

Thermoelectricité comme sonde de l'organisation électronique dans les solides

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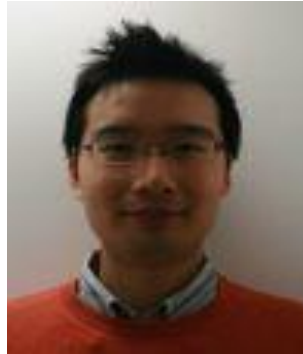
Ecole Supérieure de Physique et de Chimie
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Collaborators, ESPCI



Benoit Fauqué
CNRS researcher



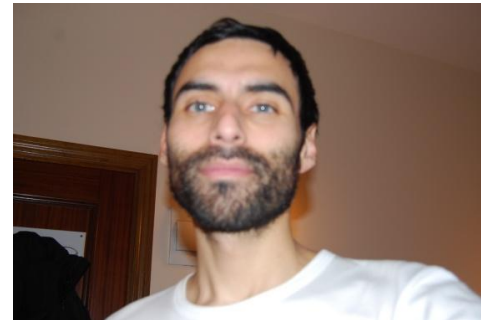
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Cyril Proust and his group, LNCMI- Toulouse and Grenoble

Jacques Flouquet and his group, SPSMS-CEA, Grenoble

Outline

I. Introduction : electric vs. thermoelectric conductance

II. From Kondo effect to heavy-electron metals

III. The Nernst effect

IV. Quantum limit and dilute metals

•**J. M. Ziman, Electrons and phonons**

•**D. K. C. Macdonald, Thermoelectricity**

Flow of heat and charge

$$\vec{J}_e = \sigma \vec{E} - \alpha \vec{\nabla} T$$

$$\vec{J}_Q = \alpha T \vec{E} - \kappa' \vec{\nabla} T$$

Electric conductivity

Thermal conductivity

Thermo-electric conductivity

In general, σ , α and κ are tensors !

Off-diagonal components emerge in presence of magnetic field:

- Hall effect
- Nernst effect
- Righi-Leduc effect

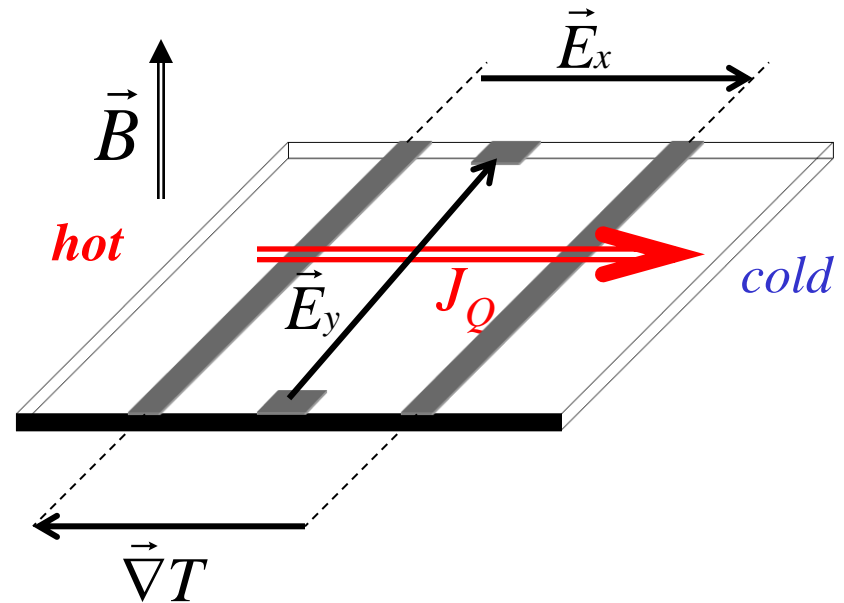
Experimental access to thermoelectric coefficients

- Impose a thermal gradient!
- Impede charge flow ($J_e=0$)!

$$\sigma \vec{E} = \alpha \vec{\nabla} T$$

Seebeck
$$S = \frac{\alpha}{\sigma} = \frac{E_x}{\nabla_x T}$$

Nernst
$$N = S_{xy} = \frac{E_y}{\nabla_x T} \quad \left[v = \frac{-E_y}{B_z \nabla_x T} \right]$$



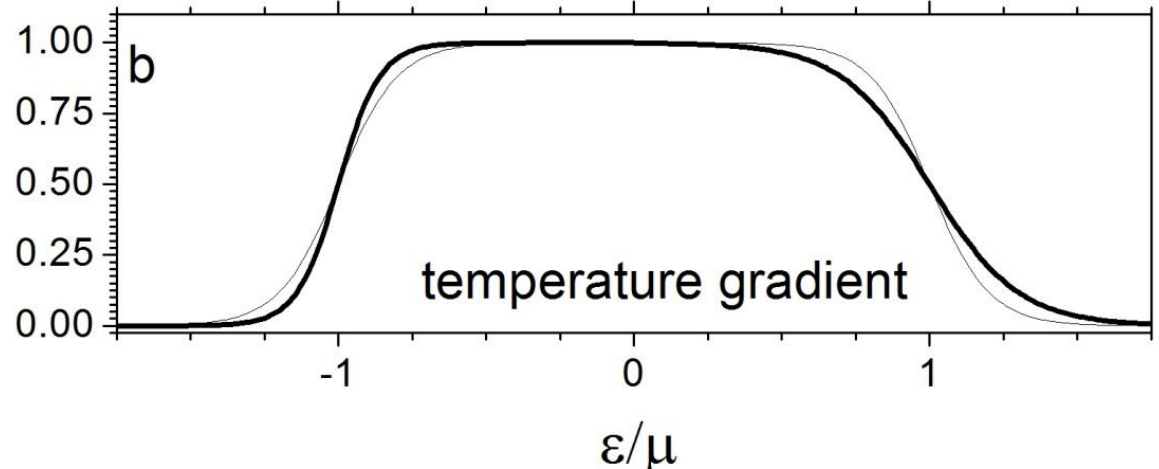
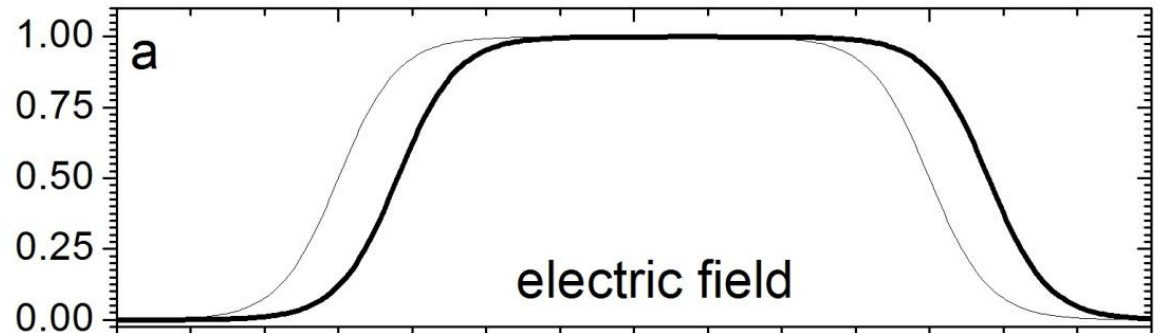
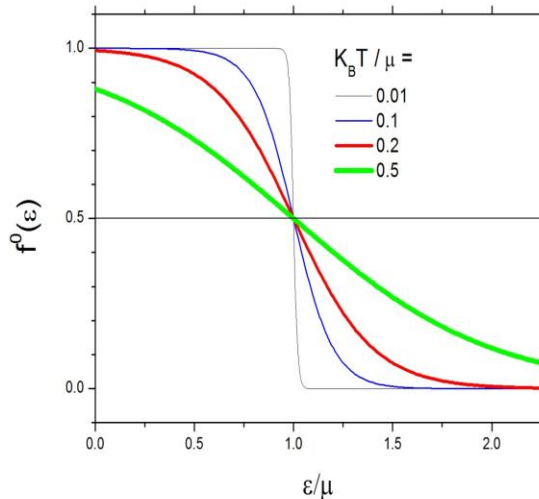
The linearized Boltzmann equation

$$\frac{f_k(\mathbf{r}) - f^0}{\tau} = \mathbf{v}_k \cdot \left(\frac{\partial f^0}{\partial T} \nabla T + \frac{\partial f^0}{\partial \epsilon_k} \mathbf{E} \right)$$

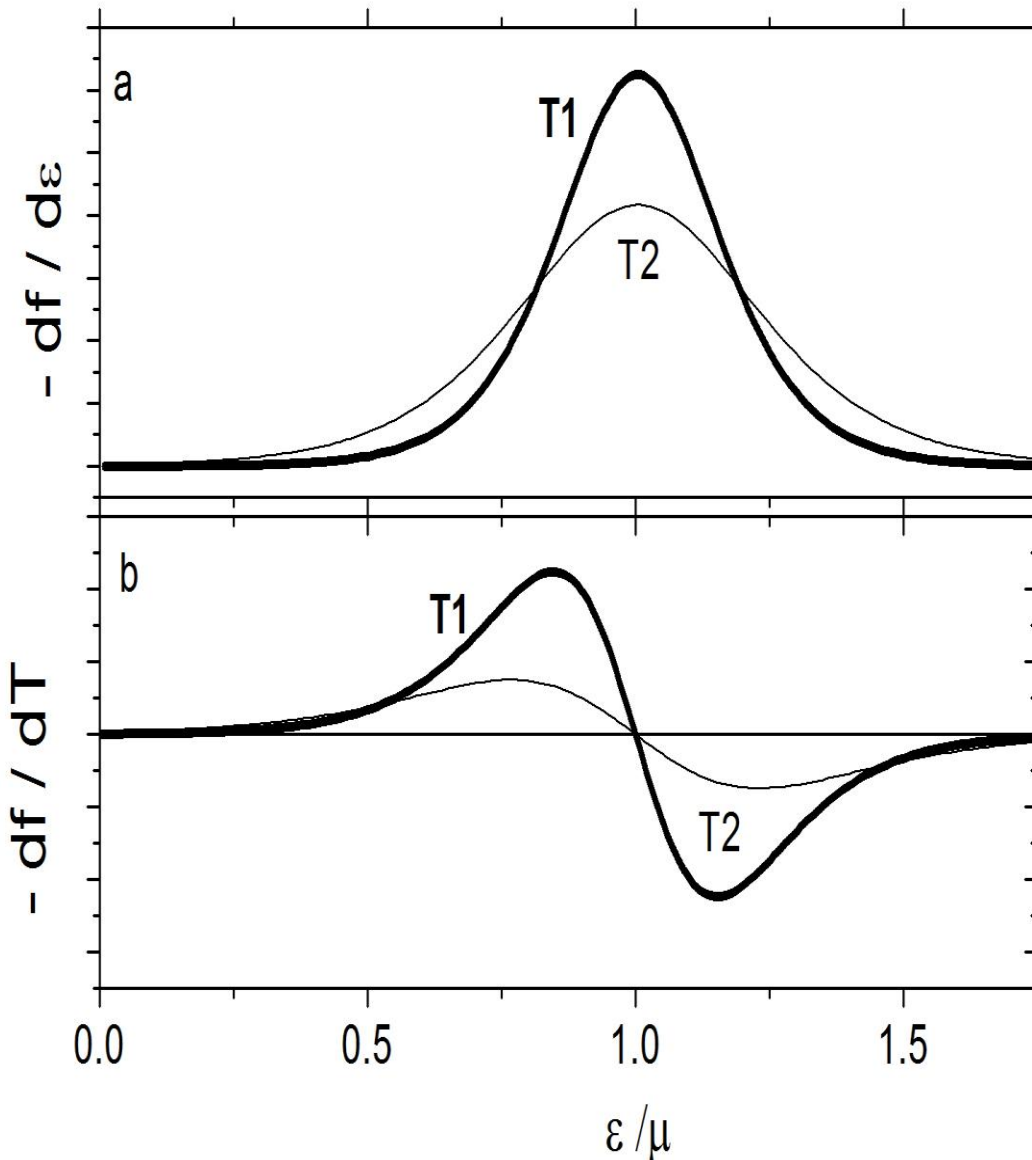
Scattering time $\rightarrow \tau$

velocity $\rightarrow \mathbf{v}_k$

$$f^0 = \frac{1}{e^{(\epsilon - \mu)/k_B T} + 1}$$



Electric and thermoelectric conductivity



$$\sigma = -e^2 \int \tau(k)(v_k)^2 \frac{\partial f^0}{\partial \epsilon_k} dk$$

Always positive

Dominant contributors: $\epsilon = \mu$

$$\alpha = e \int \tau(k)(v_k)^2 \frac{\partial f^0}{\partial T} dk$$

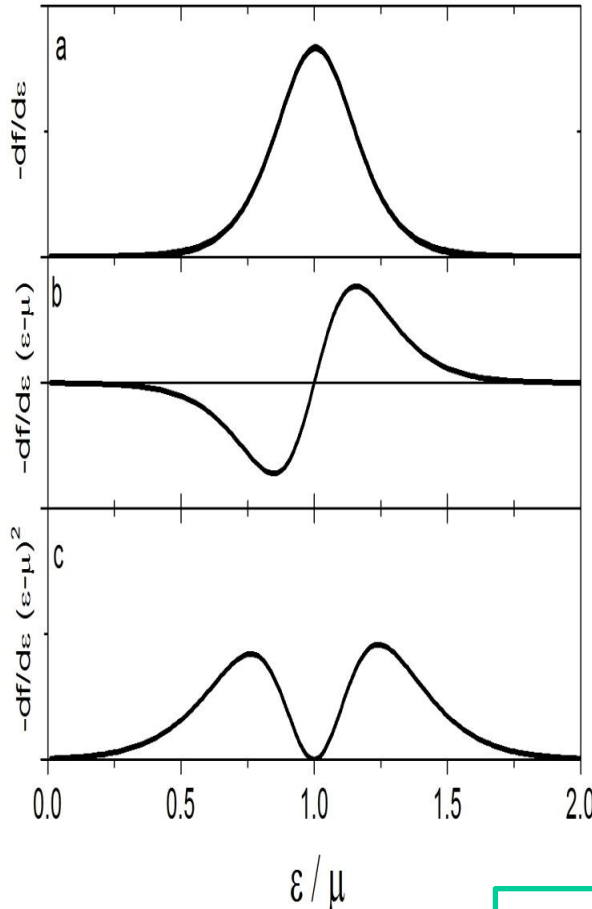
Can be positive or negative

Dominant contributors:
 $\epsilon < \mu$ and $\epsilon > \mu$

Electrons which carry charge and those which carry heat!

Quanta of conductance

electric



$$\sigma = 2 \frac{e^2}{h} \int -\frac{\partial f}{\partial \epsilon} \Xi(\epsilon) d\epsilon$$

$$\alpha = 2 \frac{ek_B}{h} \int -\frac{(\epsilon - \mu)}{k_B T} \frac{\partial f}{\partial \epsilon} \Xi(\epsilon) d\epsilon$$

$$\frac{\kappa}{T} = 2 \frac{k_B^2}{h} \int \left[\frac{(\epsilon - \mu)}{k_B T} \right]^2 \frac{\partial f}{\partial \epsilon} \Xi(\epsilon) d\epsilon$$

Transport distribution function

thermoelectric

thermal

Transport distribution function

(Mahan & Sofo, 1996)

$$\Xi(\varepsilon) = \frac{h}{2} N(\varepsilon) v_k^2(\varepsilon) \tau(\varepsilon) = \frac{h}{2} N(\varepsilon) v_k(\varepsilon) \ell(\varepsilon)$$

It depends on both the electronic structure and scattering mechanism.
In the material.

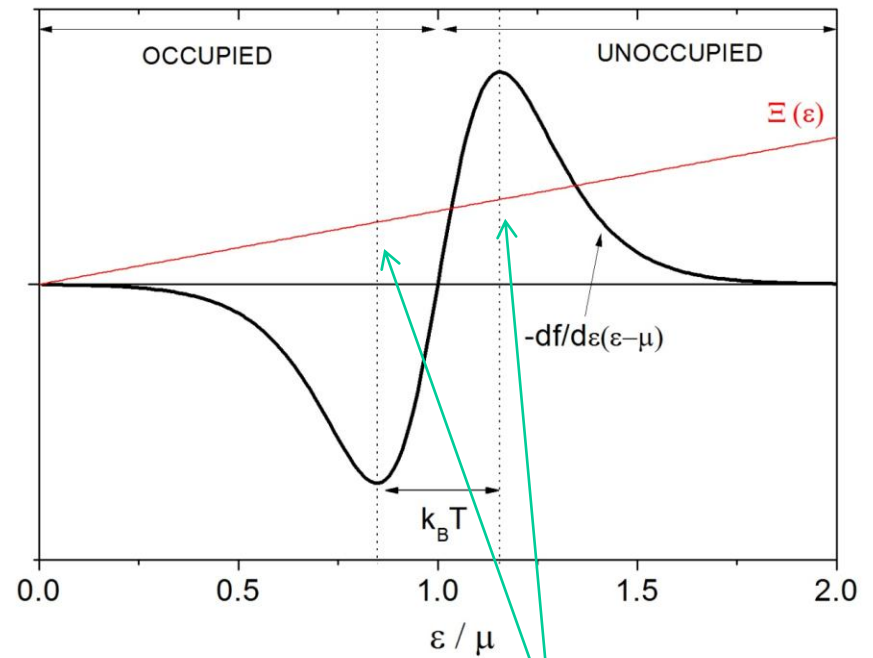
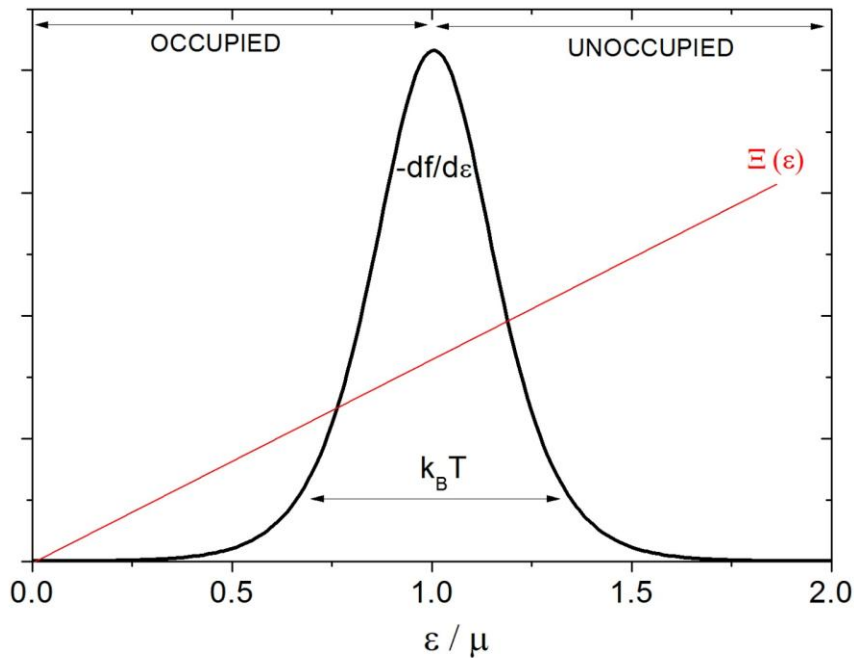
In a bulk solid, it replaces the transmission probability introduced by Landauer in the case of 1D systems!

Electric and thermoelectric conductivity

Parabolic dispersion with constant mean-free-path

$$\sigma = \frac{2e^2}{h} \int \left(-\frac{\partial f}{\partial \varepsilon}\right) \Xi(\varepsilon) d\varepsilon$$

$$\alpha = 2 \frac{ek_B}{h} \int \left(-\frac{\partial f}{\partial \varepsilon}\right) \frac{(\varepsilon - \mu)}{k_B T} \Xi(\varepsilon) d\varepsilon$$



High-energy electrons are faster and denser

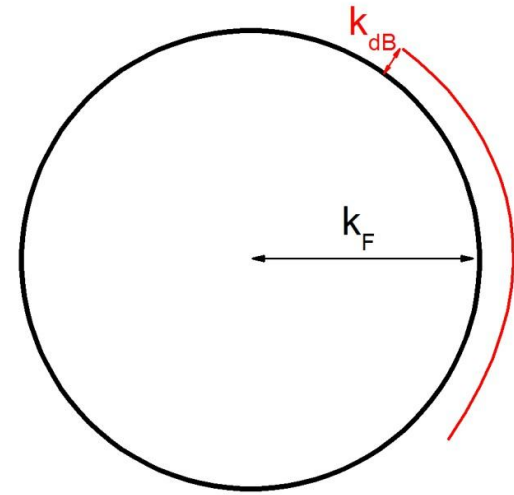
The free electron gas

$$\sigma = \frac{e^2}{h} \langle k_F^2 \ell \rangle$$

$$\alpha = \frac{k_B e}{h} \langle k_{dB}^2 \ell \rangle$$

$$S = \frac{\alpha}{\sigma} = \frac{k_B}{e} \frac{\langle k_{dB}^2 \rangle}{\langle k_F^2 \rangle} = \frac{\pi^2}{3} \frac{k_B}{e} \frac{T}{T_F}$$

$$k_{dB}^2 = \frac{2m^* k_B T}{\hbar^2}$$



de Broglie wavelength measures the thermal fuzziness of the Fermi surface!

The Seebeck coefficient becomes scattering-independent, if the mean-free-path is independent of energy.

In a degenerate Fermi liquid ($k_B T \ll \varepsilon_F$)

The Wiedemann–Franz law: $\frac{\kappa\alpha}{T} = \frac{\pi^2}{3} \frac{k_B^2}{e^2}$

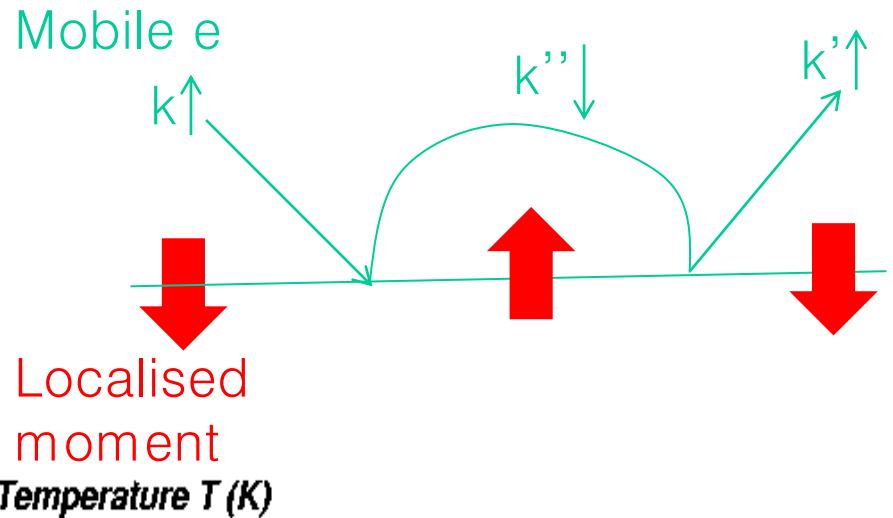
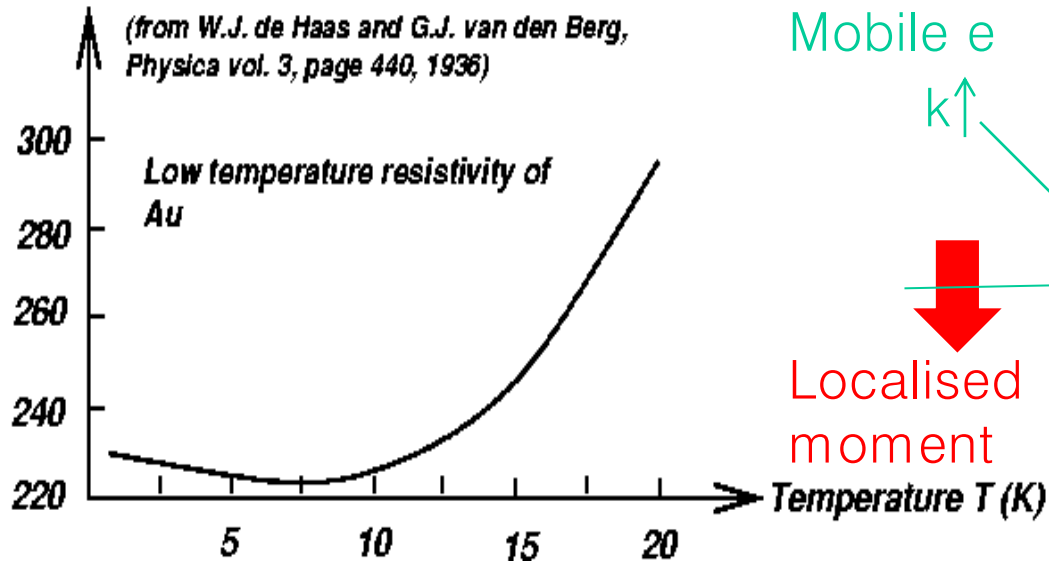
The Mott formula: $\alpha = \frac{\pi^2}{3} \frac{k_B^2}{e} T \frac{\partial \sigma}{\partial \varepsilon} \Big|_{\varepsilon=\mu}$

$$S = \frac{\alpha}{\sigma} = \frac{\pi^2}{3} \frac{k_B^2}{e} T \frac{\partial \ln \sigma}{\partial \varepsilon} \Big|_{\varepsilon=\mu}$$

Thermoelectricity probes electronic states **near ,but not exactly at,** the chemical potential , !

