



COLLÈGE  
DE FRANCE  
—1530—



CIFAR  
CANADIAN INSTITUTE  
for ADVANCED RESEARCH

*Remnant of the first order  
Mott transition at finite doping as an  
organizing principle for  
strongly correlated superconductors*

André-Marie Tremblay



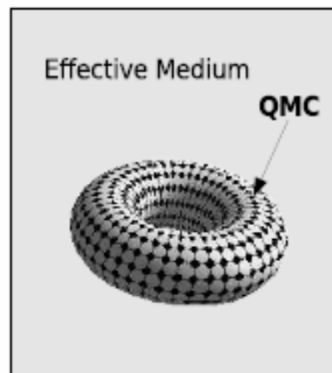
Collège de France, 26 mars 2015  
17h45 à 18h15



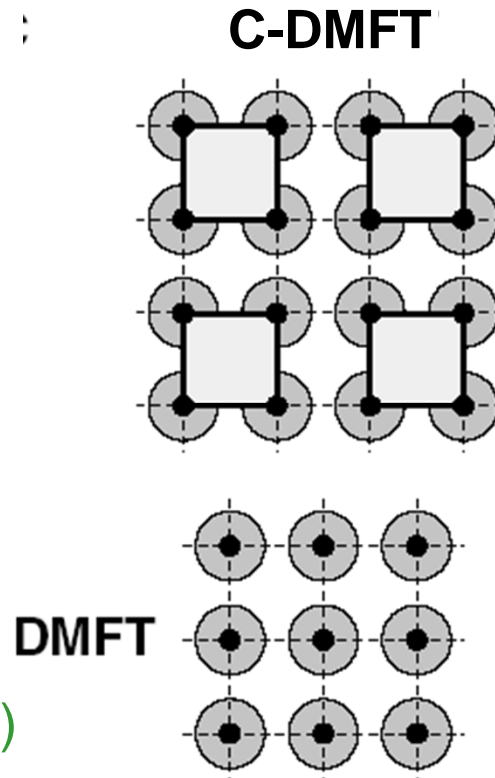
UNIVERSITÉ DE  
SHERBROOKE

# Method

# 2d Hubbard: Quantum cluster method



**DCA**



Hettler ...Jarrell...Krishnamurty PRB **58** (1998)

Kotliar et al. PRL **87** (2001)

M. Potthoff *et al.* PRL **91**, 206402 (2003).

REVIEWS

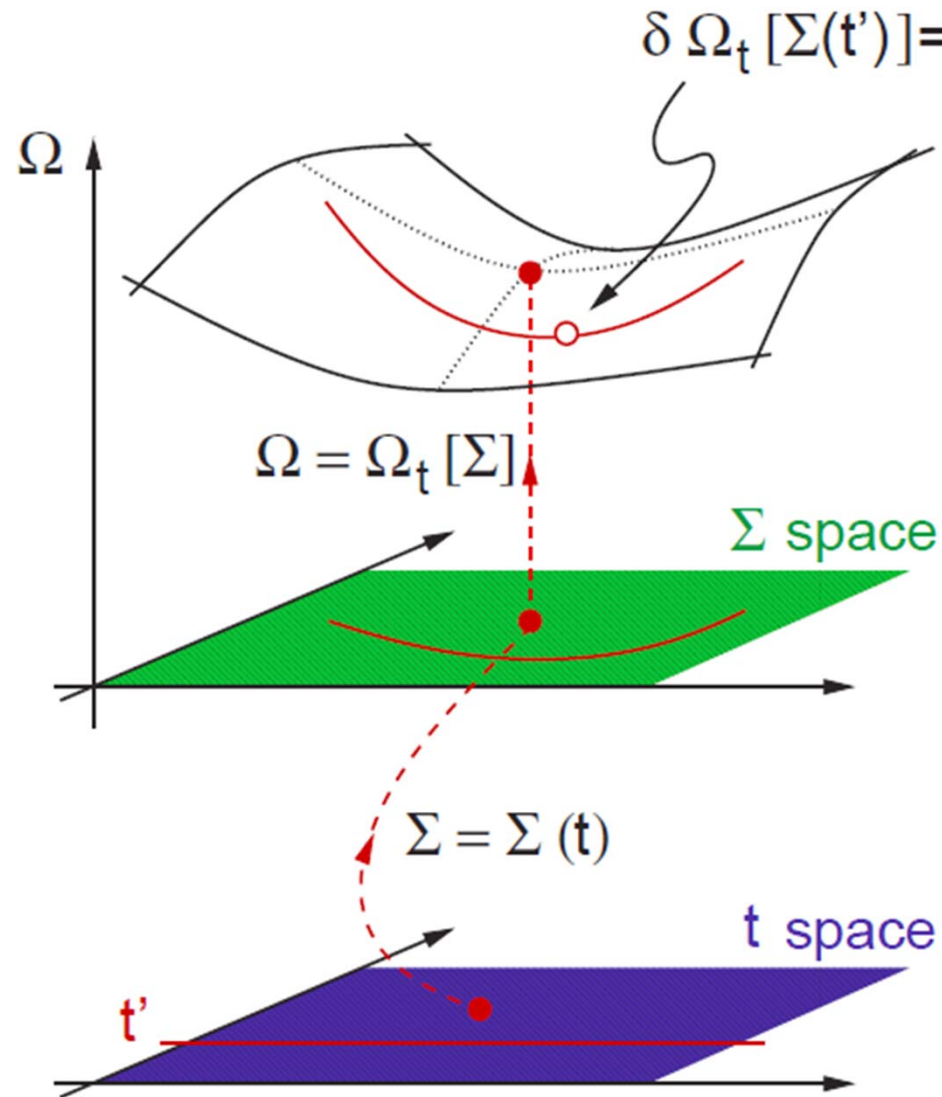
Maier, Jarrell et al., RMP. (2005)

Kotliar *et al.* RMP (2006)

AMST *et al.* LTP (2006)



# DMFT as a stationary point



M. Potthoff, Eur. Phys. J. B 32, 429 (2003).

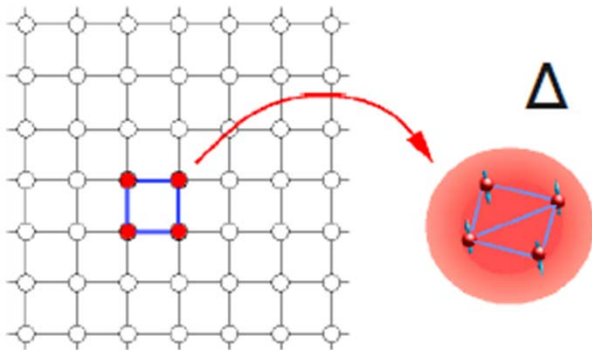


## + and -

- Long range order:
  - Allow symmetry breaking in the bath (mean-field)
- Included:
  - Short-range dynamical and spatial correlations
- Missing:
  - Long wavelength p-h and p-p fluctuations



# C-DMFT

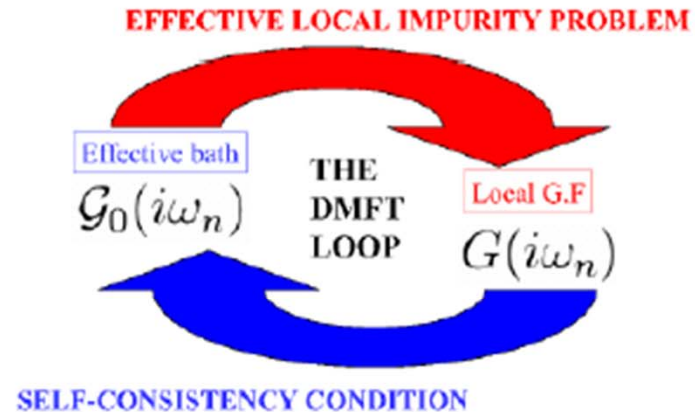


Mean-field is not a trivial problem! Many impurity solvers.

Here: continuous time QMC

P. Werner, PRL 2006  
 P. Werner, PRB 2007  
 K. Haule, PRB 2007

$$Z = \int \mathcal{D}[\psi^\dagger, \psi] e^{-S_c - \int_0^\beta d\tau \int_0^\beta d\tau' \sum_{\mathbf{k}} \psi_{\mathbf{k}}^\dagger(\tau) \Delta_{\mathbf{k}}(\tau, \tau') \psi_{\mathbf{k}}(\tau')}$$



$$\Delta(i\omega_n) = i\omega_n + \mu - \Sigma_c(i\omega_n)$$

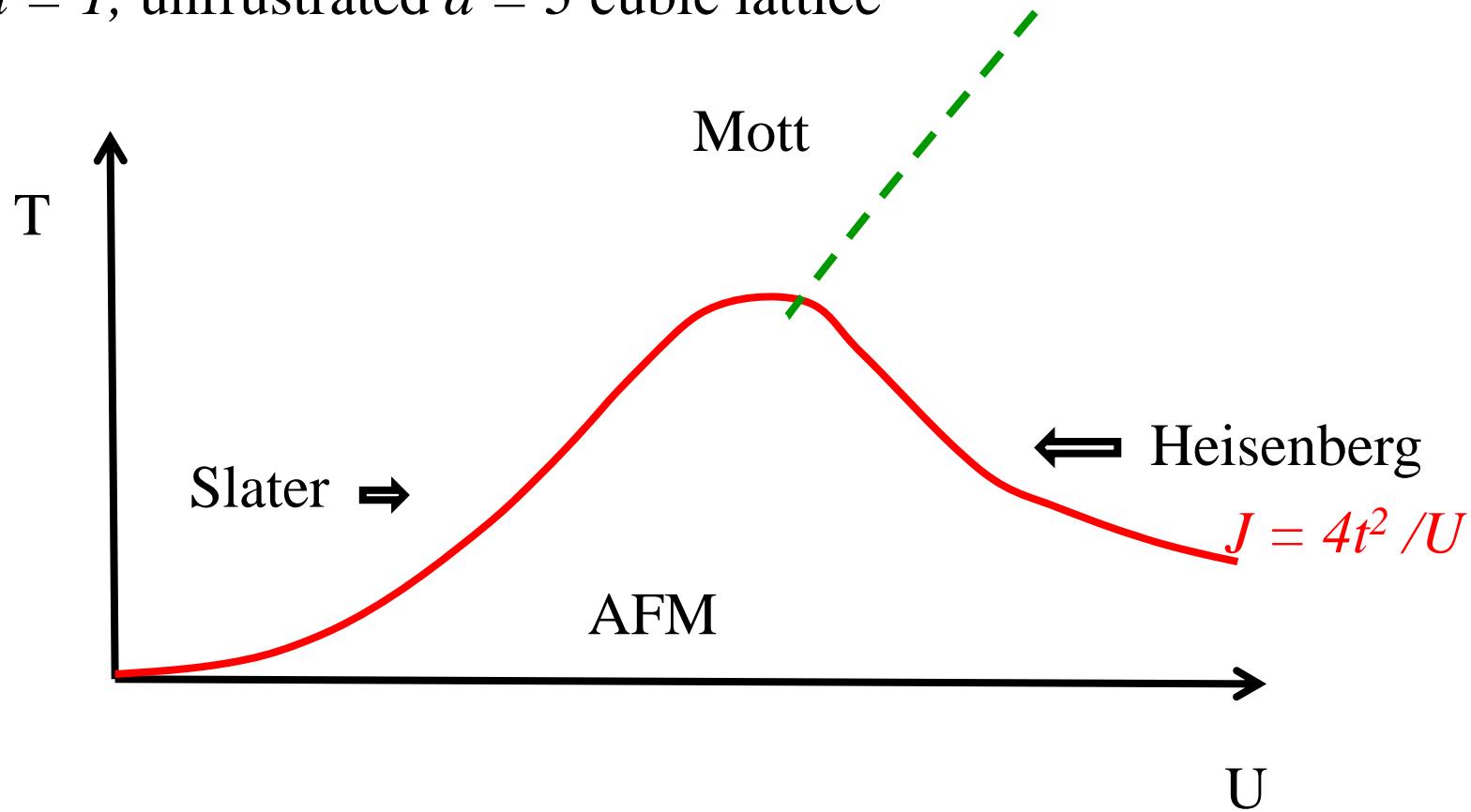
$$- \left[ \sum_{\tilde{\mathbf{k}}} \frac{1}{i\omega_n + \mu - t_c(\tilde{\mathbf{k}}) - \Sigma_c(i\omega_n)} \right]^{-1}$$

# Mott physics (half-filling)



# Local moment and Mott transition

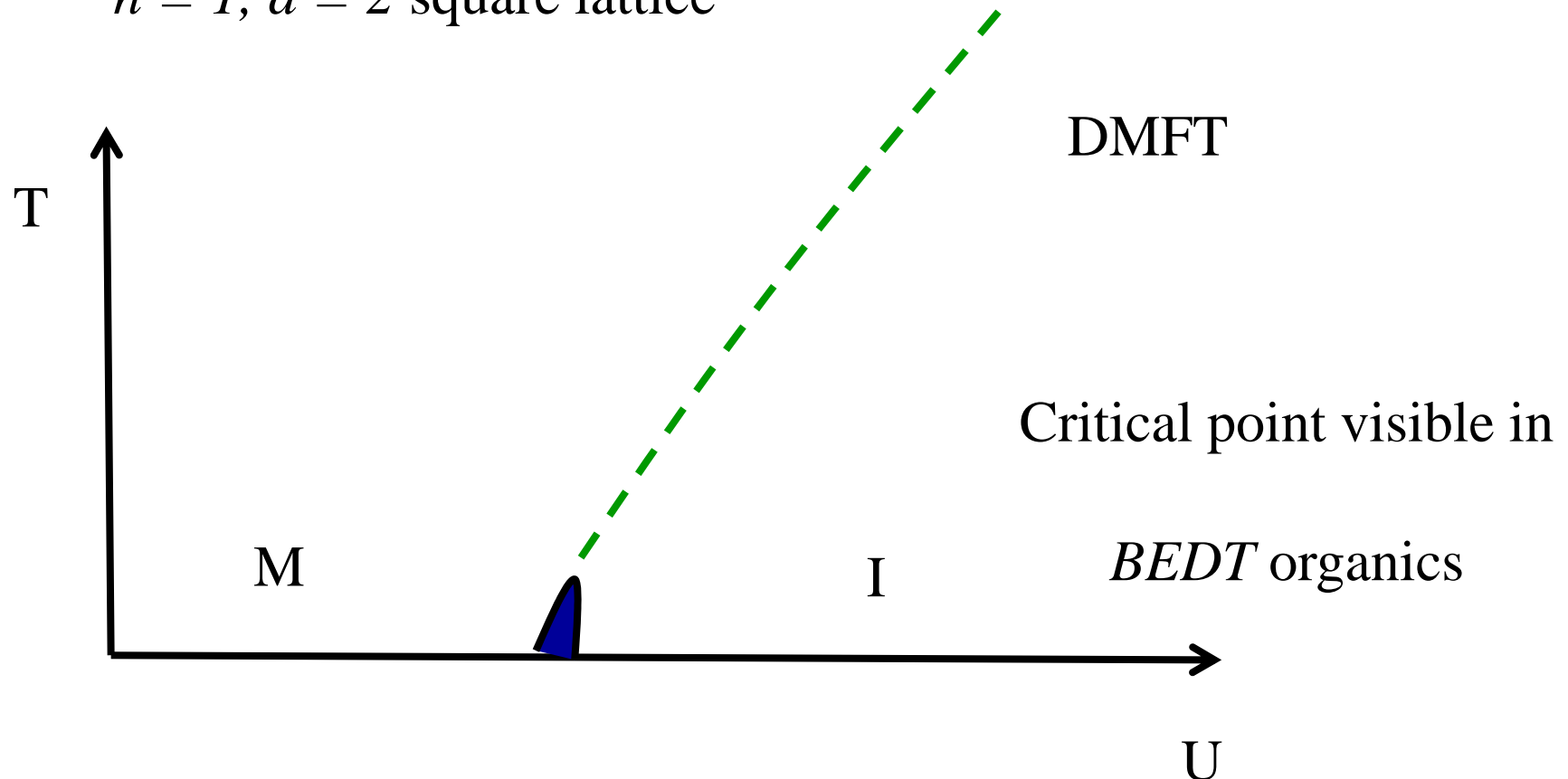
$n = 1$ , unfrustrated  $d = 3$  cubic lattice





