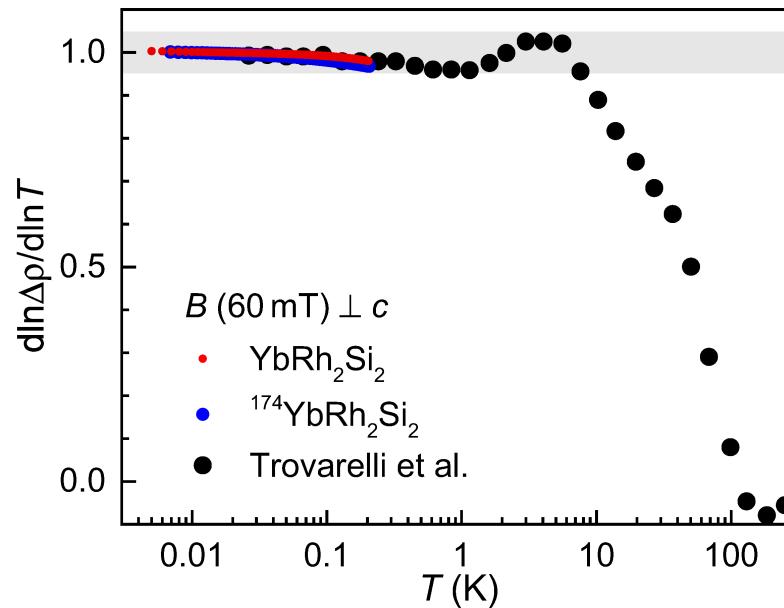


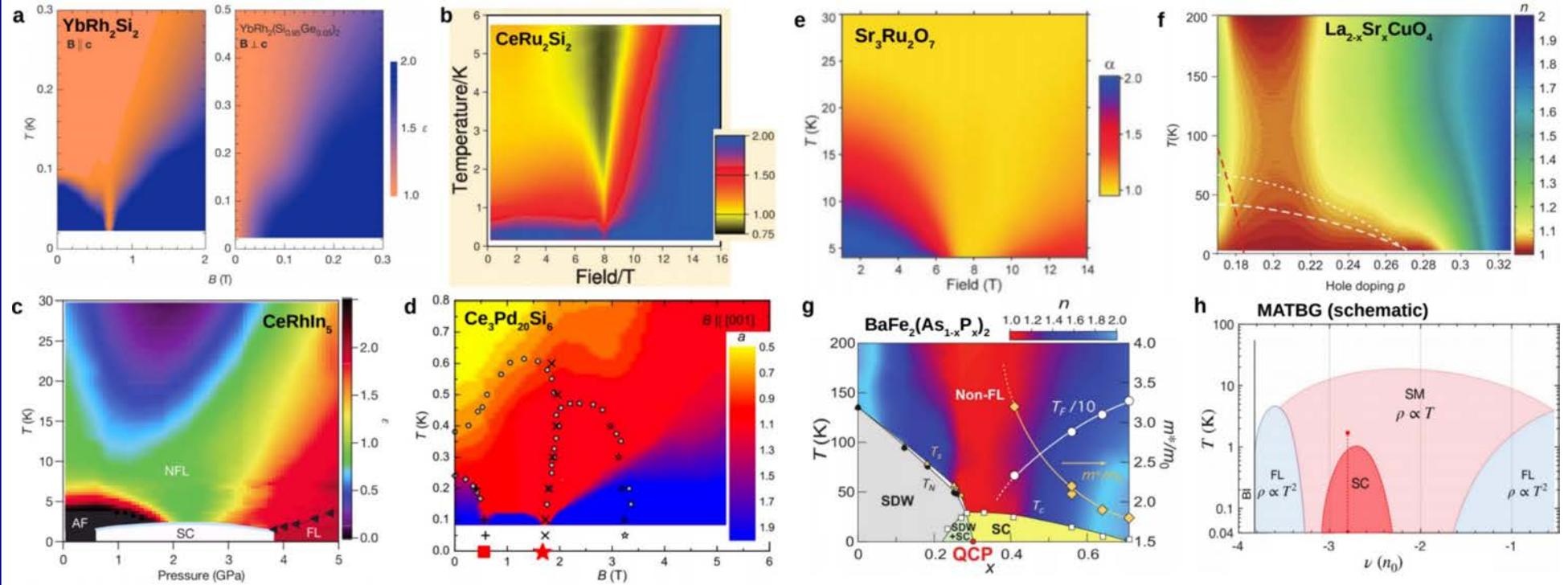
# The extreme strange metal $\text{YbRh}_2\text{Si}_2$

Silke Paschen

Institute of Solid State Physics, TU Wien



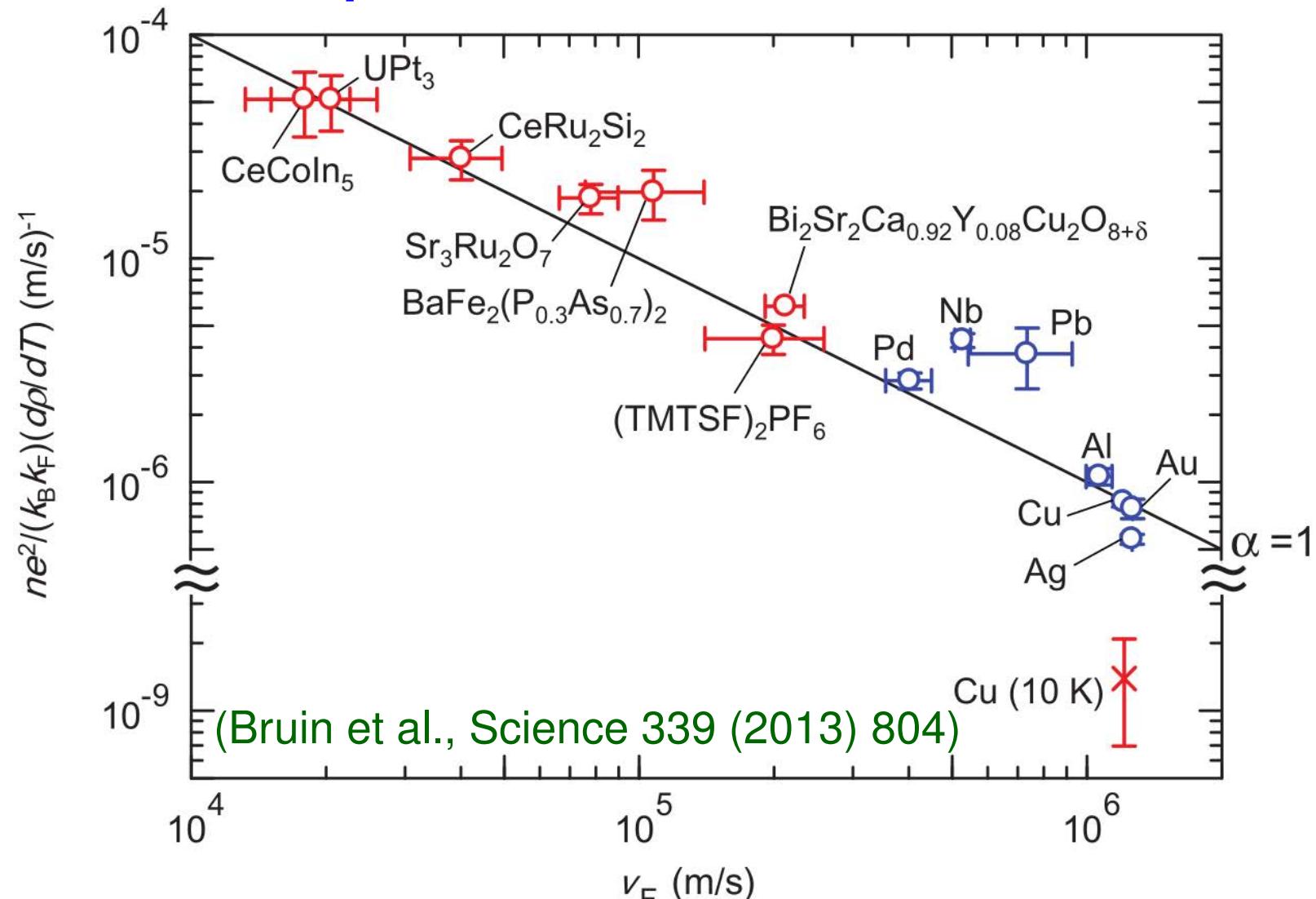
# Strange metal behaviour in SCES



(Taupin & SP, Crystals 12 (2022) 251)

$$\rho = \rho_0 + A'T$$

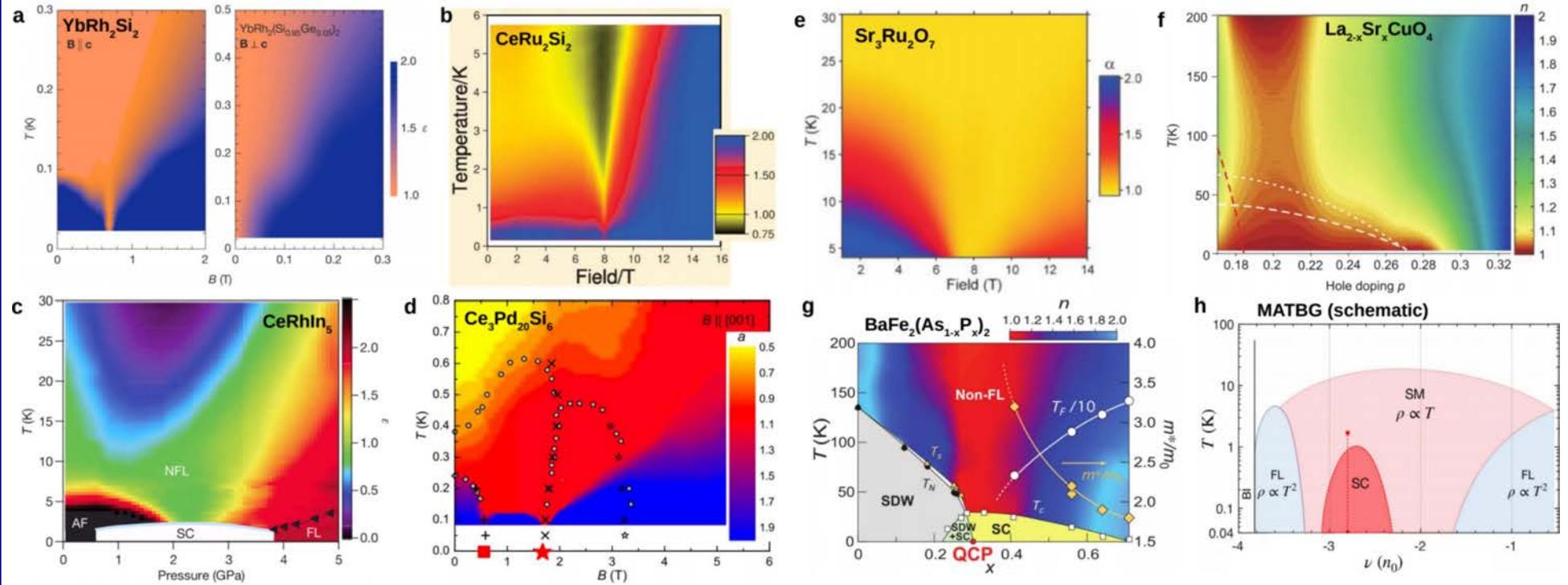
# Planckian dissipation?