The Kondo effect

Resistance/Resistance($T=0$ Celsius) x 10000



1936: Mysterious upturn in resistivity of gold seen by de Haas
1950s: Role of MAGNETIC impurities pinned down
1960s: Giant Seebeck effect in thermopower in impure noble metals
1964: Kondo offers a solution (and defines a new problem)!

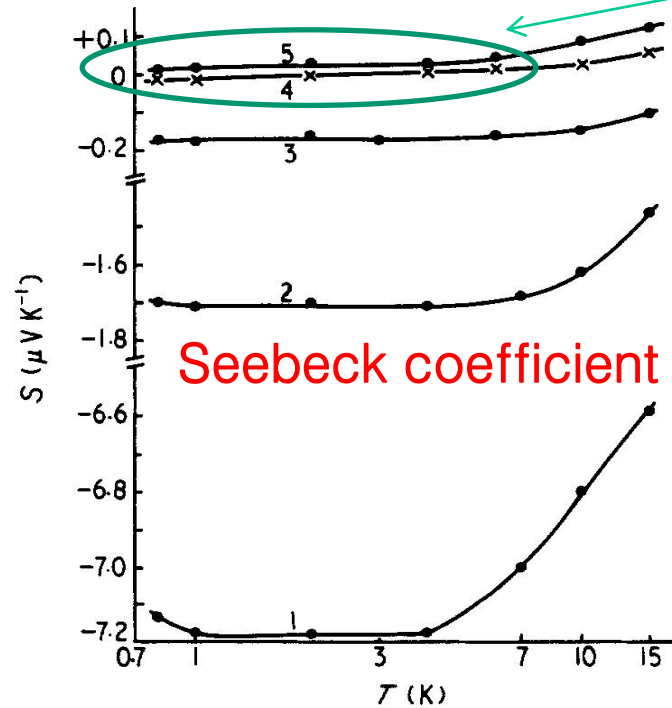
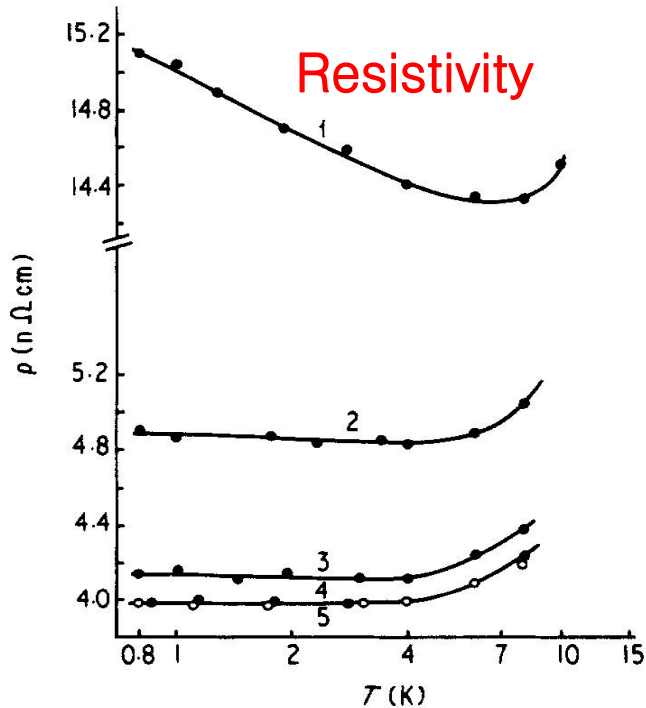
The isolated magnetic moment couples to the Fermi sea
Incoming electrons are spin-flipped and visit states of opposite spin!

The Kondo effect

Table 1.

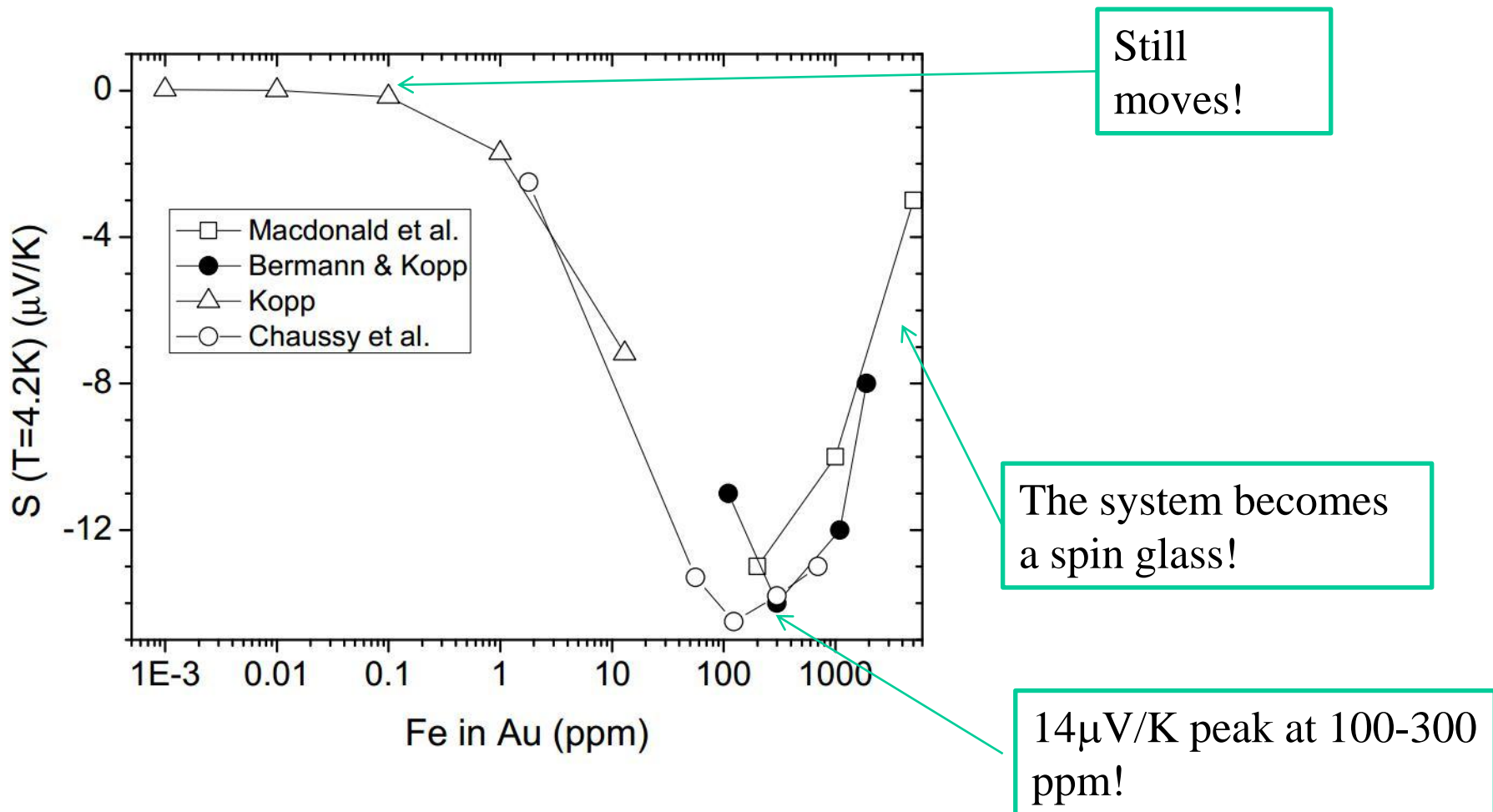
Specimen	Treatment time (h)	Fe concentration (ppm)	Resistivity (nΩ cm)	Thermopower (μV K ⁻¹)
1	0	13	14.4	-7.18
2	4.1	1	4.8	-1.71
3	8.2	0.1	4.1	-0.17
4	12.3	0.01	4.0	+0.01
5	16.4	0.001	4.0	+0.03

1 ppb to 10ppb!



Iron impurities in gold, Kopp 1975

Magnitude of Seebeck peak in Au-Fe at 4.2 K



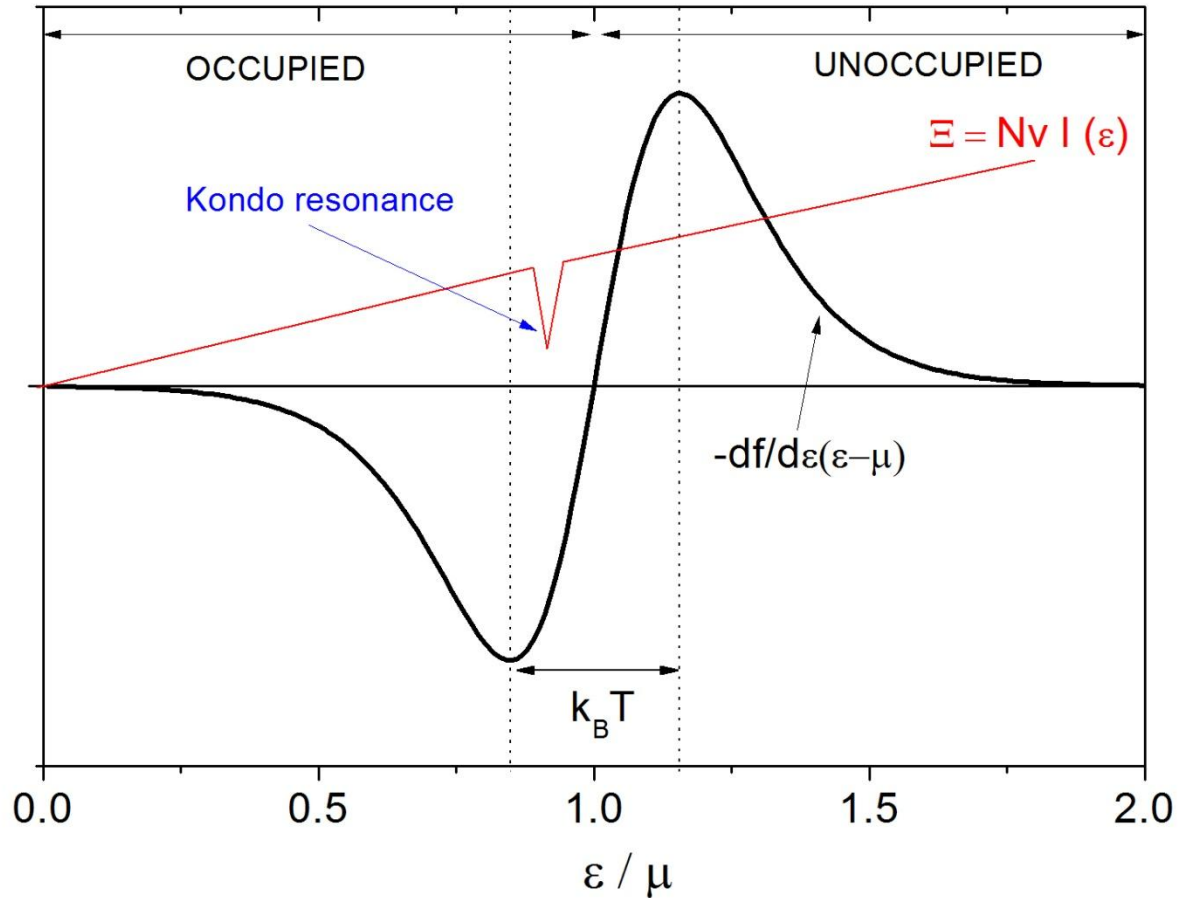
Still moves!

The system becomes a spin glass!

$14\mu\text{V/K}$ peak at 100 - 300 ppm!

- The intrinsic diffusive Seebeck coefficient of gold is only 24nV/K @ 4.2K !
- AuFe ($0.0.3\%$): the most sensitive thermocouple at low T !

Why the effect is so drastic?



A resonance peak in one side of the dividing line!

Kondo lattices

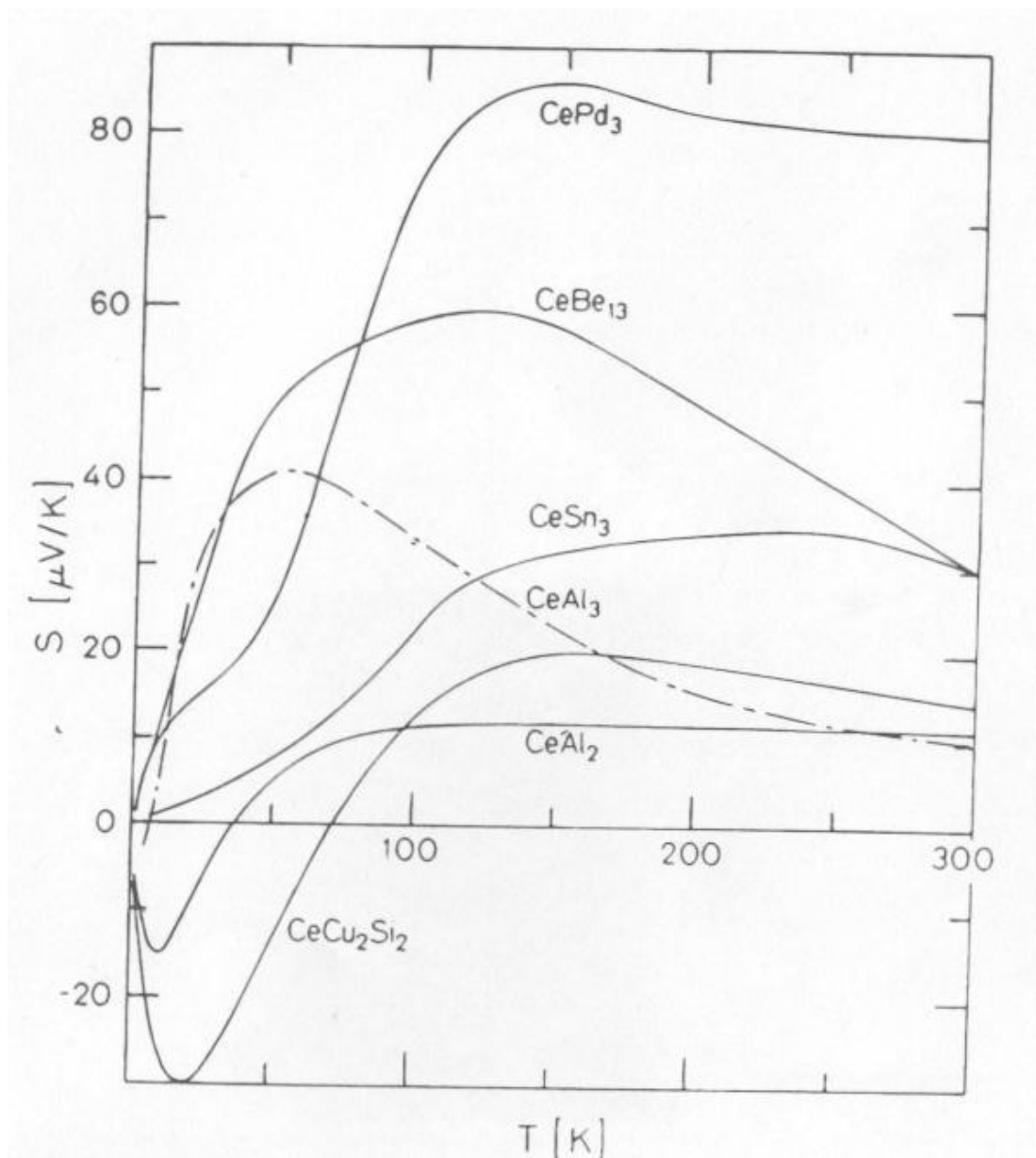
- Intermetallics with atoms hosting f electrons (CeAl_3 , YbAl_3 , UPt_3 ...)
- At high temperature, isolated magnetic moments in a Fermi sea
- At low temperature, no dichotomy between isolated spins and mobile charges. Both merge in to a sea of heavy electrons!

$$C_e = \frac{\pi^2}{3} k_B^2 T N(\varepsilon_F) = \frac{\pi^2}{3} k_B^2 T \frac{n}{T_F} \propto k_B T \frac{m^* n^{1/3}}{\hbar^2}$$

- An electronic specific heat several orders of magnitude larger than copper!

Large Seebeck coefficient in heavy-electron metals

Jaccard & Sierro 1982



Thermopower and specific heat

In a free electron gas :

$$S = -\frac{\pi^2}{3} \frac{k_B^2 T}{e} \frac{N(\epsilon_F)}{n} \quad C_{el} = \frac{\pi^2}{3} k_B^2 T N(\epsilon_F)$$

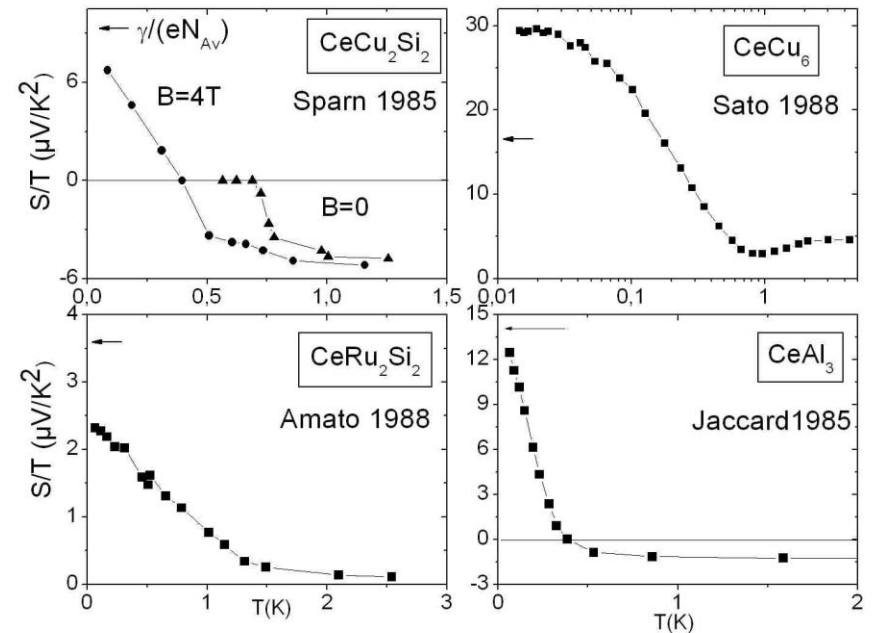
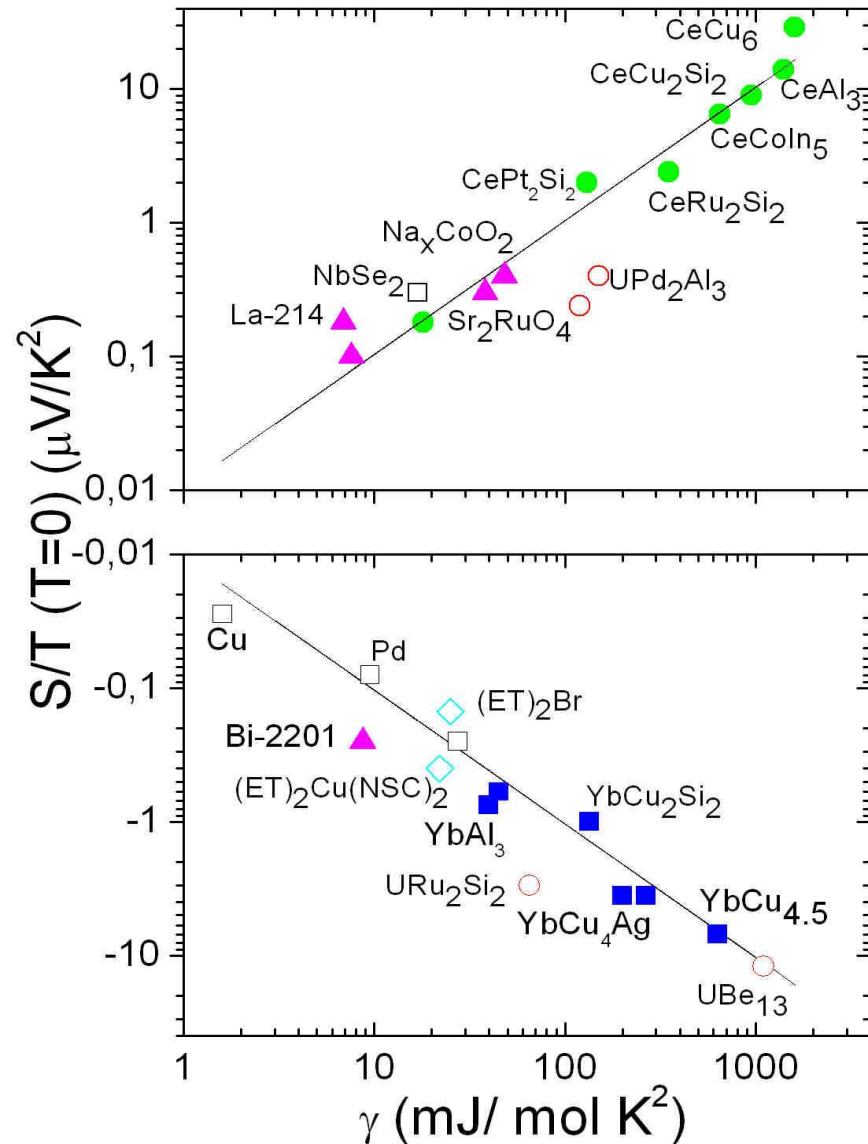
Thermopower is “specific heat per carrier”
[Macdonald 1962, Ziman, 1961, ...]

The dimensionless ratio: $q = eN_{Av} \frac{S}{C}$

is equal to -1 ($+1$) for free electrons (holes).

In many heavy-fermion metals q is close to unity!

