

“Enseigner la recherche en train de se faire”



*Chaire de
Physique de la Matière Condensée*

**CORRELATIONS ELECTRONIQUES ET TRANSPORT DANS LES
OXYDES 4d ET COMPOSES SUPRACONDUCTEURS DU FER :
HUND PLUTOT QUE MOTT, DRUDE PLUTOT QUE LANDAU**

**Les mercredis dans l'amphithéâtre Maurice Halbwachs
11, place Marcelin Berthelot 75005 Paris
Cours à 14h30 - Séminaire à 15h45**

Antoine Georges

Cycle 2011-2012
2/05/2012 – 13/06/2012
(Pas de séance le 23/05)

Séance du 16 mai 2012

- Cours à 14h30 –

*Etat métallique des ruthenates et composés supraconducteurs du fer:
rôle du couplage de Hund.*

- Séminaire : 15h45 –

Silke BIERMANN, CPHT Ecole Polytechnique

*Hubbard and Hund: Dynamical Screening Effects in Iron Pnictide
Compounds from First Principles*

- Séminaire: 16h45

Luca de' Medici, LPS Orsay

*Orbital-Selective Mott Transitions and their relevance
to Fe-superconductors*

Pas de séance le 23 mai

Reprise le 30 mai (Transport)

Séminaires du 30 mai: F. Rullier-Albenque, N. Barisic

Recall: a model study: 3 degenerate bands
w/ same bandwidth 2D
occupied by N electrons per site

$$\begin{aligned}
 H_{\text{int}} &= U \sum_m n_{m\uparrow} n_{m\downarrow} + \\
 &+ \sum_{m < n, \sigma} [(U - 2J) n_{m\sigma} n_{n\sigma} + (U - 3J) n_{m\sigma} n_{n\sigma}] \\
 &- J \sum_{m < n} [d_{m\uparrow}^\dagger d_{m\downarrow} d_{n\downarrow}^\dagger d_{n\uparrow} + d_{m\uparrow}^\dagger d_{m\downarrow}^\dagger d_{n\uparrow} d_{n\downarrow} + \text{h.c.}] \\
 &= (U - 3J) \frac{\hat{N}(\hat{N} - 1)}{2} + \frac{5}{2} J \hat{N} - 2J \vec{S}^2 - \frac{1}{2} J \vec{T}^2
 \end{aligned}$$

P.Werner et al. PRL 101 (2008) 166405

L de'Medici, J.Mravlje, AG PRL 107 (2011) 256401

studied with : DMFT

Dependence of Mott U_c on J , in hindsight

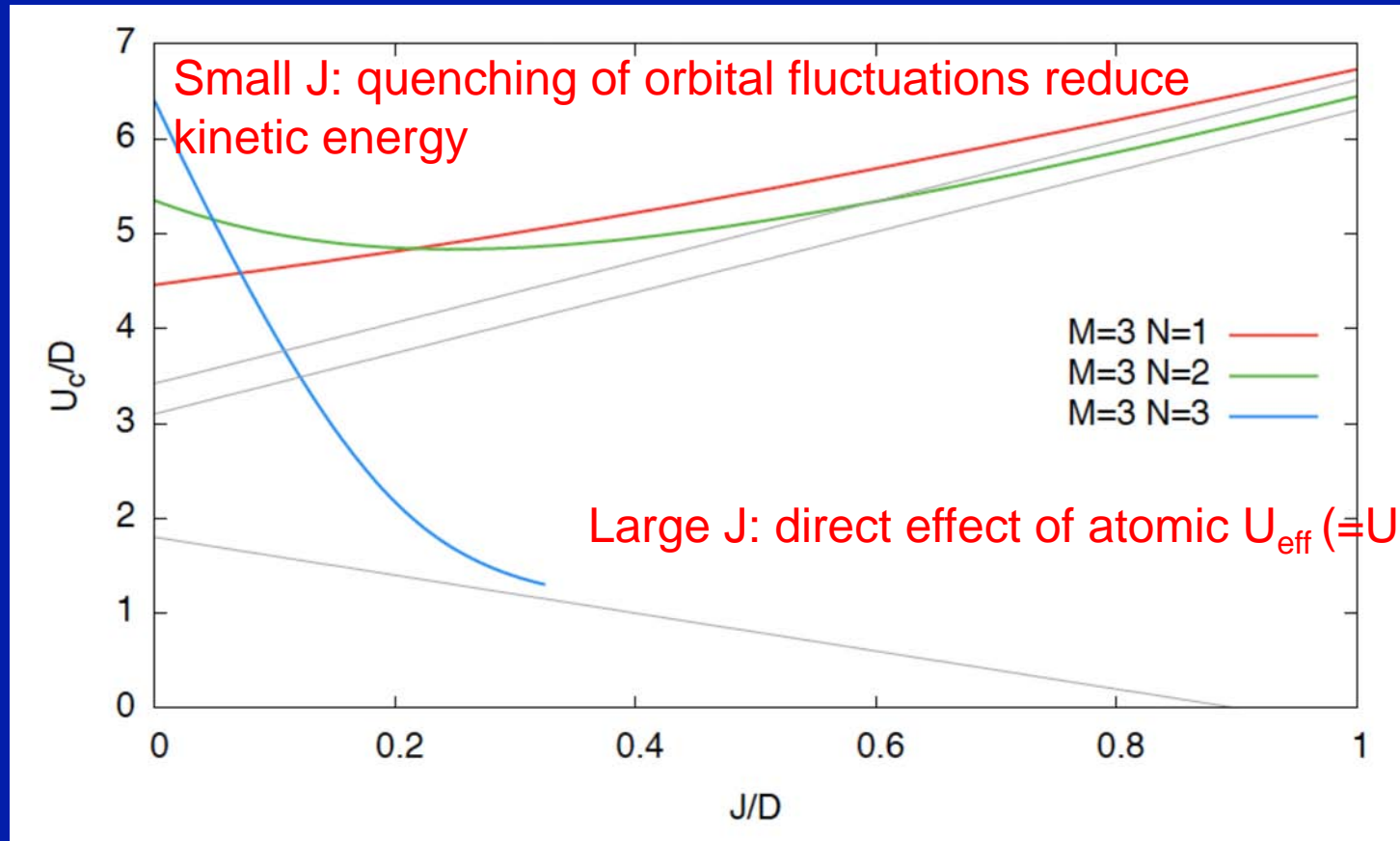


Figure 1: Critical coupling separating the metallic and Mott insulating (paramagnetic) phase, as a function of the Hund's rule coupling, for a Hubbard-Kanamori model of three degenerate bands with one (red), two (green) and three (blue) electrons per site. The model is solved with DMFT, with a semi-circular density of states of bandwidth $2D$ for each band. See Refs. [20,27].

Key points

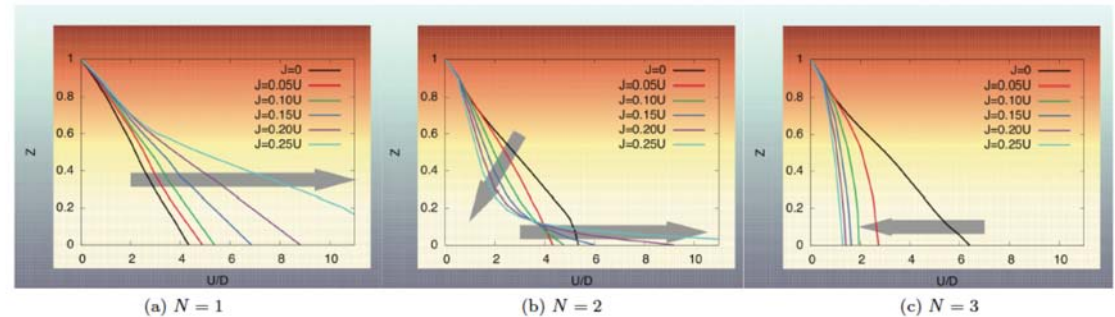


Figure 1: Quasiparticle weight Z vs. U for $N = 1, 2, 3$ electrons in $M = 3$ orbitals. The grey arrows indicate the influence of an increasing Hund's rule coupling J/U .

* At $\frac{1}{2}$ filling (3 el. In 3 orbitals) Mott critical

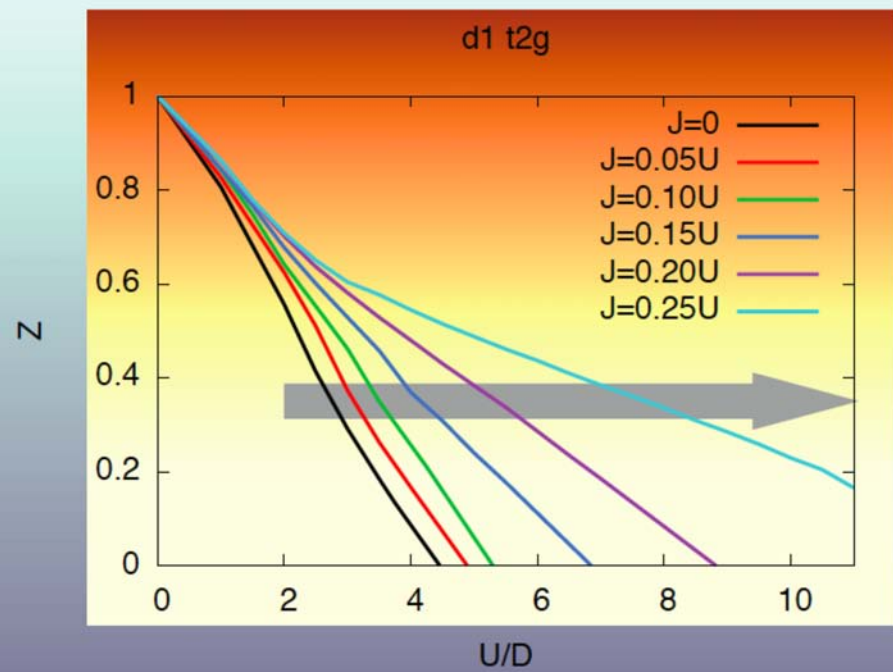
U_c is strongly reduced upon increasing J

cf. Bunemann, Weber, Gebhard et al.; Han, Jarrell, Cox PRB1998

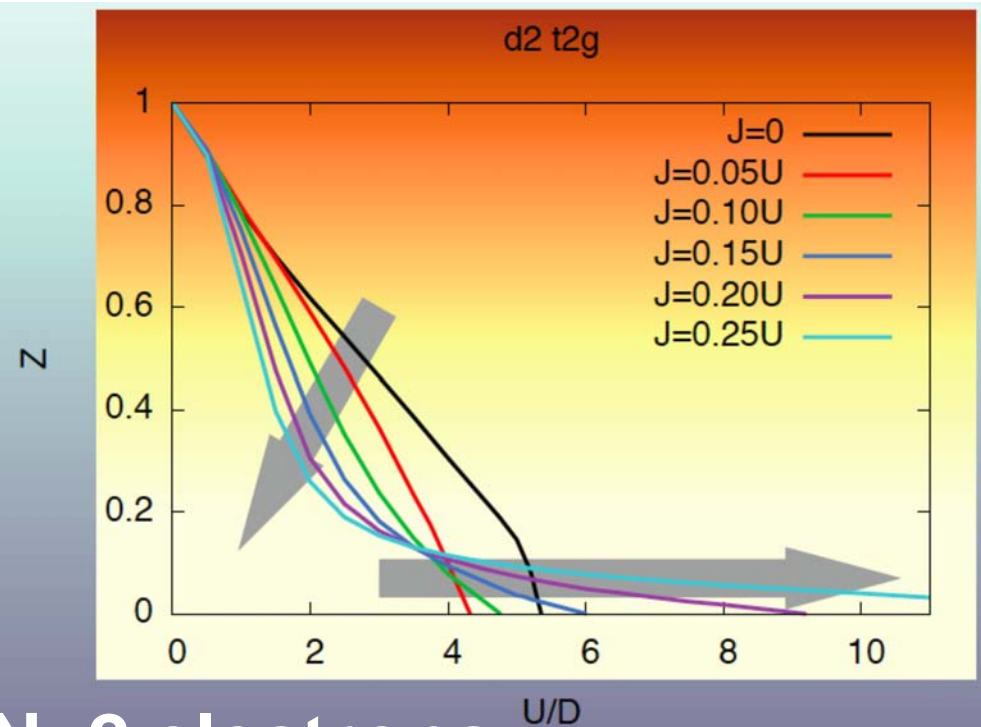
- **IN CONTRAST, away from $\frac{1}{2}$ filling (e.g. $N=1,2,4,5$) U_c is strongly ENHANCED**

cf. L. de' Medici PRB 83, 205112 (2011)