$$\rho = \rho_0 + \rho_{\text{in}} = \rho_0 + A' T = \rho_0 + \frac{m}{ne^2} \frac{1}{\tau} = \rho_0 + \frac{m}{ne^2} \alpha \frac{k_B T}{\hbar}$$

Drude model with  $\frac{1}{\tau} \sim T$

# Motivations to understand strange metal behaviour in SCES



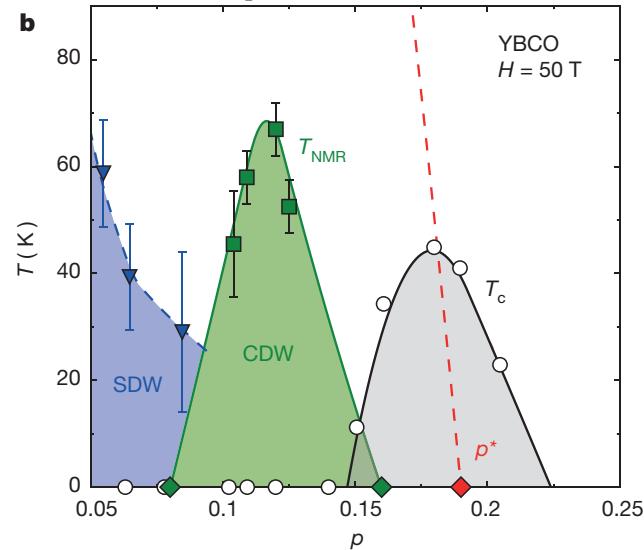
(Taupin & SP, Crystals 12 (2022) 251)

Non-Fermi liquid states of interest in their own right

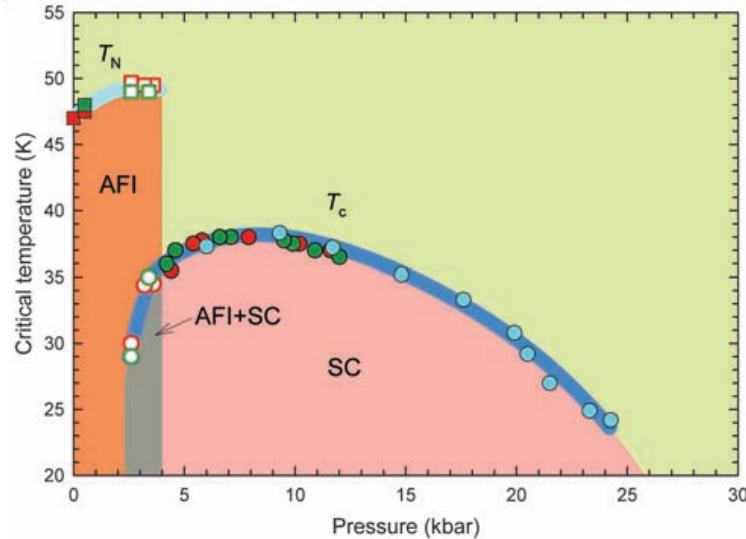
$p$  and  $x$  tuned strange metals have a superconducting dome

# Superconducting domes in SCES

## The cuprate $\text{YBaCuO}_{6-\delta}$

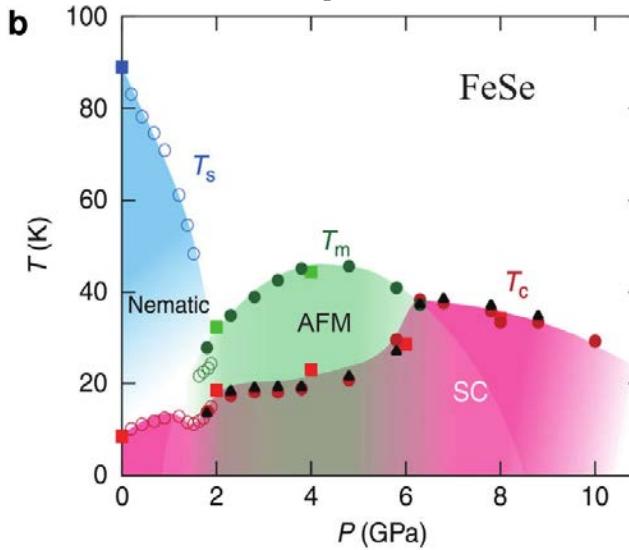


## The fulleride compound $\text{C}_{60}$

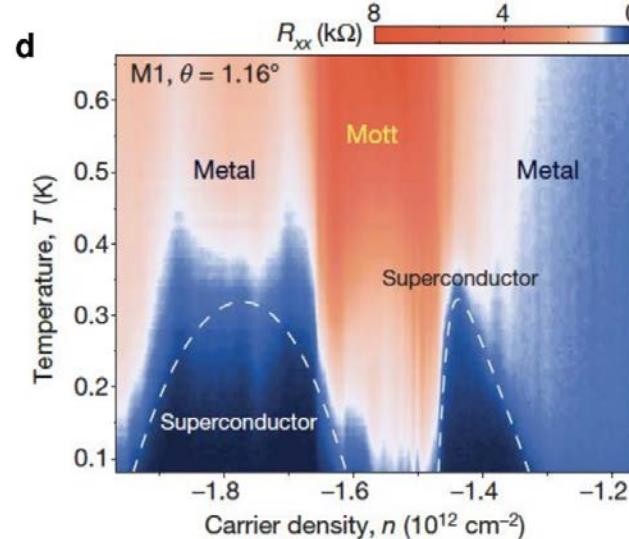


(SP & Si, Nat. Rev. Phys. 3 (2021) 9, and refs. therein)

## The iron pnictide $\text{FeSe}$

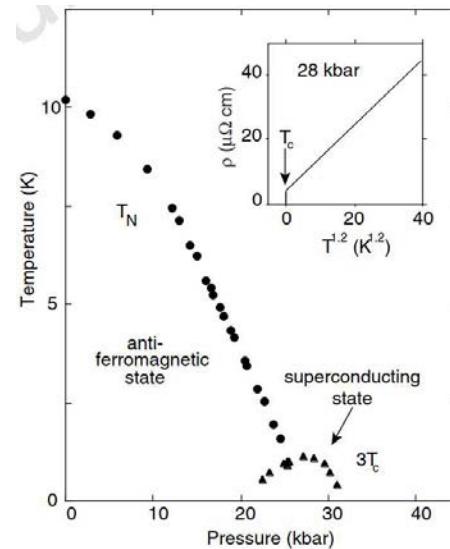
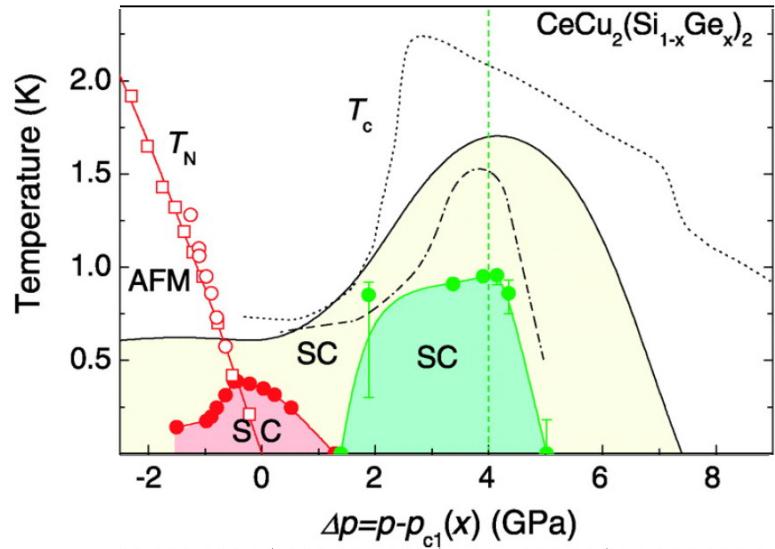


## Magic angle twisted bilayer graphene

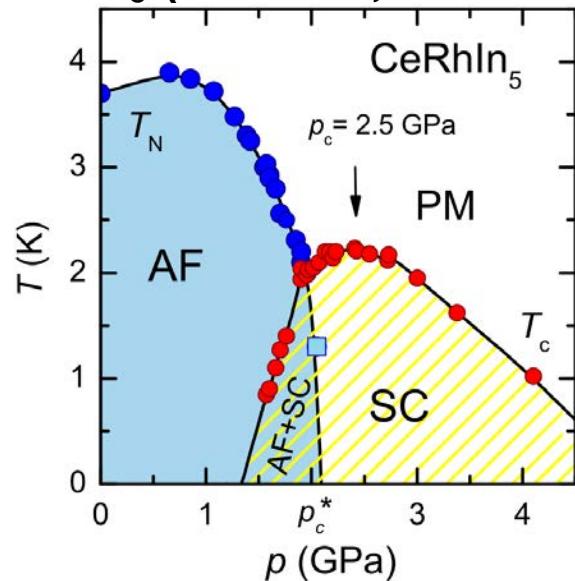


# Superconducting domes in heavy fermion metals

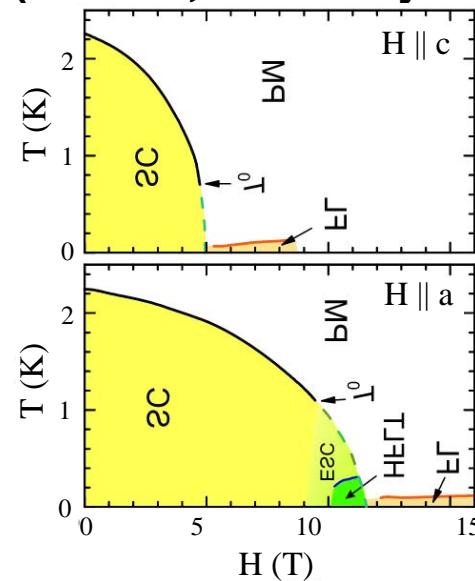
$\text{CeCu}_2\text{Si}_2$  (Yuan et al., Science 2003)    $\text{CePd}_2\text{Si}_2$  (Mathur et al., Nature 1998)



