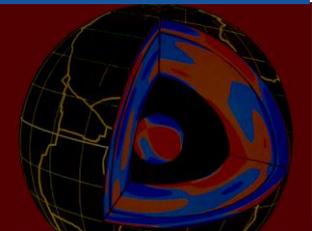


# Seismic anisotropy of the inner core deduced from geodynamical and mineralogical models



Ph. Cardin, ISTerre, Grenoble, France

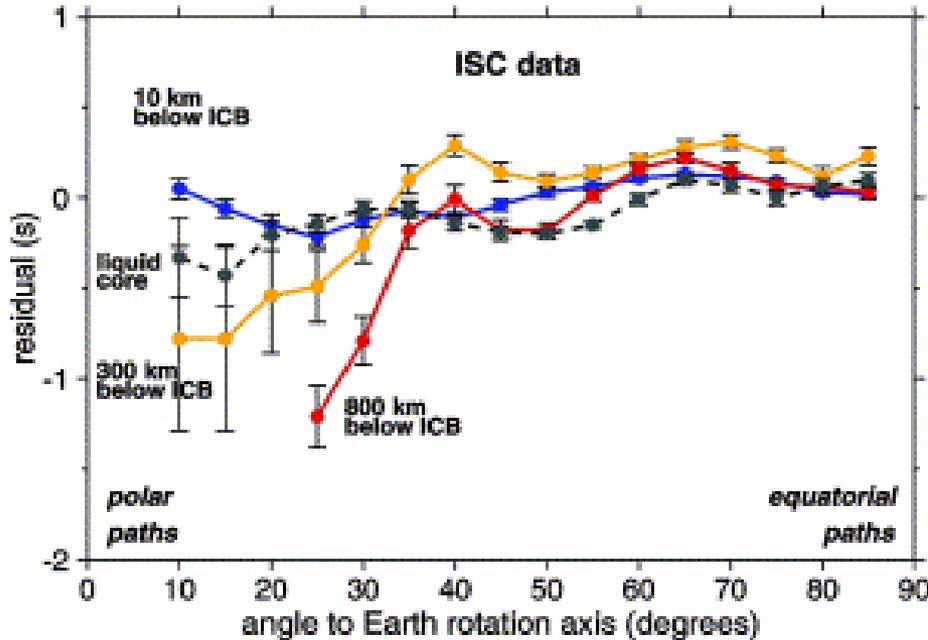
A. Lincot (ISTerre), S. Merkel (UMET-Lille)

R. Deguen (JHU, US), R. Lebenhson (LANL, US)

# Outline

1. Seismological observations, anisotropy
2. Review of proposed mechanism
3. Dynamical state of the inner core
4. Thermal convection in the inner core
5. Stratified inner core and equatorial growth
6. Perspectives

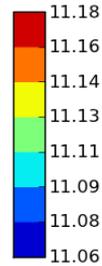
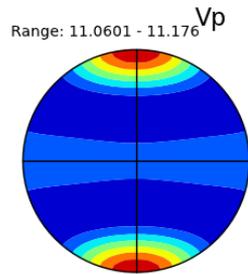
# Seismological evidences?



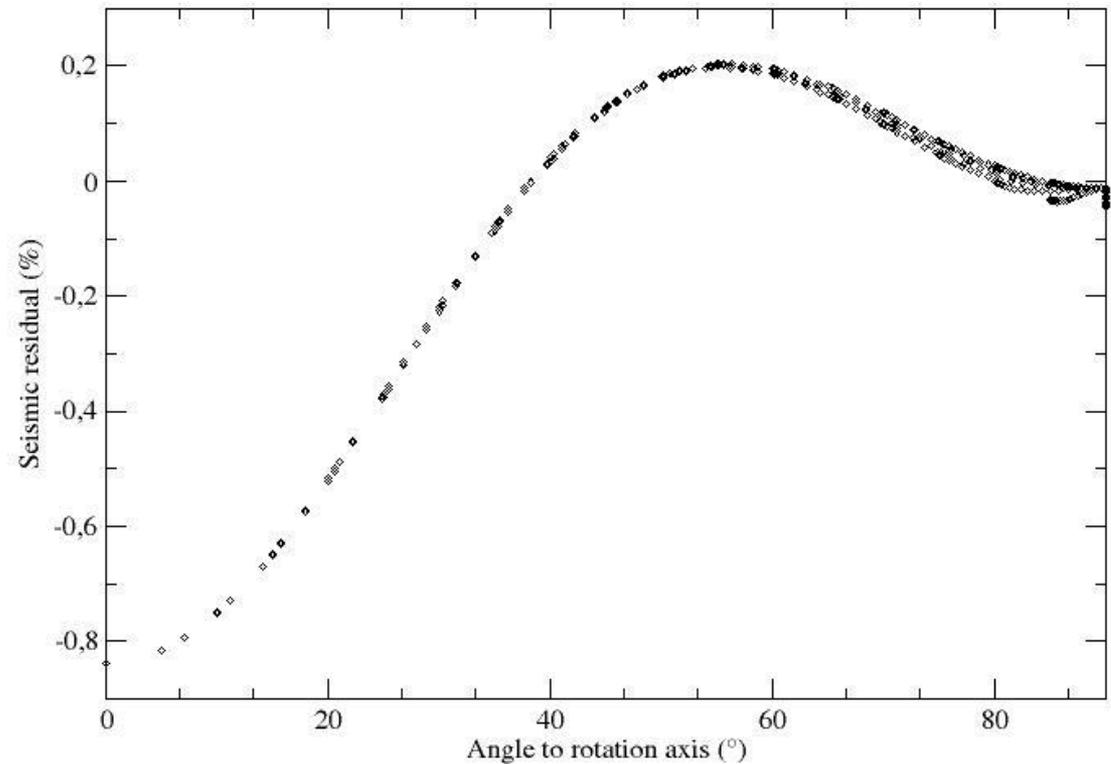
Souriau, Garcia et Poupinet 2003

- 3% central anomaly
- Fast velocity almost NS ( $\sim 10^\circ$ )
- Isotropic superficial layer (100 to 400 km)
- With a hemispheric variation
- And perhaps an innermost innercore

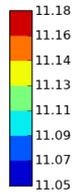
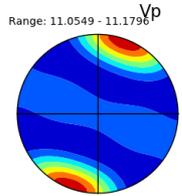
# Direct model of anisotropy



Axisymmetrical inner core

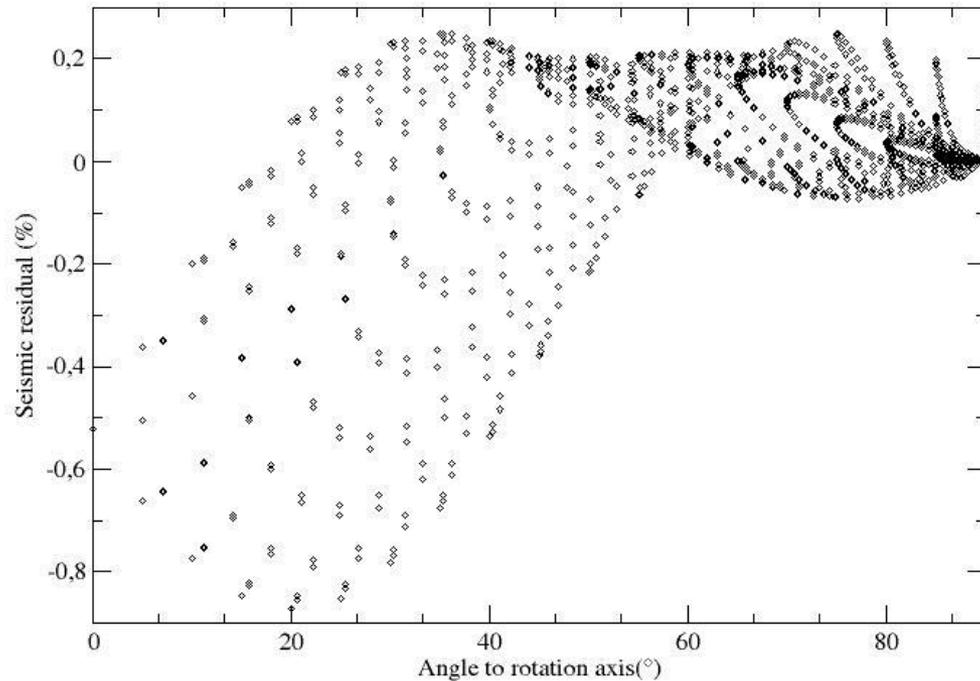


# Model of anisotropy



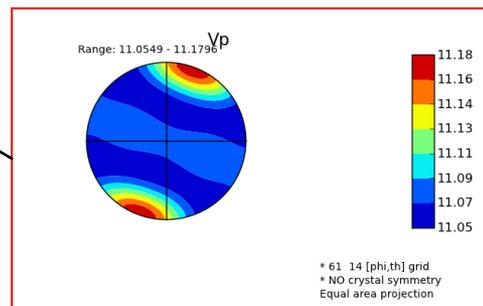
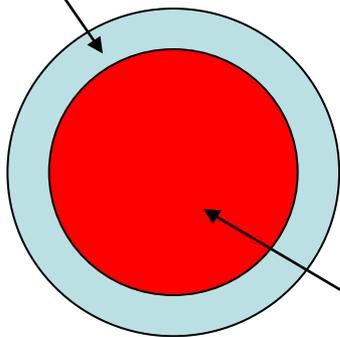
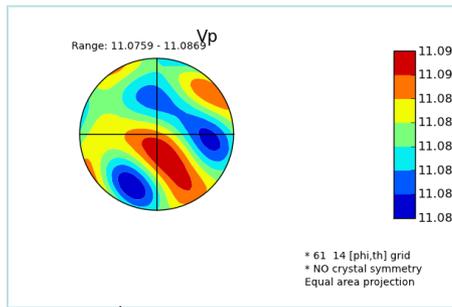
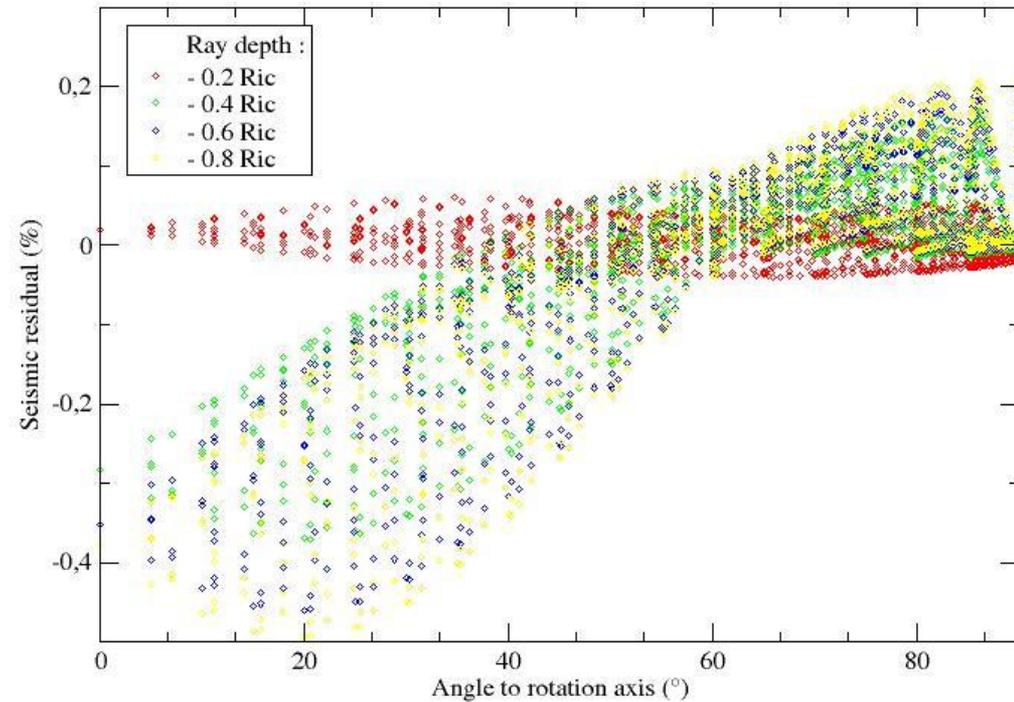
\* 61 14 (phi,th) grid  
\* NO crystal symmetry  
Equal area projection

## Non-axisymmetrical and monocristalline inner core



# Anisotropy for a bilayered inner core

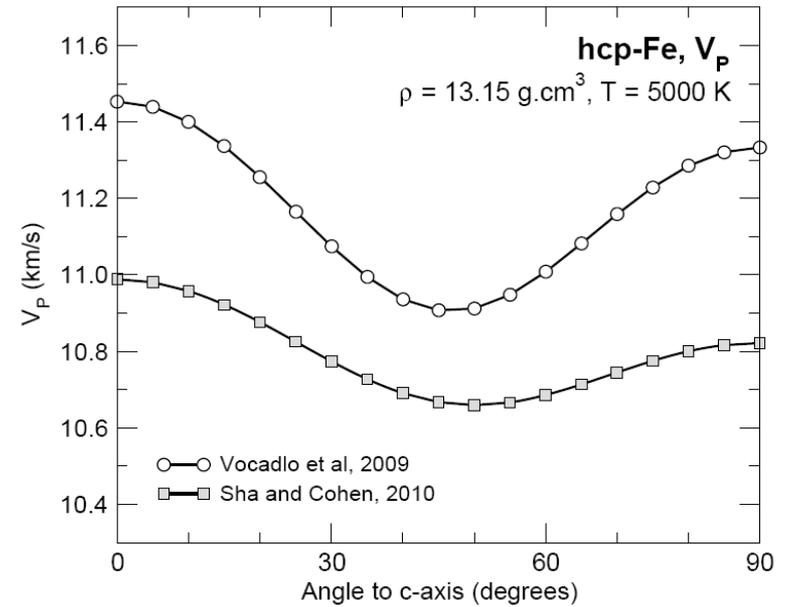
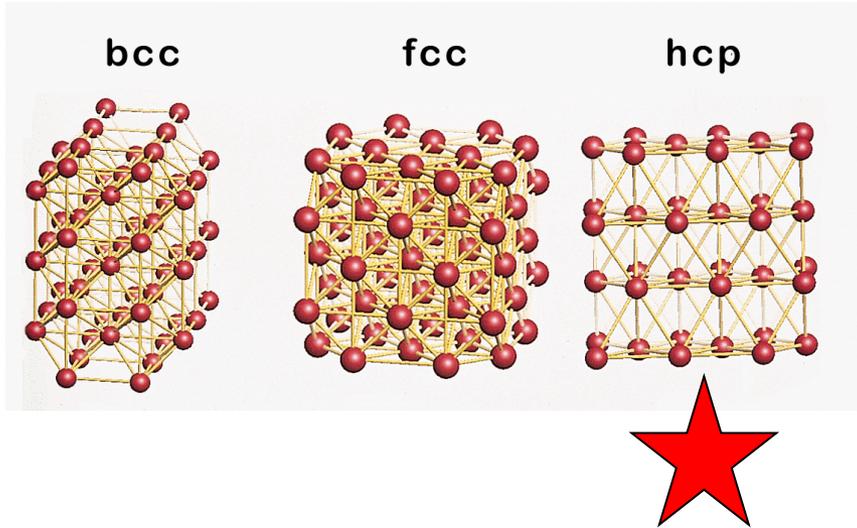
Bilayered and monocristalline inner core



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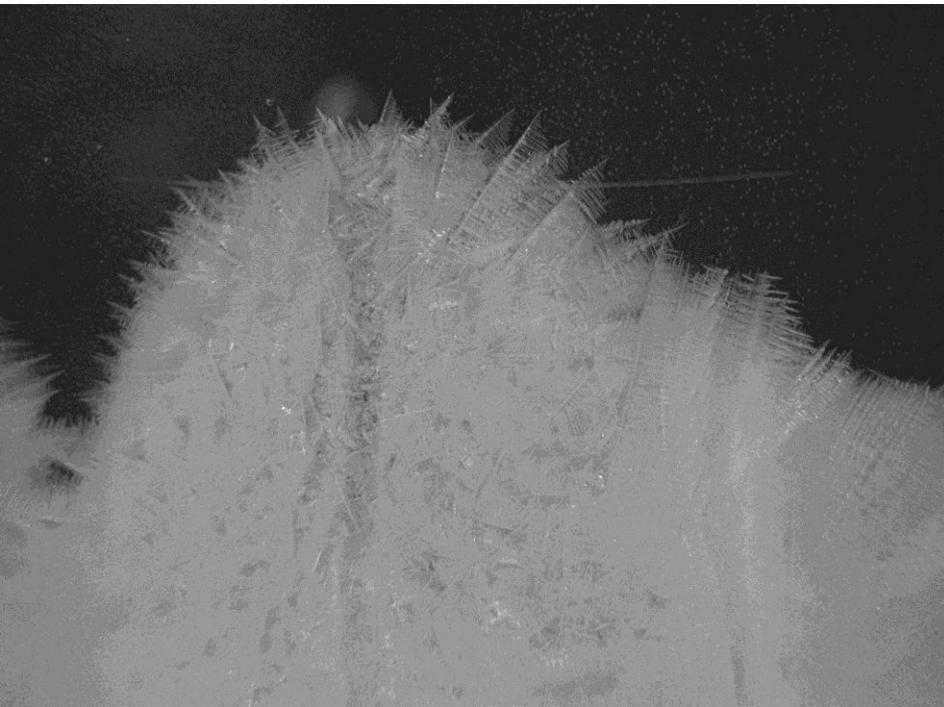
# Anisotropic crystals of iron