Behnia, Jaccard & Flouquet,
JPCM 2004



See also Sakurai & Isikawa JSPJ 2005

Theory:

Miyake & Kohno JPSJ 2005

Zlatić et al., PRB 2007

Heavy Fermi liquids

- Enhanced specific heat

$$\gamma = \frac{\pi^2}{3} k_B^2 N(\varepsilon_F)$$

- Enhanced Pauli Susceptibility

$$\chi = \mu_B^2 N(\varepsilon_F)$$

- Enhanced inelastic resistivity

$$\rho = \rho_0 + AT^2$$

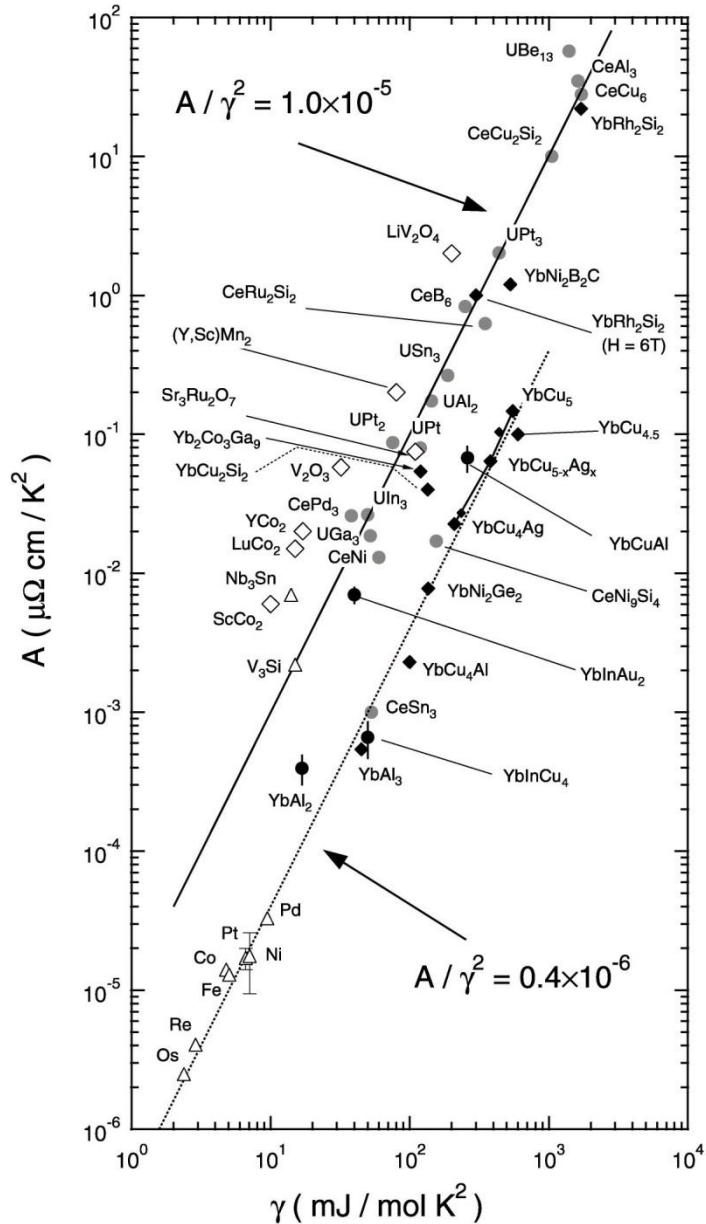
$$A \propto \frac{1}{\tau} \propto N(\varepsilon_F)^2$$

- Enhanced Seebeck coefficient

$$\frac{S}{T} = \frac{\pi^2}{3} k_B^2 \frac{N(\varepsilon_F)}{n}$$

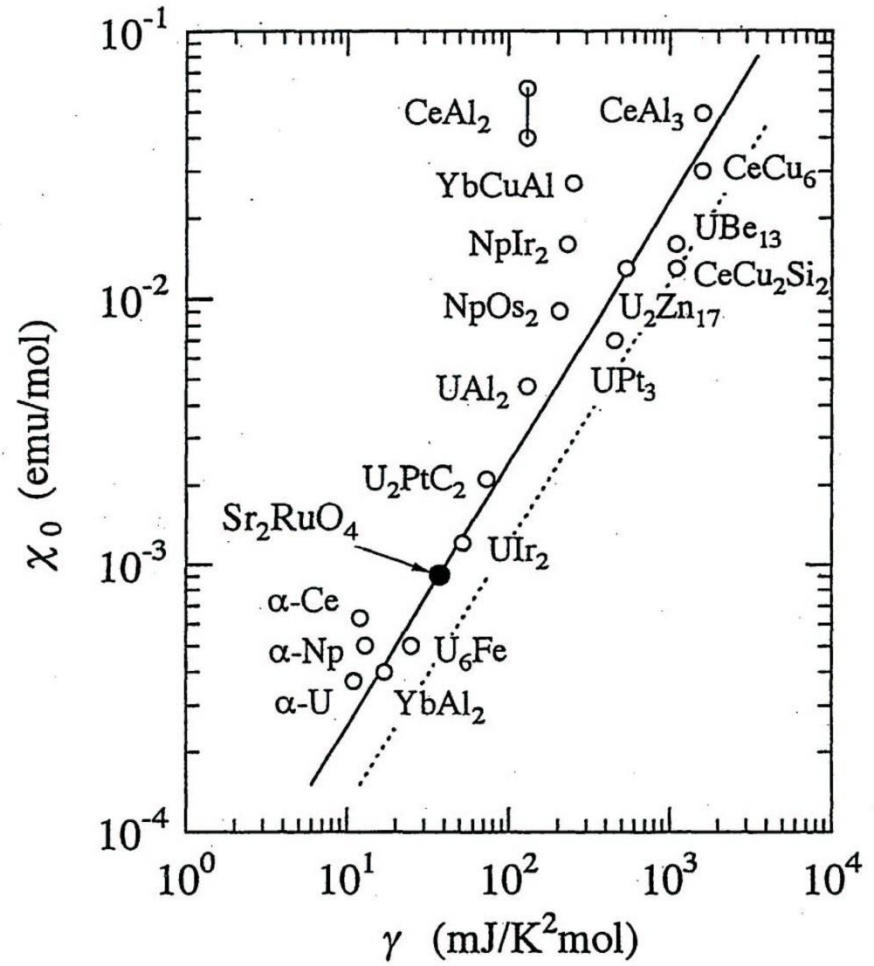
Fermi liquid ratios

The Kadowaki-Woods ratio



The Wilson ratio

$$R_W = \frac{\pi^2}{3} \frac{k_B^2}{\mu_B^2} \frac{\chi}{\gamma}$$



Current research on thermoelectricity of heavy electrons

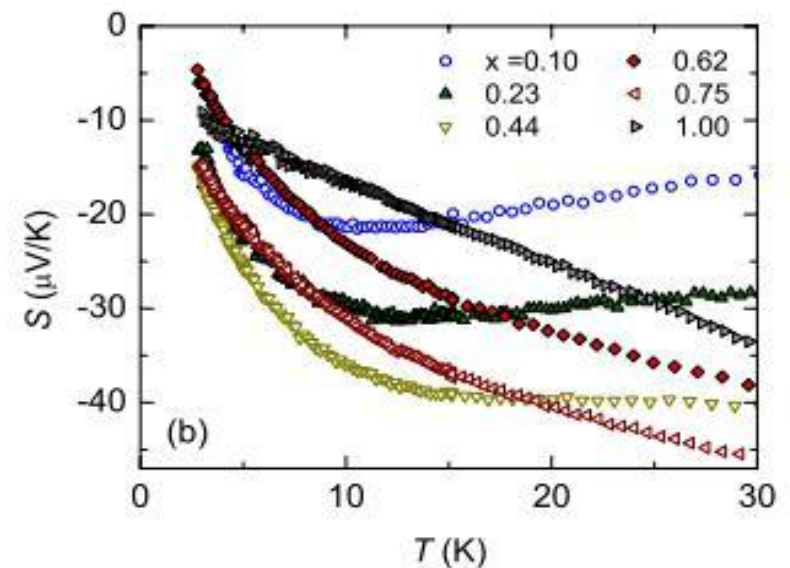
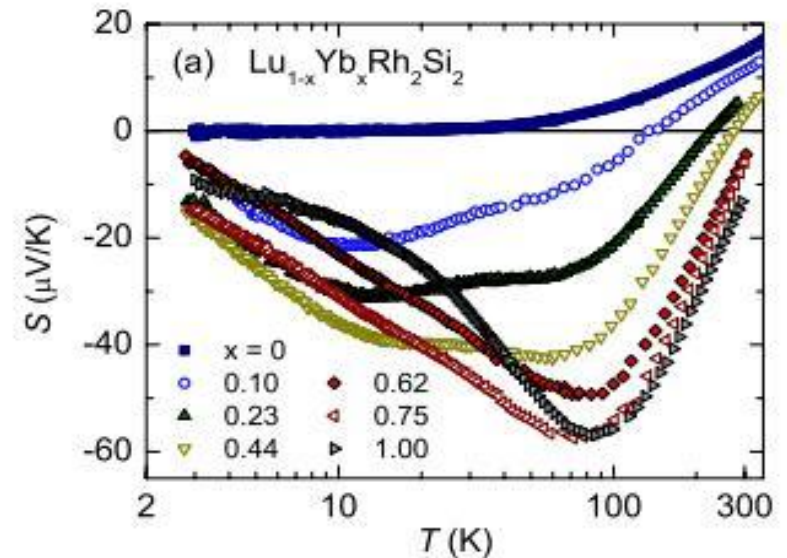
Main themes

- Quantum criticality
- Metamagnetic transitions
- Hidden electronic orders
- Fermi surface reconstruction
- Ferromagnetic superconductors

Principal actors

- Grenoble (Flouquet)
- Dresden (Steglich)
- Tokyo (Izawa)
- Ames (Canfield)
- Geneva (Jaccard)

Kohler et al., 2008 Dresden



Ferromagnetic superconductors

UGe₂

Saxena S.S. *et al.* Nature **406**, 587 (2000)

$$T_c = 52 \text{ K}, T_{SC} = 0.75 \text{ K}$$

URhGe

Aoki D. *et al.* Nature **413**, 613 (2001)

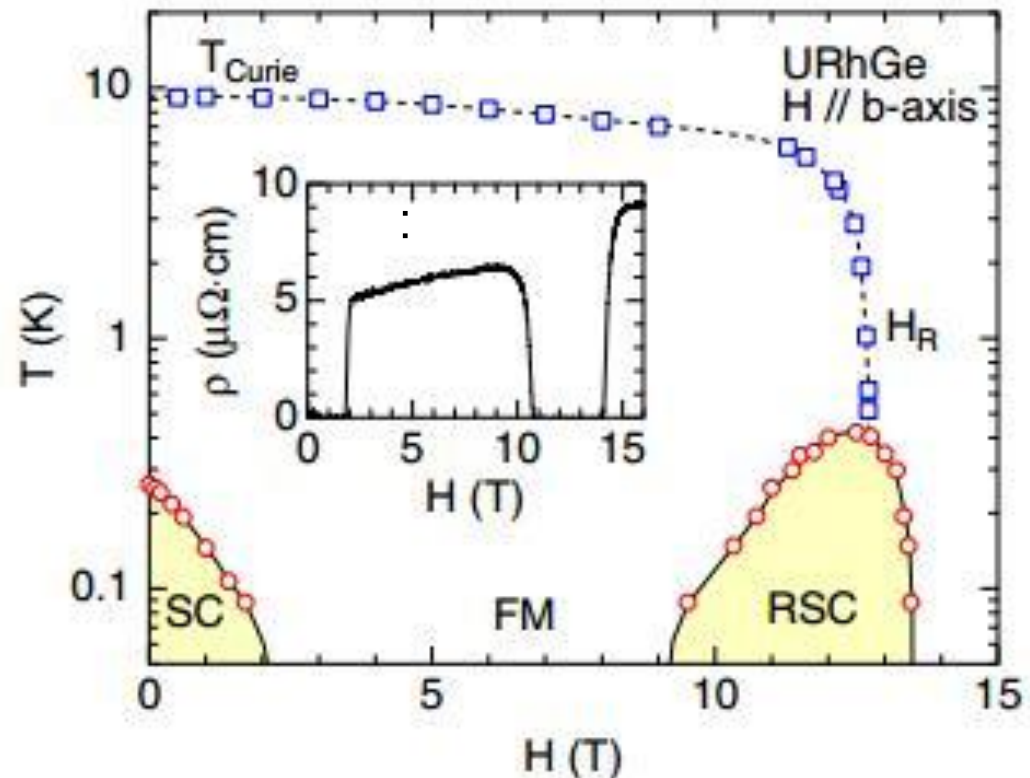
$$T_c = 9.5 \text{ K}, T_{SC} = 0.25 \text{ K}$$

UCoGe

Huy N.T. *et al.* PRL **99**, 067006 (2007)

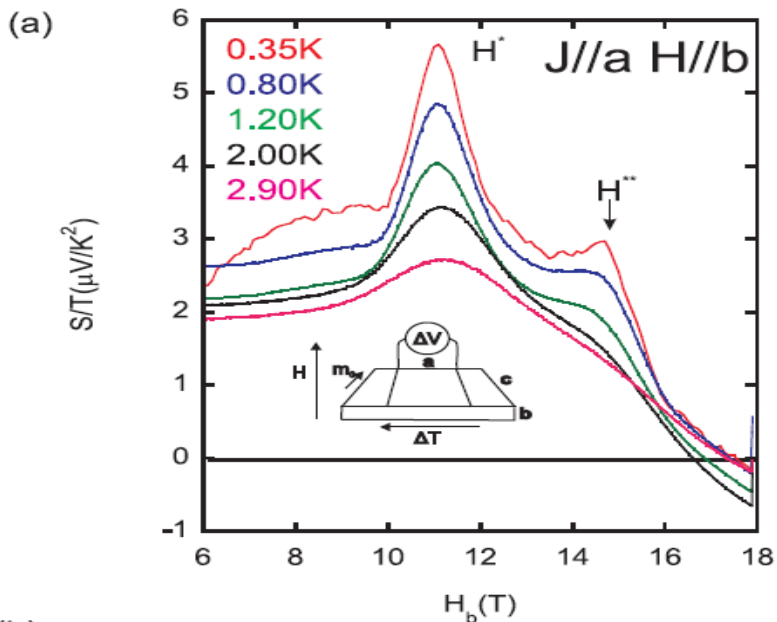
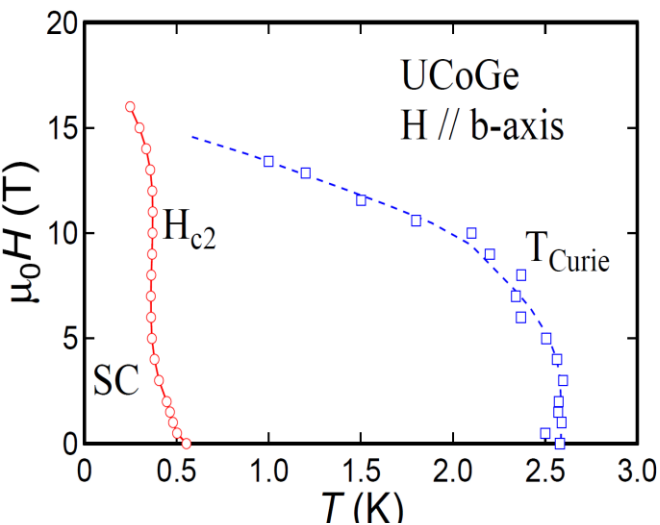
$$T_c = 2.5 \text{ K}, T_{SC} = 0.6 \text{ K}$$

For a review, see:
D. Aoki & J. Flouquet,
JPSJ 2012



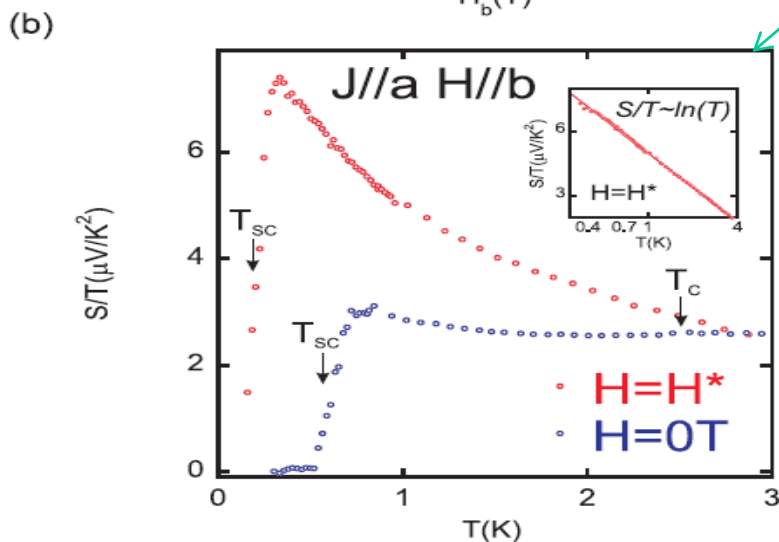
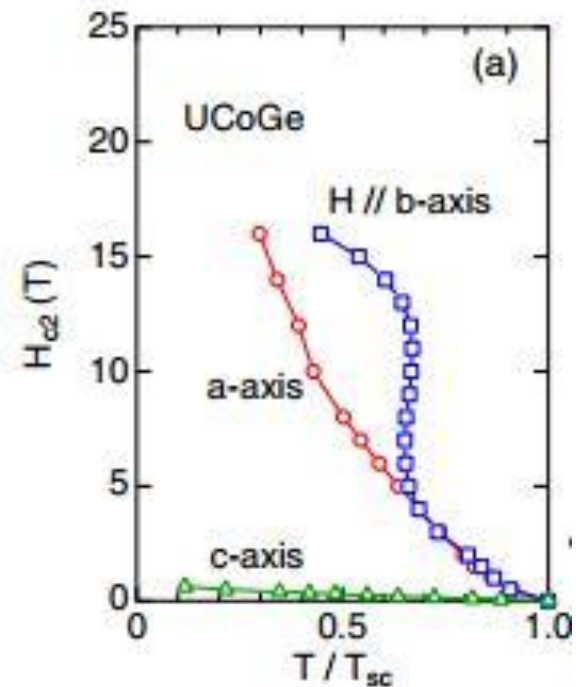
Reentrant superconductivity: Ferromagnetic fluctuations generate a SC dome!

S-shape $H_{c2}(T)$ in UCoGe



Both T_{sc} and S/T peak at H^* !

Logarithmic divergence of S/T at H^* !



Theory for QCP
Paul, Kotliar, '03

Pourret et al., 2013

Thermoelectric Response Near a Quantum Critical Point of β -YbAlB₄ and YbRh₂Si₂: A Comparative Study

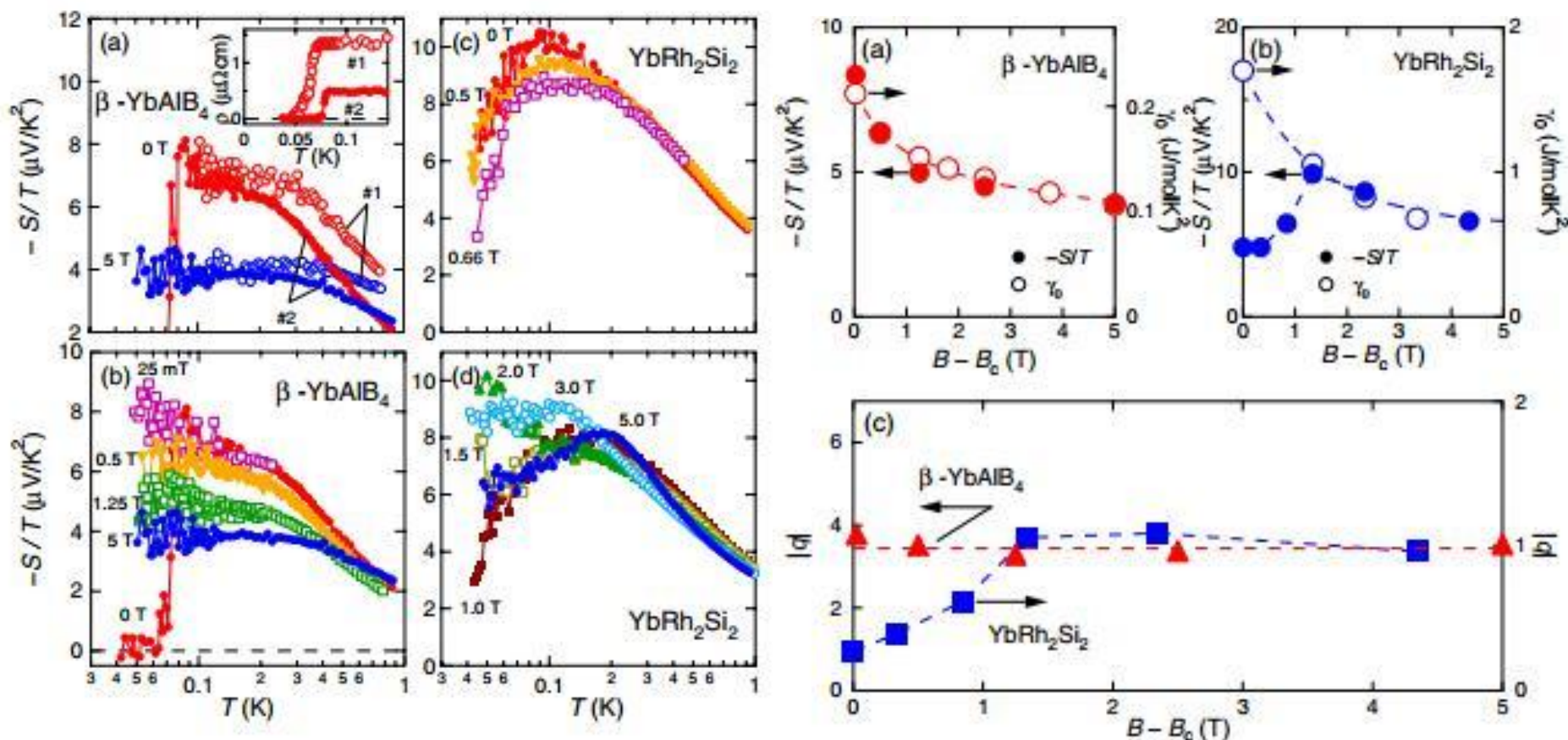
Y. Machida,¹ K. Tomokuni,¹ C. Ogura,¹ K. Izawa,¹ K. Kuga,² S. Nakatsuji,² G. Lapertot,³ G. Knebel,³ J.-P. Brison,³ and J. Flouquet³

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The effective Fermi temperature

- Resistivity
($\mu\Omega\text{cmK}^{-2}$)

$$A = \frac{h}{e^2} a \frac{1}{T_F^2}$$

- Specific heat
($\text{JK}^{-1}\text{mol}^{-1}$)

$$\gamma = \frac{\pi^2}{3} k_B n \frac{1}{T_F}$$

Material-dependent length scale

- Seebeck
(μVK^{-1})

$$\frac{S}{T} = \frac{\pi^2}{3} \frac{k_B}{e} \frac{1}{T_F}$$

Carrier density

All would diverge if T_F vanishes!

Seebeck coefficient is the only intensive coefficient (no geometric factor)!

The Nernst effect

$$\vec{J}_e = \sigma \vec{E} - \alpha \vec{\nabla} T$$

α is now a tensor

$$\vec{J}_Q = \alpha T \vec{E} - \kappa \vec{\nabla} T$$

$$0 = \sigma \vec{E} - \alpha \vec{\nabla} T \quad \longrightarrow \quad \begin{aligned} \sigma_{xx} E_x + \sigma_{xy} E_y &= \alpha_{xx} \nabla_x T + \alpha_{xy} \nabla_y T \\ -\sigma_{xy} E_x + \sigma_{yy} E_y &= -\alpha_{xy} \nabla_x T + \alpha_{yy} \nabla_y T \end{aligned}$$

$$\nabla_y T = 0 \quad \longrightarrow \quad [\sigma_{xy}^2 + \sigma_{xx} \sigma_{yy}] E_y = [\sigma_{xy} \alpha_{xx} - \sigma_{xx} \alpha_{xy}] \nabla_x T$$

$$N = \frac{-E_y}{\nabla_x T} = \frac{\alpha_{xy} \sigma_{xx} - \alpha_{xx} \sigma_{xy}}{\sigma_{xx} \sigma_{yy} + \sigma_{xy}^2}$$

Nernst effect and Hall mobility

$$N = \frac{\alpha_{xy} \sigma_{xx} - \alpha_{xx} \sigma_{xy}}{\sigma_{xx}^2 + \sigma_{xy}^2}$$

$$\Theta_H = \frac{\sigma_{xy}}{\sigma_{xx}} \quad \longrightarrow \quad \frac{\partial \Theta_H}{\partial \epsilon} = \frac{\sigma_{xy} \frac{\partial \sigma_{xx}}{\partial \epsilon} - \sigma_{xx} \frac{\partial \sigma_{xy}}{\partial \epsilon}}{\sigma_{xx}^2 + \sigma_{xy}^2}$$

Extended Mott formula:

$$\alpha_{xx} = \frac{\pi^2}{3} \frac{k_B^2 T}{e} \frac{\partial \sigma_{xx}}{\partial \epsilon}$$

$$\alpha_{xy} = \frac{\pi^2}{3} \frac{k_B^2 T}{e} \frac{\partial \sigma_{xy}}{\partial \epsilon}$$

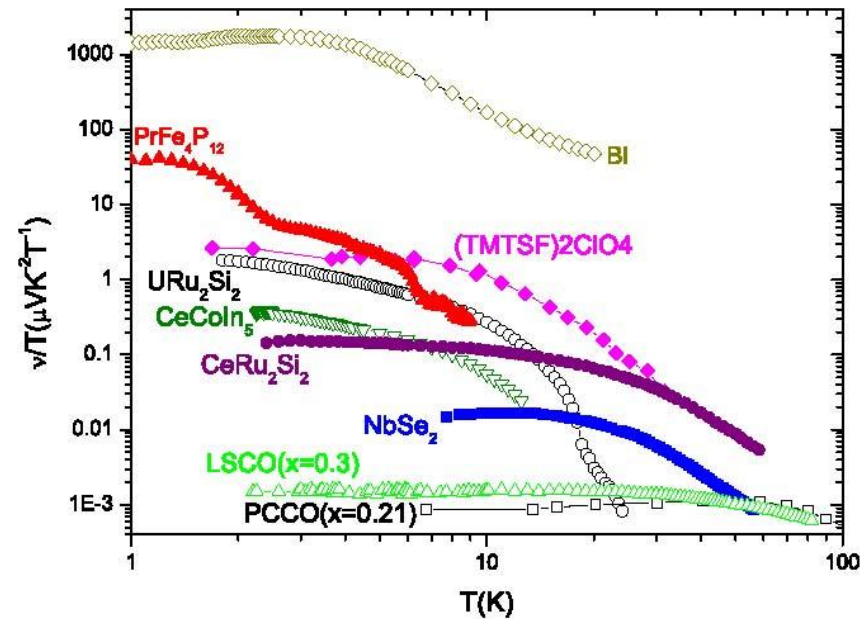
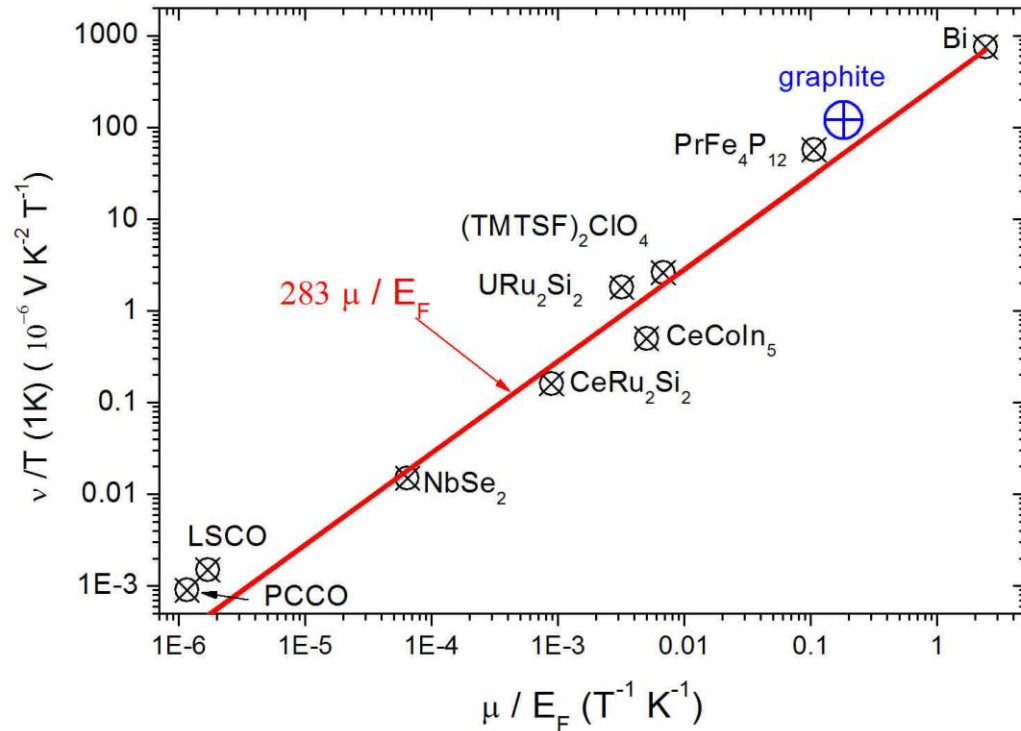
$$N = \frac{\pi^2}{3} \frac{k_B^2 T}{e} \frac{\partial \Theta_H}{\partial \epsilon} \Big|_{\epsilon_F}$$

Nernst effect measures the change in the Hall mobility induced by shifting the Fermi level!

