



Social Networks

Pierre Senellart





Most popular Web sites

- 1 google.com
- 2 facebook.com
- 3 youtube.com
- 4 yahoo.com
- 5 baidu.com
- 6 wikipedia.org
- 7 live.com
- 8 twitter.com
- 9 qq.com
- 10 amazon.com
- 11 blogspot.com
- 12 linkedin.com
- 13 google.co.in
- 14 taobao.com
- 15 sina.com.cn
- 16 yahoo.co.jp
- 17 msn.com
- 18 wordpress.com
- 19 google.com.hk
- 20 t.co
- 21 google.de
- 22 ebay.com
- 23 google.co.jp
- 24 googleusercontent.com
- 25 google.co.uk
- 26 yandex.ru
- 27 163.com
- 28 weibo.com

(Alexa)



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Social networking sites

Sites with social networking features (friends, user-shared content, user profiles, etc.)



Social data on the Web

Huge numbers of users:

Facebook 900 million

QQ 540 million

W. Live 330 million

Weibo 310 million

Google+ 170 million

Twitter 140 million

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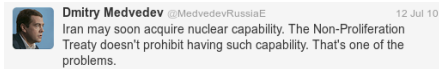
Twitter 140 million

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Huge volume of shared data:

250 million tweets per day on Twitter
(3,000 per second on average!)

... including statements by heads of states, revelations of political activists, etc.





Exploiting social Web data

Very **rich** source of information, lots that can be done with it: technology watch, sentiment analysis, sociological analysis, etc.

Many **challenges** as well: unbiased sampling from social networks? how to keep up to date with 3,000 tweets every second? how to manage the petabytes of data of social networking sites?

Focus on two problems:

- (Primarily) What is the **structure** of social networks? How to **model** them?
- **Socially aware** Web search



Outline

Social Networking Sites

Social Networks: Structure and Models

Socially Aware Web Search

Conclusion



Small worlds

I proposed a more difficult problem: to find a chain of contacts linking myself with an anonymous riveter at the Ford Motor Company — and I accomplished it in four steps. The worker knows his foreman, who knows Mr. Ford himself, who, in turn, is on good terms with the director general of the Hearst publishing empire. I had a close friend, Mr. Árpád Pásztor, who had recently struck up an acquaintance with the director of Hearst Publishing. It would take but one word to my friend to send a cable to the general director of Hearst asking him to contact Ford who could in turn contact the foreman, who could then contact the riveter, who could then assemble a new automobile for me, would I need one.

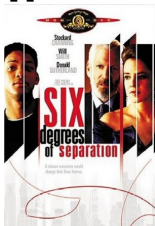
[...] Our friend was absolutely correct: nobody from the group needed more than five links in the chain to reach, just by using the method of acquaintance, any inhabitant of our Planet.

[Karinthy, 1929]



Six degrees of separation

- Idea that two persons on Earth are separated by a chain of six individuals who know each other
- Appears widely in popular culture:



It's a small world!

Stanley Milgram's experiment [Travers and Milgram, 1969]



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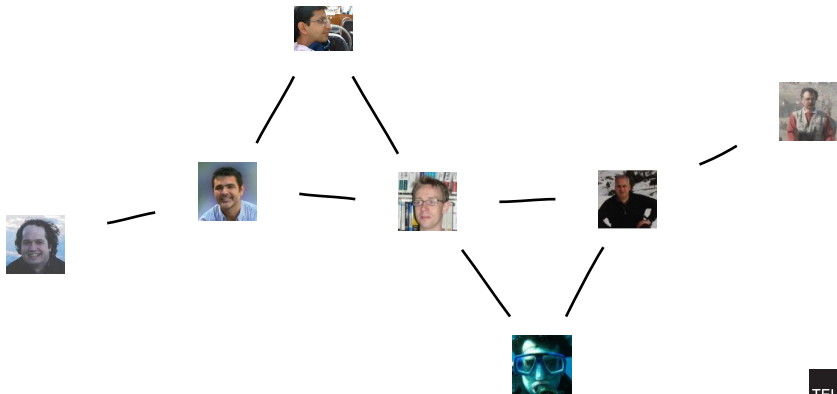
- Stanley Milgram (1933-1984): social psychologist
- **Experiment:** people are asked to send a message to some unknown person, by **forwarding** it to an **acquaintance** who might be closer to this person
- **Results:** only 29% of the messages arrived, with a mean number of acquaintances of **5.2**.
- **Validates** somehow the 6-degree theory!
- Other more recent experiments [Dodds et al., 2003] confirm this order of magnitude.



