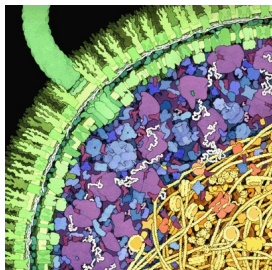


Modèles géométriques pour la prédiction des interactions macro-moléculaires

Geometric models for the prediction of macro-molecular interactions

Frederic.Cazals@inria.fr, ABS
<http://team.inria.fr/abs>



Inside Escherichia coli [D. Goodsell, The machinery of life]

Molecular interactions: function = structure (geometry) + dynamics

Protein complexes – physical chemistry 101

Modeling complexes: the machine learning approach

Modeling complexes: ab initio approaches

Conclusion

Outlook

Proteins and macro-molecular machines

Molecular interactions: function = structure (geometry) + dynamics

Protein complexes – physical chemistry 101

Modeling complexes: the machine learning approach

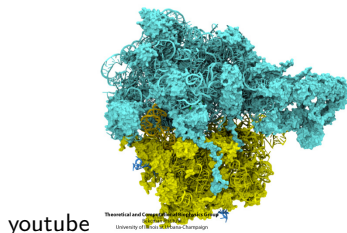
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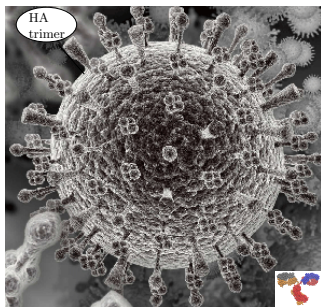
The machinery of life: protein synthesis by the ribosome

videos-science/video-ribosome-

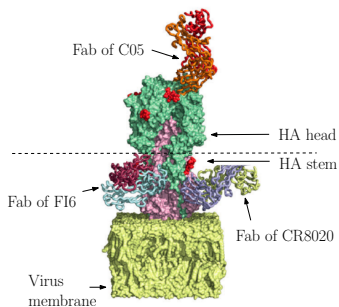


B-cell biology and antibody - antigen complexes

▷ Influenza



▷ (Broadly) neutralizing antibodies



▷ Core questions on Ig-Ag complexes

- Determinants of binding affinity
 - relationship *affinity* - *avidity* - *virus entry inhibition*
- Role of complementarity determining regions (CDRs)
- Determinants of interaction specificity

Molecular dynamics: first simulation of a protein

videos-science/video-michael-levitt-first-MD-simulation

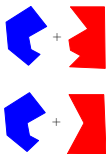


About the simulation duration, quoting M. Levitt “*Cannot remember, but likely less than 100 picoseconds*”

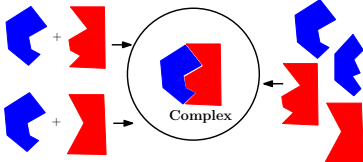
Protein interactions: docking, affinity, specificity

▷ Docking models:

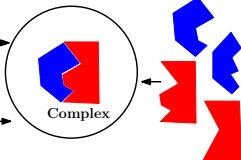
Lock-and-key
Fisher, 1894



Induced fit
Koshland, 1958

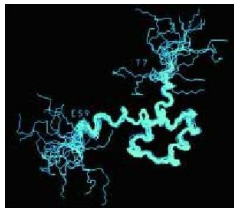


Conformer selection
Monod-Wyman-Changeux, 1965



- ▶ Lock-and-key: Fisher, 1894
- ▶ Induced fit: Koshland, 1958
- ▶ Conformer selection, Monod-Wyman-Changeux, 1965

▷ Flexibility matters



▷ Key ingredients:

– Geometry:

complementarity, conformations, flexibility

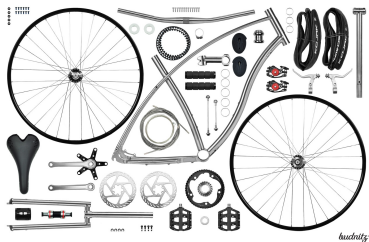
– Physics: enthalpy, entropy

▷ Major challenges (cf CAPRI):

geometry: large conformational changes

physics: entropy based affinity control

The lock and key metaphor is misleading:
function is often about dynamics



Information(spare parts)

< Information(static bicycle)