The Hall mobility

$$\Theta_H = \mu_H = \frac{e\tau}{m^*} = \frac{e}{\hbar} \frac{\ell}{k_F}$$

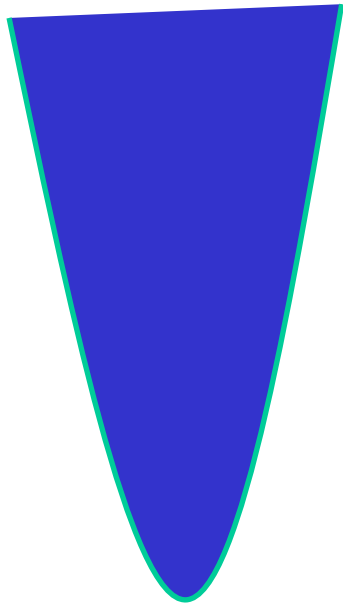
$$\Theta_H(\varepsilon) \propto \varepsilon^\gamma \quad \left. \frac{v}{T} = \frac{\pi^2}{3} \frac{k_B^2}{eB} \frac{\partial \Theta_H}{\partial \varepsilon} \right|_{\varepsilon_F} \Rightarrow \left. \frac{v}{T} \approx \frac{\pi^2}{3} \frac{k_B^2}{e} \frac{\mu}{\varepsilon_F} \right|_{\varepsilon_F}$$



Quantum oscillations and the quantum limit

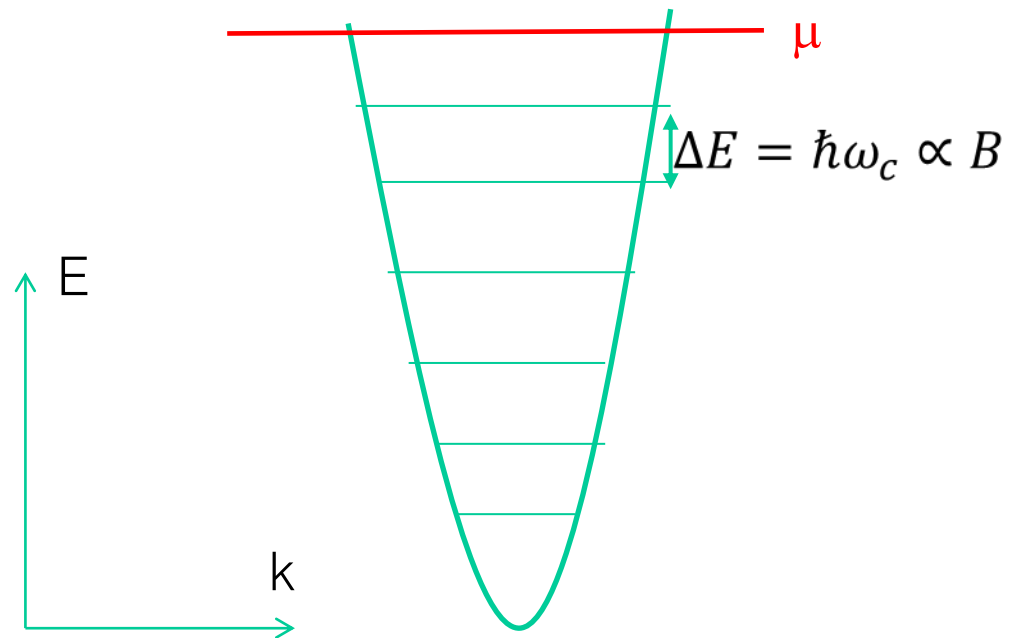
Landau quantization

$B = 0$



$$E = \frac{\hbar^2}{2m^*} (k_x^2 + k_y^2)$$

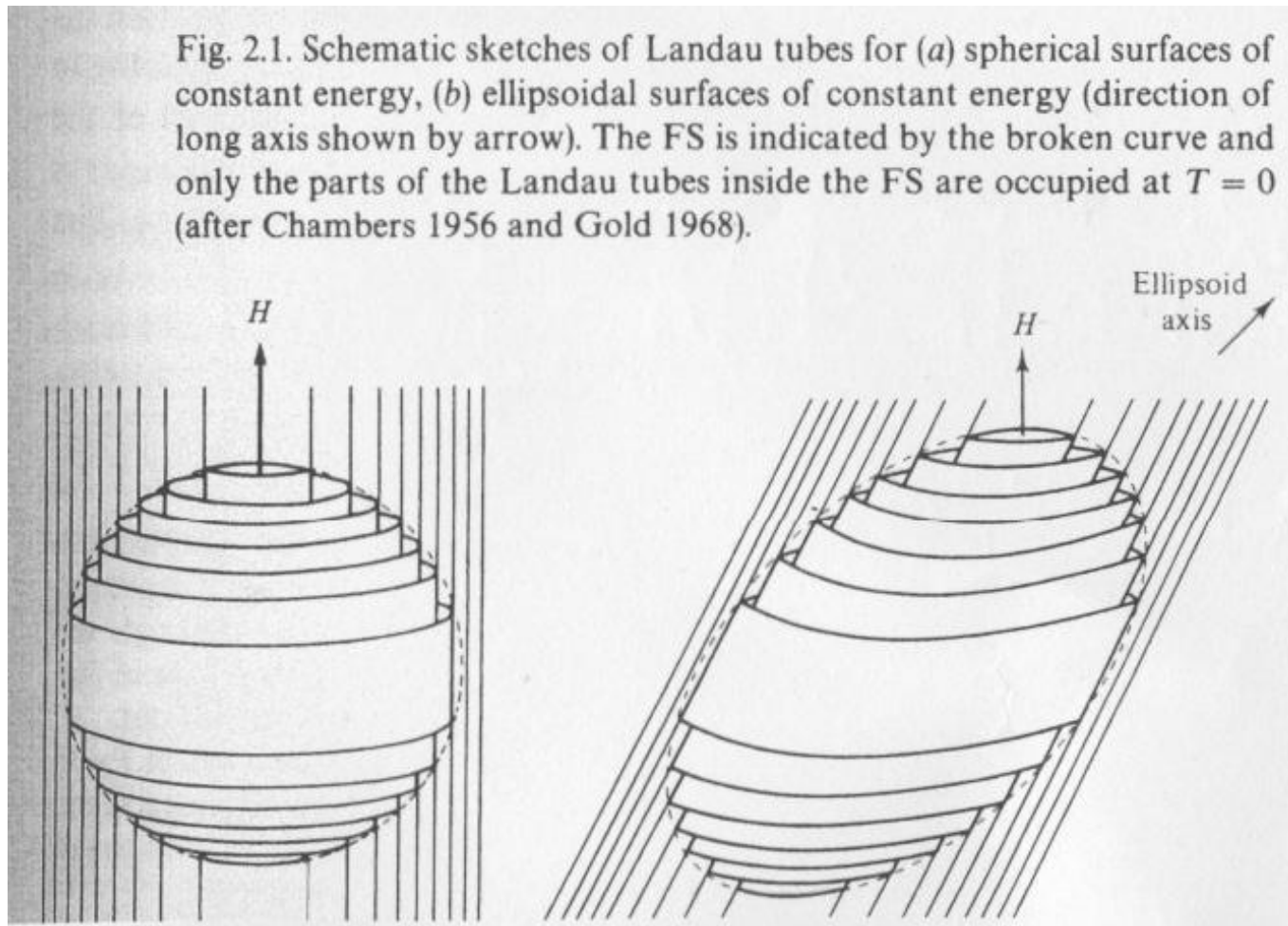
$B \neq 0$



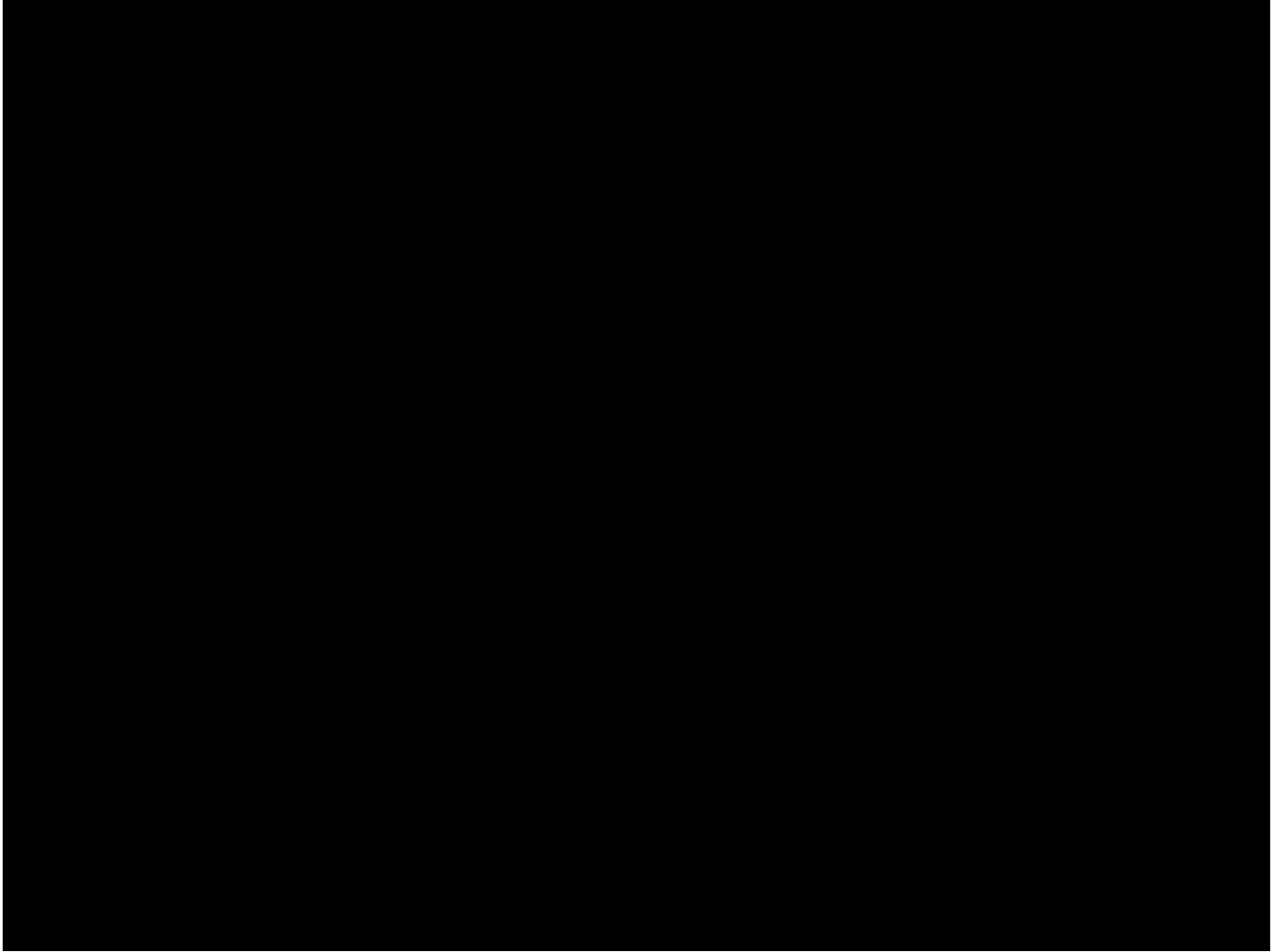
$$E_n = \hbar\omega_c \left(n + \frac{1}{2}\right)$$

Electron energy spectrum is no more a continuum.

Fermi surface truncated by Landau tubes



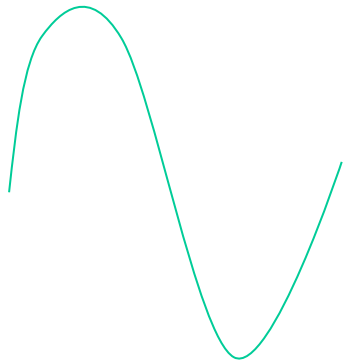
Shoenberg 1984



The magnetic field required to attain the quantum limit

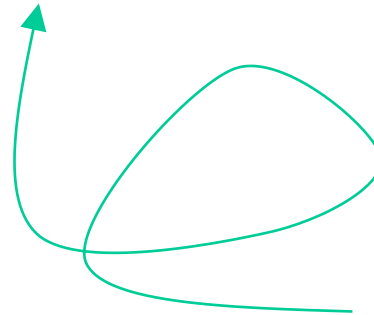
When the magnetic length becomes shorter than the Fermi wave length!

$$\lambda_F \propto n^{-1/3}$$



Wave (wave-length)

$$l_B \propto B^{-1/2}$$



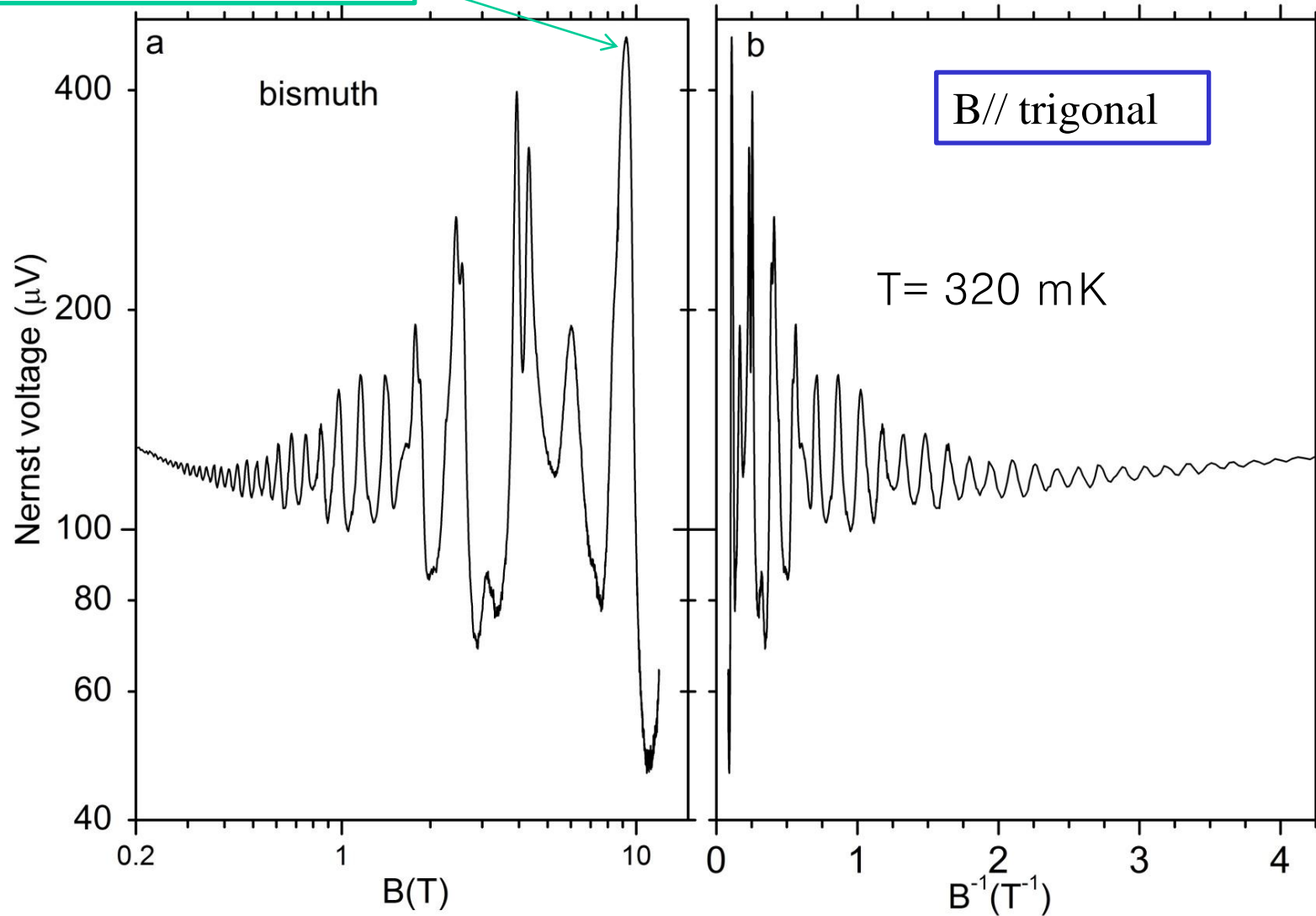
Particle (radius of curved trajectory)

The lower the carrier density, the lower B_{QL} !

	Copper	bismuth
Carrier density (cm ⁻³)	8.5 10 ²²	3 10 ¹⁷
λ_F (nm)	0.5	47
B_{QL} (T)	30000	9

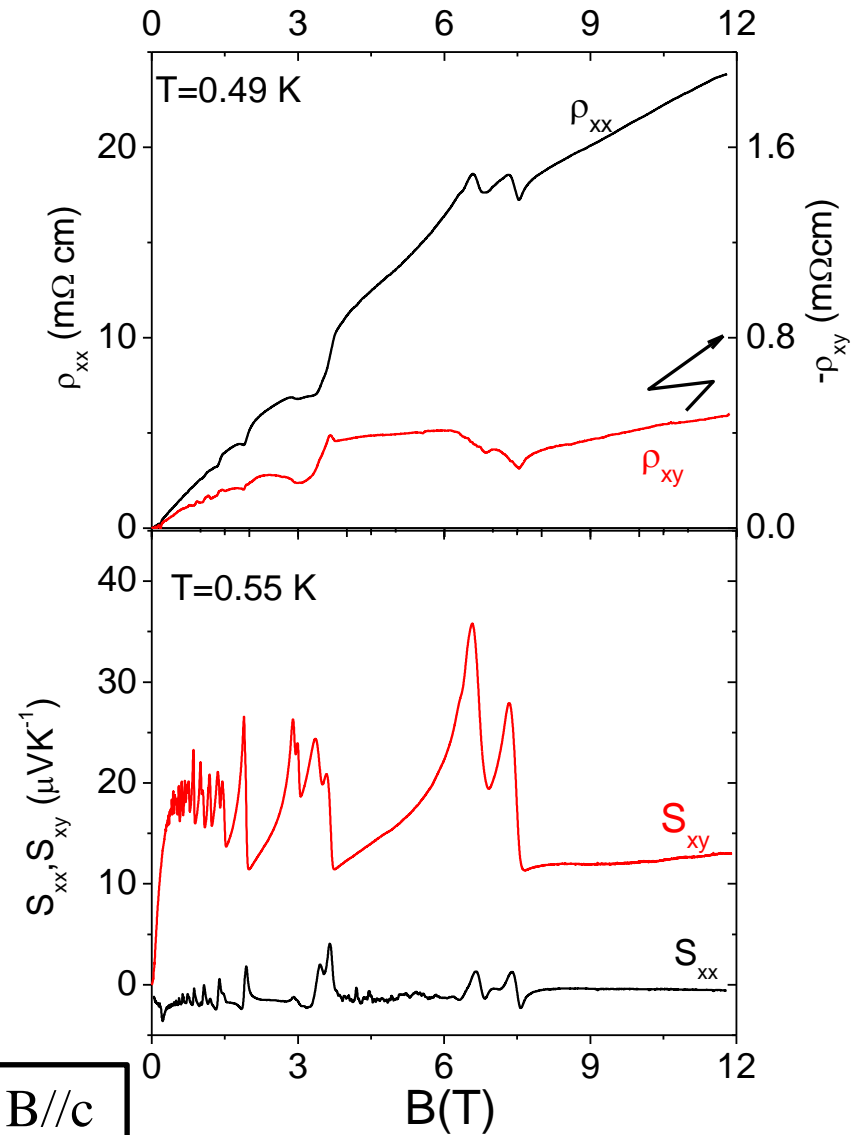
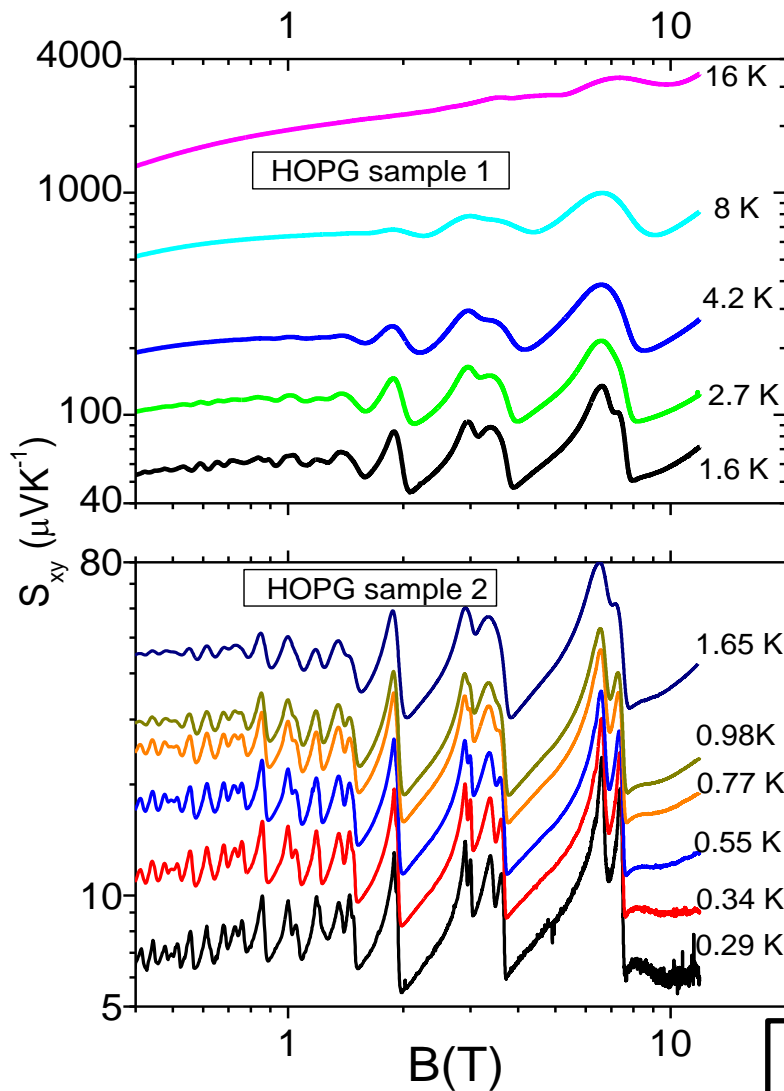
Giant quantum oscillations of the Nernst response