# Local moment and Mott transition

$n = 1, d = 2$  square lattice



Understanding finite temperature phase from a *mean-field theory* down to  $T = 0$



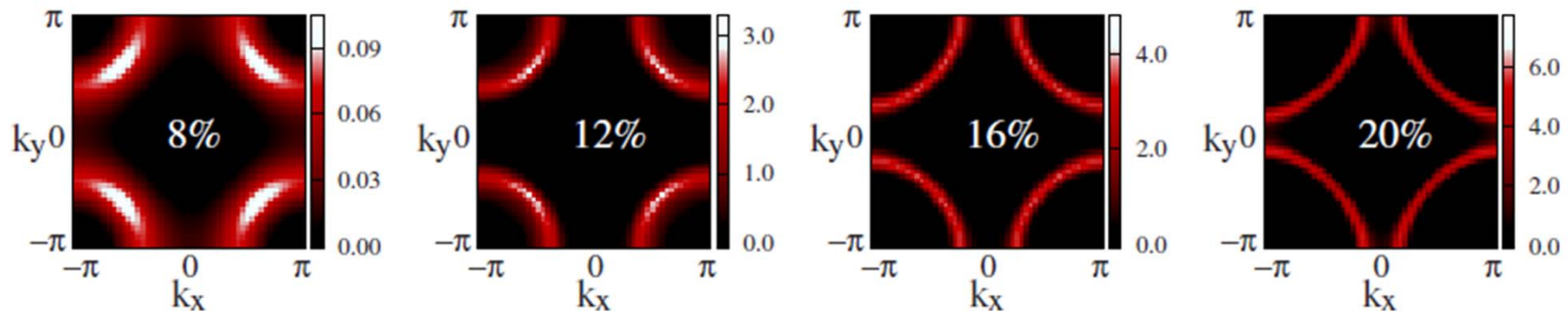
# Doped Mott insulator : normal state

# Anomalous metallic state near half-filling (examples)

- Pseudogap
  - B. Kyung et al., PRB 73, 165114 (2006).
  - N. S. Vidhyadhiraja et al., PRL 102, 206407 (2009).
  - A. Liebsch and N.-H. Tong, PrB 80, 165126 (2009).
  - D. Sénéchal, AMST, PRL **92** (2004)
- Momentum selective transition
  - P. Werner et al., PRB 80, 045120 (2009).
  - M. Ferrero et al., EPL 85, 57 009 (2009).
- Competition between Kondo and superexchange
  - K. Haule and G. Kotliar, Phys. Rev. B 76, 104509 (2007).
  - M. Ferrero et al., Europhys. Lett. 85, 57 009 (2009).
  - K. Haule and G. Kotliar, Phys. Rev. B 76, 092503 (2007).



# Pseudogap



Michel Ferrero, P. S. Cornaglia, L. De Leo, O. Parcollet, G. Kotliar, A. Georges  
PRB **80**, 064501 (2009)

Seen by all groups and DCA, CDMFT

Gull, Werner, Millis, PRB (2009)

Sénéchal, AMT, PRL **92**, 126401 (2004).

C. Huscroft, M. Jarrell, Th. Maier, et al. PRL **86**, 139 (2001)





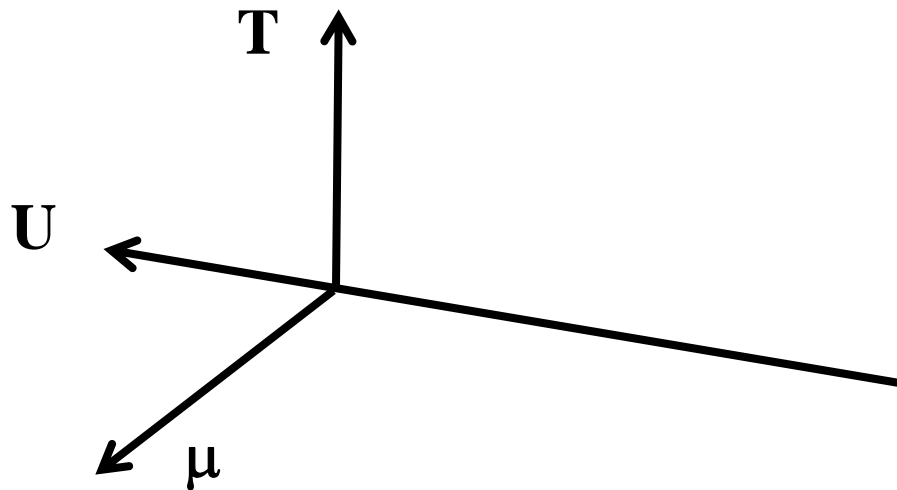
Giovanni Sordi

G. Sordi, K. Haule, A.-M.S.T  
PRL, **104**, 226402 (2010)

and

Phys. Rev. B. **84**, 075161 (2011)

## Doping-induced Mott transition ( $t'=0$ )



Kristjan Haule

Lesson from DMFT, first order transition + critical point governs phase diagram



# A first order transition?

At positive  $t'$

A. Macridin, M. Jarrell, and T. Maier,  
Phys. Rev. B **74**, 085104 (2006)

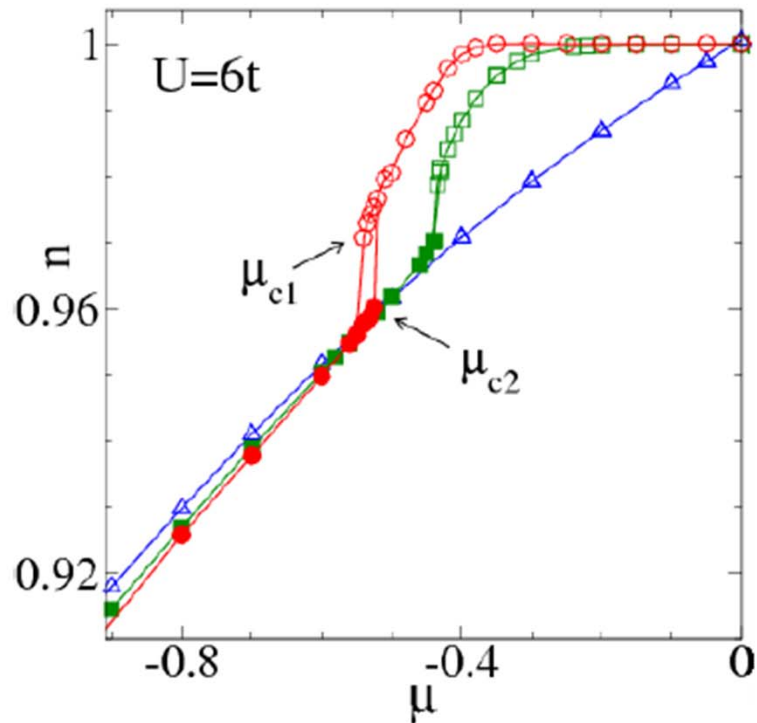
E. Khatami, K. Mielson, D. Galanakis, A. Macridin, J. Moreno,  
R. T. Scalettar, and M. Jarrell  
PRB **81**, 201101(R) 2010

A. Liebsch, N.H. Tong, PRB **80**, 165126 (2009)

Here  $t'=0$

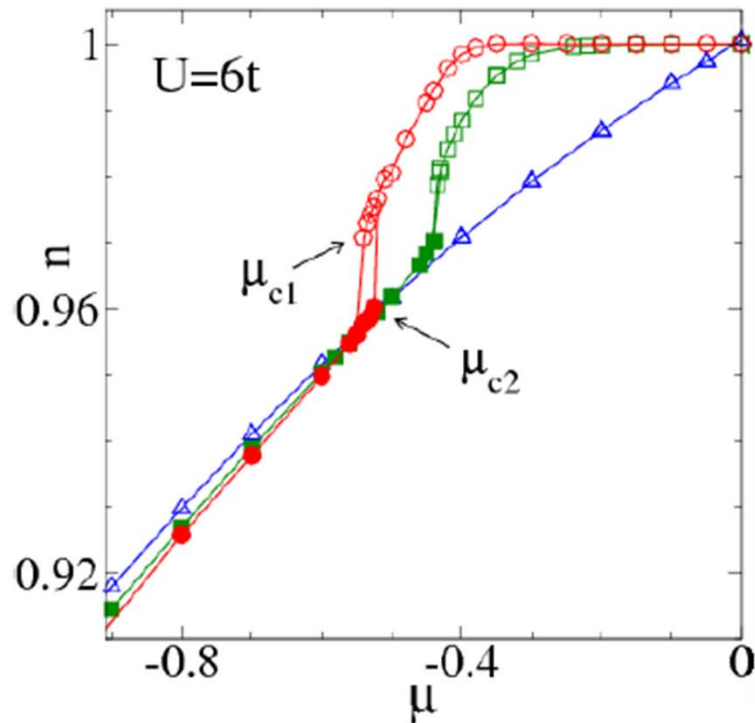


# First order transition at finite doping

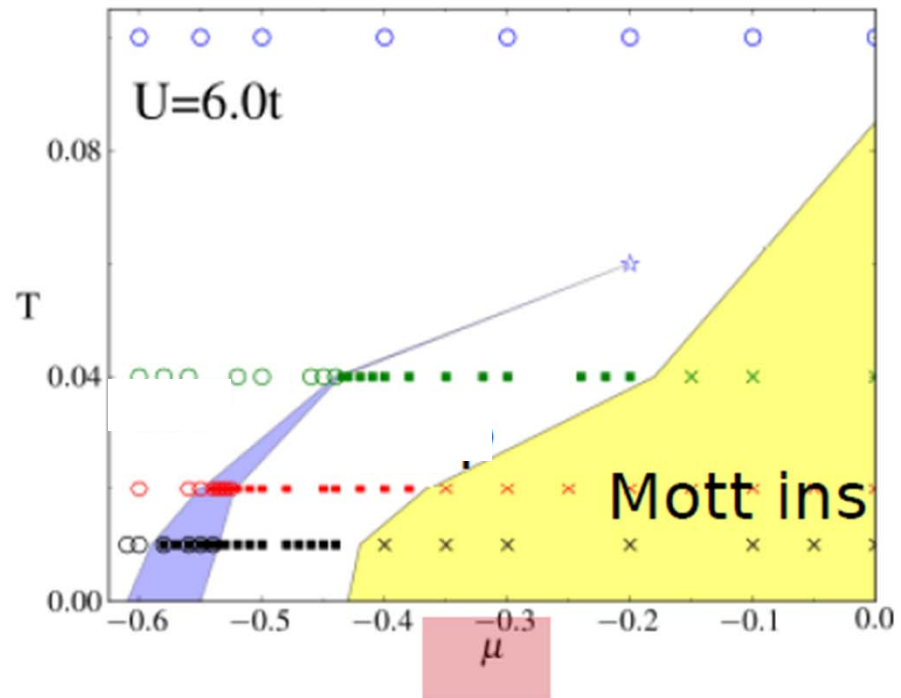


$n(\mu)$  for several temperatures:  
 $T/t = 1/10, 1/25, 1/50$

# First order transition at finite doping



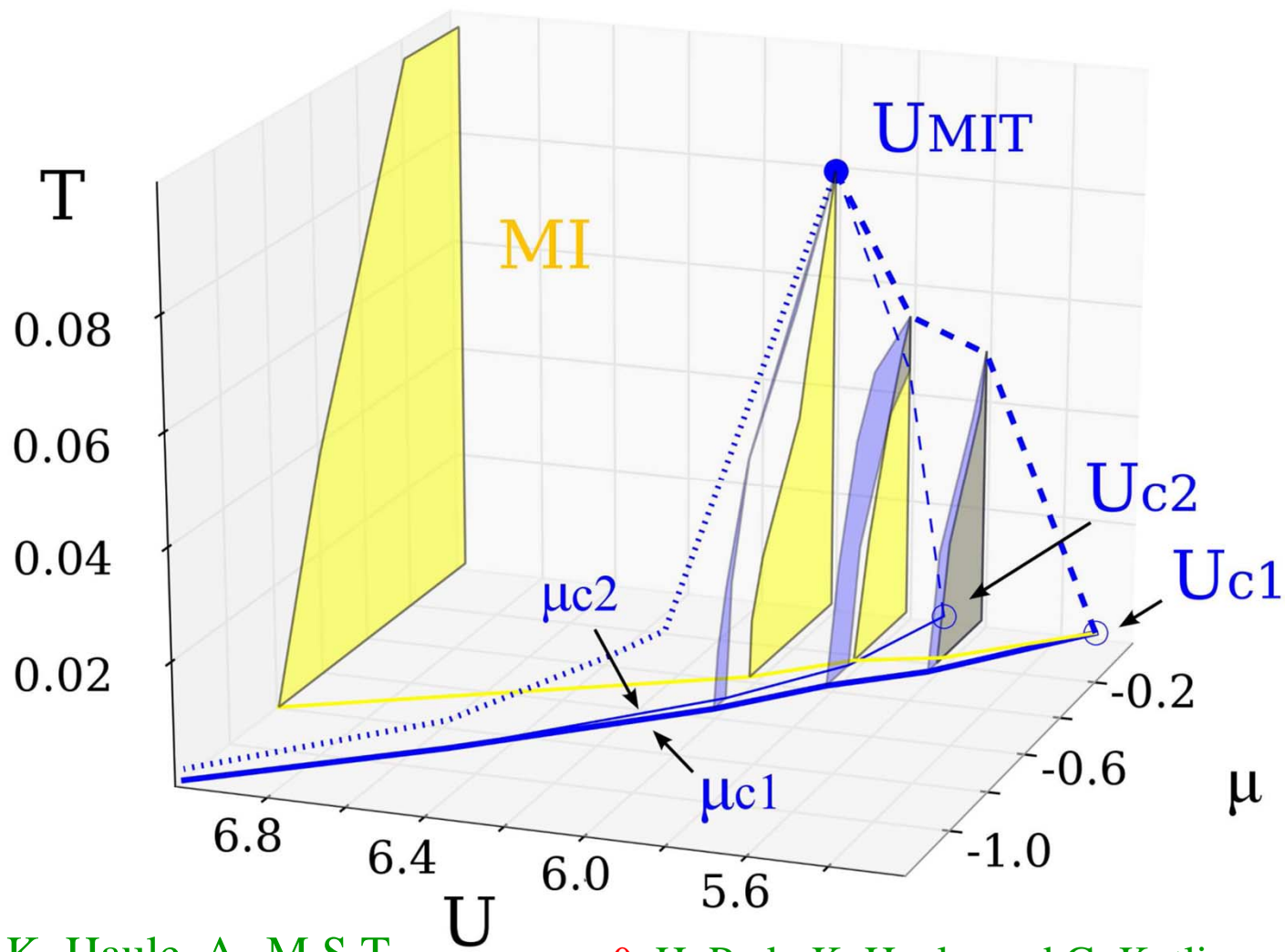
$n(\mu)$  for several temperatures:  
 $T/t = 1/10$ ,  $1/25$ ,  $1/50$



Hysteretic behavior:  
 fingerprint first order  
 transition!