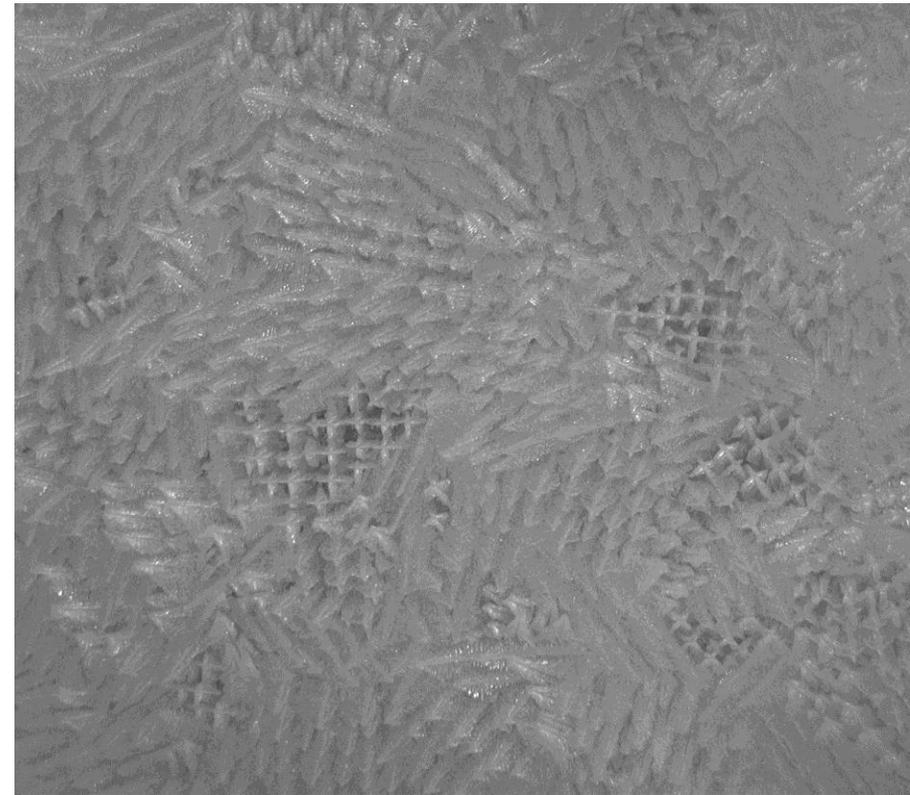
Experimental versus ab initio?

# 1-Texture by cristallisation

Dendrites

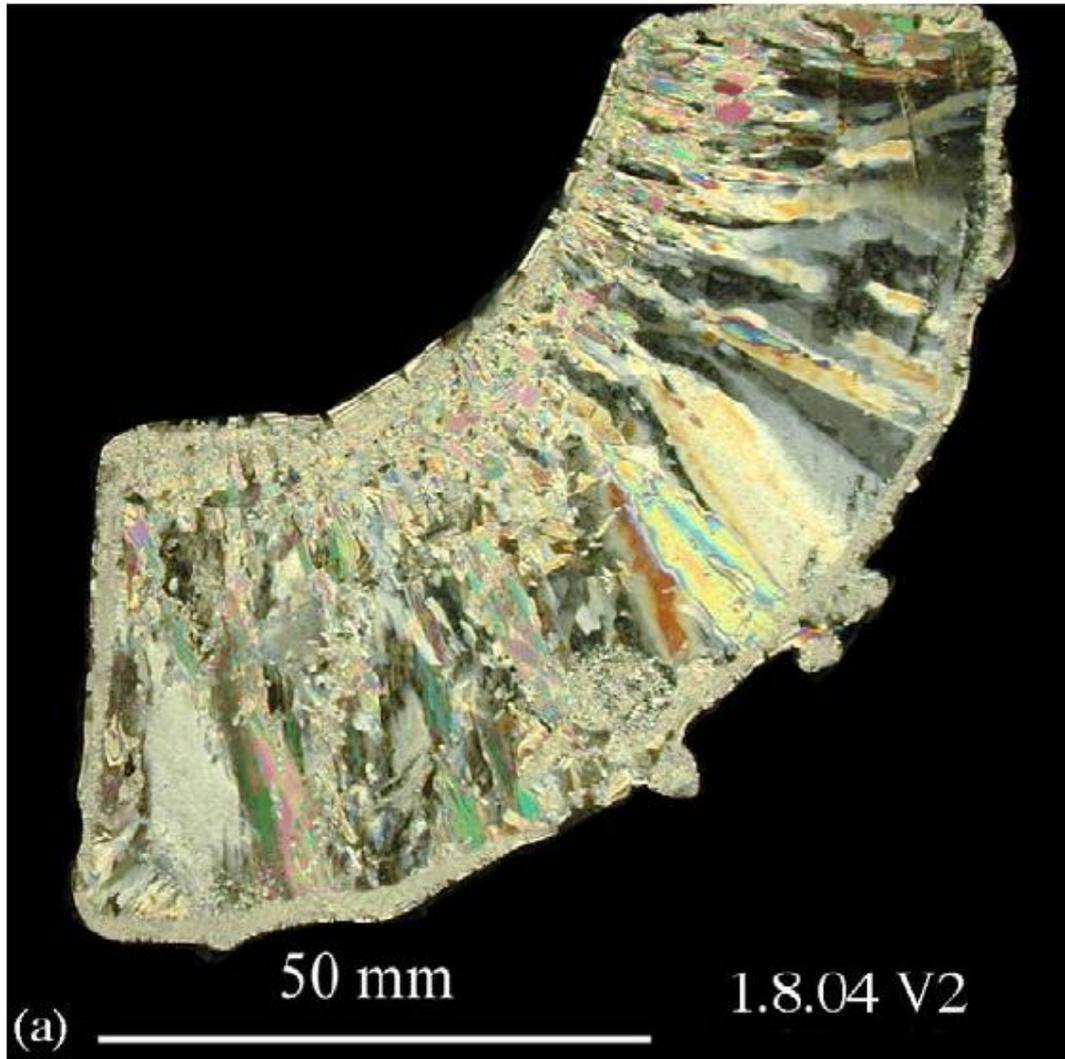


NH<sub>4</sub>Cl experiments



Deguen, 09

# Solidification texturing



Radial symmetry  
of the crystals

Effect of rotation,  
magnetic fields,  
heat flux variations

Bergman et al, 05

Salt water experiments

# 2- Texture by deformation

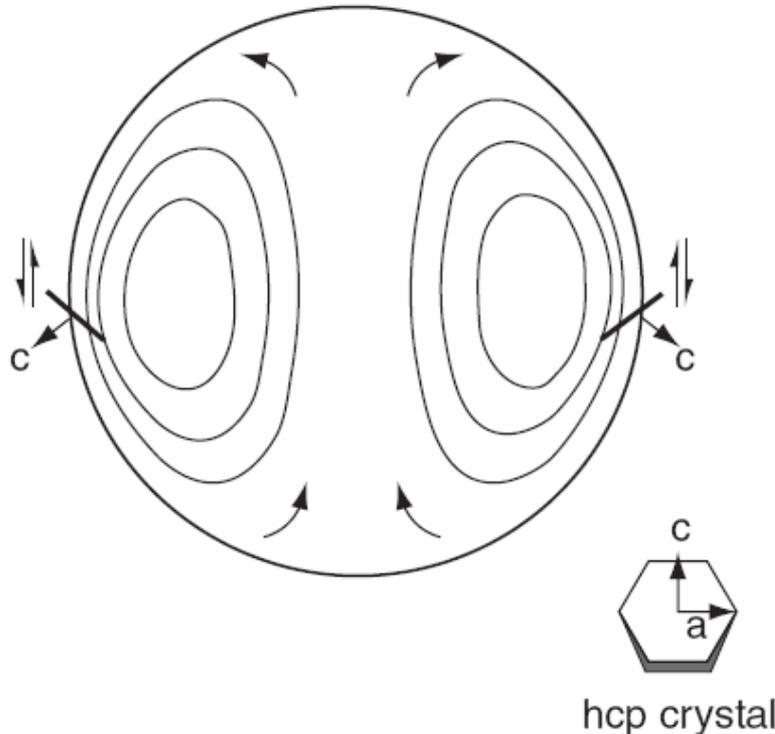
Plastic deformation

Or recrystallisation



# Deformation mechanism (1)

- Thermal convection in the inner core



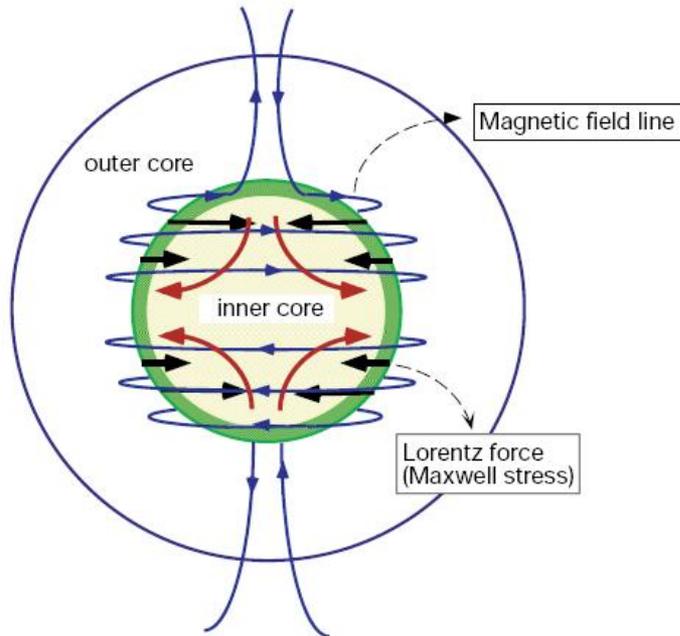
Weber et Machetel, 92

Wenk et al, 2000

# Deformation mechanism (2)

- Maxwell stress

Poloidal motions



Karato, 1999

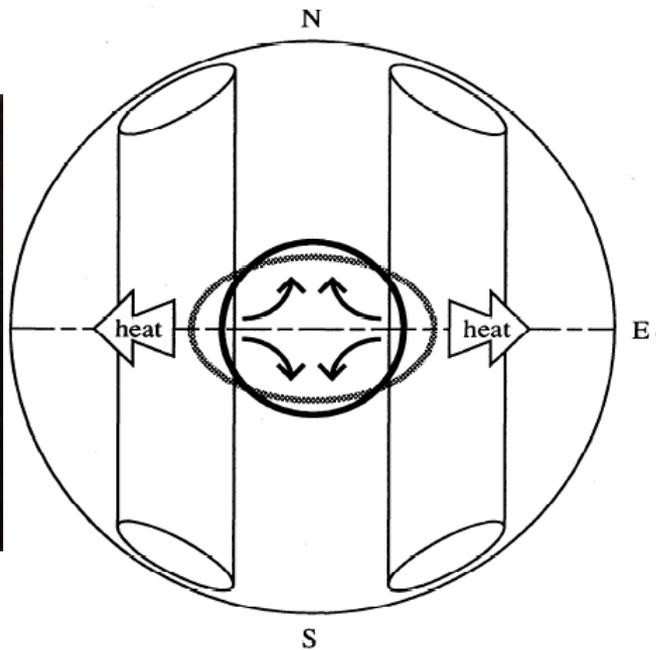
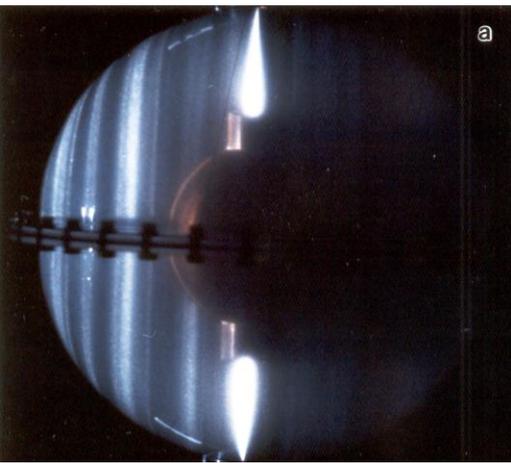
Toroidal motions

Differential motions between the gravitational torque at the ICB and the Lorentz forces in the bulk

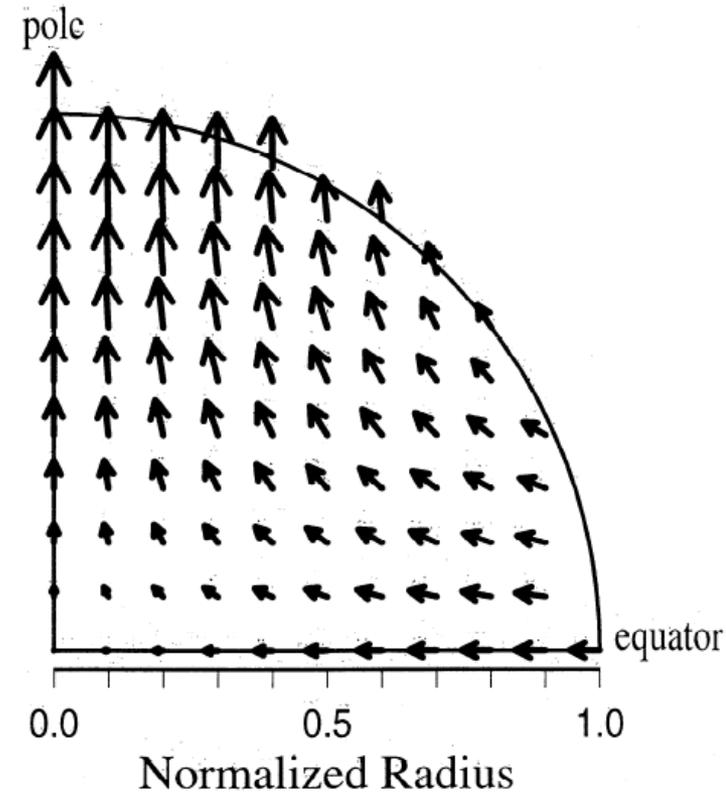
Buffet and Wenk, 2001

# Deformation mechanism (3)

- Differential growth of the inner core



Yoshida et al, 1996



# Review of proposed mechanism

## summary

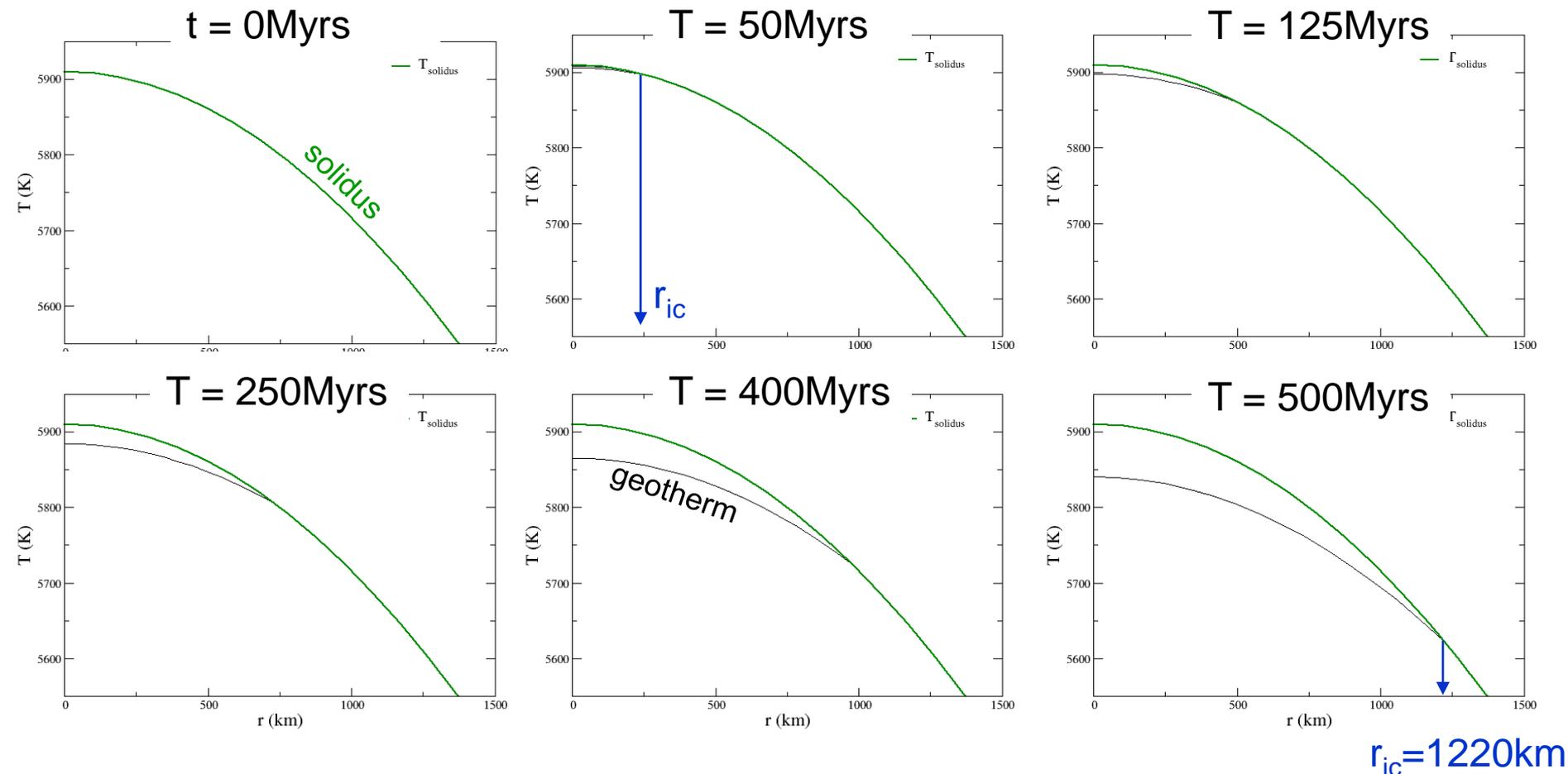
- HCP Fe crystal is anisotropic
- Texture by solidification (spherical)
- Texture by plastic deformation
  - thermal convection
  - Maxwell stress
  - differential growth