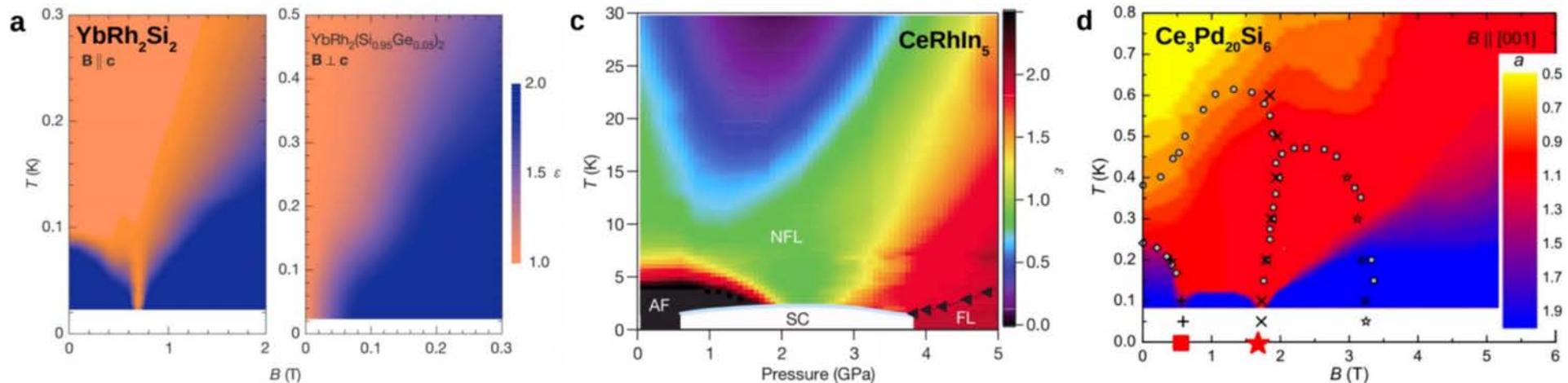
$\text{CeRhIn}_5$  (Yashima, PRB 2007)



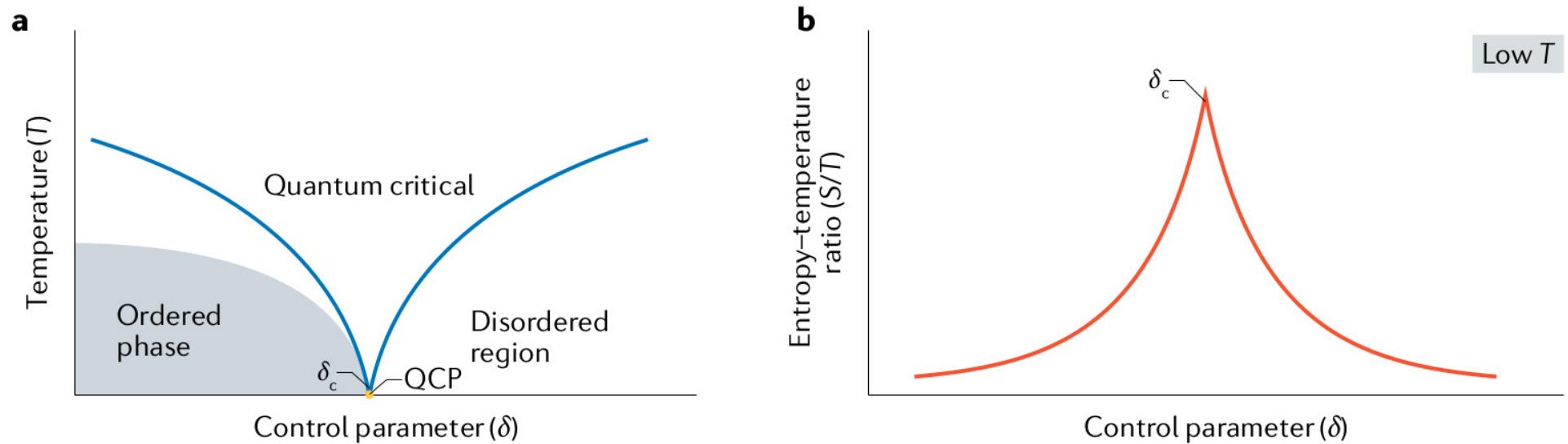
$\text{CeCoIn}_5$  (Knebel, C. R. Phys. 2011 & refs.)



# Quantum critical point scenario: Entropy accumulation

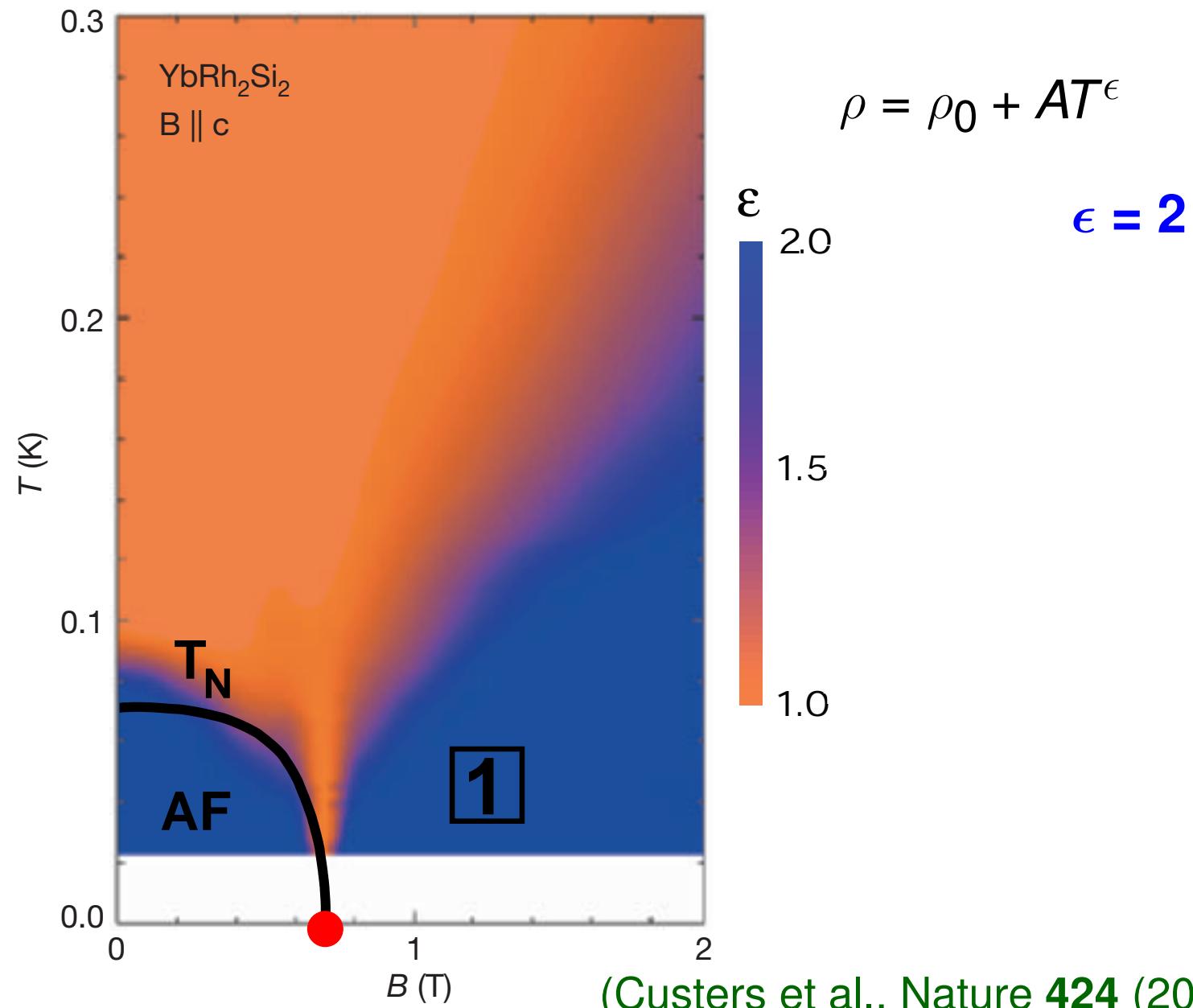


(Taupin & SP, Crystals 12 (2022) 251)



(SP & Si, Nat. Rev. Phys. 3 (2021) 9)

