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Data-mining approaches to find new materials

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Overview



Comparing methods

An electronic-structure data-base

Finding new 2D materials

Are there more high temperature superconductors ?

A data-base for Ce compounds

Some experience with DMFT

Conclusion

Comparing methods



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Density functional theory

$$\left(-\frac{\nabla^2}{2} + V_{\text{eff}}\right) \psi = \epsilon \psi$$

$$V_{\text{eff}}(n(r))$$

$$n(r) = \sum |\psi(r)|^2$$





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FP-LMTO

Springer Series in Solid-State Sciences 167

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Full-Potential Electronic Structure Method
Energy and Force Calculations with Density
Functional and Dynamical Mean Field Theory

This book covers the theory of electronic structure of materials, with special emphasis on the usage of linear muffin-tin orbitals. Methodological aspects are given in detail as are examples of the method when applied to various materials. Different exchange and correlation functionals are described and how they are implemented within the basis of linear muffin-tin orbitals. Functionals covered are the local spin density approximation, generalised gradient approximation, self-interaction correction and dynamical mean field theory.

Wills · Alouani · Andersson
Delin · Eriksson · Grechnev

SPRINGER SERIES IN SOLID-STATE SCIENCES 167

1

Full-Potential Electronic
Structure Method

Full-Potential Electronic Structure Method

Energy and Force Calculations with Density
Functional and Dynamical Mean Field Theory

123



springer.com

DMFT implementation:

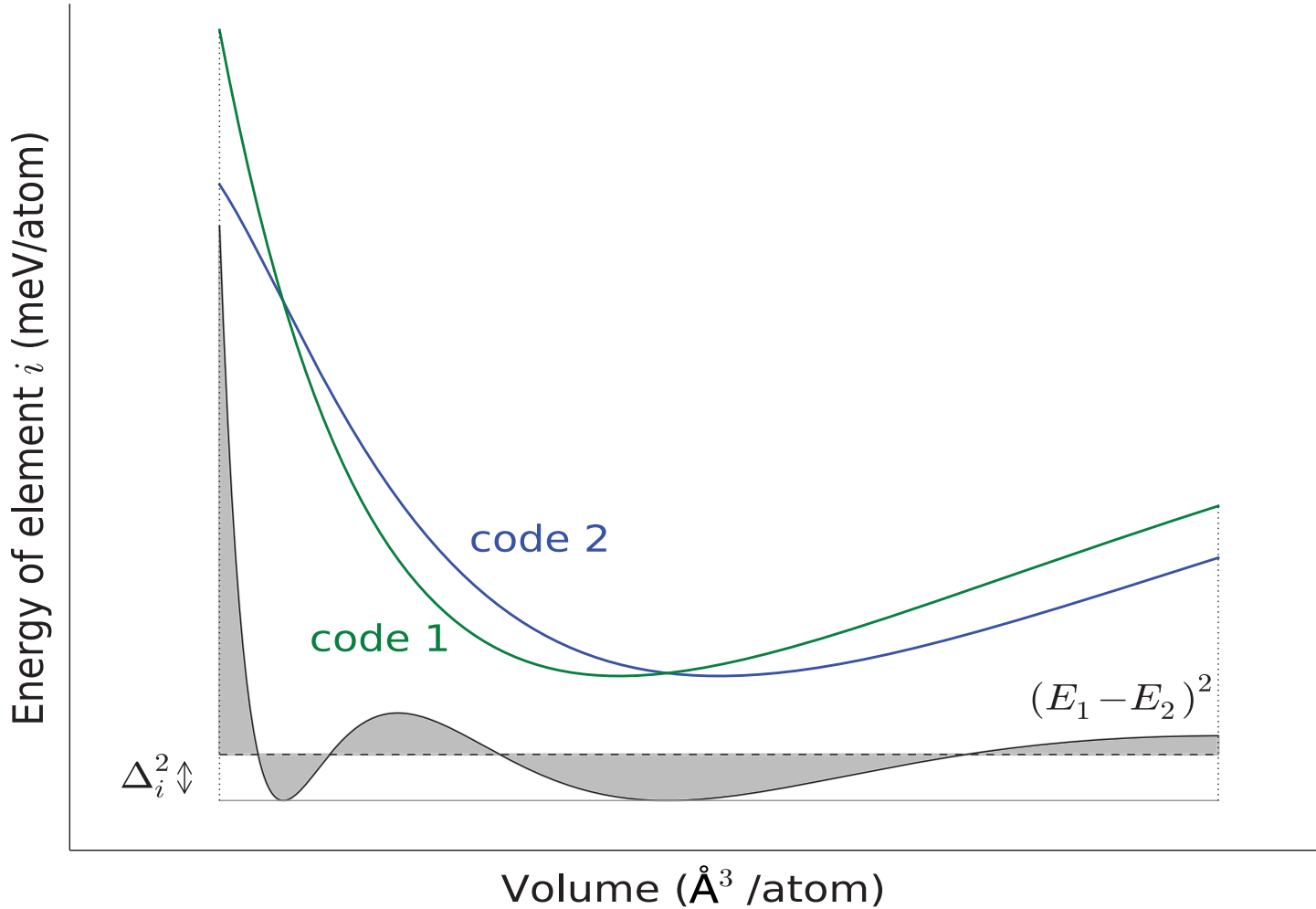
1. Grechnev, Di Marco et al.
PRB, 76, 35107 (2007)
2. Di Marco et al
PRB 79 115111 (2009)
3. Thunström et al.
PRB 79, 165104 (2009)
4. Grånäs et al.
Comp. Mat. Sci. 55, 295 (2012)
5. Thunström, Di Marco et al.
PRL 109, 186401 (2012).

Katsnelson+Lichtenstein



The delta-test setup

100-200 meV/atom



	WIEN2k-new	FLEUR	RSPt	FPLO_TplusF_soft	FPLO_TplusF	FPLO_default	Abinit_JTH2	Abinit_JTH	Abinit_delta40	GPAW09	GPAW06	QE91	VASPGW	VASP53hard	VASP52	VASP	CASTEP8	CASTEP7	CASTEP-MS	CASTEP-USP	OpenMX	DACAPO	Abinit_FHI
WIEN2k-new	0.0	0.8	0.8	0.9	1.0	3.9	0.6	1.2	1.3	1.5	3.8	1.8	0.8	0.7	1.0	2.1	0.5	2.4	3.4	7.7	2.0	6.2	14.5
FLEUR	0.8	0.0	0.7	0.9	0.9	3.5	0.7	0.8	1.5	1.7	3.4	1.6	1.2	0.9	1.3	1.8	1.0	2.8	3.7	7.8	1.7	6.5	13.8
RSPt	0.8	0.7	0.0	0.9	0.7	3.2	0.7	0.9	1.5	1.7	3.4	1.6	1.2	1.0	1.3	1.9	1.1	3.0	3.9	7.9	1.8	6.5	14.0
FPLO_TplusF_soft	0.9	0.9	0.9	0.0	0.8	3.6	0.9	1.2	1.7	1.9	3.5	1.6	1.3	1.2	1.4	1.9	1.1	2.9	3.7	7.7	1.8	6.4	13.9
FPLO_TplusF	1.0	0.9	0.7	0.8	0.0	3.1	0.9	1.0	1.8	2.0	3.4	1.6	1.3	1.1	1.5	1.9	1.2	3.1	3.9	7.9	1.8	6.4	14.6
FPLO_default	3.9	3.5	3.2	3.6	3.1	0.0	3.6	3.4	4.1	4.2	3.1	3.3	4.0	3.9	4.0	2.8	4.0	5.8	6.2	8.9	3.2	7.2	13.6
Abinit_JTH2	0.6	0.7	0.7	0.9	0.9	3.6	0.0	0.9	1.4	1.6	3.5	1.6	1.0	0.7	1.0	1.9	0.7	2.6	3.6	7.6	1.9	6.2	14.2
Abinit_JTH	1.2	0.8	0.9	1.2	1.0	3.4	0.9	0.0	1.5	1.8	3.2	1.6	1.6	1.4	1.6	1.9	1.3	3.0	3.8	7.9	1.5	6.5	13.4
Abinit_delta40	1.3	1.5	1.5	1.7	1.8	4.1	1.4	1.5	0.0	0.7	3.6	2.2	1.6	1.4	1.7	2.4	1.4	2.5	3.5	7.9	2.3	6.0	14.2
GPAW09	1.5	1.7	1.7	1.9	2.0	4.2	1.6	1.8	0.7	0.0	3.6	2.3	1.9	1.7	1.9	2.5	1.6	2.8	3.7	8.0	2.5	6.4	14.3
GPAW06	3.8	3.4	3.4	3.5	3.4	3.1	3.5	3.2	3.6	3.6	0.0	2.9	4.0	3.7	3.9	2.8	3.8	5.6	5.6	8.6	3.0	7.6	13.0
QE91	1.8	1.6	1.6	1.6	1.6	3.3	1.6	1.6	2.2	2.3	2.9	0.0	1.9	1.8	1.9	1.5	1.7	3.3	3.7	7.4	1.8	5.9	14.1
VASPGW	0.8	1.2	1.2	1.3	1.3	4.0	1.0	1.6	1.6	1.9	4.0	1.9	0.0	0.8	1.2	2.1	0.8	2.6	3.6	8.1	2.2	6.1	15.1
VASP53hard	0.7	0.9	1.0	1.2	1.1	3.9	0.7	1.4	1.4	1.7	3.7	1.8	0.8	0.0	0.5	1.8	0.8	2.6	3.5	7.8	2.1	6.3	14.5
VASP52	1.0	1.3	1.3	1.4	1.5	4.0	1.0	1.6	1.7	1.9	3.9	1.9	1.2	0.5	0.0	1.7	1.0	2.8	3.8	8.0	2.3	6.8	14.5
VASP	2.1	1.8	1.9	1.9	1.9	2.8	1.9	1.9	2.4	2.5	2.8	1.5	2.1	1.8	1.7	0.0	2.1	3.5	4.1	7.8	1.7	6.1	13.3
CASTEP8	0.5	1.0	1.1	1.1	1.2	4.0	0.7	1.3	1.4	1.6	3.8	1.7	0.8	0.8	1.0	2.1	0.0	2.2	3.2	7.6	2.0	5.6	14.7
CASTEP7	2.4	2.8	3.0	2.9	3.1	5.8	2.6	3.0	2.5	2.8	5.6	3.3	2.6	2.6	2.8	3.5	2.2	0.0	2.3	6.8	3.4	5.7	14.8
CASTEP-MS	3.4	3.7	3.9	3.7	3.9	6.2	3.6	3.8	3.5	3.7	5.6	3.7	3.6	3.5	3.8	4.1	3.2	2.3	0.0	7.6	3.9	6.0	14.3
CASTEP-USP	7.7	7.8	7.9	7.7	7.9	8.9	7.6	7.9	7.9	8.0	8.6	7.4	8.1	7.8	8.0	7.8	7.6	6.8	7.6	0.0	8.2	11.0	13.5
OpenMX	2.0	1.7	1.8	1.8	1.8	3.2	1.9	1.5	2.3	2.5	3.0	1.8	2.2	2.1	2.3	1.7	2.0	3.4	3.9	8.2	0.0	6.4	13.6
DACAPO	6.2	6.5	6.5	6.4	6.4	7.2	6.2	6.5	6.0	6.4	7.6	5.9	6.1	6.3	6.8	6.1	5.6	5.7	6.0	11.0	6.4	0.0	18.4
Abinit_FHI	14.5	13.8	14.0	13.9	14.6	13.6	14.2	13.4	14.2	14.3	13.0	14.1	15.1	14.5	14.5	13.3	14.7	14.8	14.3	13.5	13.6	18.4	0.0

A data-base of electronic structures

*Calculated
Electronic Properties
of Metals*

by

V. L. Moroz
J. F. Janak
A. R. Williams

PERGAMON



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Electronic structure database

http://gurka.fysik.uu.se/ESP/

http://gurka.fysik.uu.se/ESP/ Google

wiki saob eniro seb SAS News (168) work sj ul stockholm ord torrent LK musik SSH

ESP					
Version	Complete list				
A word of caution	Search	Element	Methods	FAQ	Contact

Element:

Element:

Element:

Element:

Element:

Antal element:

http://gurka.fysik.uu.se/ESP/

1 H																	2 He
3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne
11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
55 Cs	56 Ba	*	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
87 Fr	88 Ra	**	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Uun	111 Uuu	112 Uub	113 Uut	114 Uuq	115 Uup	116 Uuh	117 Uus	118 Uuo

Computational Materials
Science 44, 1042 (2009)

*	57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu
**	89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr

Finding new 2D materials

Search criteria

Packing ratio 0.1-0.50

Large gap along one crystallographic direction
($>2.5 \text{ \AA}$)

No covalent bonds over gap

Results: all known 2D's, including di-
chalcogenides
Many new 2D's

New 2D materials (PRX 3, 31002 (2013))

TABLE III. List of compounds found by our algorithm that do not belong to the family of dichalcogenides. The chemical formula, the ICSD number of the corresponding bulk material, the value of the minimum band gap, and an eventual magnetic ordering are given in the different columns from left to right. (The cells of the table are left blank if the material is not magnetically ordered.)

2D chemical formula	3D ICSD number	Gap (eV)	Magnetism	2D chemical formula	3D ICSD number	Gap (eV)	Magnetism
PbIF	150193	2.3		PbSb ₂ Te ₄	250250	0.8	
HgI ₂	150345	1.8		KC ₆ FeO ₃ N ₃	280850	4.5	
ZrClN	151468	1.9		MgI ₂	281551	3.6	
BaIF	155006	4.3		BiI ₂	391354	1.5	
SrIF	155009	4.5		FeBr ₃	410924	0.5	AFM
AlCl ₂	155670	Metal		MgPSe ₃	413165	2.1	
Ag ₂ ReCl ₆	156662	Metal		IYGa	417149	Metal	
Ni ₂ Te ₂ Sb	158485	Metal		PTe ₂ Ti ₂	418978	Metal	
Bi ₁₄ Te ₁₃ S ₈	159356	0.9		ScP ₂ AgSe ₆	420302	1.8	
MgBr ₂	165972	4.8		CrSiTe ₃	626809	0.6	FM
Cu ₂ S	166578	Metal		FePSe ₃	633094	0.05	
P ₂ AgSe ₆ Bi				FeS	633302	Metal	
P ₂ CuSe ₆ Bi				FeTe	633877	Metal	FM
YI ₃				Sb ₂ Ge ₂ Te ₅	637823	0.2	
GaS				SbSiNi	646436	Metal	
VCl ₂	246905	Metal		PbO	647260	2.5	
VBr ₂	246906	Metal		CdI ₂	655780	2.5	
VI ₂	246907	Metal		GaSe	660262	1.8	
PFeLi	247089	Metal		ZnIn ₂ S ₄	660273	Metal	
PbBi ₂ Te ₄	250249	1.0		Zn ₂ In ₂ S ₅	660333	Metal	

Verified in
Small 11, 1253 (2015)

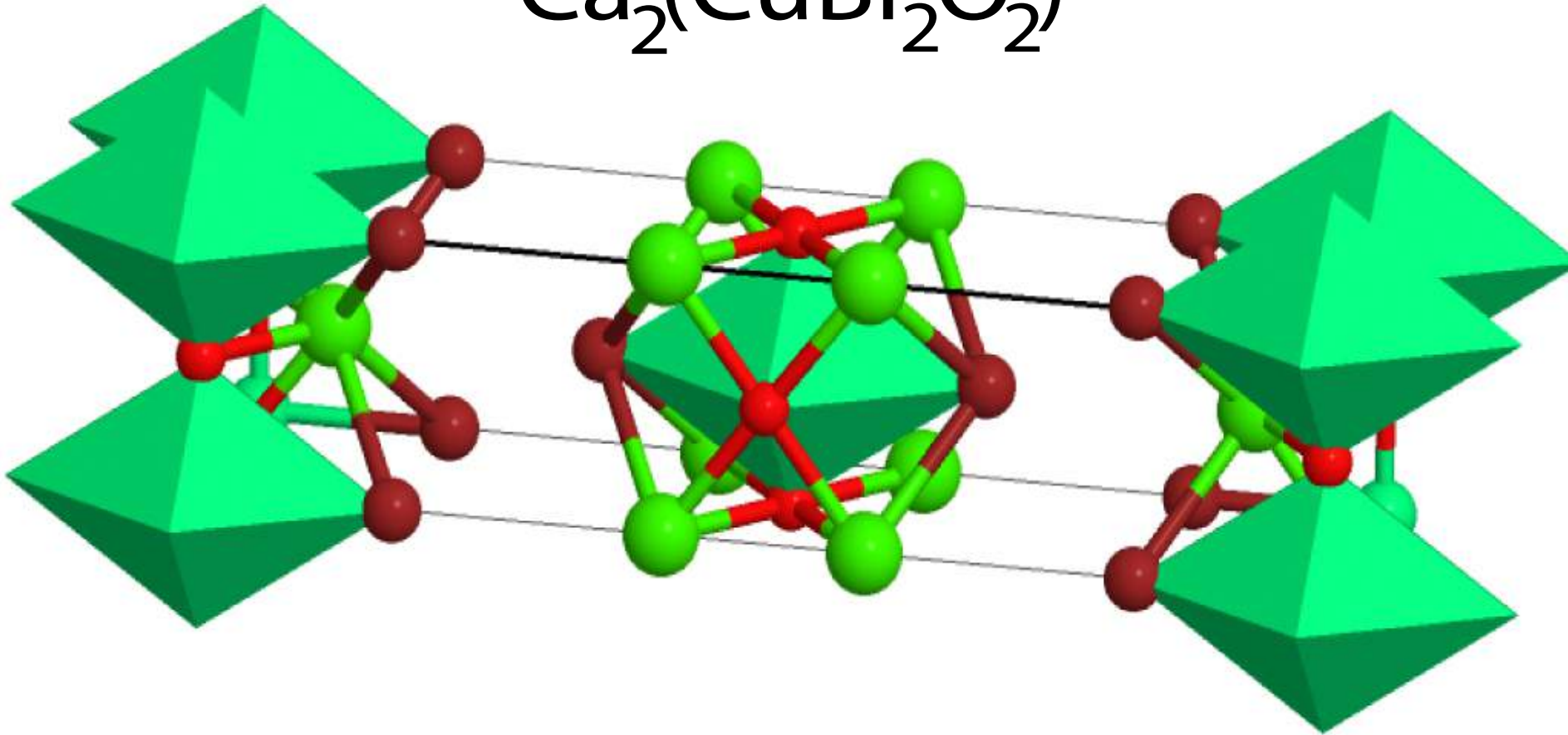
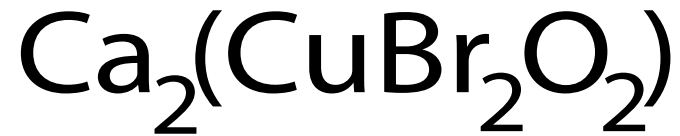