- **At the same time, quasiparticle coherence scale ($\sim ZD$) is strongly SUPPRESSED as J is increased cf. Suppression of Kondo scale**

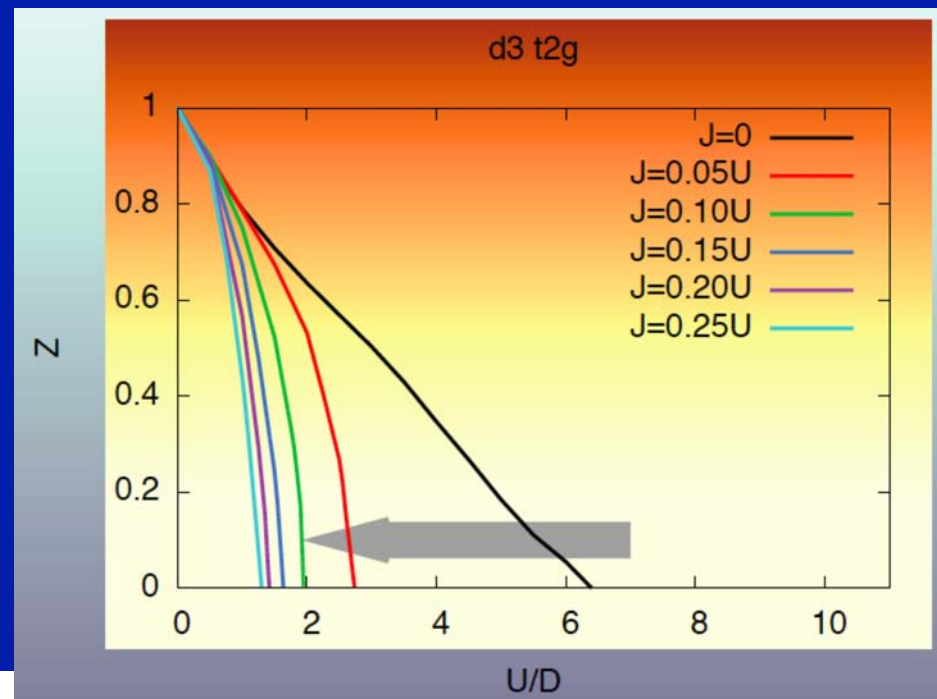


N=1 electron



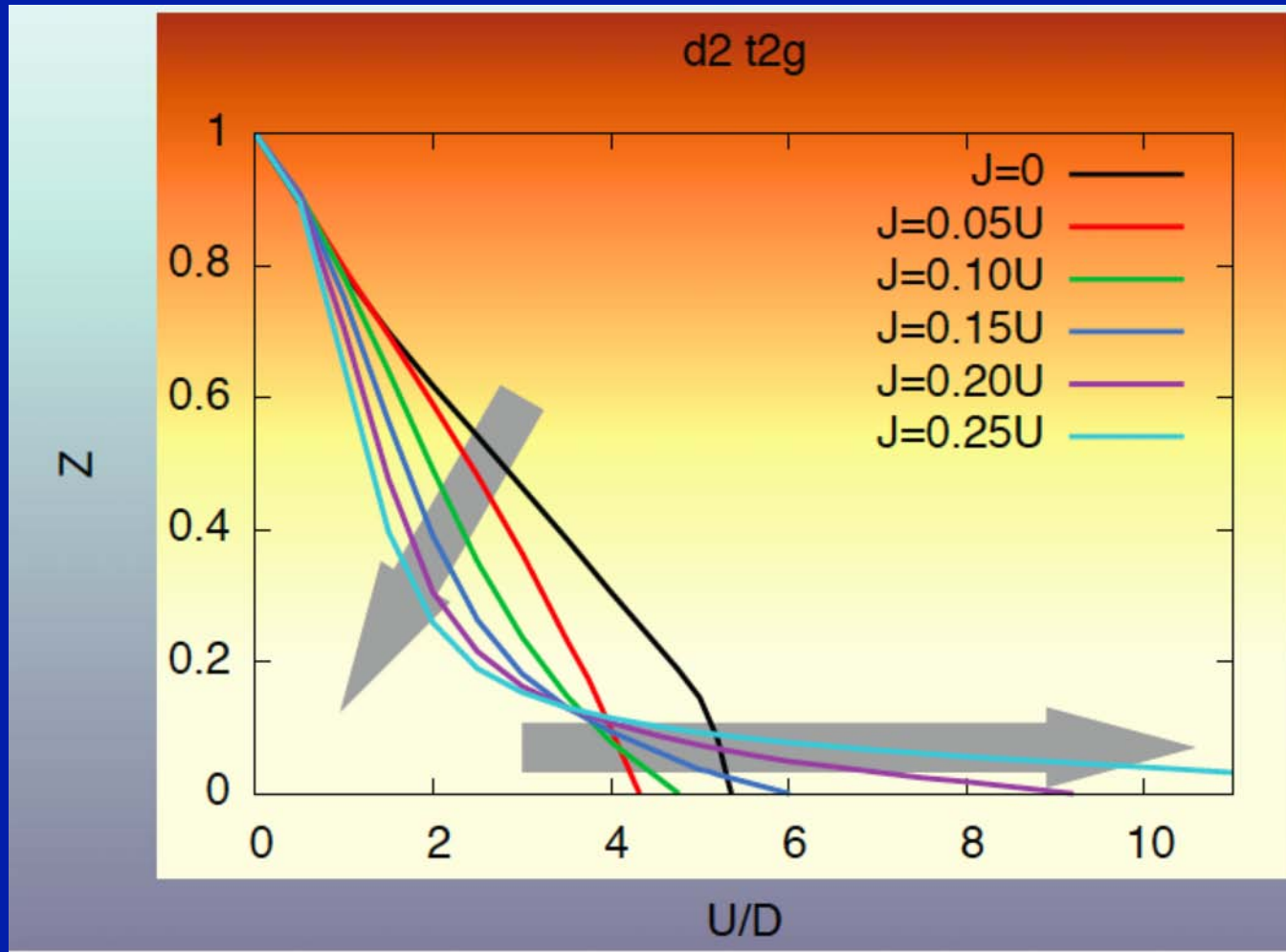
N=2 electrons

**Quasiparticle
weight Z
vs. U/D**



N=3 electrons

For $N=2,4$: Hund suppresses coherence scale \rightarrow
« Bad metal » behaviour, small Z



Increases $U_c \rightarrow$ Enhances range of metallic state

As a result, for generic filling...
(i.e. not $\frac{1}{2}$ filling
and not 1 electron or hole)
e.g. for 2 or 4 electrons
in degenerate t_{2g} bands



... J is « Janus-faced » :
it has two **ANTAGONISTIC**
effects

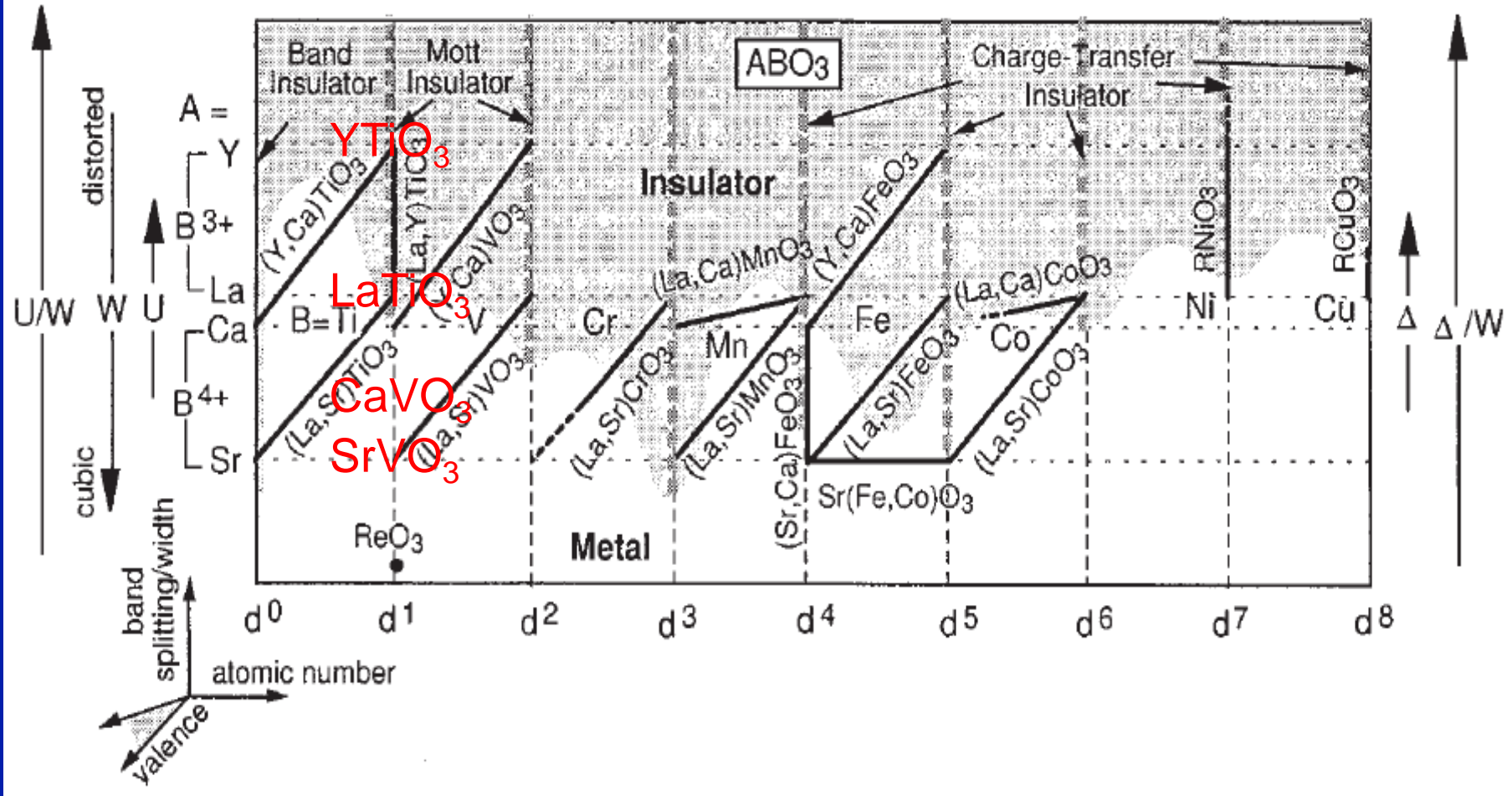
Janus is the latin god of beginnings/
transitions and is often associated
with doors and entrances
and has two faces.

