill	-0.157***	-0.151***	-0.194***	-0.189***		
	(0.006)	(0.006)	(0.010)	(0.010)		
med-skill	-0.073***	-0.070***	-0.060***	-0.059***		
	(0.004)	(0.004)	(0.008)	(0.008)		
			. ,			
Fixed Effects						
Individual	\checkmark	\checkmark	\checkmark	\checkmark		
Year	\checkmark	\checkmark	\checkmark	\checkmark		
R ²	0.889	0.908	0.796	0.785		

Table 7: Robustness to using different measures of wages

Notes: 626,210 observations. This table is similar to the last column of Table **??** but uses different measures of wages to construct the dependent variable. Column 1 uses the logarithm of total hourly earnings, column 2 uses the logarithm of the basic (fixed) hourly wages, column 3 uses the logarithm of the total weekly earning and column 4 uses the logarithm of annual gross earnings. Control variables definition and construction are given in Table A7. Ordinary Least Square regression including additive individual and year fixed effects. Heteroskedasticity robust standard errors clustered at the firm level are computed to indicate the level of significance: ***, ** and * for 0.01, 0.05 and 0.1 levels of significance.

	Dependent variable: $ln(w_{ijkft})$							
R&D function	$\frac{x}{l}$ (1)	$log(1 + \frac{x}{l})$ (2)	$ \begin{array}{c} H(x) \\ (3) \end{array} $	$ H\left(\frac{x}{l}\right) $ (4)	log(1+x)(5)	x > 0 (6)	<i>x</i> (7)	$log(\frac{x}{l})$ (8)
R&D intensity	0.000**	0.002***	0.001**	0.013***	0.001*	0.006	0.019	0.002
\times med skill	0.000*	0.002***	0.001**	0.010***	0.001**	0.011**	0.020**	0.002 (0.001)
\times low-skill	0.001*	0.006***	0.003***	0.024***	0.002***	0.026***	0.072**	0.005***
Age Sq.	-0.001***	-0.001***	-0.001***	-0.001***	-0.001***	-0.001***	-0.001***	-0.001***
Tenure	0.008***	0.007***	0.007***	0.007***	0.007***	0.007***	0.008***	0.005***
Tenure Squared	-0.000***	-0.000***	-0.000***	-0.000***	-0.000***	-0.000***	-0.000***	-0.000***
Firm Size	-0.006*** (0.002)	-0.006*** (0.002)	-0.007*** (0.002)	-0.006*** (0.002)	-0.007*** (0.002)	-0.007*** (0.002)	-0.006*** (0.002)	-0.002 (0.004)
Full-Time	-0.003 (0.005)	-0.004 (0.005)	-0.004 (0.005)	-0.004 (0.005)	-0.004 (0.005)	-0.003 (0.005)	-0.003 (0.005)	-0.080*** (0.023)
low-skill	-0.147*** (0.006)	-0.157*** (0.006)	-0.154*** (0.006)	-0.156*** (0.006)	-0.153*** (0.006)	-0.152*** (0.006)	-0.147*** (0.006)	-0.067*** (0.007)
med-skill	-0.067*** (0.004)	-0.073*** (0.004)	-0.071*** (0.004)	-0.073*** (0.004)	-0.071*** (0.004)	-0.070*** (0.004)	-0.067*** (0.004)	-0.038*** (0.005)
Fixed Effects								
Individual	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark
Year	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark
R ²	0.889	0.889	0.889	0.889	0.889	0.889	0.889	0.917
Observations	626,210	626,210	626,210	626,210	626,210	626,210	626,210	162,696

Table 8: Testing different function of R&D

Notes: This table presents the coefficient on the function of R&D intensity when estimating the same model as in the last column of Table ?? but replacing the log of R&D per employee by alternative functions of this variable. Each line corresponds to a different functional form. Hyperbolic function is $H(x) = ln(x + \sqrt{x^2} + 1)$. Ordinary Least Square regression including additive individual and year fixed effects. Ordinary Least Square regression including additive individual and year fixed effects. Heteroskedasticity robust standard errors clustered at the firm level are computed to indicate the level of significance: ***, ** and * for 0.01, 0.05 and 0.1 levels of significance.

4.6.4 Different functions of R&D

Here we show that our main results hold using alternative function of R&D. Our baseline results use the logarithm of total R&D expenditure divided by total employment in the firm. Figure 2 shows that the relationship between the log of hourly wage and this function of R&D seems to be close to linear. Nevertheless, in this section, we see that our results hold when we consider different functional form of R&D, that can give different weight to different level of R&D intensity. Hence, in Table 8, we successively consider: $\frac{R&D}{L}$, $ln(1 + \frac{R&D}{L})$, an hyperbolic function with R&D and with R&D per employee, ln(1 + R&D), R&D > 0 and R&D > 0. In each case, the coefficient is positive and significant in the case of low-skilled occupation workers consistently with our baseline model that is shown again in column 2.

Next, to allow for even more flexibility, we let the coefficient adjust at different point in the R&D distribution. To do so, we include a binary variable for each of the twenty quantile of R&D:

$$ln(w_{ijkft}) = x'_{ift}\beta_1 + z'_{ft}\beta_2 + \sum_{l=1}^{20}\beta_{3l}R_{ftl} + \nu_i + \nu_t + \epsilon_{it}$$
(5)

Where R_{ftl} is equal to 1 if firm f belongs to quantile l in year t. The resulting estimated coefficients β_{3l} on each of these binary variables are presented in Table 9, where the reference is the group of firm with no R&D. We see that the coefficients are positive and increase with the quantile of R&D for low skill occupations (column 1), is positive and significant for the highest quantiles in the case of intermediate skill occupations (column 2) and never significant in the case of high skill occupations (column 3). Column 4 shows that overall, innovation is associated with higher wages for most quantiles.

4.6.5 Other measures of innovation

Our results are therefore robust to considering different functional form of R&D, but what happens when we change the definition of R&D expenditures? Table 10 shows how our results are affected compared to our baseline definition that use both intramural and extramural R&D expenditures (the baseline specification is reported in column 1). We hence estimate equation (4), allowing the coefficient on R&D and the intercept to vary across skill categories, and using different proxies for the intensity of R&D: first using only intramural R&D (column 2), then using only extramural (column 3) and then using the number of workers directly involve in R&D activities that we directly take from BERD (column 4). Results are consistent with our baseline model, that is, the effect is always stronger and significant for low-skilled occupation workers. Finally, we measure R&D as the share of workers that correspond to a skill category 6 (PhD level scientific occupations, see Appendix A.2.3). This measures does not require any information from the BERD database and allows us to relax the restriction to firms of more than 400 employees. The results presented in column 5 is, here again, consistent with our baseline model.