# $\text{YbRh}_2\text{Si}_2$ : A model quantum critical heavy fermion metal



# Heavy Fermi liquids

$$\rho = \rho_0 + A T^2$$

$$C/T = \gamma$$

$$A \sim (m^*)^2$$

$$\gamma \sim m^*$$

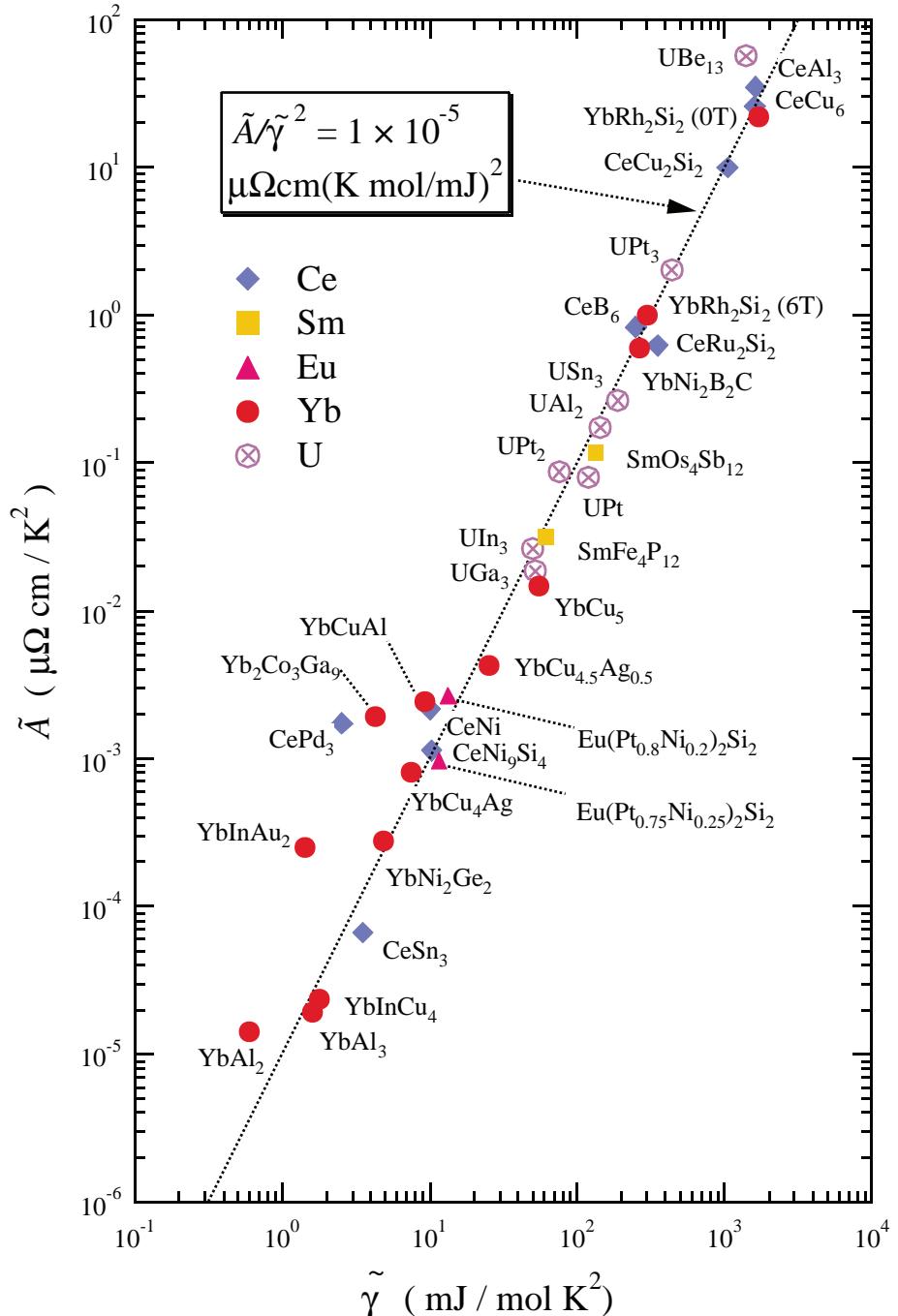
$$m^* = m(1 + \frac{1}{3}F_1^S)$$

With orbital degeneracy:

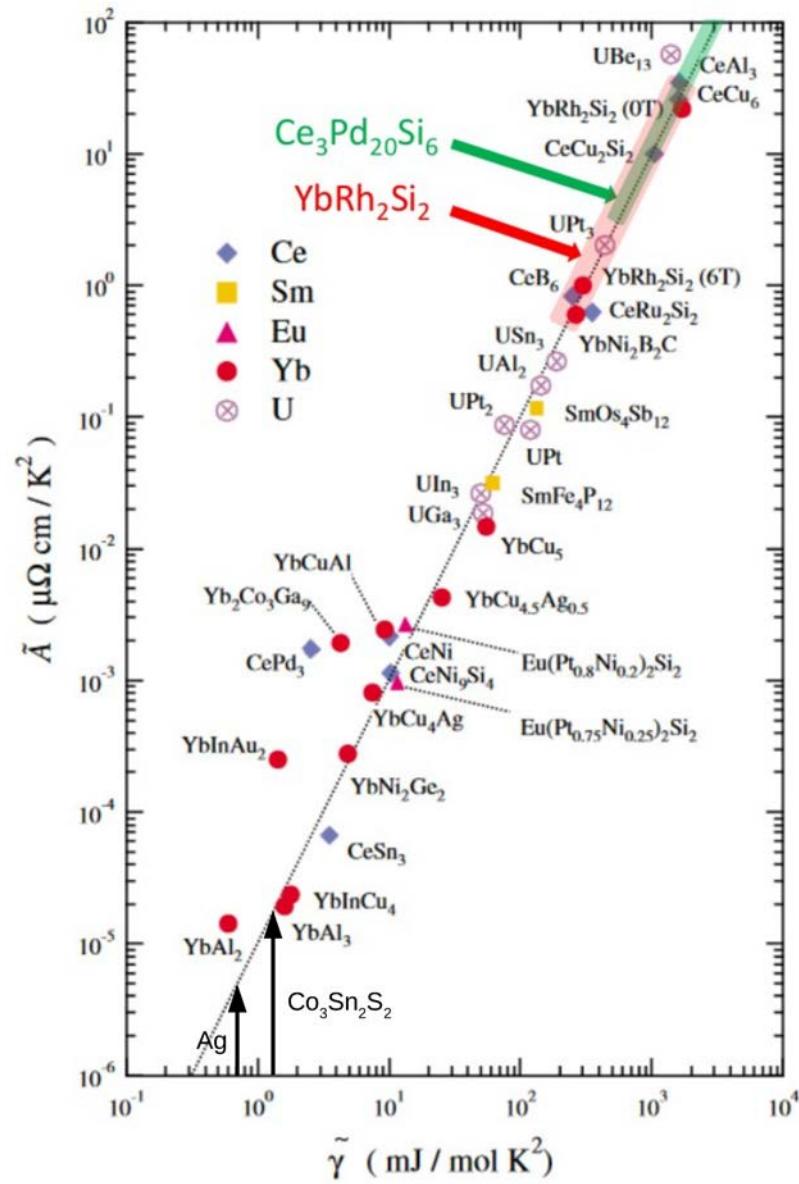
$$\tilde{A} = \frac{A}{\frac{1}{2}N(N-1)}$$

$$\tilde{\gamma} = \frac{\gamma}{\frac{1}{2}N(N-1)}$$

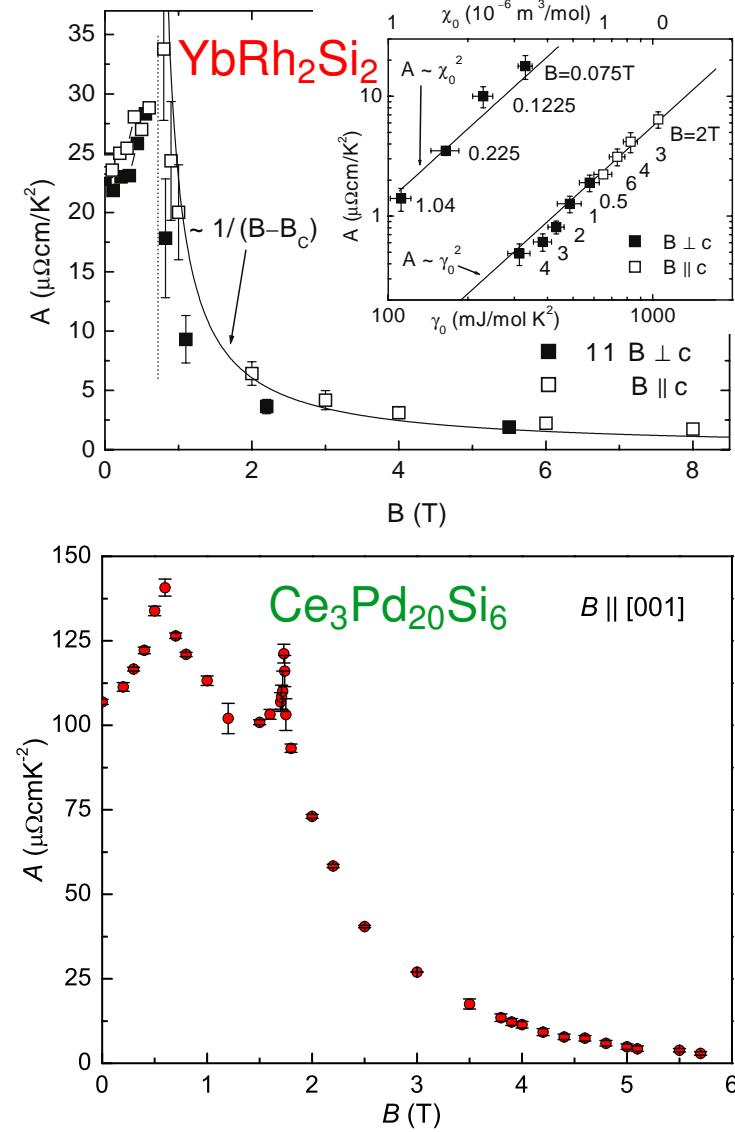
(Tsujii et al., Phys. Rev. Lett. 94 (2005) 057201) →