≪ Information(moving bicycle)

Proteins and macro-molecular machines

Molecular interactions: function = structure (geometry) + dynamics

Protein complexes – physical chemistry 101

Modeling complexes: the machine learning approach

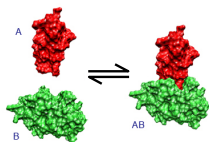
Modeling complexes: ab initio approaches

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Binding affinity: dissociation free energy

- ▶ Protein complexes rock back and forth



- ▶ Dissociation constant and dissociation free energy:

$$K_d = [A][B]/[AB]$$
$$\Delta G_d = -RT \ln K_d/c^\circ = \Delta H - T\Delta S.$$

- ▶ Binding affinities (thermodynamics):

- random complex: $K_d \sim 10^{-6}$
- high: $K_d \sim 10^{-9}$
- very high: $K_d \sim 10^{-12}$
- extreme: $K_d \sim 10^{-15}$

- ▶ Time scales (kinetics):

- short-lived complexes: 10^{-6} s (e.g. enzyme-substrate)
- stable complexes: 10^3 s (e.g. antibody-antigen)
- permanent complexes: 10^6 s (aggregates)

Binding affinity: thermodynamics

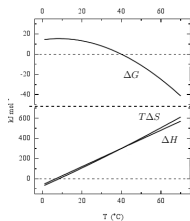
- ▷ Dissociation constant k_D for $C \rightleftharpoons A + B$:

$$K_d = \frac{[A][B]}{[C]}; \Delta G_d = -RT \ln K_d/c^\circ = \Delta H - T\Delta S. \quad (1)$$

- ▷ The enthalpy - entropy compensation:

- ▶ enhanced packing of interface atoms due to attractive forces: $\Delta H < 0$
- ▶ higher packing, restricted atomic motions: $T\Delta S < 0$

- ▷ Marginal stability of proteins and complexes:



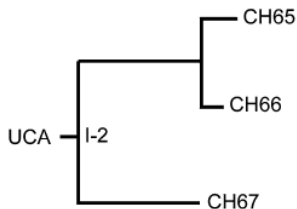
- ▶ Large ΔH and $T\Delta S$ compensate
- ▶ Crossing of curves difficult to predict
- ▶ Marginal stability is key to regulation

Pict. courtesy of Alan Cooper (Thermodynamics of unfolding)

The immune response: affinity maturation

Rigidification of CDR loops limits the entropic penalty upon binding

▷ **Antibodies:** lineage



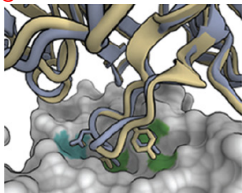
▷ **Binding affinities:** K_d analysis by SPR

Fab	K_d (μM)
UCA	118 ± 14
I-2	142 ± 15
CH65	$0.49 \pm .10$
CH67	0.36 ± 0.04

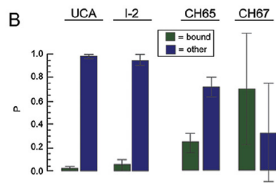
CH65 \sim CH67; wrt UCA:

$\Rightarrow \sim 200$ -fold improvement

▷ **But UCA and CH65 have similar binding modes!!!**



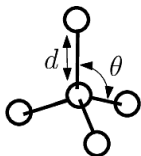
▷ **Solution:** time spent bound conformations – long MD simulations



▷Ref: Harisson et al; PNAS 110, 2013

Force fields: the potential energy of a (bio-)molecular system

▷ The $3n - 6$ degrees of freedom of a molecule:



- types for atoms (element, bonds)
- covalent: bond lengths, angles
- non covalent: pairwise distances
- solvent model

▷ Potential energy:

$$U_{\text{total}} = E_{\text{bond}} + E_{\text{angle}} + (E_{\text{proper}} + E_{\text{improper}}) + (E_{\text{vdw}} + E_{\text{electro}}) \quad (2)$$

E_{bond} : bonds

E_{angle} : covalent angles

E_{proper} : proper dihedrals

E_{improper} : improper dihedrals

E_{vdw} : van der Waals

E_{electro} : electrostatics

▷ Examples:

▶ AMBER: $S_u = (73, 133, 112, 3, 14, 758)$

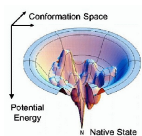
1093 unique parameters

▶ CHARMM: $S_u = (85, 152, 209, 13, 33, 1)$

493 unique parameters

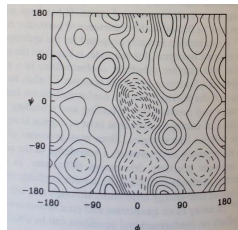
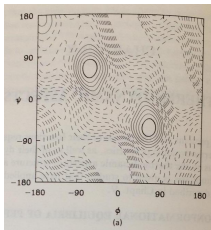
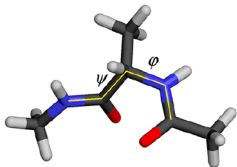
▶ MARTINI: $S_u = (16, 4, 0, 2, 21, 3)$

46 unique parameters



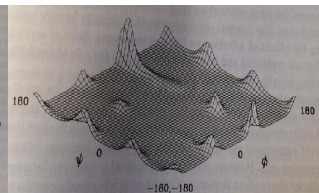
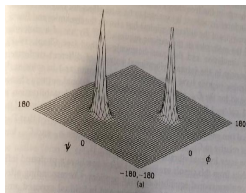
Potential energy landscapes: illustration

▷ Potential energy map: vacuum versus solvated



▷ Corresponding Boltzmann-weighted probability maps:

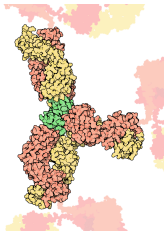
- Solvent stabilizes many more conformers—hydrogen bonding.
- Dramatic incidence of the PES and FES.



▷Ref: Petitt, Karplus, Chem. Phys. Lett., 121, 1985

Binding affinity: direct calculation

▷ A standard antibody-antigen complex:



▷ Model without solvent:

- ▶ FAB of antibody ~ 3000 atoms
- ▶ Antigen (lysozyme) ~ 1000 atoms
- ▶ One conformation: 1 point in $\mathbb{R}^{3 \times 4000}$

▷ ΔG_d as a multidimensional integral:

$$\Delta G = -\frac{1}{\beta} \ln \left(\frac{1}{8\pi^2} \frac{C_A C_B}{C_{AB}} \frac{\int e^{-\beta U(r_{AB})} dr_{AB}}{\int (e^{-\beta U(r_A)} dr_A) (\int e^{-\beta U(r_B)} dr_B)} \right) \quad (3)$$

▷ Ref: Woo and Roux, PNAS 102 (19), 2005

Free energy, density of states, and volume calculations

▷ Density of states

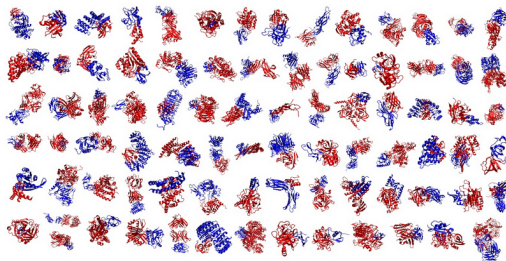
▷Ref: Dyer, Freeze, Kannan, J. ACM 38(1), 1991

▷Ref: Lovász, Vempala, J. Comput. Syst. Sci., 71(2), 2006

▷ Volume of polytopes: hardness

Protein interactions: the structure affinity benchmark

<http://bmm.cancerresearchuk.org/~bmmadmin/Affinity/>



▷ **Dissociation constant vs affinity**

$$\Delta G_d = -RT \ln K_d/c^\circ$$

▷ **NB:** in general, bound partners only do not suffice to get accurate predictions

▷ **144 protein complexes**

17 IG - Ag complexes

▷ **Binding affinity known:** ITC, SPR

caveat: order of magnitude matter (pH, ion strength, ...)

▷ **Three crystal structures known:** bound complex + 2 unbound partners

▷ Ref: Kastritis et al; Protein Science (20), 2011

Estimating K_d : two routes

- ▶ Learning: regression
 - ▶ Databases of crystal structures + affinity measurements
 - ▶ Regression models involving relevant variables
- ▶ From first principles
 - ▶ Atomic models of the partners
 - ▶ A force field and a thermodynamic sampling algorithm

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Binding affinity estimation as a regression problem

▷ Regression:

- ▶ Regression: predicting the value of a continuous (dependent) variable from the values of other (independent) variables.
- ▶ ΔG is the dependent variable
- ▶ Many types of regressors: least squares, regularized least squares, k nearest neighbours, regression trees, multivariate adaptive splines, ...