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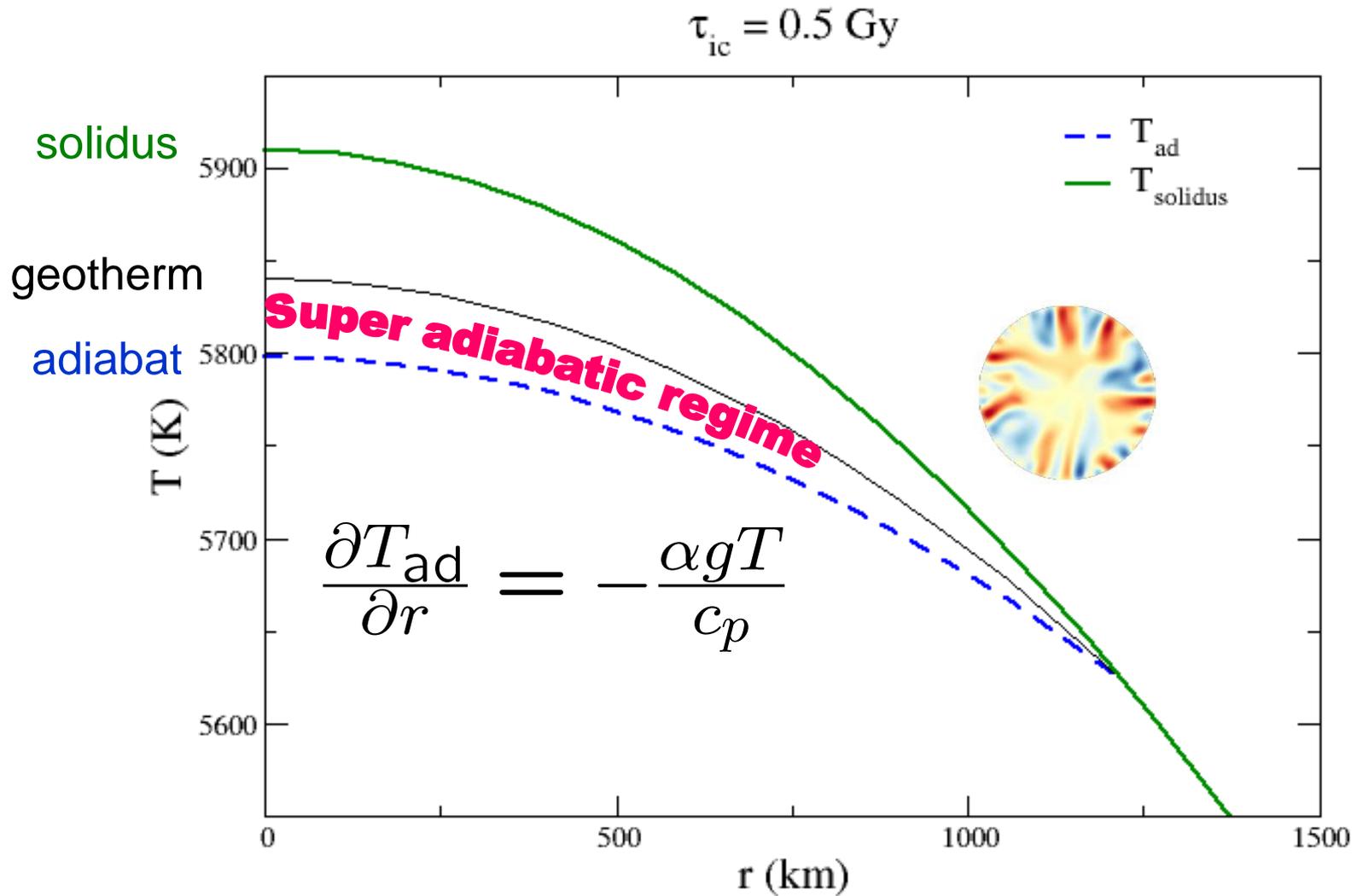
# Time evolution of thermal state of the inner core

- Take an inner core of 500Myrs

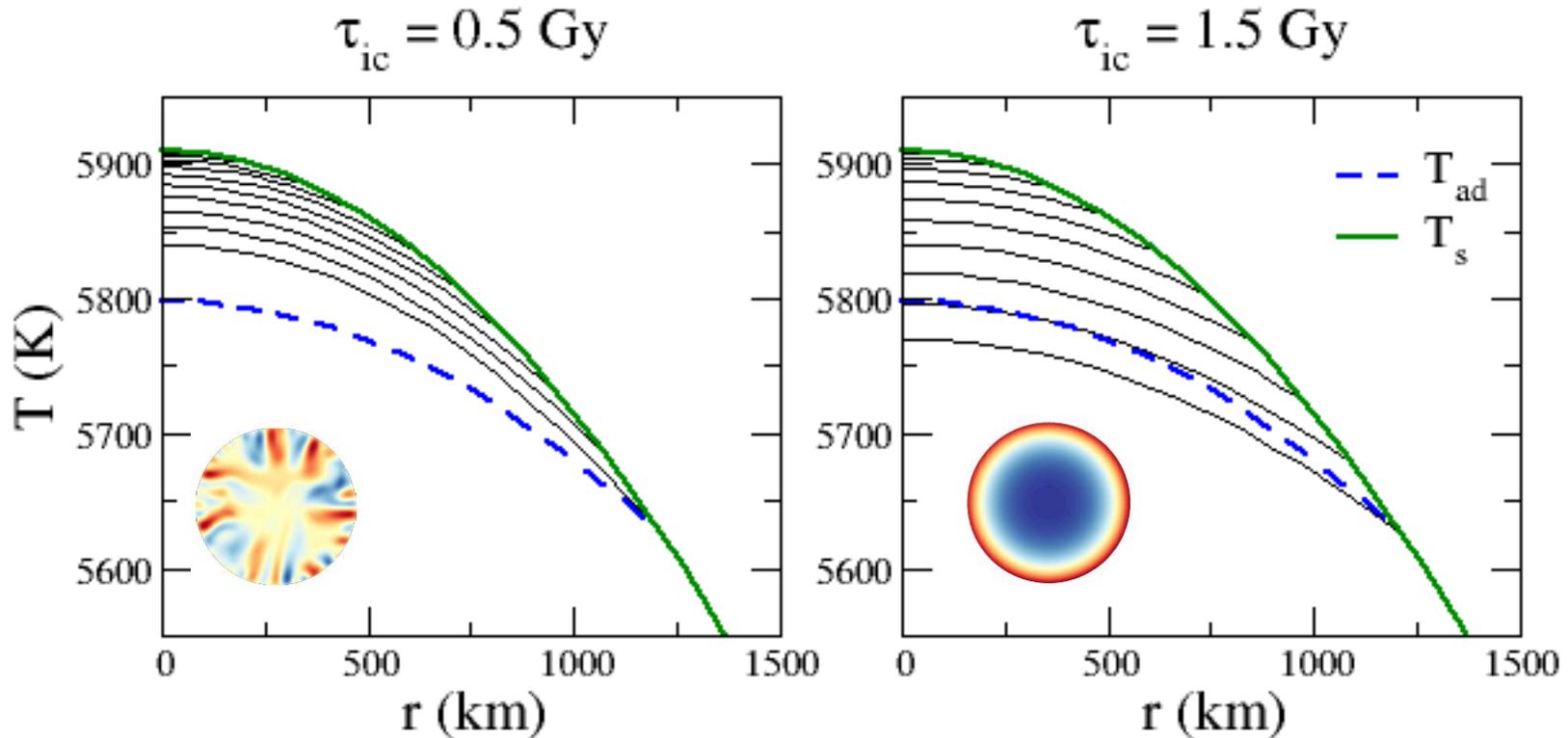


$r_{\text{ic}} = 1220\text{km}$

# Dynamical thermal state ?



# Inner core age



Inner core cooling (age) is the key parameter to predict the dynamical state.

CMB heat flux

Thermal conductivity

# Dynamical state of the inner core

- Age of IC is the key parameter:

$$\tau_{ic} < \tau_{\kappa} \left( \frac{dT_S}{dT_{ad}} - 1 \right) = \frac{r_{ic}^2}{3\kappa} \left( 1 - \frac{1}{3\gamma} \right) \left( \frac{1}{\gamma} + \alpha T \right)$$

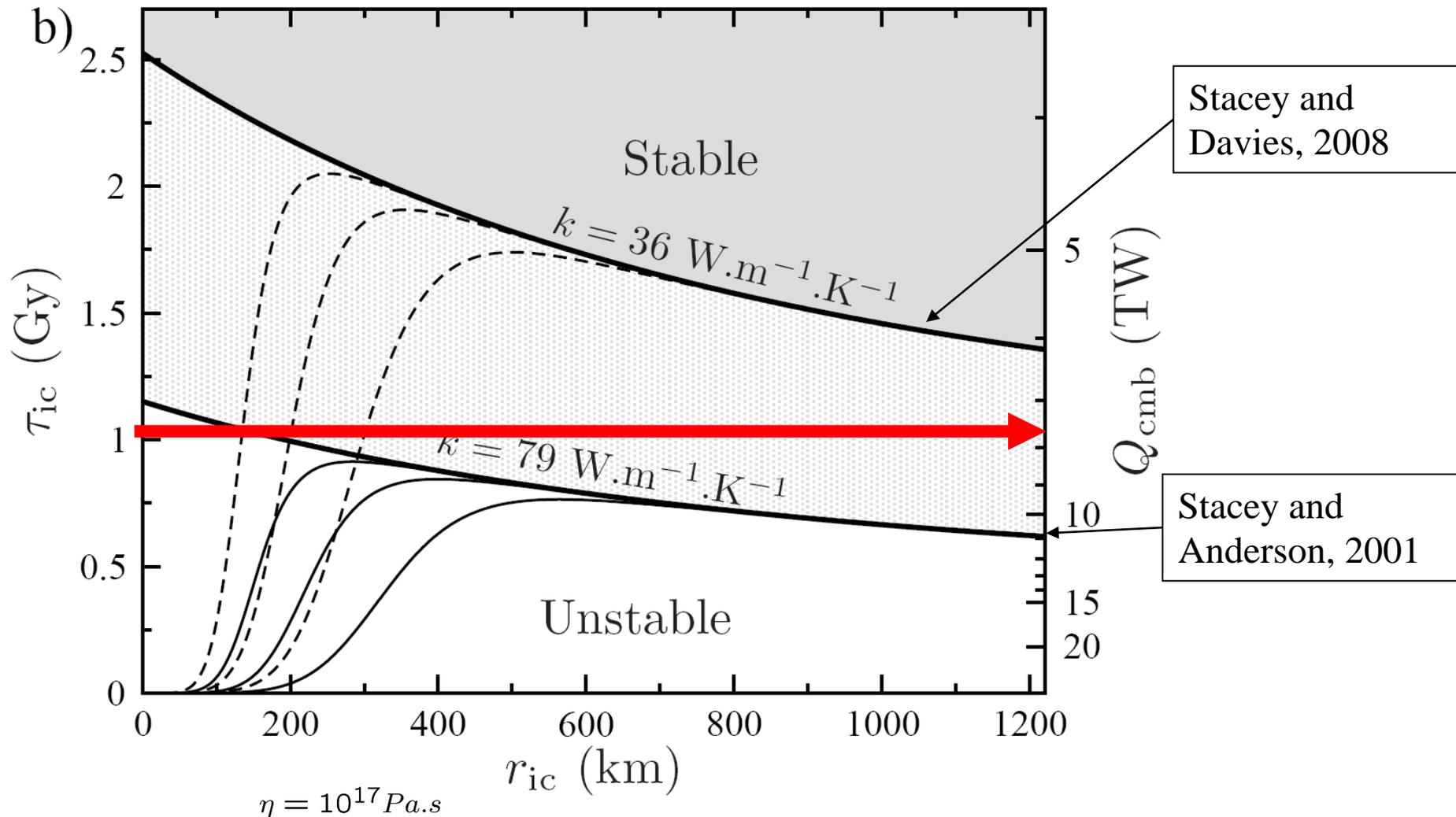
$$\tau_{ic}^{crit} = 0.9 \pm 0.6 Gy$$

- Controlled mainly by the CMB heat flux

$$\tau_{ic} = \frac{E_{tot}}{Q_{cmb}} = \frac{\int_0^{r_{ic}} P_c + P_g + P_L dr}{Q_{cmb}} = \frac{29 \pm 18 \cdot 10^{28} J}{Q_{cmb}}$$

$$\tau_{ic} = 0.6 Gy(12 TW) - 2.3 Gy(4 TW)$$

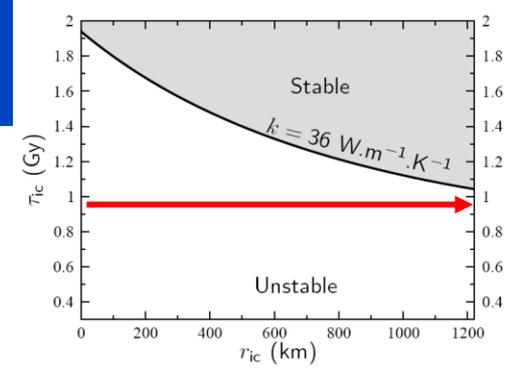
# Adiabatic state of the inner core



# Outline

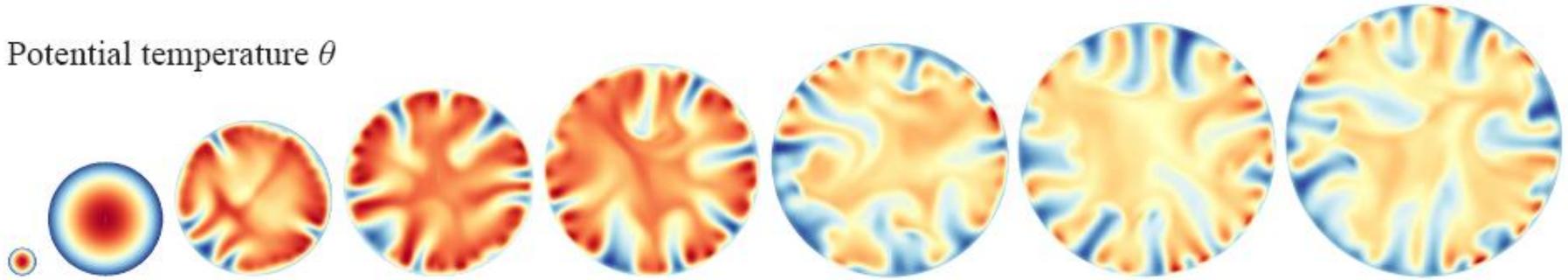
1. Seismological observations, anisotropy
2. Review of proposed mechanism
3. Dynamical state of the inner core
4. **Thermal convection in the inner core**
5. Stratified inner core and equatorial growth
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# Thermal convection

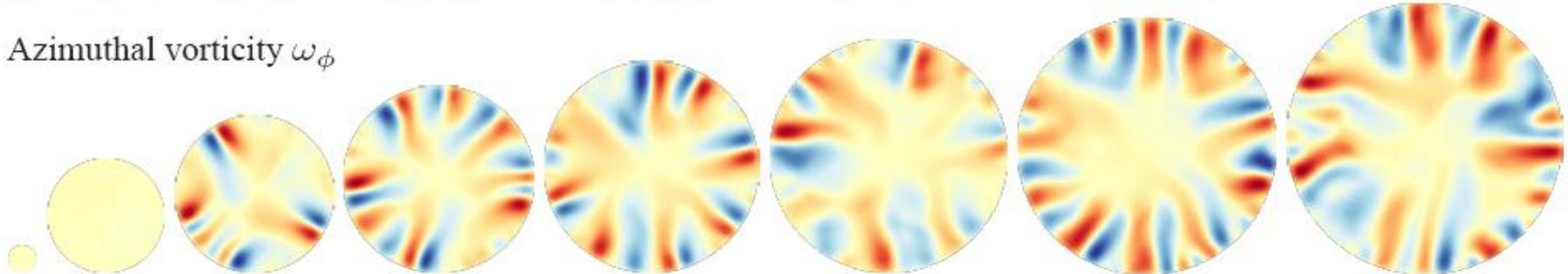


a.  $\tau_{ic} = 0.9 \text{ Gy}$ ,  $\eta = 10^{18} \text{ Pa.s}$ ,  $k = 36 \text{ W.m}^{-1}.\text{K}^{-1}$ .