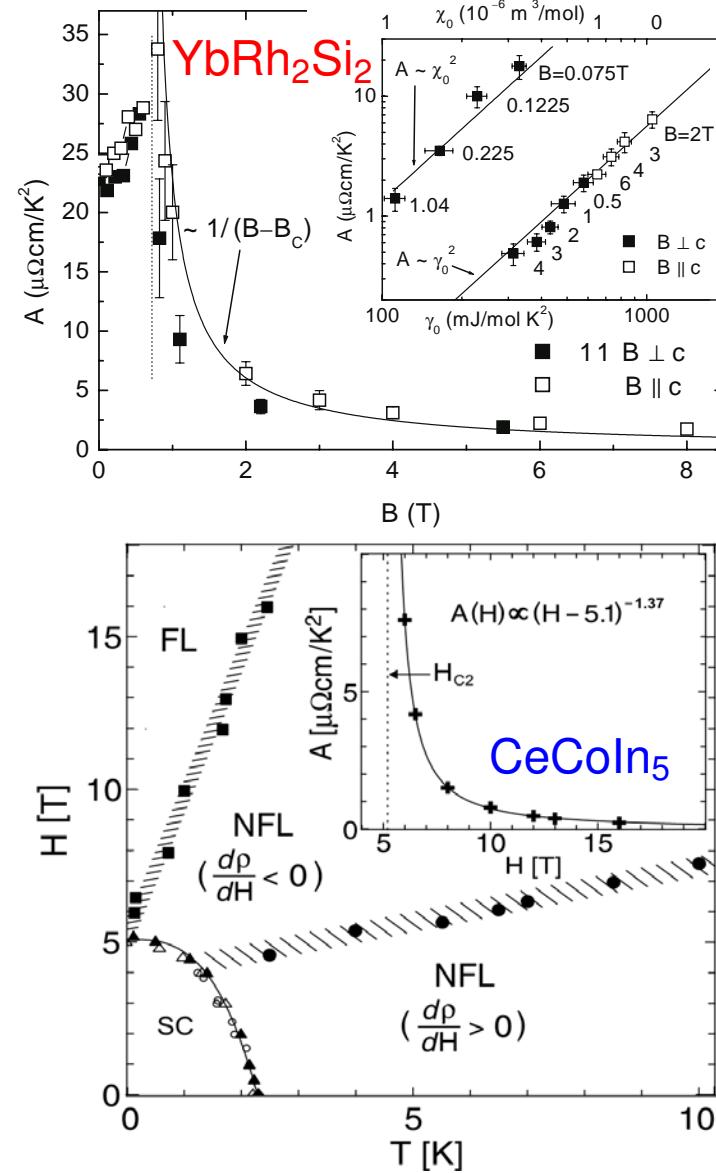
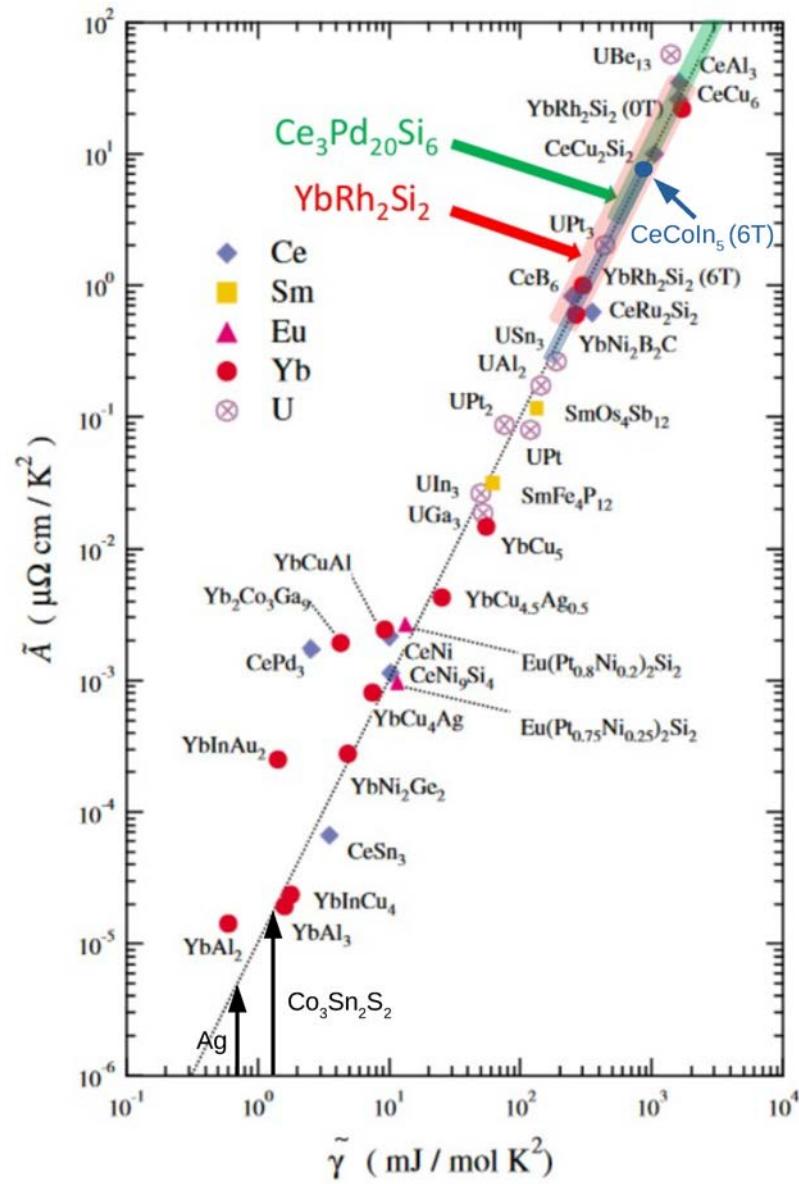
# Discontinuities appear upon tuning: FL parameters diverge



(SP & Si, Nat. Rev. Phys. 3 (2021) 9, and refs. therein)

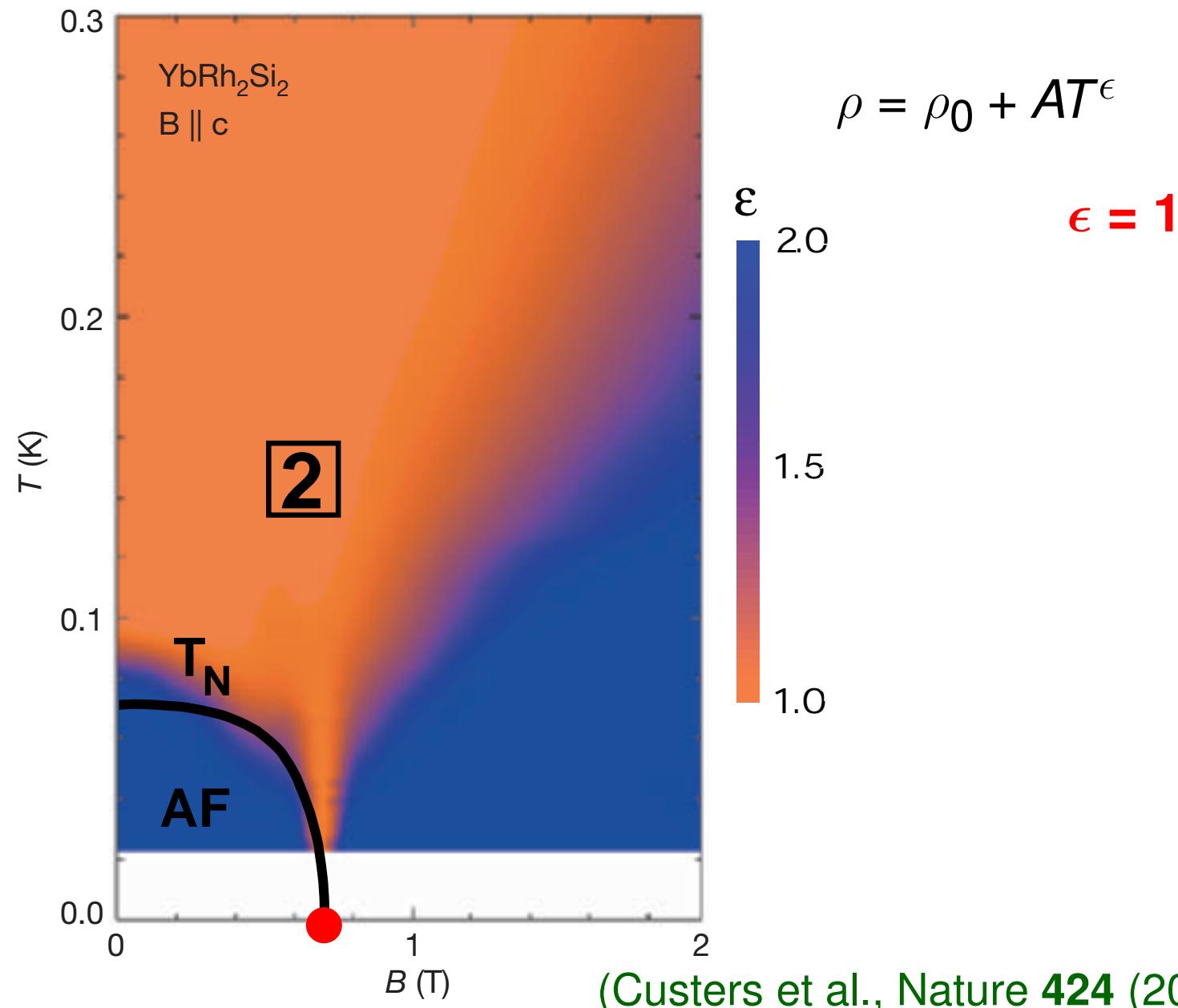


# Discontinuities appear upon tuning: FL parameters diverge



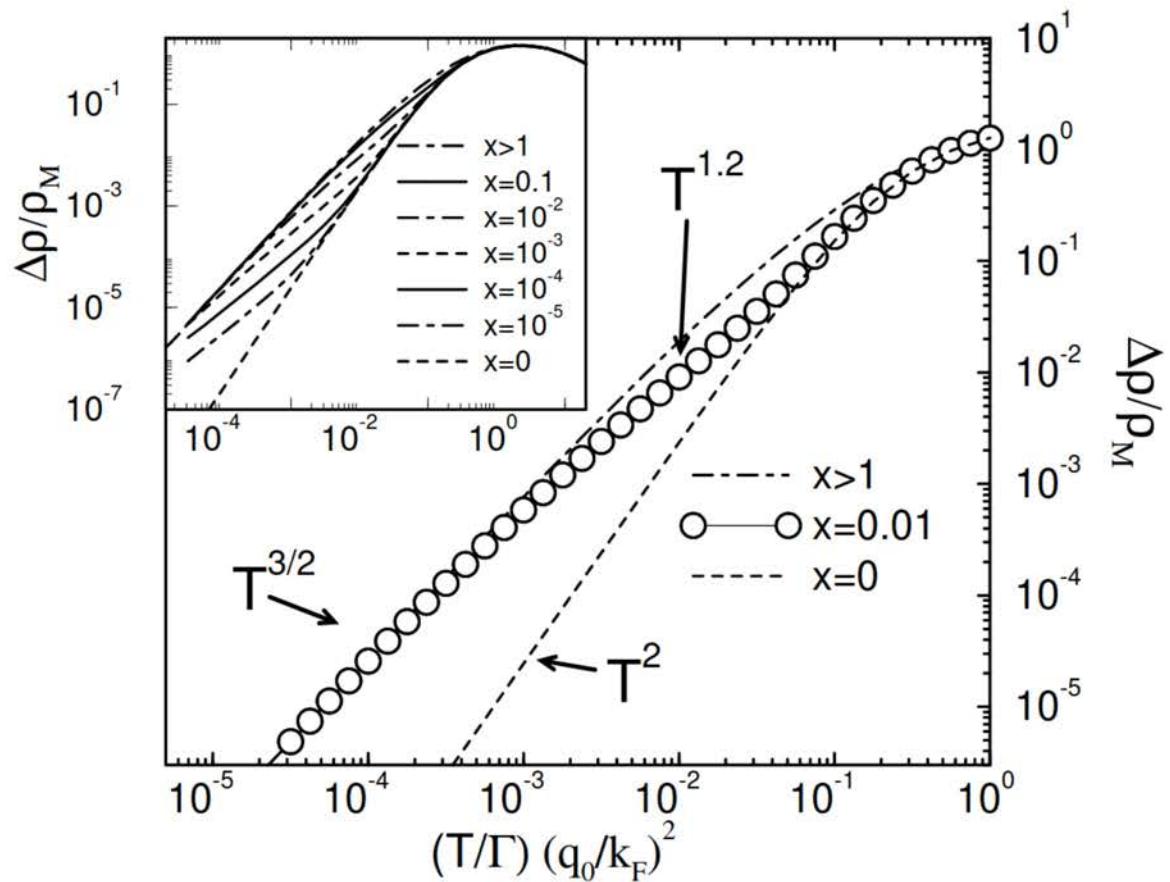
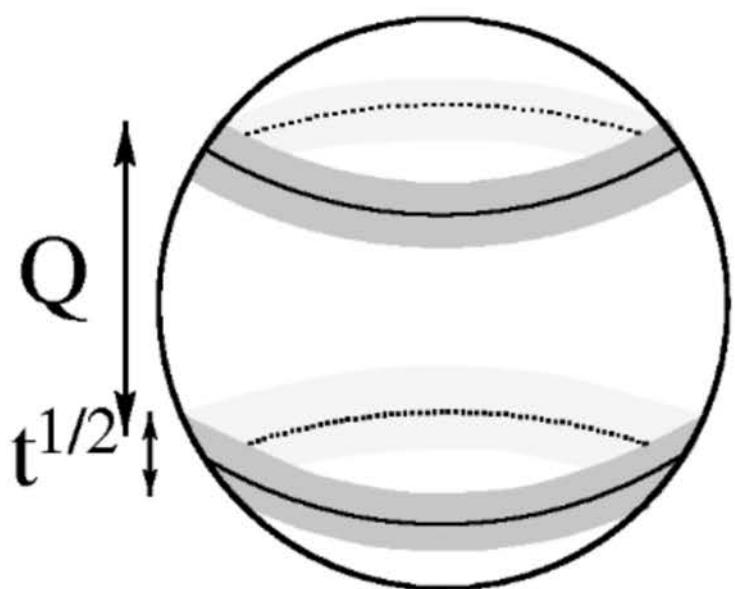
(Nat. Rev. Phys. 3 (2021) 9; Paglione et al., Phys. Rev. Lett. 24 (2003) 246405)