His first mention in physics is due
to P.G. de Gennes

*Drawing a map of early
transition-metal oxides
(both 3d and 4d)
with Hund's rule coupling
as guidance*

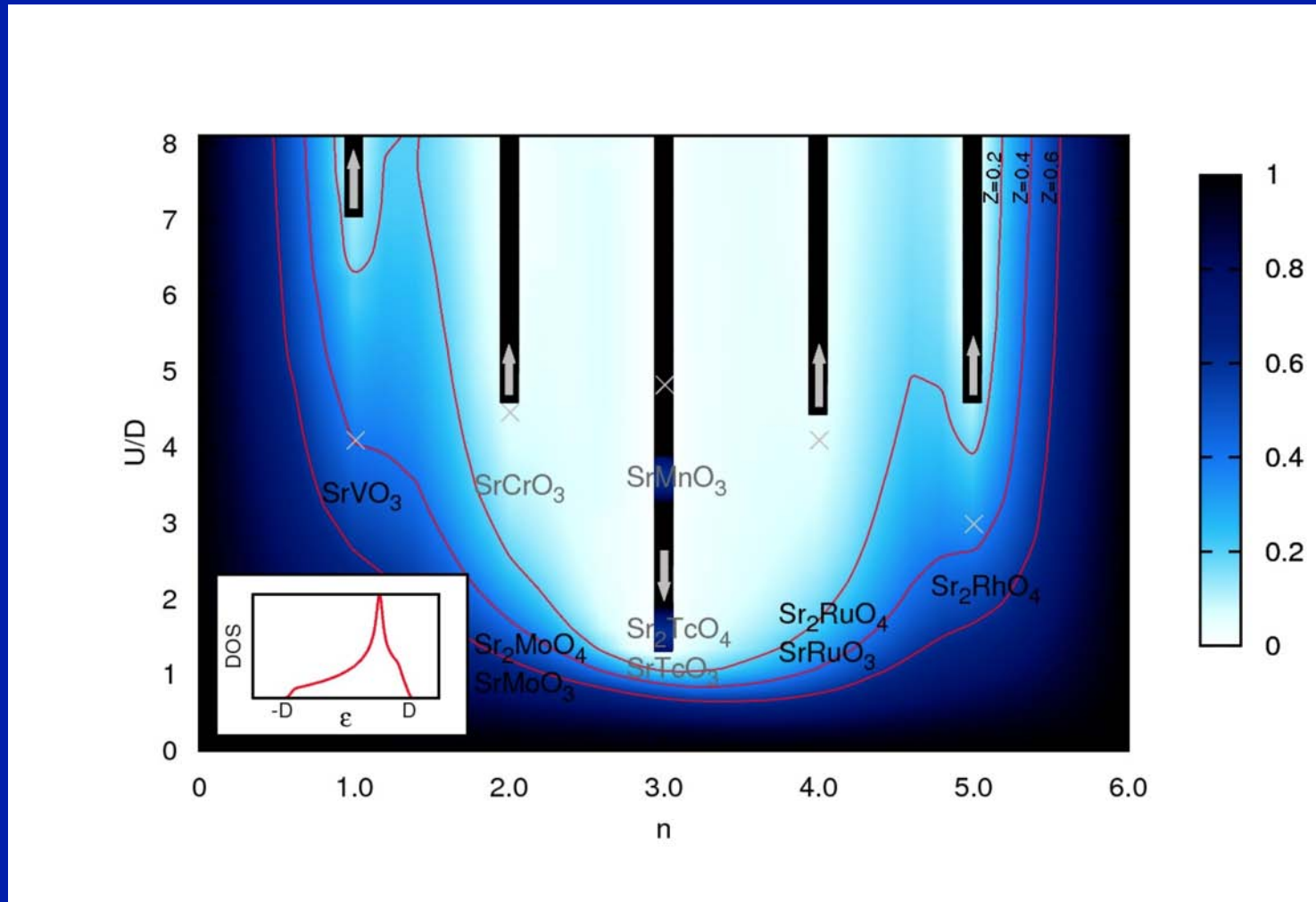


Cf. "Atsushi Fujimori's map of RMO_3 perovskites" J.Phys Chem Sol. 53 (1992) 1595



Partially filled d-shells... and yet often insulators

Correlation effects in 4d oxides due to J, not to Mott physics (except when strong splitting between orbitals)



3d oxides: $U/D \sim 4$
4d oxides: $U/D \sim 2$

Focus in the following on:
Technetium and Ruthenate oxides

OUTLINE of this lecture:

- 1. A remark on AF order in Technetium
- 2. Evidence for key role of Hund's coupling in ruthenate Sr_2RuO_4
- 3. Nature of the 'spin-freezing' non-Fermi liquid regime:
 - Behaviour of physical quantities and possible relevance
 - Status of theoretical understanding
- 4. Moving on to iron pnictides and chalcogenides
→ seminars

1. Record-high Néel temperature in Technetium oxide (SrTcO_3) - contrast to SrMnO_3

PRL **106**, 067201 (2011)

PHYSICAL REVIEW LETTERS

week ending
11 FEBRUARY 2011

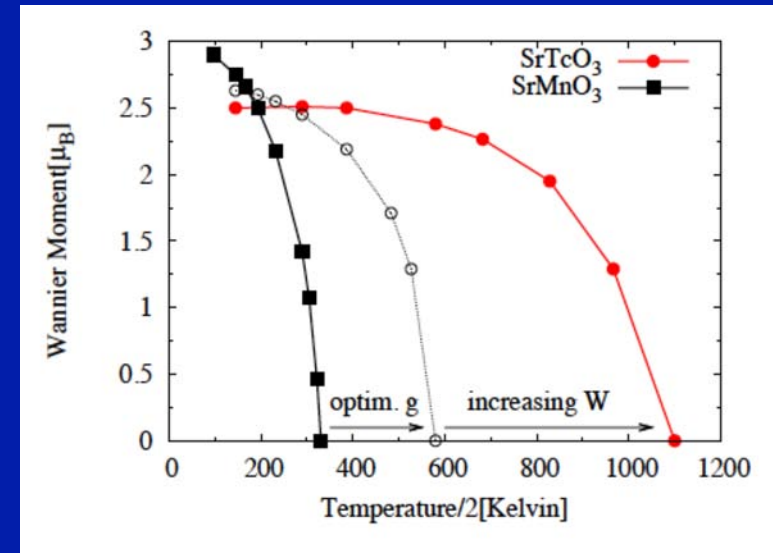
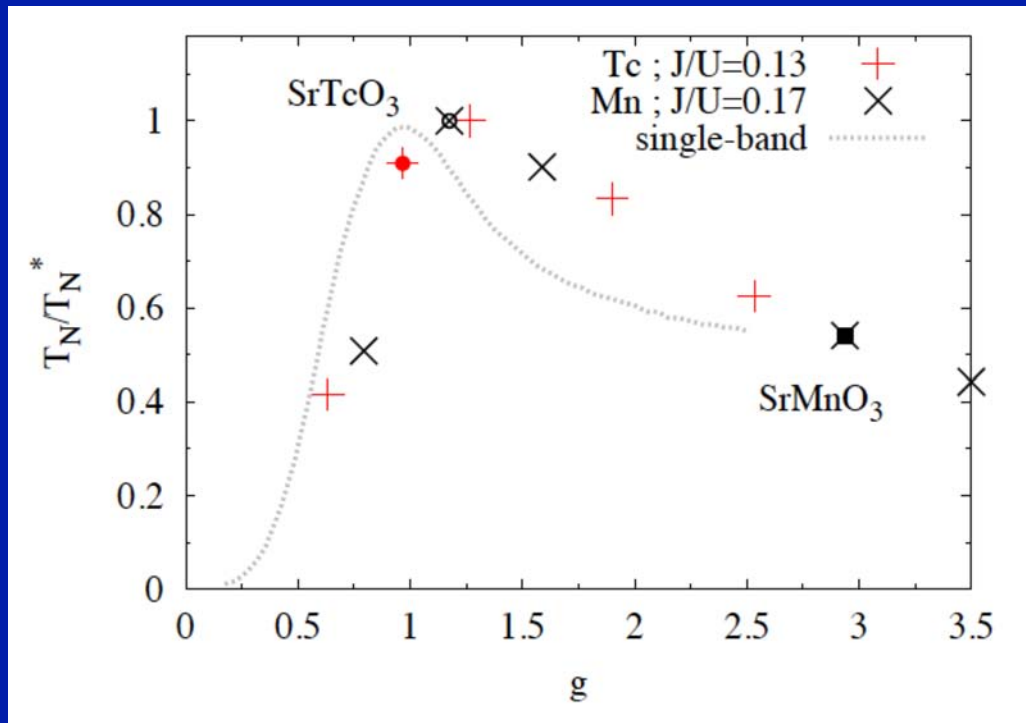


High Temperature Magnetic Ordering in the 4d Perovskite SrTcO_3

Efrain E. Rodriguez,¹ Frédéric Poineau,² Anna Llobet,³ Brendan J. Kennedy,⁴ Maxim Avdeev,⁵ Gordon J. Thorogood,⁶ Melody L. Carter,⁶ Ram Seshadri,⁷ David J. Singh,⁸ and Anthony K. Cheetham⁹

We present evidence for possibly the highest magnetic ordering temperature in any compound without 3d transition elements. Neutron powder diffraction measurements, at both time-of-flight and constant wavelength sources, were performed on two independently prepared SrTcO_3 powders. SrTcO_3 adopts a distorted perovskite structure with *G*-type antiferromagnetic ordering and has a moment of $1.87(4)\mu_B$ per Tc cation at room temperature with an extraordinarily high Néel point close to 750°C . Electronic structure calculations reveal extensive mixing between the technetium 4d states and oxygen states proximal to the Fermi level. This hybridization leads to a close relationship between magnetic ordering temperature and moment formation in SrTcO_3 .

Mechanism: SrTcO_3 ($T_N \sim 1000\text{K}$)
 very close to Mott transition (Hund lowers U_c)
 (In contrast SrMnO_3 is a more localized insulator, $T_N \sim 260\text{K}$)



J.Mravlje et al.
 PRL 108,
 197202 (2012)

Figure 3. The Néel temperatures as a function of coupling $g \equiv U/U_c$, with $U \equiv U + 2J$ and $U_c = (U + 2J)_c$ the value at which the metal-insulator transition occurs in the paramagnetic state. T_N are normalized to the maximum Néel temperature T_N^* found when varying U . The gray line is for the single-band Hubbard model (DMFT calculation of Ref. [19]).