▷ Adequate variables: two classes of methods

- ▶ Large collections of parameters coding distances, biochemical properties (H-bonds, properties of a.a.), conservation of a.a., etc.
NB: requires a close monitoring to avoid overfitting.
- ▶ A small number of them: more precise encoding of enthalpy and entropy related quantities.

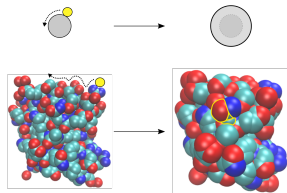
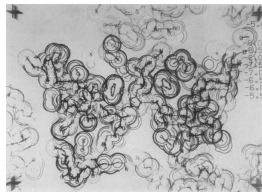
▷ Overfitting and sparsity

- ▶ Variable selection and regularization via the LASSO
- ▶ Sparse model enumeration + cross validation

Solvent Accessible Models: the birth

"The successful elucidation of the structure of a protein by single-crystal diffraction procedures provides a list of atomic co-ordinates whose reliability will vary in different parts of the molecule."

"The topology of the surface of a protein is intimately related to its function; parts of the surface are directly involved in interactions with other molecules; the solvent- protein interface is almost certainly related to the structure of the native molecule; and the chemical reactivity of the various functional groups will depend on their relation to this interface."



▷Ref: Lee and Richards, JMB, 3 (55), 1971

▷Ref: M.L. Connolly, J. Appl. Crystallography, 1983

▷Ref: Akkiraju and Edelsbrunner, Discrete Appl. Math., 1996

Solvent Accessible Models: the rise

From Chotia, *Structural invariants in protein folding*:

“An analysis of 15 protein structures indicates: First, the loss of accessible surface area by monomeric proteins on folding—proportional to hydrophobic energy—is a simple function of molecular weight; second, the proportion of polar groups forming intramolecular hydrogen bonds is constant; and third, protein interiors are closely packed, each residue occupying the same volume as it does in crystals of amino acids.”

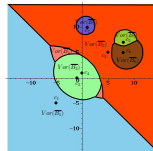
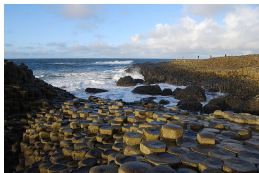
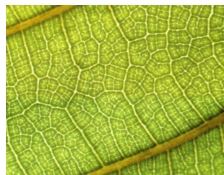
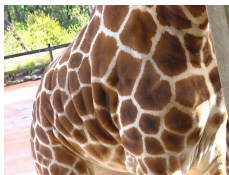
From Janin, *Principles of protein–protein recognition*:

“The formation of the protein–protein interface by the insulin dimer, the trypsin-PTI complex and the $\alpha\beta$ oxyhaemoglobin dimer removes 1,130–1,720 ² of accessible surface from contact with water. The residues forming the interface are close packed: each occupies the same volume as it does in crystals of amino acids. These results indicate that hydrophobicity is the major factor stabilising protein–protein association, while complementarity plays a selective role in deciding which proteins may associate.”

▷Ref: Chothia, Nature 254, 1975

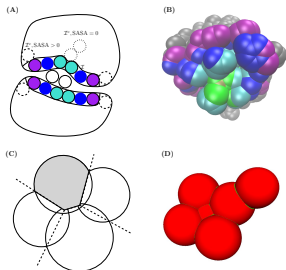
▷Ref: Janin, Nature 256, 1975

Voronoi diagrams in Biology, Geology, Engineering



Our parameters: overview

► **Our variables:** proxies for enthalpy and (vibrational) entropy variations upon binding, the latter based on packing properties