4.6.6 Other robustness

We conclude by performing two additional robustness checks. First, as seen in Table A1 in Appendix A, firms from the highest quantile of R&D are very different from others. We thus check that our results are not mainly driven by these firms by removing observa-

	Dependent variable: $ln(w_{ijkft})$					
Skill Category	Low	Intermediate	High	All		
	(1)	(2)	(3)	(4)		
Quantile 1	0.004	-0.001	0.001	0.004		
Quantile 2	0.017**	0.003	-0.007	0.010		
Quantile 3	0.006	0.003	-0.001	0.002		
Quantile 4	0.031***	-0.018	-0.008	0.012*		
Quantile 5	0.036**	0.010	-0.000	0.023***		
Quantile 6	0.036***	0.012	0.011	0.027***		
Quantile 7	0.037***	0.009	-0.008	0.025***		
Quantile 8	0.039***	0.014	0.000	0.031***		
Quantile 9	0.044***	0.021*	-0.007	0.035***		
Quantile 10	0.048***	0.021	-0.001	0.038***		
Quantile 11	0.065***	0.029*	-0.006	0.053***		
Quantile 12	0.070***	0.046***	-0.003	0.056***		
Quantile 13	0.073***	0.029**	-0.013	0.051***		
Quantile 14	0.073***	0.035***	0.012	0.064***		
Quantile 15	0.061***	0.035***	0.012	0.064***		
Quantile 16	0.096***	0.048***	-0.011	0.081***		
Quantile 17	0.085***	0.022*	-0.003	0.071***		
Quantile 18	0.090***	0.043***	0.007	0.082***		
Quantile 19	0.114***	0.028**	-0.013	0.077***		
Quantile 20	0.147***	0.020	-0.001	0.099***		
Fixed Effects						
Individual	\checkmark	\checkmark	\checkmark	\checkmark		
Year	\checkmark	\checkmark	\checkmark	\checkmark		
R ²	0.774	0.851	0.885	0.887		
Observations	407,341	104,318	114,535	626,210		

Table 9: 20 quantiles of R&D based on level of total R&D expenditures

Notes: This table presents the coefficient on each of the 20 quantiles of total R&D expenditure when estimating equation 5. The usual set of control variables are included but not reported. Ordinary Least Square regression including additive individual and year fixed effects. Heteroskedasticity robust standard errors clustered at the firm level are computed (but not reported) to indicate the level of significance: ***, ** and * for 0.01, 0.05 and 0.1 levels of significance.

	Dependent variable: $ln(w_{ijkft})$						
Measure of R&D	Baseline (1)	Only Intramural (2)	Only Extramural (3)	R&D workers (4)	Scientists (5)		
ln R&D int	0.002***	0.002***	-0.000	0.009***	0.012		
	(0.001)	(0.001)	(0.001)	(0.002)	(0.009)		
\times med skill	0.002***	0.002***	0.004***	0.002**	0.055***		
	(0.001)	(0.001)	(0.001)	(0.001)	(0.019)		
* low-skill	0.006***	0.006***	0.008***	0.005***	0.151***		
	(0.001)	(0.001)	(0.001)	(0.001)	(0.020)		
Age Sq.	-0.001***	-0.001***	-0.001***	-0.001***	-0.001***		
	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)		
Tenure	0.007***	0.007***	0.007***	0.007***	0.011***		
	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)		
Tenure Squared	-0.000***	-0.000***	-0.000***	-0.000***	-0.000***		
	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)		
Firm Size	-0.006***	-0.006***	-0.006***	-0.006***	0.007***		
	(0.002)	(0.002)	(0.002)	(0.002)	(0.001)		
Full-Time	-0.004	-0.004	-0.004	-0.004	-0.005		
	(0.005)	(0.005)	(0.005)	(0.005)	(0.003)		
low-skill	-0.157***	-0.157***	-0.162***	-0.155***	-0.196***		
	(0.006)	(0.006)	(0.006)	(0.006)	(0.004)		
med-skill	-0.073***	-0.073***	-0.077***	-0.071***	-0.098***		
	(0.004)	(0.004)	(0.004)	(0.004)	(0.003)		
Fixed Effects							
Individual	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark		
Year	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark		
R^2	0.889	0.889	0.889	0.889	0.854		
Observations	626,210	626,210	626,210	626,210	1,815,722		

Table 10: Robustness to using different measures of R&D.

Notes: This table presents results from estimating the same model as in the last column of Table ?? but using different measure for R&D. Column 1 uses total R&D expenditures per number of employees, column 2 and 3 uses respectively intramural and extramural R&D expenditures per number of employees, column 4 uses the share of workers involved in R&D activities taken from BERD and Column 5 uses the share of workers in occupation skill category 6 using the whole ASHE database. All these measures are transformed with a function ln(1 + x). Control variables definition and construction are given in Table A7. Ordinary Least Square regression including additive individual and year fixed effects. Heteroskedasticity robust standard errors clustered at the firm level are computed to indicate the level of significance: ***, ** and * for 0.01, 0.05 and 0.1 levels of significance.

tions associated with total R&D expenditures higher than 293,634,000 pounds. Results are shown in Table 11.

Second, we test the robustness of our results regarding the different effects of R&D on wages by skill to using an alternative definition of skill level as defined in Appendix A.2.3. Results are robust in the sense that there is no effect of R&D expenditures on wages for high occupation workers as presented in Table 12 where each column corresponds to a different skill level (1 for the lowest and 4 for the highest).

	Dependent variable: $ln(w_{ijkft})$							
Skill Category	Low (1)	Intermediate (2)	High (3)	All (4)				
ln R&D int × med skill	0.007*** (0.001)	0.003*** (0.001)	-0.000 (0.001)	0.002*** (0.001) 0.002*** (0.001)				
\times low-skill				0.006***				
Age Sq.	-0.000***	-0.001***	-0.001***	-0.001***				
Tenure	0.009***	0.006***	(0.000) (0.000) (0.001)	0.007***				
Tenure Squared	-0.000***	-0.000***	(0.001) 0.000 (0.000)	-0.000***				
Firm Size	-0.005**	0.002	(0.000) 0.003 (0.003)	-0.006***				
Full-Time	-0.011*	-0.089***	-0.111*** (0.014)	(0.002) -0.004 (0.005)				
low-skill	(0.000)	(0.015)	(0.014)	-0.157***				
med-skill				-0.073*** (0.004)				
Fixed Effects								
Individual Year	\checkmark	\checkmark	\checkmark	\checkmark				
R^2	0.771	0.850	0.885	0.888				
Observations	405,331	102,733	110,444	618,524				

Table 11: Robustness: Removing firms from the highest quantile of R&D expenditures.

Notes: This table shows results from estimating the same model as in Table **??** but removing firms belonging to the highest quantile (out of 20) in terms of R&D intensity. Ordinary Least Square regression including additive individual and year fixed effects. Heteroskedasticity robust standard errors clustered at the firm level are computed to indicate the level of significance: *******, ****** and ***** for 0.01, 0.05 and 0.1 levels of significance.

	Dependent variable: $ln(w_{ijkft})$						
Skill Category	1 (low) (1)	2 (2)	3 (3)	4 (high) (4)	All (5)		
ln R&D int	0.005*** (0.001)	0.007*** (0.001)	0.002** (0.001)	-0.000 (0.001)	0.003*** (0.001)		
imes med-high skill					0.002**		
× med-low skill					(0.001) 0.005^{***} (0.001)		
\times low-skill					0.004*** (0.001)		
Age Sq.	-0.000*** (0.000)	-0.000*** (0.000)	-0.001*** (0.000)	-0.001*** (0.000)	-0.001*** (0.000)		
Tenure	0.007*** (0.001)	0.009*** (0.001)	0.004*** (0.001)	0.002*** (0.001)	0.007*** (0.000)		
Tenure Squared	-0.000*** (0.000)	-0.000*** (0.000)	-0.000*** (0.000)	-0.000 (0.000)	-0.000*** (0.000)		
Firm Size	0.003 (0.003)	-0.007*** (0.003)	0.000 (0.002)	0.004 (0.003)	-0.006*** (0.002)		
Full-Time	-0.038*** (0.006)	-0.014** (0.007)	-0.115*** (0.014)	-0.110*** (0.014)	-0.006 (0.005) -0.170*** (0.006)		
med-low-skill					-0.143***		
med-high-skill					(0.006) -0.049*** (0.004)		
R^2	0.706	0.782	0.872	0.901	0.889		
Observations	103,136	293,543	113,802	115,729	626,210		

Table 12: Robustness: Alternative measure of skill

Notes: This table shows results from estimating the same model as in Table **??** but defined skill level of occupations differently. Ordinary Least Square regression including additive individual and year fixed effects. Heteroskedasticity robust standard errors clustered at the firm level are computed to indicate the level of significance: *******, ****** and ***** for 0.01, 0.05 and 0.1 levels of significance.