**Are there more high temperature
superconductors ?**



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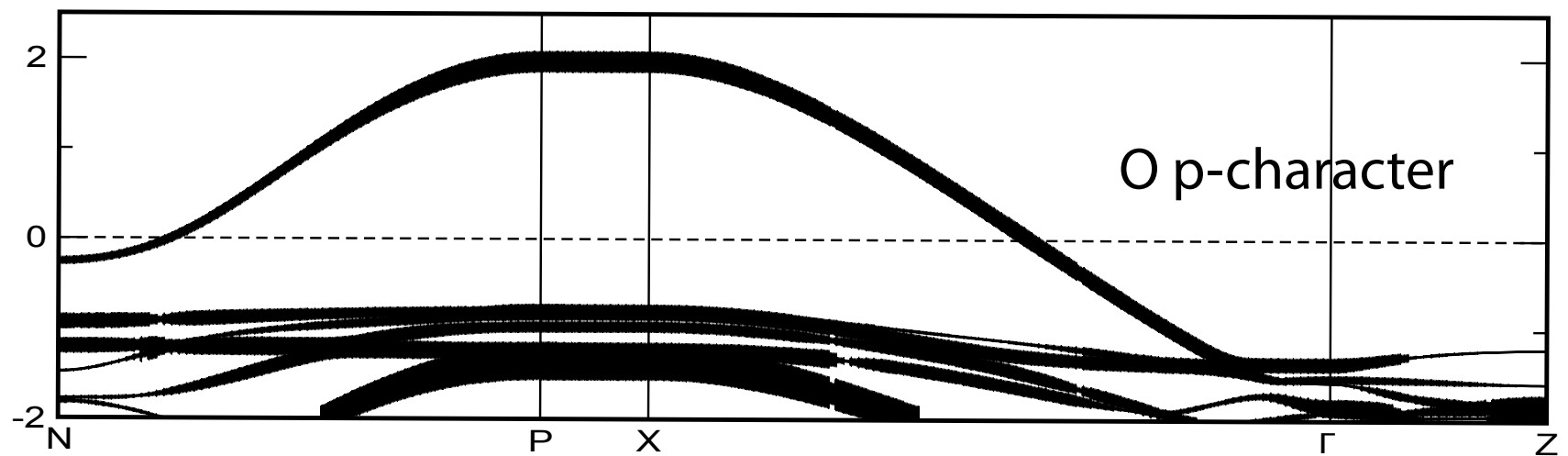
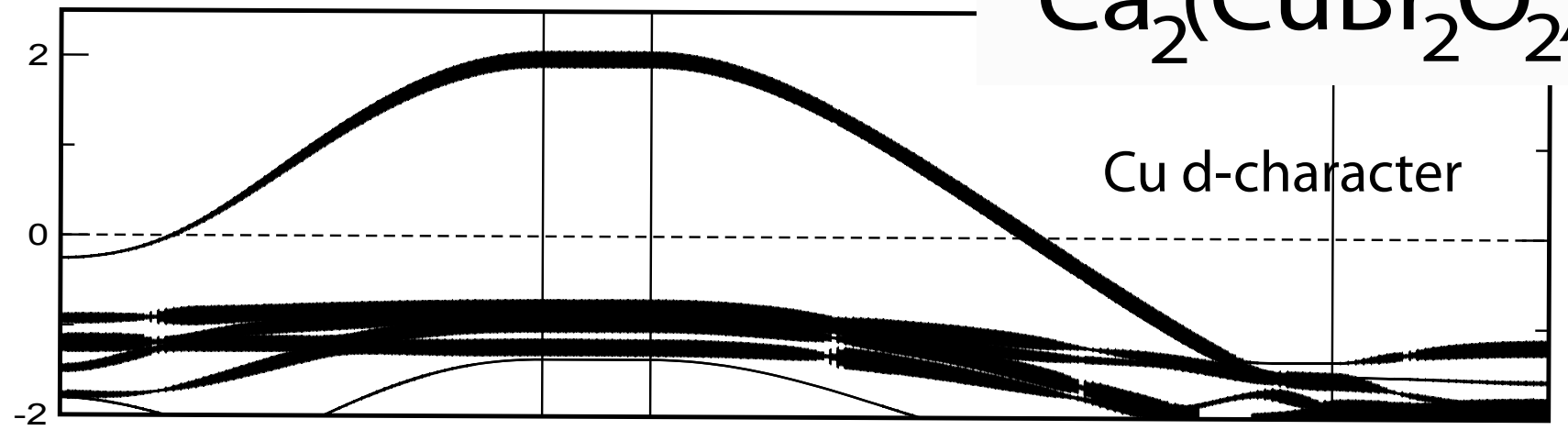
Data-mining criterion-structure



Computational Materials Science 67 282 (2013)



Data-mining criterion-bands/bonds



Supplementary information

The table below shows compound name, space group, space group number, bravais lattice and ICSD reference number. Using the ICSD web-site [1], and the ICSD reference number, allows the reader to generate pictures of the crystal structure.

In the fat-band representation the thickness of the band corresponds to the amount of s -, p - or d -character of the band. This is calculated as follows. Let $n(\mathbf{k})$ be the occupation at \mathbf{k} given by

$$n(\mathbf{k}) = Tr(O(\mathbf{k})\rho(\mathbf{k}))$$

where $O(\mathbf{k})$ and $\rho(\mathbf{k})$ is the overlap and density, respectively. The fatness f_l for eigenvalue ν can then be calculated using

$$f_l = \frac{Tr(O(\mathbf{k})\rho^{\nu_l}(\mathbf{k}))}{Tr(O(\mathbf{k})\rho(\mathbf{k}))}$$

where element ij of the density matrix is given in terms of weights (w) and eigenvectors (Z) by:

$$\rho_{ij}(\mathbf{k}) = \sum_{\nu} w_{\nu,\mathbf{k}} Z_i(\mathbf{k}, \nu) Z_j^{\dagger}(\mathbf{k}, \nu)$$

$$\rho_{ij}^{\nu_l}(\mathbf{k}) = w_{\nu_l,\mathbf{k}} Z_i(\mathbf{k}, \nu_l) Z_j^{\dagger}(\mathbf{k}, \nu_l)$$

$\sum_l f_l$ sums up to one electron and l runs over the complete basis. Note that in the figures below the Fermi level is at zero. Also, in the band plots we make a projection on atomic and l-resolved fat bands.

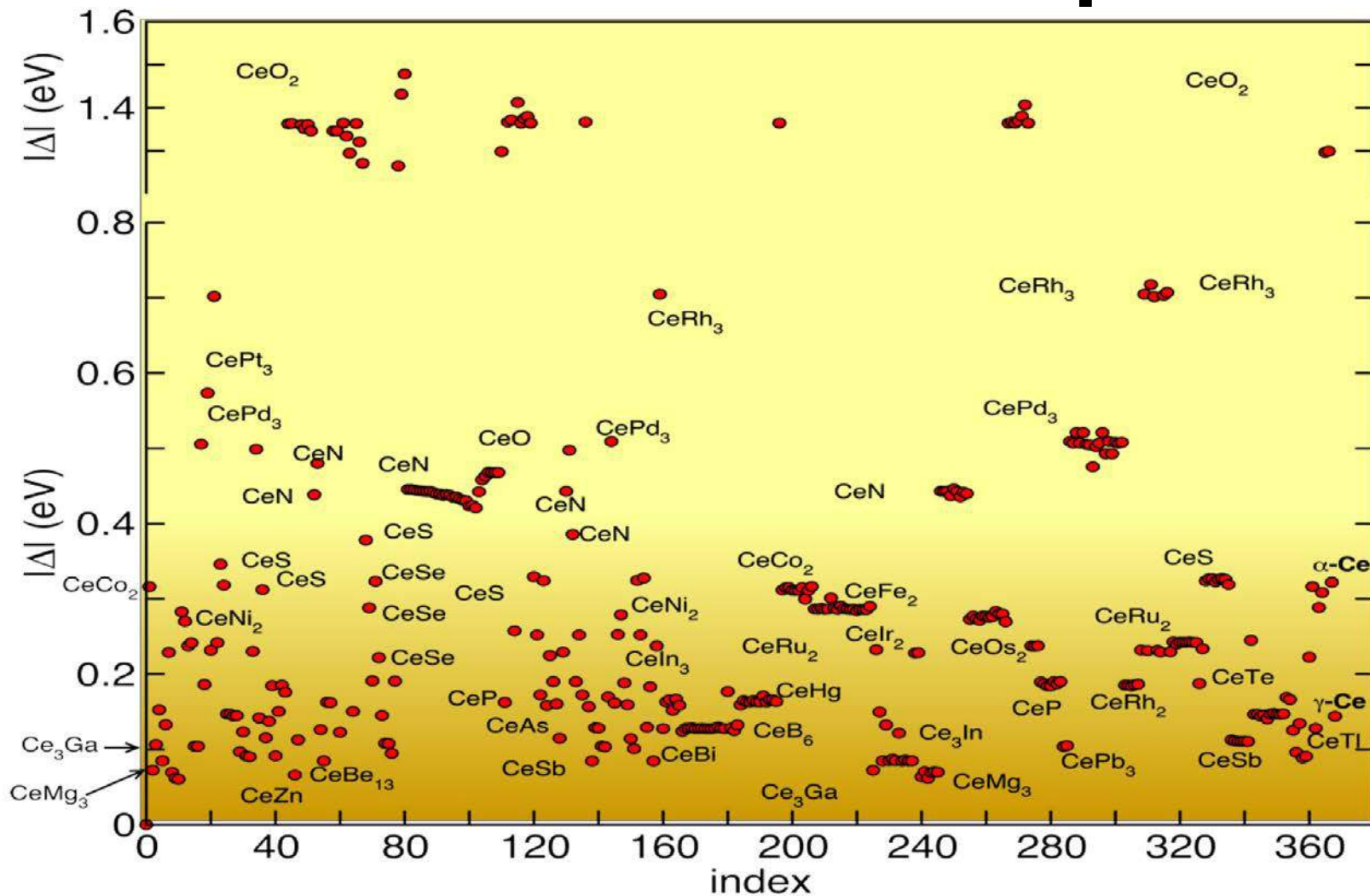
[1] G. Bergerhoff and I. D. Brown, in Crystallographic Databases, F. H. Allen et al. (Hrsg.) Chester, International Union of Crystallography, (1987). The figures were generated using ICSD Web (<http://icsd.fiz-karlsruhe.de/icsd>) using version 2.1.0.

Material	Space group	(#)	Bravais lattice	ICSD #
AuCuZn ₂	F m -3 m	(225)	cubic face-centred	150571
AgAuZn ₂	F m -3 m	(225)	cubic face-centred	604792
CuNi ₂ Sb	F m -3 m	(225)	cubic face-centred	53320
CuNi ₂ Sn	F m -3 m	(225)	cubic face-centred	103068
ErPt ₂	F d -3 m S	(227)	cubic face-centred	103287
EuPt ₂	F d -3 m S	(227)	cubic face-centred	103430
HoPt ₂	F d -3 m S	(227)	cubic face-centred	104441
NaPt ₂	F d -3 m S	(227)	cubic face-centred	644945
BaPt ₂	F d -3 m S	(227)	cubic face-centred	616039
CuSe	P 63/m m c	(194)	hexagonal primitive	240
KAuTe	P 63/m m c	(194)	hexagonal primitive	40165
RbAuTe	P 63/m m c	(194)	hexagonal primitive	75026
CdInGaS ₄	P -3 m 1	(164)	hexagonal primitive	20785
ZrNCl	P -3 m 1	(164)	hexagonal primitive	25506
KCuSe	P 63/m m c	(194)	hexagonal primitive	12157
KCuTe	P 63/m m c	(194)	hexagonal primitive	12158
Li ₂ ZnGe	P -3 m 1	(164)	hexagonal primitive	53678
Li ₂ ZnSi	P -3 m 1	(164)	hexagonal primitive	16221
AuYO ₂	P 63/m m c	(194)	hexagonal primitive	95675
AgAlO ₂	P 63/m m c	(194)	hexagonal primitive	300020
CuBr	P 63 m c	(186)	hexagonal primitive	30092
Ca ₂ CuZn ₂ P ₃	P 63/m m c	(194)	hexagonal primitive	89517
Al ₅ C ₃ N	P 63 m c	(186)	hexagonal primitive	26859
Ca ₃ Cu ₂ Zn ₂ P ₄	P -3 m 1	(164)	hexagonal primitive	89515
Eu ₃ Cu ₂ Zn ₂ P ₄	P -3 m 1	(164)	hexagonal primitive	89516
Cu ₄ (S ₂) ₂ (CuS) ₂	P 63/m m c	(194)	hexagonal primitive	26968

Material	Space group	(#)	Bravais lattice	ICSD #
LaKPdO ₃	C 1 2/m 1	(12)	monoclinic base-centred	417108
BaY ₂ F ₈	C 1 2/m 1	(12)	monoclinic base-centred	74359
AgCuS	C m c m	(63)	orthorhombic base-centred	30233
LaSeTe ₂	C m c m	(63)	orthorhombic base-centred	413171
NbS ₂	C m 2 m	(38)	orthorhombic base-centred	67443
BaNiY ₂ O ₅	I m m m	(71)	orthorhombic body-centred	68795
RuOCl ₂	I m m m	(71)	orthorhombic body-centred	83883
Bi ₂ (CO ₃)O ₂	I m m 2	(44)	orthorhombic body-centred	94740
Al ₂ Ba ₃ Ge ₂	I m m m	(71)	orthorhombic body-centred	52612
Ba ₃ Al ₂ Si ₂	I m m m	(71)	orthorhombic body-centred	100128
Ba ₃ Al ₂ Sn ₂	I m m m	(71)	orthorhombic body-centred	9565
NbSe ₂	F m 2 m	(42)	orthorhombic face-centred	71339
TaS ₂	F m 2 m	(42)	orthorhombic face-centred	280988
TaS ₂	F 2 m m	(42)	orthorhombic face-centred	67651
TaSe ₂	F m 2 m	(42)	orthorhombic face-centred	72198
Tl ₂ Ba ₂ CuO ₆	F m m m	(69)	orthorhombic face-centred	41569
TiNCl	P m m n S	(59)	orthorhombic primitive	27396
Pb ₂ Ba ₂ YCuCu ₂ O ₈	P 2 21 2	(17)	orthorhombic primitive	66088
Pb ₂ Sr ₂ YCu ₃ O ₈	P 2 21 2	(17)	orthorhombic primitive	66587
YBa ₂ Cu ₃ O _{6.5}	P m m m	(47)	orthorhombic primitive	75697
YBa ₂ Cu ₃ O _{6.5}	P m m m	(47)	orthorhombic primitive	96016
EuBa ₂ Cu ₃ O ₇	P m m m	(47)	orthorhombic primitive	81171
Ba ₂ GdCu ₃ O ₇	P m m m	(47)	orthorhombic primitive	56514
HoBa ₂ Cu ₃ O ₇	P m m m	(47)	orthorhombic primitive	68044
LaBa ₂ Cu ₃ O ₇	P m m m	(47)	orthorhombic primitive	81167
NdBa ₂ Cu ₃ O ₇	P m m m	(47)	orthorhombic primitive	81169
PrBa ₂ Cu ₃ O ₇	P m m m	(47)	orthorhombic primitive	81168
SmBa ₂ Cu ₃ O ₇	P m m m	(47)	orthorhombic primitive	71705
Ba ₂ YCu ₃ O ₇	P m m m	(47)	orthorhombic primitive	202770
Ba ₂ YCu ₃ O ₇	P m m m	(47)	orthorhombic primitive	77737
LaBa ₂ Cu ₃ O ₈	P m m m	(47)	orthorhombic primitive	85291
Na ₃ Cu ₄ S ₄	P b a m	(55)	orthorhombic primitive	10004
Sr ₄ V ₃ O ₁₀	I 4/m m m	(139)	tetragonal body-centred	73698
MoB	I 41/a m d S	(141)	tetragonal body-centred	24280
WB	I 41/a m d S	(141)	tetragonal body-centred	24281
Yb(AgS ₂)	I 41 m d	(109)	tetragonal body-centred	27091
LaI ₂	I 4/m m m	(139)	tetragonal body-centred	202452
SmCu ₂ Si ₂	I 4/m m m	(139)	tetragonal body-centred	106843
TbCu ₂ Si ₂	I 4/m m m	(139)	tetragonal body-centred	106844
Cu ₂ TmSi ₂	I 4/m m m	(139)	tetragonal body-centred	53349
Cu ₂ YSi ₂	I 4/m m m	(139)	tetragonal body-centred	23551
Li ₂ PdH ₂	I 4/m m m	(139)	tetragonal body-centred	108534
Na ₂ PdH ₂	I 4/m m m	(139)	tetragonal body-centred	68071
(Cu ₂ S ₂)(Sr ₂ NiO ₂)	I 4/m m m	(139)	tetragonal body-centred	88424
Ca ₂ (CuBr ₂ O ₂)	I 4/m m m	(139)	tetragonal body-centred	1028
Sr ₂ CoO ₂ Br ₂	I 4/m m m	(139)	tetragonal body-centred	151789
CuSr ₂ Br ₂ O ₂	I 4/m m m	(139)	tetragonal body-centred	1178
Ca ₂ (CuCl ₂ O ₂)	I 4/m m m	(139)	tetragonal body-centred	1027
Ca ₂ CuO ₂ Cl ₂	I 4/m m m	(139)	tetragonal body-centred	83117
Sr ₂ CuO ₂ Cl ₂	I 4/m m m	(139)	tetragonal body-centred	4087
Tl ₂ Ba ₂ CaCu ₂ O ₈	I 4/m m m	(139)	tetragonal body-centred	78592
Bi ₂ Sr ₂ CaCu ₂ O ₈	I 4/m m m	(139)	tetragonal body-centred	68188
Ce ₂ BiO ₂	I 4/m m m	(139)	tetragonal body-centred	9099
Ce ₂ SbO ₂	I 4/m m m	(139)	tetragonal body-centred	9100
CePd ₂ Si ₂	I 4/m m m	(139)	tetragonal body-centred	621852
CePt ₂ Si ₂	I 4/m m m	(139)	tetragonal body-centred	52895
Cu ₂ ErGe ₂	I 4/m m m	(139)	tetragonal body-centred	53251
ErCu ₂ Si ₂	I 4/m m m	(139)	tetragonal body-centred	106845
Cu ₂ GdSi ₂	I 4/m m m	(139)	tetragonal body-centred	64825