► **Or particular interest**

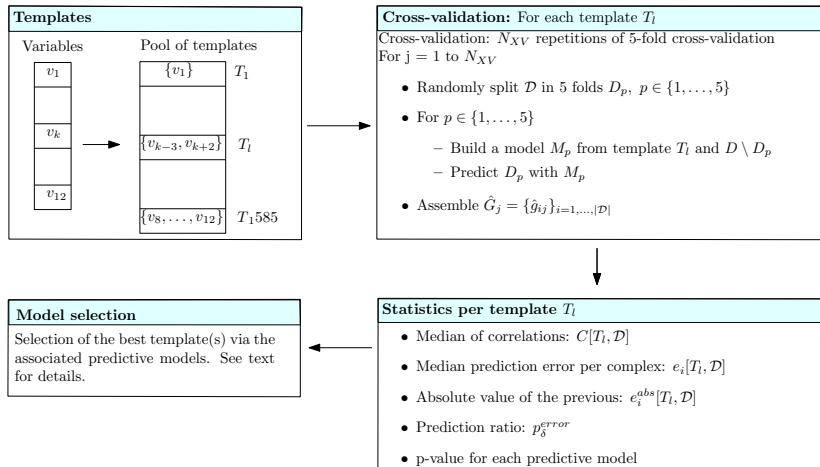
- **IVW-IPL:** inverse volume-weighted internal path length
- **NIS^{charged}:** fraction of charged residues on the non-interacting surface (NIS)

- **(A)** Binding patch and labeling of interface atoms The non interface atoms (\mathcal{I}^c) are split into those which retain solvent accessibility ($SASA > 0$, dashed balls), and those which do not ($SASA = 0$, dotted balls)

NB: **Buried Surface Area** or **BSA**: area of colored spherical caps

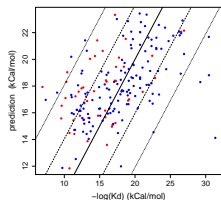
- **(B)** Shelling order of an atom: smallest number of atoms traveled to reach an exposed non interface atom, i.e. an atom belonging to \mathcal{I}^c and with $SASA > 0$ (in grey)
- **(C,D)** Atomic packing: via Voronoi volumes

Statistical methodology

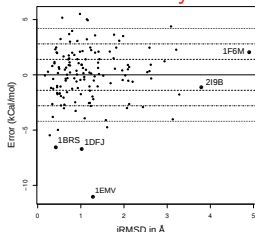


Results on the structure affinity benchmark

▷ Predictions vs measurements



▷ Hardness vs flexibility



▷ State-of-the-art binding affinity estimates on the SAB:

- Whole SAB: K_d within one and two OOM in 48% and 79% of cases
- high resolution (2.5Å): K_d within one and two OOM in 62% and 89%
- Absence of correlation between prediction hardness and protein flexibility

▷ References:

- 1 OOM (order of magnitude) \Leftrightarrow 1.4 kcal/mol
- kT per molecule, or RT per mole at room temperature: 0.6 kcal/mol
- ΔG_d , exp. errors \sim 0.3 kcal/mol

Proteins and macro-molecular machines

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Protein complexes – physical chemistry 101

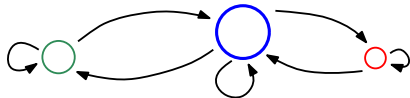
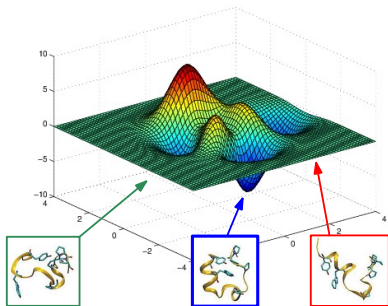
Modeling complexes: the machine learning approach

Modeling complexes: ab initio approaches

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Emergence of function from Structure – Thermodynamics – Dynamics



Potential Energy Landscape

- large number of local minima
- enthalpic barriers
- entropic barriers

Structure: stable conformations i.e. local minima of the PEL

Thermodynamics: meta-stable conformations i.e. ensemble of conformations easily inter-convertible into one - another.