5 Summary and conclusion

In this paper we used matched employee-employer data from the UK that we augment with information on R&D expenditures, to analyze the relationship between innovation and between-firm inequality. Our first finding is that more R&D intensive firms pay higher wages on average. Our second finding is that workers in low-skilled occupations benefit more from working in more R&D intensive firms than workers in high-skilled occupations.

To account for these findings, we developed a simple model of the firm where the complementarity between employees in "high-skilled occupation" and "low-skilled occupation" within the firm increases with the firm's degree of innovativeness. An additional prediction of the model, which we also confronted to the data, is that workers in low-skilled occupations stay longer in more innovative firms.

Our analysis can be extended in several directions. One would be to look at whether, as our model predicts, the (low-skilled) occupations that yield more return to innovativeness (i.e. for which wage increases more with innovativeness) are more "relational". A second idea is to further explore whether more innovative firms provide more training to workers in low-skilled occupations. Third, our model predicts that our main effect (namely that workers in low-skilled occupations benefit more from working in a more innovative firm) is stronger in more competitive sectors or in areas where potential replacements for incumbent workers in low-skilled occupations are of lower quality: these predictions can be tested using our data. Fourth, we used R&D investment as our measure of innovativeness, and one could use other measures such as patenting.

Finally, one may want to look at subgroups of agents within the high- and low-skilled occupation categories. In particular we should look at whether the premium to working in a more innovative firm, is not larger at the very top end of the occupation distribution. One first place to look at, are CEOs, taking into account their total revenues (wage income plus capital income). These and other extensions of the analysis in this paper await further research.

References

- Abowd, J. M., F. Kramarz, and D. N. Margolis (1999, March). High Wage Workers and High Wage Firms. *Econometrica* 67(2), 251–334.
- Acemoglu, D. (2002, mar). Technical change, inequality, and the labor market. *Journal of Economic Literature* 40(1), 7–72.
- Acemoglu, D. and D. H. Autor (2011). Skills, tasks and technologies: Implications for employment and earnings. In *Handbook of Labor Economics*, Number 4 in Orley Ashenfelter and David E. Card (eds.),, pp. 1043–1171. Amsterdam: Elsevier.
- Aghion, P., U. Akcigit, A. Bergeaud, R. Blundell, and D. Hémous (2018). Innovation and top income inequality. Forthcoming.
- Aghion, P., U. Akcigit, A. Hyytinen, and O. Toivanen (2018). On the returns to invention within firms: Evidence from Finland. Forthocoming, AEA Papers and Proceedings.
- Aghion, P. and P. Howitt (1992, March). A Model of Growth through Creative Destruction. *Econometrica* 60(2), 323–351.
- Akcigit, U., J. Grigsby, and T. Nicholas (2017, feb). Immigration and the rise of american ingenuity. Technical report.
- Akerman, A., I. Gaarder, and M. Mogstad (2015). The skill complementarity of broadband internet. *The Quarterly Journal of Economics* 130(4), 1781–1824.
- Barth, E., A. Bryson, J. C. Davis, and R. Freeman (2016). It's where you work: Increases in the dispersion of earnings across establishments and individuals in the united states. *Journal of Labor Economics* 34(S2), S67–S97.
- Bell, B. D. and J. Van Reenen (2013, May). Extreme Wage Inequality: Pay at the Very Top. *American Economic Review 103*(3), 153–57.
- Bell, B. D. and J. Van Reenen (2014, 02). Bankers and Their Bonuses. *Economic Journal* 124(574), F1–F21.
- Cahuc, P., F. Postel-Vinay, and J.-M. Robin (2006). Wage bargaining with on-the-job search: Theory and evidence. *Econometrica* 74(2), 323–364.
- Card, D., A. R. Cardoso, J. Heining, and P. Kline (2016, November). Firms and Labor Market Inequality: Evidence and Some Theory. NBER Working Papers 22850, National Bureau of Economic Research, Inc.
- Dunne, T., L. Foster, H. Haltiwanger, and K. Troske (2004). Wage and Productivity Disperion in United States Manufacturing: The Role of Computer Investment. *Journal of Labor Economics* 22(2), 397–429.
- Elias, P. and K. Purcell (2004). SOC (HE): A classification of occupations for studying the graduate labour market. Research Paper 6, Research Graduate Careers Seven Years On.

- Elias, P. and K. Purcell (2013). Classifying graduate occupation for the knowledge society. FutureTrack Working Paper 5.
- Garicano, L. (2000, October). Hierarchies and the Organization of Knowledge in Production. *Journal of Political Economy* 108(5), 874–904.
- Garicano, L. and E. Rossi-Hansberg (2006). Organization and inequality in a knowledge economy. *The Quarterly Journal of Economics* 121(4), 1383–1435.
- Gibbons, R. and L. Katz (1992). Does unmeasured ability explain inter-industry wage differentials? *The Review of Economic Studies* 59(3), 515–535.
- Goldin, C. and L. F. Katz (2010). *The Race between Education and Technology*. Belknap Press.
- Goldschmidt, D. and J. F. Schmieder (2017). The rise of domestic outsourcing and the evolution of the german wage structure. *The Quarterly Journal of Economics*, qjx008.
- Groshen, E. L. (1991). Sources of intra-industry wage dispersion: How much do employers matter? *The Quarterly Journal of Economics 106*(3), 869–884.
- Kline, P., N. Petkova, H. Williams, and O. Zidar (2017). Who profits from patents? rentsharing at innovative firms.
- Kremer, M. (1993). The o-ring theory of economic development. *The Quarterly Journal* of *Economics 108*(3), 551–575.
- Kremer, M. and E. Maskin (1996, August). Wage inequality and segregation by skill. Working Paper 5718, National Bureau of Economic Research.
- Krusell, P., L. E. Ohanian, J.-V. Ríos-Rull, and G. L. Violante (2000). Capital-skill complementarity and inequality: A macroeconomic analysis. *Econometrica* 68(5), 1029–1053.
- Office for National Statistics (2016a). Annual survey of hours and earnings, 1997-2015: Secure access. 8th edition. Technical Report SN:6689, UK Data Service.
- Office for National Statistics (2016b). Business expenditure on research and development, 1994-2014: Secure access. 5th edition. Technical Report SN:6690, UK Data Service.
- Oi, W. Y. and T. L. Idson (1999). Firm size and wages. *Handbook of labor economics 3*, 2165–2214.
- Romer, P. M. (1990, October). Endogenous Technological Change. Journal of Political Economy 98(5), 71–102.
- Song, J., D. J. Price, F. Guvenen, N. Bloom, and T. v. Wachter (2015). Firming up inequality.
- Stole, L. and J. Zwiebel (1996). Intra-firm bargaining under non-binding contracts. *Review* of *Economic Studies* 63(3), 375–410.