# $\text{YbRh}_2\text{Si}_2$ : A model quantum critical heavy fermion metal



# “Normal” QCPs follow Ginzburg, Landau, Wilson paradigm

## Predictions for electrical resistivity



No linear resistivity

$x = 0$ : clean limit

$x > 1$ : dirty limit

(Rosch, Phys. Rev. Lett. 82 (1999) 4280)

# “Normal” QCPs follow Ginzburg, Landau, Wilson paradigm

## Predictions for some thermodynamic properties

	$d = 2$	$d = 3$	$d = 2$	$d = 3$
	$z = 2$	$z = 2$	$z = 3$	$z = 3$
$\alpha_{\text{cr}} \sim$	$\ell n \ell n \frac{1}{T}$	$T^{1/2}$	$\ell n \frac{1}{T}$	$T^{1/3}$
$C_{\text{cr}} \sim$	$T \ell n \frac{1}{T}$	$-T^{3/2}$	$T^{2/3}$	$T \ell n \frac{1}{T}$
$\Gamma_{r,\text{cr}} \sim$	$\frac{\ell n \ell n \frac{1}{T}}{T \ell n \frac{1}{T}}$	$-T^{-1}$	$T^{-2/3} \ell n \frac{1}{T}$	$\left(T^{2/3} \ell n \frac{1}{T}\right)^{-1}$

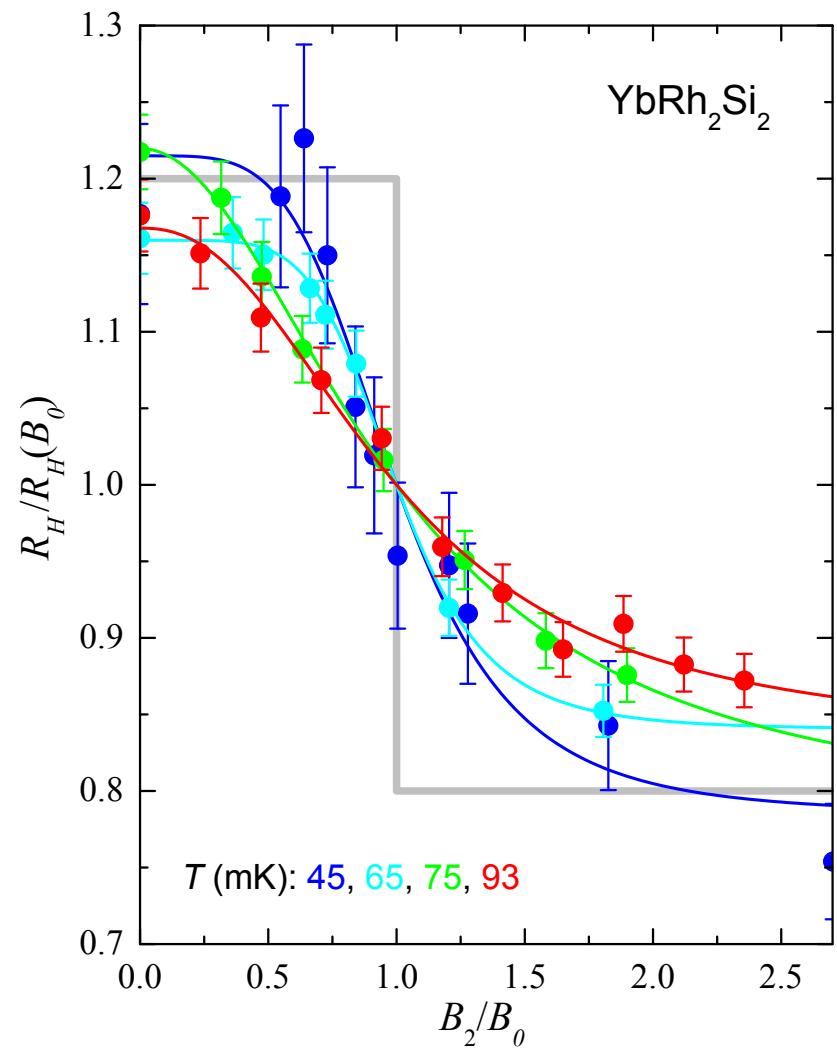
$d$ : dimension,  $z = 2$ : AFM metal,  $z = 3$ : FM metal

$\alpha$ : thermal expansion,  $C$ : specific heat,  $\Gamma = \alpha/C$ : Grüneisen ratio

**No hyperscaling above the upper critical dimension**

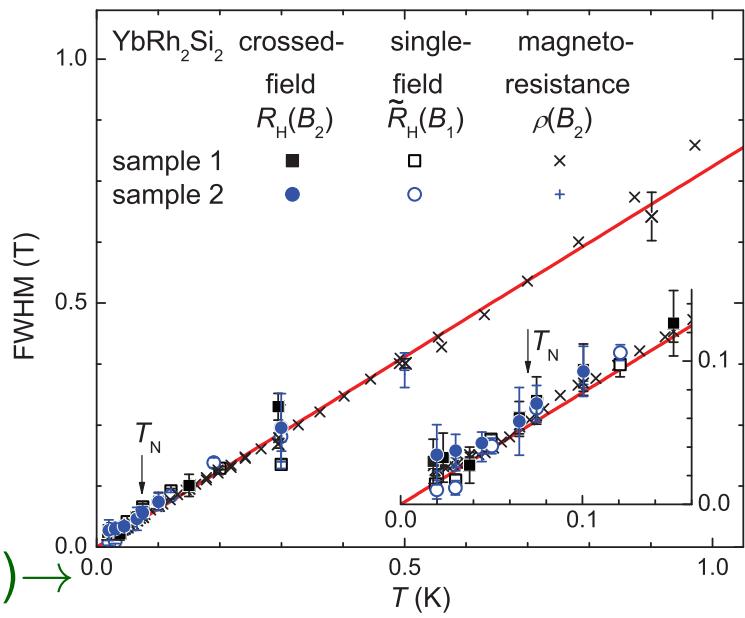
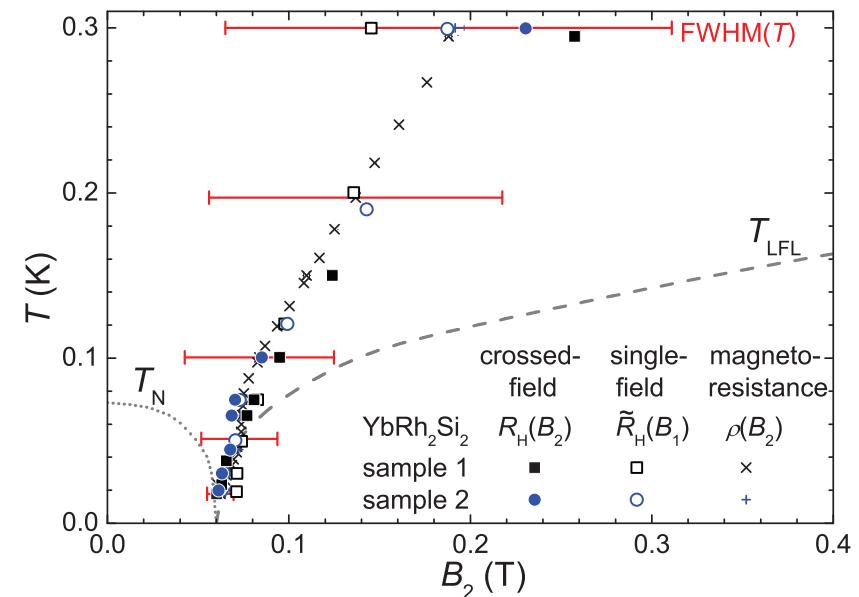
(v. Löhneysen et al., Rev. Mod. Phys. 79 (2007) 1015; Hertz & Millis)