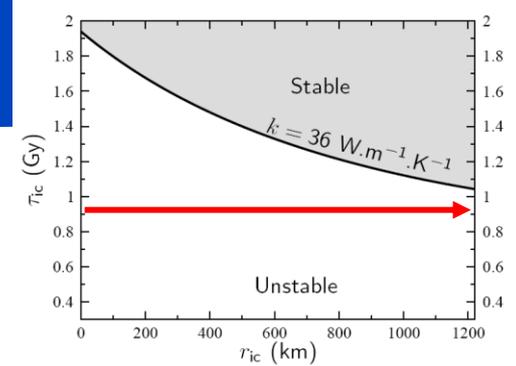
Potential temperature  $\theta$



Azimuthal vorticity  $\omega_\phi$

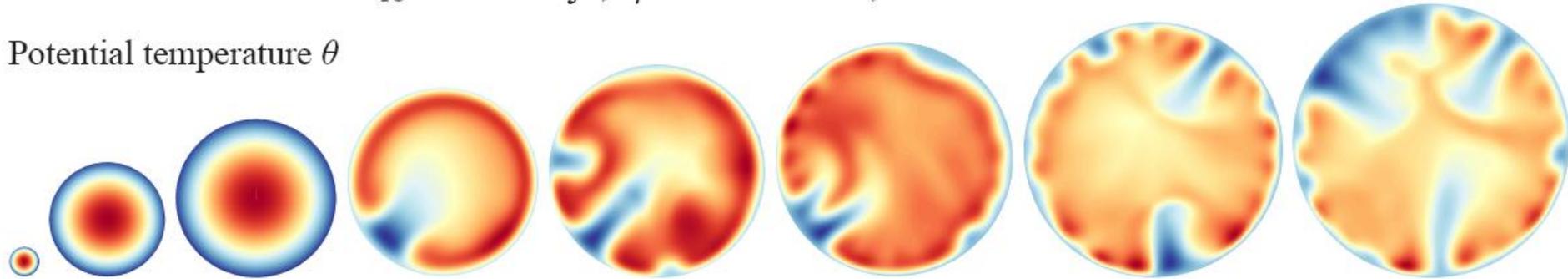


# Thermal convection

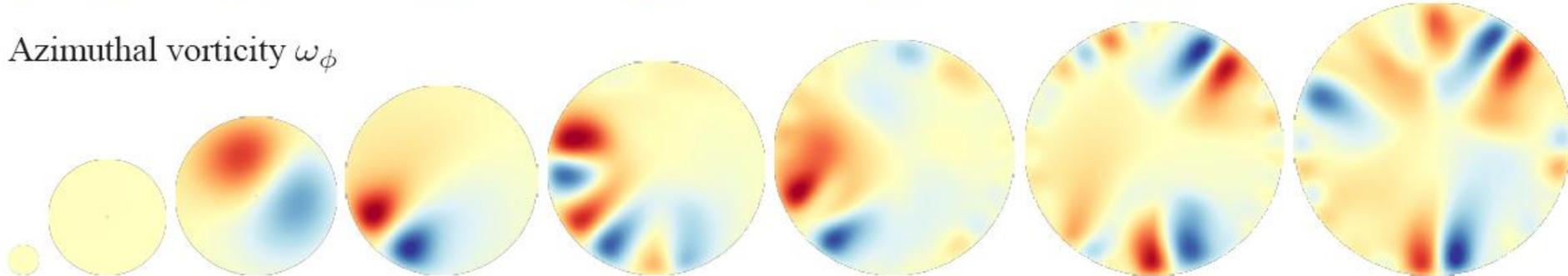


**b.**  $\tau_{ic} = 0.9 \text{ Gy}$ ,  $\eta = 10^{19} \text{ Pa.s}$ ,  $k = 36 \text{ W.m}^{-1}.\text{K}^{-1}$ .

Potential temperature  $\theta$



Azimuthal vorticity  $\omega_\phi$



# Scaling laws

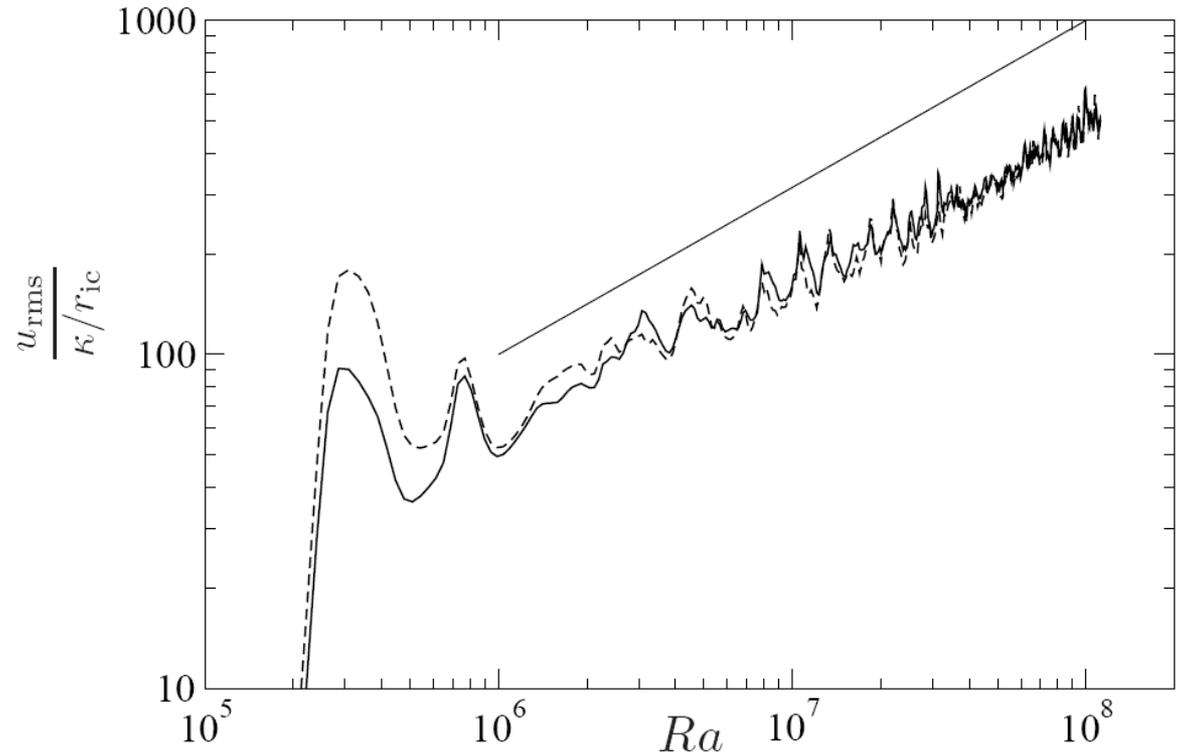
$$u_{rms} \approx 0.04 \frac{\kappa}{r_{ic}} Ra^{0.51}$$

$$u_{rms} \propto Ra^{1/2}$$

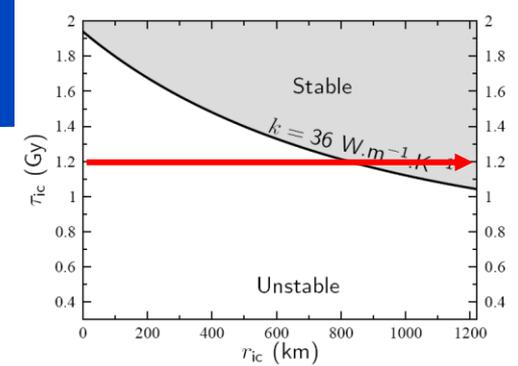
Parmentier and Sotin, 2000

$$\delta\theta \approx 1.4 \frac{Sr_{ic}}{6\kappa} Ra^{0.27}$$

$$\delta\theta \approx 1K$$

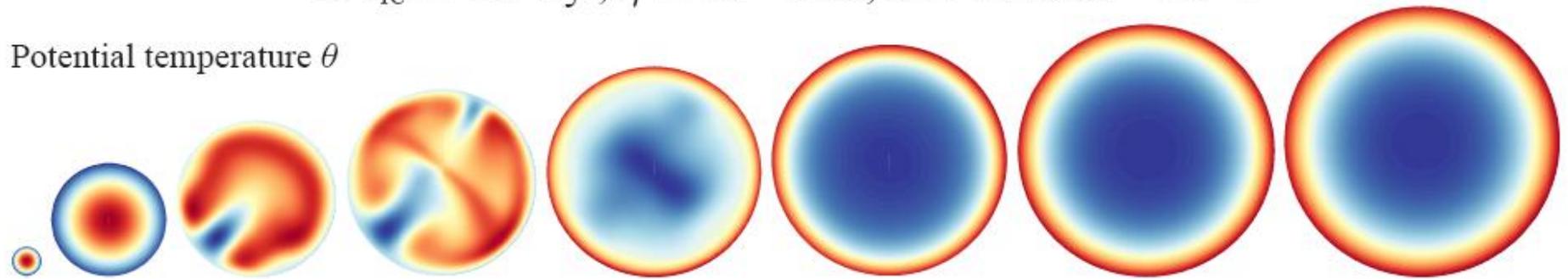


# A convective window

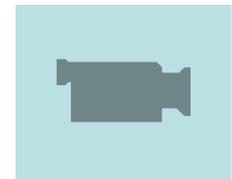
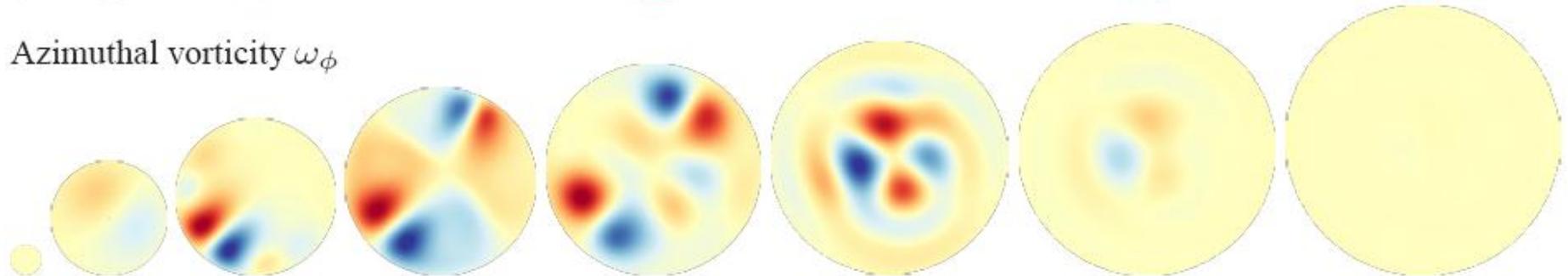


**b.**  $\tau_{ic} = 1.2 \text{ Gy}$ ,  $\eta = 10^{18} \text{ Pa.s}$ ,  $k = 36 \text{ W.m}^{-1}.\text{K}^{-1}$ .

Potential temperature  $\theta$

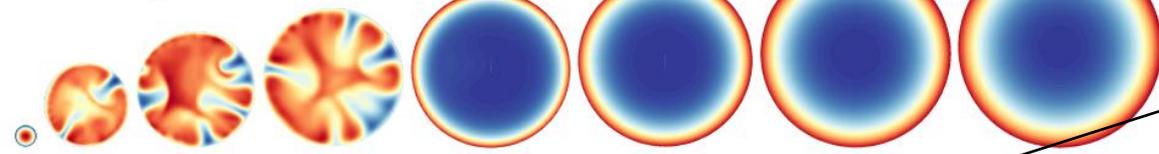


Azimuthal vorticity  $\omega_\phi$

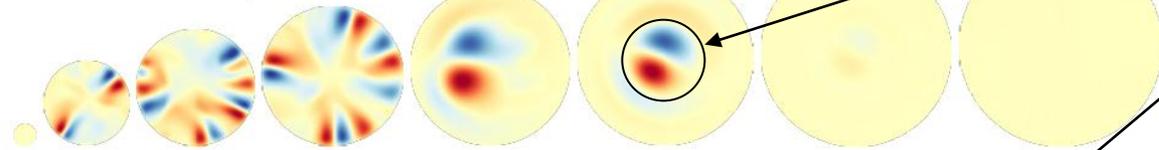


**a.**  $\tau_{ic} = 1.2 \text{ Gy}$ ,  $\eta = 10^{17} \text{ Pa.s}$ ,  $k = 36 \text{ W.m}^{-1}.\text{K}^{-1}$ .

Potential temperature  $\theta$

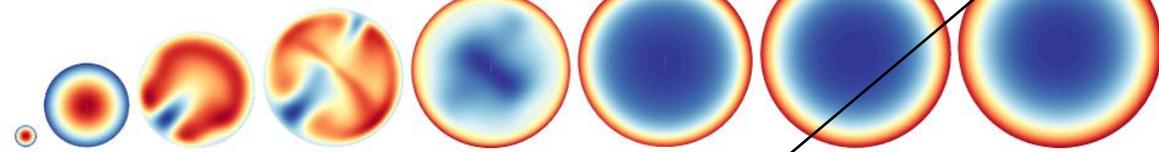


Azimuthal vorticity  $\omega_\phi$

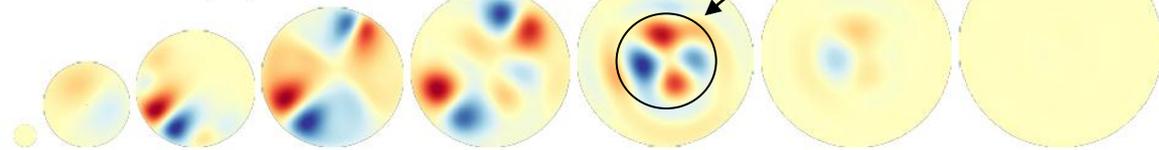


**b.**  $\tau_{ic} = 1.2 \text{ Gy}$ ,  $\eta = 10^{18} \text{ Pa.s}$ ,  $k = 36 \text{ W.m}^{-1}.\text{K}^{-1}$ .

Potential temperature  $\theta$

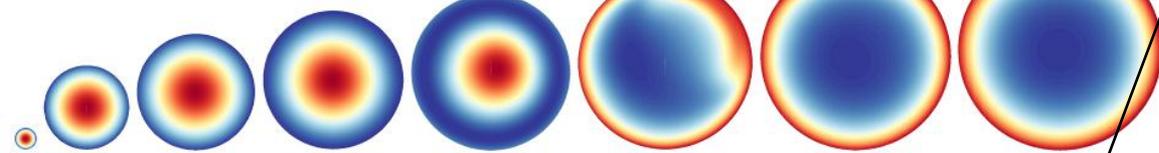


Azimuthal vorticity  $\omega_\phi$

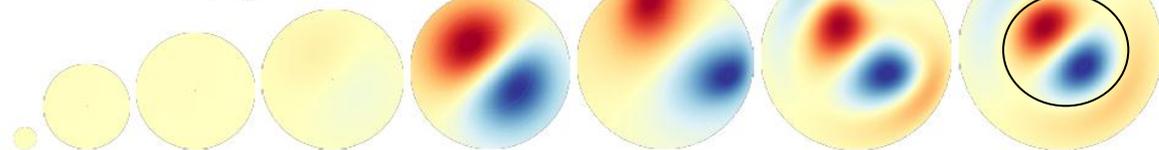


**c.**  $\tau_{ic} = 1.2 \text{ Gy}$ ,  $\eta = 10^{19} \text{ Pa.s}$ ,  $k = 36 \text{ W.m}^{-1}.\text{K}^{-1}$ .

Potential temperature  $\theta$



Azimuthal vorticity  $\omega_\phi$

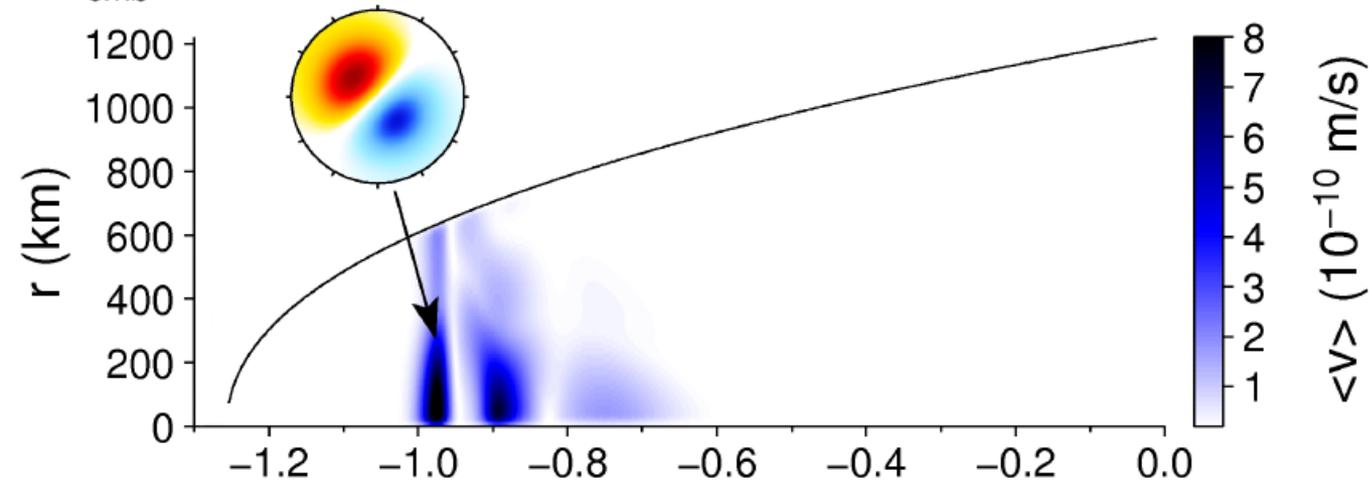


Innermost  
Inner Core ?