# Normal state phase diagram



G. Sordi, K. Haule, A.-M.S.T  
PRL, **104**, 226402 (2010)

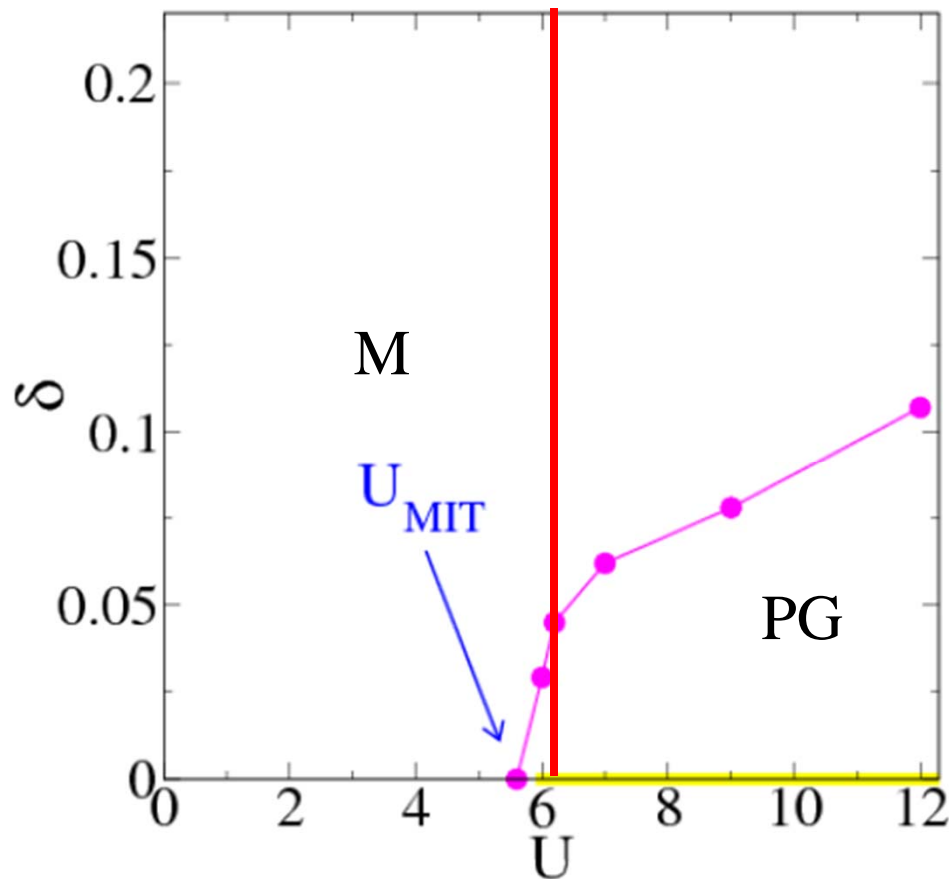
$\mu = 0$ , H. Park, K. Haule, and G. Kotliar,  
Phys. Rev. Lett. 101, 186403 (2008)



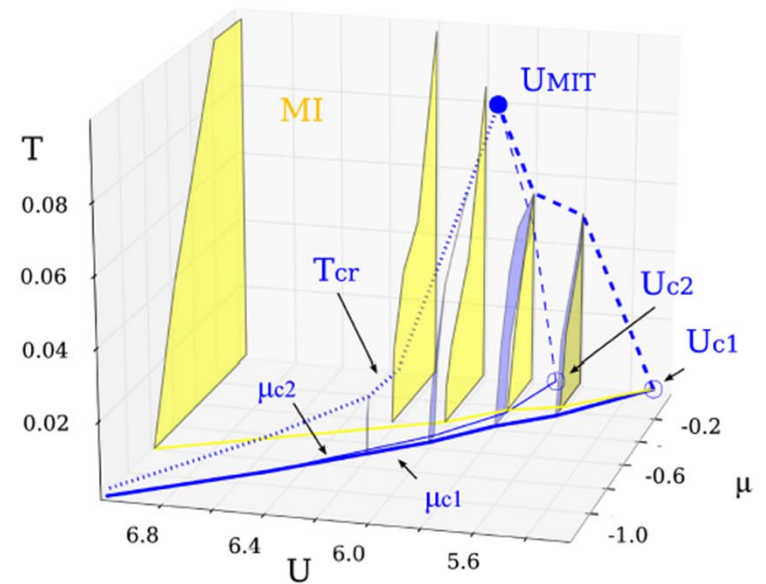
UNIVERSITÉ DE  
SHERBROOKE

# Link to Mott transition up to optimal doping

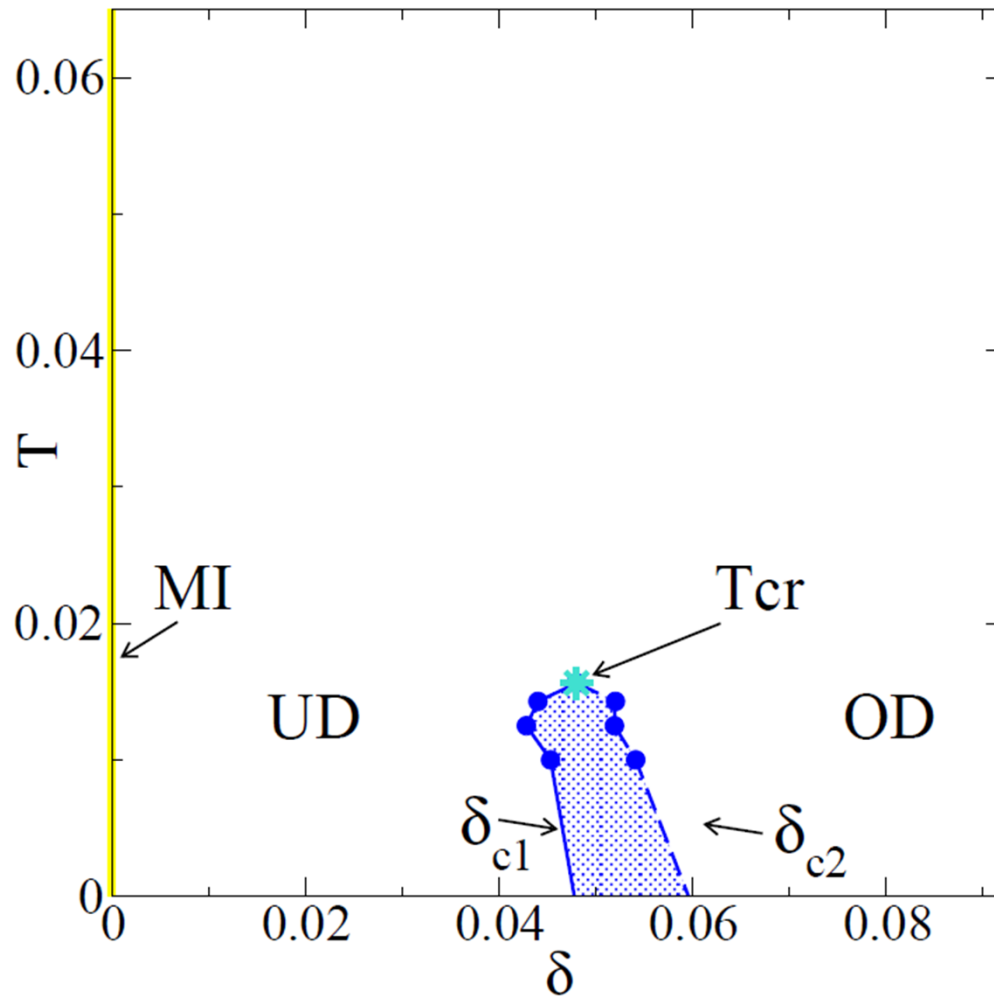
Doping dependence of critical point as a function of  $U$



Smaller  $D$  and  $S$



# Characterisation of the phases ( $U=6.2t$ )





Giovanni Sordi



Patrick Sémon



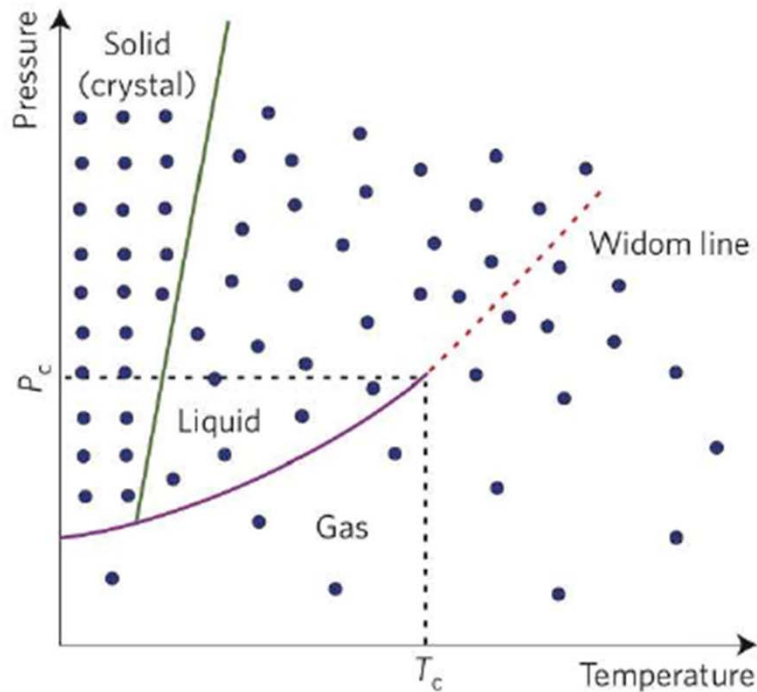
Kristjan Haul

Widom line ( $t' = 0$ )