Van Reenen, J. (1996). The creation and capture of rents: Wages and innovation in a panel of u. k. companies. *The Quarterly Journal of Economics* 111(1), 195–226.

A Data construction and additional description

This appendix describes the construction of our main sample which results from the merge of two datasets provided by the ONS: the Annual Survey of Hours and Earnings (ASHE) and the Business Expenditures on Research and Development (BERD).

A.1 Business Expenditures on Research and Development

The Business Expenditures on Research and Development (BERD, Office for National Statistics, 2016b) is an annual survey conducted by the Office of National Statistics (ONS) that collects information on R&D activities of businesses in the United Kingdom. It is a stratified random sample from the population of firms that conduct R&D. The selected firms then receive a form asking them to detail their innovative activities in accordance to the OECD's Frascati Manual guidelines. The stratification scheme has changed over time, but includes a census of firms with over 400 employees. These are the firms we are interested in. The BERD data is available from 1994-2014 with a coverage that is consistent since 2000.

BERD records expenditure at the level of the firm, the product that the R&D is related to, and the establishment carrying out the R&D. We also know whether R&D was carried out in house (intramural) or outsourced (extramural). Product is recorded at the level of 33 categories. We know the split between civil and defense. More than 99% of the sampled firms report R&D for only one product, representing 75% of total intramural expenditures and 69% of extramural expenditures. 88.2% of intramural R&D expenditure and 96.5% of extramural R&D is civilian; 10% of firms that report doing some R&D do at least some defense R&D. Total R&D expenditures are the sum of intramural and extramural R&D at the firm level. In the paper, we refer to the level of R&D "R&D expenditures" and the level of R&D divided by the number of employees in the firm as "R&D intensity". Including extramural R&D is important as many large firms outsource a large part of their R&D activities, see Figure A1, and this varies across industries.



Figure A1: Share of total R&D expenditures that is outsourced (extramural) against R&D intensity.

Notes: Source: BERD. R&D intensity is defined as the logarithm of total R&D expenditures divided by employment. Dashed lines correspond to the upper and lower bound of a 95% confident interval.

Table A1 reports the average amount of intramural and extramural R&D across 20 quantiles of the distribution of total R&D intensity.¹³ The distributions of both intra and extramural R&D are highly skewed, in particular, firms in the highest vintile are very different from others.

¹³Quantiles of R&D are computed each year, so firms can move across quantiles.

Quantile of R&D	Employment	Intramural R&D	Extramural R&D	Number of firm-years
0 (no R&D)	2,365	0	0	29,848
1	8,337	76	5	434
2	4,634	233	14	427
3	3,129	298	22	426
4	2,775	382	62	429
5	2,890	653	80	427
6	1,702	541	56	427
7	1,916	808	66	427
8	1,761	1,038	88	427
9	1,344	1,019	110	427
10	1,700	1,618	211	426
11	1,732	2,138	293	431
12	1,958	3,177	557	427
13	1,625	3,486	417	427
14	1,439	4,345	390	428
15	1,627	6,793	488	424
16	2,499	16,306	799	429
17	2,635	24,618	1,358	429
18	2,290	34,882	2,891	426
19	2,480	62,946	10,027	427
20	2,282	140,744	81,145	422

Table A1: Distribution of employment and R&D

Notes: This table presents the average number of employees, average expenditures in intramural R&D (in thousand pounds) and average expenditures in extramural R&D (in thousand pounds) for 20 quantiles of R&D intensity (defined as the sum of intramural and extramural R&D expenditures per employee). The first categories "0 (no R&D)" corresponds to firm that do not report R&D in the current year. Quantiles of R&D are computed each year on the sample of firms that have been matched to ASHE and that contains more than 400 employees (see subsection A.4).

Our measure of R&D intensity is the logarithm of total R&D expenditure (including both intramural and extramural R&D) divided by the number of employee in the firm. R&D expenditure, as well as total employment, are defined at the firm level. In practice, we use $ln(1 + R_{ft})$, where R_{ft} is the ratio of total R&D expenditure over total employment, to accommodate values of 0 in firms that do not do any R&D; it is almost always equal to $ln(R_{ft})$ given the magnitude of R&D expenditure, so we can interpret β_3 as the elasticity of wage with respect to R&D intensity.

A.2 Annual Survey on Hours and Earnings (ASHE)

The Annual Survey of Hours and Earning (ASHE, Office for National Statistics, 2016a) is a 1% random sample of the UK workforce based on the last two digits of the national insurance numbers. We use data from 2004 to 2015.¹⁴ The level of observation in ASHE is

¹⁴There is a discontinuity in ASHE in 2004.

the individual job, however, over 98% of individuals have only one job at any point in time, so appear only once per year in the dataset. We have a total of over 1,850,000 observations on around 340,000 individuals working in around 158,000 enterprises.¹⁵

A.2.1 Cleaning

We clean the data and remove observations: with a missing individual identifier (variable *piden*), with a missing firm identifier (variable *entref*) or those not coded with an adult rate marker (variable *adr*), which mostly involves removing trainees from the sample. We keep only the main job for each individual. This cleaning removes 4.2% of observations. The version of ASHE we use is a panel where individuals are uniquely identified by their (transformed) national insurance number. However, a problem occurs with temporary national insurance number that are reused for different people. We drop all individuals that change gender or change birth dates: 1.2% of observations are affected and dropped. We delete individuals where the data are clearly miscoded, e.g. their age that is less than their tenure in the firm, and we drop individuals aged less than 18 or older than 64 (around 2% of total observations). The outcome of this cleaning is a database of more than 1,650,000 observations on around 320,000 individuals working in 140,000 enterprises. We call this database "Clean ASHE".

A.2.2 Wages

There are various measures of wages in ASHE. Gross weekly wage is collected during the survey period (from one to four weeks) in April of each year. This is reported by the employer and is considered to be very accurate. The gross weekly wage can be broken down into basic pay, incentive pay, overtime pay, additional premium payment for shifts that are not considered overtime and additional pay for other reasons. The gross weekly wage does not include any capital income such as stock-options (reported "incentive pay" includes profit sharing, productivity, performance and other bonus or incentive pay, piecework and commission.). The number of hours worked are reported, split between overtime and basic paid hours. ASHE also provides data on gross annual earnings, as well as the share of this earning that is an incentive payment.

We define hourly wages as the ratio of gross weekly wage divided by total number of paid hours (including overtimes). This is the measure of wage we will consider as a baseline but we also show descriptive statistics for gross annual earnings. Including other types of

¹⁵An enterprise can be a private corporation, public company, government agency, non profit organisation, etc.

earnings and incentive payments is arguably relevant especially in the case of high income individuals as shown by Bell and Van Reenen (2013, 2014). We study the sensitivity of our results to including or excluding additional types of income in the basic pay in section 4.6.3.¹⁶

A.2.3 Skills classification

We use a classification based on a match between the National Qualification Framework (NQF) and the Standard Occupation Code (SOC).¹⁷ The NQF defines 8 levels of skill based on the required qualification from PhD (level 8) to Entry level (less than GCSE grade D-G). The current UK immigration rules use 6 groups (see Table A2).¹⁸

Note that there is another possible classification of skills, based on the standard occupational classification (SOC). Skills here are defined as "the length of time deemed necessary for a person to become fully competent in the performance of the tasks associated with a job". Level 4 corresponds to the highest skill level and includes Corporate Managers, Science and technology professionals, Health professionals, Teaching and research professionals and Business and public service professionals. Level 1 corresponds to the lowest skill level and includes elementary trades, plant and storage related occupations and elementary administration and service occupations.

