



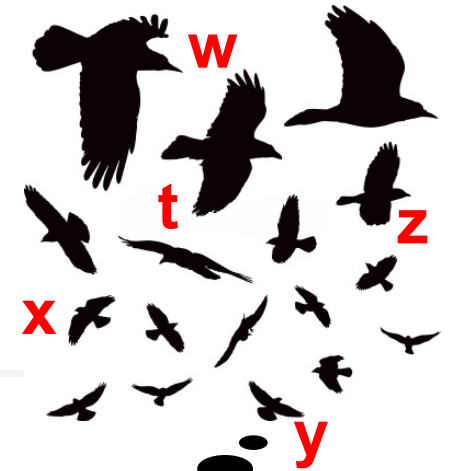
Challenges in Population Protocols

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Colloquium on Distributed Algorithms
Collège de France, 2019

Population Protocols (PP)

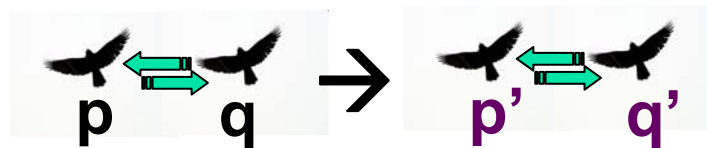
[Angluin et al. PODC'04, DC'06]



- Collection (*population*) of computational *agents*
 - of unknown size n
 - uniform (indistinguishable)
 - finite state, independent of n (constant)
 - anonymous
- Interacting
 - in asynch. and unpredictable way
 - in pairs, while exchanging and updating their states according to a *transition function*



Transition
 $(p, q) \rightarrow (p', q')$



- Example of a protocol:
compute a global property (predicate/function)
eventually on the input values of the agents
 - E.g., whether 10% of the population have an elevated input value?

predicate $P(x, y, z, w, \dots)$

Motivating scenarios

- **Passively mobile sensor networks**

- ZebraNet [ASPLOS'02] (wildlife tracking)
- EMMA [WCMC'07] (pollution monitoring)



- **Social networks**
propagation of:

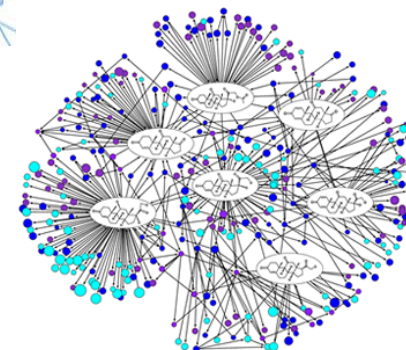
- trust [Diamadi, Fischer WU.J.Nat.Sci.01]
- rumors [Daley, Kendall J.Inst.Math.Appl.65]
- epidemics [Bailey,75] [Herbert et al, SIAM'00]



- **Chemical Reaction Networks**

dynamics of well mixed solutions

[Gellespie 77], [SoloveichikCookWinfreeBruck 08], [Doty SODA'2014]

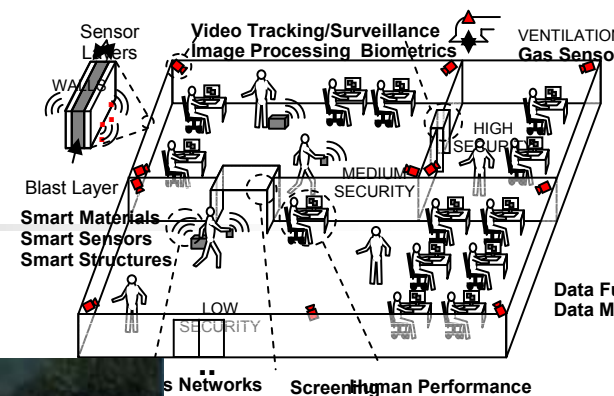
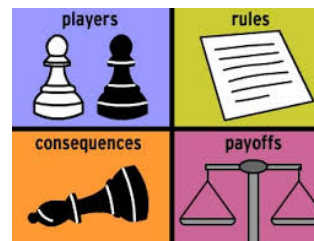


Small fraction of the Organic Chemistry Network (~0.001%). Here, the nodes represent chemical compounds, which are connected by directed arrows representing chemical reactions.