Pseudogap in the normal state and the  
Widom line



# What is the Widom line?

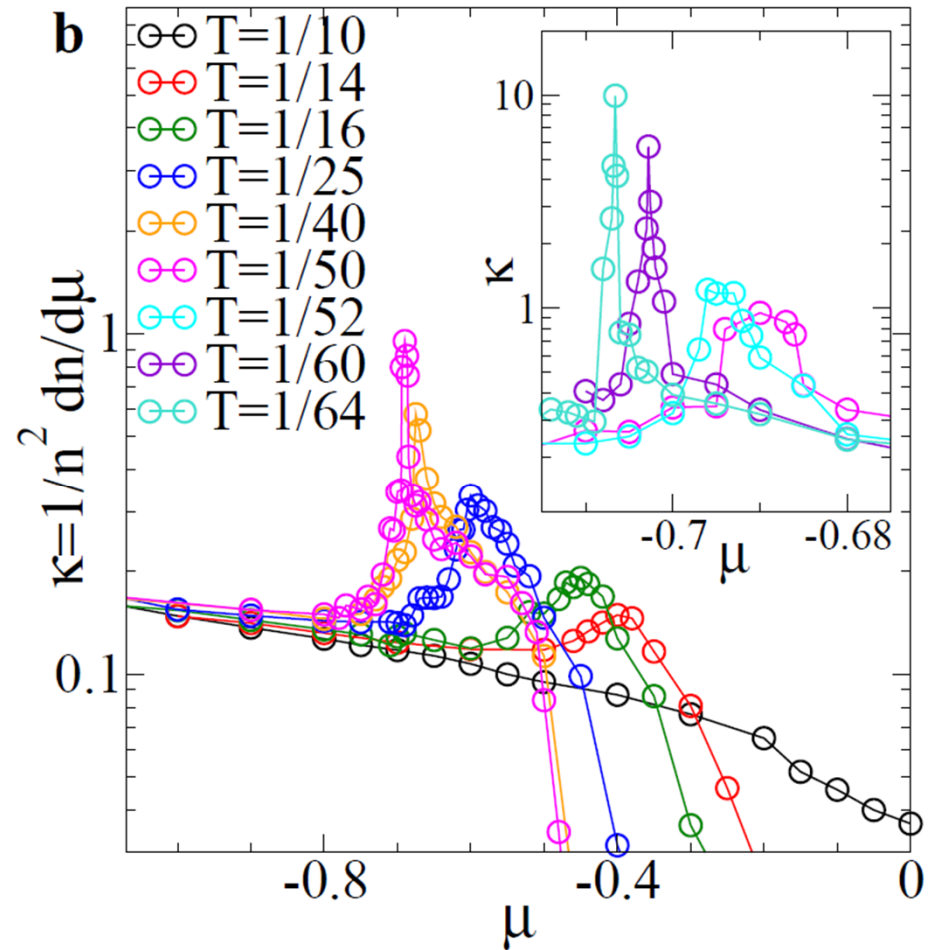
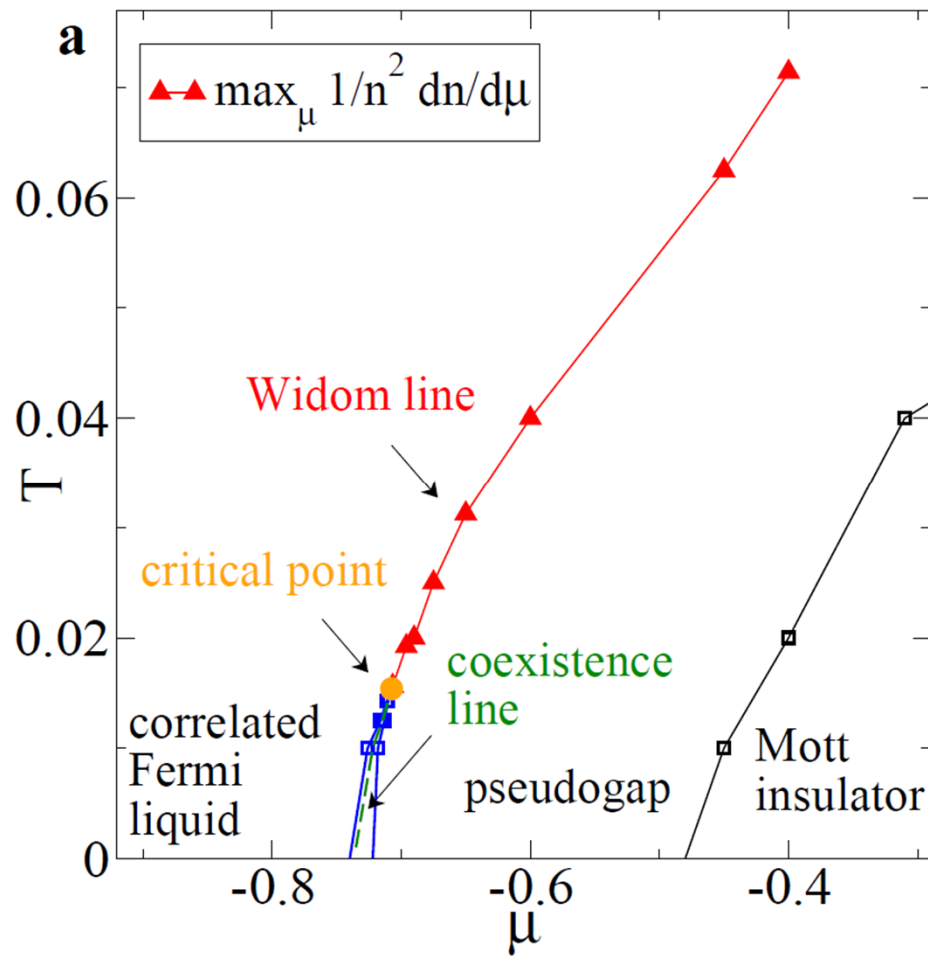


McMillan and Stanley, Nat Phys 2010

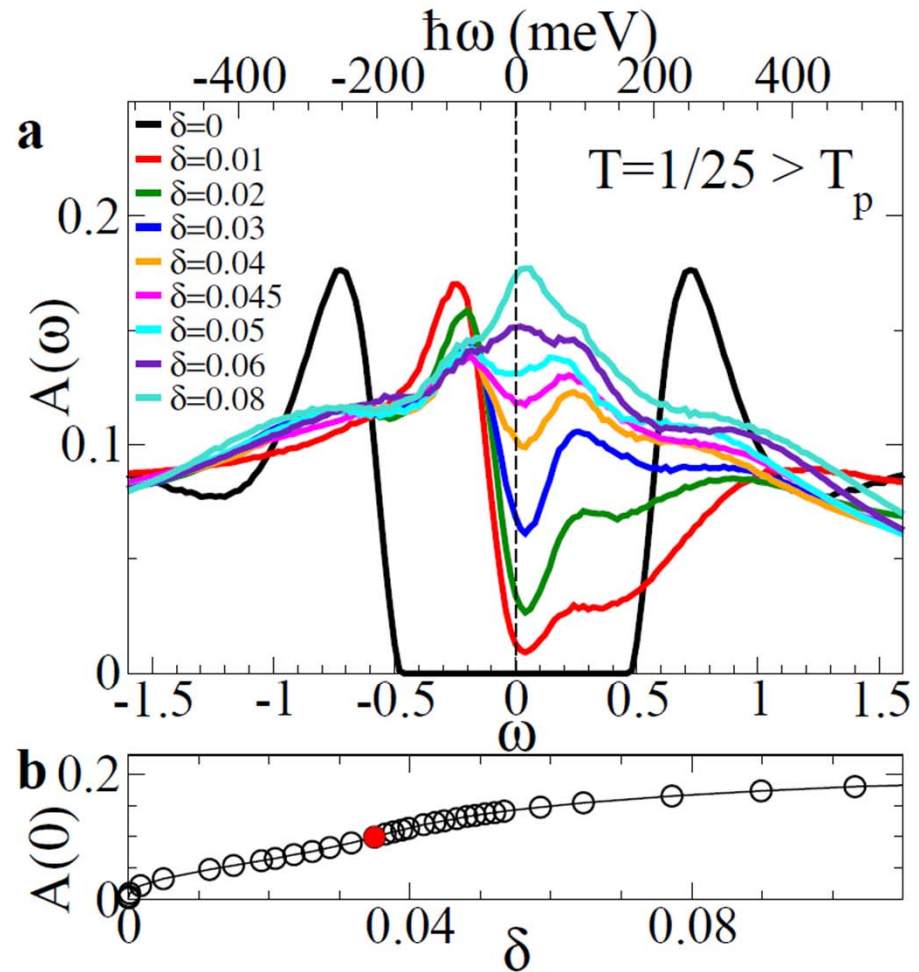
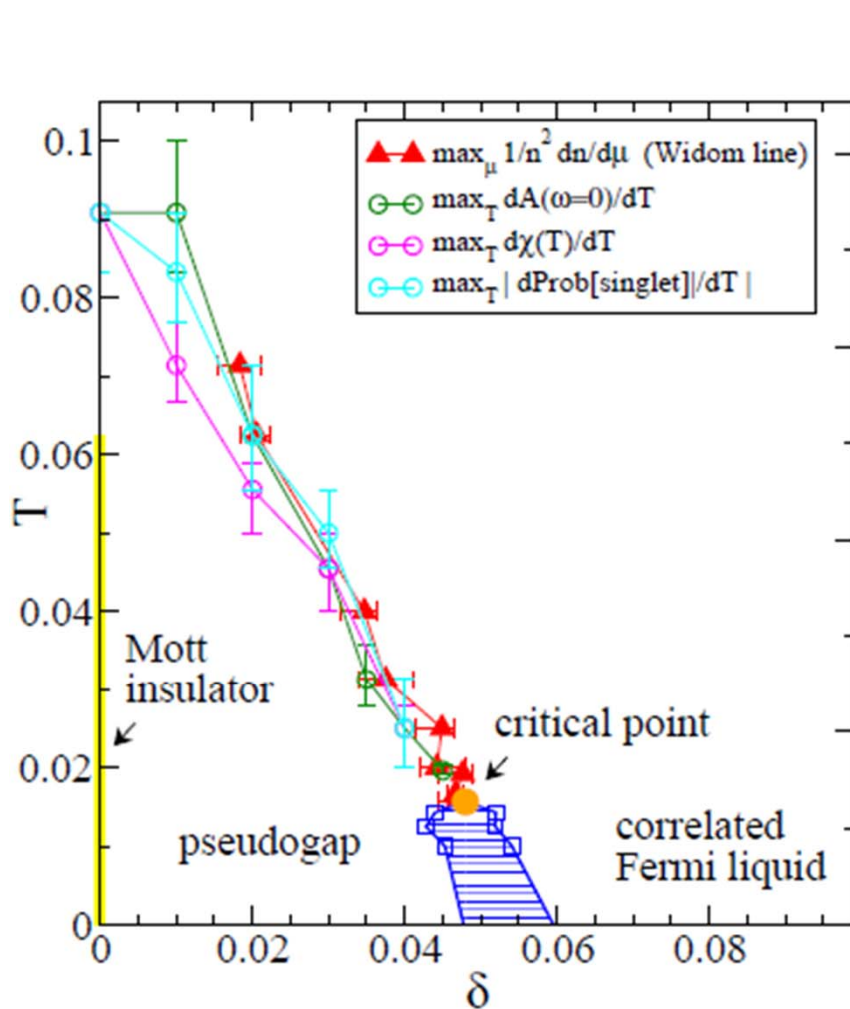
- ▶ it is the continuation of the coexistence line in the supercritical region
- ▶ line where the **maxima of different response functions** touch each other asymptotically as  $T \rightarrow T_p$
- ▶ liquid-gas transition in water: max in isobaric heat capacity  $C_p$ , isothermal compressibility, isobaric heat expansion, etc
- ▶ **DYNAMIC crossover arises from crossing the Widom line!**  
water: Xu et al, PNAS 2005, Simeoni et al Nat Phys 2010



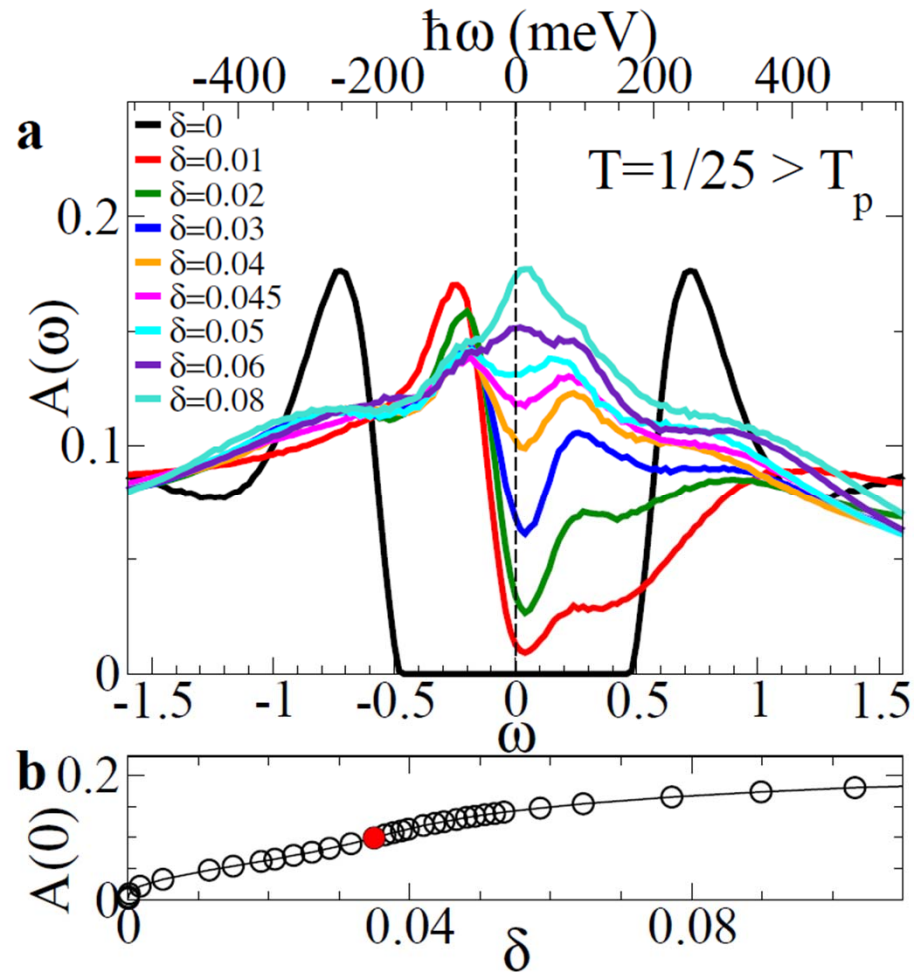
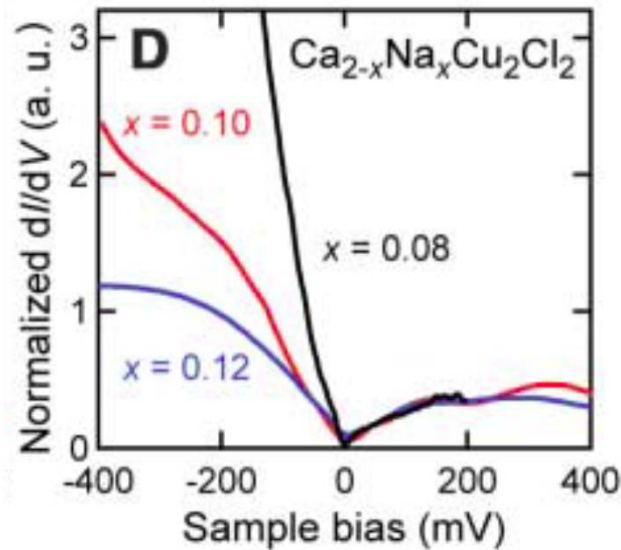
# The Widom line