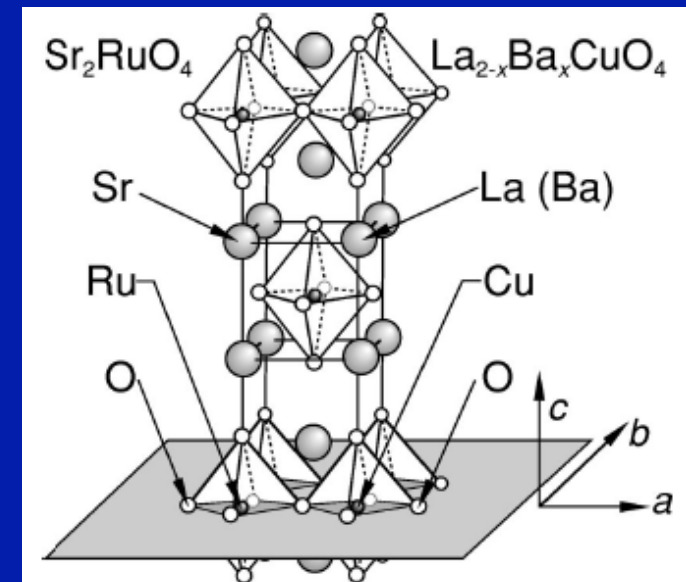
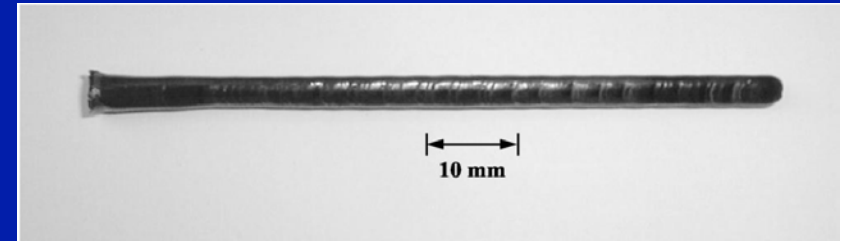
2. Sr_2RuO_4 : A Hund's correlated metal

J.Mravlje et al., PRL 106, 096401 (2011)

Ruthenates: cf. seminar last week by F.Baumberger

Sr_2RuO_4 : the 'Helium 3' of transition-metal oxides !

- Huge high-quality crystals !
- Has been investigated with basically all techniques in the experimentalist's toolbox
- 4d-row structural analogue of La_2CuO_4
- Beautiful review articles:
 - A.Mackenzie and Y.Maeno
RMP 75, 657 (2003)
 - Bergemann, Adv. Phys. 52, 639 (2003)
[Focus on dHvA quantum oscillations]



Yet, outstanding puzzles about this compound remain...

- A 4d material
 - expect not very large U ($< 3\text{eV}$)
 - Yet, effective mass enhancement (vs. band/LDA value) as large as ~ 5
 - Strong orbital dependence
 - Low Fermi-liquid coherence scale:
 - T^2 law obeyed only below $\sim 30\text{K}$
 - Quasiparticles suppressed above $\sim 130\text{K}$, at which interlayer resistivity crosses over from metallic to insulating

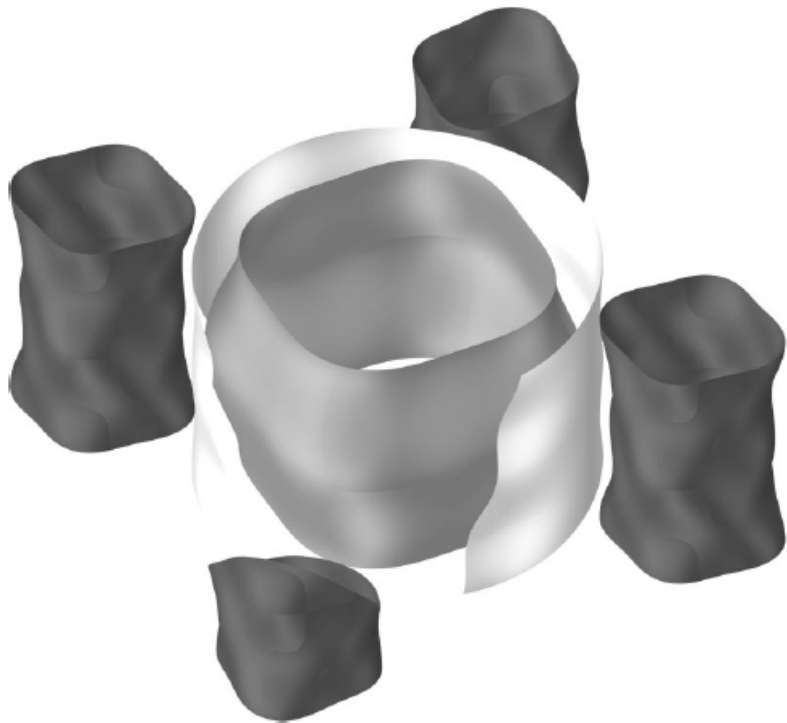
Basic electronic structure :

- 4 electrons in t_{2g} shell
- d_{xy} orbital yields a quasi 2D band \rightarrow γ -sheet of FS
- d_{xz} , (resp. d_{yz}) \rightarrow bands with directional hopping along x (resp. y) \rightarrow α, β sheets

Fermi surface of Sr_2RuO_4

and populations from dHvA:

FS from quantum oscillations:

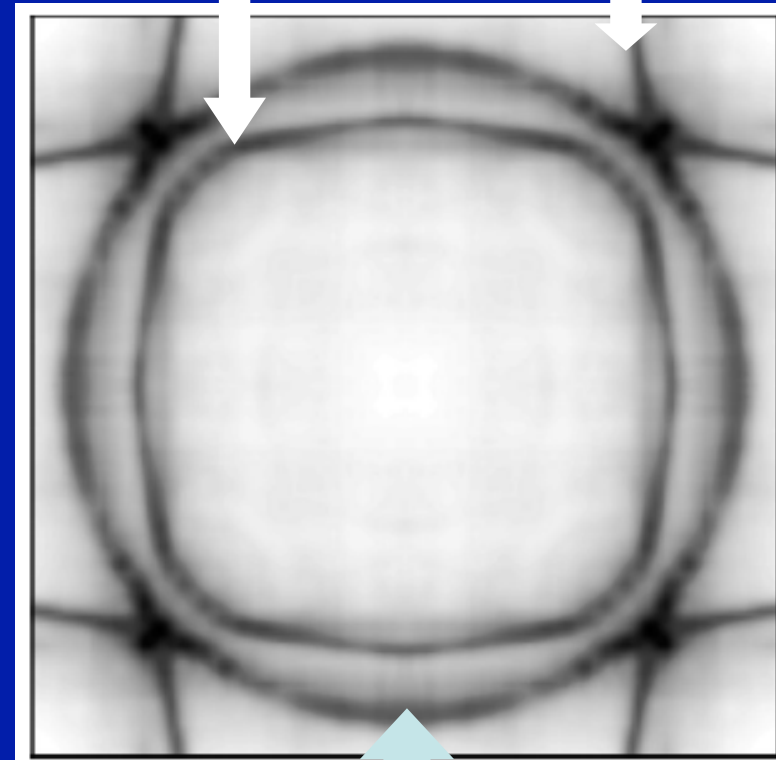


FS from photoemission:

β -sheet
(0.9 electrons)

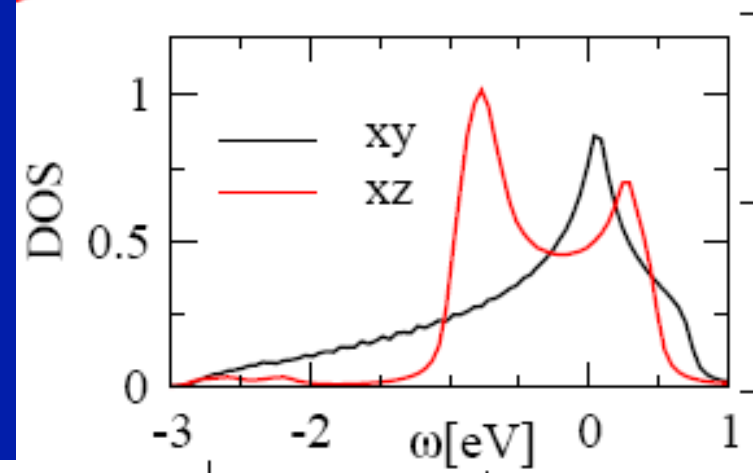
α -sheet
0.2 hole

k_y

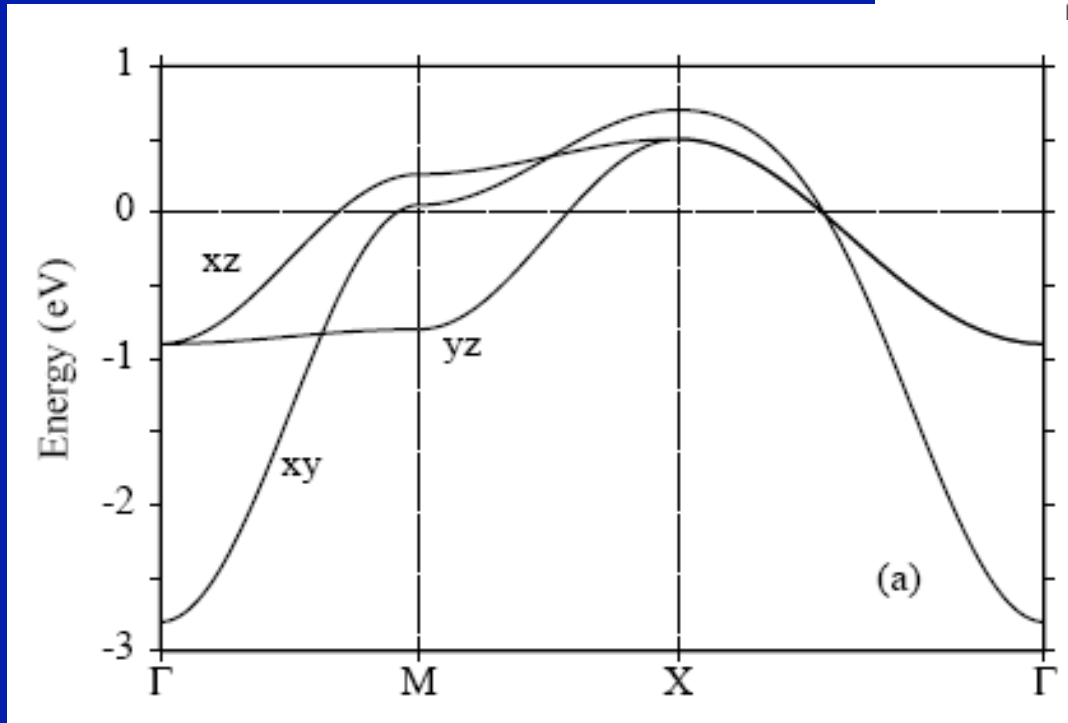


γ -sheet (xy)
1.3 electrons

Bands (LDA)



~ 1.5 eV
(xz,yz)



~ 3.6 eV
(xy band)

But kinetic energies of all bands comparable

Effective masses

TABLE II. Summary of quasiparticle parameters of Sr_2RuO_4 .