This classification relies on the first two digits of the 4-digit SOC code. Its main advantage is that it is very straightforward to implement and it is consistent in time. Indeed, although the SOC changed its classification in 2000 and 2010, the first two digits remain unchanged. However, one disadvantage is that relying on the first two digit is not accurate enough to distinguish between, for example, a restaurant manager (SOC2010 code 1223) and a natural environment and conservation manager (SOC2010 code 1212). But according to the work of Elias and Purcell (2004), the former group counts 9.5% of people aged 21-35 and holding a first degree or higher whereas the latter counts 72% of them. This analysis uses on the labor Force Survey 2001-2003. In another article, Elias and Purcell (2013), they advocate the use of another classification and consider the restaurant manager group as a "non graduate group' and the natural environment manager as an "expert group".

¹⁶The share of incentive pay increases strongly with earnings, while the share of overtime pay is stable around 5% for the first three quarters of the wage distribution, and decreases with wage for the remaining top quarter.

¹⁷See for example the "code of practice for skilled work, Immigration Rule Appendix J".

¹⁸A few specific occupations, which we don't use in our analysis, are unclassified: clergy, military, elected officers, sports players and coaches and prison service officers.

Table A2:	Skill	classification
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Skill category	Description
Low-skill	
Skill cat 1	Lowest skill occupations, includes many manufacturing basic oc- cupations, child-care related education, housekeeping, telephone salespersons
Skill cat 2	corresponds to a NQF below 3 but not considered as an entry level. Occupations such as pharmaceutical dispensers, green- keepers, aircraft maintenance technician
Intermediate-skil	l
Skill cat 3	Requires a NQF of 3 which corresponds to a Level of Advanced GCE (A-level). This category spans many different occupations from Fitness instructors to Legal associate professionals.
Skill cat 4	Requires a NQF of 4 and above which corresponds to a Certifi- cate of Higher Education. It includes many technical occupations like Medical technicians or IT operations technicians and some managerial occupations.
High-skill	
Skill cat 5	Includes most managerial and executive occupations as well as engineers. These occupations require at least a NQF of 6 which corresponds to a Bachelor???s degree or a Graduate Certificate.
Skill cat 6	Corresponds to occupational skilled to PhD-level and include most scientific occupations like Chemical scientists, Biological scientists, Research and development manager but also Higher education teaching professionals.

Notes: This table describe the education requirement for each of our six skill categories. These requirements have been taken from the "code of practice for skilled work, Immigration Rule Appendix J".

	Obs.	Hours	% Work full-Time	% Male	Age	Tenure
Low-skill Skill cat 1	371 613	30.1	60	<i>4</i> 9	37 3	62
Skill cat 2	39,165	35.4	83	68	39.1	8.2
Intermediate-skill						
Skill cat 3	77,847	36	88	60	39.1	9.4
Skill cat 4	27,115	36.4	93	60	39.6	9.1
High-skill						
Skill cat 5	111,539	36.4	94	70	40.7	9.8
Skill cat 6	3,475	35.8	92	61	39.3	10.4

Table A3: Demographics by skill level

Notes: Skill categories are based on occupation codes as described in A.2.3.

Tables A3 and A4 show that these workers have different labor market participation behaviour and different outcomes in the labor market.

A.3 Travel to work areas

A labor market is defined as a travel to work area and there are around 240 such areas in the UK depending on the year.¹⁹ Since 2011, there are exactly 228 travel to work areas (TTWAs) in the UK with 149 in England, 45 in Scotland, 18 in Wales, 10 in Northern Ireland and 6 cross-border. This is a tool widely used by geographers and statisticians although they have no legal status. They are defined as a form of Metropolitan Area and intent to group urban areas and their commuters hinterland. London, Bristol and Manchester are examples of Travel To Work Areas.

A.4 Matching BERD and ASHE

We match the individuals in "Clean ASHE" with the firms they work for in BERD; we restrict attention to private corporations (dropping public corporations, charities, unincorporated firms, etc). We start with all individuals in "Clean ASHE" who work for a firm

¹⁹Definition of travel to work areas change in time. For this reason, we never use a travel to work area continuously in time.

Skill	Hourly	Weekly	% incentive	% overtime	Annual
	pay	pay			earnings
Low-skill					
Skill cat 1	8.64	286	2.54	5.64	13,612
Skill cat 2	11.59	446	2.25	5.32	21,970
Intermediate-skill					
Skill cat 3	13.59	507	5.21	3.56	25,936
Skill cat 4	16.83	625	5.21	2.13	32,820
High-skill					
Skill cat 5	25.62	938	7.64	1.42	54,075
Skill cat 6	22.39	810	6.33	1.11	43,868

Table A4: Pay by skill categories

Notes: Skill categories are based on occupation codes as explained in subsection A.2.3.

with 400 or more employees and match them to the population of firms in BERD with 400 or more employees. Our final sample includes around 580,000 observations on around 150,000 individuals working in around 6,300 different firms; there are around 31,000 firmyear combinations. The implication of the matching and exact numbers can be found in Table A5 and the outcome of merging the subsample of firms in BERD over 400 employees and private firms in ASHE over 400 employees is presented in Table A6.

We use information on firms with more than 400 employees. These firms differ from smaller ones in some ways that are shown in Table A5. However, the distribution of wage in this sample is very similar to the one in the total sample, as seen in Figure A2. The geographical coverage of these firms is also very similar.

ASHE	Observations	Individuals	Mean wage	Sd wage
Raw ASHE	2,023,886	355,546	13.1	41.5
Clean ASHE	1,818,812	336,794	13.3	15
Private Corporations	1,074,318	243,010	12.9	17.3
Final Sample	626,722	156,966	12.9	18.7
BERD	Observations	Firms	% intramural R&D	% extramural R&D
Raw BERD	247,468	53,394	100	100
400+ Employees	9,013	1,917	75	85
Final Sample	8,562	1,884	66	80

Table A5: Construction of the sample

Notes: This table presents the evolution of the two databases ASHE and BERD across the successive steps conducted to match them. **ASHE**: Raw data corresponds to the standard ASHE database 2004-2015. Clean ASHE corresponds to the database "Cleaned ASHE" as described in subsection A.2.1. Private corporation corresponds to "Clean ASHE" restricted to private corporations and Final corresponds to "Clean ASHE" restricted to private corporations with more than 400 employees. Mean wage is measured as the average total weekly earning. **BERD**: Raw data corresponds to the standard BERD database 2004-2015. 400+ employees corresponds to this database restricted to firm with more than 400 employees and Final corresponds to firms of more than 400 employees that matched the final version of ASHE. % of intramural and extramural R&D are measured with respect to Raw data.

Year	in BERD not in ASHE	in ASHE not in BERD	in BERD and ASHE
2004	102	2394	670
2005	91	2365	808
2006	91	2329	956
2007	102	2363	757
2008	96	2400	628
2009	75	2360	798
2010	86	2310	696
2011	97	2360	708
2012	98	2419	781
2013	109	2464	800
2014	109	2592	844
2015	123	2674	890

Table A6: Matching results at the firm-year level

Notes: This table presents the number of firms that did not match because they are in BERD but not in ASHE (column 1) or because they are in ASHE but not in BERD (column 2) and the firms that are both in BERD and ASHE (column 3).