Material	Space group	(#)	Bravais lattice	ICSD #
Cu ₂ HoGe ₂	I 4/m m m	(139)	tetragonal body-centred	53270
YCu ₂ Ge ₂	I 4/m m m	(139)	tetragonal body-centred	52764
Cu ₂ HoSi ₂	I 4/m m m	(139)	tetragonal body-centred	53289
NdCu ₂ Si ₂	I 4/m m m	(139)	tetragonal body-centred	106842
Eu ₂ (VO ₄)	I 4/m m m	(139)	tetragonal body-centred	89000
K ₂ (NiF ₄)	I 4/m m m	(139)	tetragonal body-centred	15576
K ₂ (NiF ₄)	I 4/m m m	(139)	tetragonal body-centred	631720
Rb ₂ (NiF ₄)	I 4/m m m	(139)	tetragonal body-centred	69682
La ₂ (NiO ₄)	I 4/m m m	(139)	tetragonal body-centred	1179
La ₂ (NiO ₄)	I 4/m m m	(139)	tetragonal body-centred	33536
La ₂ PdO ₄	I 4/m m m	(139)	tetragonal body-centred	40262
Sr ₂ (MoO ₄)	I 4/m m m	(139)	tetragonal body-centred	152123
Sr ₂ (RuO ₄)	I 4/m m m	(139)	tetragonal body-centred	157401
Sr ₂ VO ₄	I 4/m m m	(139)	tetragonal body-centred	72219
Cs ₂ AgF ₄	I 4/m m m	(139)	tetragonal body-centred	16254
K ₂ CoF ₄	I 4/m m m	(139)	tetragonal body-centred	33522
Rb ₂ CoF ₄	I 4/m m m	(139)	tetragonal body-centred	69683
Gd ₂ (CuO ₄)	I 4/m m m	(139)	tetragonal body-centred	41844
In ₂ CuO ₄	I 4/m m m	(139)	tetragonal body-centred	39475
La ₂ (CuO ₄)	I 4/m m m	(139)	tetragonal body-centred	41643
Ba ₂ CoF ₆	I 4/m m m	(139)	tetragonal body-centred	21057
Ba ₂ NiF ₆	I 4/m m m	(139)	tetragonal body-centred	21056
Ba ₂ (ZnF ₆)	I 4/m m m	(139)	tetragonal body-centred	21054
(Cu ₂ S ₂)(Sr ₂ CuO ₂)	I 4/m m m	(139)	tetragonal body-centred	88423
Ba ₂ Cu ₃ O ₄ Br ₂	I 4/m m m	(139)	tetragonal body-centred	36128
Ba ₂ Cu ₃ O ₄ Cl ₂	I 4/m m m	(139)	tetragonal body-centred	355
Ca ₃ Cu ₂ O ₄ Br ₂	I 4/m m m	(139)	tetragonal body-centred	69182
Ca ₃ Cu ₂ O ₄ Cl ₂	I 4/m m m	(139)	tetragonal body-centred	69181
La ₃ Ni ₂ O ₆	I 4/m m m	(139)	tetragonal body-centred	249209
K ₃ Ni ₂ F ₇	I 4/m m m	(139)	tetragonal body-centred	33523
Sr ₃ V ₂ O ₇	I 4/m m m	(139)	tetragonal body-centred	71320
Sr ₃ (V ₂ O ₇)	I 4/m m m	(139)	tetragonal body-centred	71451
K ₃ Co ₂ F ₇	I 4/m m m	(139)	tetragonal body-centred	33524
K ₃ Cu ₂ F ₇	I 4/m m m	(139)	tetragonal body-centred	15373
La ₄ Ni ₃ O ₈	I 4/m m m	(139)	tetragonal body-centred	173372
K ₅ Te ₃	I 4/m	(87)	tetragonal body-centred	96743
CaSmCuO ₃ Cl	P 4/n m m Z	(129)	tetragonal primitive	86428
HgBa ₂ CaCu ₂ O ₆	P 4/m m m	(123)	tetragonal primitive	75725
HgBa ₂ CaCu ₂ O ₆	P 4/m m m	(123)	tetragonal primitive	83087
TlYBa ₂ Cu ₂ O ₇	P 4/m m m	(123)	tetragonal primitive	74163
TlCaSr ₂ Cu ₂ O ₇	P 4/m m m	(123)	tetragonal primitive	74165
NdBa ₂ Cu ₂ NbO ₈	P 4/m m m	(123)	tetragonal primitive	44255
Sr ₂ CoO ₃ Cl	P 4/n m m Z	(129)	tetragonal primitive	91750
HgBa ₂ CuO ₄	P 4/m m m	(123)	tetragonal primitive	75720
Sr ₂ CuO ₂ (CO ₃)	P 4 21 2	(90)	tetragonal primitive	83096
KCeSe ₄	P 4/n b m Z	(125)	tetragonal primitive	67656
NdLi ₂ Sb ₂	P 4/n m m Z	(129)	tetragonal primitive	36020
HgBa ₂ Ca ₂ Cu ₃ O ₈	P 4/m m m	(123)	tetragonal primitive	75730
HoBa ₂ Cu ₃ O ₆	P 4/m m m	(123)	tetragonal primitive	68047
LuBa ₂ Cu ₃ O ₆	P 4/m m m	(123)	tetragonal primitive	98113
NdBa ₂ Cu ₃ O ₆	P 4/m m m	(123)	tetragonal primitive	83074
Cs(Cu ₄ Se ₃)	P 4/m m m	(123)	tetragonal primitive	75196
KCu ₄ S ₃	P 4/m m m	(123)	tetragonal primitive	23336
KCu ₄ Se ₃	P 4/m m m	(123)	tetragonal primitive	280072

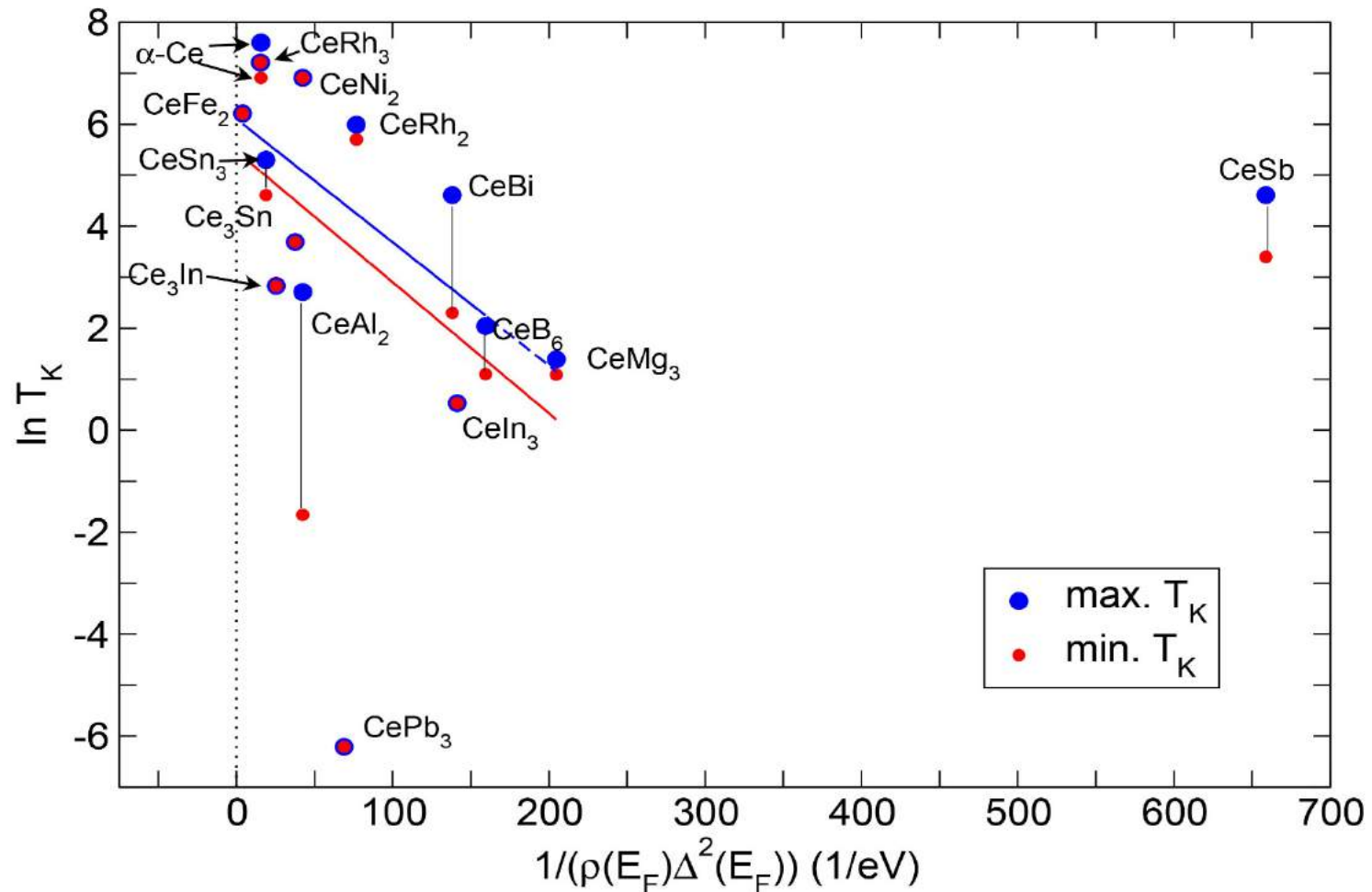
A data-base for Ce compounds



$$\Delta(E) = (E - H) - G_0^{-1}$$

Kondo temperatures

$$T_K = \alpha \exp \left[-\frac{2}{(2J+1)J_K \rho(E_F)} \right] \quad J_K = \frac{2\Delta^2(E_F)}{(E_f - E_F)}$$



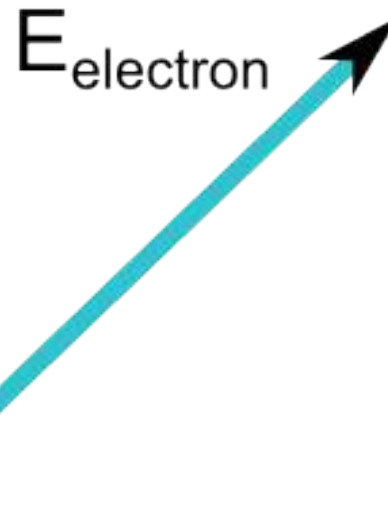
Some experience with DMFT



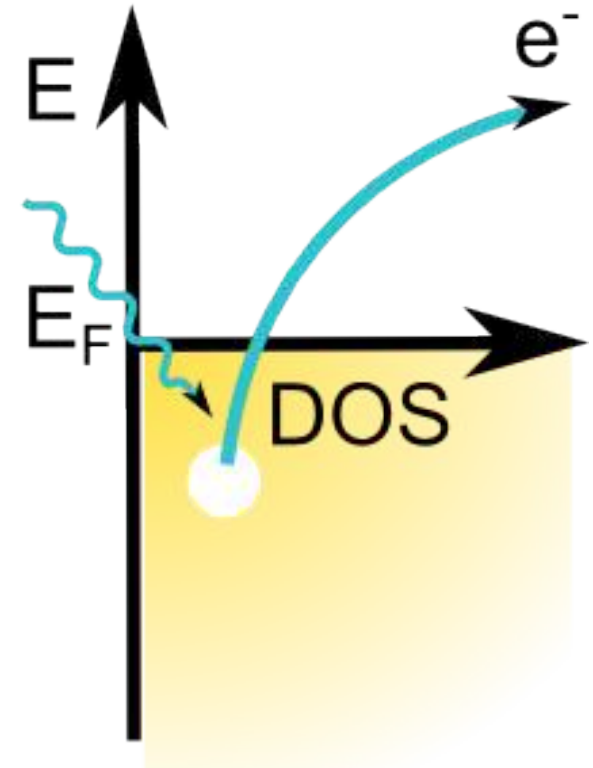
Spectra (XPS)

Photon beam

Emitted electron

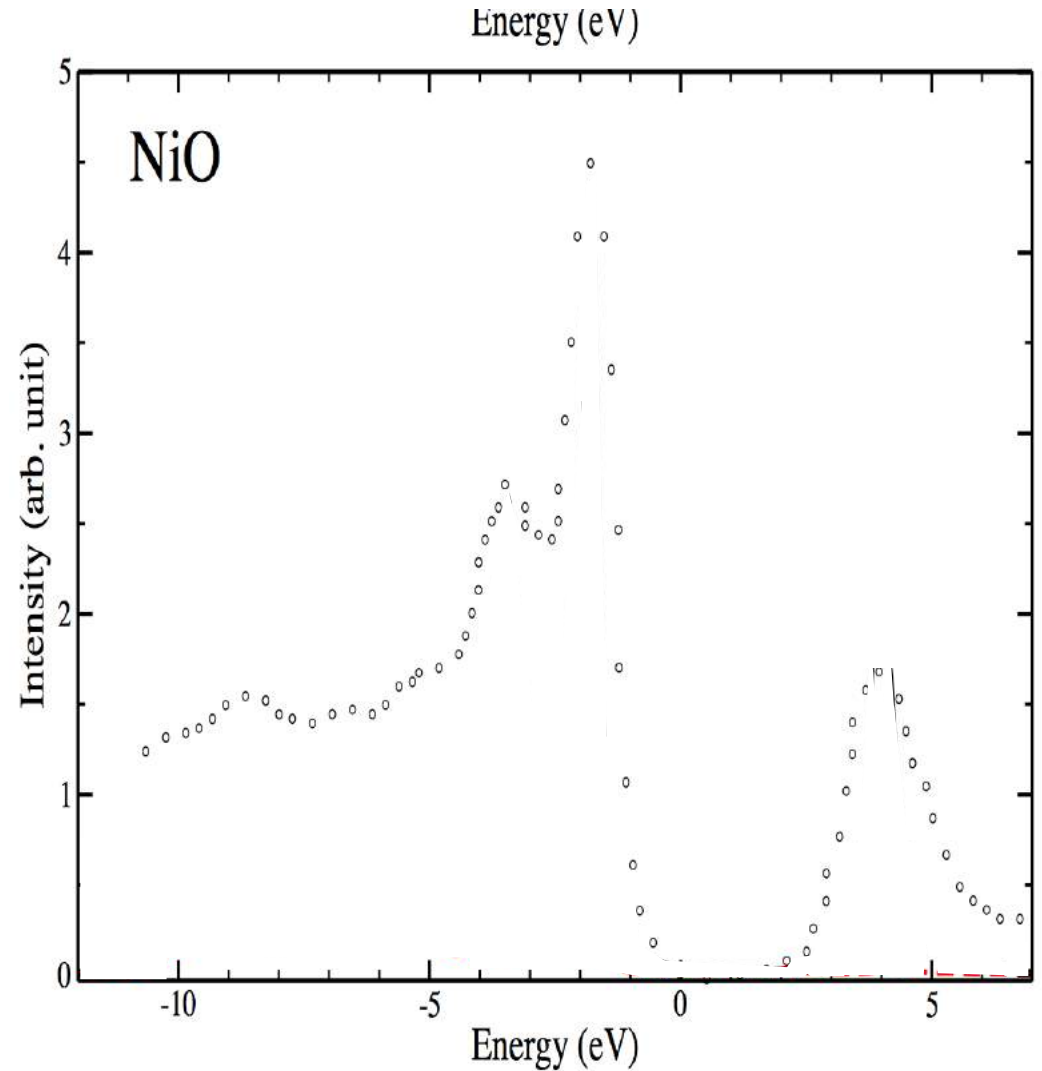
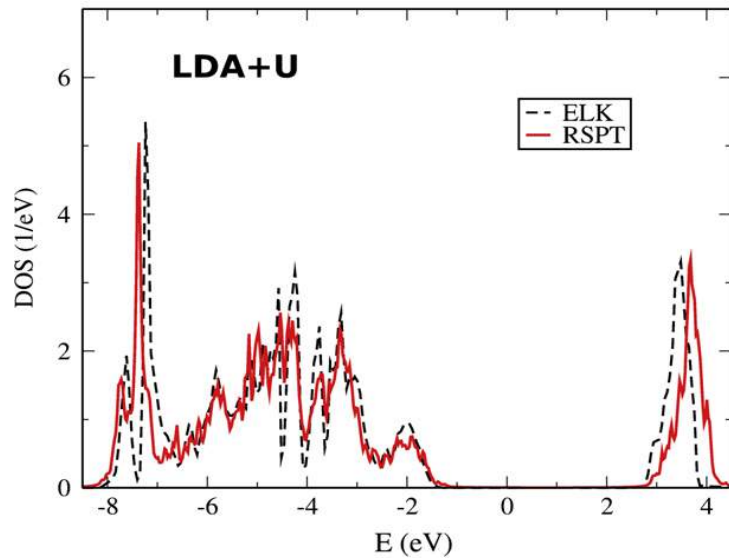
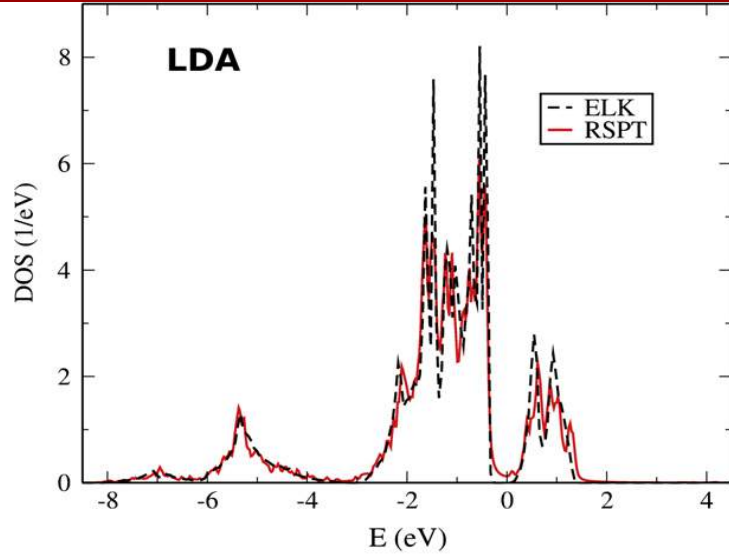