The last expected peak @ 9 T



Giant Nernst quantum oscillations in graphite

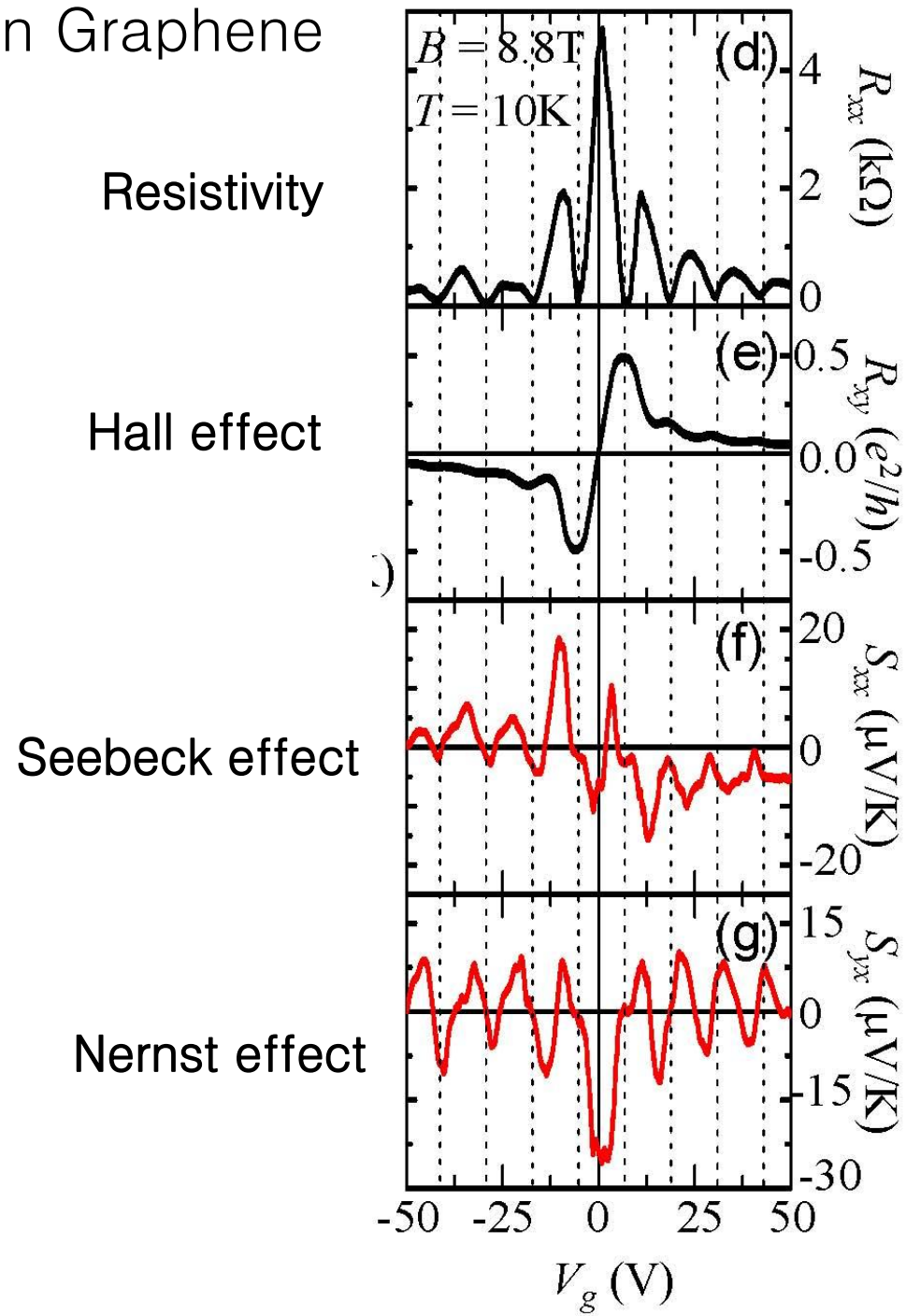
Zhu et al., Nature Physics 2009



Nernst quantum oscillations in Graphene

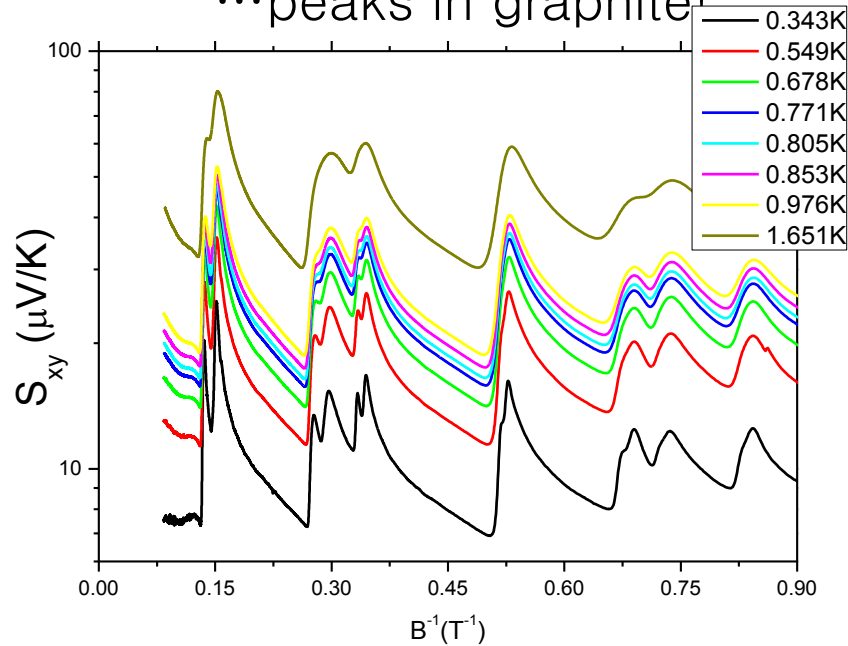
Zuev et al. (Philip Kim's group)
PRL 2009

Magnetic field is kept constant
and the gate voltage is scanned.

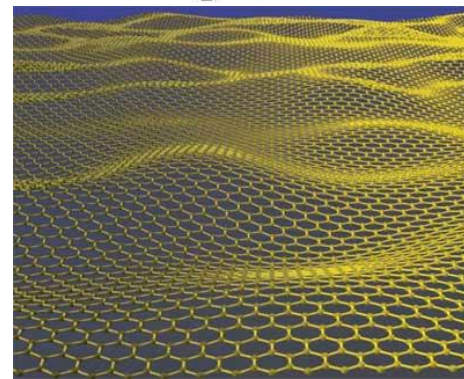
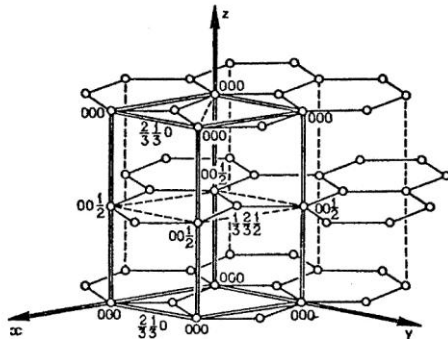
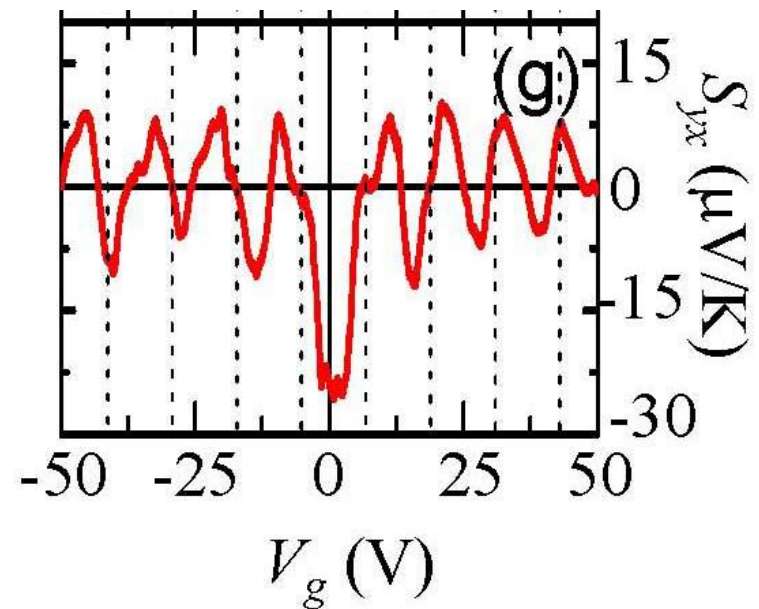


When a Landau level intersects the Fermi level, the Nernst response...

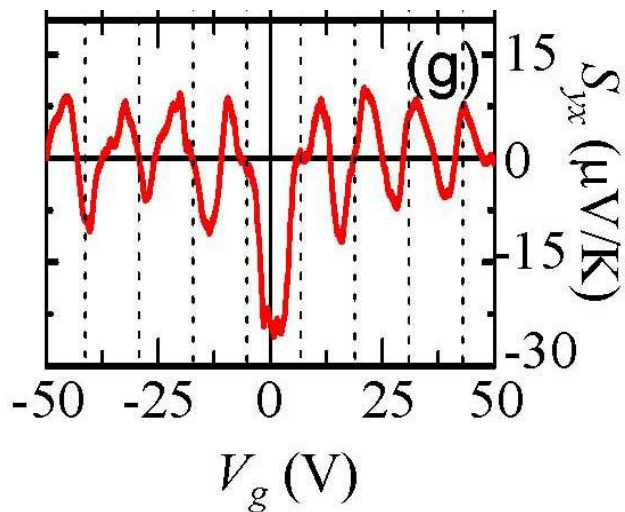
...peaks in graphite!



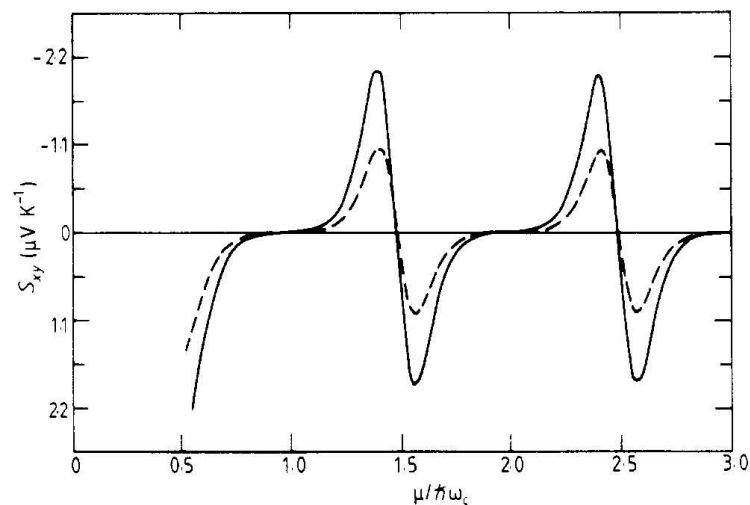
...vanishes in graphene!



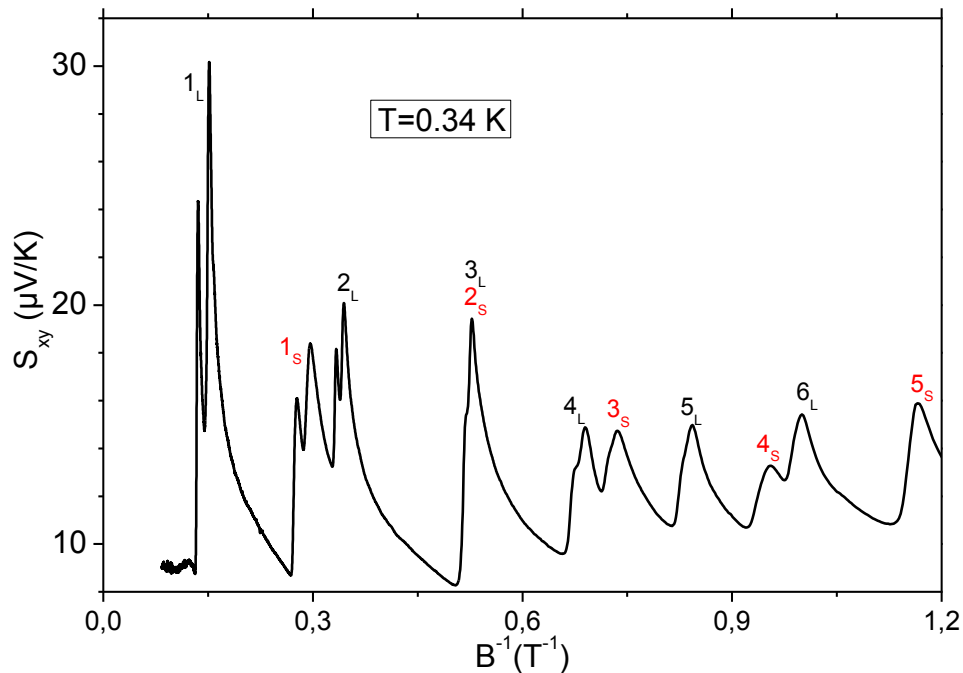
Experiment: graphene



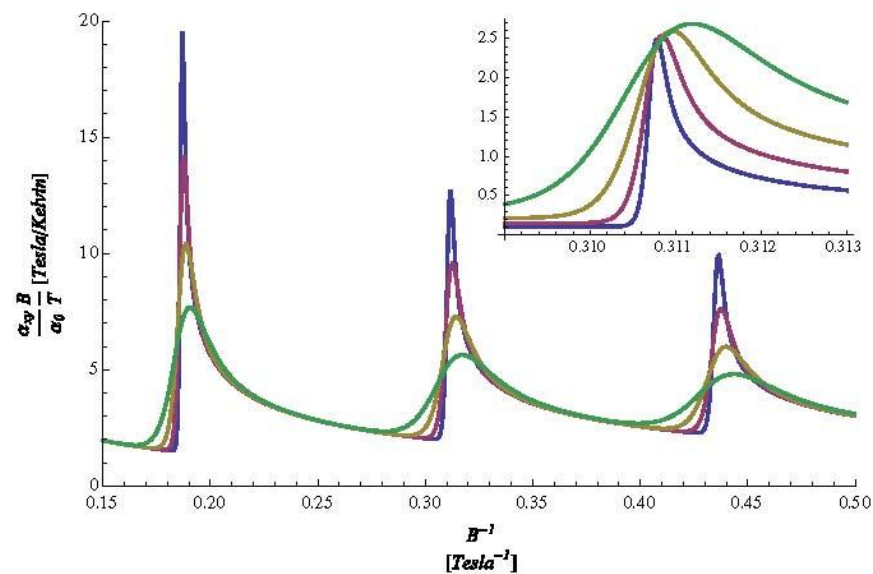
Theory :2D
(Girvin, Jonson PRB 1984)



Experiment: graphite



Theory :3D
(Bergman&Oganesyan PRL 2010)



Recent theory on Nernst quantum oscillations

PRL **104**, 066601 (2010)

PHYSICAL REVIEW LETTERS

week ending
12 FEBRUARY 2010

Theory of Dissipationless Nernst Effects

Doron L. Bergman¹ and Vadim Oganesyan²

¹*Department of Physics, California Institute of Technology, Pasadena, California 91125, USA*

²*Department of Engineering Science and Physics, College of Staten Island, CUNY, Staten Island, New York 10314, USA*

(Received 14 October 2009; published 11 February 2010)

PHYSICAL REVIEW B **83**, 085103 (2011)

Oscillations of the Nernst coefficient in bismuth

Yu. V. Sharlai and G. P. Mikitik

B. Verkin Institute for Low Temperature Physics & Engineering, Ukrainian Academy of Sciences, Kharkov 61103, Ukraine

(Received 29 October 2010; published 9 February 2011)

PRL **107**, 016601 (2011)

PHYSICAL REVIEW LETTERS

week ending
1 JULY 2011

Giant Nernst-Ettingshausen Oscillations in Semiclassically Strong Magnetic Fields

Igor A. Luk'yanchuk,¹ Andrei A. Varlamov,² and Alexey V. Kavokin³

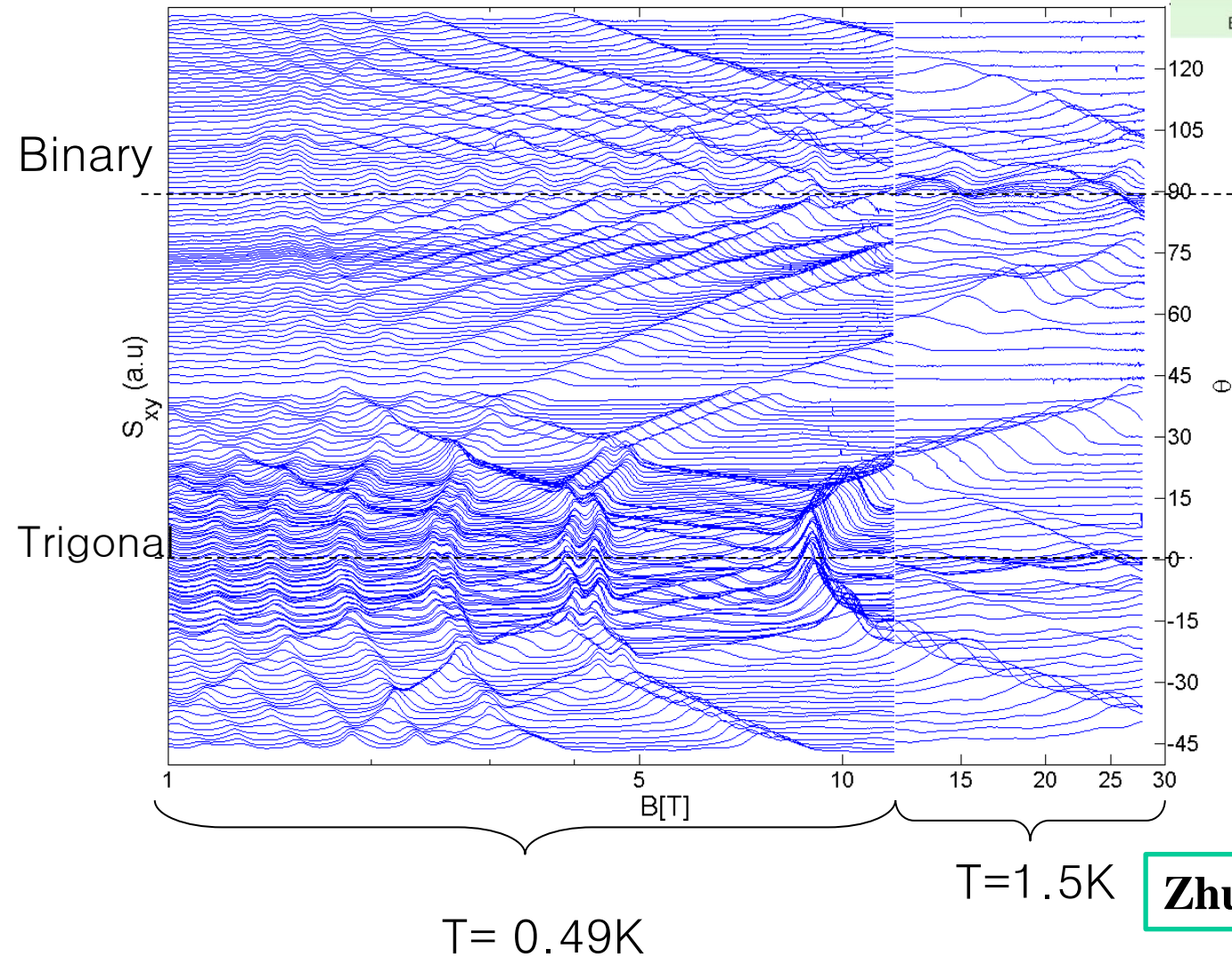
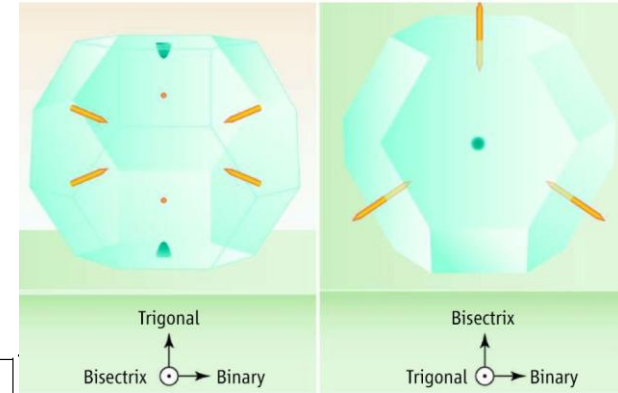
¹*Laboratory of Condensed Matter Physics, University of Picardie Jules Verne, Amiens, 80039, France*

²*CNR-SPIN, Viale del Politecnico 1, I-00133 Rome, Italy*

³*Physics and Astronomy School, University of Southampton, Highfield, Southampton, SO171BJ, United Kingdom*

(Received 28 November 2010; published 29 June 2011)

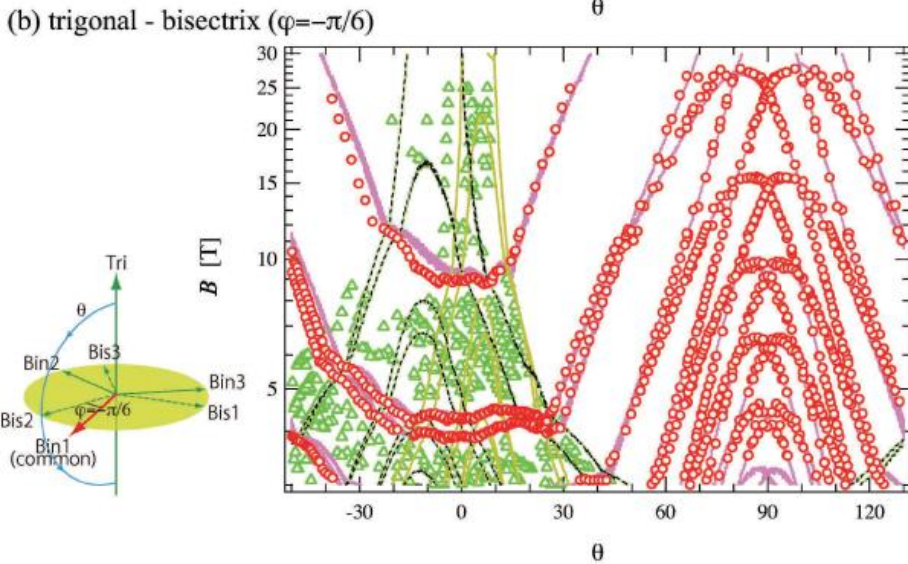
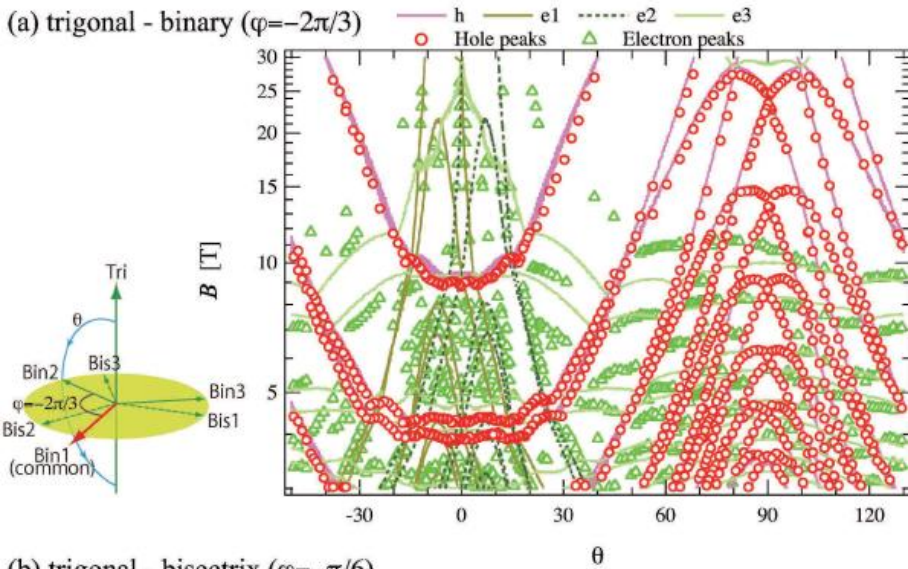
Angle-resolved Nernst effect in bismuth



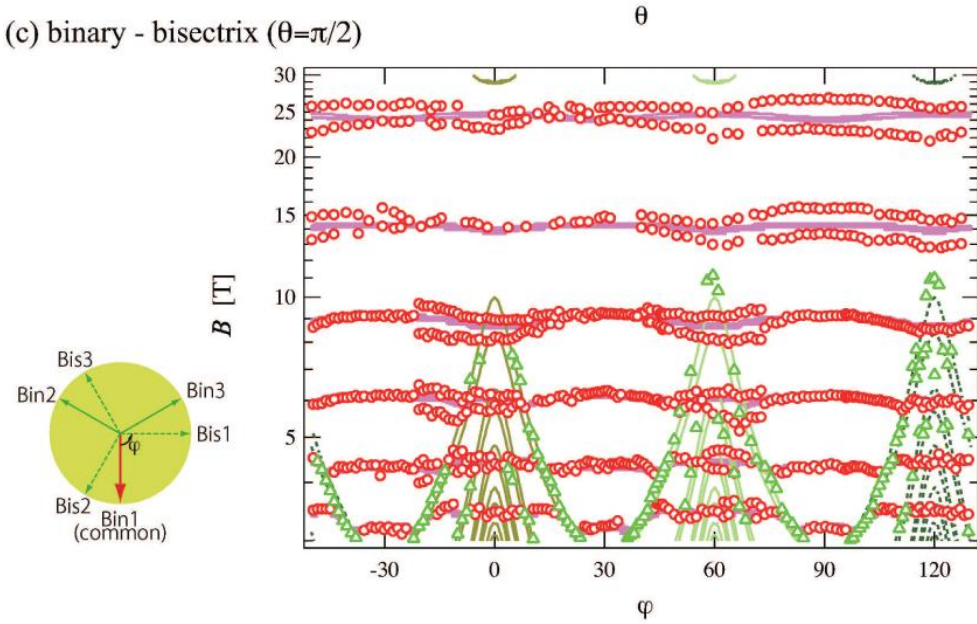
Nernst peaks shift as the magnetic field tilts!

Zhu et al., PNAS (2012)

Angle-resolved Landau spectrum in bismuth (experiment and theory)



(c) binary - bisectrix ($\theta = \pi/2$)



Symbols: experimental data;
Lines: theory

Agreement is very good for holes,
but only fair for electrons

Zhu et al., PNAS (2012)

The band picture of metals and insulators!