Simple model of a social network

A social network is just a **graph**:

- individuals, data items, groups, etc., are nodes
- connections are (possibly directed and labeled) edges





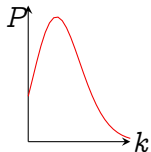
Characteristics of interest of a network

Sparsity. Is the network sparse ($|A| \ll |S|^2$)?

Typical distance. What is the **mean distance** between any pairs of vertices?

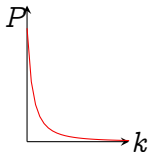
Local clustering. If a is connected to both b and c , is the probability that b is connected to c significantly greater than the probability any two nodes are connected?

Degree distribution. What is the distribution of the degree of vertices?



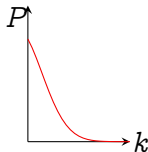
Poisson

$$\frac{\lambda^k}{k!}$$



Power-law

$$k^{-\gamma}$$



Gaussian

$$e^{-k^2}$$



Characteristics of social networks

- Choose any social network: real-life acquaintance network [Amaral et al., 2000], Twitter follower graph [Kwak et al., 2010], scientific collaboration network [Amaral et al., 2000], romantic or sexual relationships [Amaral et al., 2000, Liljeros et al., 2001], etc.



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- **Sparse** graph.



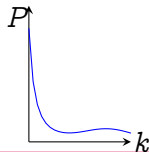
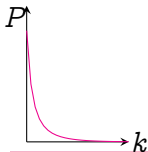
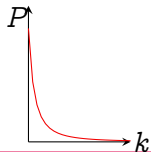
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- **Strong** local clustering (well, not for romantic relationships)



Characteristics of social networks

- Choose any social network: real-life acquaintance network [Amaral et al., 2000], Twitter follower graph [Kwak et al., 2010], scientific collaboration network [Amaral et al., 2000], romantic or sexual relationships [Amaral et al., 2000, Liljeros et al., 2001], etc.
- **Sparse** graph.
- **Strong** local clustering (well, not for romantic relationships)
- Degree distribution: usually a **power-law with γ between 2 and 3**. Sometimes slightly modified: exponential or Gaussian **cut-off** (real-life acquaintances) or, on the contrary, **more high-degree nodes than expected** (Twitter). Sometimes even more complicated [Sala et al., 2010b].





Other kinds of networks

Similar characteristics for:

- Neural network of a worm [Watts and Strogatz, 1998]
- Metabolic interaction network [Jeong et al., 2000]
- The Internet [Faloutsos et al., 1999]
- The World Wide Web [Broder et al., 2000]

Counter-examples: networks with a 2D embedding, such as road networks.



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Why?

Construction

1. Start with n vertices and a probability p . Assume $p > \frac{1}{n}$.
2. For each pair of vertices (u, v) , insert an edge between u and v with probability p .

Random networks [Solomonoff and Rapoport, 1951, Erdős and Rényi, 1960]

Network characteristics

- Sparse if $p \ll 1$

Const

1. St
 2. Fo
- w

v

Random networks [Solomonoff and Rapoport, 1951, Erdős and Rényi, 1960]

Network characteristics

- **Sparse** if $p \ll 1$
- **Logarithmic** typical distance (inside the giant connected component)!

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Network characteristics

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- No local clustering.

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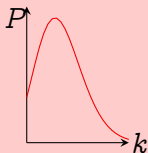
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Random networks [Solomonoff and Rapoport, 1951, Erdős and Rényi, 1960]

Network characteristics

- **Sparse** if $p \ll 1$
- **Logarithmic** typical distance (inside the giant connected component)!
- **No local clustering.**
- **Poisson** degree distribution



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Construction

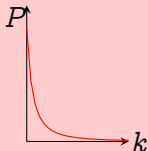
1. Start with a small graph of size m_0 , let m be a constant with $m < m_0$.
2. **One after the other**, $n - m_0$ vertices are added to the graph, connecting them to m **existing vertices**; the probability of connecting to a vertex is **proportional** to its degree.