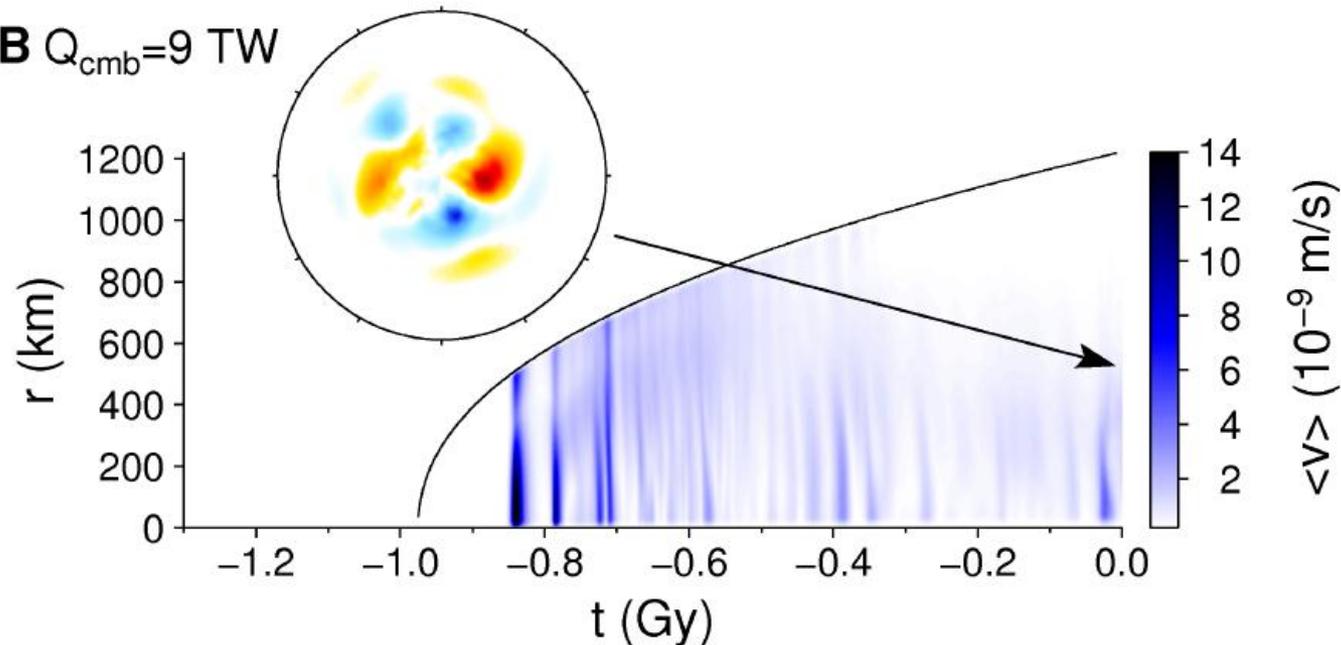
Higher viscosity

# IIC: a thermal signature?

**A**  $Q_{\text{cmb}}=7$  TW

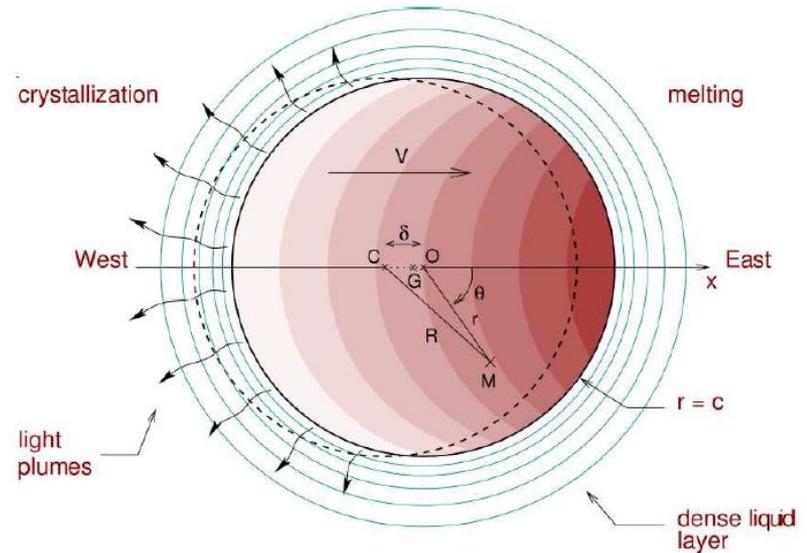


**B**  $Q_{\text{cmb}}=9$  TW



# Translation of the inner core

- A rigid inner core
- EW perturbation of T, change the density field and the center of mass.
- **Allow quick fusion and solidification.**
- Misfit between center of mass and “center” of T.
- Archimedean force translate the inner core.



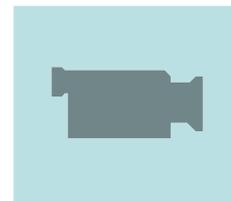
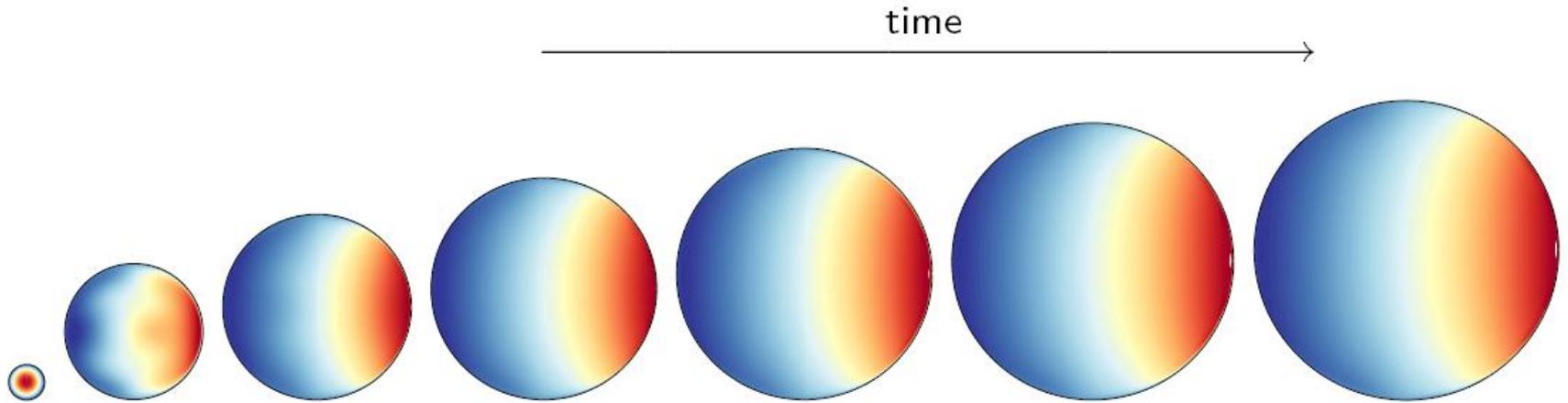
Alboussière et al, 2010

Monnereau et al, 2010

# translation

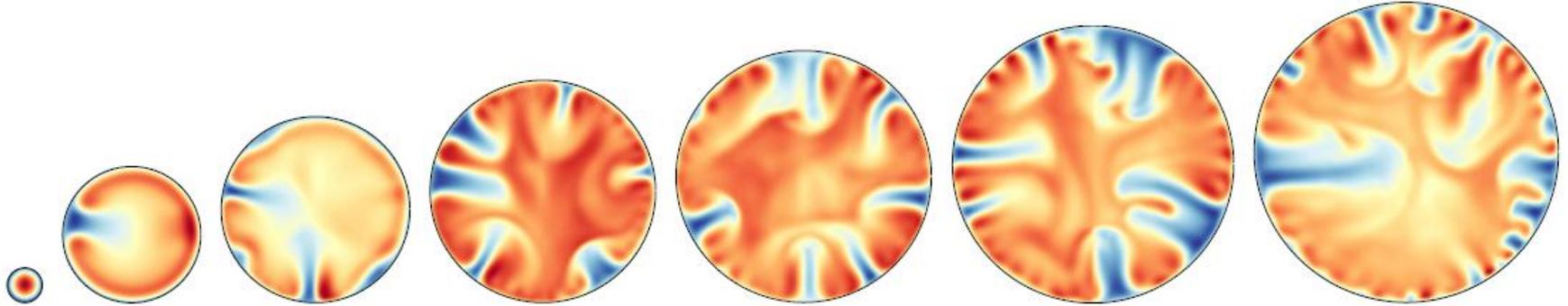
$\tau_{ic} = 0.9 \text{ Gy}$  ,  $k = 36 \text{ W.m}^{-1}.\text{K}^{-1}$  , potential temperature :

►  $\eta = 10^{19} \text{ Pa.s}$  , translation regime :

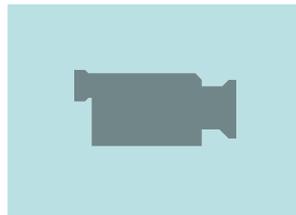


# Convection and translation

- ▶  $\eta = 3 \times 10^{17}$  Pa.s, chaotic plume convection :



For moderate viscosity, thermal convection and translation together.



# Thermal convection in the inner core

- Whole sphere convection with active cold plumes
- Convective time window: signature of the innermost inner core?
- Fusion and solidification may generate a translation regime dor a very viscous inner core.
- Convection and translation may coexist

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# Ligth element in the core

$$c(t) = c_0 \left[ \frac{r_c^3 - r_{ic}^3}{r_c^3} \right]^{k-1}$$

$k$ , partition coefficient

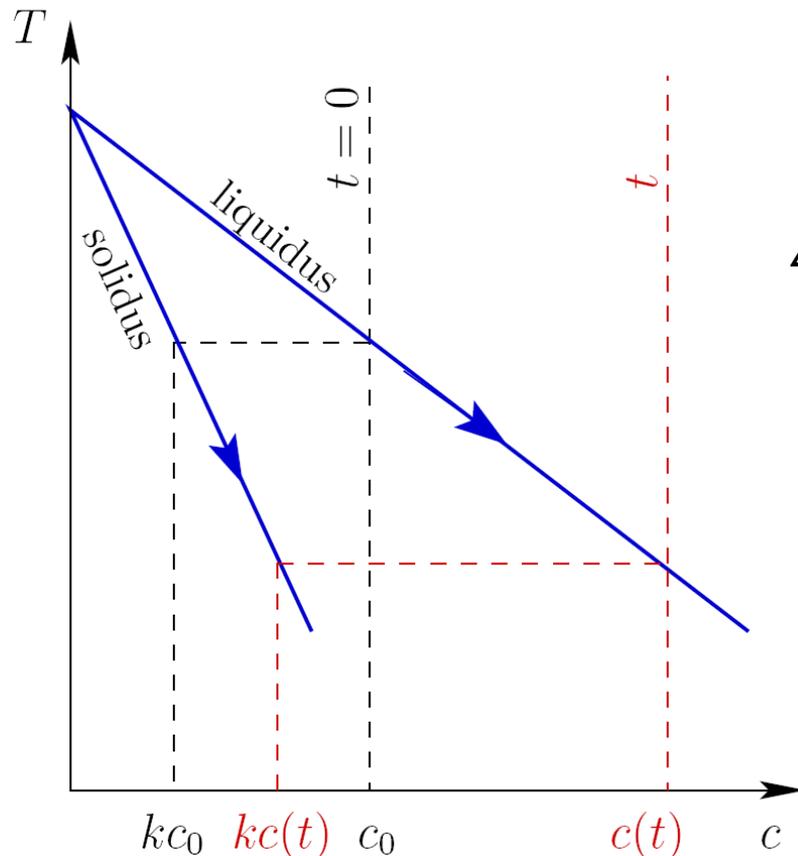
$$\Delta\rho(t) = \beta\rho kc_0 \left[ \left( 1 - \left( \frac{r_{ic}}{r_c} \right)^3 \right)^{k-1} - 1 \right]$$

$$\sim \beta\rho c_0 k(1-k) \left( \frac{r_{ic}}{r_c} \right)^3$$

$$\beta = \frac{1}{\rho} \frac{\partial \rho}{\partial c}$$

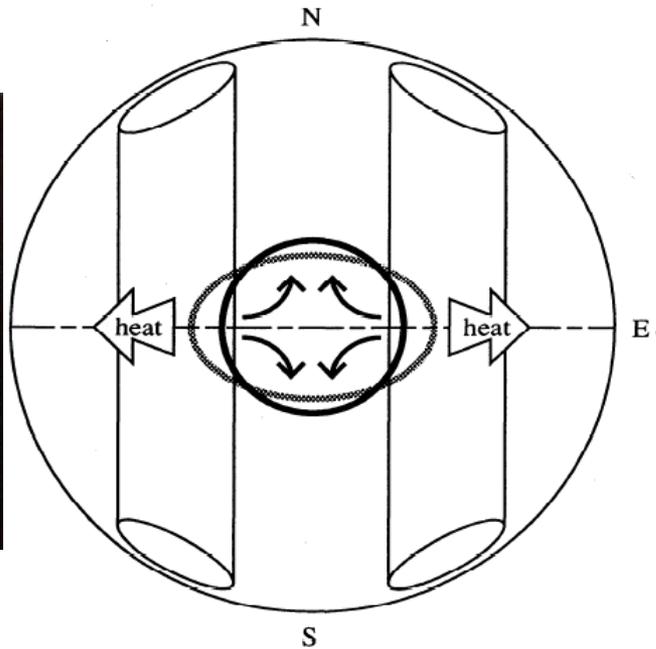
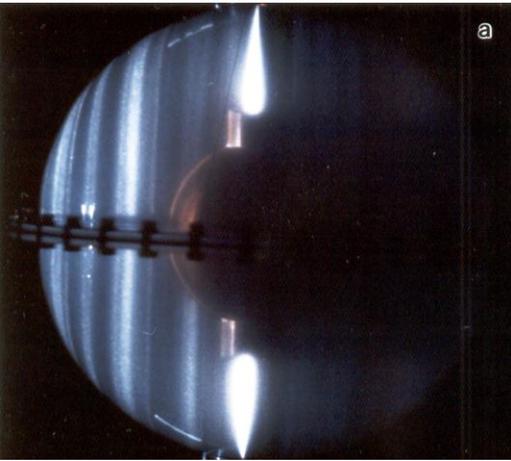
$$k_{Si} \sim k_S \sim 0.8, k_O \sim 2.5 \cdot 10^{-3}$$

(Alfè et al, 2002)