Fermi-surface sheet	α	β	γ
Character	Holelike	Electronlike	Electronlike
k_F (\AA^{-1}) ^a	0.304	0.622	0.753
m^* (m_e) ^b	3.3	7.0	16.0
m^*/m_{band} ^c	3.0	3.5	5.5
v_F (ms^{-1}) ^d	1.0×10^5	1.0×10^5	5.5×10^4
$\langle v_{\perp}^2 \rangle$ ($\text{m}^2 \text{s}^{-2}$) ^e	7.4×10^5	3.1×10^6	1.0×10^5
t_{\perp} (K) ^f	7.3	15.0	2.7

- Rather large !
- Strongly orbital dependent.
- **The widest band has the largest eff. mass enhancement !**

Dynamical Mean-Field Theory calculations (using full LDA bandstructure):

- effective masses -

J [eV]	m_{xy}^*/m_{LDA}	m_{xz}^*/m_{LDA}	T_{xy}^* [K]	T_{xz}^* [K]	$T_{>}$ [K]
0.0, 0.1	1.7	1.7	> 1000	> 1000	> 1000
0.2	2.3	2.0	300	800	> 1000
0.3	3.2	2.4	100	300	500
0.4	4.5	3.3	60	150	350

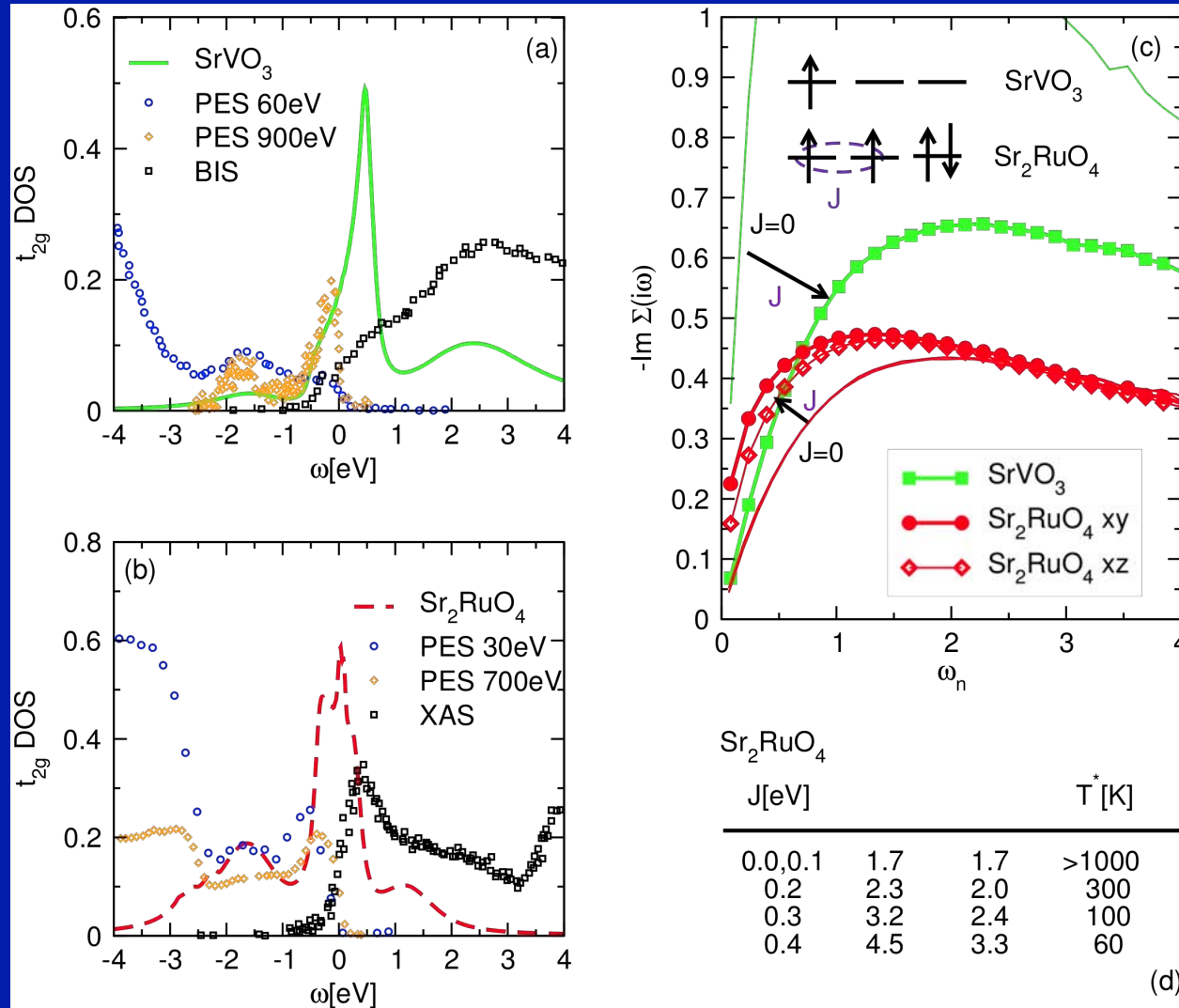
Table I. Mass enhancement of the xy and xz orbitals, as a function of Hund's coupling, for $U = 2.3$ eV. Other columns: coherence temperatures as defined in the text.

- Increase of effective mass as J is increased
- Orbital differentiation: xy heavier
- Comparable mass enhancement would require $U=5\text{eV}$ at $J=0$!

For
 $U=2.3$ eV

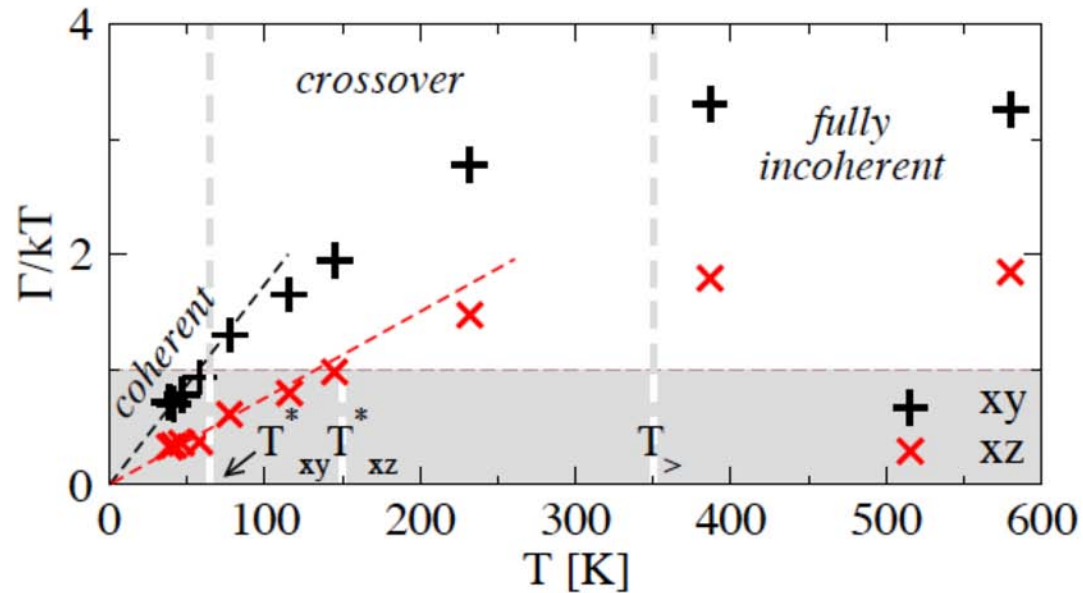
Contrast: Hund's correlations vs. Hubbard U

Sr_2RuO_4 (d^4) vs. SrVO_3 (d^1)



SrVO_3 :
 Courtesy
 M.Casula
 Fig: J.Mravlje

Quasiparticle coherence scale



Inverse QP lifetime / T:

Fermi Liquid @ low-T
 T-linear above ~ 400 K
 Reaches ~kT at ~ 70K

Figure 1. Temperature-dependence of Γ/kT , with \hbar/Γ the quasiparticle lifetime. The shaded region corresponds to the 'coherent' regime with long-lived quasiparticles such that $\Gamma \lesssim kT$.

Low-T calculations made possible by recent progress in DMFT technology: CT-QMC solver of P. Werner et al.