Dynamics: transitions between meta-stable conformations e.g. Markov state model

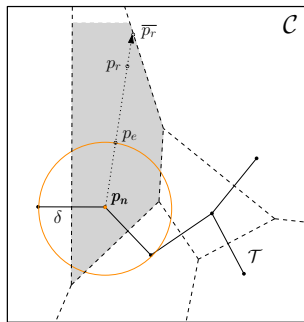
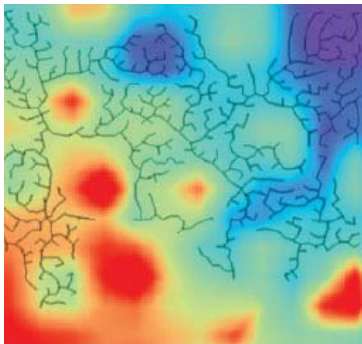
Contributions discussed

- ▶ (Structure) Sampling potential energy landscapes
- ▶ (Thermodynamics) Simplifying potential energy landscapes

Exploring Potential Energy Landscapes:

transition based rapidly exploring random trees (T-RRT)

- ▷ **Goal:** sample basins and transitions
- ▷ **Algorithm growing a random tree favoring yet unexplored regions**
 - node to be extended selection: *Voronoi* bias
 - node extension: interpolation + Metropolis criterion (+temperature tuning)
- ▷ **Limitation:** oblivious to local minima

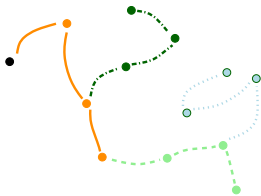


▷Ref: LaValle, Kuffner, IEEE ICRA 2000

▷Ref: Jaillet, Corcho, Pérez, Cortés, J. Comp. Chem., 2011

Exploring energy landscapes: *a generic approach yielding BH, T-RRT,...*

- ▶ **Input:** potential energy function with million, billion, trillion of local minima
- ▶ **Goal:** enumerate low energy + persistent local minima
- ▶ **Hybrid algorithm:** alternate BH and T-RRT extensions



- ▶ **Key ingredients:**
 - ▶ Boost the exploration of yet-unexplored regions – Voronoi bias
 - ▶ Meaning-full management of distances – due to concentration phenomena
 - ▶ Favor spatial adaptation – local Metropolis-Hasting tests
- ▶ **Ref:** Roth, Dreyfus, Robert, Cazals; J. Comp. Chem.; 2015

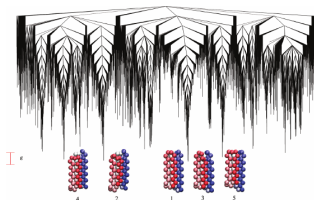
Protein model BLN69: model and force field

▷ Description:

- Three types of Beads: : hydrophobic(B), hydrophylic(L) and neutral(N)
- Configuration space of intermediate dimension: 207
- Challenging: frustrated system
- Exhaustively studied: DB of $\sim 450k$ critical points (Industry)

$$V_{BLN} = \frac{1}{2} \cdot K_r \sum_{i=1}^{N-1} (R_{i,i+1} - R_e)^2 + \frac{1}{2} K_\theta \sum_{i=1}^{N-2} (\theta_i - \theta_e)^2 + \epsilon \cdot \sum_{i=1}^{N-3} [A_i(1 + \cos \phi_i) + B_i(1 + 3 \cos \phi_i)] \\ + 4\epsilon \sum_{i=1}^{N-2} \sum_{j=i+2}^N \cdot C_{ij} \left[\left(\frac{\sigma}{R_{i,j}} \right)^{12} - D_{ij} \left(\frac{\sigma}{R_{i,j}} \right)^6 \right]$$

▷ Disconnectivity graph: describes merge events between basins



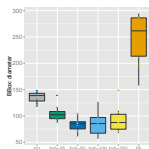
▷Ref: Honeycutt, Thirumalai, PNAS, 1990

▷Ref: Oakley, Wales, Johnston, J. Phys. Chem., 2011

Exploring energy landscapes: performances of Hybrid

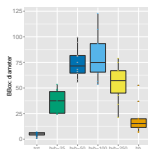
- ▷ **Contributions:** enhanced exploration of low lying regions of a complex landscape
- ▷ **Protocol:**
 - Contenders: BH, T-RRT, Hybrid for various parameter values b
 - Count and assess the local minima reported from two reference databases:
 - $BLN69 - min - all$: 458,082 minima
 - $BLN69 - min - E_{-100}$: 5932 minima.