# Evolution of Hall effect across the QCP: $\text{YbRh}_2\text{Si}_2$

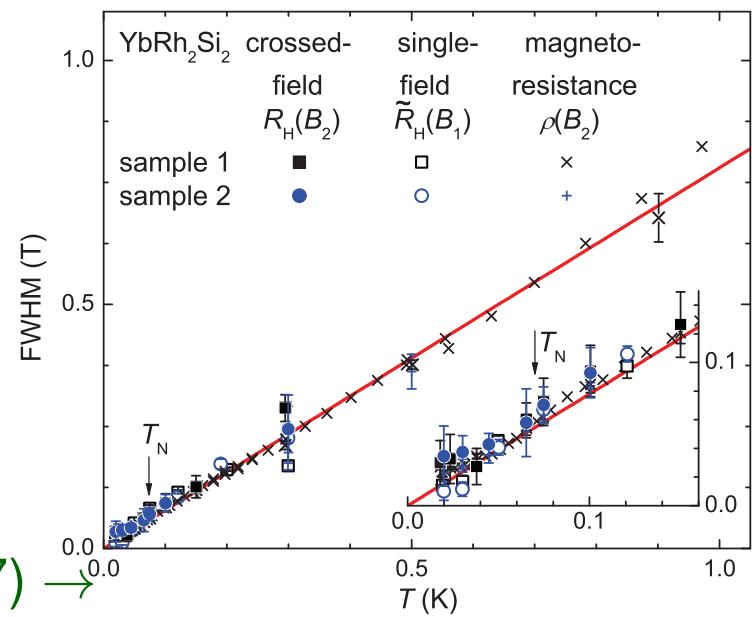
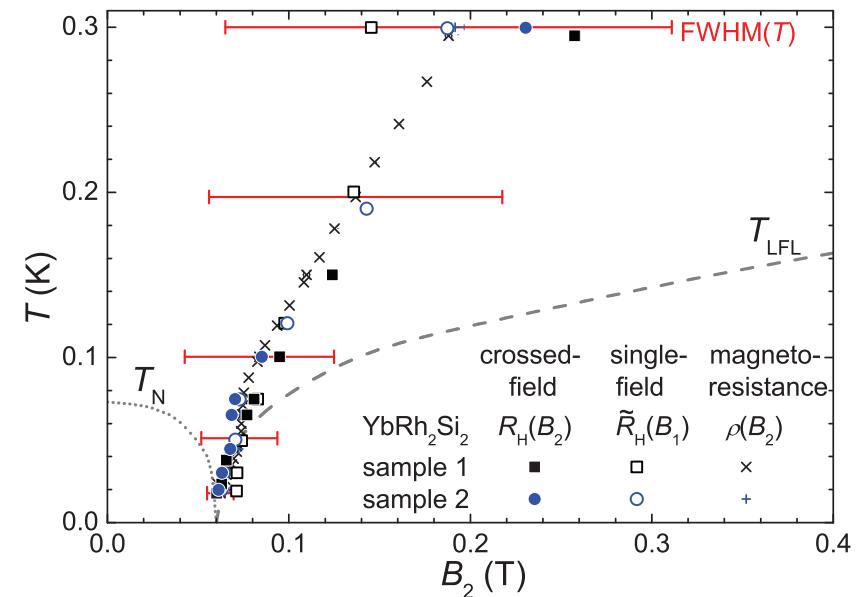
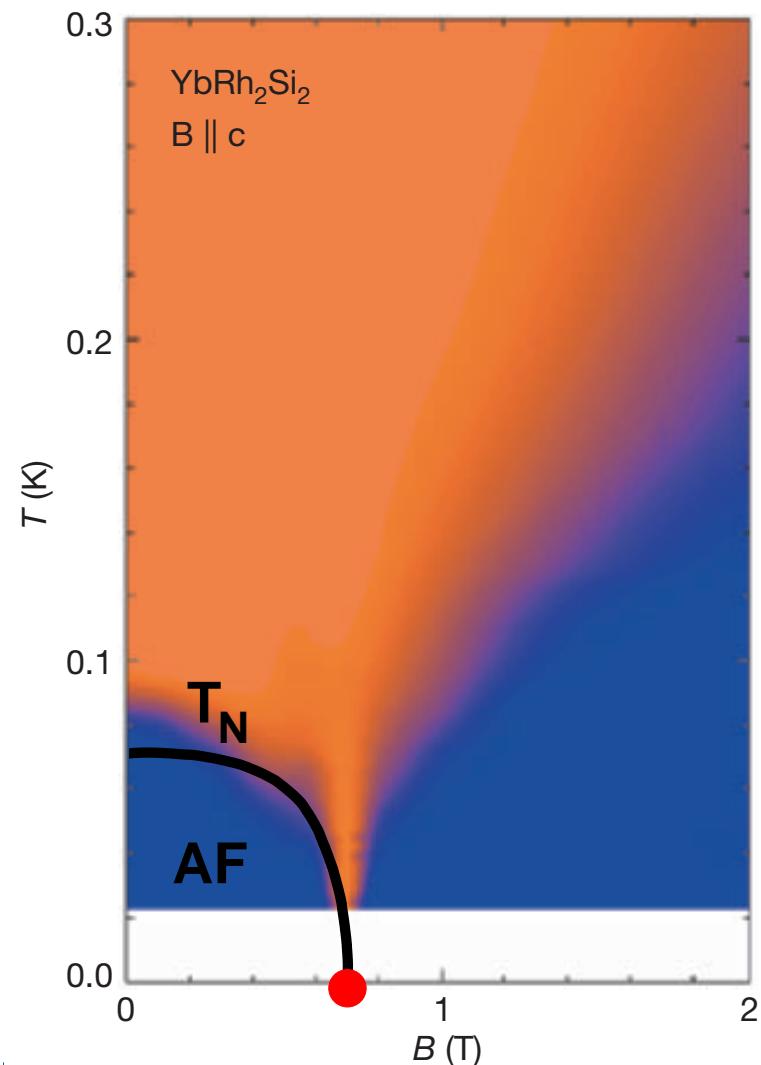


(SP et al., Nature 432 (2004) 881) ↑

(Friedemann et al., PNAS 107 (2010) 14547) →



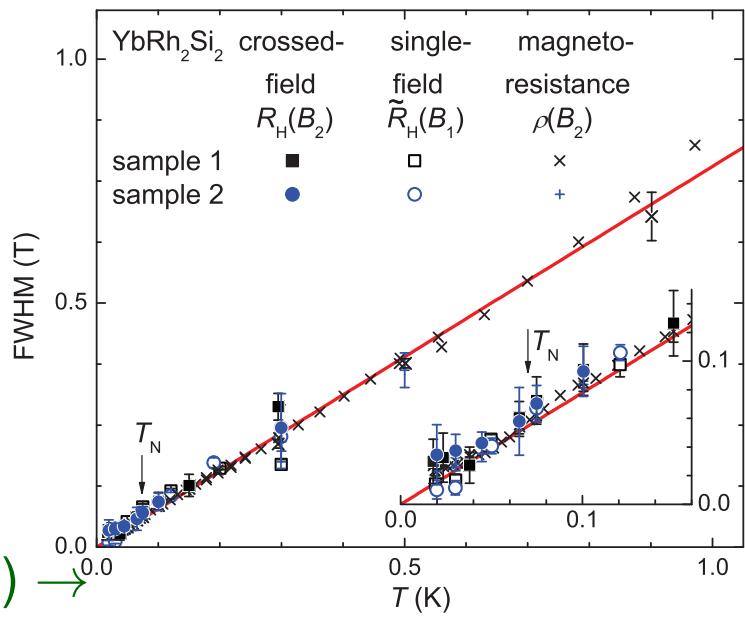
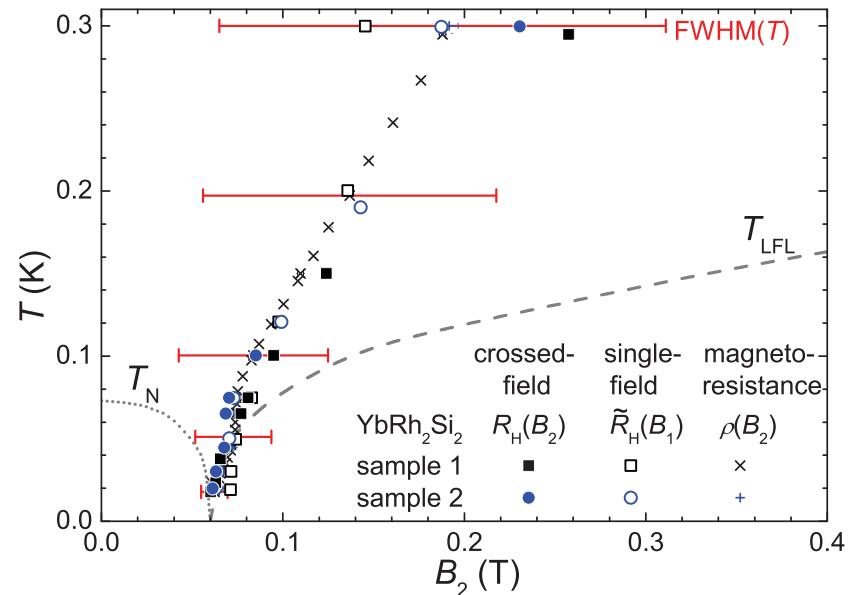
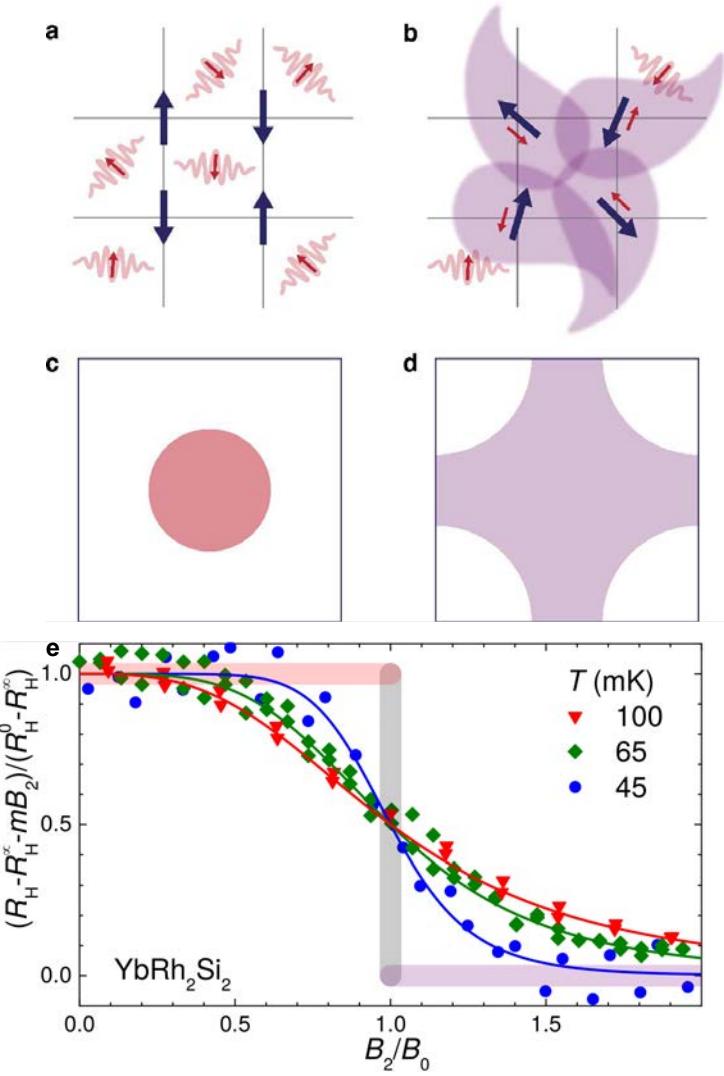
# Relation of Hall crossover and NFL behavior in $\rho(T)$