- **Game Theory**

repetitive games of n-participants

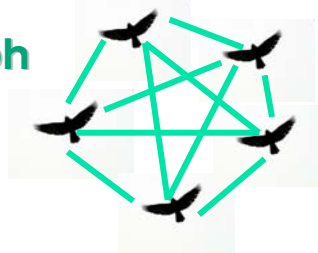
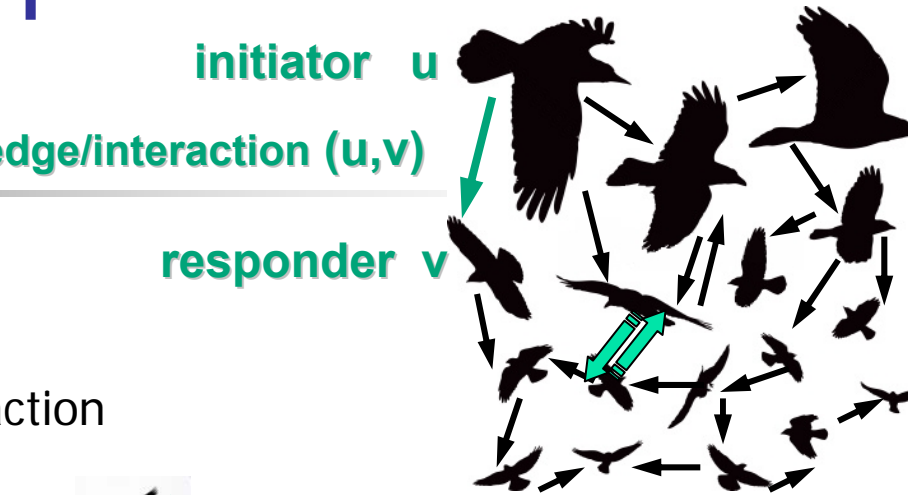
[Bournez, Chalopin, Cohen, Koegler, Rabie OPODIS'11]



Interaction graph and fairness

Interaction Graph

- nodes = agents
- edge (u,v) = possible interaction
- weakly connected
- Frequently a **complete graph**



Fairness

- Weak
each pair of agents interacts infinitely often
- Global
infinitely often reachable *configuration*
is reached infinitely often
- Probabilistic
each pair interacts uniformly at random

A vector of states
of all the agents

Probabilistic Fairness → Global Fairness w.p.1



Main complexity measures in PP

Space complexity: in number of different possible **memory states** of an agent

Time complexity with probabilistic fairness: in terms of expected ***parallel interactions*** (1 parallel = n consecutive interactions) ***until stabilization*** (to the correct output/behavior)

PP – Minimalist Model

- PP compute a predicate $P \Leftrightarrow$
 P is **semi-linear** eq. 1st order formula in
Presburger arithmetic [Angluin et al. DC'07]*

predicate $P(x,y,z,w,\dots)$



- * holds even with $o(\log \log n)$ memory bits
[Chatzigiannakis, Michail, Nikolaou, Pavlogiannis,
Spirakis TCS'11]



PP – Minimalist Model

- **Termination is impossible** (only eventual stabilization)
- **Fault-tolerance is limited:**
 - $O(1)$ crash and transient faults can be tolerated [Delporte-Gallet, Fauconnier, Guerraoui, Ruppert DCOSS'06]
 - Any number of transient faults (self-stabilization) is frequently impossible to tolerate (leader election [Cai, Izumi, Wada TCS'12], phase clock [Beauquier, Burman DCOSS'10], counting [Beauquier, Clement, Messika, Rosaz, Rozoy DISC'07], bipartition [Yasumi, Ooshita, Yamaguchi, Inoue – OPODIS'17], ...)
 - Communication faults are impossible to tolerate [Luna, Flochini, Izumi, Izumi, Santoro, Viglietta TCS'19]
 - Byzantine tolerant protocols are impossible [Guerraoui & Ruppert ICALP'09]
- **Stabilization time acceleration is limited**
 - Every semi-linear predicate computable in $O(n)$ parallel time [Angluin, Aspnes, Eisenstat DC'08], and some (e.g., majority) cannot be computed faster [Belleville, Doty, Soloveichik ICALP'2018]
 - Leader Election takes $\Omega(n)$ parallel time [Doty & Soloveichik DISC'15]