Sample





NiO - an example



Correlated basis

$$\hat{\mathbf{A}}_R \equiv \sum_{\xi, \xi'} |R, \xi\rangle \langle R, \xi| \sum_{\mathbf{k}} \hat{\mathbf{A}}_{\mathbf{k}} |R, \xi'\rangle \langle R, \xi'|$$

Two choices of $|R, \xi\rangle$, muffin-tin based and orthogonal:

i) MT

$$|\xi\rangle = i^l Y_{lm} \phi_l$$

ii) ORT

$$(\mathbf{H} - \epsilon \mathbf{O}) \mathbf{x} = 0$$

$$\mathbf{O} = \mathbf{L} \mathbf{L}^h$$

Cholesky decomposition gives

$$(\mathbf{L}^{-1} \mathbf{H} \mathbf{L}^{-h} - \epsilon \mathbf{1}) \mathbf{y} = 0$$

$$\mathbf{y} = \mathbf{L}^h \mathbf{x}$$



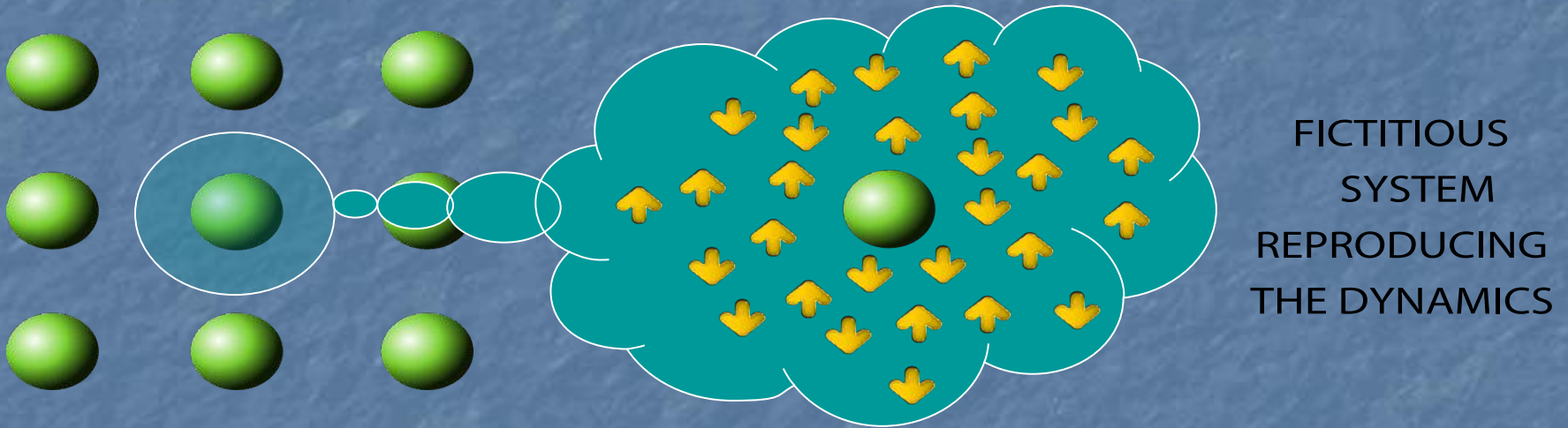
Dynamical mean field theory



$$H = H_{LDA} + \sum_R \sum_{\xi_1 \xi_2 \xi_3 \xi_4} U_{\xi_1 \xi_2 \xi_3 \xi_4} c_{R\xi_1}^\dagger c_{R\xi_2}^\dagger c_{R\xi_3} c_{R\xi_4}$$

U-matrix expressed in terms of Slater integrals

The Hubbard model is mapped into an Anderson Impurity Model

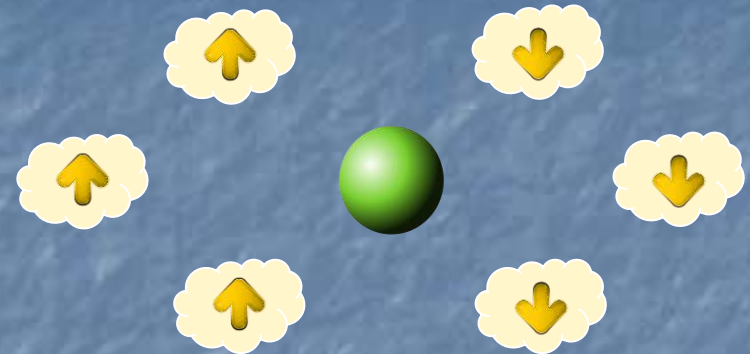


The mapping is made with the condition of preserving the local Green's function and is exact in the limit of infinite nearest neighbors

Exact Diagonalization Solver

The finite size problem can be solved exactly with a direct construction of all the accessible many-body states.

N=5 electrons in K=10 orbitals:



$$|\Psi_1^5\rangle = |1111100000\rangle,$$

$$|\Psi_2^5\rangle = |1111010000\rangle,$$

⋮

$$|\Psi_M^5\rangle = |0000011111\rangle.$$

M corresponds to $\binom{K}{N}$

Too large for standard computational resources!

Block diagonalization



up to 30 bath states!

Exact Diagonalization Solver

The finite size problem can be solved exactly with a direct construction of all the accessible many-body states.

N=5 electrons in K=10 orbitals:

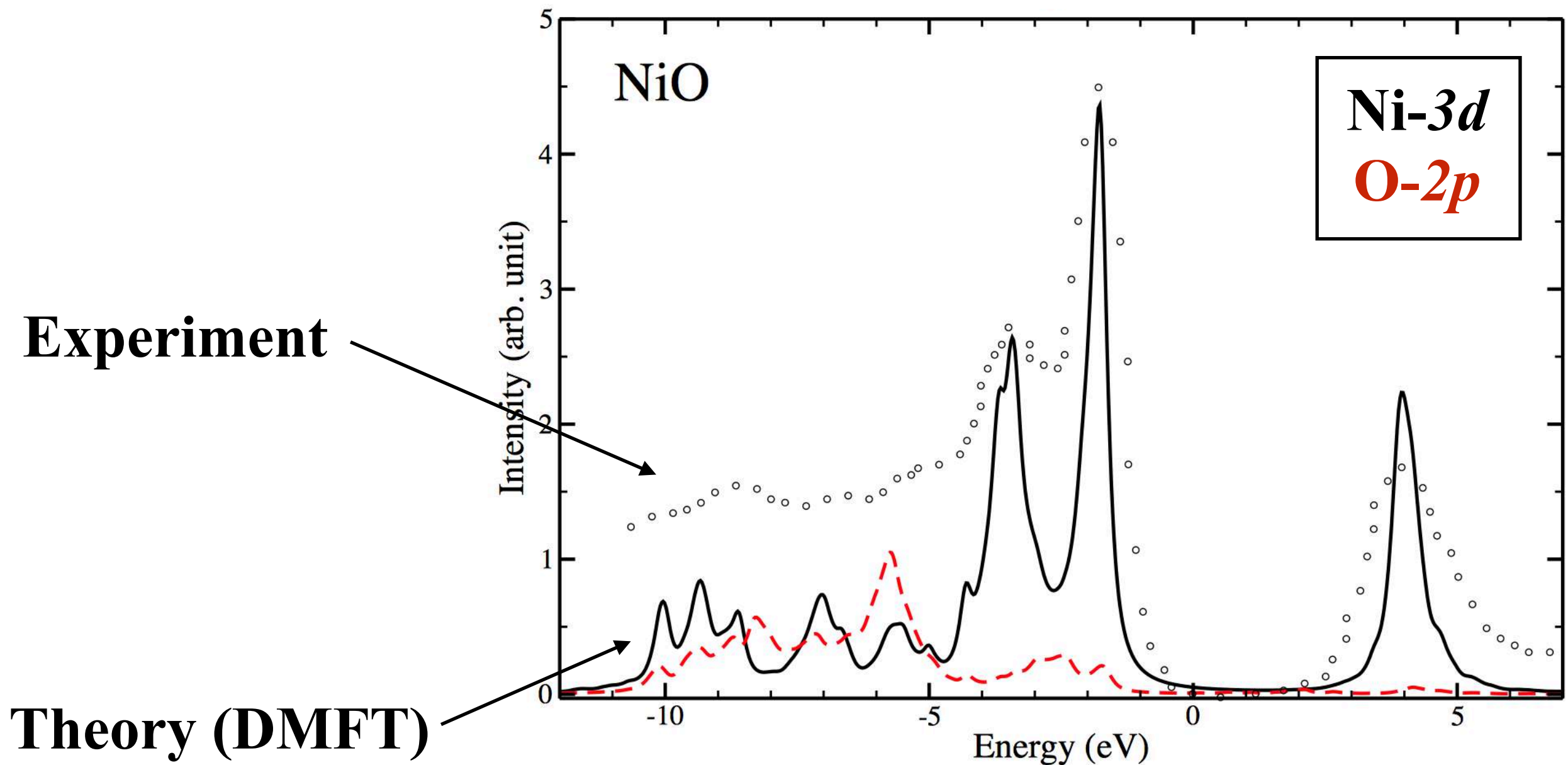


Once the many-body states have been determined, the one-particle Green's function can be obtained through the Lehmann representation

$$G^{\text{ED}}(i\omega)_{\xi_1\xi_2} = \frac{1}{Z} \sum_{\nu\mu} \frac{\langle \mu | \hat{c}_{\xi_1} | \nu \rangle \langle \nu | \hat{c}_{\xi_1}^\dagger | \mu \rangle}{i\omega + E_\mu - E_\nu} \left(e^{-\beta E_\mu} + e^{-\beta E_\nu} \right)$$

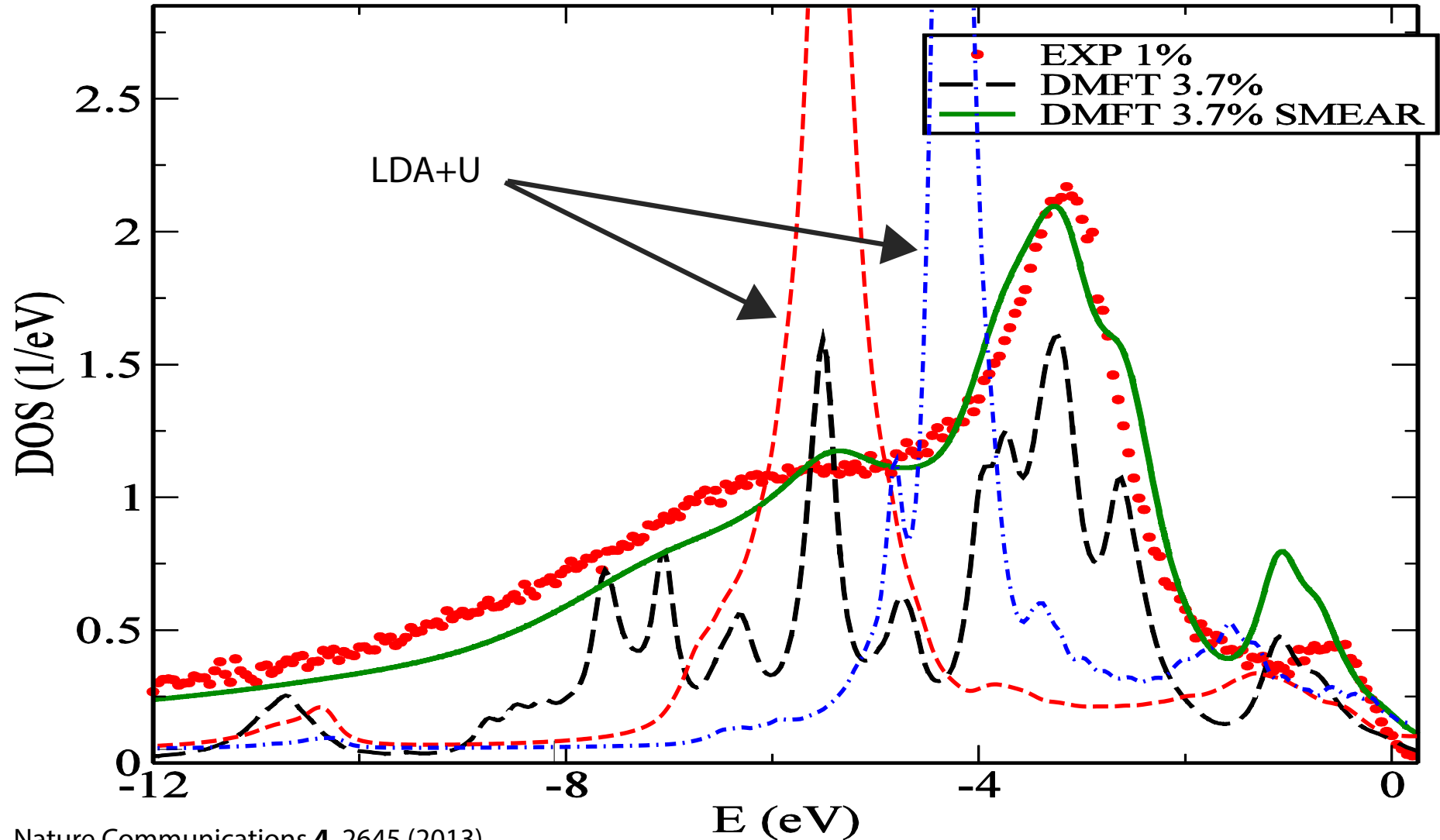
Paramagnetic NiO

DOS





Valence band of Mn-doped GaAs

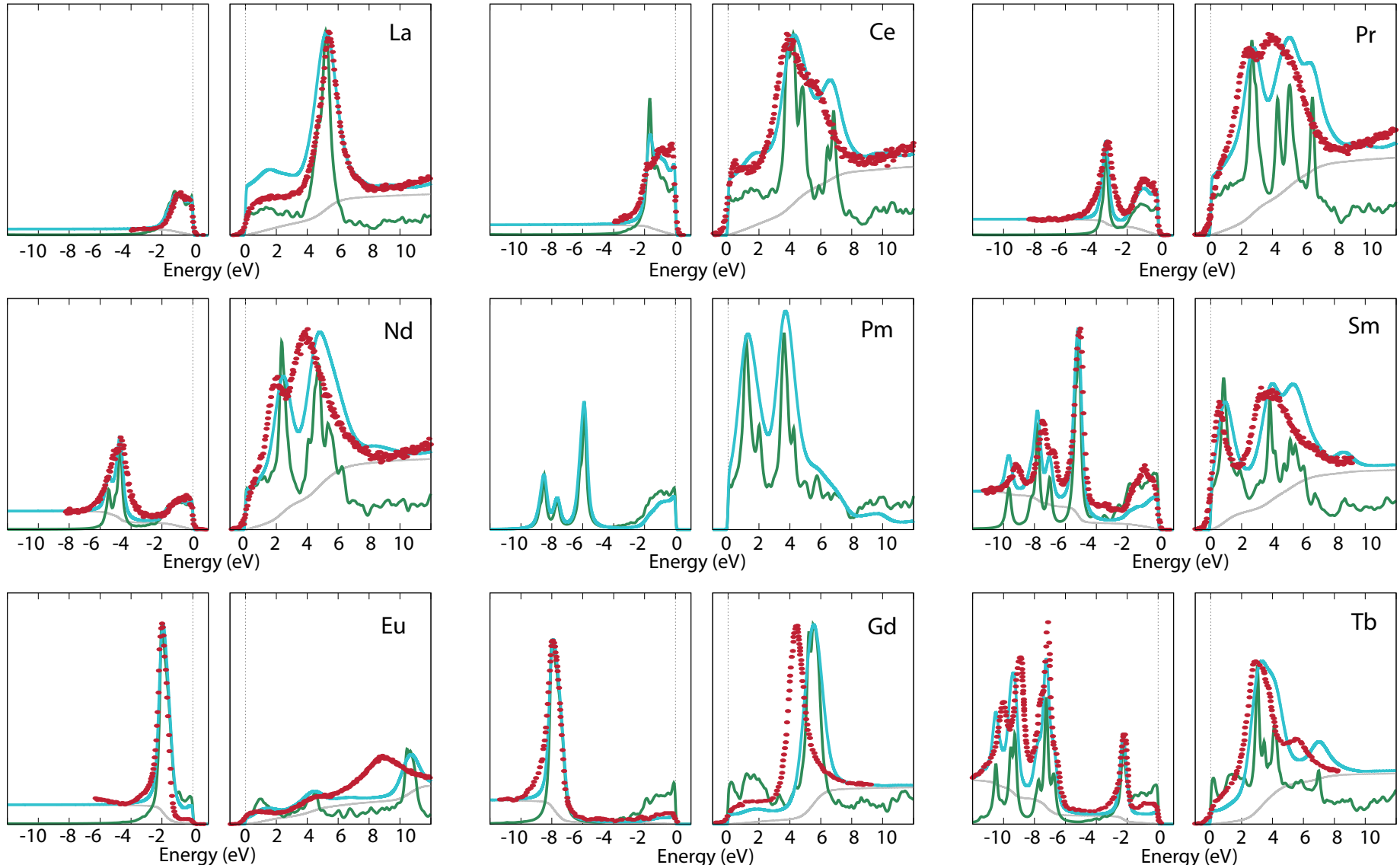




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Valence band spectra of rare-earths