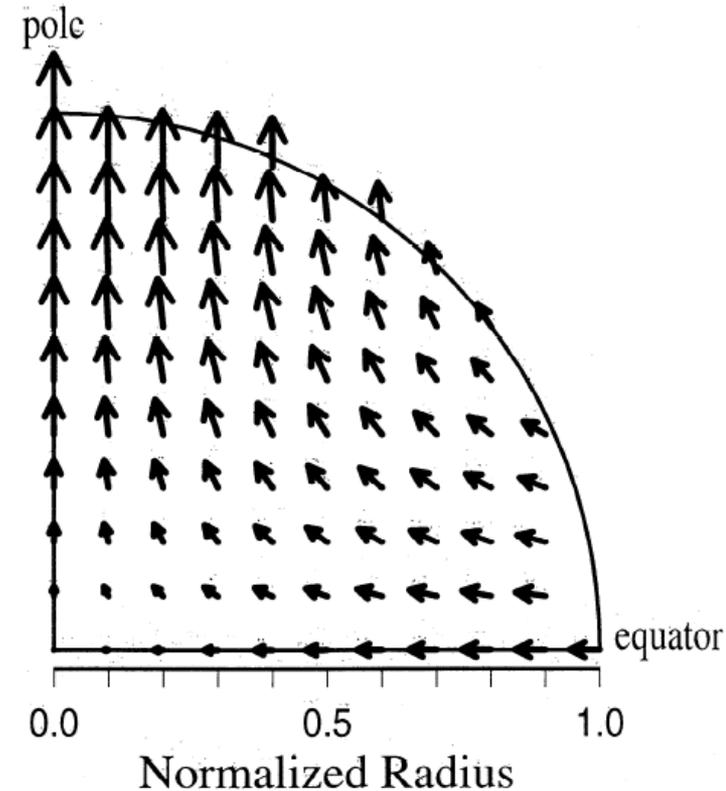


$$\Delta\rho \sim -5 \text{ kg/m}^3$$

# Equatorial growth



Yoshida et al, 1996



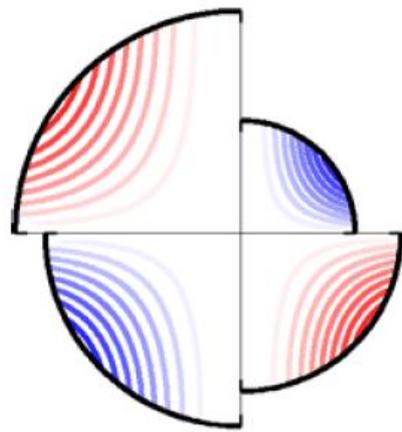
$$B = \frac{g(t) \beta \rho \Delta c(t) r_{ic}(t)^2}{\eta u_{ic}(t)}$$

$$S_2 = 2/5$$

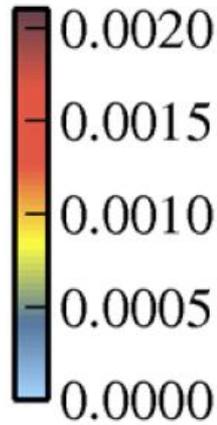
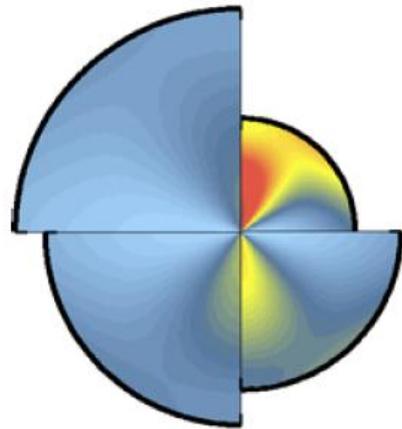
The rate of crystallisation in the equator is twice the polar one

$$u_r(r_{ic}, \theta) = -S_2 u_{ic} P_2(\cos \theta)$$

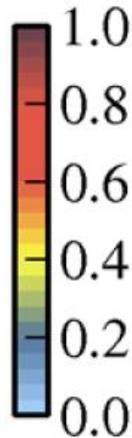
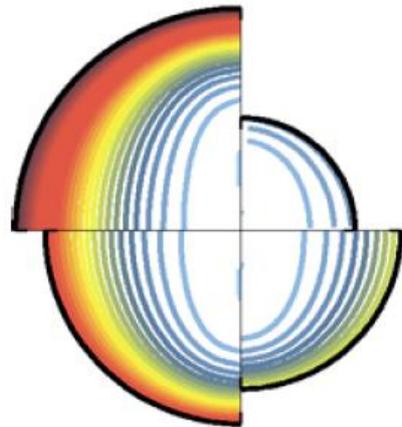
No stratification



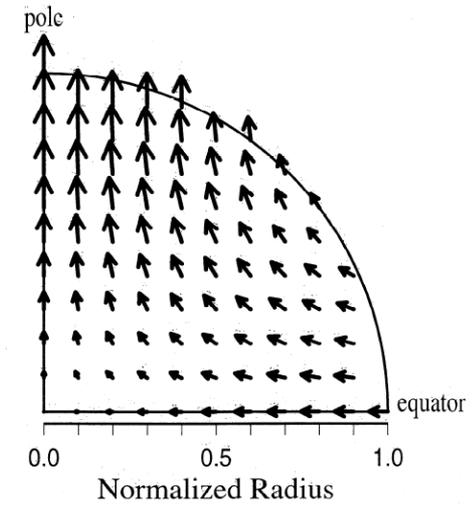
$\psi$



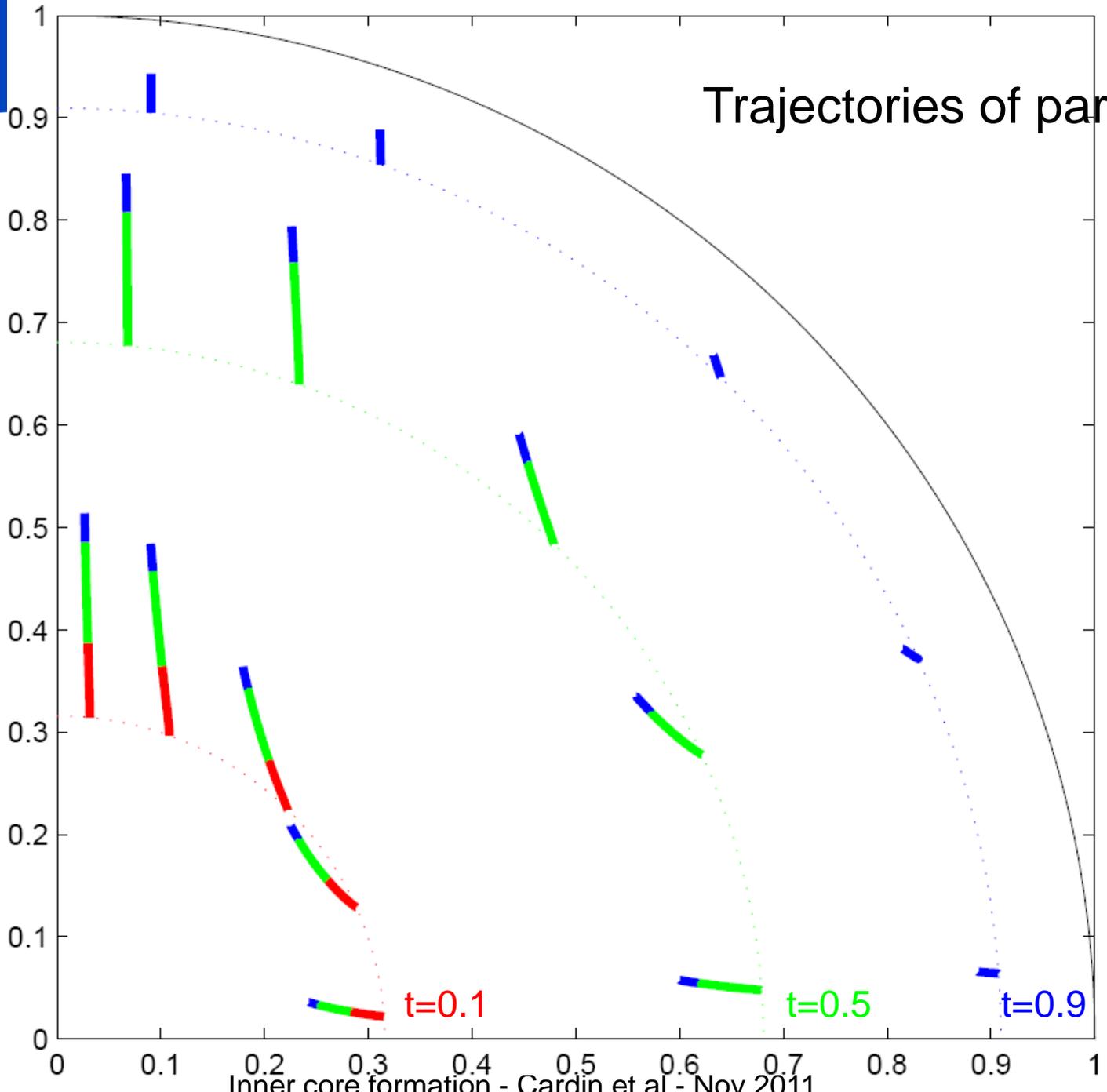
$\dot{\epsilon}$  (My<sup>-1</sup>)

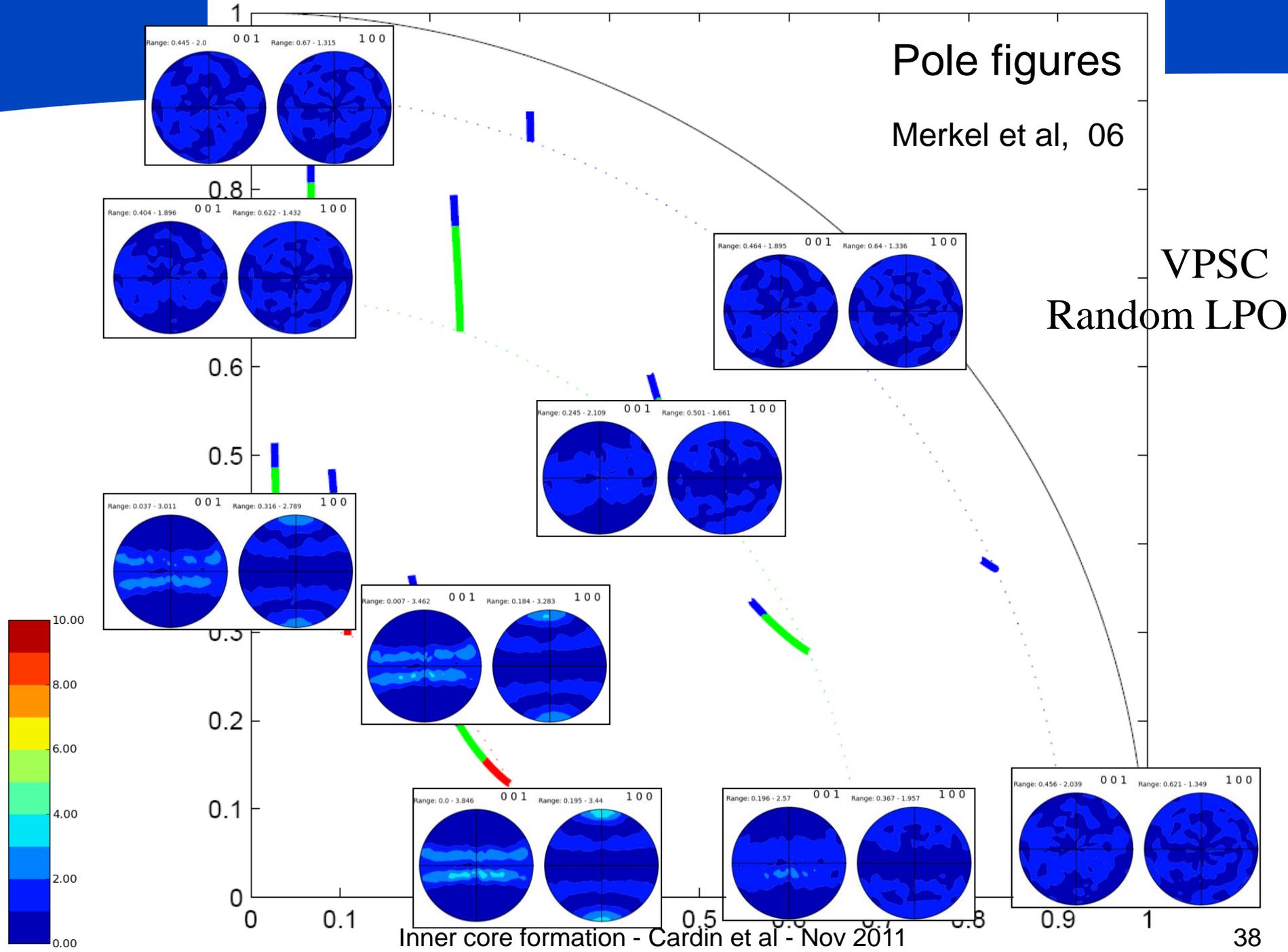


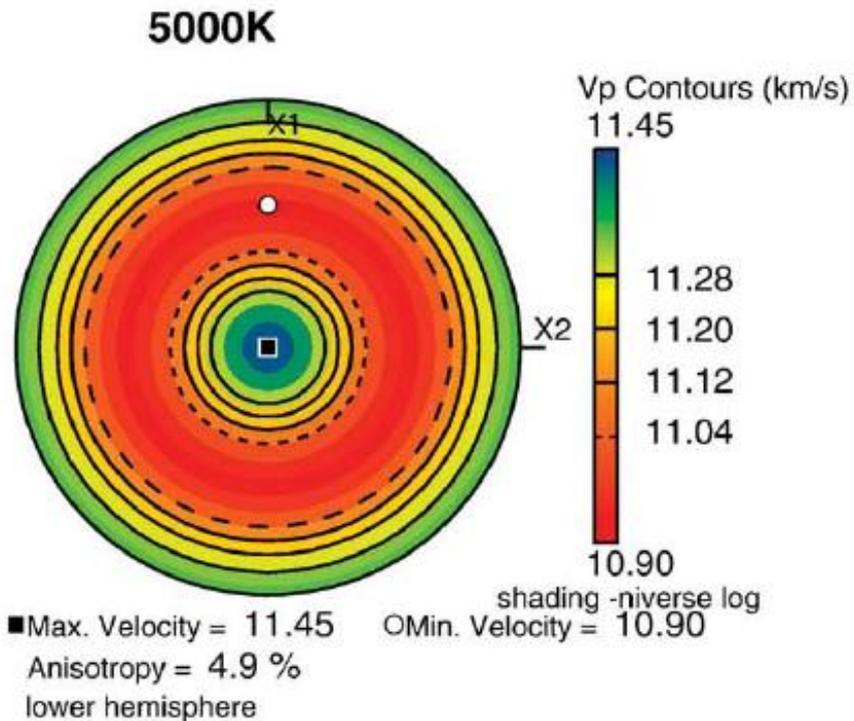
$\chi$



# Trajectories of particles







Vocadlo et al., 09

L. Vočadlo et al. / Earth and Planetary Science Letters 288 (2009) 534–538

535

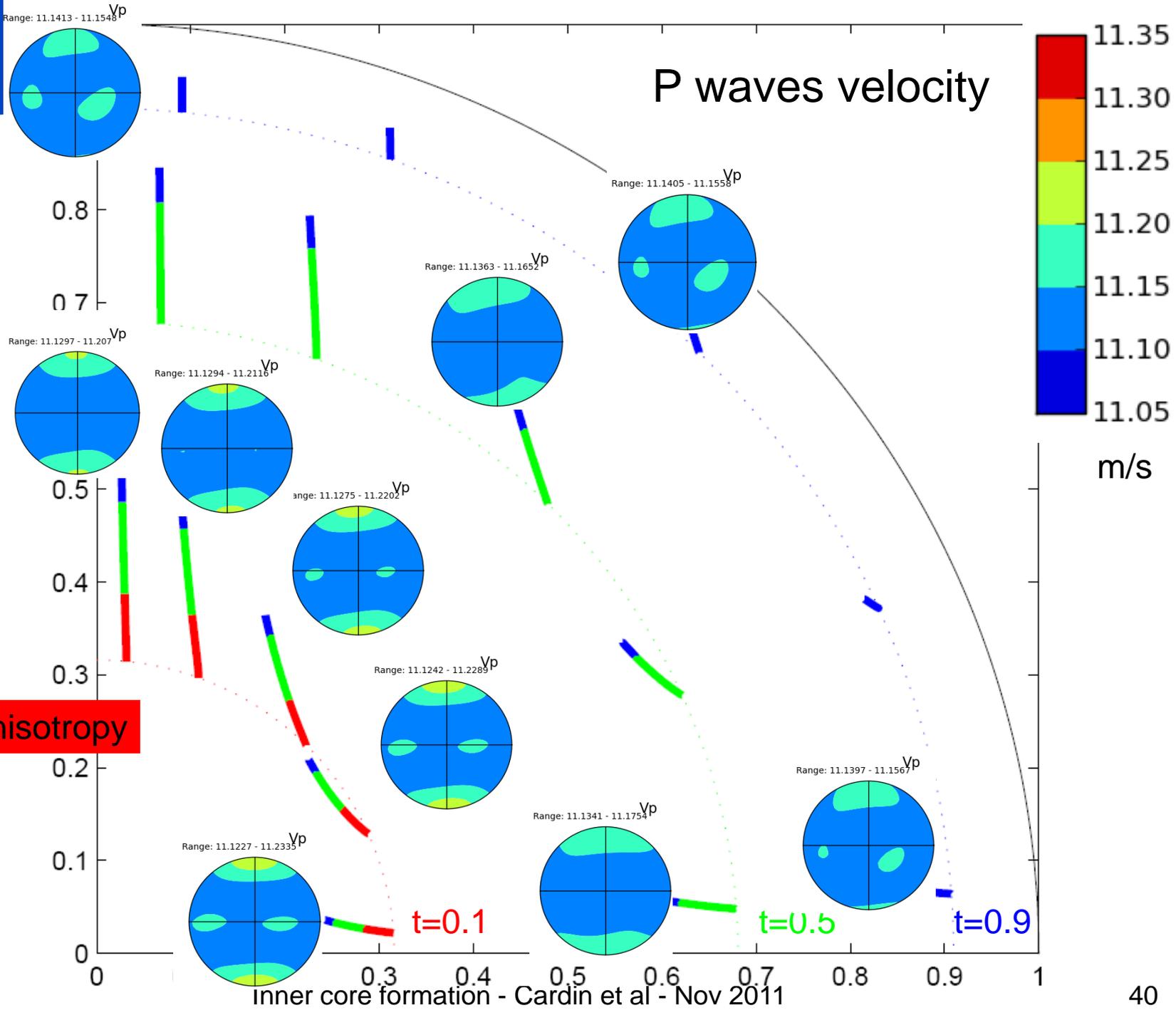
**Table 1**

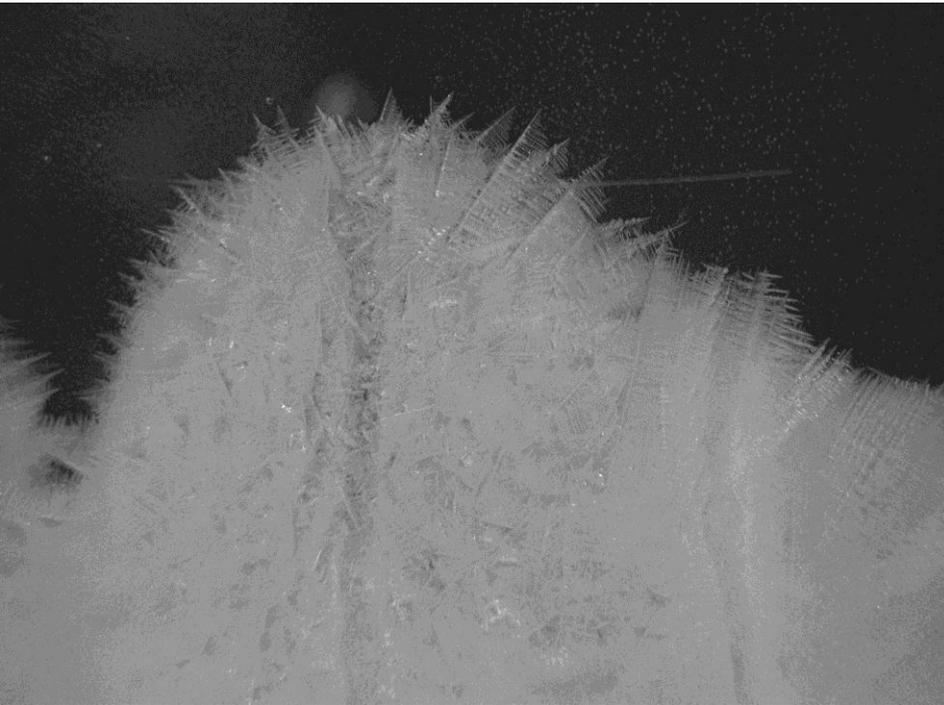
Isothermal elastic constants (in GPa), adiabatic incompressibility, shear modulus and sound velocities for hcp-Fe as a function of temperature.