Rich get richer!

Preferential attachment [Barabási and Albert, 1999]

Network characteristics

- Const
1. Sparse if m and n are chosen appropriately.
 1. Small typical distance.
 - m
 2. Strong local clustering
 2. Power-law degree distribution (actually, with $\gamma = 3$, but variations allow arbitrary exponents).
 - cc
 - cc





So why not a full power-law distribution?

- Exponential or Gaussian people (real-life networks): in the real life, there is a **cost** to establish connections, cannot have too many of them. In addition, **people die** and stop making connections.
- More connections than expected (Twitter): **celebrities** have a special status on Twitter and attract more followers than the preferential attachment model predicts.



What have we learned?

- Nothing surprising about the small-world effect! Already happens in a completely random graph: due to **random connections**.
- Clustering, degree distribution: partly explained by the **history of the network**, and by the fact that **rich get richer** (preferential attachment)
- Preferential attachment is **not the last word** on this. More refined models do exist! [Sala et al., 2010a, Vazquez, 2003]
- We know how to build reasonable **synthetic** social networks.



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Why social search?

- Many Web queries are **ambiguous** or **too broad** to retrieve what the user is looking for: “music”, “president”, “Paris”
- General idea: my **friends’ interest** are **correlated to mine**.
- If I **bias** my search results based on **my social network**:
 - I can be less precise in my queries; when I talk about spouse it is by default my spouse, company my company, etc.
 - I can get info about my friends
 - I can get sentiment/opinion/taste (e.g., about a new gadget) biased by those of of people like me (even if I don’t know them)
- **Risks**:
 - Remove objectivity in Web search – what I want to hear and not the truth
 - Community withdrawal



Information retrieval with social scoring

[Schenkel et al., 2008]

- **Setting:** multi-partite graph, e.g., Flickr (user-photo-tag)
- **Social weighting:**
 - Given a friendship relation $F(u, u')$ (explicit or implicit) between two users, compute an **extended friendship** relation:

$$\tilde{F}(u, u') = \frac{\alpha}{|U|} + (1 - \alpha) \max_{\text{chemin } u = u_0 \dots u_k = u'} \prod_{i=0}^{k-1} F(u_i, u_{i+1})$$

($0 < \alpha < 1$ constant; $|U|$: number of users)

- Instead of using a **global weighting** $\text{tf-idf}(t, d) = \text{tf}(t, d) \times \text{idf}(t, d)$ use a **social weighting** dependent of u :

$$\text{tf-idf}_u(t, d) = \left(\sum_{u' \in U} F(u, u') \cdot \text{tf}_{u'}(t, d) \right) \times \text{idf}(t, d)$$



Top- k with social score [Benedikt et al., 2008]

- Possible to use refined algorithms to get only top- k best results (as in classical Web search)...
- ... but this requires **precomputing** $\text{tf-idf}_u(t, d)$ for each user: impossible
- To avoid this:
 1. Partition the graph of users in clusters of **very similar** users
 2. Use the scores **inside each cluster** as estimations of whether the top- k results found are the best
 3. \Rightarrow gives **approximate** results, but good enough



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Many challenges, many applications

- **better models** of social graphs (taking into account locality, dynamics, etc.)
- **applications** of network models: epidemiology simulations, propagation of rumors, resilience to censorship
- mass of social data on the Web, waiting **to be exploited**:
 - better search results, better recommendation, better understanding of our world
 - monitoring the Web for things that may interest me
 - intrusive advertising, extreme profiling (determine whether you're gay, pregnant, or activist by looking at your social network or social data)
- a wide collection of **social algorithms**
- need for data sharing models in social networks, taking into account privacy, distribution, etc. – **Webdamlog**



To go further

[Watts, 2003]: an easy-to-read book describing the area of **network science**, including models and concrete applications

[Newman et al., 2006]: an in-detail survey of the most fundamental works on network theory, networks models, and experimentations on real-world networks

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