(Loch et al. PRB 2016)

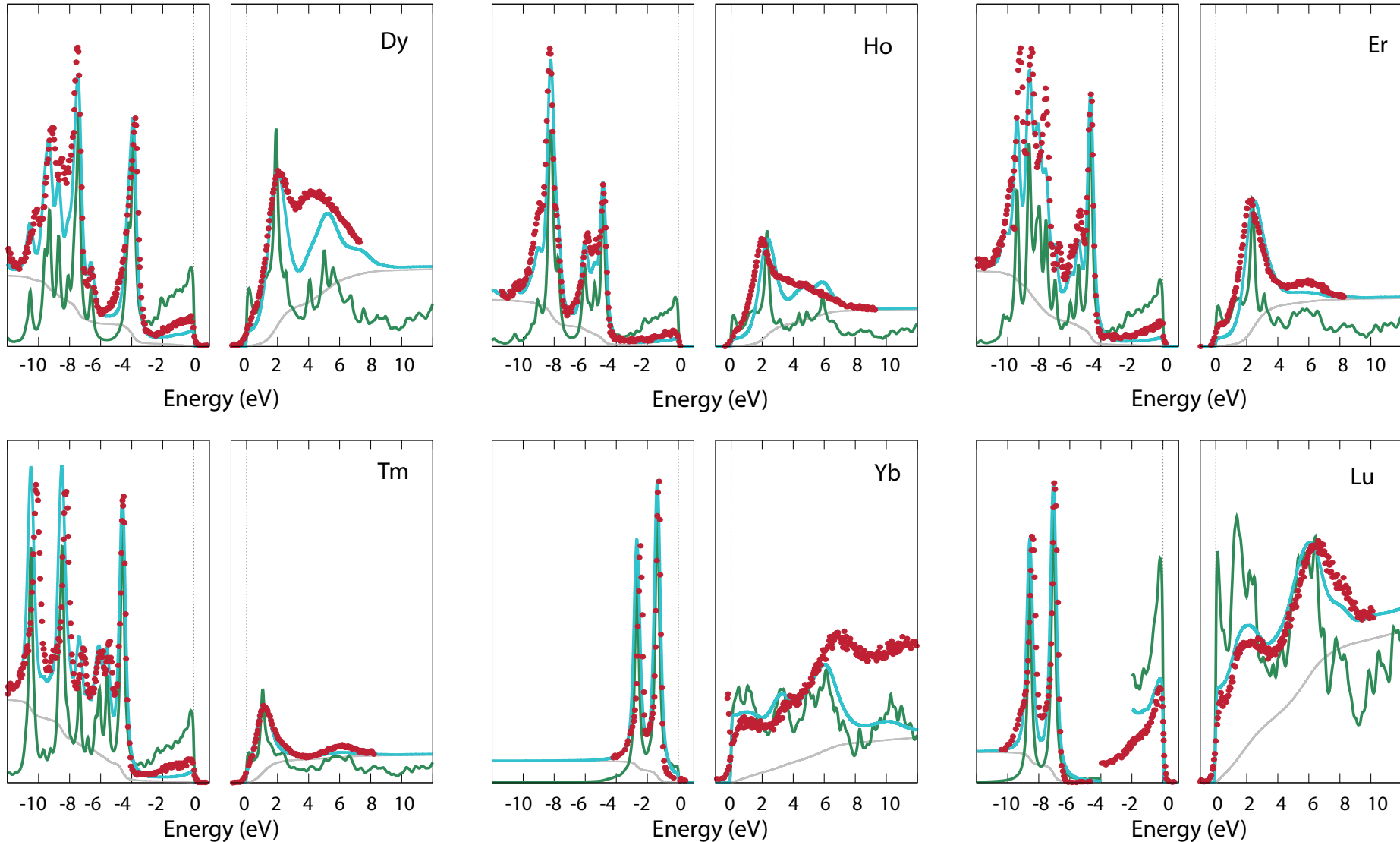




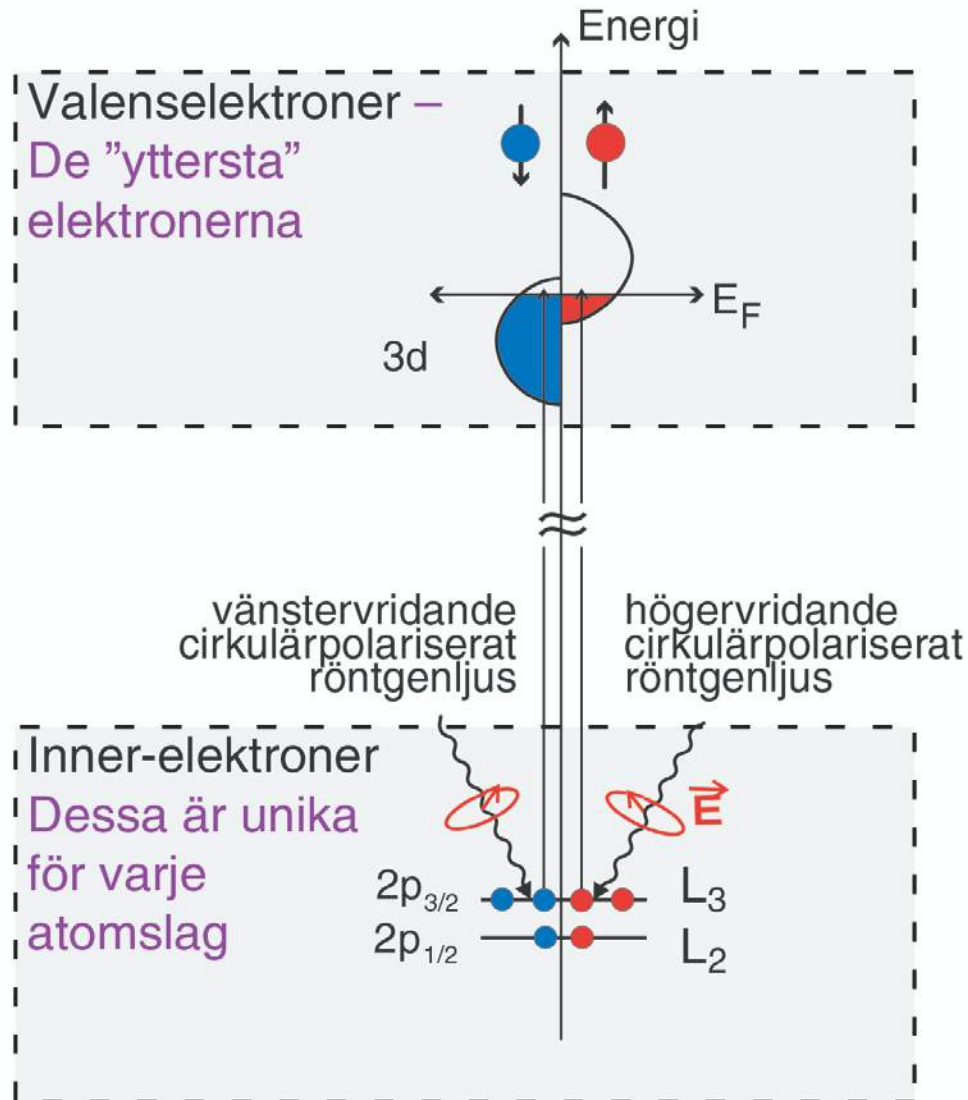
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Valence band spectra of rare-earths

(Loch et al. PRB 2016)



The XAS process





Hamiltonians

The initial state SIAM Hamiltonian:

$$\hat{H}_{init} = \sum_{ij} \varepsilon_{3d,ij} \hat{d}_i^\dagger \hat{d}_j + \sum_{ij} \varepsilon_{L,ij} \hat{L}_i^\dagger \hat{L}_j + \sum_{ij} v_{ij}^{3dL} \left[\hat{d}_i^\dagger \hat{L}_j + \hat{L}_j^\dagger \hat{d}_i \right] + \lambda_{3d} \sum_n \hat{I}_{3d,n}^+ \cdot \hat{\mathbf{s}}_{3d,n} + \sum_{ijkl} U_{ijkl}^{3d3d} \hat{d}_i^\dagger \hat{d}_j^\dagger \hat{d}_l \hat{d}_k$$

$\sum_{ij} \varepsilon_{3d,ij} \hat{d}_i^\dagger \hat{d}_j$ splitting of the 3d levels (10Dq)

$\sum_{ij} \varepsilon_{L,ij} \hat{L}_i^\dagger \hat{L}_j$ and of the ligand states following the symmetry of the 3d

$\sum_{ij} v_{ij}^{3dL} \left[\hat{d}_i^\dagger \hat{L}_j + \hat{L}_j^\dagger \hat{d}_i \right]$ coupling between ligands and d orbitals



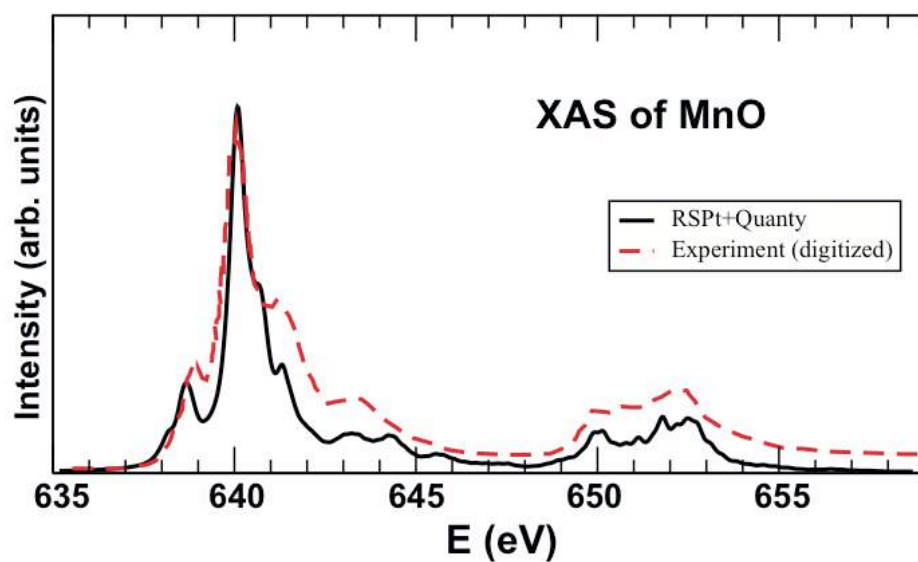
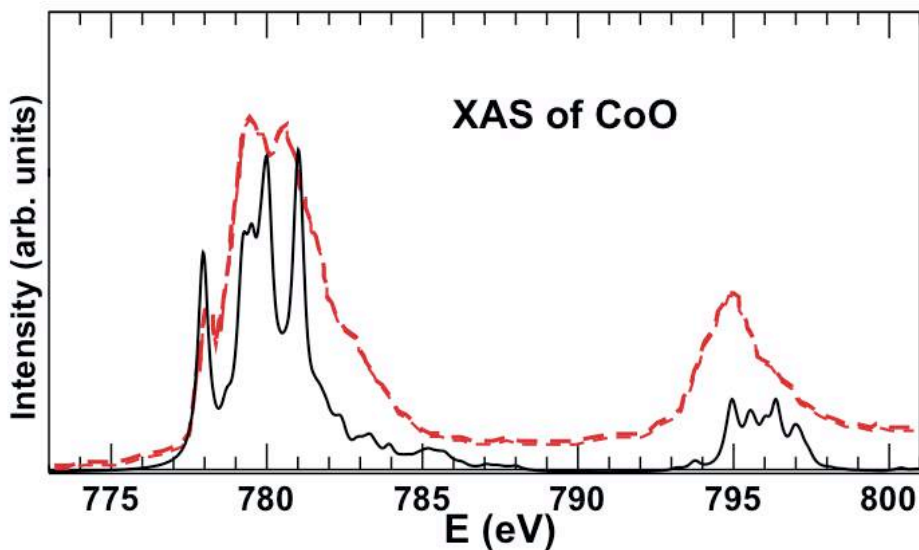
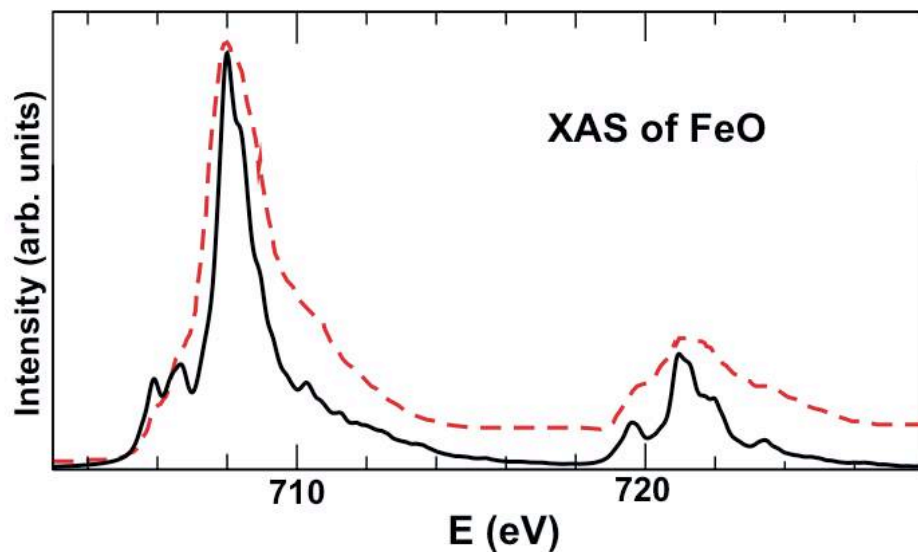
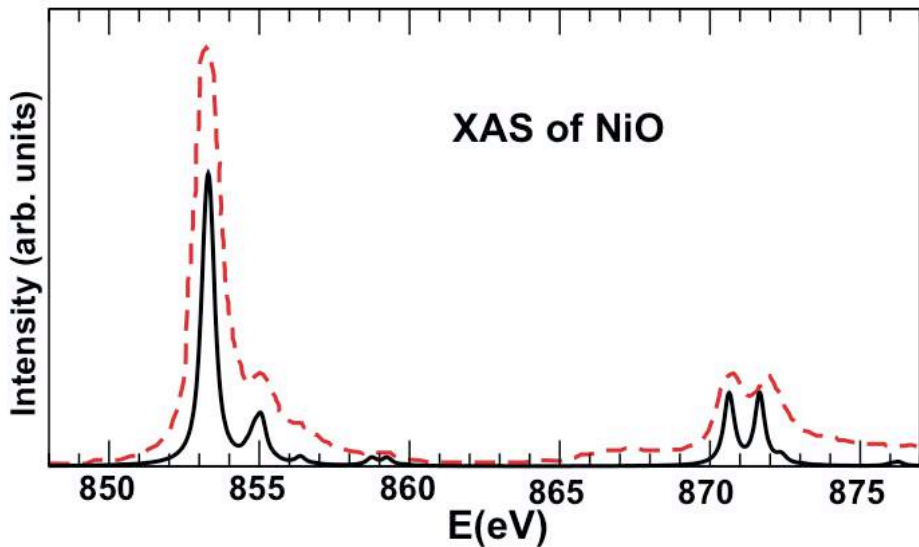
Final state

The final state XAS Hamiltonian accounts in addition for the 2p to 3d excitations (Quanty):

$$\hat{H}_{XAS} = \hat{H}_{init} + \sum_{ij} \varepsilon_{2p} \hat{p}_i^+ \hat{p}_j + \lambda_{2p} \sum_n \hat{I}_{2p,n}^+ \cdot \hat{s}_{2p,n} + \sum_{ijk} U_{ijk}^{2p3d} \hat{d}_i^+ \hat{p}_j^+ \hat{p}_l \hat{d}_k$$