$T$ (K)	$c/a$	$\rho$ ( $\text{kgm}^{-3}$ )	$P$ (GPa)	$c_{11}$	$c_{33}$	$c_{12}$	$c_{23}$	$c_{44}$	$c_{66}$	$K_S$ (GPa)	$G$ (GPa)	$V_p$ ( $\text{kms}^{-1}$ )	$V_s$ ( $\text{kms}^{-1}$ )
0	1.585	13698	295	2205	2418	1053	950	479	576	1419	564	12.59	6.42
2000	1.59	13401	290	1998	2183	1111	986	375	444	1412	444	12.23	5.75
3000	1.60	13324	293	1915	2109	1121	986	313	397	1407	394	12.05	5.44
4000	1.61	13236	298	1830	1905	1150	1004	248	340	1399	328	11.78	4.98
5000	1.62	13154	308	1689	1725	1186	990	216	252	1365	266	11.44	4.50
5500	1.62	13155	316	1646	1559	1253	995	153	197	1363	208	11.17	3.97

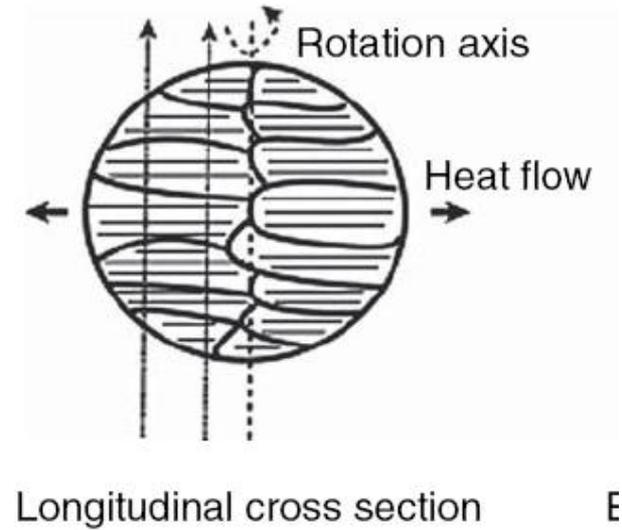
$c_{66}$  is not independent and is equal to  $1/2 (c_{11} - c_{12})$ . Uncertainties in  $c_{ii} < 2.5\%$ ; uncertainties in  $V_p$  and  $V_s$  are  $\sim 1\%$ . The values for  $c/a$  were taken from Gannarelli et al. (2005).