Comparison to ARPES

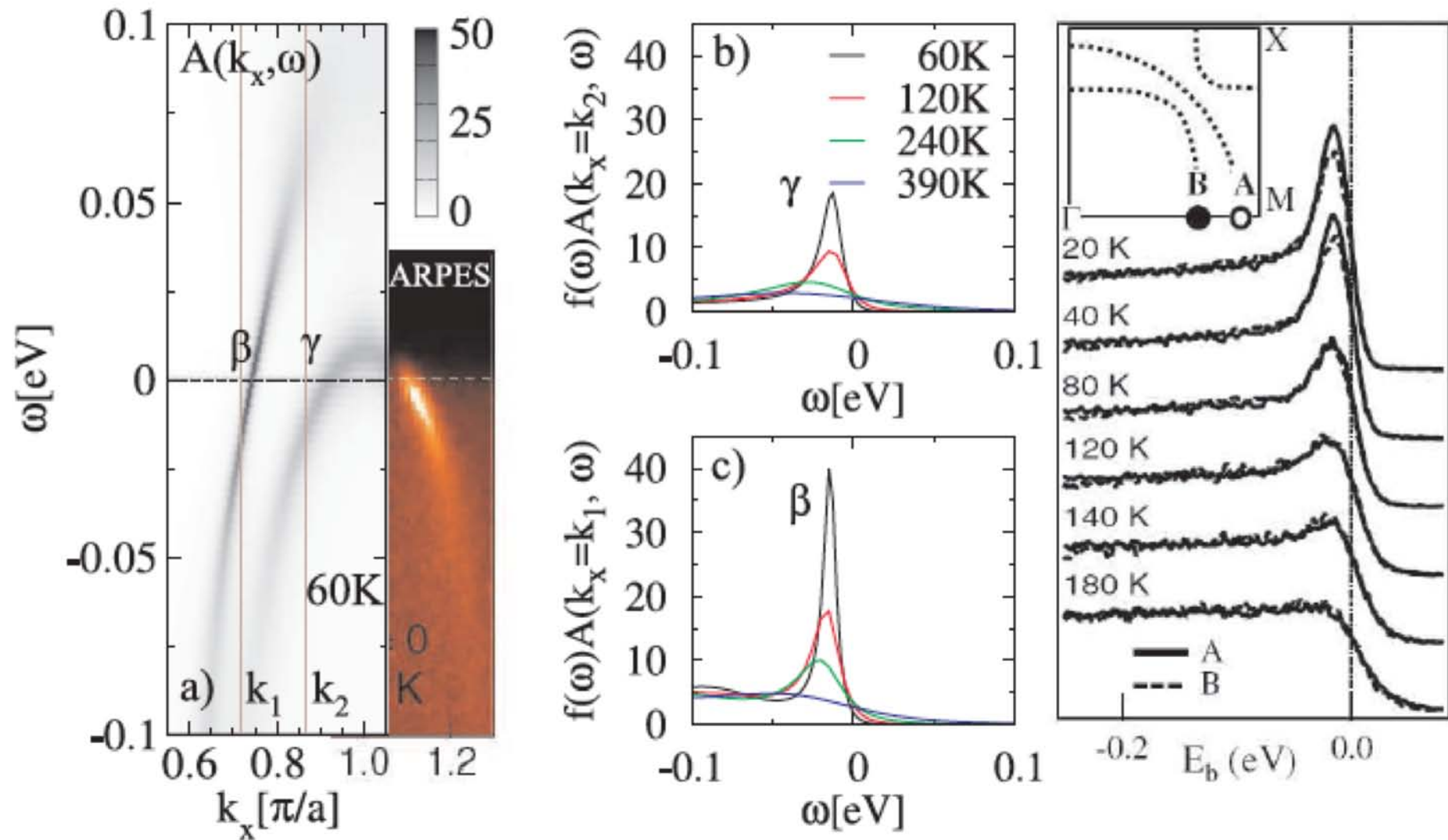
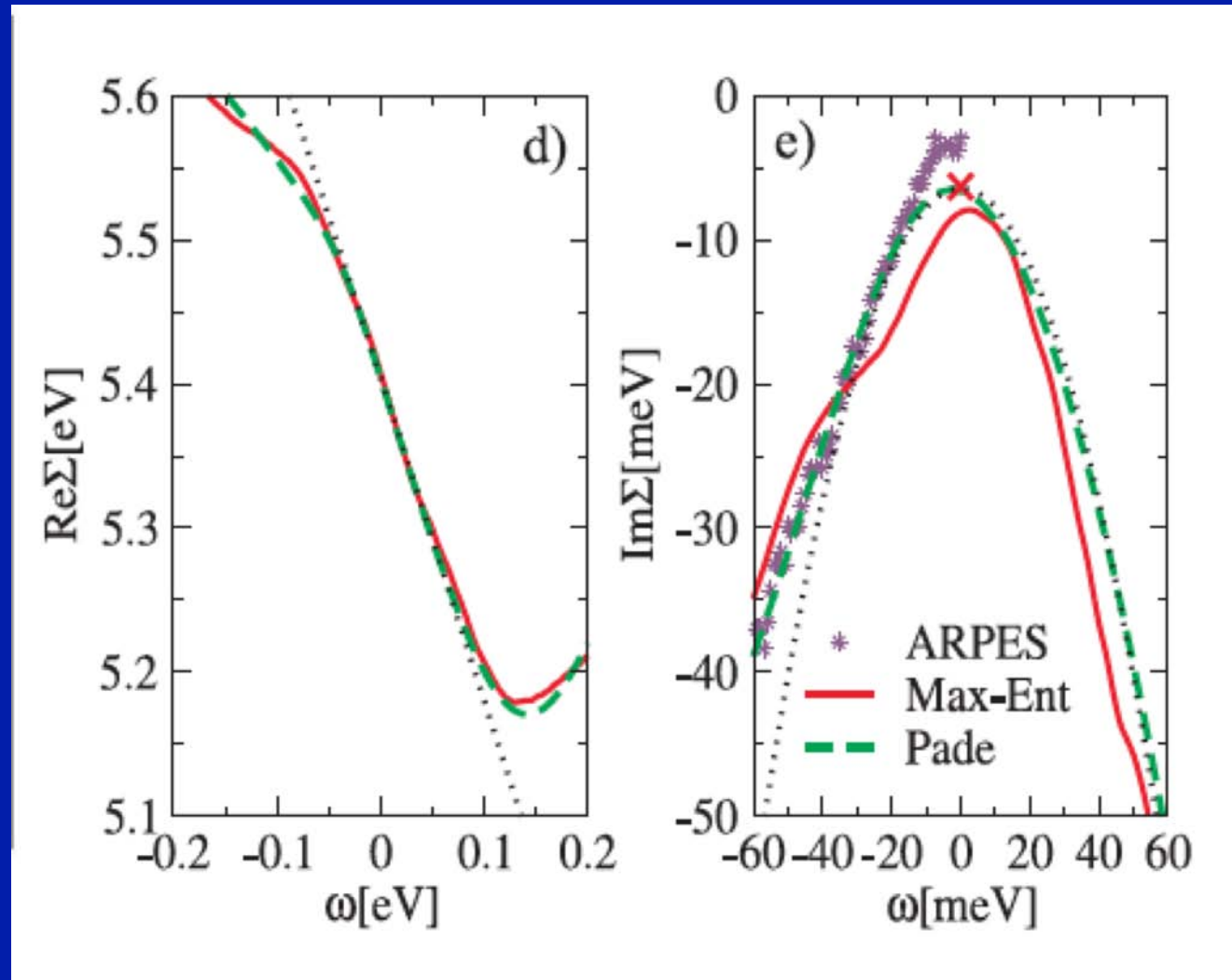


Figure 2. (a) Intensity map of the spectral function $A(k, \omega)$ along $\Gamma \rightarrow M$ for $0.55\pi/a \leq k_x \leq 1.05\pi/a$, $k_y = 0$ at $T = 60$ K compared to ARPES [14]. (b,c) Spectral lineshapes at wavevectors k_1 , k_2 compared to ARPES [3]. (d,e) $\text{Im}\Sigma(\omega + i0^+)$ and

Self-energies vs. ARPES



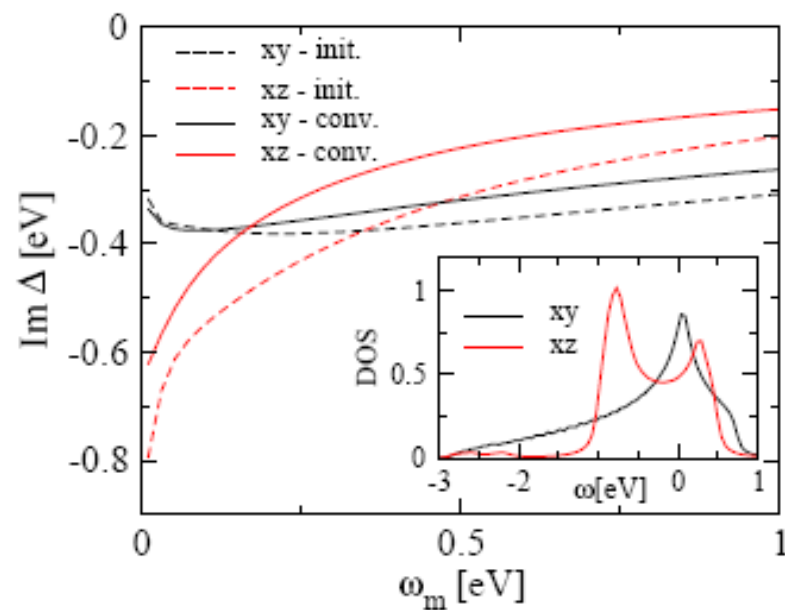
Orbital dependence: why is xy more correlated ?

Hund's coupling lowers the inter-orbital coupling:
Individual fermiology of orbitals becomes relevant

xy `effective hybridization strength' to environment is smaller (by at least a factor of 2) than xz, yz

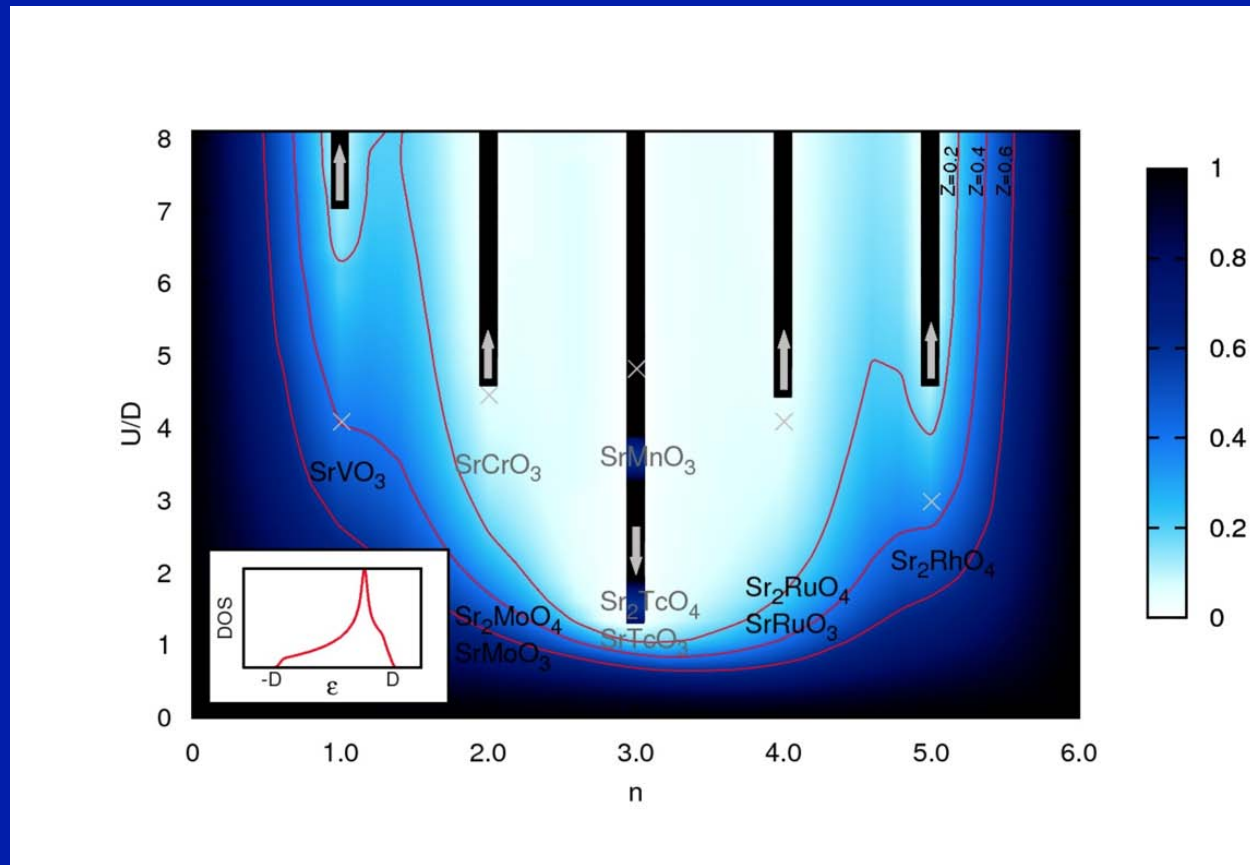
Initial LDA eff. Hybridization:

$$\text{Im}\Delta(i\omega \rightarrow 0) = G_{\text{loc}}^{-1} = -\frac{\text{Im}G_{\text{loc}}}{(\text{Re}G_{\text{loc}})^2 + (\text{Im}G_{\text{loc}})^2}.$$



Proximity of van Hove singularity
for xy makes DOS larger and
Strongly p-h asymmetric
→ Both effects reduce
hybridization