# Density of states



# Density of states

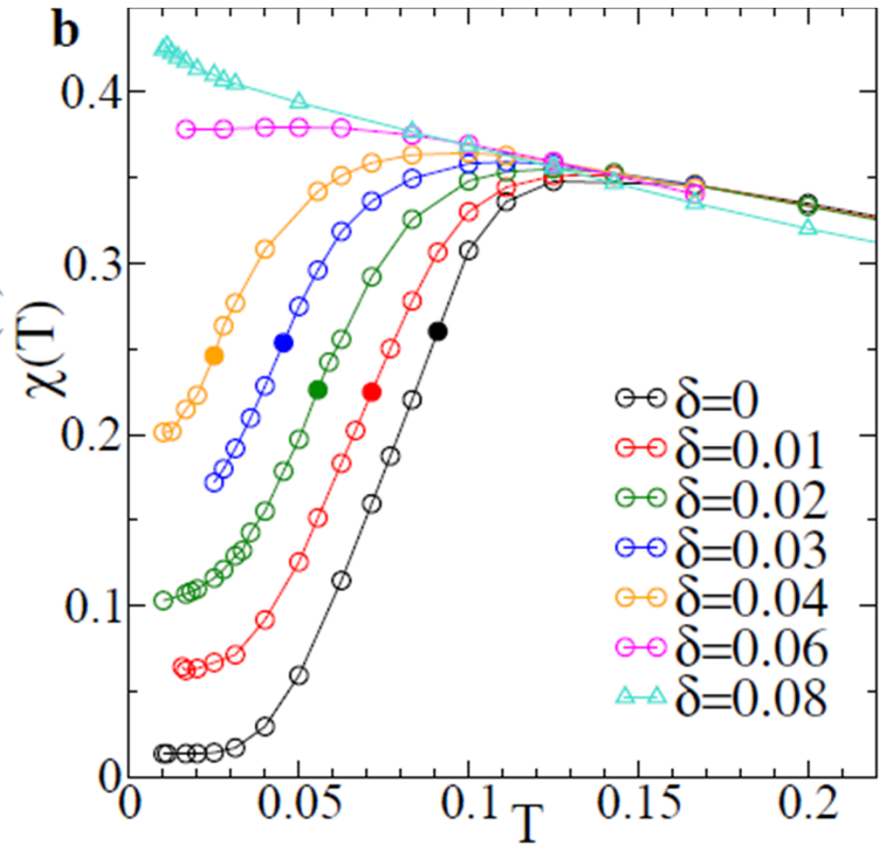
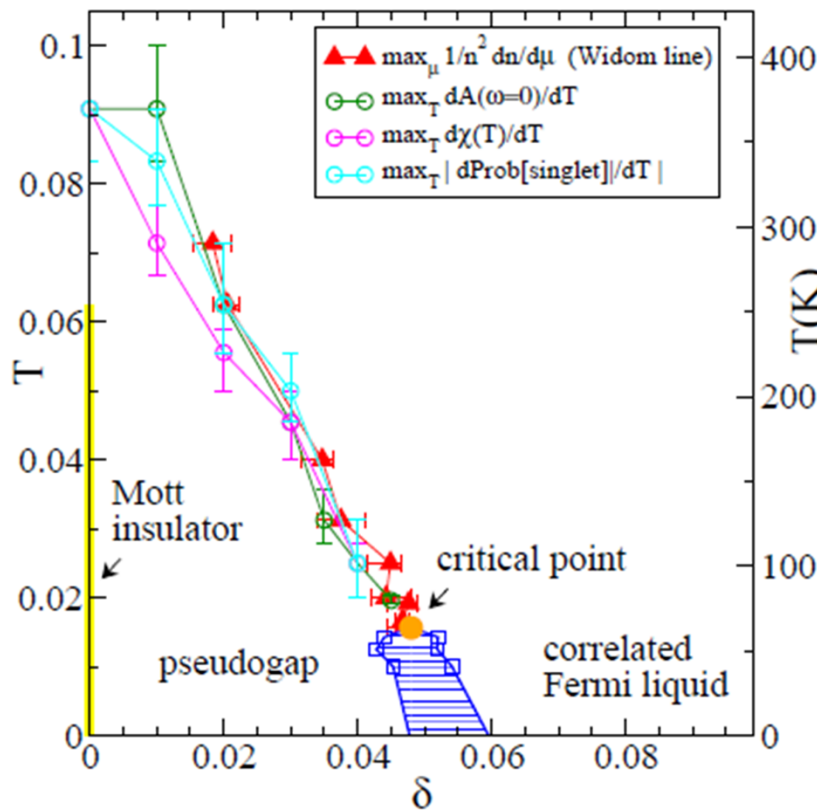


Khosaka et al. *Science* **315**, 1380 (2007);

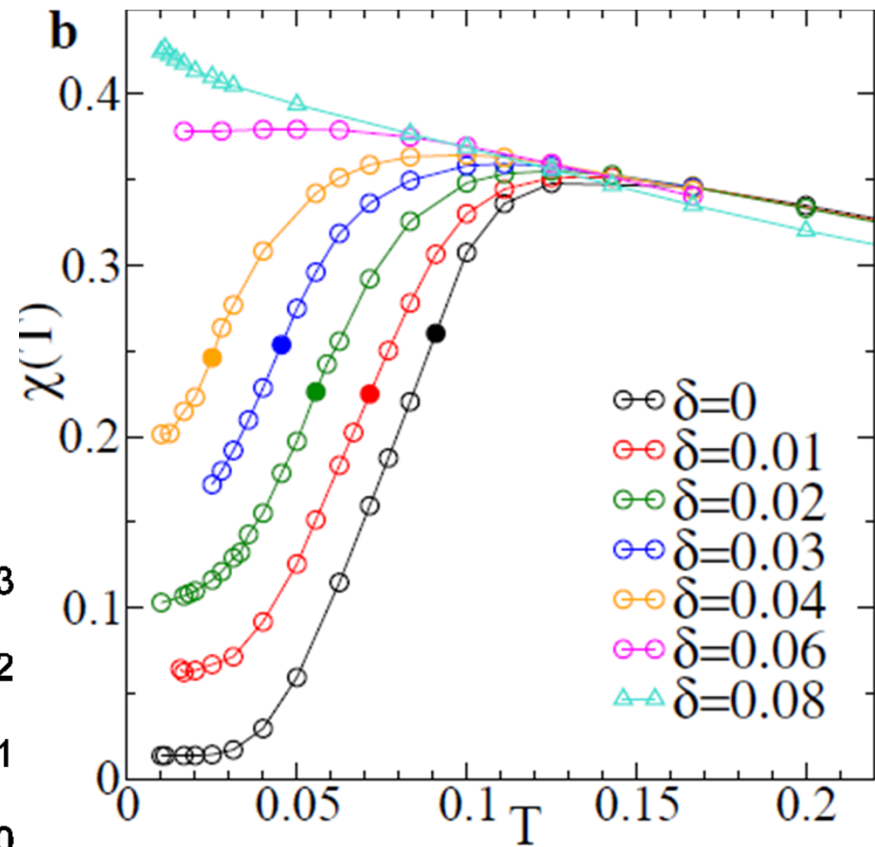
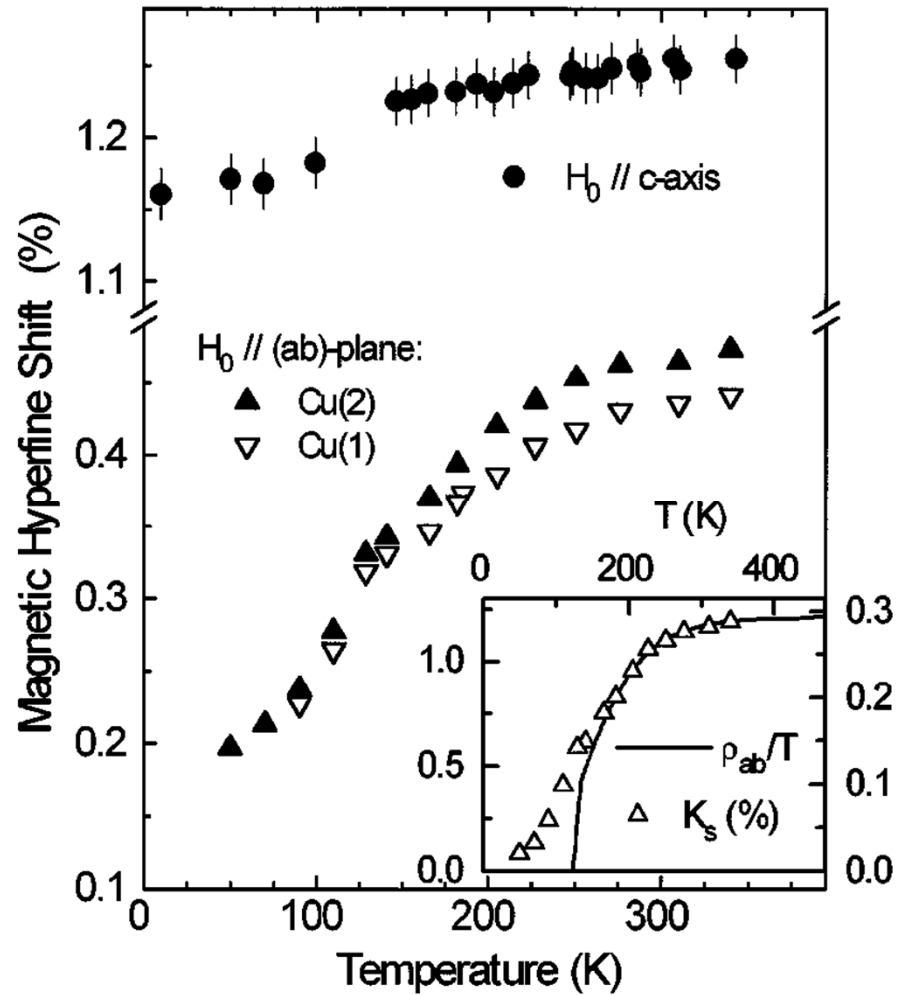




# Spin susceptibility



# Spin susceptibility



Underdoped Hg1223

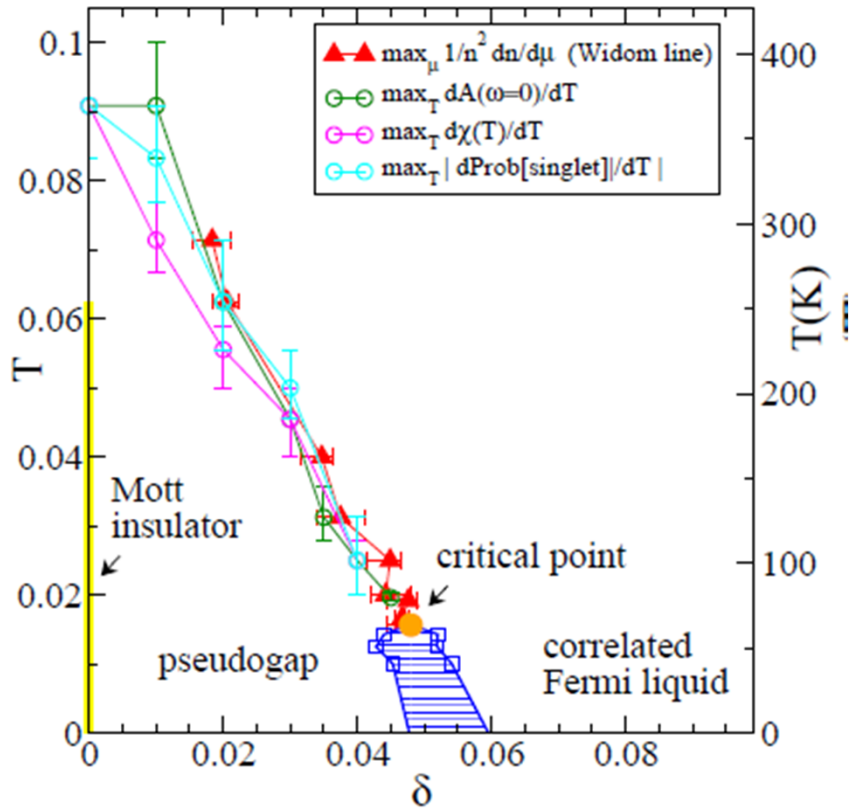
Julien et al. PRL **76**, 4238 (1996)