Notes: This figure plots the empirical cumulative distribution function for two samples: Clean ASHE, corresponding to the 1% random sample of the British population without restriction (other than some cleaning described in Appendix A.2 and Final Sample corresponding to workers of private companies with more than 400 employees.

A.5 Descriptive statistics

Table A7 gives description of the variables used in the regressions throughout the paper while A8 shows statistical moments of the main variables of interest at the individual level. Low-skill workers represent the majority of workers in our sample $(59\%)^{20}$, see Table A3. Workers with higher skill level earn higher wages with the exception of skill category 6 (researchers and professors), where the average is below the average for category 5. We also see from Table A4 that more innovative firms have on average a larger proportion of workers in high-skilled occupations.

 $^{^{20}}$ This is a slightly larger proportion than when considering the share of low skilled worker in the whole "clean ASHE" dataset (48%).

Variable name	Description
Age	Age of the individual at the time of the survey in year
Tenure	Number of year spent in the firm by the individual
Male	Dummy for being a male
Full Time	Dummy for working more than 25 hours a week on average
Age2	Age squared
Tenure2	Tenure squared

Table A7: Variable description

Notes: This table presents the description of the main variables used in the regressions.

		1			0			
Variable	Mean	sd	p10	p25	p50	p75	p90	p99
Total Hourly Wage (£)	14.1	13.5	6.5	7.5	10.3	16.2	25.5	61
Weekly Wage (£)	501	476	121	231	388	632	962	2202
Weekly Incentive Pay (£)	8.4	81.1	0	0	0	0	0	182.7
Weekly Overtime Pay (£)	20.1	60.9	0	0	0	3.6	62.7	292.9
Total Annual Wage (£)	26,173	44,143	4,563	9,776	19,069	32,069	49,652	135,958
Basic Paid Hours	35.8	11.8	16.8	30.8	40.6	42.8	44.2	57.8
Paid Overtime	1.7	4.5	0	0	0	0.4	5.8	22
Age	42.2	13.5	24.2	30.8	41.8	52.8	61.6	69.3
Tenure	8.2	8.9	1.1	2.2	4.4	11	20.9	39.6

Table A8: Descriptive statistics of wage variables

Notes: This table presents some moments (mean, standard deviation and different percentile thresholds) for a set of key variables. Tenure is the number of year an individual has been working in its current firm.

	Skill category						
	Lo)W	Interm	ediate	Hi	gh	
Quantile of R&D	1	2	3	4	5	6	Obs.
0 (no R&D)	63.7	5.6	11.7	3.9	14.8	0.3	467,207
1	66	7.7	9.9	2.8	13.4	0.2	23,168
2	63.8	7.7	10.1	3.3	14.6	0.5	13,708
3	59.7	8.2	11.5	3.8	16.2	0.5	9,983
4	59.6	5.5	14.4	3.3	16.6	0.6	8,380
5	60.6	4.9	14	3.3	16.9	0.3	9,478
6	53.7	6.2	14.8	4.3	20.2	0.9	5,613
7	53.6	8.8	11.2	4.9	20.9	0.6	6,328
8	46.9	7.9	16.8	5.5	22.2	0.7	5,730
9	51.6	8.4	11.2	4.4	23.7	0.7	4,486
10	43.1	9.2	13.1	5.4	28.3	0.9	5,755
11	36	10.1	15.1	5.8	32.2	0.7	6,090
12	37.1	8.8	15.1	6.1	32	0.9	6,612
13	34.3	8.3	15.2	6	35.4	0.8	5,473
14	31.2	9.4	13.4	6.7	38.3	1.1	4,862
15	30.7	8	18.2	8.9	32.8	1.3	5,270
16	22.9	7.8	20.4	10.1	37.4	1.3	8,442
17	21.9	6.1	20.4	11.9	38.7	0.9	9,291
18	25.1	7.8	18.1	9	38	1.9	7,858
19	22.6	13.2	15.7	6.3	39.8	2.3	9,306
20	20.1	6	13.9	6.7	41.6	11.7	7,714

Table A9: Share of workers at each skill category and quantiles of R&D

Notes: This table presents the average proportion of each skill group by quantile of R&D intensity. Skill groups are defined in Appendix A.2.3. Quantiles are the same as in Table A1.



Figure A3: Distribution of workers by skill category and R&D intensity of firm

Figure A4 shows that the share of workers that work in a firm that does any R&D increases from just over 20% for workers at the bottom of the wage distribution, to over 55% after the 80th percentile of the distribution where it plateaus. The share falls right at the top, where workers in the (low innovative) financial sector are heavily represented. This effect holds within innovative firms.



Figure A4: Share of workers in R&D firms at each percentile of the overall wage distribution

Notes: This figure plots the share of workers from innovative firms (defined as firms reporting a positive amount of R&D expenditure since 2000) at each percentile of the overall hourly wage distribution. All observations from our Final Sample from 2004 to 2015 are considered independently.

A.6 O*NET data

The O*NET dataset is a database aiming at providing an accurate definition of each occupations in the US at a very detailed level. Information include the type of tasks, the skills and abilities usually required and many characteristics such as, for example, the level of exposition to noise.

The database is freely available from the dedicated website²¹ and we use the version 21.1 Database - November 2016 Release.

The information have been gathered either from interviewing workers or from experts descriptions. Although the O*NET data is only based on US workers, we believe that the

²¹http://www.onetcenter.org/database.html

job descriptions are very similar to those of the UK. To match the different occupation classification we match O*NET data to UK data via isco08.

We summarize the responses to four questions which provide evidence to the effect that workers in low-skilled occupations are more complementary to other workers in high R&D intensive firms than in low R&D intensive firms.

- What are the consequences of your making an error (1 = no consequences; 2, 3, 4, 5 = very large consequences)
- 2. What is the impact of decisions you make (1 = no impact; 2, 3, 4, 5 = very large impact)
- 3. On-site or in-plant training (none, up to 6 months, between 6 months and a year, a year or more)
- 4. On-the-job training (none, up to 6 months, between 6 months and a year, a year or more)

Workers are asked to estimate the consequences of their making an error. They provide a grade between 1 (no consequence) and 5 (very large consequence) as spelled out above. In Table A10, we provide, for each skill level, the average values of the response in our sample across firms with three levels of R&D intensity compared to firms with no R&D. The values are standardized to be equal to 1 for no R&D firms, separately for each skill level. The consequences of a worker in a low-skilled occupation making an error are larger in a more R&D intensive firm than in a less R&D intensive firm. We see however that this pattern does not hold when R&D intensity is replaced by size (measured by total employment of the firm). The fact that R&D intensive firms do focus on tasks that are associated with a higher score for the "consequence of an error" is therefore not a size effect.

	Tercile of R&D intensity			Quartile of employment			t	
	None (1)	Low (2)	Middle (3)	High (4)	Very Small (1)	Small (2)	Middle (3)	Large (4)
Skill level								
Low	1.00	1.01	1.11	1.14	1.00	0.98	0.94	0.85
Intermediate	1.00	1.00	1.02	1.03	1.00	1.01	1.01	1.02
High	1.00	1.02	1.00	0.99	1.00	1.00	1.01	1.02

Table A10: Consequence of an error

Notes: R&D firms are split in three groups of equal size based on the value of their total R&D expenditure per employee. Data are taken from O*NET and report the average of the score for the question "What are the consequences of you making an error?" across our final sample standardized to be equal to one for non R&D firms (resp. for the lowest quartile of firm employment) at each skill level.