3. 'Spin-freezing' regime and non Fermi-liquid behaviour



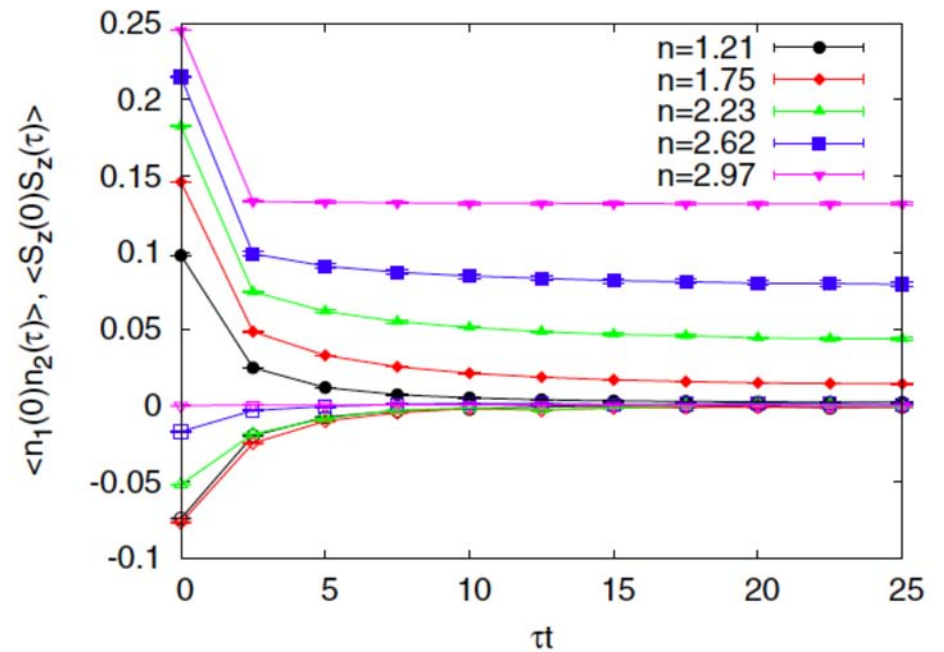
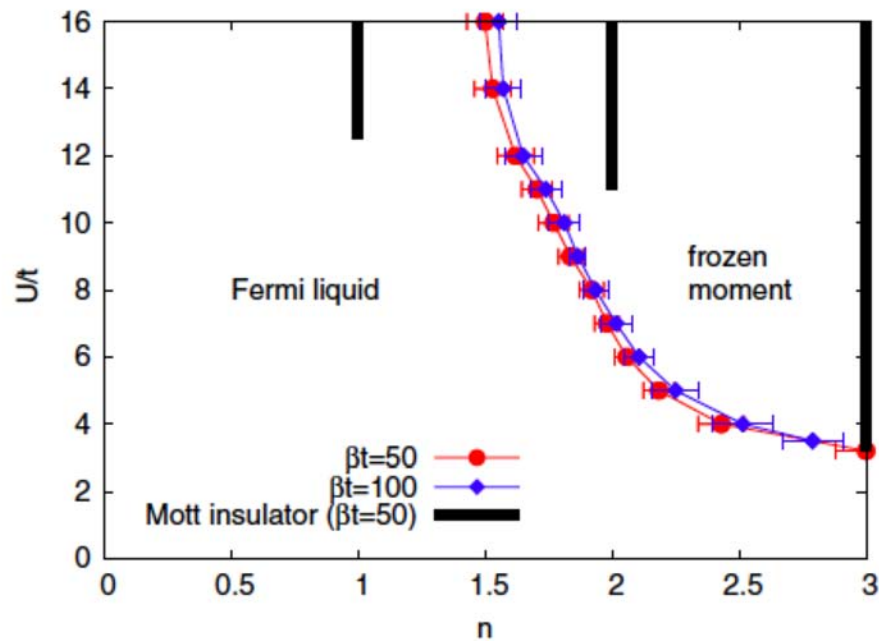
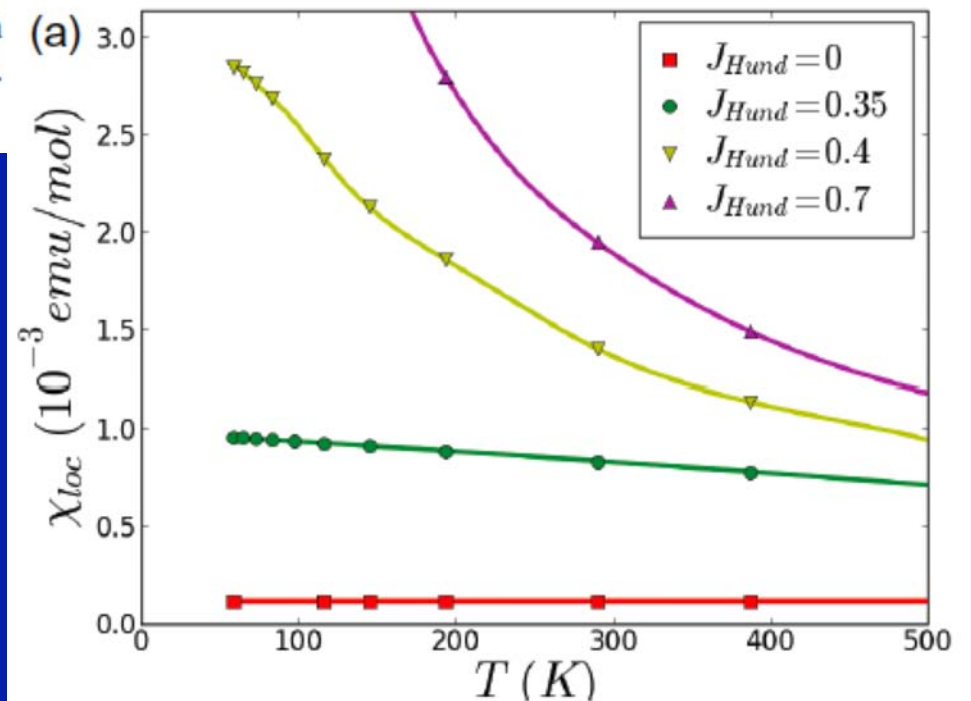


FIG. 1 (color online). Phase diagram for $J/U = 1/6$ and $\beta t = 50, 100$ in the space of density n and interaction strength U . The light line with circles or diamonds indicates a phase transition between a Fermi liquid metal and a "frozen-moment" metal. The black lines mark the regions of Mott insulating behavior.

'Spin freezing'

Werner et al. PRL 2008

Haule&Kotliar NJP 2009



Non Fermi-Liquid regime Power-law self-energy (P.Werner et al)

$$D \text{Im}\Sigma \sim C + (\omega/D)^\alpha$$

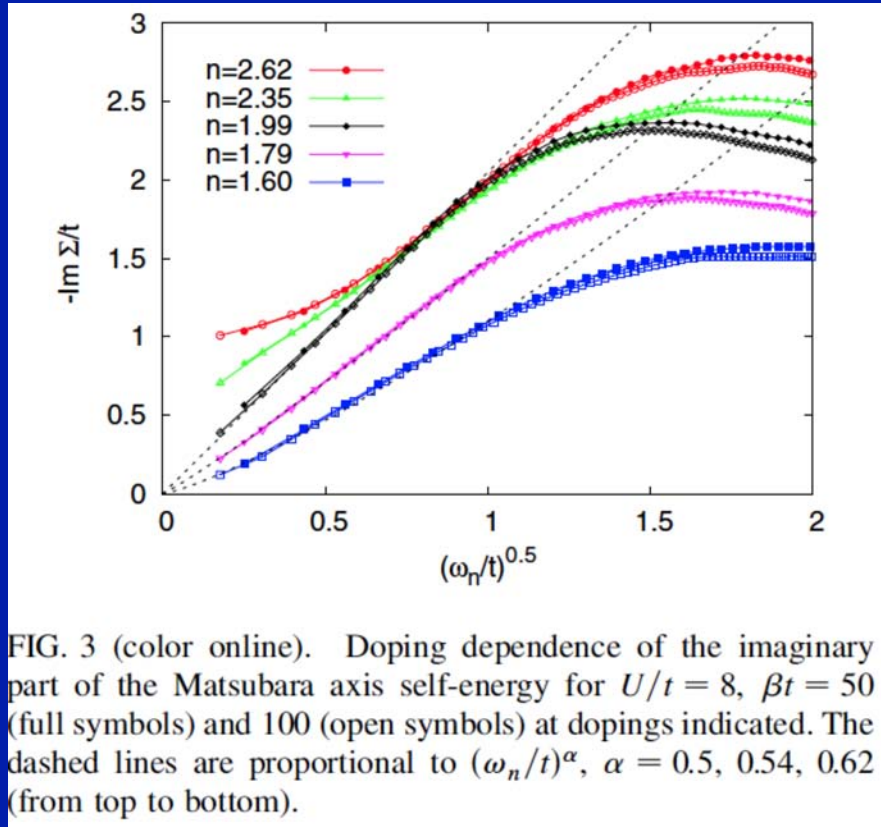


FIG. 3 (color online). Doping dependence of the imaginary part of the Matsubara axis self-energy for $U/t = 8$, $\beta t = 50$ (full symbols) and 100 (open symbols) at dopings indicated. The dashed lines are proportional to $(\omega_n/t)^\alpha$, $\alpha = 0.5, 0.54, 0.62$ (from top to bottom).