UNIVERSITÉ DE  
SHERBROOKE

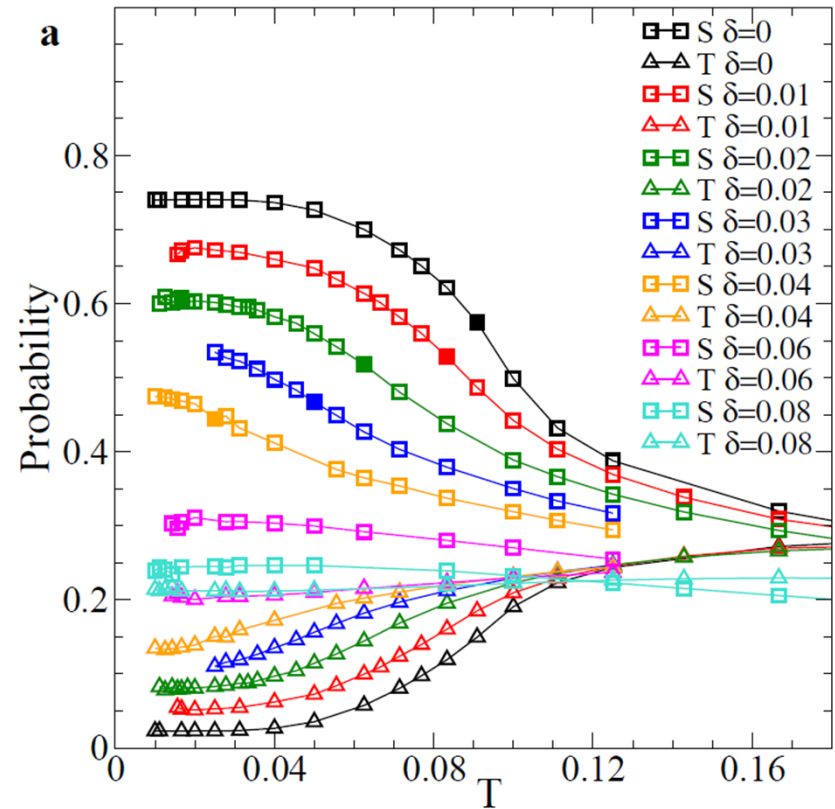
# Physics

# Plaquette eigenstates

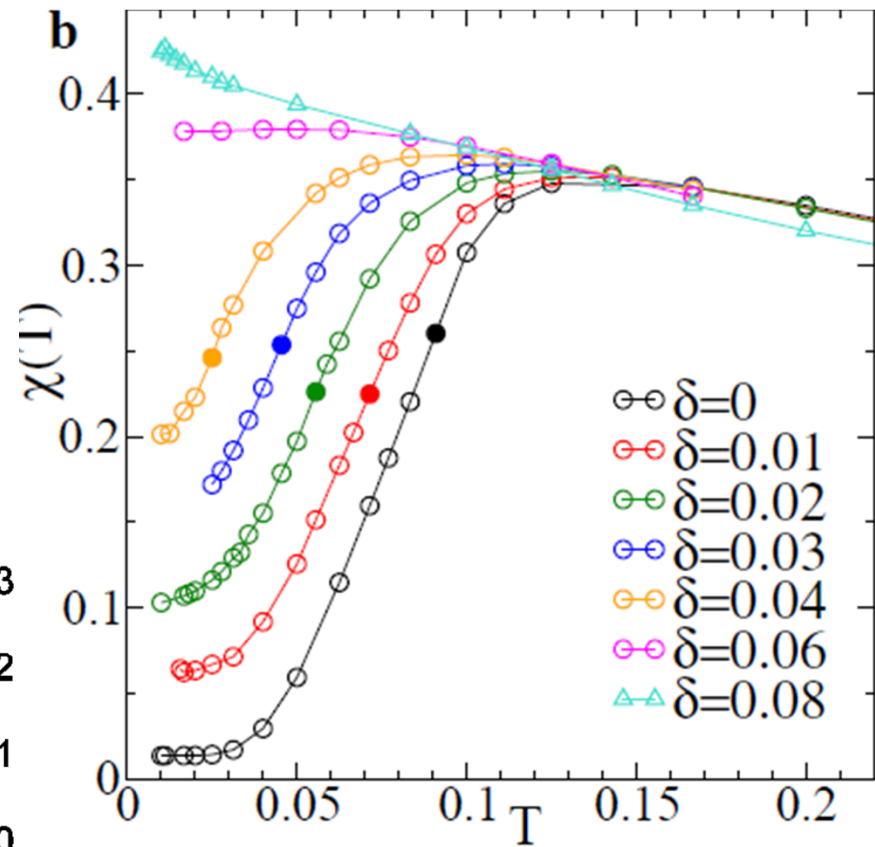
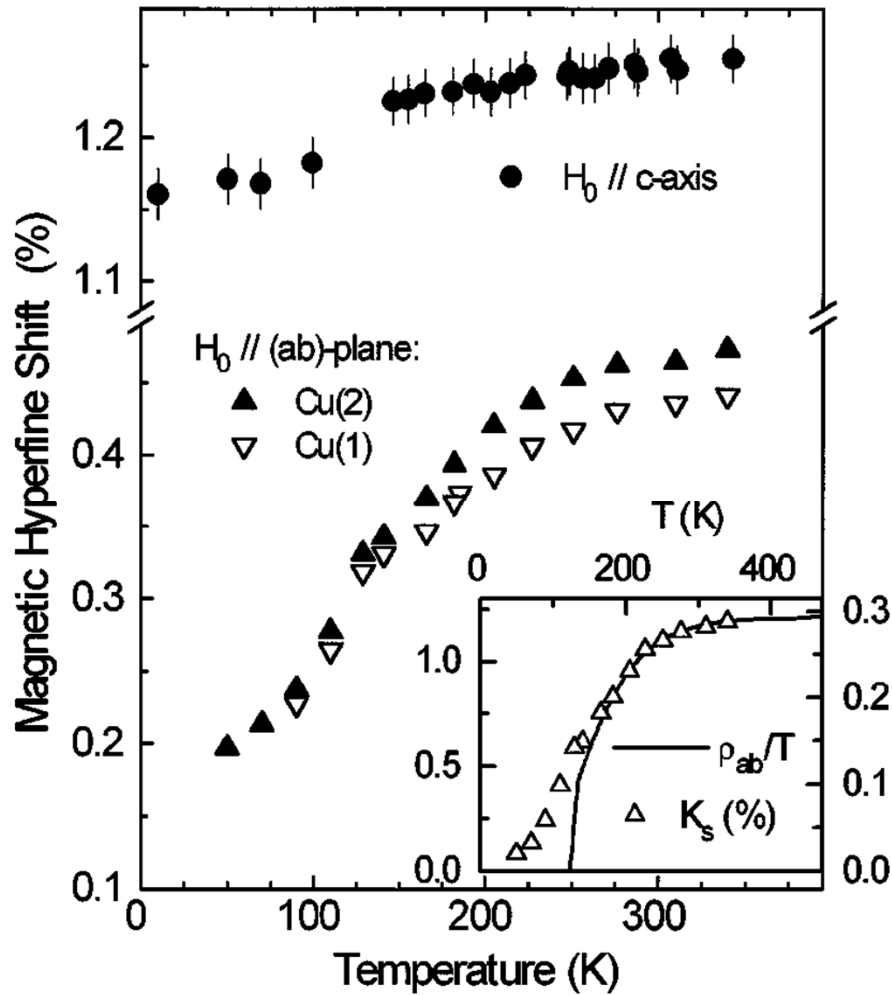


See also:

Michel Ferrero, P. S. Cornaglia, L. De Leo, O. Parcollet, G. Kotliar, A. Georges  
 PRB **80**, 064501 (2009)



# Spin susceptibility



Underdoped Hg1223

Julien et al. PRL **76**, 4238 (1996)



UNIVERSITÉ DE  
SHERBROOKE

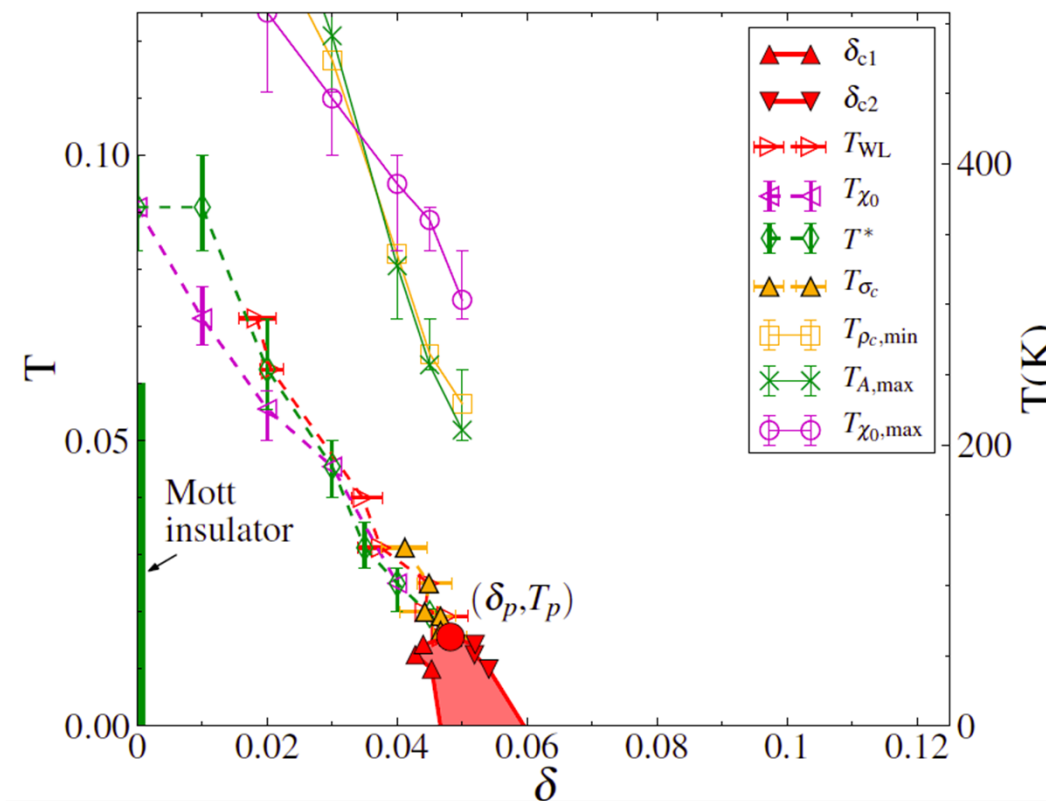


Giovanni Sordi

# Two crossover lines



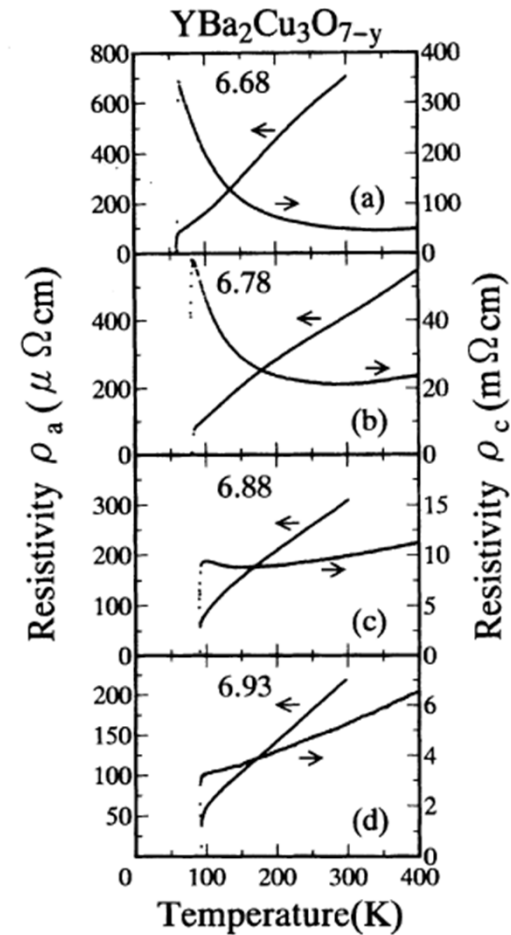
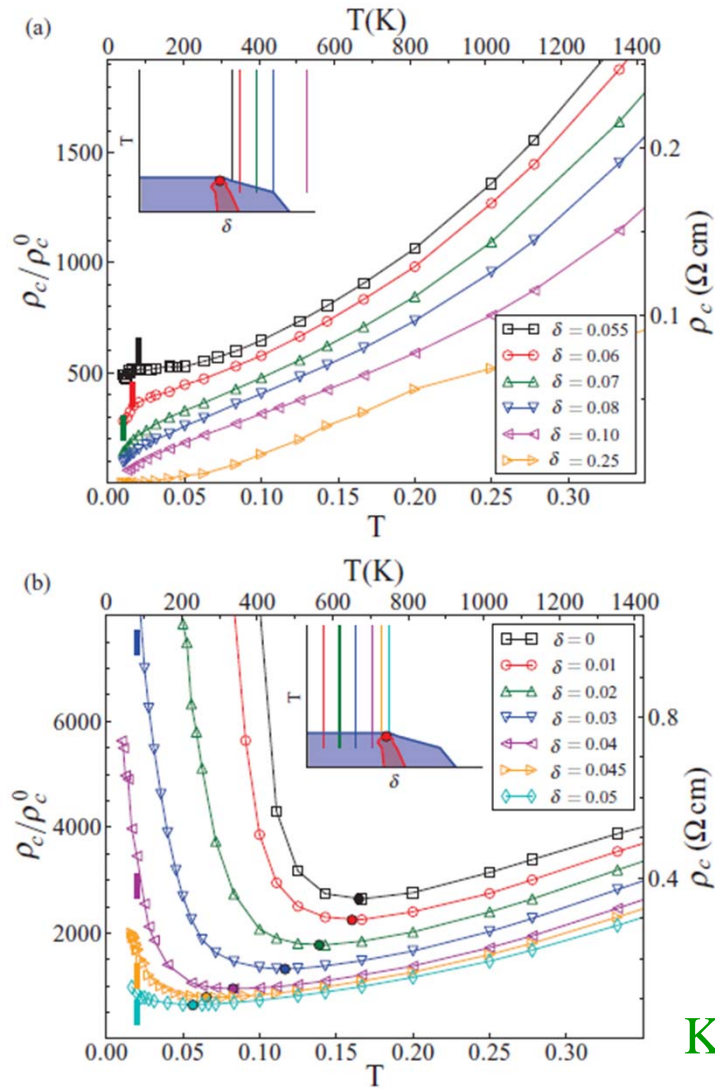
Patrick Sémon



G. Sordi et al. Phys. Rev. Lett. 108, 216401/1-6 (2012)

P. Sémon, G. Sordi, A.-M.S.T., Phys. Rev. B **89**, 165113/1-6 (2014)

# c-axis resistivity



K. Takenaka, K. Mizuhashi, H. Takagi, and S. Uchida,  
 Phys. Rev.B 50, 6534 (1994).



# What is the minimal model?

H. Alloul arXiv:1302.3473  
C.R. Académie des Sciences, (2014)

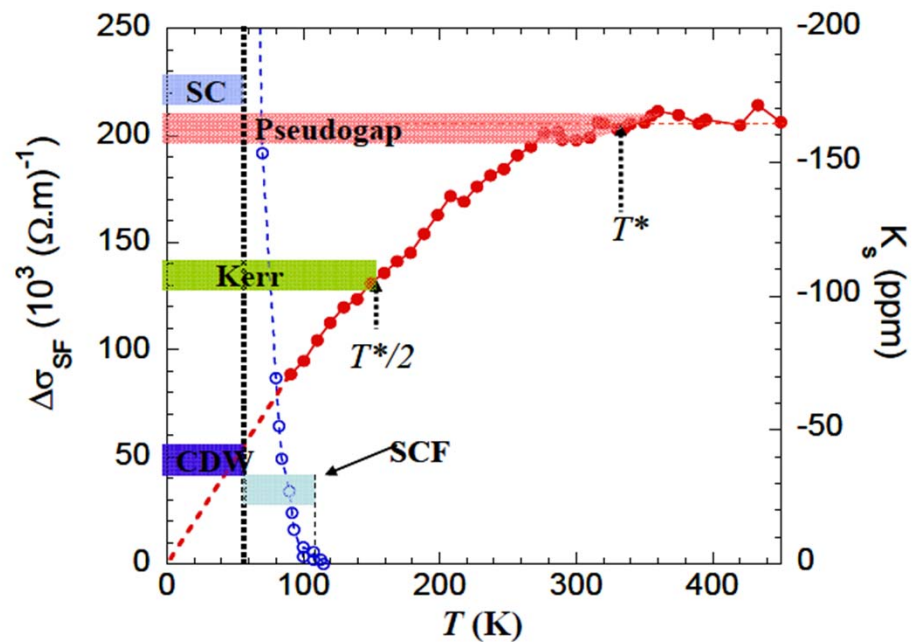


Fig 1 Spin contribution  $K_s$  to the  $^{89}\text{Y}$  NMR Knight shift [11] for  $\text{YBCO}_{6.6}$  permit to define the PG onset  $T^*$ . Here  $K_s$  is reduced by a factor two at  $T \sim T^*/2$ . The sharp drop of the SC fluctuation conductivity (SCF) is illustrated (left scale) [23]. We report as well the range over which a Kerr signal is detected [28], and that for which a CDW is evidenced in high fields from NMR quadrupole effects [33] and ultrasound velocity data [30]. (See text).