Extensions to obtain termination

- Relaxing the termination requirement
 - eventual stabilization may be sufficient
 - depending on an application
 - composing non-terminating protocols is possible [Angluin, Aspnes, Chan, Fischer, Jiang, Peralta DCOSS'15]
- Oracles
 - “heard of all” detector for solving consensus [Beauquier, Blanchard, Burman, Kuttan AlgoSensors'15]
 - “state absence” detector based leader → allow terminating PP with Turing Machine power of space $O(\log n)$ [Michail & Spirakis JPDC'15]



Extensions to augment computational power

- With $\Theta(\log \log n)$ memory bits eq. $\Theta(\log^{O(1)} n)$ identifiers (homonyms)
 - the first non-semi-linear predicate can be computed [Chatzigiannakis, Michail, Nikolaou, Pavlogiannis, Spirakis TCS'11]
allows to simulate **Turing Machine on space $O(\log^{O(1)} n)$** [Bournez, Cohen, Rabie TCS'18]
- Adding **unique identifiers - $\Omega(\log n)$ memory bits** (Community Protocols or Passively mobile Machines model) \rightarrow symmetric predicates in $\text{NSPACE}(n \log n)$ eq. to a power of **TM with $O(n \log n)$ space** [Guerraoui & Ruppert ICALP'09], [Chatzigiannakis, Michail, Nikolaou, Pavlogiannis, Spirakis TCS'11]
- Adding **shared memory per agent pair** (Mediated Population Protocols) \rightarrow symmetric predicates in $\text{NSPACE}(n^2)$ eq. to **TM with $O(n^2)$ space** [Chatzigiannakis, Michail, Nikolaou, Pavlogiannis, Spirakis ICALP'09]



Extensions for speed up

- With a **given leader** constant-space PP (semi-linear predicates) converge exponentially faster – **$O(\text{polylog } n)$ parallel time** [Angluin, Aspnes, Eisenstat DC'08], [Belleville, Doty, Soloveichik ICALP'2018]
- With a **small probability of error** constant-space PP converge in **$O(\text{polylog } n)$ parallel time** [Kosowski & Uznanski]



Extensions for fault-tolerance

- Adding **unique identifiers** - $\Omega(\log n)$ memory **bits** - Community Protocols – **$O(1)$ Byzantine faults can be tolerated** [Guerraoui & Ruppert ICALP'09]
- With a **leader and/or unbounded memory** some **communication faults can be tolerated** [Luna, Flochini, Izumi, Izumi, Santoro, Viglietta TCS'19]
- What about **any transient number of faults** – **self-stabilization?**

Self-stabilization [Dijkstra'74]