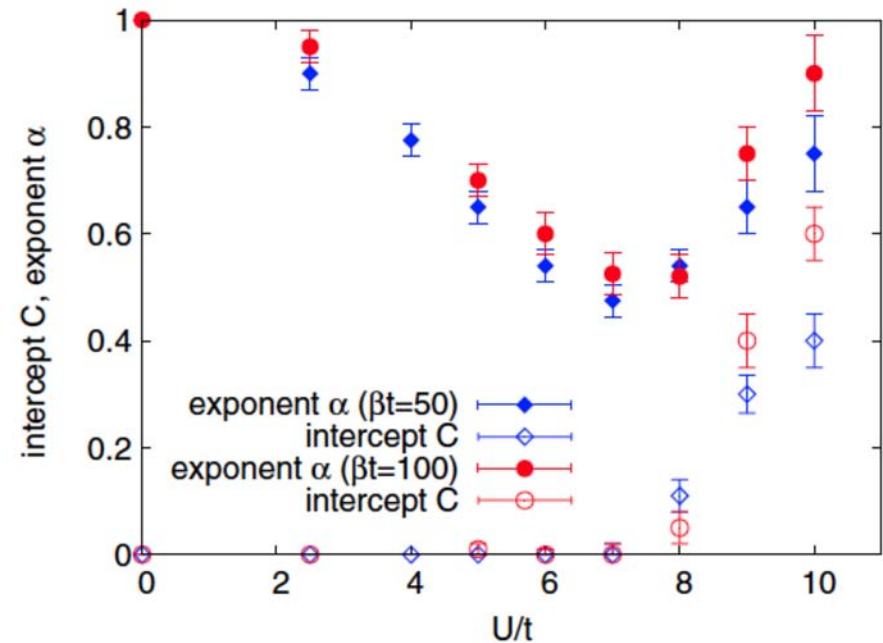
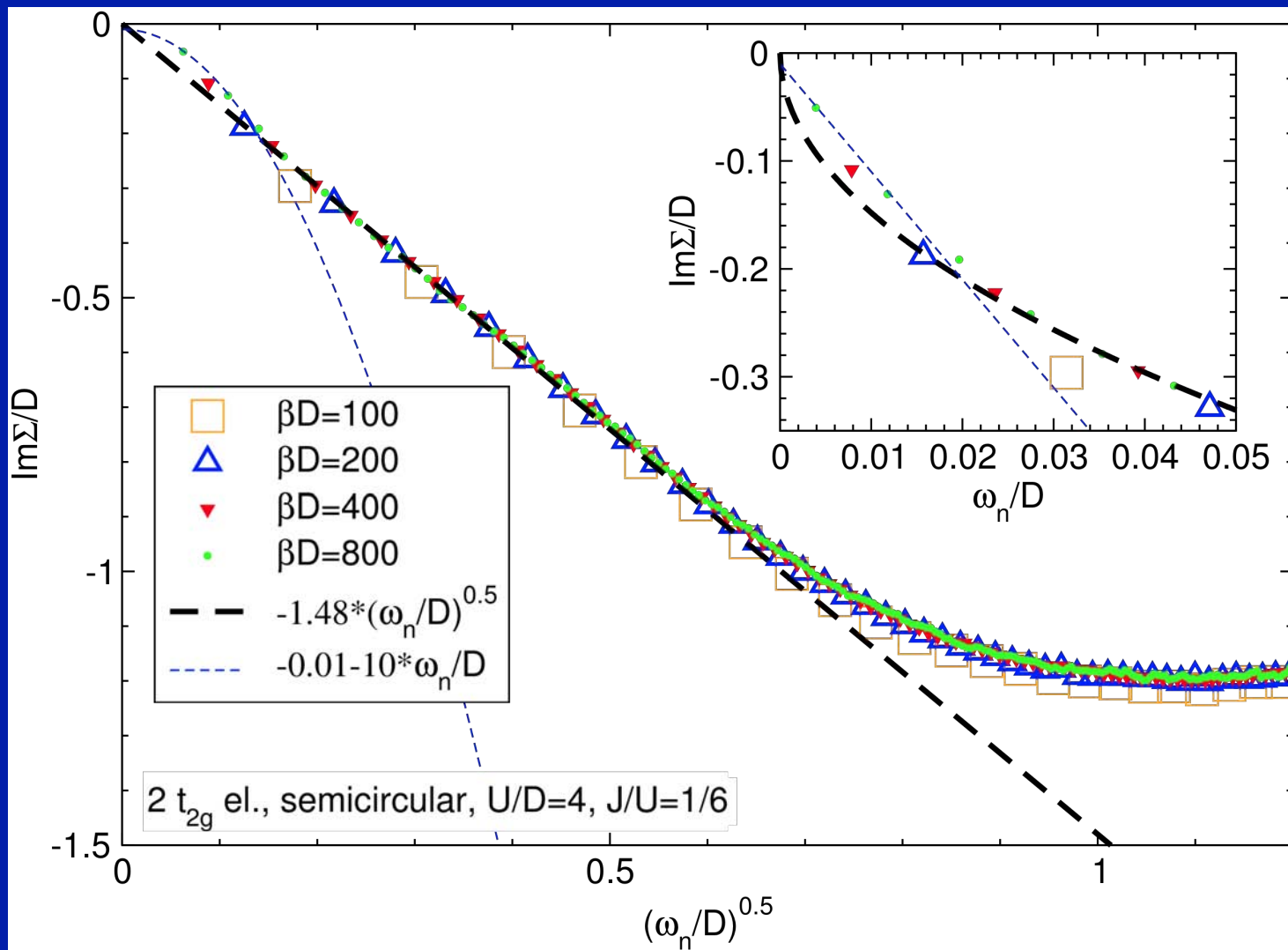


FIG. 4 (color online). Results of a fit of the computed Matsubara-axis self-energy to the scaling form $-\text{Im}\Sigma/t = C + A(\omega_n/t)^\alpha$ at temperatures $T = t/50$ (diamonds; blue online) and $T = t/100$ (circles; red online) at density $n = 2$ and interaction strengths indicated. The plot illustrates the wide quantum critical regime of the spin-freezing transition.

A Fermi liquid is recovered at (very) low T



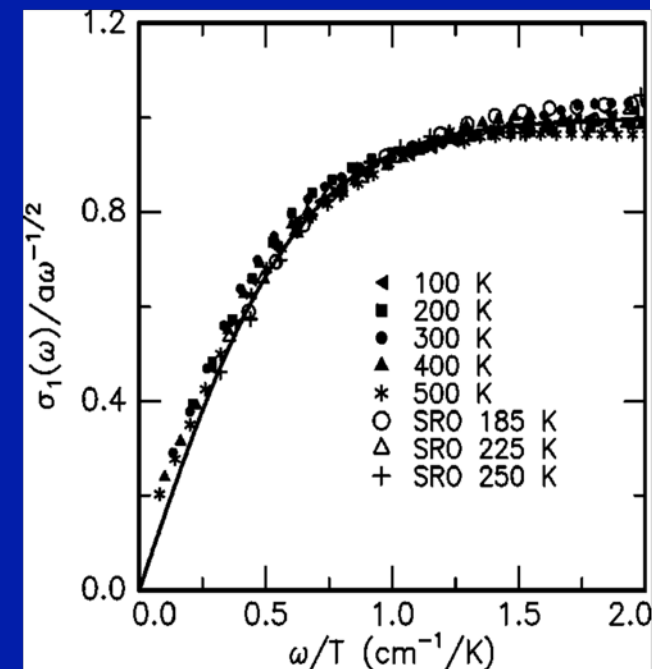
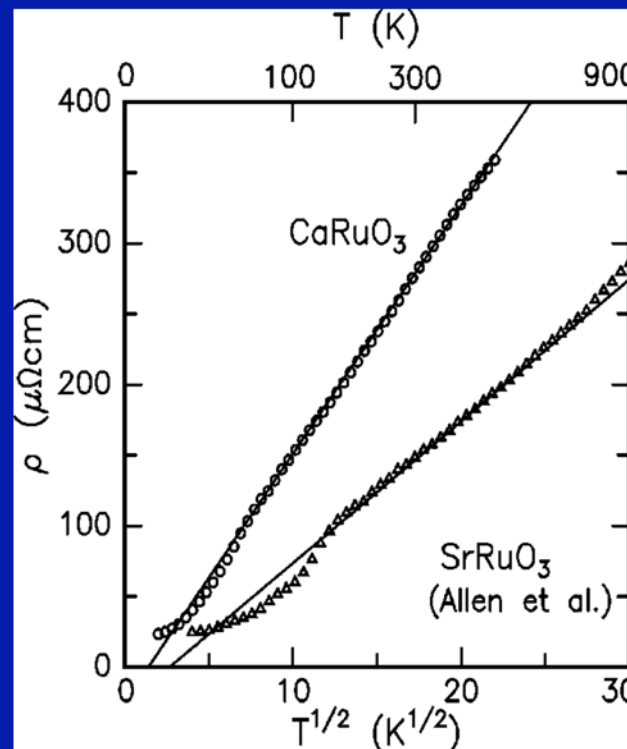
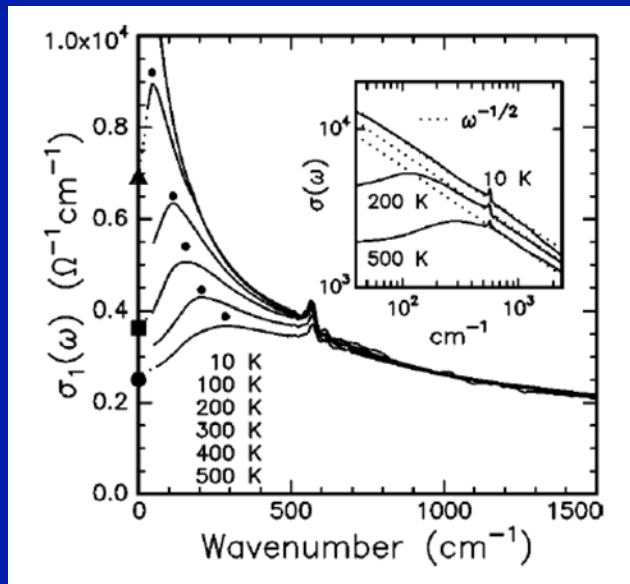
Possible phenomenological consequences

Theory still partly to be worked out
and experimental evidence wanted !

Bad metal, non- T^2 resistivity ($T^{1/2}$?)

Non-Drude optics at low-frequency ($1/\omega^{1/2}$?)

Local moments coexisting with metallic transport



Lee et al.
PRB 66 041104 (2002)

4. Current status of theoretical understanding → Blackboard

Key ref: L. De Leo PhD thesis (SISSA, Trieste)

See also: De Leo and Fabrizio, PRB 69 (2004) 245114

After Schrieffer-Wolf
transformation
of impurity model:

Strategy
(a la Nozieres-Blandin)
Diagonalize HK first
Residual degree of
freedom and
interaction ?

$$H_K = -J \left[2\vec{S}_d \cdot \vec{S}_d + \frac{1}{2} \vec{T}_d \cdot \vec{T}_d \right] \\ + \frac{4t^2}{U} \sum_{ab} \sum_{\alpha\beta} c_{1,a\alpha}^\dagger c_{1,b\beta} d_{b\beta}^\dagger d_{a\alpha} \\ - \frac{2t^2}{U} \sum_{a\alpha} \left(c_{1,a\alpha}^\dagger c_{1,a\alpha} + d_{a\alpha}^\dagger d_{a\alpha} \right)$$

$$H = H_K + H_{cond} \\ = H_K + \sum_{n=1}^{\infty} t_n \left(c_{n,a\alpha}^\dagger c_{n+1,a\alpha} + h.c. \right).$$

Spectrum of atomic t_{2g} hamiltonian with $U'=U-2J$

N	S	L	Degeneracy = $(2S + 1)(2L + 1)$	Energy
0,[6]	0	0	1	0
1,[5]	1/2	1	6	$-5J/2, [10U - 5J/2]$
2,[4]	1	1	9	$U - 5J, [6U - 5J]$
2,[4]	0	2	5	$U - 3J, [6U - 3J]$
2,[4]	0	0	1	$U, [6U]$
3	3/2	0	4	$3U - 15J/2$
3	1/2	2	10	$3U - 9J/2$
3	1/2	1	6	$3U - 5J/2$

Table 1: Eigenstates and eigenvalues of the t_{2g} Hamiltonian $U\hat{N}(\hat{N} - 1)/2 - 2J\hat{S}^2 - J\hat{T}^2/2$ in the atomic limit ($U \equiv U - 3J$). The boxed numbers identifies the ground-state multiplet and its degeneracy, for $J > 0$.

- Hund's rule ground-state in each particle-number sector
- Symmetry broken by J from $SU(6)$ to $U(1)_c \times SU(2)_s \times SO(3)_o$
- \rightarrow Degeneracies lifted by J

Iron-based superconductors: pnictides and chalcogenides

A controversial question since discovery (2008):
How correlated are these materials ?

- Weak coupling itinerant antiferromagnets (SDW)
a.k.a Chromium ?
- Strongly correlated metals, possibly driven
by Hund's coupling rather than proximity to Mott ?
- Very localized magnetism