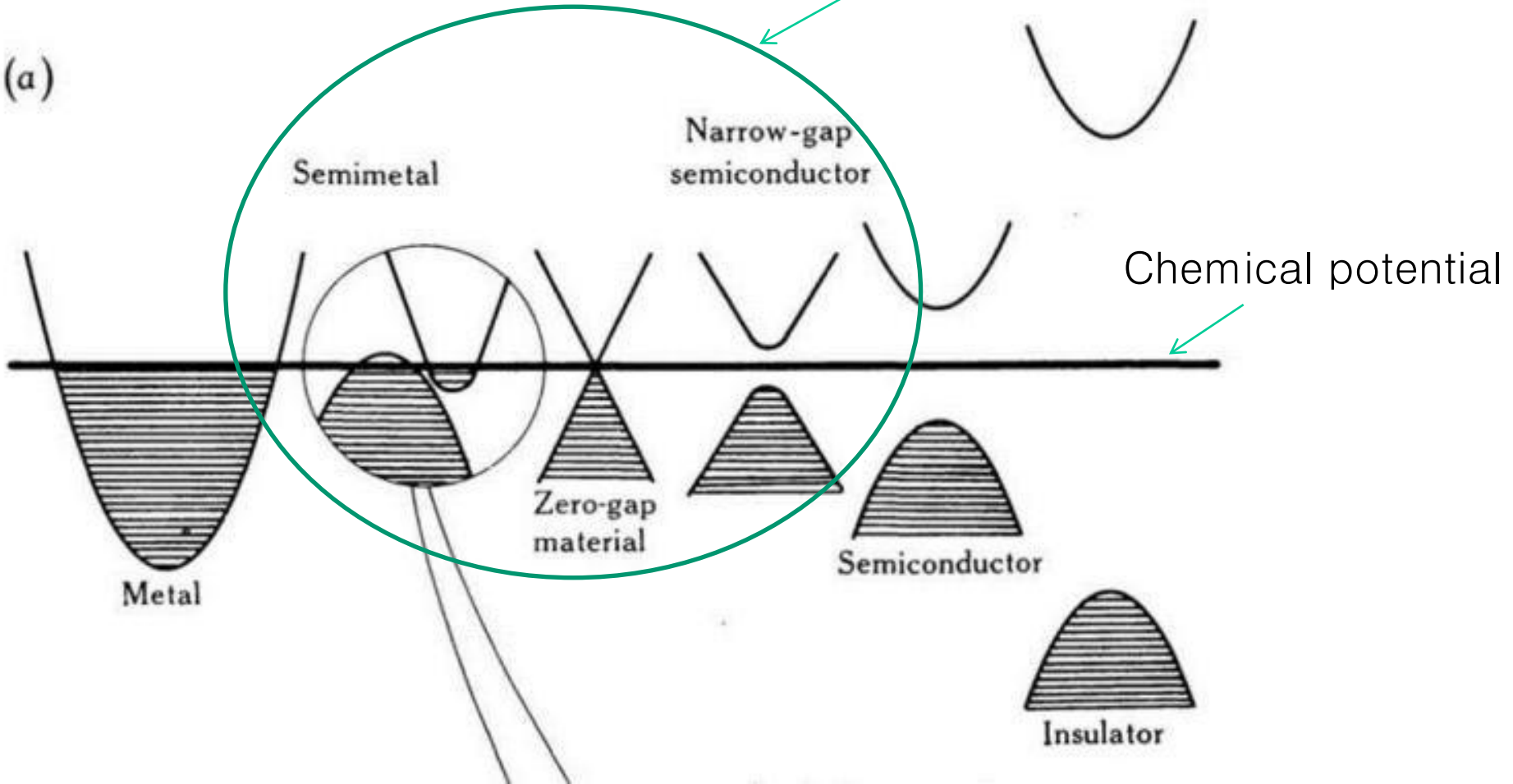
Interesting thermoelectricity

Conductors

J.-P. Issi,
Aust. J. Phys. (1979)

Insulators

(a)



Chemical potential

How does an insulator become a metal?

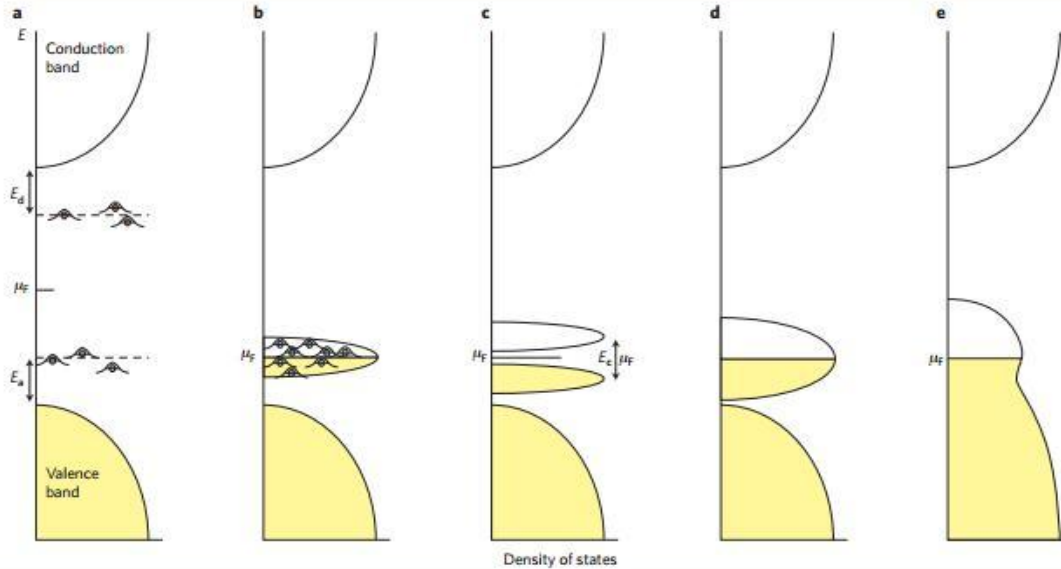
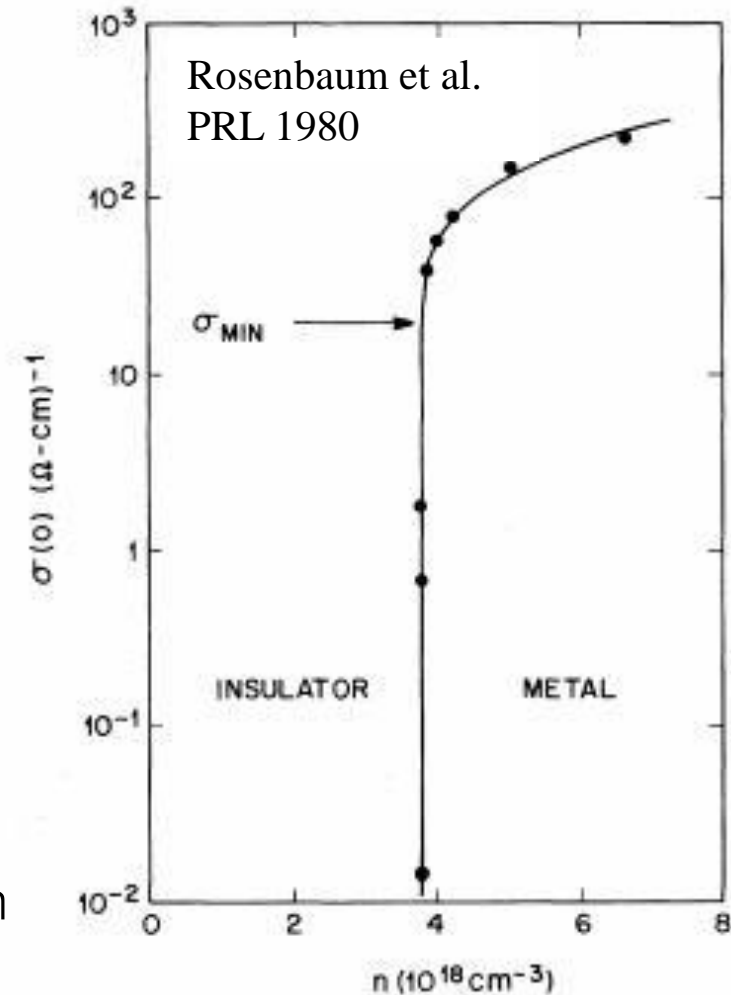


Figure B2 | Evolution of the electronic density of states and band structure with increasing p-type doping. Doping increases from a to e. Colour area represents filled states.

doping

X. Blase et al.,
Nature Materials (2009)

phosphorus-doped silicon



Fermiology of doped semi-conductors

- **Self-doped Bi_2Se_3** believed to be a bulk topological insulator with non-trivial surface states.
- **$\text{SrTiO}_{3-\delta}$** discovered in 1964 as the first case of a “semiconducting superconductor”
- Many others to be explored: PbTe, InSb, ...)

Topological insulators in Bi_2Se_3 , Bi_2Te_3 and Sb_2Te_3 with a single Dirac cone on the surface

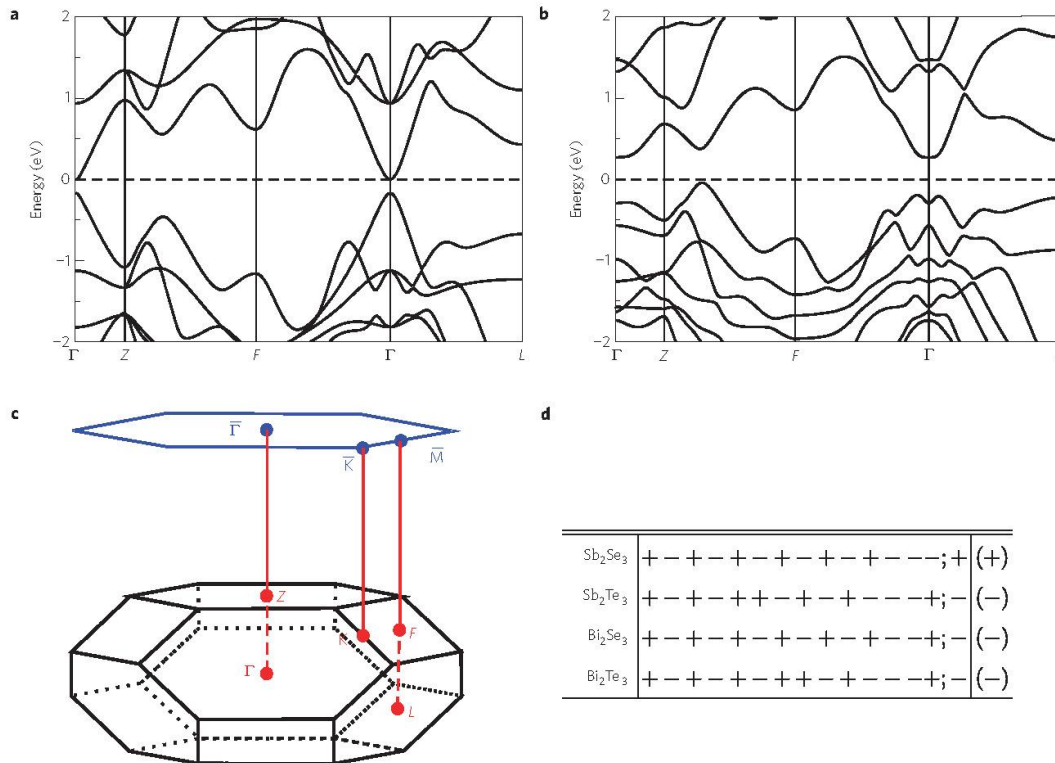


Figure 2 | Band structure, Brillouin zone and parity eigenvalues. **a, b**, Band structure for Bi_2Se_3 without (**a**) and with (**b**) SOC. The dashed line indicates the Fermi level. **c**, Brillouin zone for Bi_2Se_3 with space group $R\bar{3}m$. The four inequivalent time-reversal-invariant points are $\Gamma(0, 0, 0)$, $L(\pi, 0, 0)$, $F(\pi, \pi, 0)$ and $Z(\pi, \pi, \pi)$. The blue hexagon shows the 2D Brillouin zone of the projected $(1, 1, 1)$ surface, in which the high-symmetry \mathbf{k} points $\bar{\Gamma}$, \bar{K} and \bar{M} are labelled. **d**, The parity of the band at the Γ point for the four materials Sb_2Te_3 , Sb_2Se_3 , Bi_2Se_3 and Bi_2Te_3 . Here, we show the parities of fourteen occupied bands, including five s bands and nine p bands, and the lowest unoccupied band. The product of the parities for the fourteen occupied bands is given in brackets on the right of each row.

Topological? Sure!
Insulator? Hum...

Which side of the metal–insulator transition?

Critical density for metal-insulator transition

The Mott criterion:
Metallicity emerges
when two length
scales become
comparable

$$a_H n^{1/3} \cong 0.26$$

Edwards and Sienko,
PRB 1978

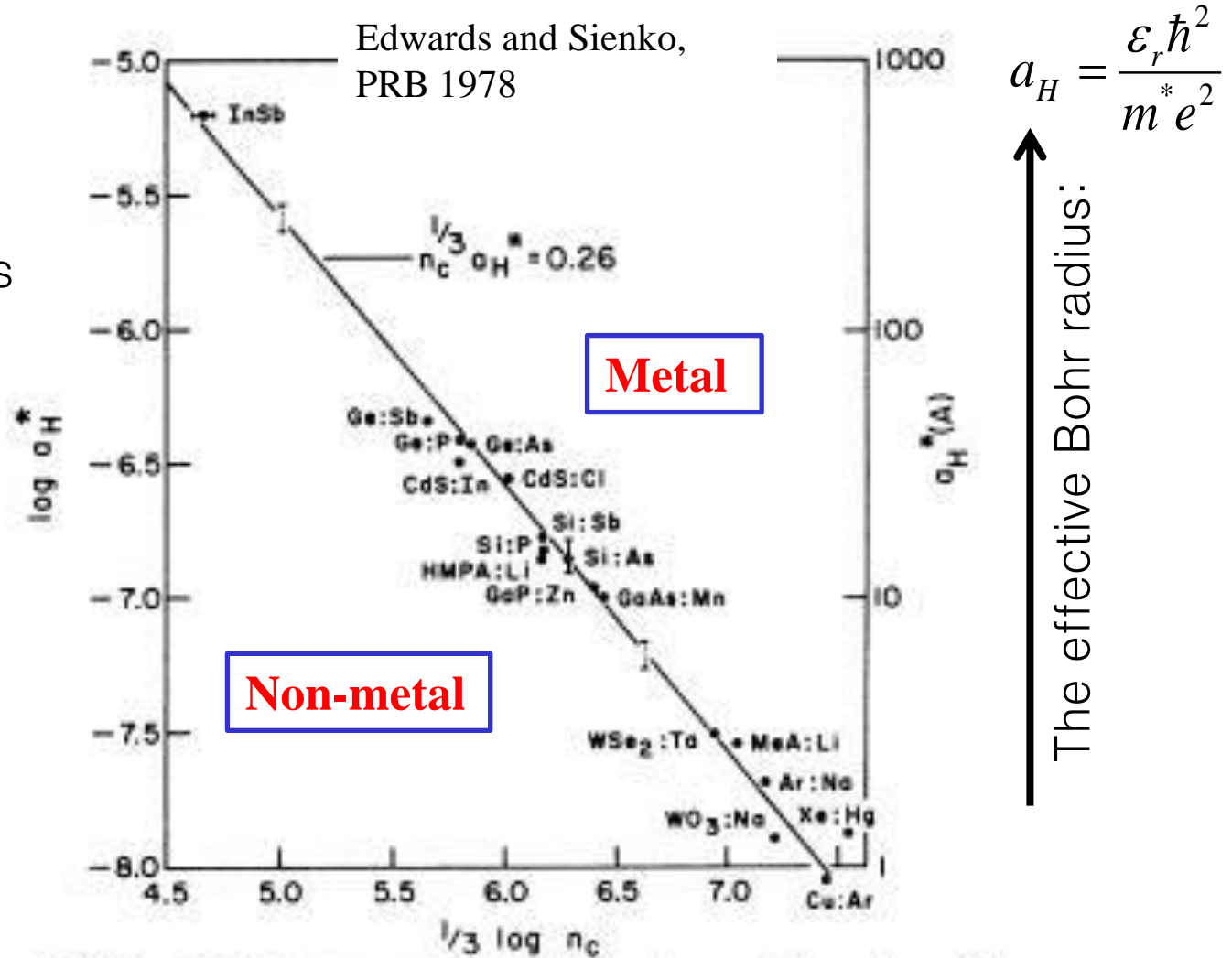
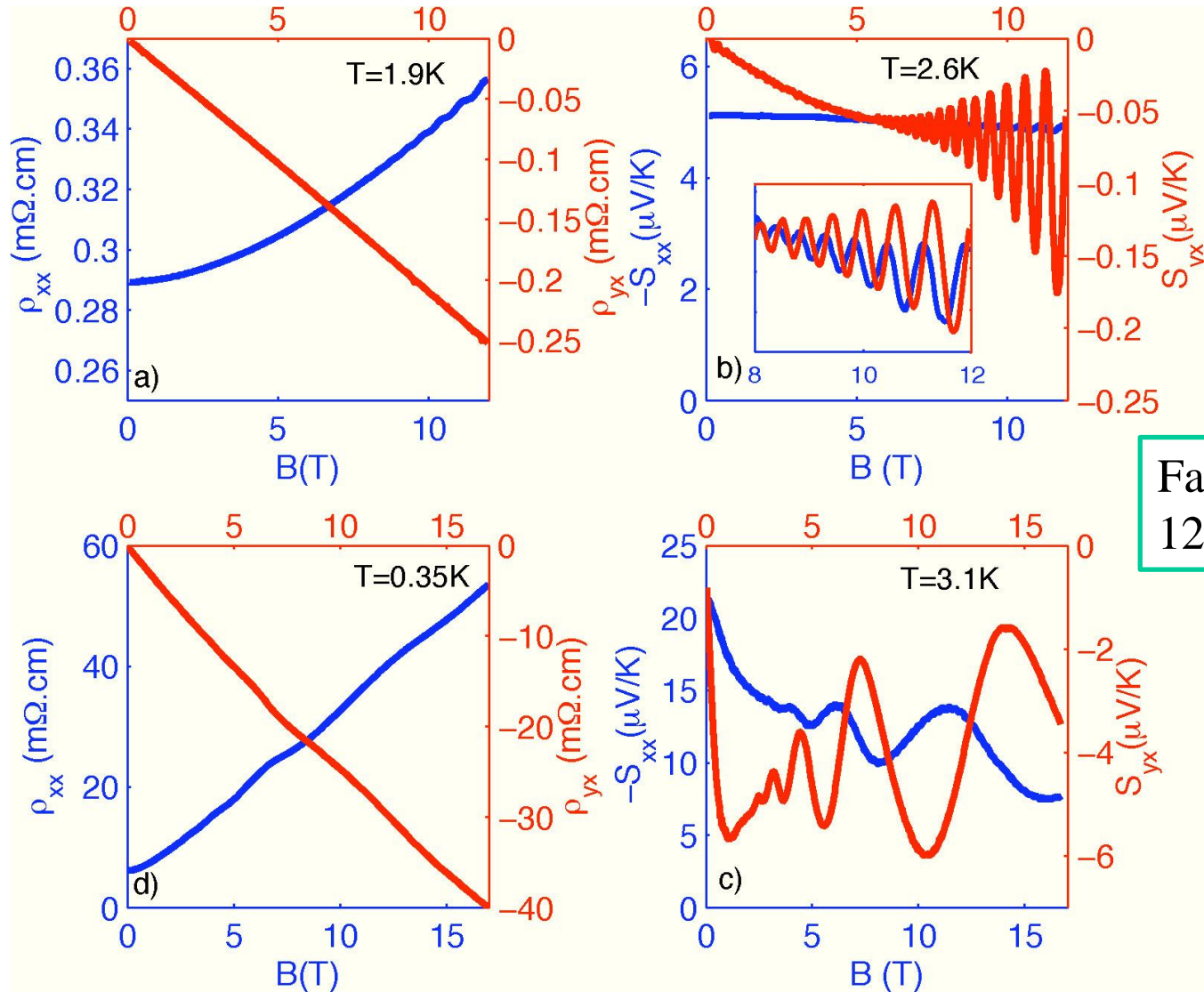


FIG. 1. Metal-nonmetal transition in condensed media. A plot of $\log a_H^*$ vs $\frac{1}{3} \log n_c$ (symbols defined in the text).

The interdopant distance: $n^{1/3}$

Quantum oscillations of the Nernst effect in Bi_2Se_3



$n = 10^{19} \text{ cm}^{-3}$

Fauqué et al., arXiv:
1209.1312

$n = 10^{17} \text{ cm}^{-3}$

A sharp bulk Fermi surface down to 10^{17} cm^{-3}

Two routes towards Fermi temperature

Thermopower

$$\frac{S}{T} = \frac{\pi^2}{3} \frac{K_B}{e} \frac{1}{T_F}$$

@ 10^{19} cm^{-3}

Fauqué et al., PRB (2013)

Quantum oscillations:

$$k_B T_F = \frac{\hbar^2 k_F^2}{2m^*}$$

@ 10^{17} cm^{-3}

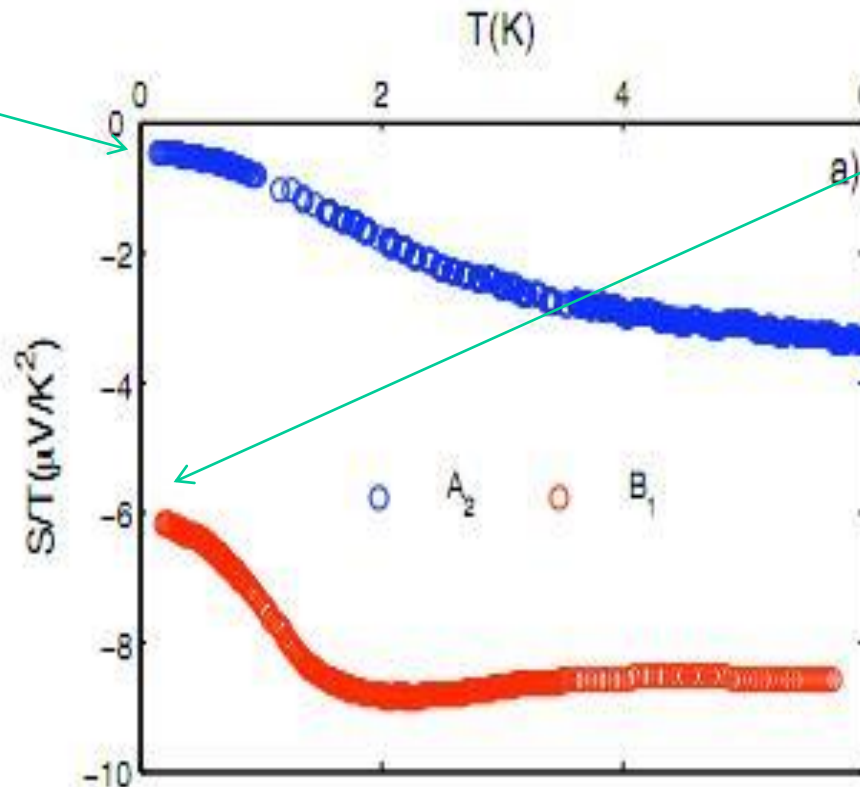
$S/T = -0.45 \mu\text{VK}$

$F = 170 \text{ T}$

$m^* = 0.2m_e$



$T_F = 900 \text{ K}$



$S/T = -6.1 \mu\text{VK}^{-2}$

$F = 15 \text{ T}$

$m^* = 0.18m_e$



$T_F = 87 \text{ K}$

n- doped SrTiO₃

PHYSICAL REVIEW

VOLUME 163, NUMBER 2

10 NOVEMBER 1967

Superconducting Transition Temperatures of Semiconducting SrTiO₃

C. S. KOONCE* AND MARVIN L. COHEN†

Department of Physics, University of California, Berkeley, California

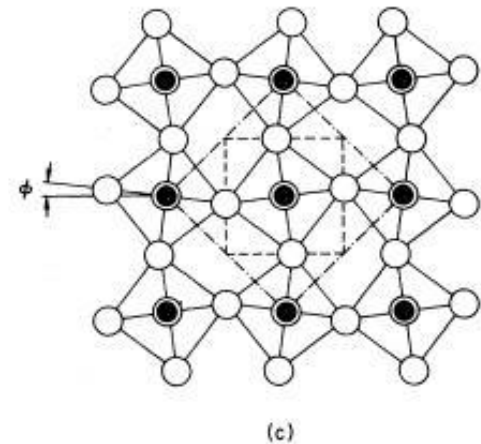
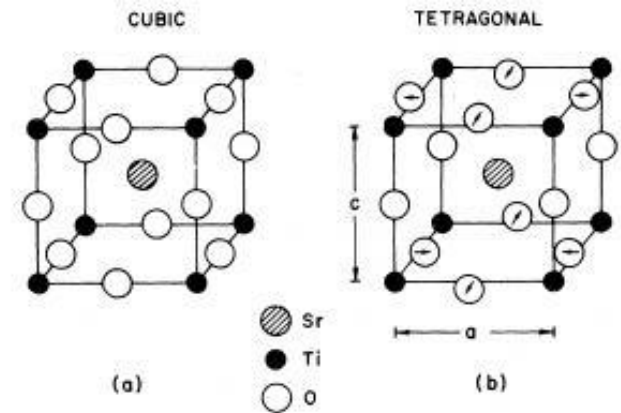
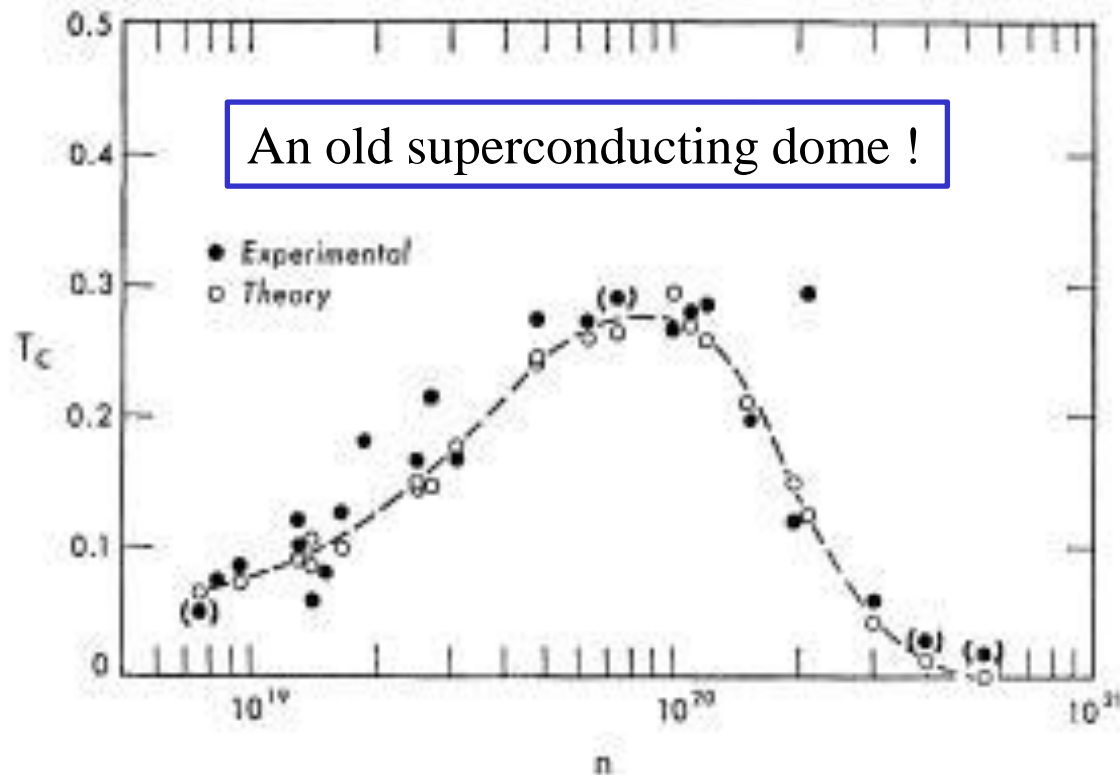
AND

J. F. SCHOOLEY,‡ W. R. HOSLER,§ AND E. R. PFEIFFER

National Bureau of Standards, Washington, D. C.