<1% of anisotropy





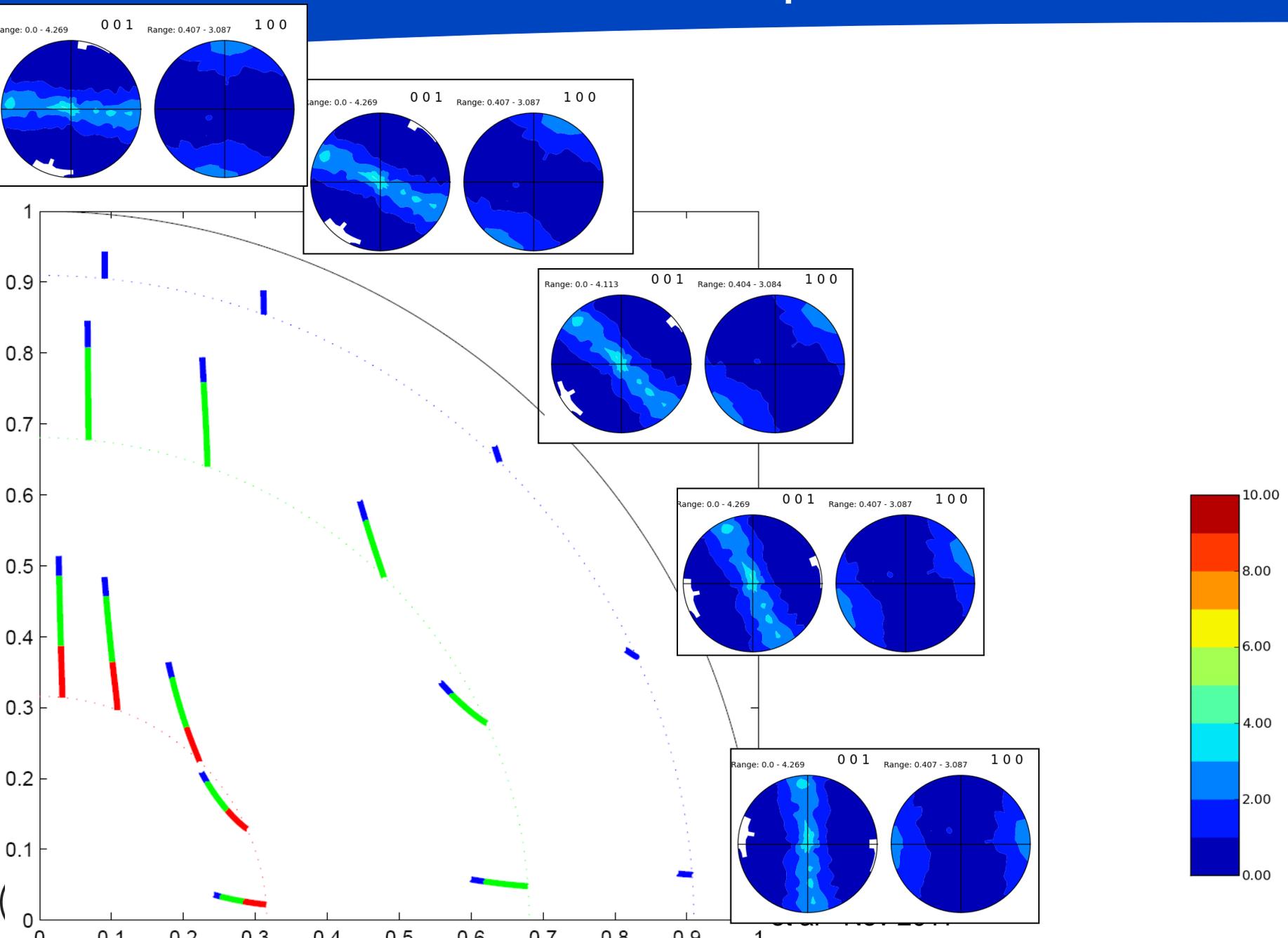
Deguen, 09



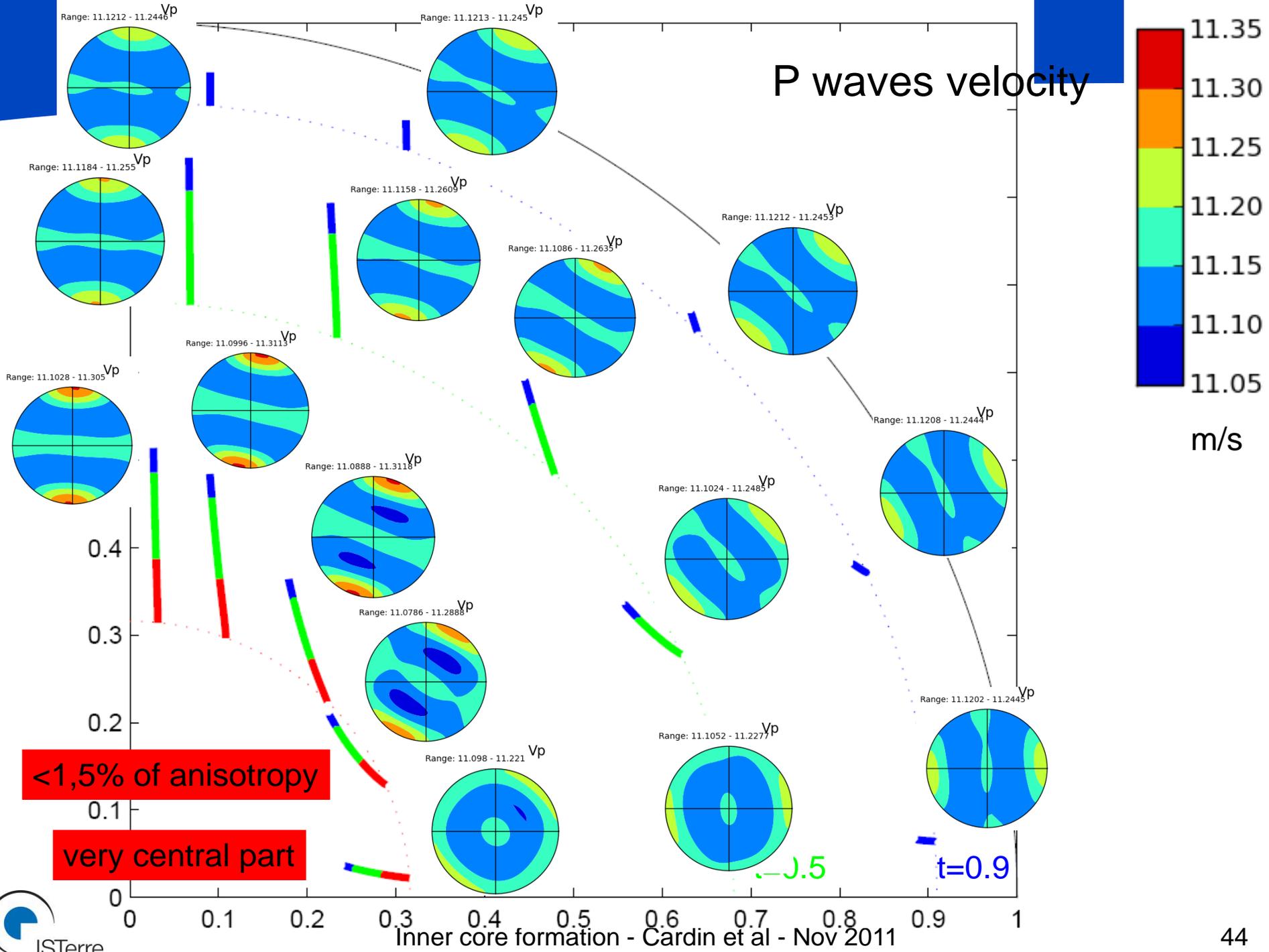
Bergman, 97

C axes parallel to cristallisation front

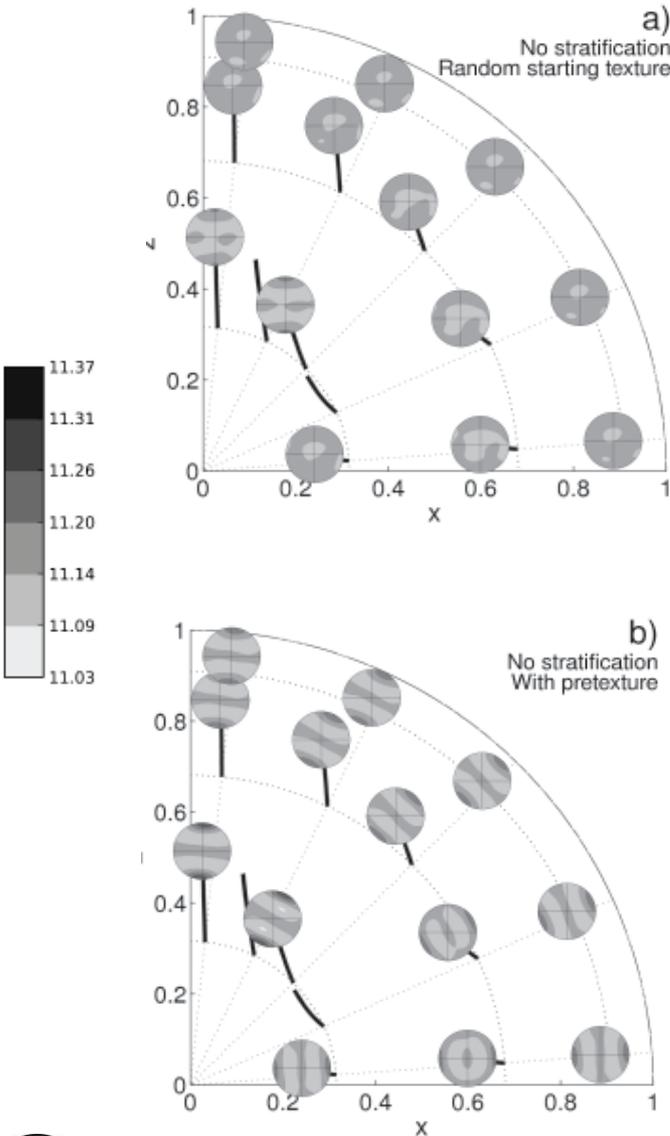
# Surface pretexturation



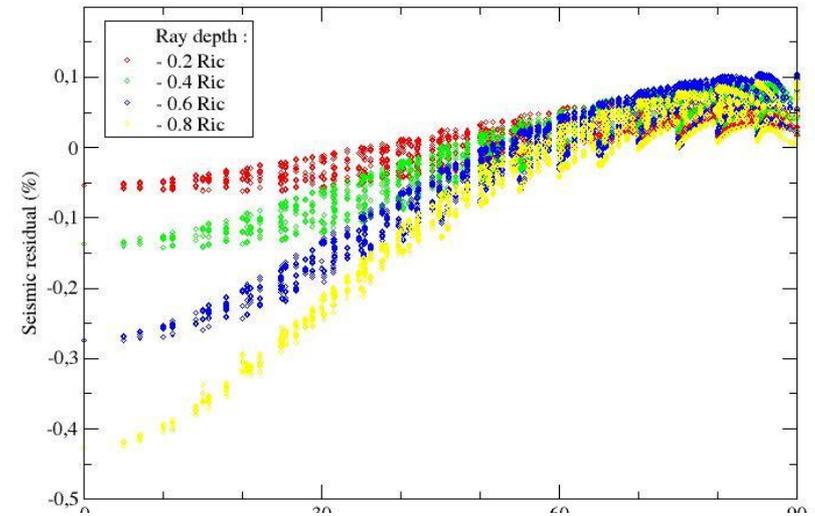




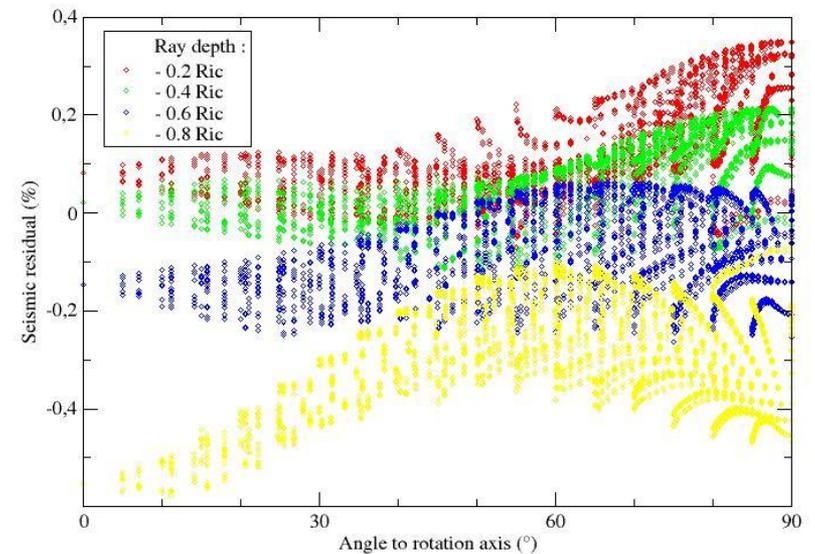
# Residuals for Yoshida model



Yoshida's model, not pretexture inner core

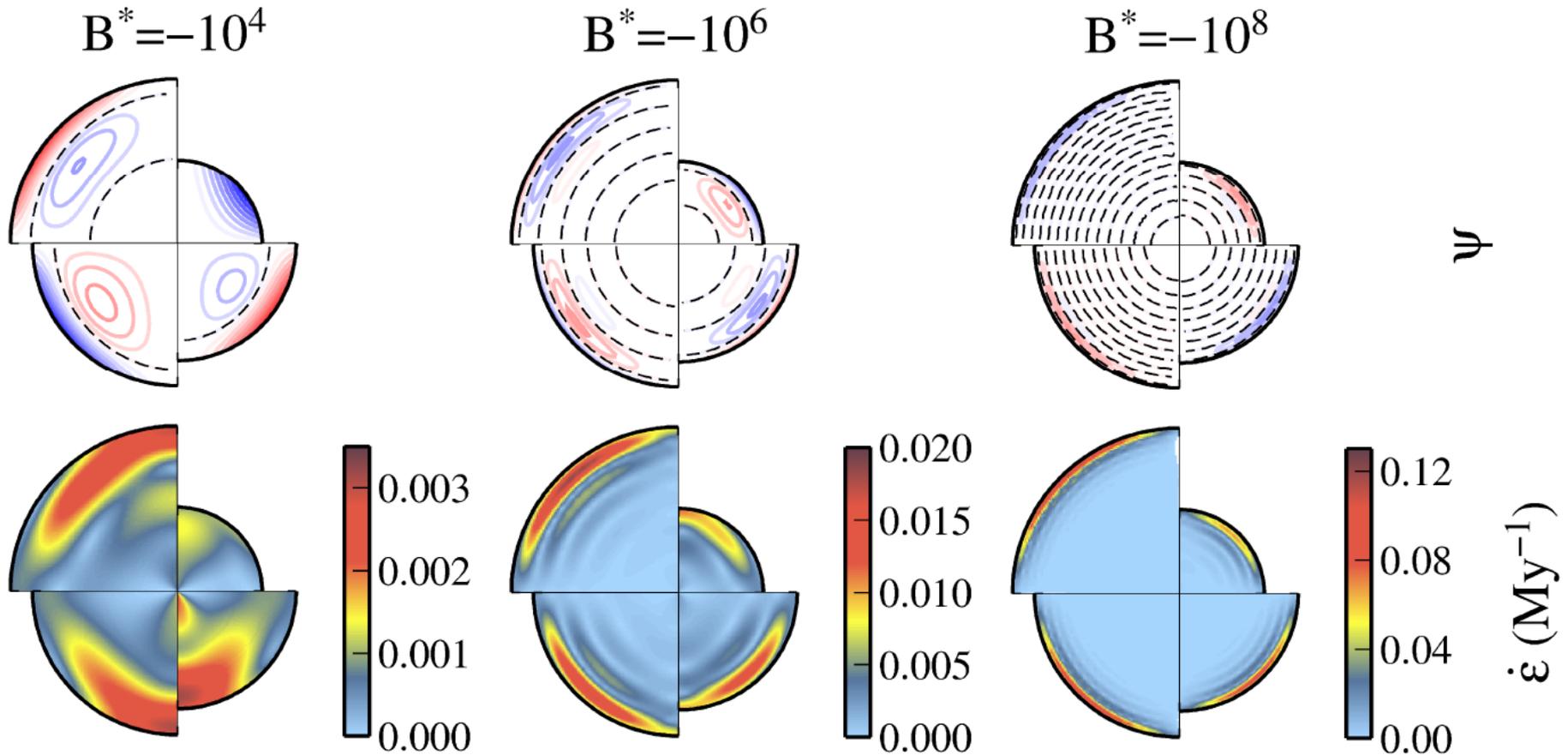


Yoshida's model, pretexture inner core



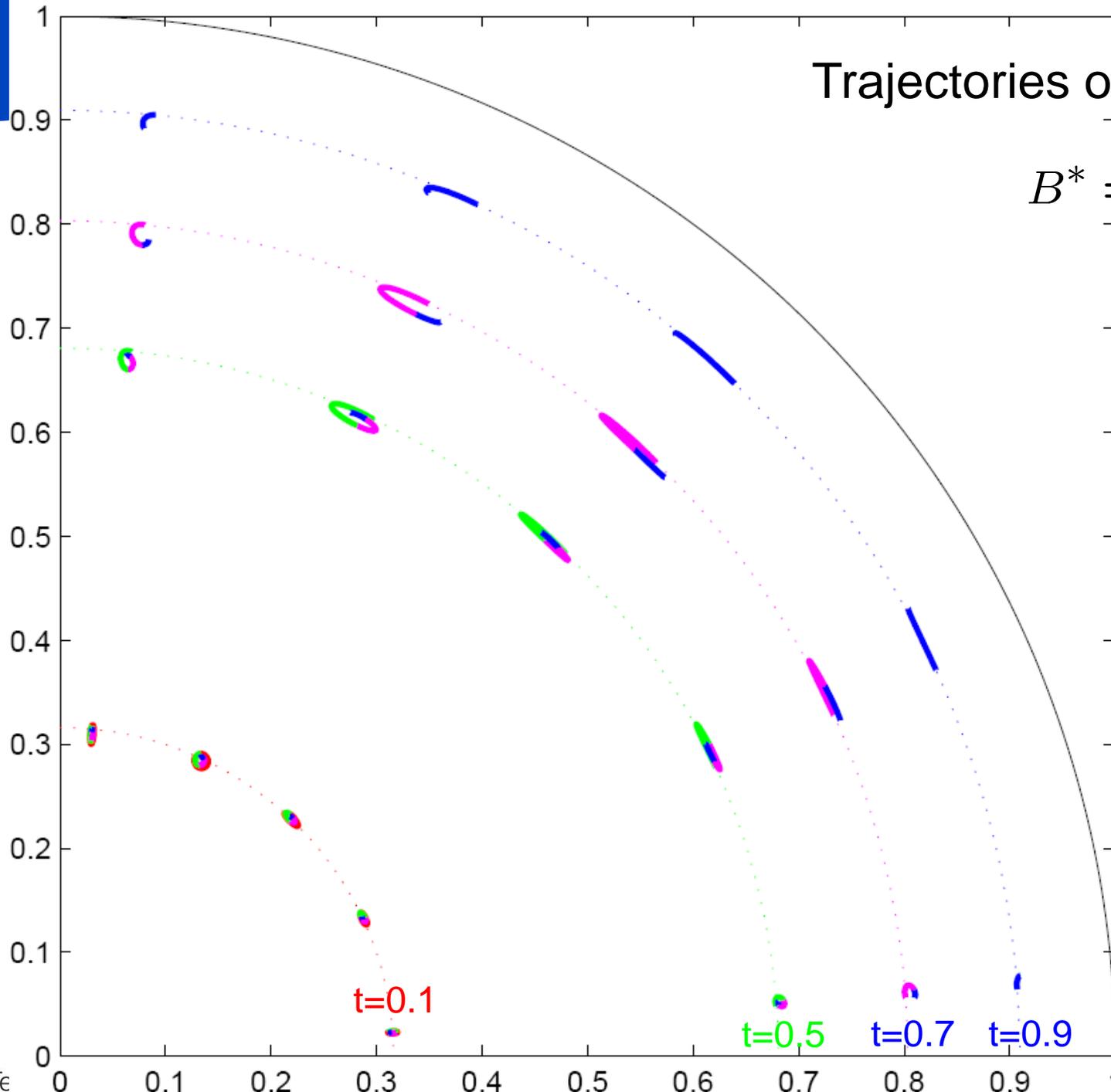
# Stratified models

More and more stratification

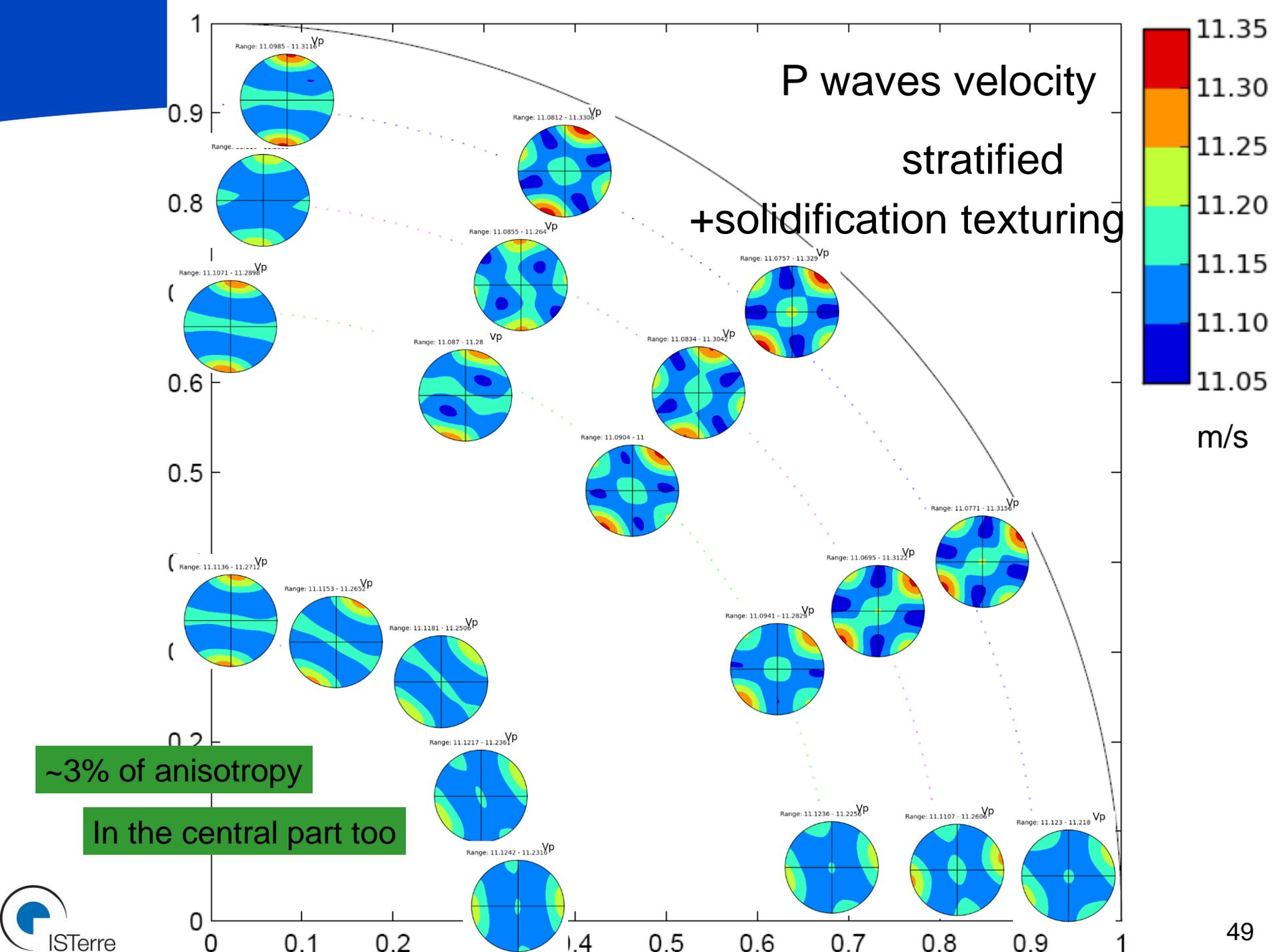


# Trajectories of particules

$$B^* = -10^6$$







# Stratified inner core and equatorial growth

- Stratification inhibits radial motion
- Superficial layer with large stresses
- With no stratification, anisotropy is too small
- Stratification and solidification texture produce  $V_p$  maps compatible to seismic observation.

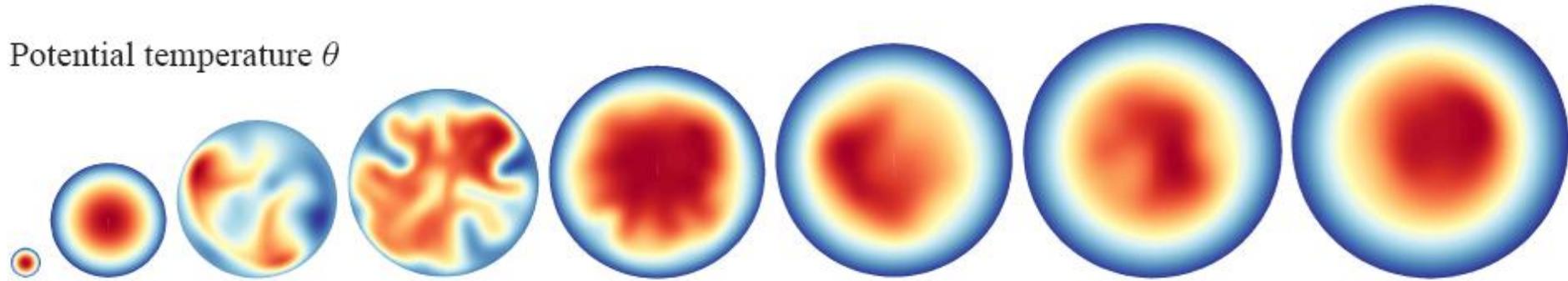
# Outline

1. Seismological observations, anisotropy
2. Review of proposed mechanism
3. Dynamical state of the inner core
4. Thermal convection in the inner core
5. Stratified inner core and equatorial growth
6. Perspectives

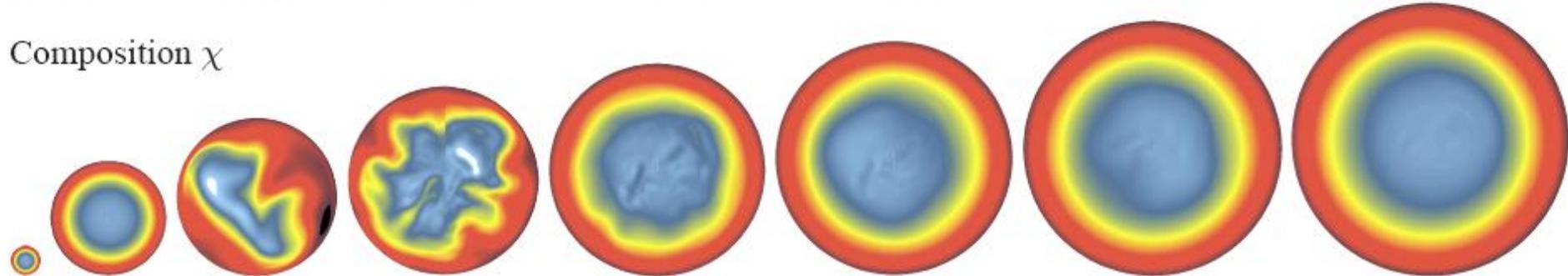
# Double diffusive convection

**a.**  $\tau_{ic} = 1 \text{ Gy}$ ,  $\eta = 10^{18} \text{ Pa.s}$ ,  $k = 36 \text{ W.m}^{-1}.\text{K}^{-1}$ ,  $c_0 = 5.6 \text{ wt.}\%$ .

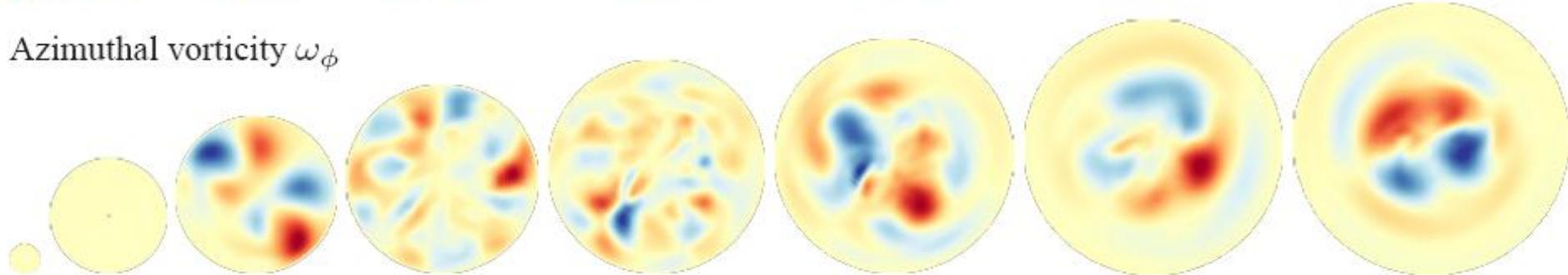
Potential temperature  $\theta$



Composition  $\chi$



Azimuthal vorticity  $\omega_\phi$



# References

- Tectonic history of the Earth's inner core preserved in its seismic structure. Deguen, R., Cardin, P. *Nature Geoscience* 2, 419–422, 2009.
- Texturing in the Earth's inner core due to preferential growth in its equatorial belt, R. Deguen, Ph. Cardin, S. Merkel, R. Lebensohn, PEPI, 2011
- Thermo-chemical convection in the Earth's inner core, R. Deguen and P. Cardin, *Geophysical Journal International*, 2011
- Thèse en cours Ainhoa Lincot