Impact of decision

Similarly, workers are asked to evaluate the impact of the decision they make. They provide grades reflecting their estimated impact, as specified above. We report the average values of the response across firms with three levels of R&D intensity compared to firms with no R&D. The results are shown in Table A11 where the same standardization as in Table A10 is done. In particular, we see that the impact of decisions of a worker in a low-skilled occupation, is larger in a more R&D intensive firm than in a less R&D intensive firm. The difference is small, but yet it is statistically significant.

Table A11: In	npact of d	lecision
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	Tercile of R&D intensity				Quartile of employment			
	None (1)	Low (2)	Middle (3)	High (4)	Very Small (1)	Small (2)	Middle (3)	Large (4)
Skill level								
Low	1.00	1.00	1.00	1.01	1.00	1.00	1.00	0.99
Intermediate High	1.00 1.00	0.99 1.00	0.98 0.98	0.98 0.97	1.00 1.00	1.01 1.00	1.02 0.99	1.03 1.02

Notes: R&D firms are split in three groups of equal size based on the value of their R&D expenditure per employee. Data are taken from O*NET and report the average of the score for the question "What is the impact of decisions that you make?" across our final sample standardized to be equal to one for non R&D firms (resp. for the lowest quartile of firm employment) at each skill level.

B Theoretical Appendix

B.1 Proof of Proposition 1

To measure the complete effect of innovation, let us consider how equilibrium wages react to a continuous increase in z (hence in λ_z wich corresponds to an upward shift of $\mathbb{E}_{\phi}[\lambda]$). For notation simplicity, let us consider that $z_{max} = 1$ which implies that $\lambda_z = z$.

We have:

$$\frac{dw_q(z)}{dz} = \frac{dw_q(z)}{d\lambda_z} = \frac{1}{4C} \left[\left(\overline{Q} - 1 \right) (Q_L - 1) \lambda_z + \frac{\overline{Q} + Q_L - 2}{2} \right]$$
$$= \frac{q(\lambda_z) - q_L}{2} (\overline{Q} - 1) + \frac{dq(\lambda_z)}{dz} \frac{Q - 1}{2} \lambda_z$$

and:

$$\frac{dw_{Q}(z)}{dz} = \frac{dw_{Q}(z)}{d\lambda_{z}} = \frac{(\overline{Q} - Q_{L})}{2} \left[(q_{L} - 1) + \frac{\lambda_{z}}{2C} (Q_{L} - 1) + \frac{1}{4C} \right]$$
$$= \frac{\overline{Q} - Q_{L}}{2} \left[(q - 1) + \lambda_{z} \frac{dq(\lambda_{z})}{dz} \right]$$

The inequality

$$\frac{dw_q(z)}{dz} > \frac{dw_Q(z)}{dz}$$

then results from the fact that $\forall z$:

1. $(q(\lambda_z) - q_L)(\overline{Q} - 1) > (\overline{Q} - Q_L)(q(\lambda_z) - 1);$ 2. $\frac{dq(\lambda_z)}{dz} = \frac{dq(\lambda_z)}{d\lambda_z} > 0;$ 3. $(\overline{Q} - 1) > (\overline{Q} - Q_L).$

B.2 Proof of Proposition 2

We have:

$$\frac{dw_q(\lambda, z)}{dz} = \left[\lambda(\overline{Q} - 1) + 1\right] \left(\frac{d\phi(\lambda, z)}{dz}(q(\lambda, z) - q_L) + \phi(\lambda, z)\frac{dq(\lambda, z)}{dz}\right)$$

and

$$\frac{dw_{Q}(z)}{dz} = \left(\overline{Q} - Q_{L}\right) \int_{0}^{1} \left(\left[\lambda(q(\lambda, z) - 1) + 1\right] \frac{d\phi(\lambda, z)}{dz} + \phi(\lambda, z)\lambda \frac{dq(\lambda, z)}{dz} \right) d\lambda$$

The proposition then follows from the following facts:

1. $\frac{d\phi(\lambda,z)}{\lambda} > 0$ and $\frac{d\phi(\lambda,z)}{dz} > 0$, which imply that $\frac{dq(\lambda,z)}{dz} > 0$ 2. $(\overline{Q} - Q_L) < (q - q_L)$ and $\overline{Q} > \overline{q}$.

B.3 Proof of Proposition 3

We start from the maximization problem (recall that the optimal value of Q is \overline{Q} :

$$\max_{\vec{q}} \left(\tilde{\Pi}(\vec{q}) - \int_0^1 C(\lambda) \left(q(\lambda) - q_L \right)^2 d\lambda \right) \text{s.t. } \int_0^1 \left(q(\lambda) - q_L \right) d\lambda \le T,$$

If ν denotes the Lagrange multiplier associated with the time constraint, then the optimal value of $q(\lambda)$ is:

$$q^{*}(\lambda) = q_{L} + \max\{0, \phi(\lambda, z) \frac{\lambda(Q_{L} - 1) + 1}{4C} - \frac{\nu}{2C}\}.$$

Let

$$g(\lambda) = \phi(\lambda, z) \frac{\lambda(Q_L - 1) + 1}{4C}$$

The function g is clearly increasing in λ and $g(0) = \frac{\phi(0,z)}{4C}$ and $g(1) = \frac{\phi(1,z)Q_L}{4C}$. Then for each value of z, there exists a cutoff value $\overline{\lambda}$ such that when $\lambda \leq \overline{\lambda}$, then $q^*(\lambda) = q_L$ and the firm outsources this task. This cutoff value is simply determined by:²²

$$g(\bar{\lambda}) = \frac{\nu}{2C} \Longrightarrow \phi(\bar{\lambda}, z) \frac{\bar{\lambda}(Q_L - 1) + 1}{2} = \nu.$$

To determine the value of v, we use the fact that the constraint is binding, so we must have:

$$T = q_L + \int_{\bar{\lambda}}^1 g(\lambda) d\lambda - \frac{\nu(1-\bar{\lambda})}{2C} = q_L + \int_{\bar{\lambda}}^1 g(\lambda) d\lambda - g(\bar{\lambda})(1-\bar{\lambda}).$$

From here, we will assume that $\phi(\lambda, z) = (1 + z)\lambda^z$ and $z \in \mathbb{N}$. This implies that:

$$\int_{\bar{\lambda}}^{1} g(\lambda) d\lambda = \frac{z+1}{z+2} \frac{(Q_L - 1)}{4C} (1 - \bar{\lambda}^{z+2}) + \frac{(1 - \bar{\lambda}^{z+1})}{4C}$$

we get $\overline{\lambda}$ to be the solution of the equation:

$$4C(T-q_L) = \frac{z+1}{z+2}(Q_L-1)(1-\bar{\lambda}^{z+2}) + (1-\bar{\lambda}^{z+1}) - \bar{\lambda}^z(1-\bar{\lambda})(z+1)(\bar{\lambda}(Q_L-1)+1)$$
(6)

²²There is always one and only one value of $\overline{\lambda}$ for each value of z. However, this value is not necessarily bound to the [0, 1] interval. If $\overline{\lambda} < 0$, then we shall consider that there is no outsourcing.

We want to show that $\overline{\lambda}$ increases with z.

Example 3. Consider the case of two firms A and B. Firm A is not innovative: z = 0 whereas Firm B is innovative with z = 1.