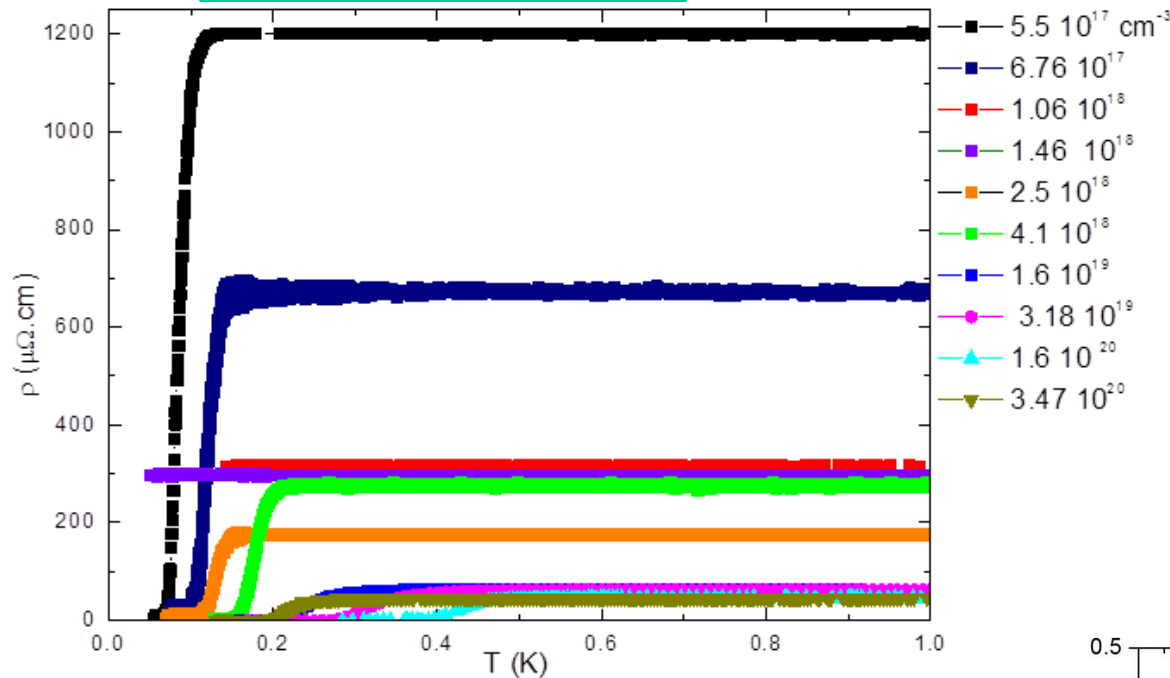
(Received 5 July 1967)

An old superconducting dome !



Superconductivity in bulk n-doped SrTiO₃

Lin et al., PRX 2013

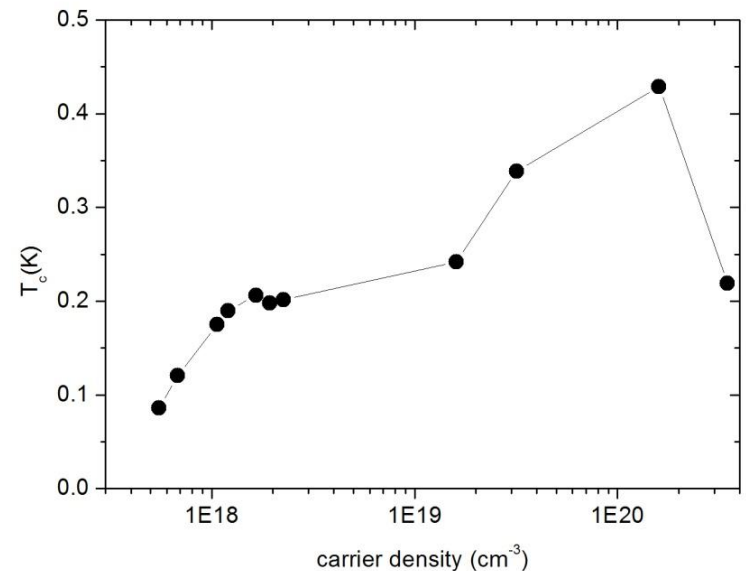


- n-doping:

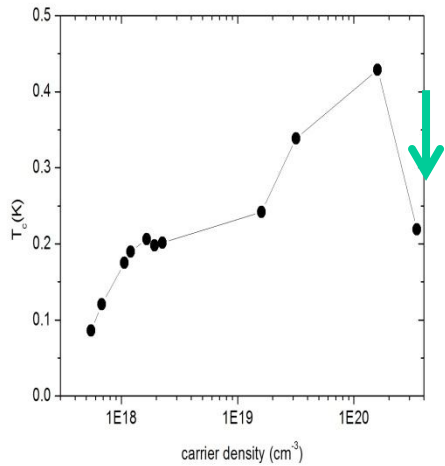
removing oxygen or replacing Ti with Nb

- Carrier density window:

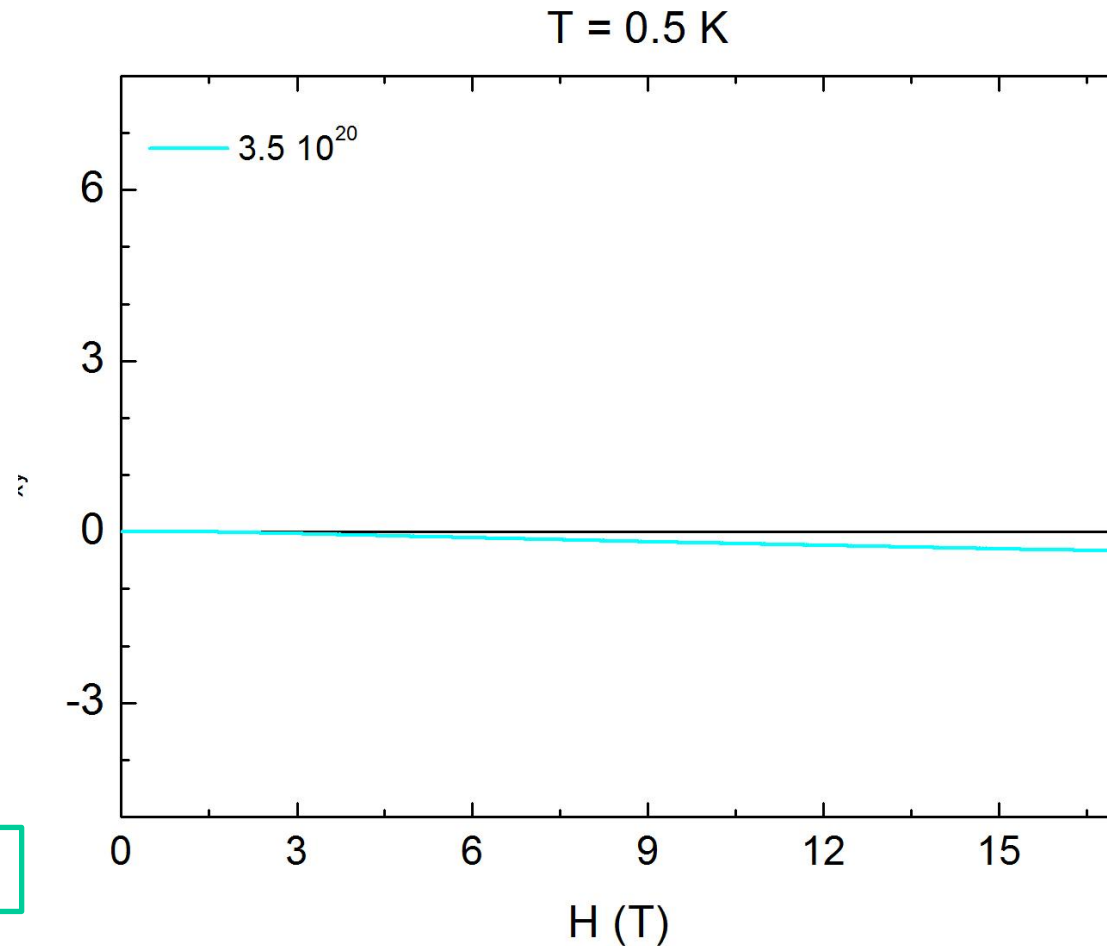
between 5×10^{17} to $3 \times 10^{20} \text{ cm}^{-3}$



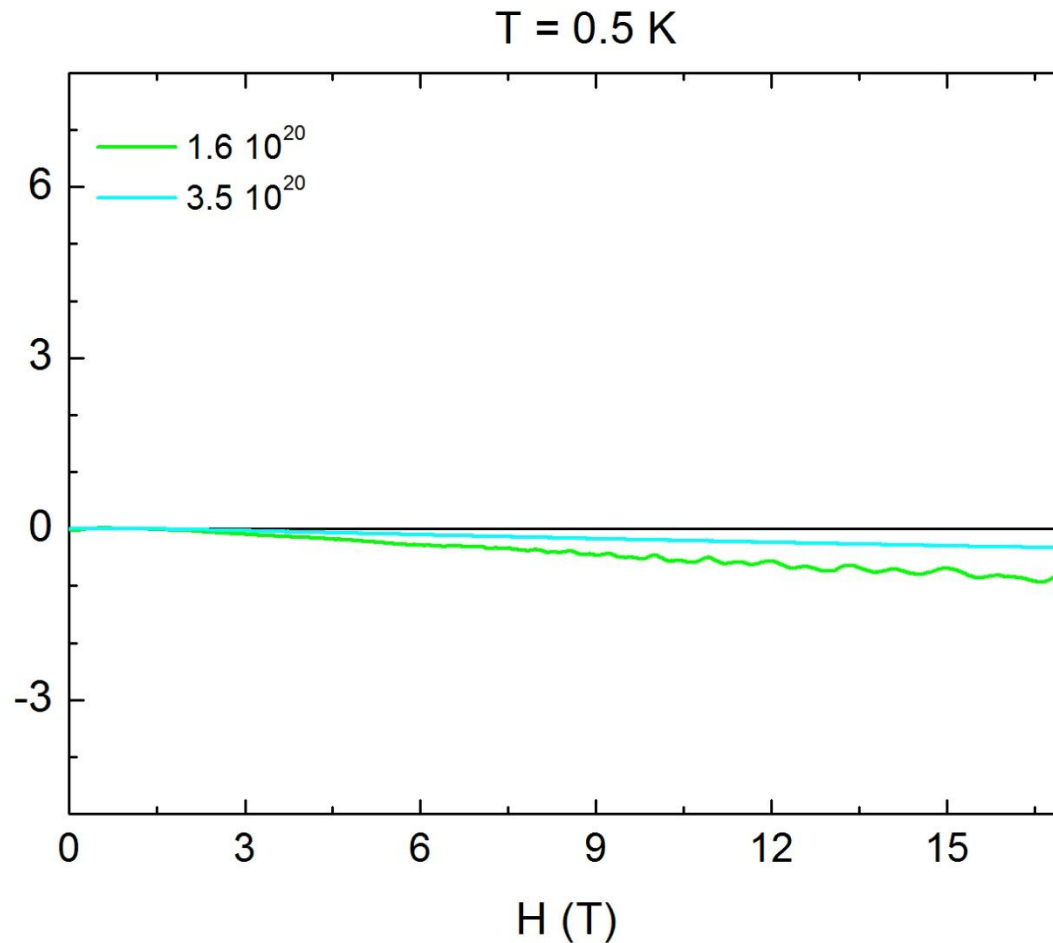
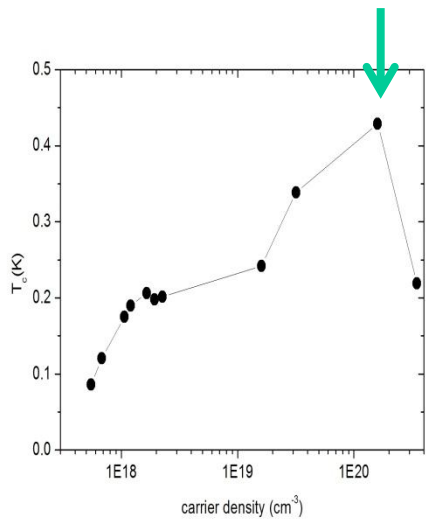
Emergence of Nernst oscillations with underdoping



Lin et al., PRX 2013

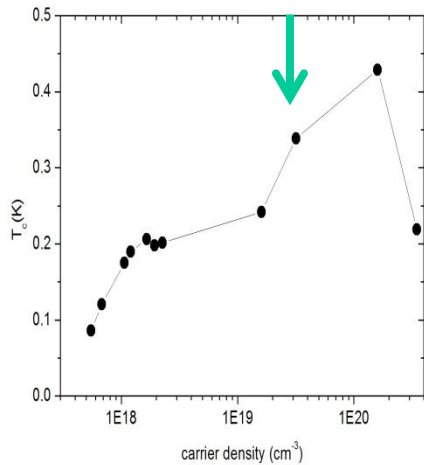


Emergence of Nernst oscillations with underdoping

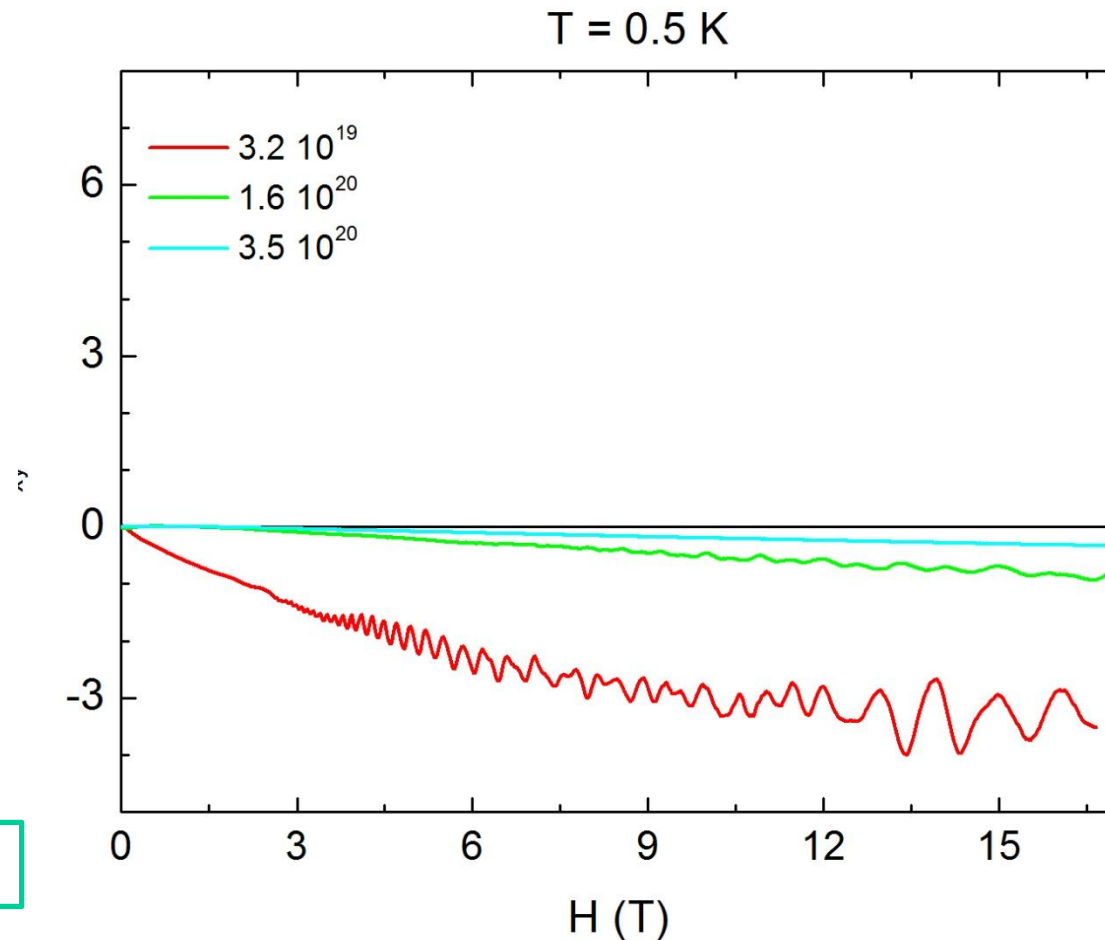


Lin et al., PRX 2013

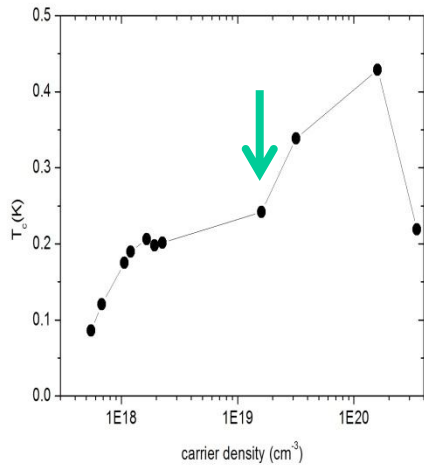
Emergence of Nernst oscillations with underdoping



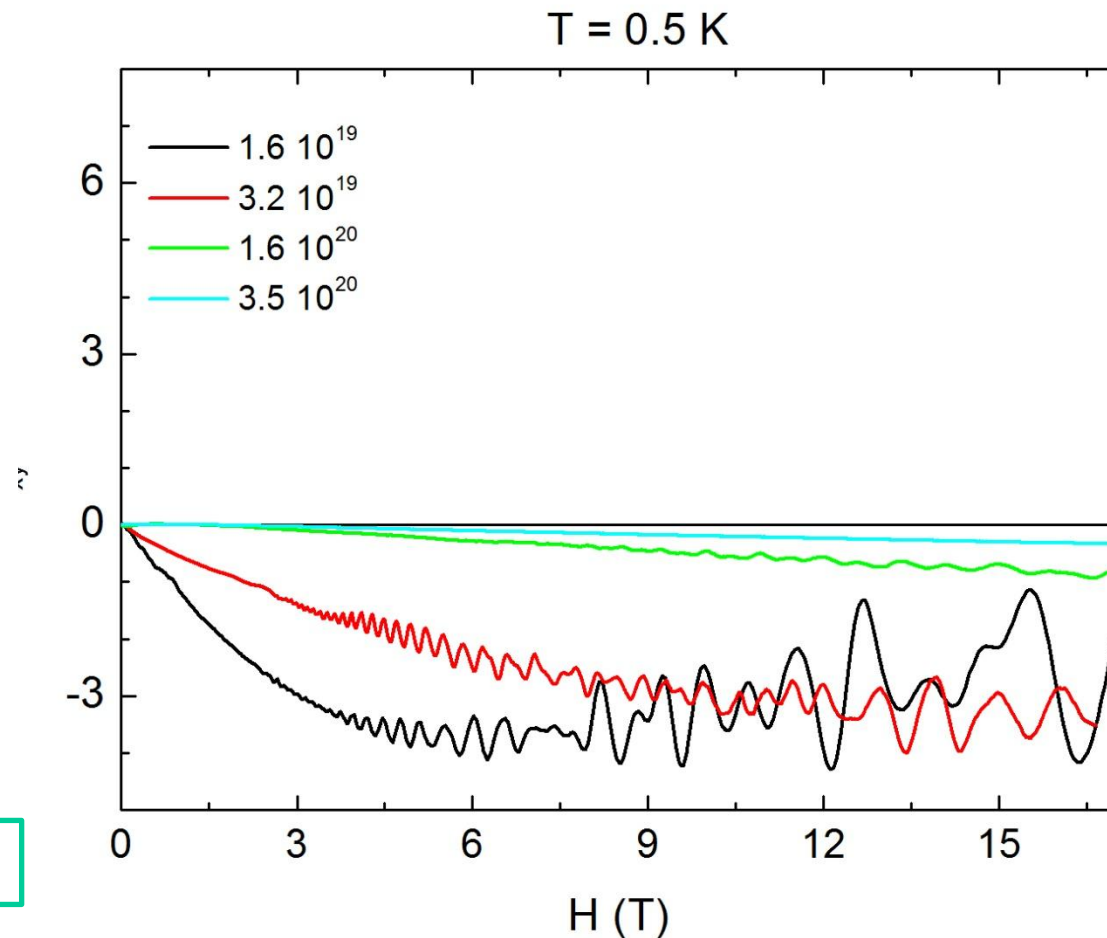
Lin et al., PRX 2013



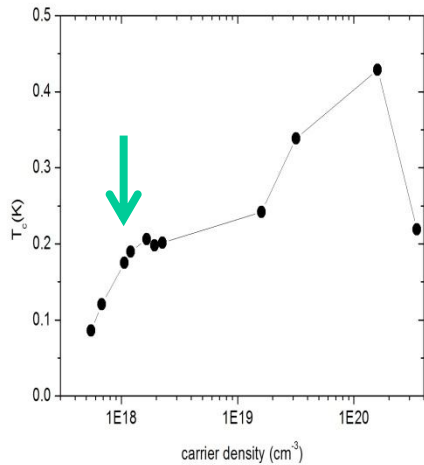
Emergence of Nernst oscillations with underdoping