- **Bounding box \emptyset :** all mins



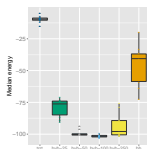
$BLN69 - min - all$

- **vs low lying**



$BLN69 - min - E_{-100}$

- **Median energies**



$BLN69 - min - all$

- ▷ **Assessment:**

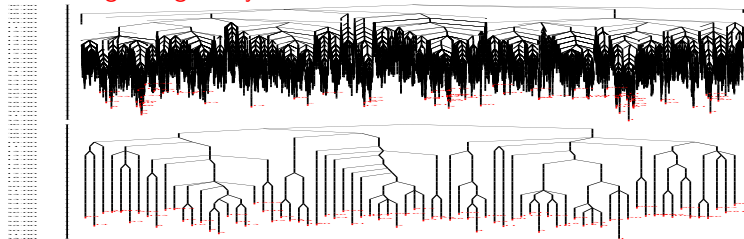
- Combines critical building blocks:
 - minimization, spatial exploration boosting, nearest neighbor searches
- Bridging the gap to thermodynamics

▷ Ref: Oakley et al; J. of Physical Chemistry B; 2011

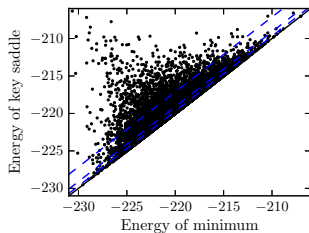
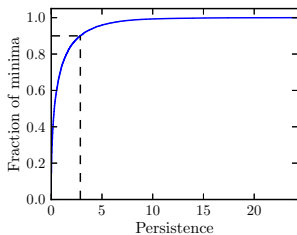
▷ Ref: Roth, Dreyfus, Robert, Cazals; J. Comp. Chem.; 2015

Binary Lennard-Jones LJ_{60}

▷ Coarse graining the system:



▷ Using the distribution of barriers' heights:



▷Ref: Carr, Mazaauric, Cazals, Wales; J. Chem. Phys.; 2016

Proteins and macro-molecular machines

Molecular interactions: function = structure (geometry) + dynamics

Protein complexes – physical chemistry 101

Modeling complexes: the machine learning approach

Modeling complexes: ab initio approaches

Conclusion

Outlook

Learning vs ab-initio approaches: different philosophy?

▷ No since the development of force fields involves:

- tuning the parameters so as to match experimental data using (small) organic molecules

NB: identical methods: optimization, cross-validation, Bayesian models

- extrapolating to bio-molecules

The Journal of Physical Chemistry Letters

Letter

Table 1. Comparison of Water Model Performance at 298.15 K, 1.0 atm^a

property	expt.	TIP3P	SPC/E	TIP4P	TIP4P-Ew	TIP4P/2005	TIP3P-FB (this work)	TIP4P-FB (this work)	iAMOEBA
$\rho/\text{g cm}^{-3}$	0.997	0.98	0.994	0.992	0.995	0.993	0.995	0.996	0.997
$\Delta H_{\text{vap}}/\text{kcal mol}^{-1}$	10.52	10.05	10.43	9.90	10.58	10.93	10.71	10.80	10.94
$\alpha/10^{-4} \text{K}^{-1}$	2.56	9.2	5.0	4.4	3.2	2.8	4.1 (1)	2.5 (1)	2.5 (1)
$\kappa_{\text{T}}/10^{-6} \text{bar}^{-1}$	45.3	57.4	46.1	60	48	46	44.5 (3)	45.2 (2)	41.1 (4)
$C_p/\text{cal mol}^{-1} \text{K}^{-1}$	18.0	18.74	18.3	18.9	19.2	19.0	19.1 (1)	19.0 (1)	18.5 (2)
$\epsilon(0)$	78.5	94	68	53	62	58	81.3 (9)	77.3 (4)	80.7 (11)
$D_{\text{H}_2\text{O}}/10^{-5} \text{cm}^2 \text{s}^{-1}$	2.29	6.05	2.97	4.05	2.83	2.59	2.28 (2)	2.21 (2)	2.54 (2)
$\eta/\text{mPa s}$	0.896	0.321	0.729	0.494	0.72	0.855	0.91 (2)	0.94 (3)	0.85 (2)
$\sigma/\text{mJ m}^{-2}$	71.8	52	63	59	65	69	64 (1)	70 (1)	69 (1)
TMD ($^{\circ}\text{C}$)	+4	-91	-36	-20	+1	+5	-12	+4 (1)	+4 (1)

^aProperties listed are density ρ , heat of vaporization ΔH_{vap} , thermal expansion coefficient α , isothermal compressibility κ_{T} , isobaric heat capacity C_p , static dielectric constant $\epsilon(0)$, self-diffusion coefficient $D_{\text{H}_2\text{O}}$, shear viscosity η , surface tension σ , and temperature of maximum density TMD. The polarizable and relatively complex iAMOEBA model (right column) is included for comparison because it was parameterized using ForceBalance and a similar data set.