Computed L-edge X-Ray Absorption Spectra

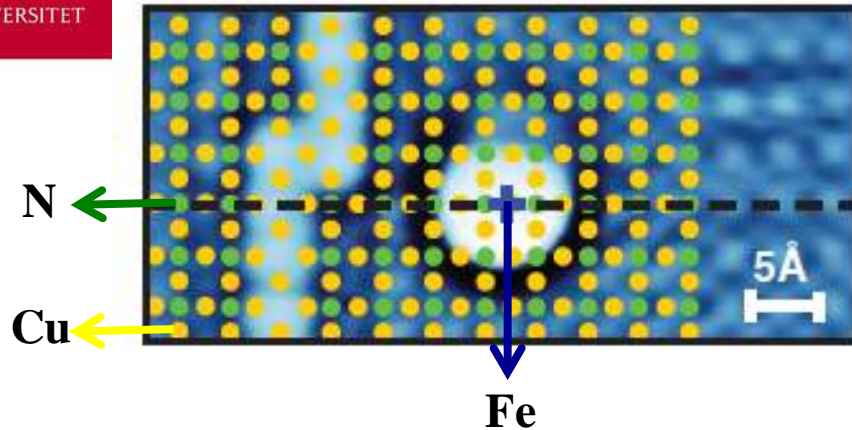


Experimental scenario: STM image

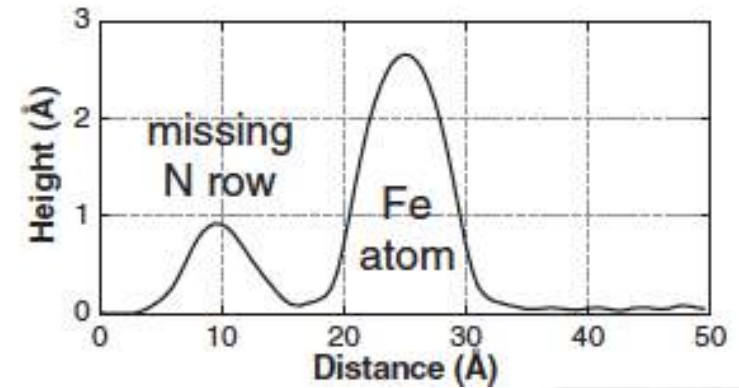


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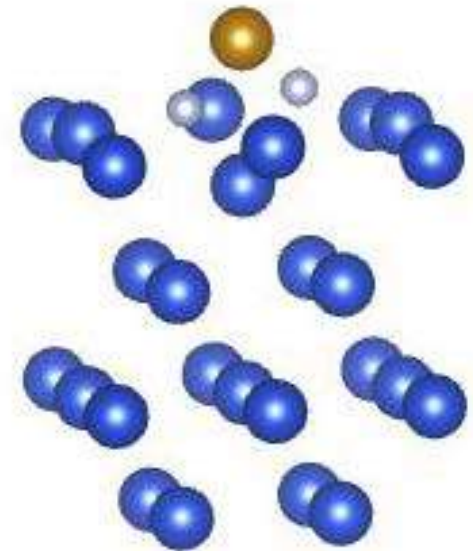
Constant-current topograph (10 mV, 0.5 nA)



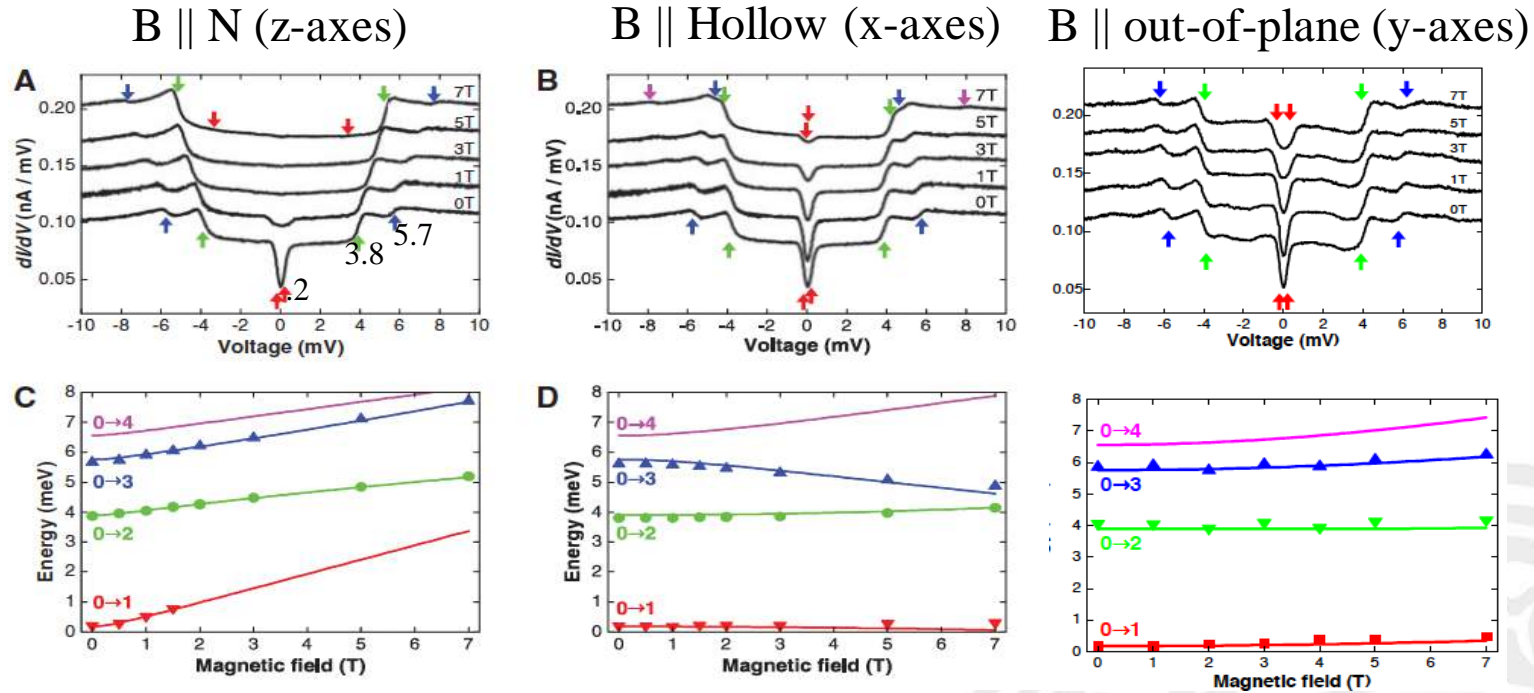
Cross section of the unfiltered topograph



- ❖ **Experimental system:** a single atomic layer of CuN to decouple the spin of the Fe atom from the underlying Cu (100) surface.
- ❖ **Cross section-** Fe atom has large apparent height of 2.6 Å.



Conduction spectra



- ❖ The changes in the excitation energies are markedly different when the magnetic field is applied in the three different directions- **evidence of strong magnetic anisotropy.**
- ❖ **Spin Hamiltonian:**
$$H = g\mu_B \mathbf{B} \cdot \mathbf{S} + D S_z^2 + E(S_x^2 - S_y^2)$$

Zeeman Axial Transverse magnetic anisotropy
- ❖ Using the spin of a free Fe atom ($S = 2$), a best fit of all of the excitations give $g = 2.11$, $D = -1.55$ meV, and $E = 0.31$ meV.
- ❖ **Primary anisotropy axis:** along the N direction-**indication of the importance of local molecular bonding for magneto crystalline anisotropy.**

Spin excitation spectra for B=0



Spin Hamiltonian $H = D S_z^2 + E(S_x^2 - S_y^2) = D S_z^2 + E/2(S_+^2 + S_-^2)$
 When $S = 2, m_s = -2, -1, 0, +1, +2$

For experimental $D = -1.55, E = 0.31$

The eigen states are

$$|X0\rangle = -0.6973 |2\rangle + 0.1660 |0\rangle - 0.6973 |-2\rangle$$

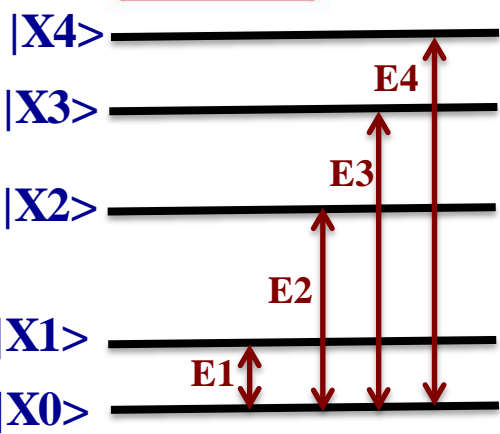
$$|X1\rangle = -0.7071 |2\rangle - 0.7071 |-2\rangle$$

$$|X2\rangle = 0.7071 |1\rangle - 0.7071 |-1\rangle$$

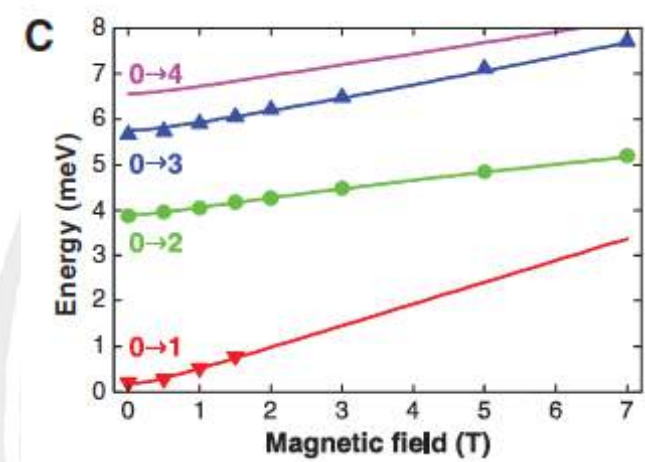
$$|X3\rangle = 0.7071 |1\rangle + 0.7071 |-1\rangle$$

$$|X4\rangle = -0.1174 |2\rangle - 0.9860 |0\rangle - 0.1174 |-2\rangle$$

$$\begin{pmatrix} 4D & 0 & \sqrt{6}E & 0 & 0 \\ 0 & D & 0 & 3E & 0 \\ \sqrt{6}E & 0 & 0 & 0 & \sqrt{6}E \\ 0 & 3E & 0 & D & 0 \\ 0 & 0 & \sqrt{6}E & 0 & 4D \end{pmatrix}$$



	E1	E2	E3	E4
Exp	0.18	3.90	5.76	6.56
LSDA	0.09	0.99	1.71	1.87
LSDA+U	0.10	1.06	1.84	2.00
HIA (FLL)	0.36	1.46	1.70	2.41
ED	0.49	5.32	6.34	7.68



STEINER



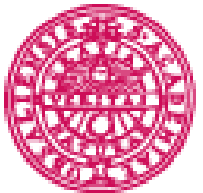
Atomistic Spin Dynamics

Foundations and Applications

Dirk Essler, Anders Hagman,
Lars Hilgert, John Hultsch



Magnetic properties



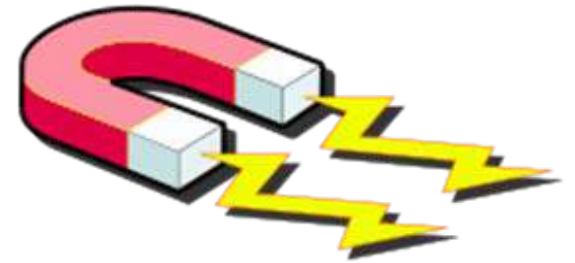
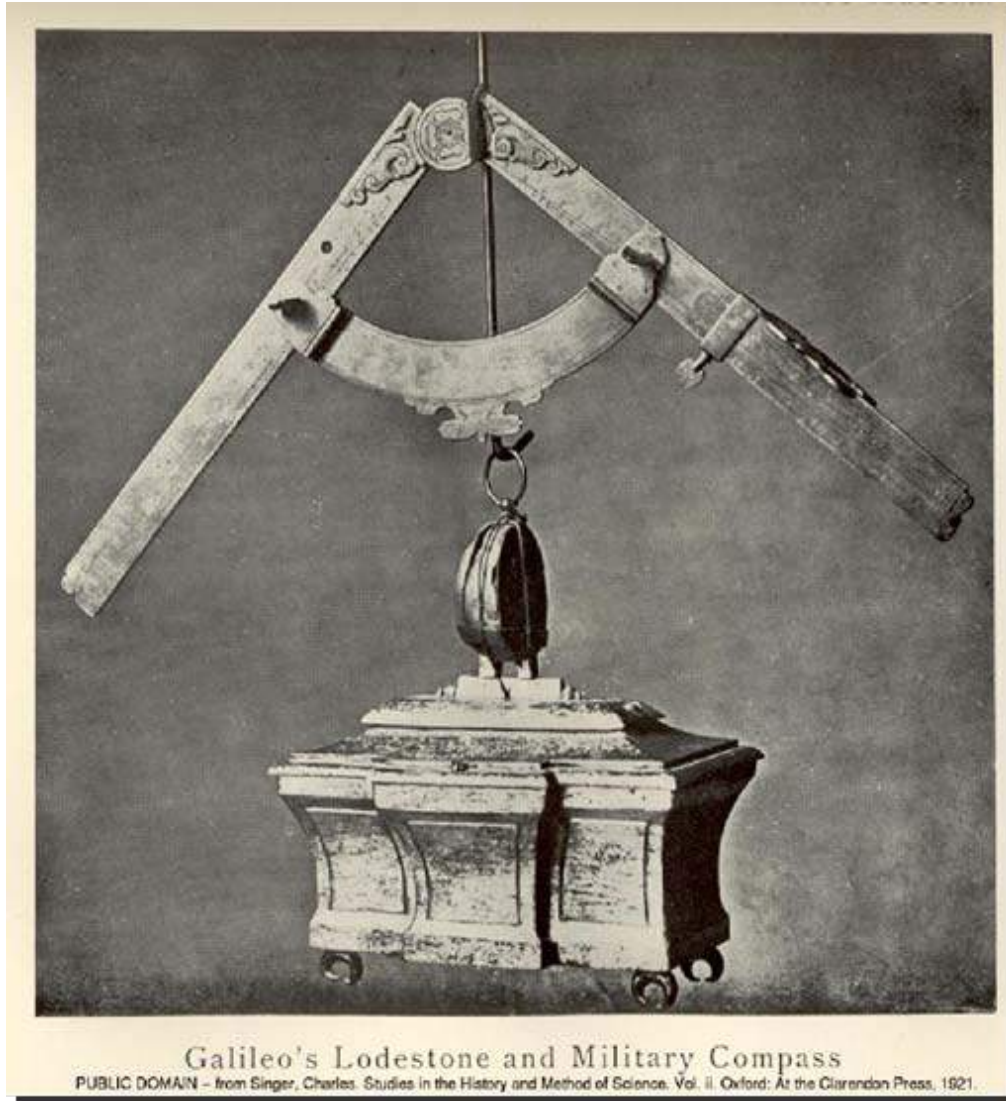
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Magnetism i historien