Hence in firm A the outsourcing equation (6) *yields:*

$$\bar{\lambda}_A = 1 - \sqrt{\frac{8C(T-q_L)}{Q_L - 1}}$$

whereas in Firm B the outsourcing equation (6) yields a $\bar{\lambda}_B$ which satisfies:

$$4C(T-q_L) = (1-\bar{\lambda})^2 \left(1 + \frac{2(Q_L-1)}{3}(2\bar{\lambda}+1)\right)$$

Since for all $\lambda \in [0, 1]$, we have

$$1 + \frac{2(Q_L - 1)}{3}(2\lambda + 1) > \frac{Q_L - 1}{2},$$

then we must have $(1 - \overline{\lambda}_A)^2 > (1 - \overline{\lambda}_B)^2$ which implies $\overline{\lambda}_B > \overline{\lambda}_A$.

Note that a necessary condition for A to outsource is that:

$$q_L < \left(T - \frac{Q_L - 1}{8C}\right)$$

and similarly for B:

$$q_L < \left(T - \frac{1 + 2Q_L}{12C}\right) < \left(T - \frac{Q_L - 1}{8C}\right)$$

In other words, if the outside quality q_L is too low then firms won't outsource. The propensity to outsource also increases with the training cost and with the tightness of the capacity constraint is tight inversely measured by T.

More generally, and as long as $z \in \mathbb{N}$, the outsourcing condition (6) becomes:

$$4C(T - q_L) = (1 - \bar{\lambda})^2 \underbrace{\left[\frac{z+1}{z+2}(Q_L - 1)\sum_{i=0}^{z+1}i\bar{\lambda}^{i-1} + \sum_{i=0}^{z}i\bar{\lambda}^{i-1}\right]}_{u_z(\bar{\lambda})}$$

where $u_z(\bar{\lambda})$ is increasing in z and always positive when $\bar{\lambda} \in [0, 1]$. This ensures that $\bar{\lambda}$ is increasing with z, which completes the proof.

B.4 Extension to multiple workers in the same task

We now consider the more general case with $n \ge 1$ low-skilled occupation workers and $m \ge 1$ workers in high-skilled occupations. To determine the equilibrium wages resulting from ex post negotiation, we rely on Stole and Zwiebel (1996). In their framework, if the n^{th} low-skilled occupation worker refuses the wage offer w_n^q , then the remaining n - 1 low-skilled occupation workers renegotiate a wage w_{n-1}^q . By induction, this provides a generic expression for the two equilibrium wages $w_{n,m}^q(Q, q, \lambda)$ and $w_{n,m}^Q(Q, \overline{q})$ (up to a constant in q, Q and λ):

$$w_{n,m}^{q}(Q,q,\lambda) = \lambda \phi(\lambda) \frac{q(\lambda) - q_{L}}{n(n+1)} \sum_{i=0}^{n} iQ^{m}q(\lambda)^{i-1} + \frac{(1-\lambda)}{2}(q(\lambda) - q_{L})\phi(\lambda)$$
$$w_{n,m}^{Q}(Q,\overline{q}) = \frac{Q - Q_{L}}{m(m+1)} \sum_{i=0}^{m} i \int_{0}^{1} q(\lambda)^{n}Q^{i-1}\lambda\phi(\lambda)d\lambda + \frac{1 - \mathbb{E}_{\phi}[\lambda]}{2}(Q - Q_{L}),$$

when assuming equal bargaining powers for high- and low-skilled occupation workers. Note that this extension nests the baseline version of the model since taking n = 1 and m = 1 yields the same results as above.

Let us now assume that we are in the toy case, that is, $\phi(\lambda) = 1$ if $\lambda = \lambda_z \equiv \frac{z}{z_{max}}$ and 0 otherwise. In that case:

$$w_{n,m}^{q}(Q,q,\lambda_{z}) = \lambda_{z} \frac{q-q_{L}}{n(n+1)} \sum_{i=0}^{n} iQ^{m}q^{i-1} + \frac{1-\lambda_{z}}{2}(q-q_{L})$$

$$w_{n,m}^{Q}(Q,\overline{q},\lambda_{z}) = \lambda_{z} \frac{Q-Q_{L}}{m(m+1)} \sum_{i=0}^{m} iq^{n}Q^{i-1} + \frac{1-\lambda_{z}}{2}(Q-Q_{L}),$$
(7)

The case where n = 1 and m = 2

In this case, we have:

$$\frac{\partial w_{1,2}^q(Q,q,\lambda_z)}{\partial \lambda_z} = \frac{(q-q_L)(Q^2-1)}{2} \text{ and } \frac{\partial w_{1,2}^Q(Q,q,\lambda_z)}{\partial \lambda_z} = \frac{(Q-Q_L)}{2} \left(\frac{q(1+2Q)}{3}-1\right),$$

and since Q > q implies q(1 + 2Q) < Q(Q + 2Q), then $\frac{q(1+2Q)}{3} - 1 < Q^2 - 1$, which, combined with the assumption that $(Q - Q_L) < (q - q_L)$, immediately implies that:

$$\frac{\partial w_{1,2}^{q}(Q,q,\lambda_{z})}{\partial \lambda_{z}} > \frac{\partial w_{1,2}^{Q}(Q,q,\lambda_{z})}{\partial \lambda_{z}}$$

The case where n = 2 and m = 1

In this case, we have:

$$\frac{\partial w_{2,1}^q(Q,q,\lambda_z)}{\partial \lambda_z} = \frac{(q-q_L)(Q+2qQ)}{6} - \frac{q-q_L}{2} \text{ and } \frac{\partial w_{2,1}^Q(Q,q,\lambda_z)}{\partial \lambda_z} = \frac{(Q-Q_L)(q-1)}{2},$$

Then a sufficient condition for $\frac{\partial w_{2,1}^q(Q,q,\lambda_z)}{\partial \lambda_z} > \frac{\partial w_{2,1}^Q(Q,q,\lambda_z)}{\partial \lambda_z}$ is that Q + 2qQ > 3q which in turn is always true since Q > q > 1.

The case where n = m

For a given $n \ge 2$, a sufficient condition for $\frac{\partial w_{n,n}^q(Q,q,\lambda_z)}{\partial \lambda_z} > \frac{\partial w_{n,n}^Q(Q,q,\lambda_z)}{\partial \lambda_z}$ is:

$$\frac{1}{n(n+1)}\sum_{i=0}^{n}iQ^{n}q^{i-1} > \frac{1}{n(n+1)}\sum_{i=0}^{n}iq^{n}Q^{i-1},$$

which is equivalent to:

$$\sum_{i=0}^{n} \frac{i}{q^{n-i+1}} > \sum_{i=0}^{n} \frac{i}{Q^{n-i+1}},$$

which is automatically true as long as $n \ge 2$.

The case where *n* < *m*

By induction, for a given n > 2, if we assume that $\frac{\partial w_{n,m}^q(Q,q,\lambda_z)}{\partial \lambda_z} > \frac{\partial w_{n,m}^Q(Q,q,\lambda_z)}{\partial \lambda_z}$, then it is easy to show that:

$$\frac{1}{n(n+1)}\sum_{i=0}^{n}iQ^{m+1}q^{i-1} > \frac{1}{(m+1)(m+2)}\sum_{i=0}^{m+1}iq^{n}Q^{i-1},$$

and therefore that

$$\frac{\partial w_{n,m}^{q}(Q,q,\lambda_{z})}{\partial \lambda_{z}} > \frac{\partial w_{n,m+1}^{Q}(Q,q,\lambda_{z})}{\partial \lambda_{z}}$$