▷Ref: Pande et al, The J. Phys. Chem. letters, 5 (11), 2014

What are we critically missing to enter the era of atomic level engineering?

▷ Fundamental insights into equilibrium thermodynamics require:

- potential energy: enhanced exploration algorithms
akin to shape / model learning
- free energy: enhanced multicanonical sampling algorithms
akin to high dimensional volume calculations
- dynamics: multi-scale Markov state models

▷ Countless breakthroughs in terms of applications:

- biology: understanding processes; understanding evolution
coding sequences \sim 80 millions in UniProt/TrEMBL
structures: 125,000 in the Protein Data Bank
- medicine: immunology, cancer, neurosciences,...
- material sciences
- synthetic biology

▷Ref: UniProt/Trembl: <http://www.ebi.ac.uk/uniprot/TrEMBLstats>

▷Ref: PDB: http://www.rcsb.org/pdb/static.do?p=general_information/pdb_statistics/index.html

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Hall of fame

- ▶ **More than 20 structural biology-related Nobel Prizes in 50 years:**
 - ▶ J. Kendrew and M. Perutz, chemistry 1962: *for their studies of the structures of globular proteins*
 - ▶ F. Crick, J. Watson and M. Wilkins, medicine 1962: *for their discoveries concerning the molecular structure of nucleic acids and its significance for information transfer in living material*
 - ▶ C. Anfinsen, chemistry 1972: *for his work on ribonuclease, especially concerning the connection between the amino acid sequence and the biologically active conformation*
 - ▶ K. Wutrich and J. Fenn, chemistry 2002: *for the development of methods for identification and structure analyses of biological macromolecules*
 - ▶ R. Kornberg, chemistry 2006: *for his studies of the molecular basis of eukaryotic transcription*
 - ▶ V. Ramakrishnan, T. Steitz, A. Yonath, chemistry 2009: *for studies of the structure and function of the ribosome*
 - ▶ M. Karplus, M. Levitt, A. Warshell, chemistry 2013: *for the development of multiscale models for complex chemical systems*

Methods: molecular simulation



The Nobel Prize in Chemistry 2013

Martin Karplus, Michael Levitt, Arieh Warshel

The Nobel Prize in Chemistry 2013



© Harvard University

Martin Karplus



Photo: © S. Fisch

Michael Levitt



Photo: Wikimedia Commons

Arieh Warshel

The Nobel Prize in Chemistry 2013 was awarded jointly to Martin Karplus, Michael Levitt and Arieh Warshel *"for the development of multiscale models for complex chemical systems"*.

Connexions between my talk and Prof. Boissonnat's course

C1: Modèles géométriques discrets

→ Voronoi models in various guises

C2: La puissance de l'aléa

→ Randomized constructions, Monte Carlo algorithms

C3: Le calcul géométrique

→ Robust geometric predicates and constructions

The Computational Geometry Algorithms Library – code and spirit!

C4. Génération de maillages

→ The Poisson-Boltzmann equation

C5: Courbes et surfaces

→ Surface / shape reconstruction

→ Convergence of regressors

C6: Espaces de configurations

→ Conformational spaces: exploration, planning

C7. Structures de données géométriques

→ Geometric approximation theory, geometric optimization

C8: Analyse géométrique et topologique des données

→ Topological persistence, geometric/topological data analysis

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 - ▶ Joël Janin
 - ▶ Sylvain Pion (software engineering), Dorian Mazauric (algorithms)
 - ▶ Charles Robert (biophysics), Pierre Boudinot (immunology), Félix Rey (virology)
 - ▶ PhD students: Sébastien Loriot, Tom Dreyfus, Andrea Roth, Simon Marillet, Augustin Chevallier, Romain Tetley
- ▶ Inria ... Algorithms-Biology-Structure is already 10 years old