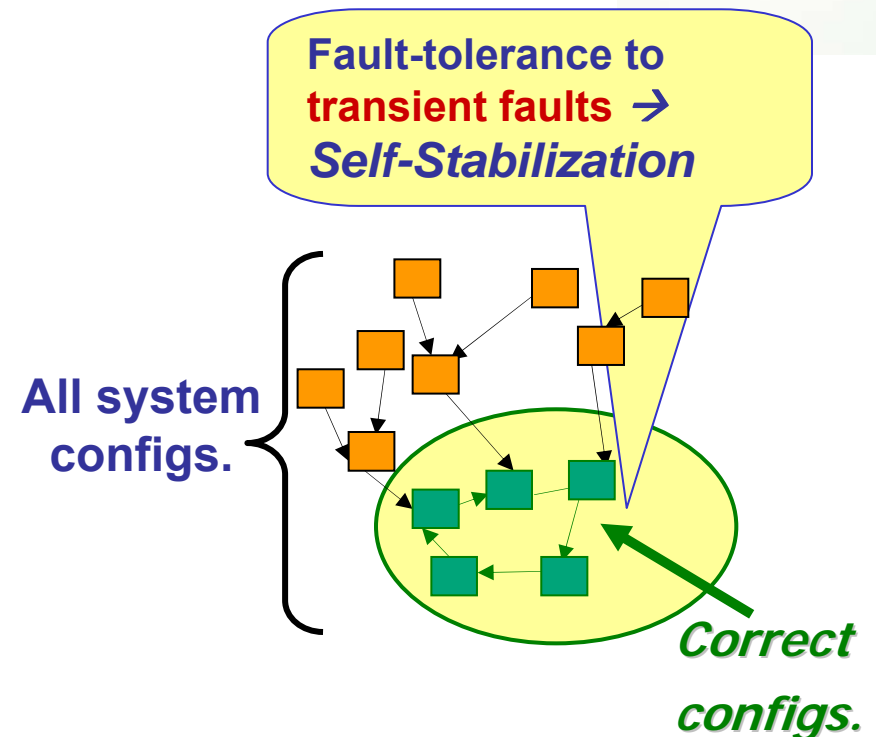
Fault attack

Motivation: any number of transient failures,
hard to initialize, agents that leave and join



Self-stabilizing protocol:

starting from an
arbitrary configuration,
reaches (barring additional faults)
correct configurations
eventually (and stays correct)





Self-stabilizing PP

[Angluin, Aspnes, Fischer ACMJ'08]

Positive results:

- coloring, orientation, spanning-tree in bounded degree graphs
- **non-uniform Leader Election (LE) in rings**

Negative result:

- **uniform LE in complete graphs is impossible**

→ No general characterization of self-stabilizing PP

Extensions for fault-tolerance

Self-stabilizing LE

- with “leader absence detector” - oracle Ω ?
 - uniform leader election in rings [Fischer & Jiang OPODIS'06]
 - uniform leader election in arbitrary graphs [Beauquier, Blanchard, Burman OPODIS'13, SSS'16] [Canepa & Potop-Butucaru WRAS'10]

Extensions for fault-tolerance

Self-stabilizing LE (cont.)

- With **n states** and **knowledge of n**
[Cai, Izumi, Wada TCS'12]
 - $\rightarrow O(n^2)$ time solution
 - impossible otherwise
- With **stronger models** and **less than n states**
 - mediated PP [Mizoguchi, Ono, Kijima, Yamashita DC'12]
 - k-interaction PP [Xu, Yamauchi, Kijima, Yamashita SSS'13]
- With **upper bound N on n** and **relaxed self-stabilization** - loose-stabilization
 - With $\exp(N)$ holding time: stabilization $\Omega(Nn)$ and $\Omega(N)$ states are necessary and sufficient [Izumi SIROCCO'15]
 - Solution stabilizing in $\text{polylog}(n)$ time but with $\text{poly}(n)$ holding time [Sudo, Ooshita, Kakugawa, Masuzawa, Datta, Larmore OPODIS'18]



Self-stabilizing LE vs. Initialized LE

- While impossible without initialization, easy with uniform initialization
 - with one bit of memory
 - one transition rule *(leader, leader) → (leader, non-leader)*
(when two candidate leaders meet, one drops out)
- The best SS-LE stabilizes in $O(n^2)$ time – exponentially slower than $\text{polylog}(n)$ time initialized LE
- Very few studies on self-stabilizing PP!

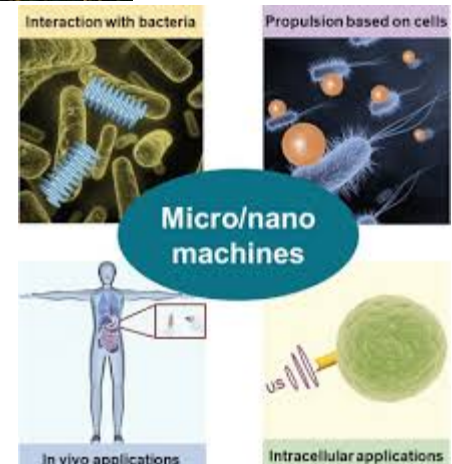


Future directions: self-stab. PP

- Study time efficiency limits (time-space trade-offs) of self-stab. LE
- Study other self-stab. PP (majority, counting, naming ...)
- General characterization of n-state self-stab. PP

Future Population Protocols

- Adapt to new applications (e.g. more nature inspired)
 - position aware PP
 - beeping PP
 - PP implementing micro-biological circuits
 - future biological computers
 - intelligent drugs





Why Population Protocols?

- Simple and convenient model allowing formal analysis
 - Can be extended
- Model many real world phenomena
 - Many existing and future applications
- Still many open algorithmic questions
 - Related to model, problems and complexity

Thank you!