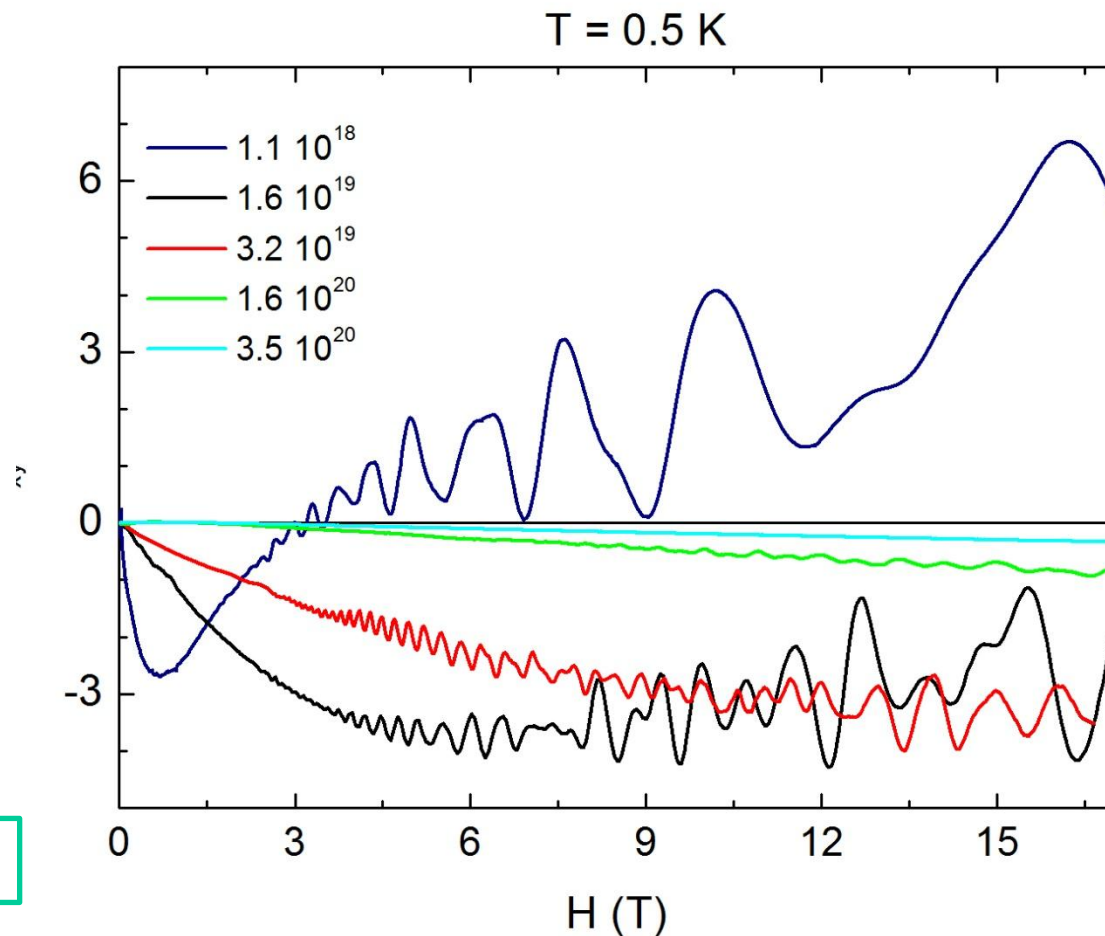
Lin et al., PRX 2013



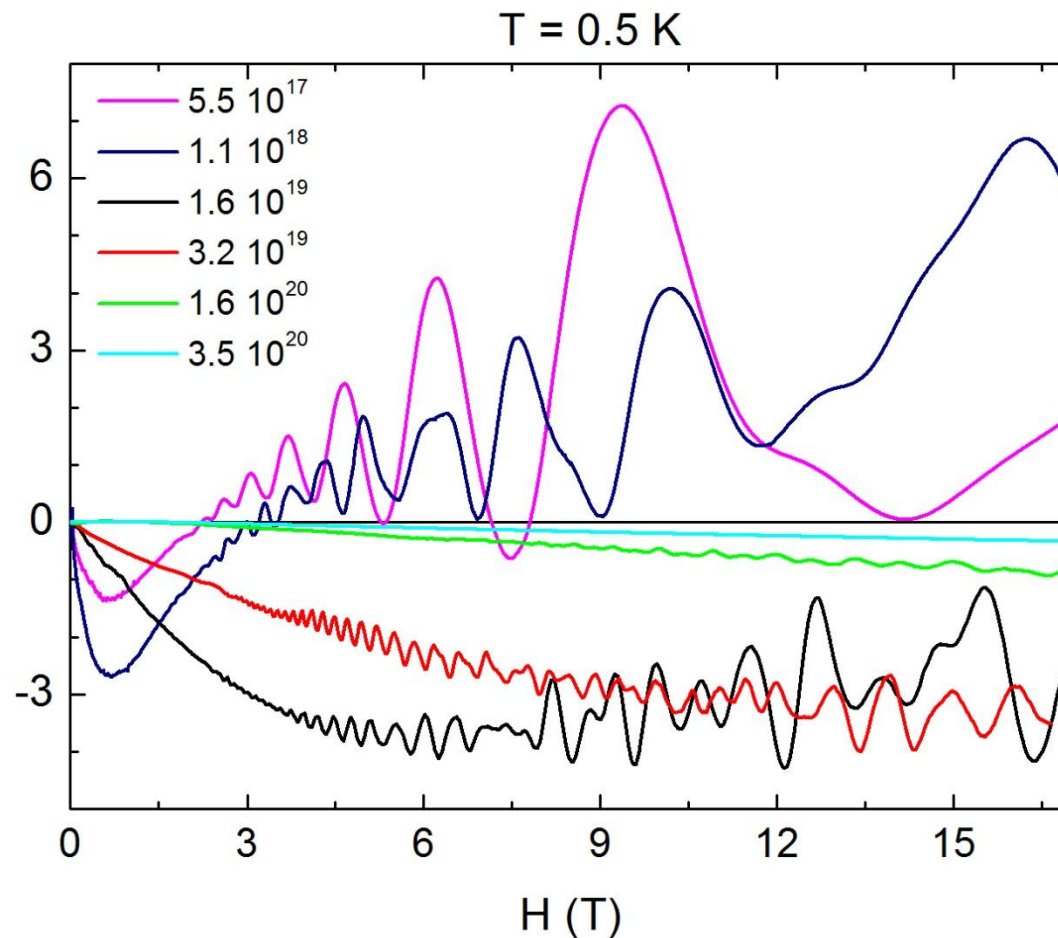
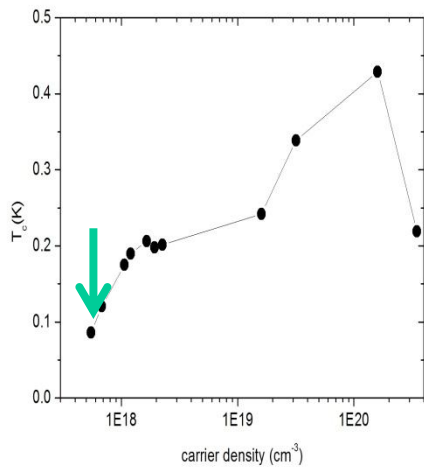
Emergence of Nernst oscillations with underdoping



Lin et al., PRX 2013

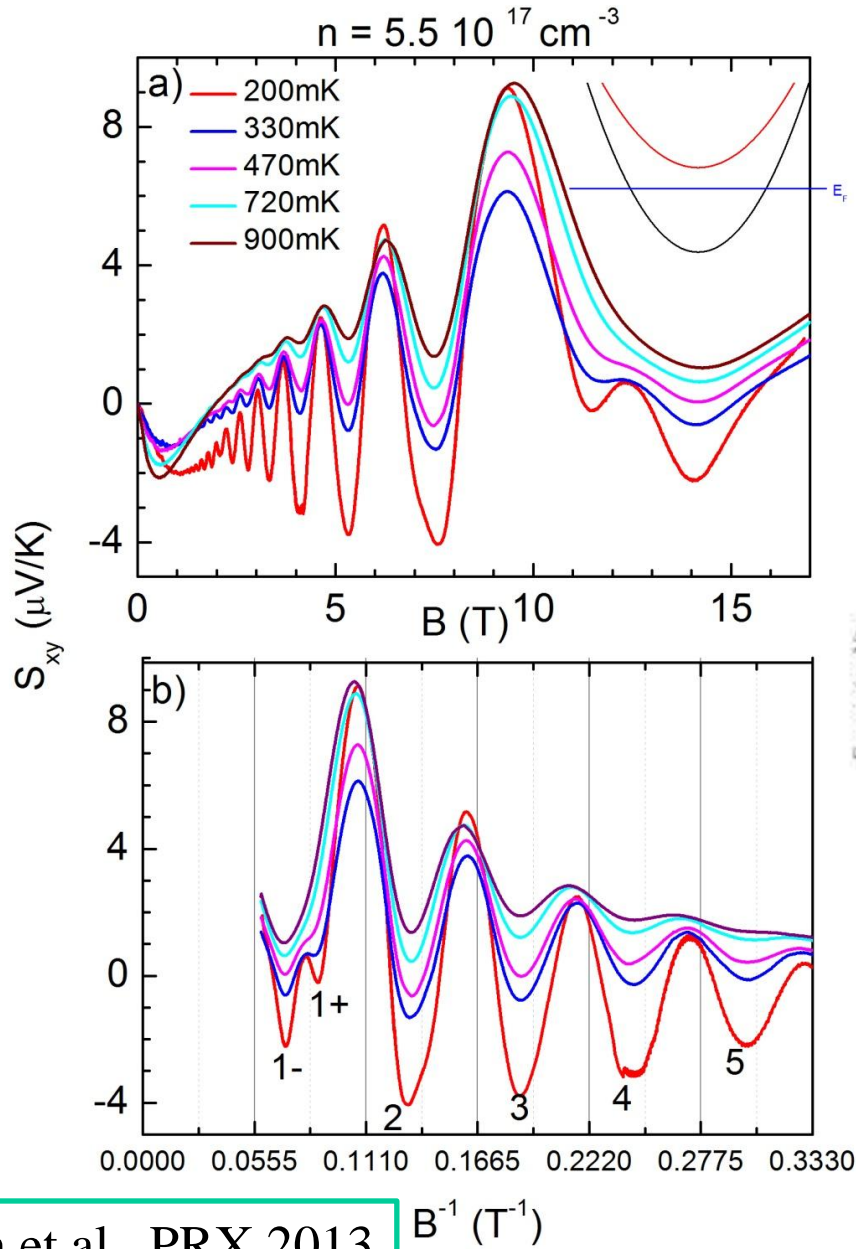


Emergence of Nernst oscillations with underdoping

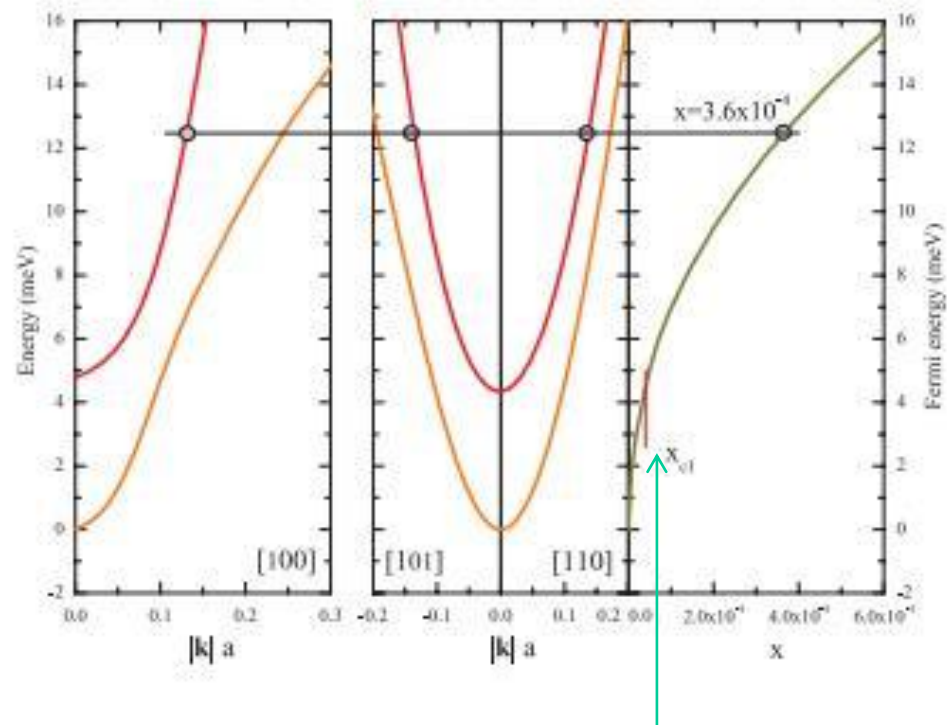


Lin et al., PRX 2013

The lowest concentration has a single frequency

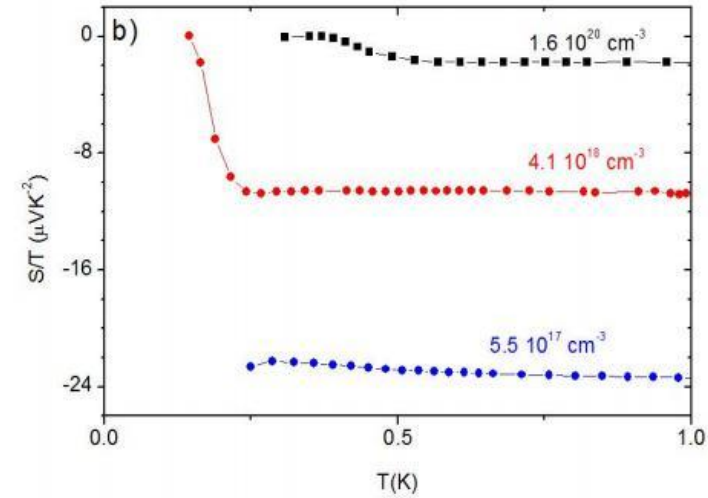
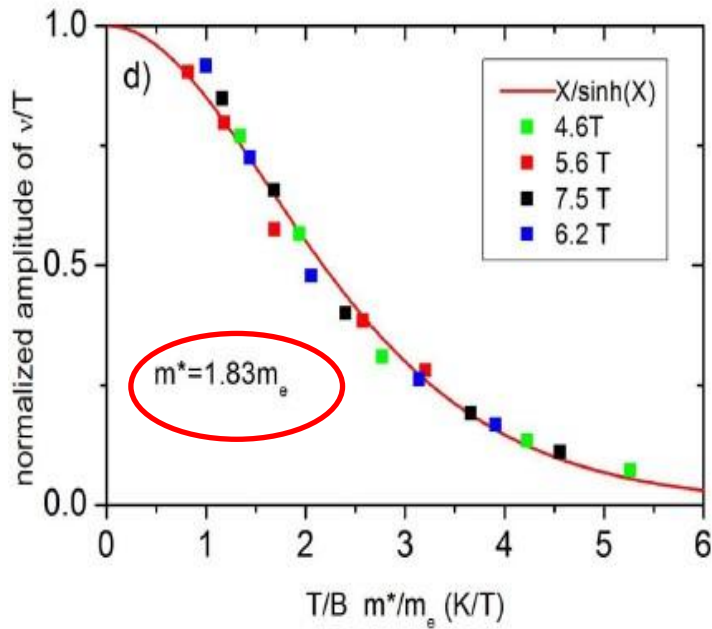


Band calculations:
van der Marel, van Mechelen
and Mazin PRB (2011)



$6.8 \cdot 10^{17} \text{ cm}^{-3}$

Two ways to estimate the Fermi energy

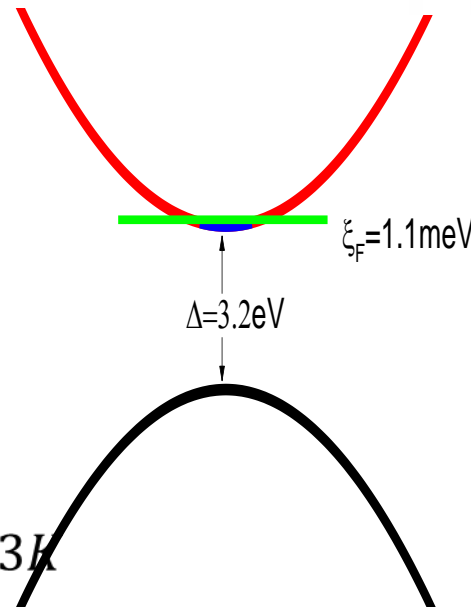


$$m^* = 1.83 m_e$$

$$k_F = 2.35 \times 10^6 \text{ cm}^{-1}$$

$$\varepsilon_F = \frac{(\hbar k_F)^2}{2m^*} = 1.15 \text{ meV}, T_F = 13 \text{ K}$$

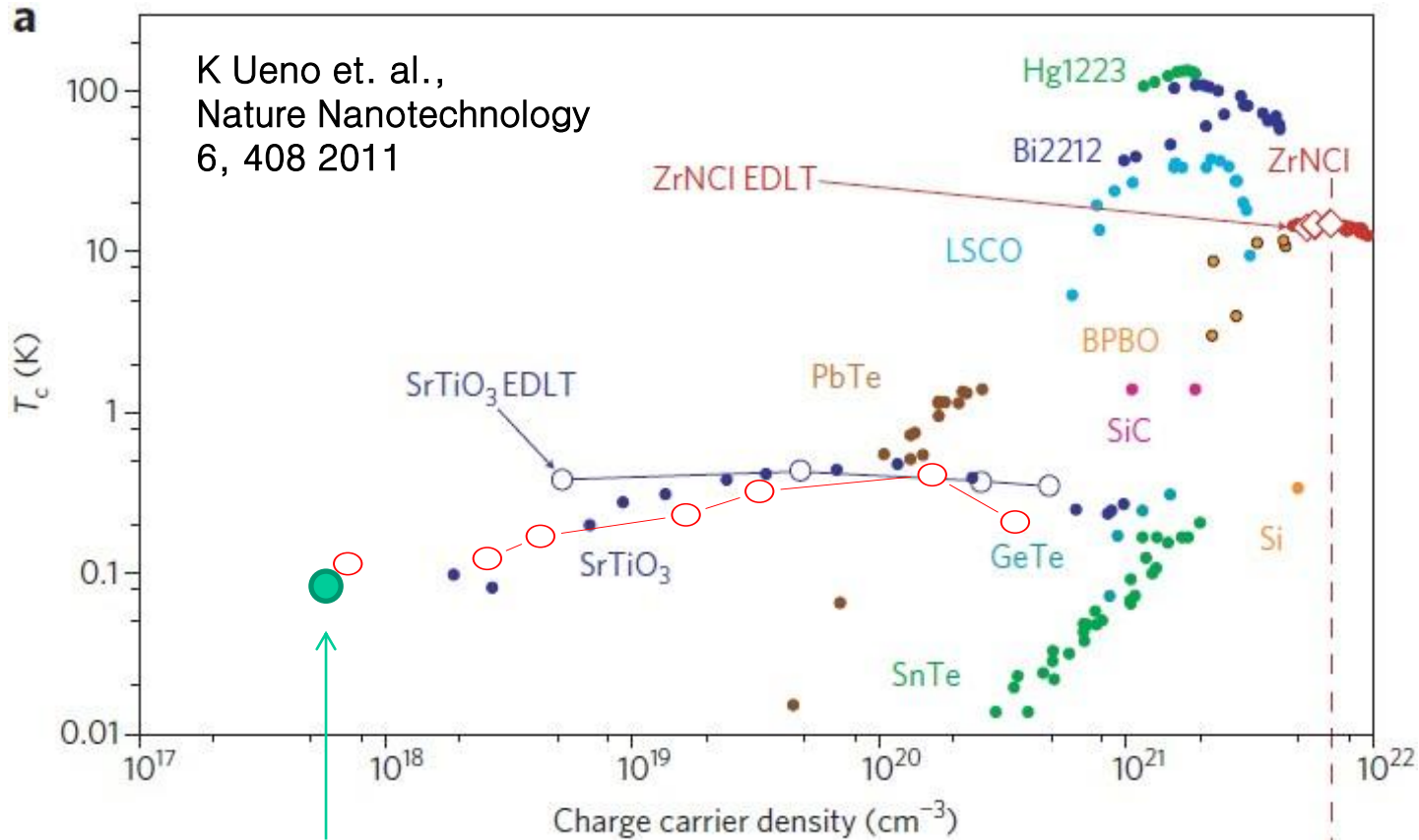
Lin et al., PRX 2013



$$S/T = (\pi^2/3)(k_B/e) 1/T_F$$

$$T_F = 12.9 \text{ K}$$

Dilute superconductors



$5.5 \cdot 10^{17} \text{ cm}^{-3}$

$\text{SrTiO}_{3-\delta}$ [With $\delta \approx 10^{-5}$] is the most dilute superconductor!

SUMMARY

- Thermoelectricity is poorly understood and barely explored in many solids! Often, it opens another window to electronic properties.
- At the boundary between metals and insulators, a large entropy is shared by few carriers with a remarkable thermoelectric response .
- In dilute metals, when few Landau tubes survive, the exit of each of them generates a large Nernst oscillation.
- Many interesting thermoelectric materials are on the metallic side of metal–insulator transition and have a Fermi surface.

Neville Mott on metals and non-metals

Dear Peter
I've thought a lot
about "What is a metal"
+ I think one can only
answer the question at $T=0$.
Then a metal conducts, + a
non-metal doesn't. Yours
Neville



Dear Peter, I've thought a lot about 'What is a metal?' and I think one can only answer the question at $T=0$ [the absolute zero of temperature]. There a metal conducts, and a non-metal doesn't.

(Edwards 1998)

Edwards, Phil. Trans. R. Soc. A **368**, 941–965 (2010)

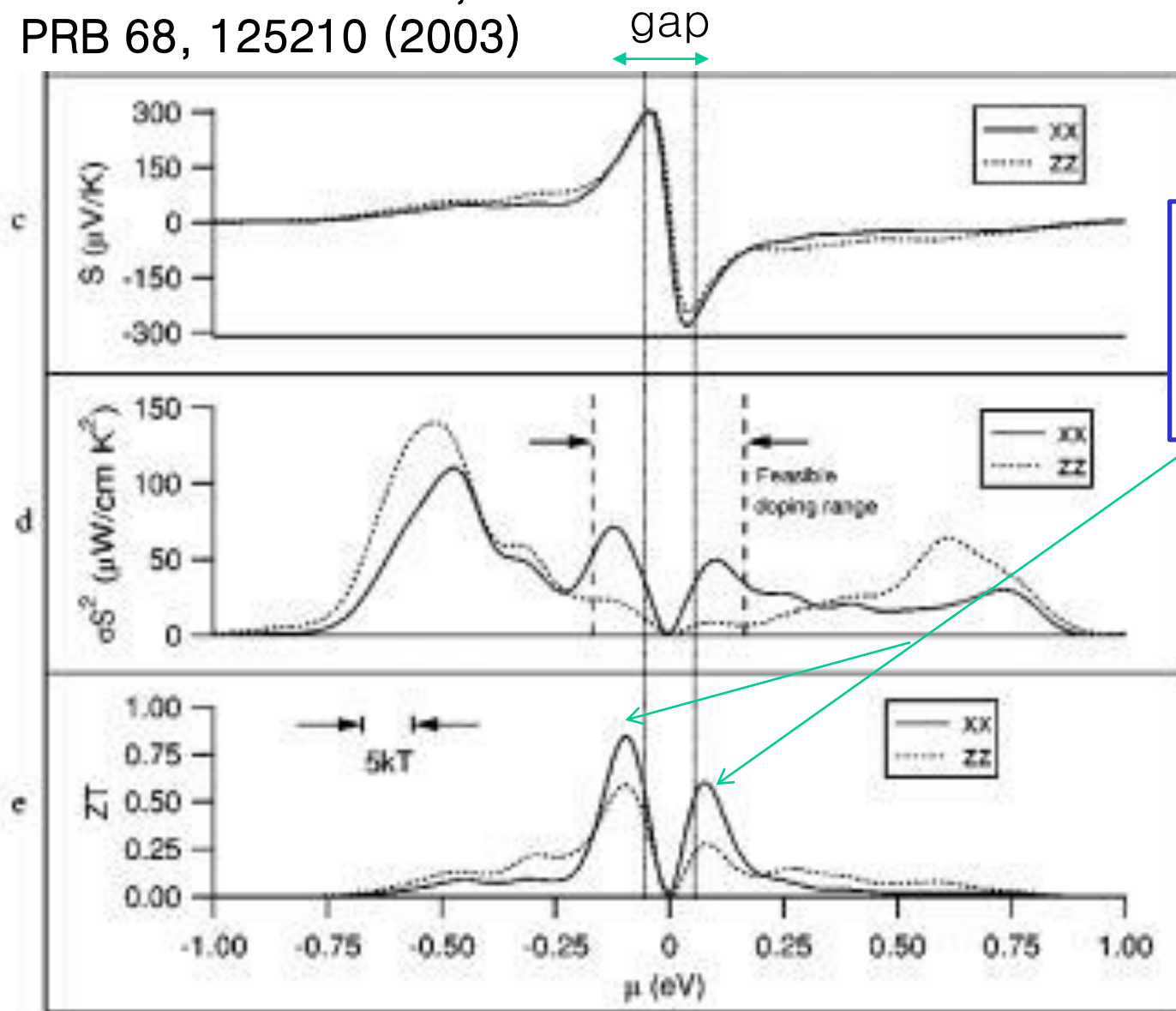
“Everyone knows what a metal is and can describe many of its characteristics. It is safe to say, however, that few people would define a metal as a ‘solid with a Fermi surface’. This may nevertheless be the most meaningful definition of a metal...and provides a precise explanation of the main physical properties ...”

A. R. Mackintosh

Scientific American 1963

First-principle calculations for Bi_2Te_3

Scheidemental et al.,
PRB 68, 125210 (2003)



ZT peaks on the metallic side of the metal-insulator transition!