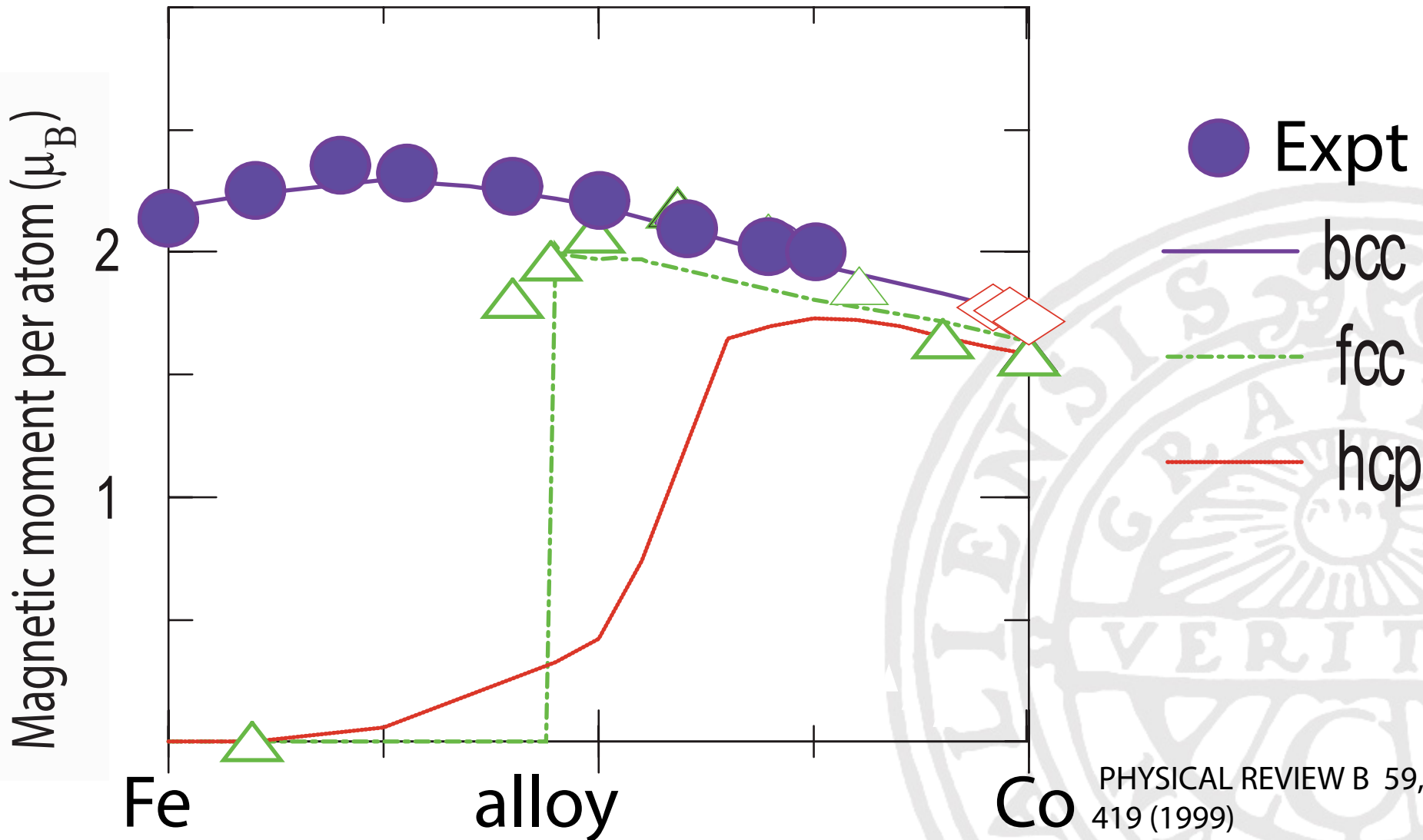
Galileo's compass

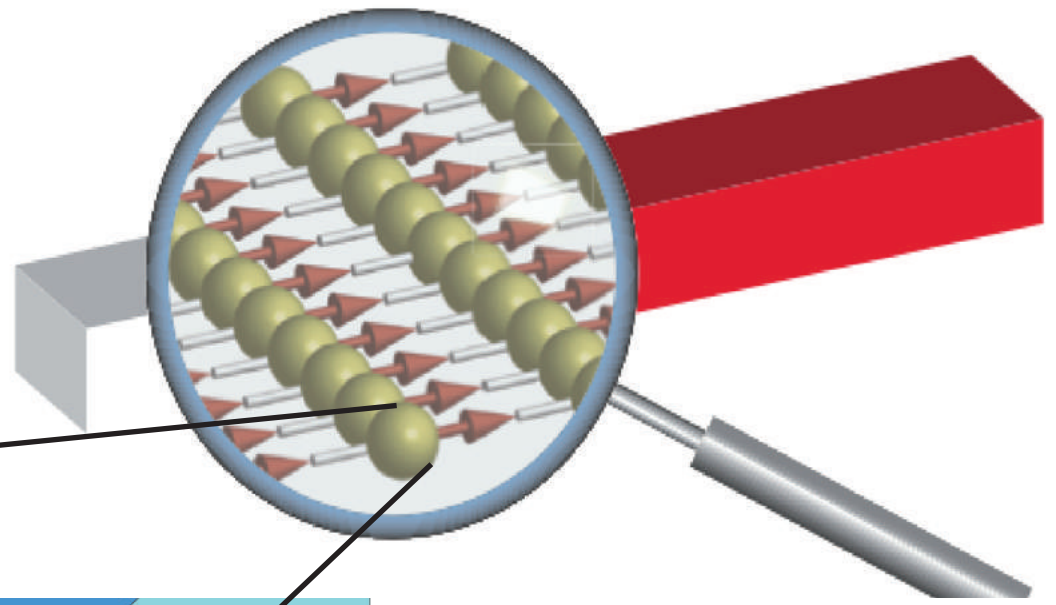
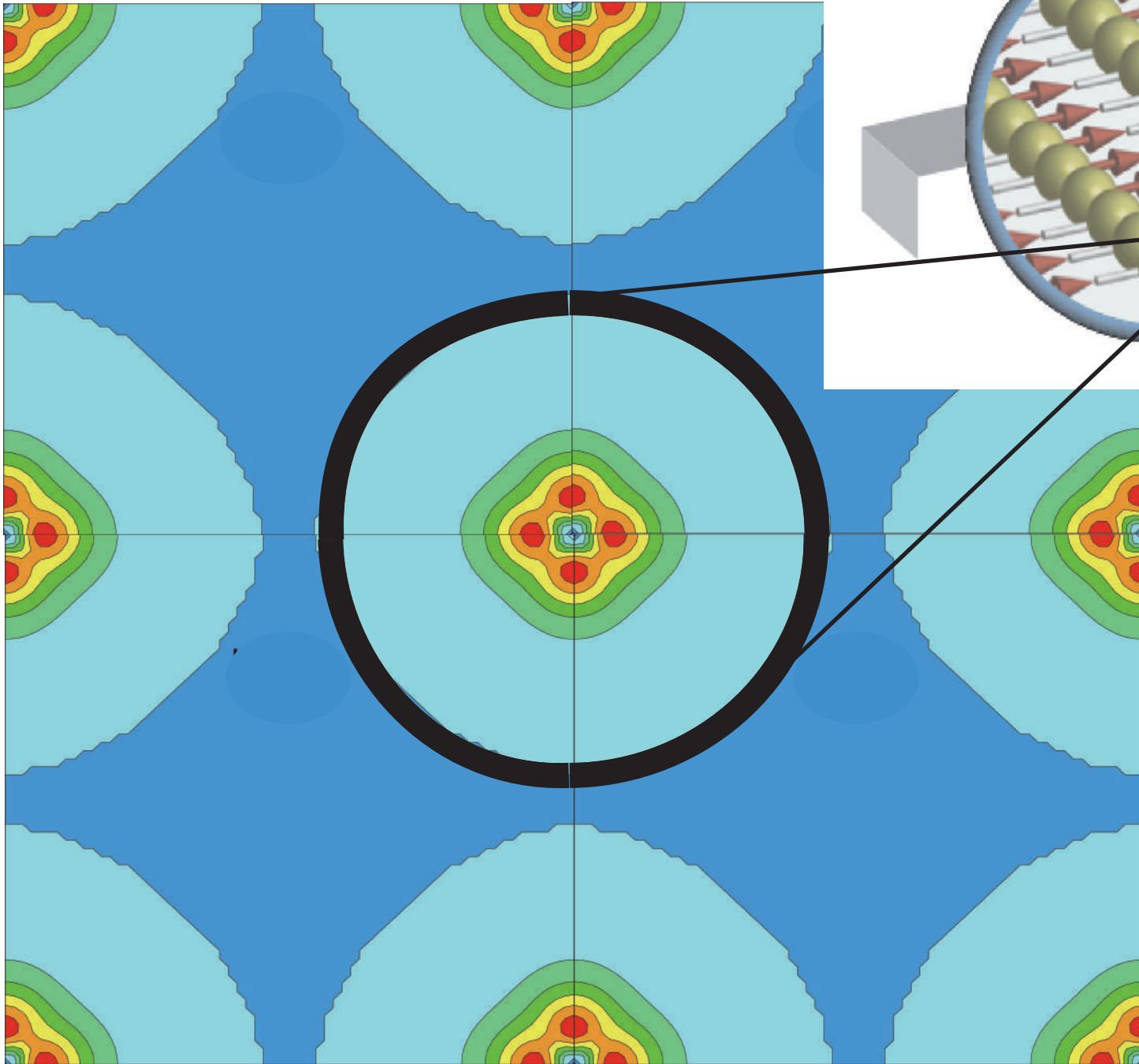


- Magnetic Interaction lead to mechanical forces and torque



Spin moments of Fe-Co alloys







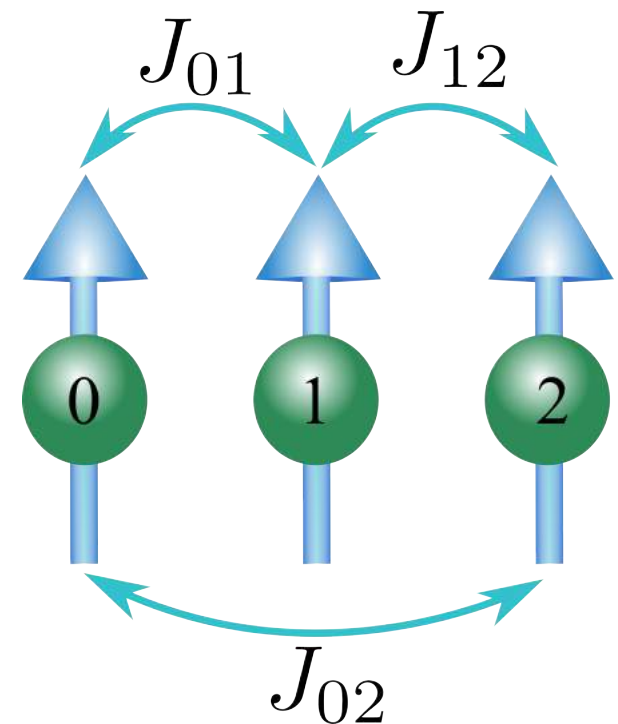
Heisenberg Model



- A picture of localised spins
- Magnetization is a “classical” vector, assigned to each site

$$\hat{H} = - \sum_{i \neq j} J_{ij} \cdot (\vec{e}_i \cdot \vec{e}_j)$$

$$\text{With } \vec{e}_i = \frac{\vec{S}_i}{|\vec{S}_i|}$$





Exchange parameters

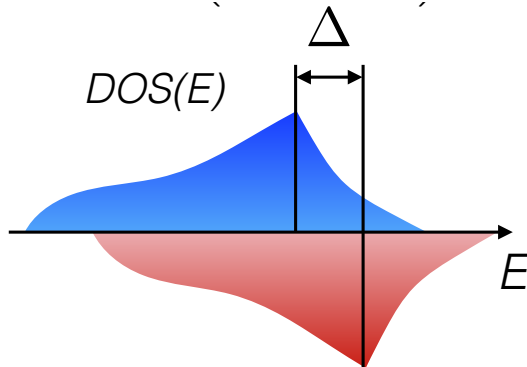


Expansion of the Hamiltonian in $\delta\vec{\theta}_i$ and $\delta\vec{\theta}_j$ gives

$$J_{ij} = \frac{-1}{4\pi} \int_{-\infty}^{E_F} \delta\epsilon \text{Tr}_m \left[\Delta_i \cdot G_{ij}^{\uparrow}(\epsilon) \cdot \Delta_j \cdot G_{ij}^{\downarrow}(\epsilon) \right]$$

Local exchange field

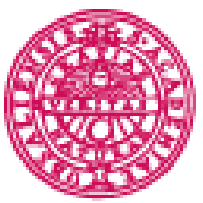
$$\Delta_i = (\hat{H}_i^{\uparrow} - \hat{H}_i^{\downarrow})$$



Inter-site Greens function

$$G_{ij}^{\sigma} = \langle i | \hat{G}(z) | j \rangle = \left\langle i \left| \frac{1}{z - \hat{H}^{\sigma}} \right| j \right\rangle$$

Lichtenstein *et al* JMMM **67** 65 (1987),
Katsnelson *et al* PRB **61** 8906 (2000),
Kvashnin *et al* PRB **91** 125133 (2015)



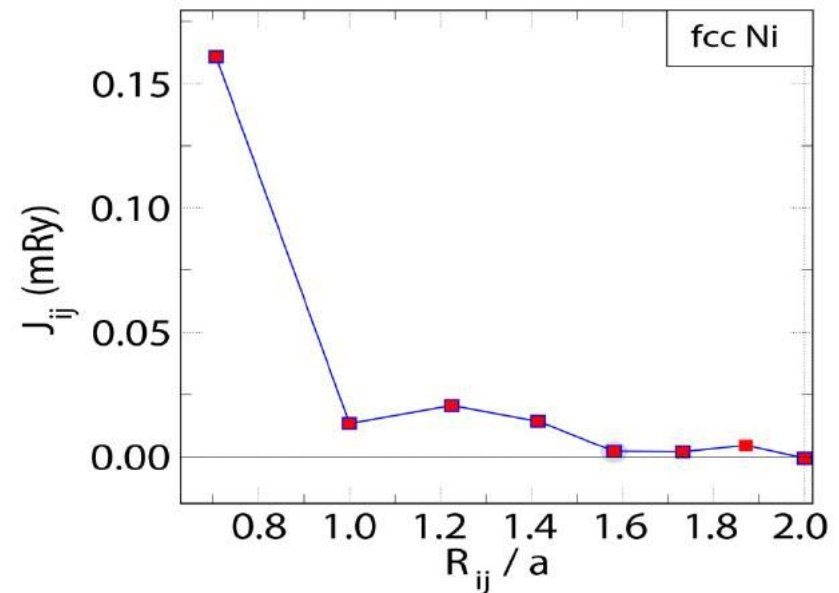
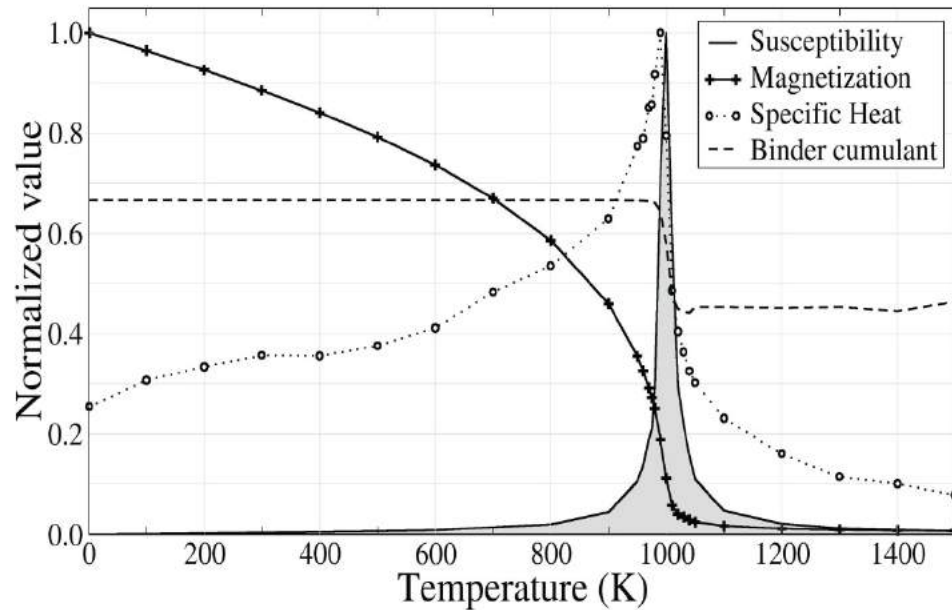
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Heisenberg spin Hamiltonian

$$H_{spin} = - \sum_{\langle ij \rangle} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j$$

$$H_{spin} = -J \sum_{\langle ij \rangle} \mathbf{S}_i \cdot \mathbf{S}_j$$

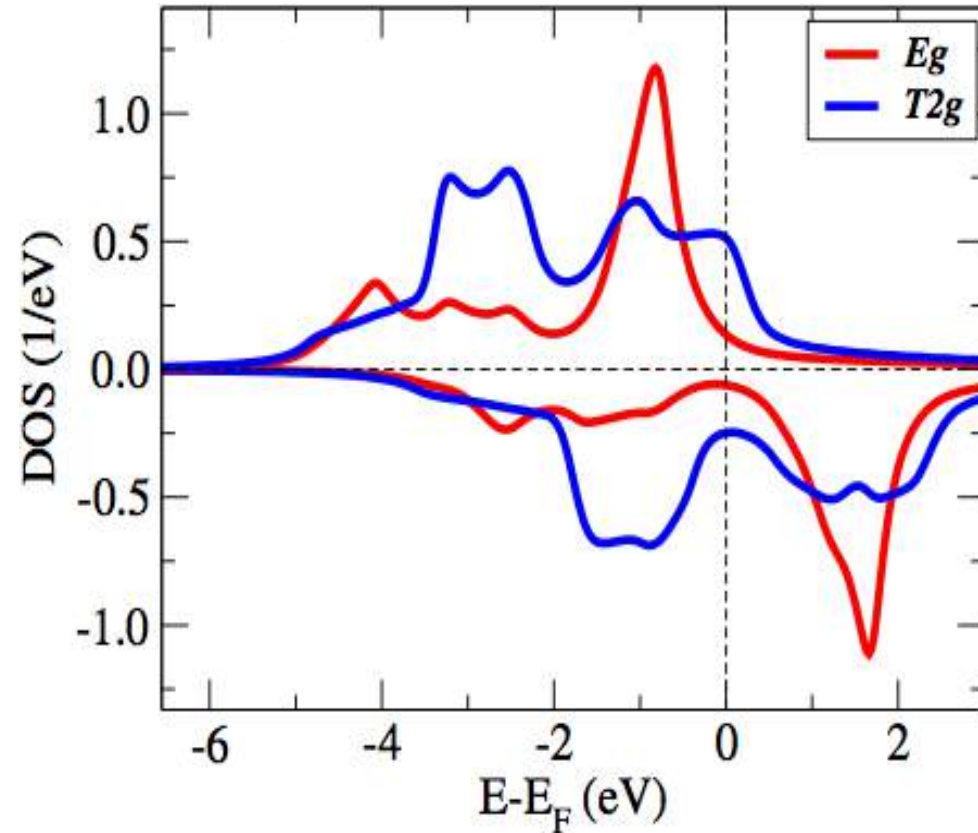
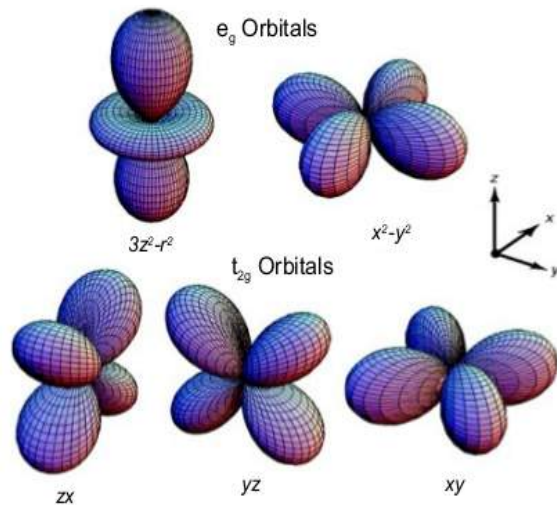
M vs T for bcc Fe