# Anisotropy (nematicity)

Normal state and large anisotropy  
in an *orthorhombic* crystal



# Underdoped metal very sensitive to anisotropy

$$\delta_\sigma = \frac{\sigma_x - \sigma_y}{(\sigma_x + \sigma_y)/2} \quad t_{x,y} = t(1 \pm \delta_0/2)$$

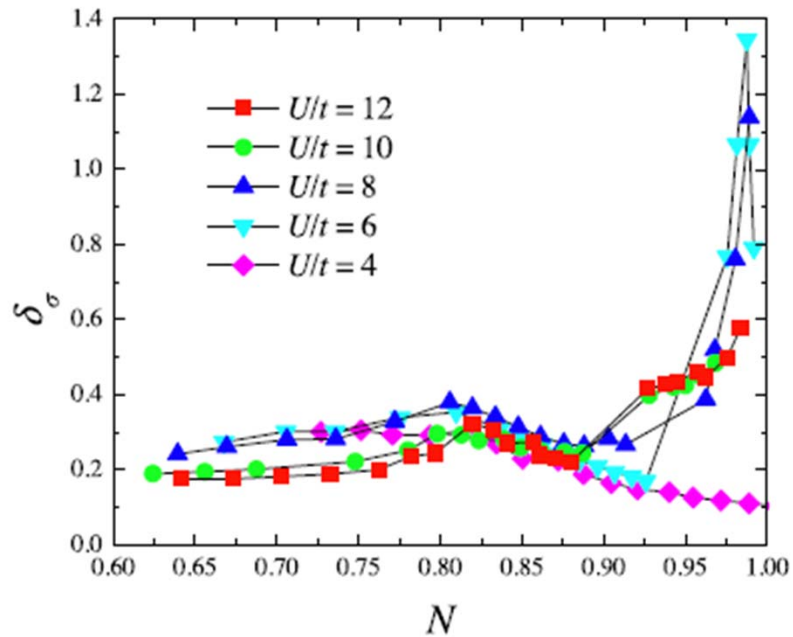
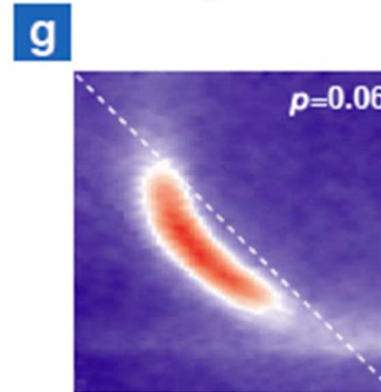
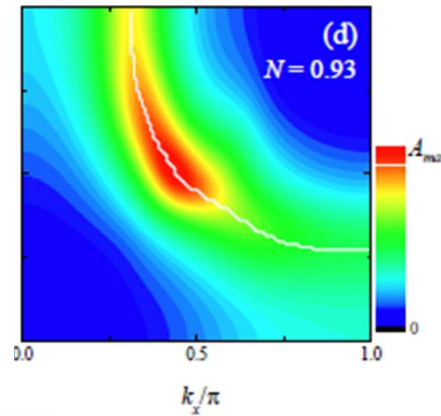


FIG. 3: (Color online) Anisotropy in the CDMFT conductivity  $\delta_\sigma = 2[\sigma_x(0) - \sigma_y(0)] / [\sigma_x(0) + \sigma_y(0)]$  as a function of filling  $N$  for various values of  $U$  and  $\eta = 0.1$ ,  $\delta_0 = 0.04$ .



Satoshi Okamoto



David Sénéchal



Okamoto, Sénéchal, Civelli, AMST  
Phys. Rev. B **82**, 180511R 2010

D. Fournier *et al.* Nature Physics ( Marcello Civelli )

# At finite temperature anisotropy in $Z$

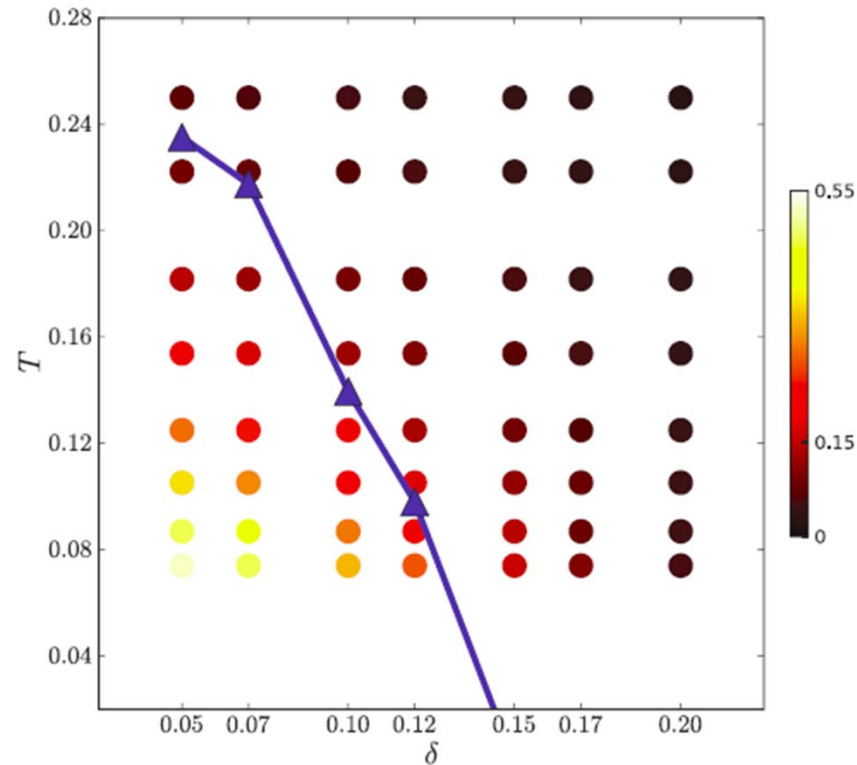


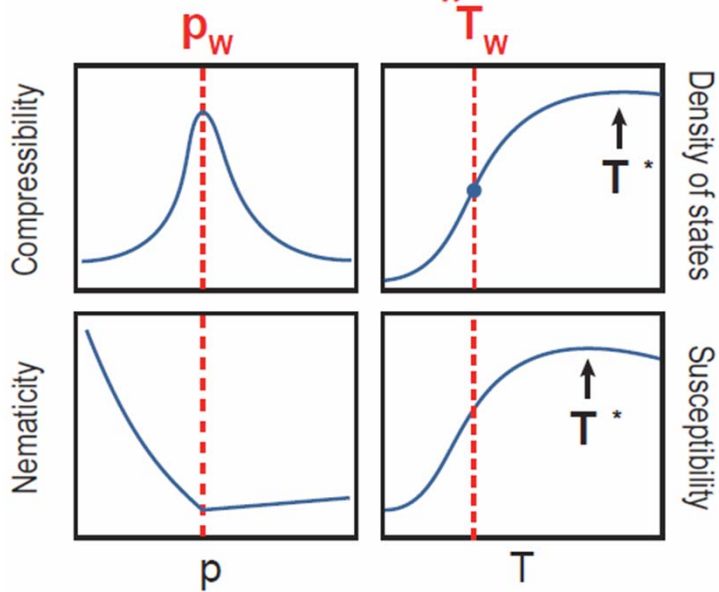
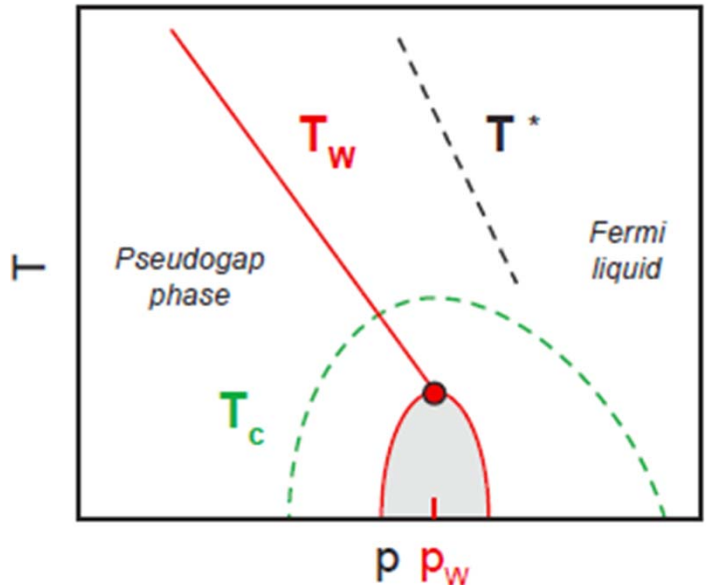
FIG. 3. (Color online) Color map of the anisotropic ratio of the quasiparticle weight  $\sigma_Z$  over the temperature-doping plane, for  $U = 6t$ . The solid blue curve indicates the pseudogap temperature  $T^*(\delta)$  which is obtained as the temperature at which the uniform magnetic susceptibility  $\chi_m[q = (0,0), T]$  has a maximum.

$$U = 6t, \text{ DCA}, 4 \times 4$$

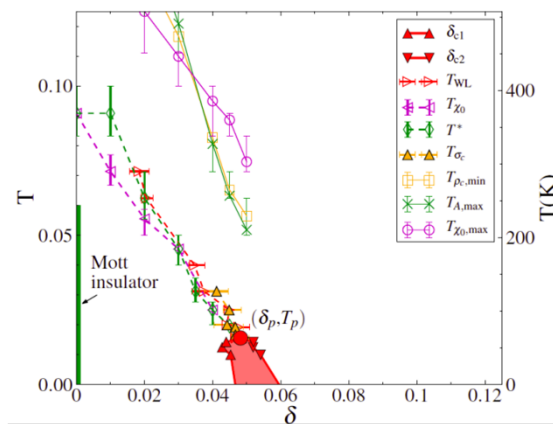
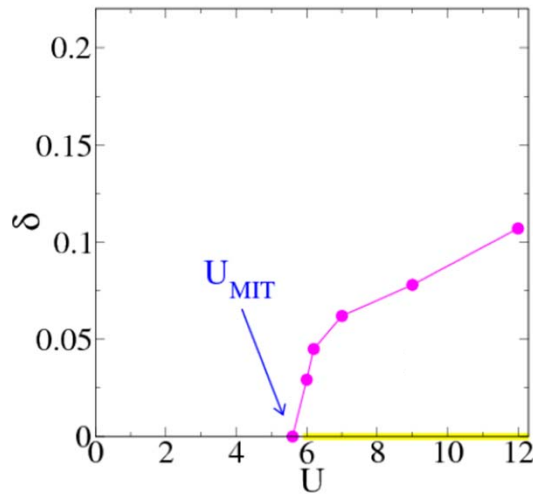
Su, Maier, PRB **84**, 220506(R) (2011)



# CDMFT: Emergent first-order transition



# Summary: normal state



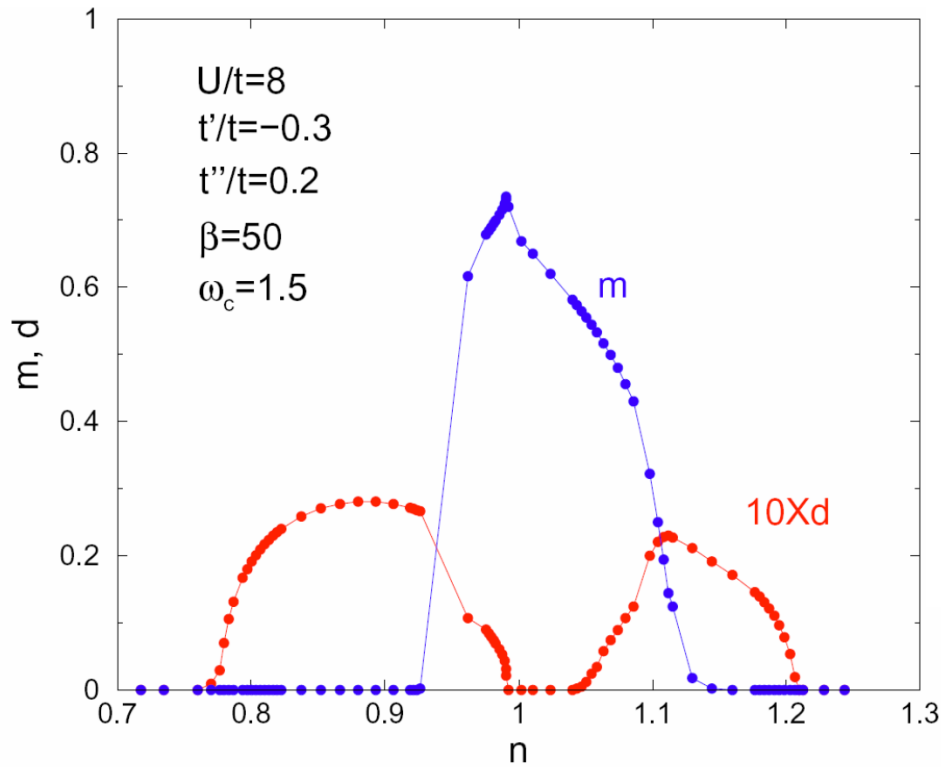
- Signatures of Mott physics extend way beyond half-filling
- Pseudogap is a phase
- Pseudogap  $T^*$  controlled by a Widom line and its precursor
- High compressibility (stripes?)
- Widom line
  - Thermodynamics (Susceptibility)
  - Transport (c-axis resistivity)
  - DOS



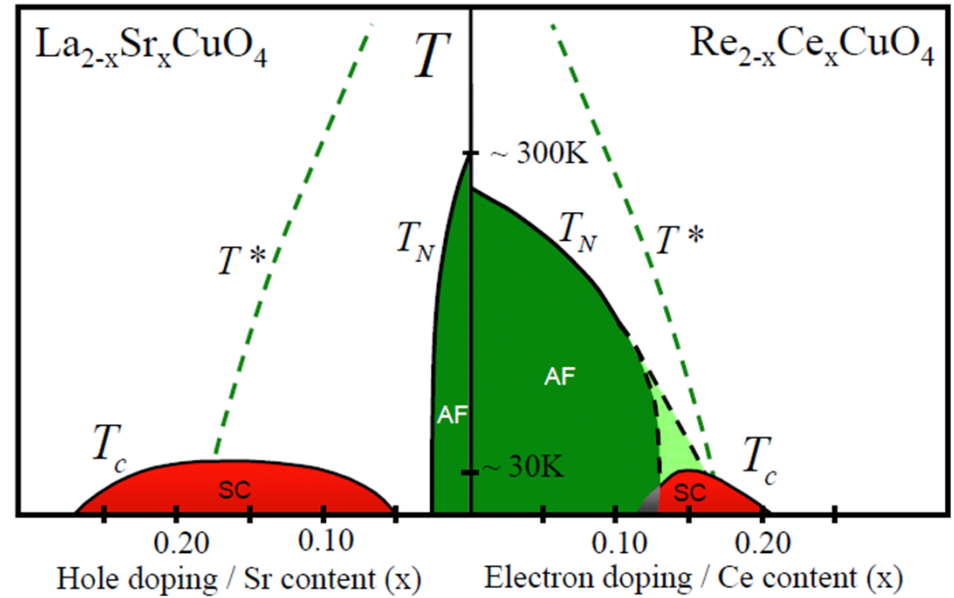
# Superconductivity



# CDMFT global phase diagram



Kancharla, Kyung, Civelli,  
 Sénéchal, Kotliar AMST  
 Phys. Rev. B (2008)  
 AND Capone, Kotliar PRL (2006)

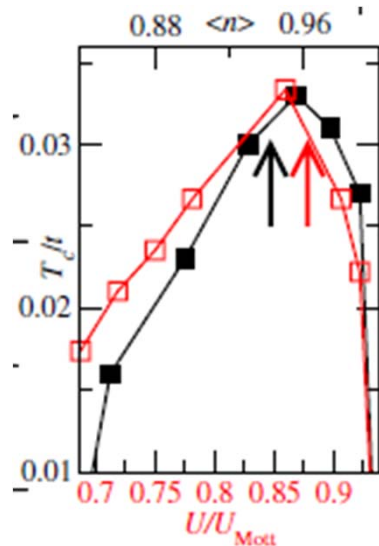


Armitage, Fournier, Greene, RMP (2009)



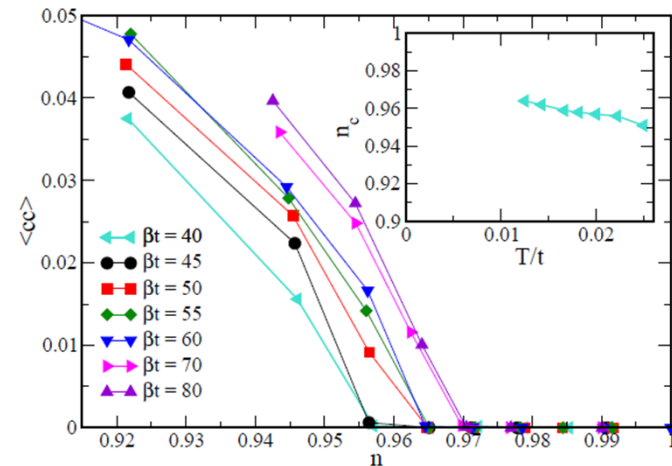
# 8 site clusters

8 site DCA,  $U=6t$



Gull Parcollet Millis  
PRL **110**, 216405 (2013)

8 site DCA,  $U=6.5t$



- In  $2 \times 2$   $T_c$  vanishes extremely close to half-filling. In larger cluster, earlier.
- Local pairs in underdoped ( $2 \times 2$ )

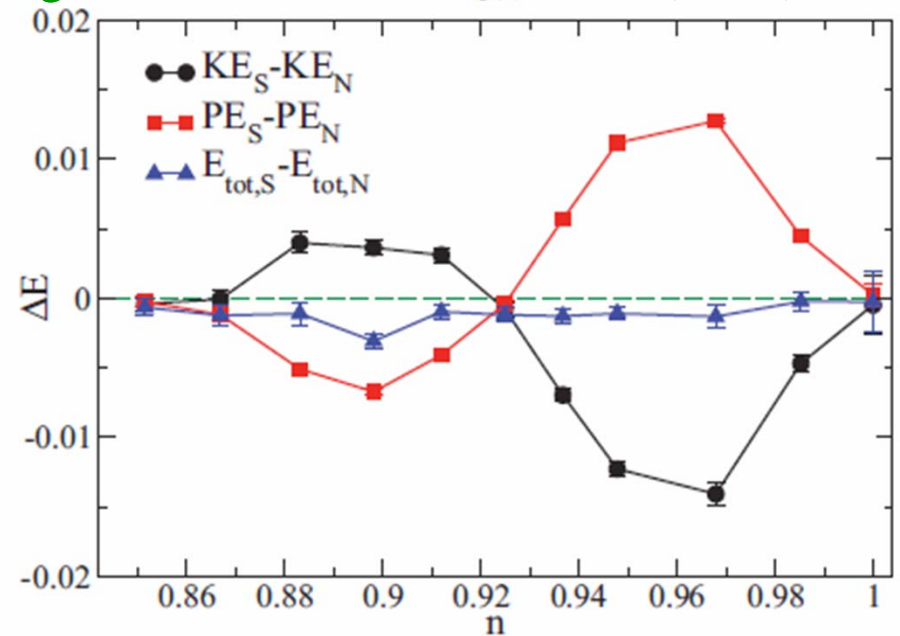
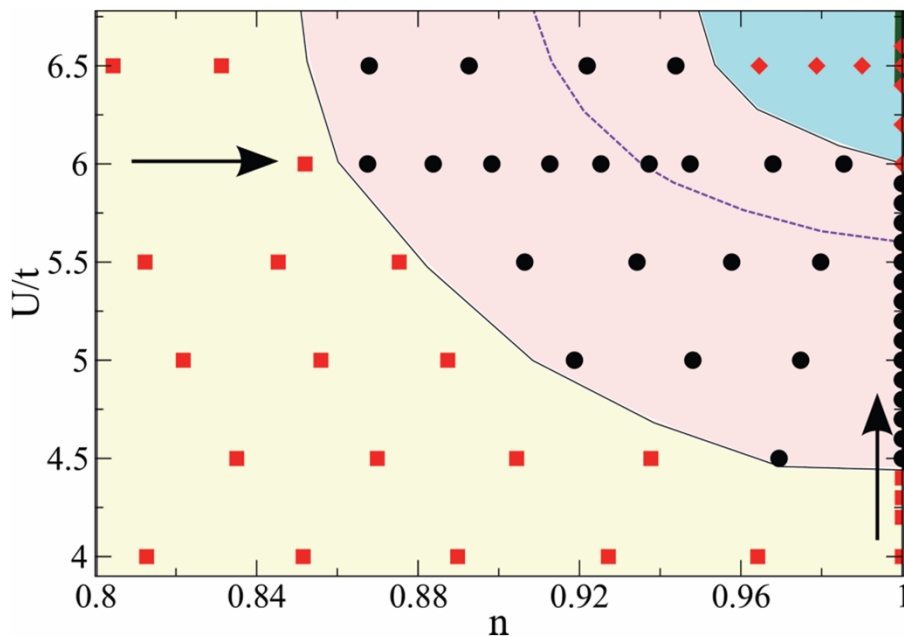


# Condensation energy

Experiments: Guy Deutscher, Phys. Rev. B 72, 092504(2005)

N. Bontemps et al. Annals of Physics 321 (2006) 1547–1558

F. Carbone, A. B. Kuzmenko, H. J. A. Molegraaf, et al, PRB 74, 064510 (2006)



$$U = 6t, \quad T = 1/60, \quad 8 \text{ sites} - DCA$$

E. Gull, A. Millis, PRB 86, 241106(R) (2012)

Th. A. Maier, M. Jarrell, et al. PRL 92, 027005 (2004)

See also

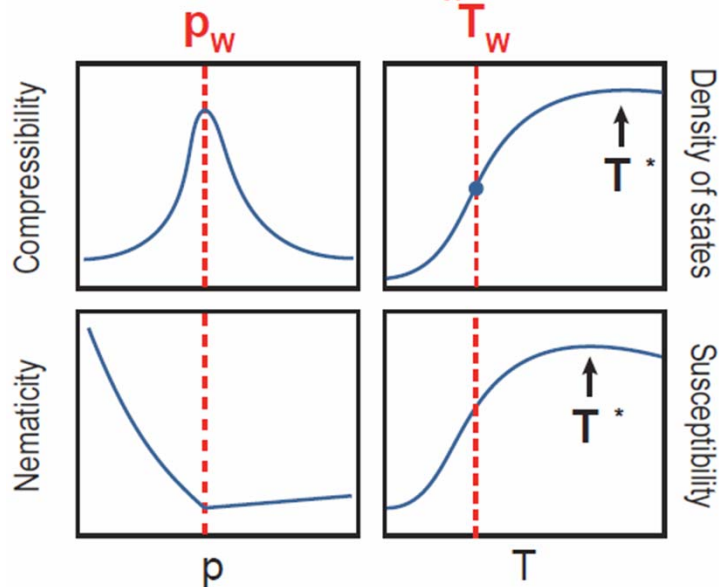
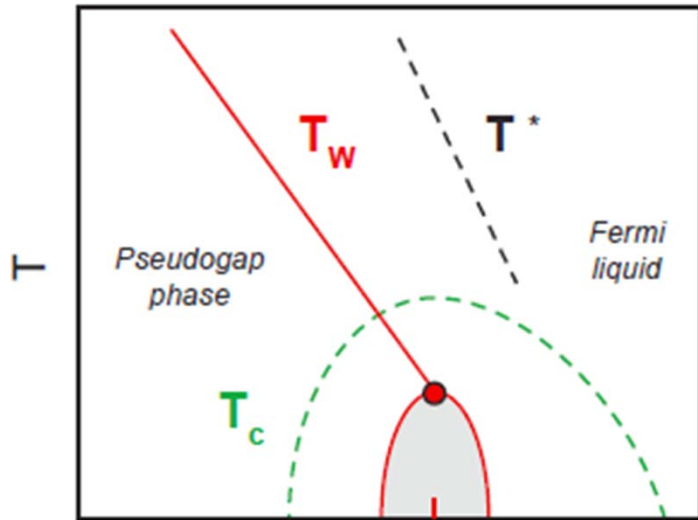
K. Haule, G. Kotliar EPL, 77 (2007) 27007



# Summary

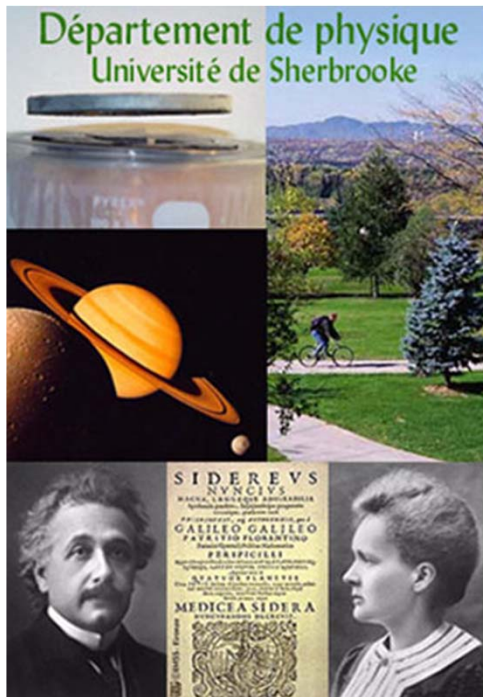


# CDMFT: Emergent first-order transition



- Is the pseudogap (PG) a crossover or a phase transition ?
- Origin of nematicity ?
- Why a dome of SC ?
- Why superconducting ?
- Does a one-band model capture the key physics ?
- Lessons from other SC?
  - Organics
  - Heavy fermions
- AFM QCP important?
- Relation between CDW and the PG ?
- Why CDW peaked at 12% doping ?

# André-Marie Tremblay



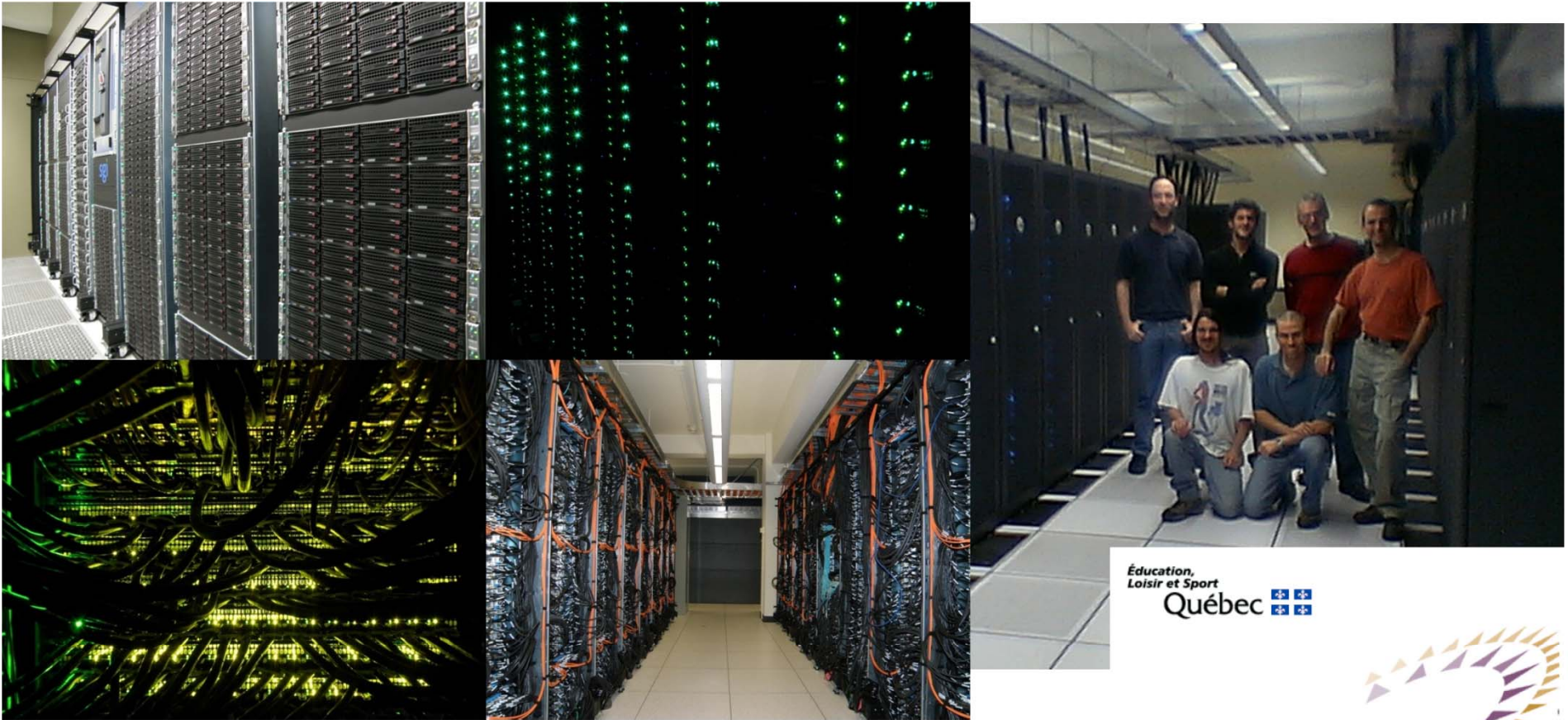
Le regroupement québécois sur les matériaux de pointe



## Sponsors:



# Mammoth



 **compute + calcul**  
CANADA

**High Performance Computing**

CREATING KNOWLEDGE  
DRIVING INNOVATION  
BUILDING THE DIGITAL ECONOMY

**Le calcul de haute performance**

CRÉER LE SAVOIR  
ALIMENTER L'INNOVATION  
BÂTIR L'ÉCONOMIE NUMÉRIQUE

  
**Calcul Québec**

  
Canada Foundation for Innovation  
Fondation canadienne pour l'innovation

 **UNIVERSITÉ DE SHERBROOKE**

Merci

Thank you