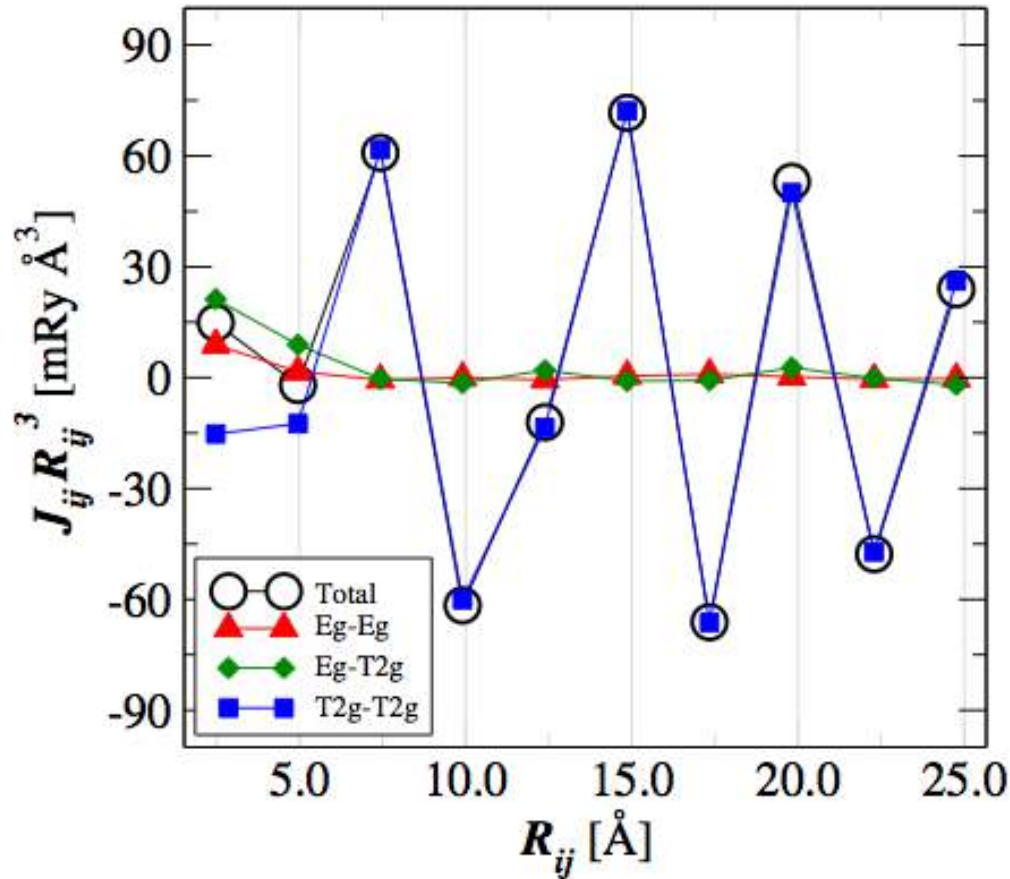
Symmetry resolved interactions

E_g and T_{2g} orbitals in cubic environment



bcc Fe

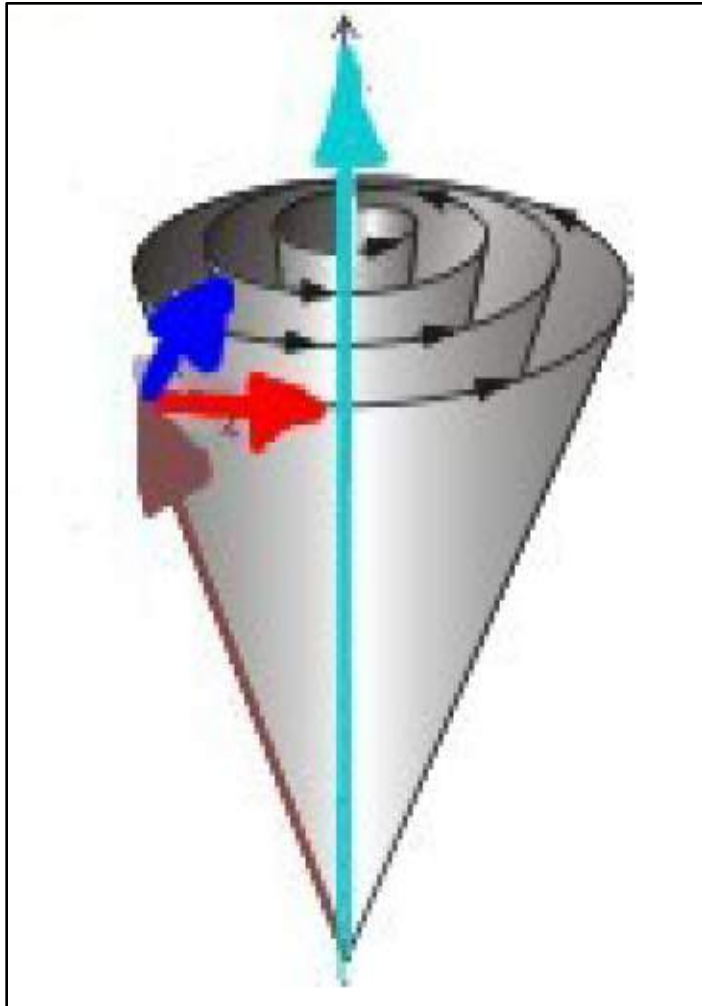
Interactions along the NN direction — (111)



Long-ranged J_{ij} 's are completely defined by T_{2g} states



Atomistic Landau-Lifshitz equation



$$\frac{d\mathbf{m}_i}{dt} = -\gamma\mathbf{m}_i \times \mathbf{B}_i - \gamma\frac{\alpha}{m_i}[\mathbf{m}_i \times [\mathbf{m}_i \times \mathbf{B}_i]]$$

Precession Damping

Energy dissipation

$$\frac{dE}{dt} = \frac{dE}{d\mathbf{m}} \cdot \frac{d\mathbf{m}}{dt} = \mathbf{B} \cdot \frac{d\mathbf{m}}{dt}$$

$$\mathbf{B} \cdot \frac{d\mathbf{m}}{dt} \propto 0 + \alpha$$

$$\frac{dE}{dt} \longleftrightarrow \alpha$$



Time scales

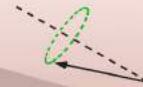
Lifetime of magnetic data storage media

http://www.cbir.org/pubs/reports/pub54/4life_expectancy.html
<http://www.apple.com>



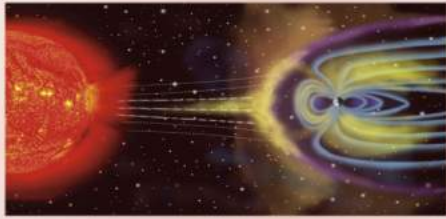
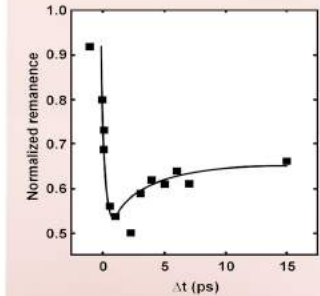
Magnetization precession

$$\frac{d\mathbf{m}}{dt} = [\mathbf{m} \times \mathbf{H}] + \frac{\gamma}{m} [\mathbf{m} \times \frac{d\mathbf{m}}{dt}]$$
$$T \approx 2\pi \frac{m_e}{eB} \approx 36ps \quad B = 1T$$



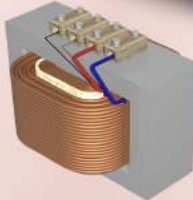
Demagnetization by fs Laser

E Beaupaire et. al, PRL, 76, 4250 (1996)



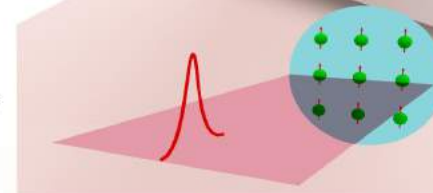
Geomagnetic reversal

http://en.wikipedia.org/wiki/Earth's_magnetic_field



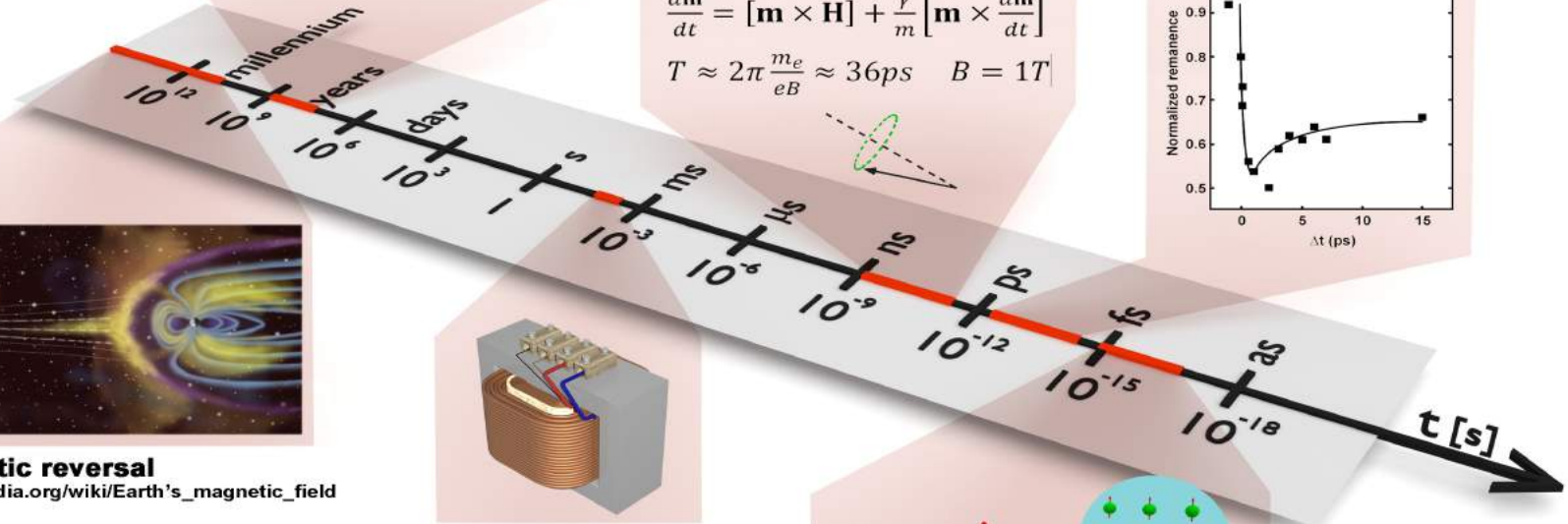
AC Transformer

<http://en.wikipedia.org/wiki/Transformer>



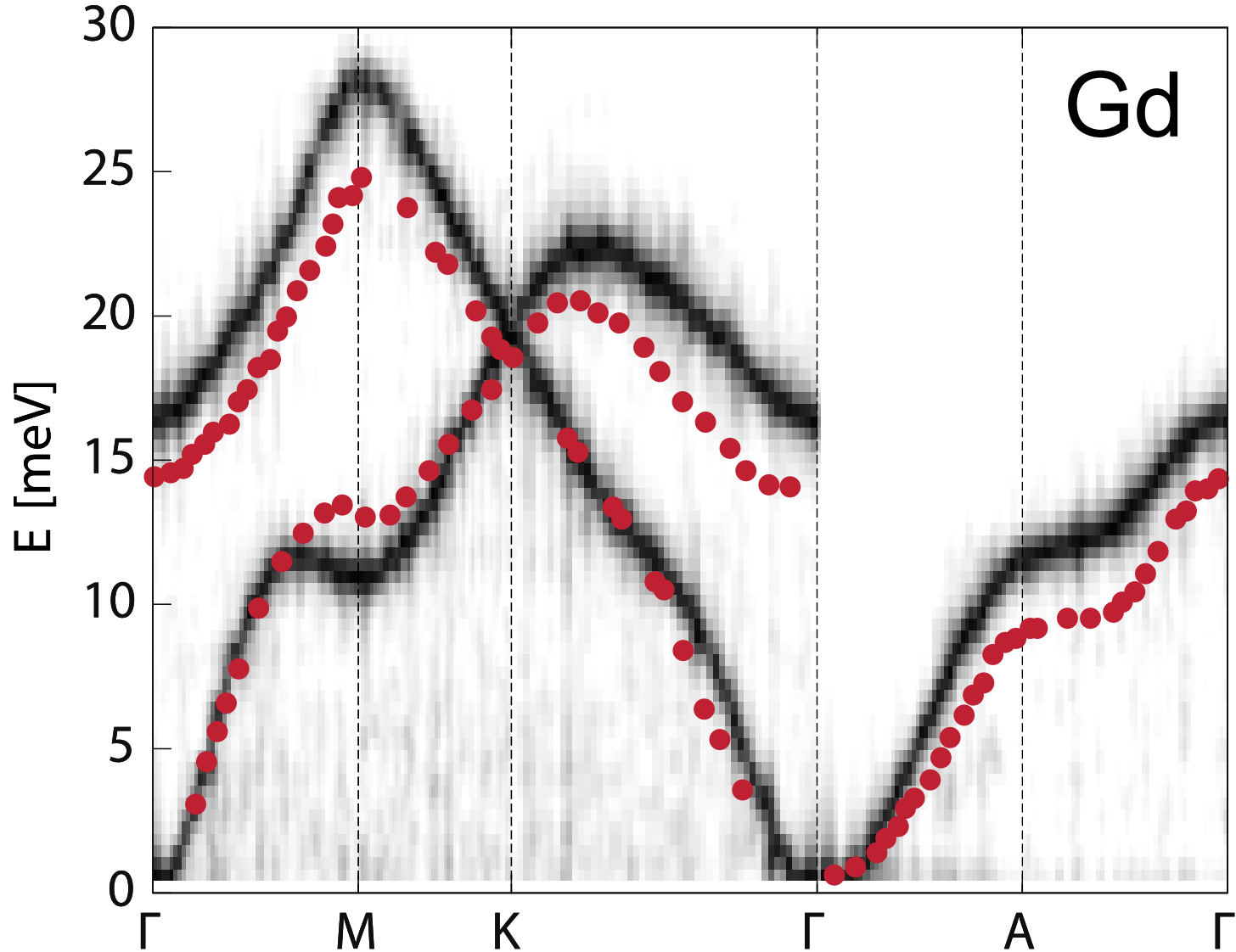
Coherent interaction between light and magnetization

Bigot et. al, Nat Phy vol 5(7), 515 (2009)

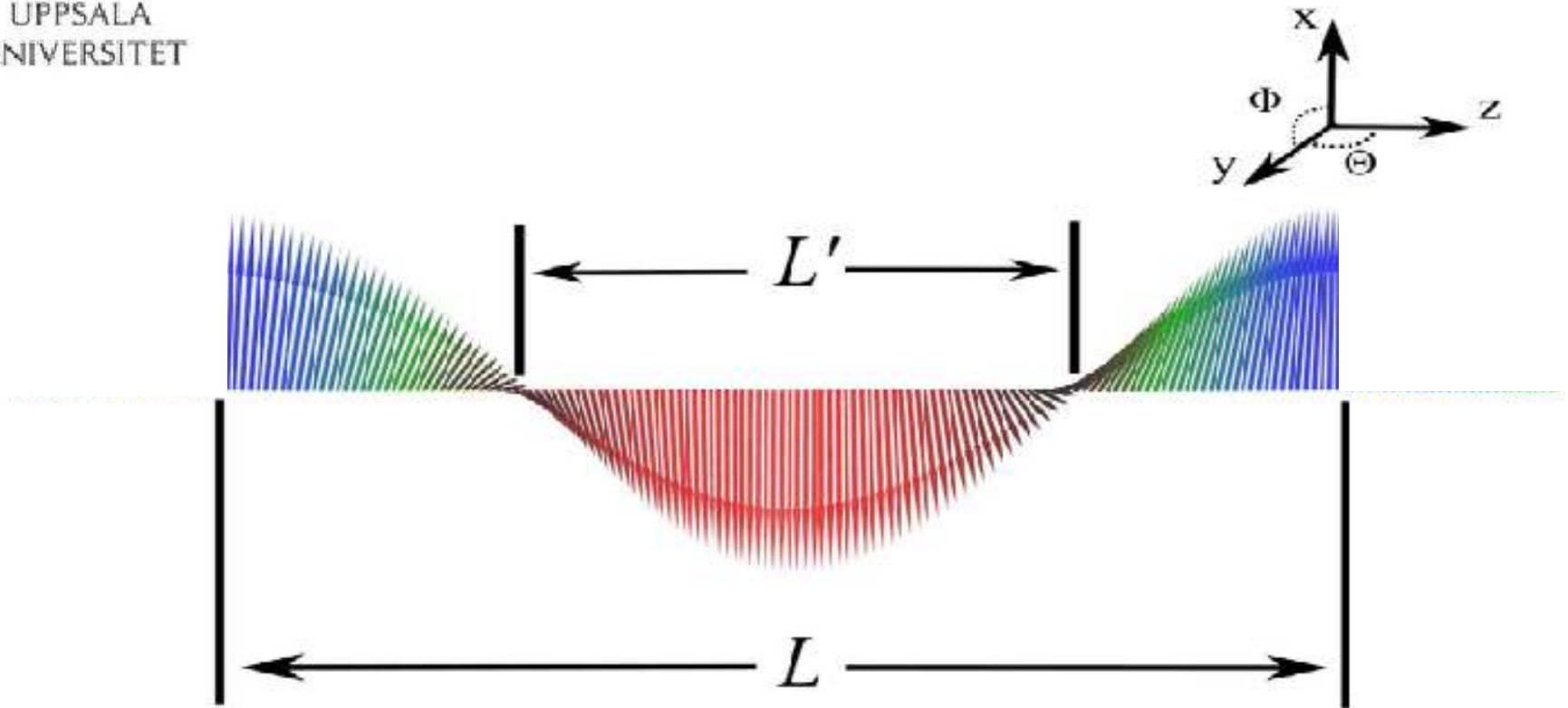




Spin wave dispersion spectrum



Solitons



A chiral knot of energy, being the solution to the sine-Gordon equation:

$$\Phi_{tt} - \Phi_{zz} + \sin\Phi = 0$$

Magnonics