(Custers et al., Nature 424 (2003) 524) ↑

(Friedemann et al., PNAS 107 (2010) 14547) →

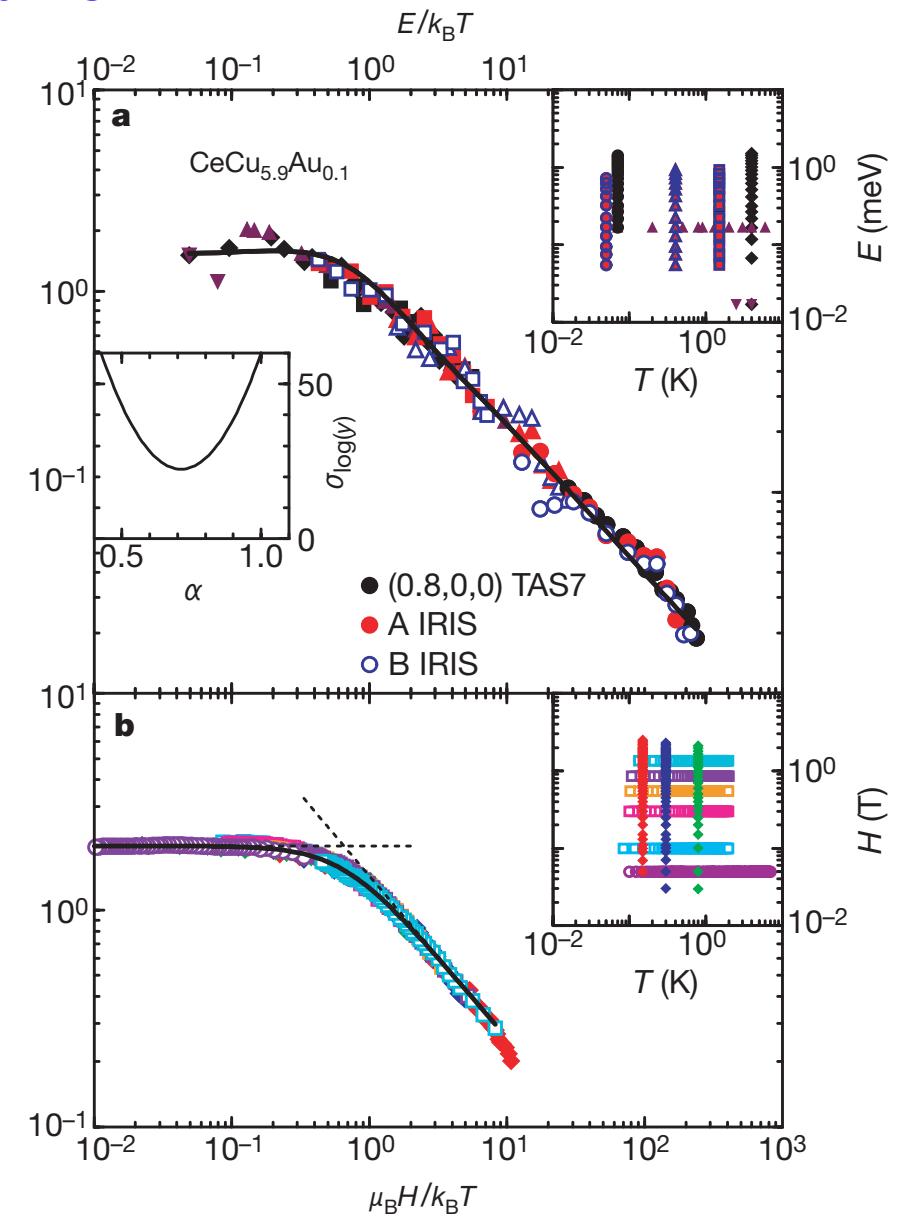
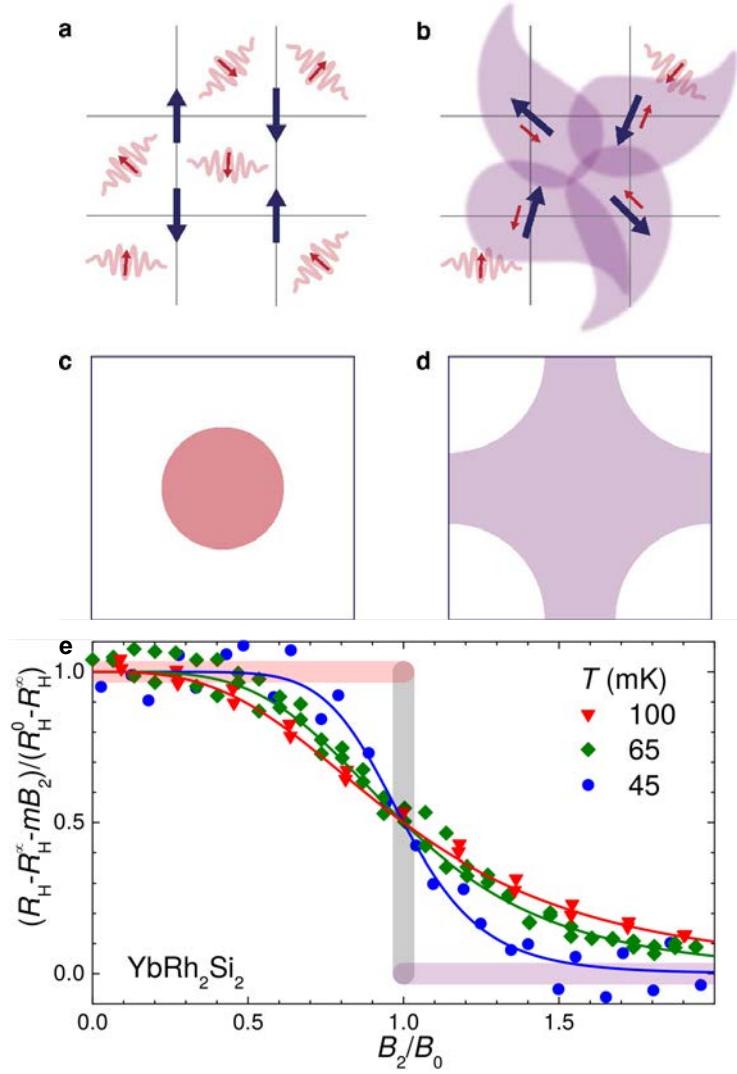
# Kondo destruction QCP scenario



(SP & Si, Nat. Rev. Phys. 3 (2021) 9) ↑

(Friedemann et al., PNAS 107 (2010) 14547) →

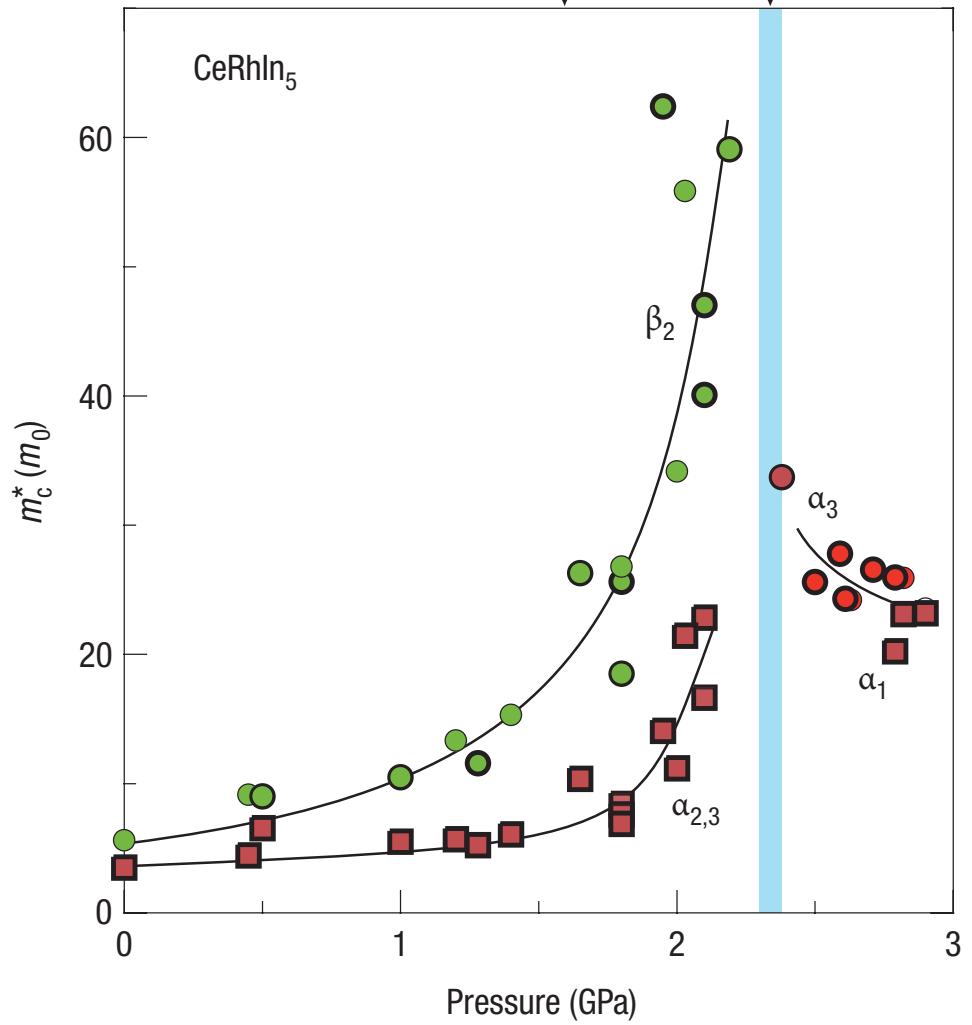
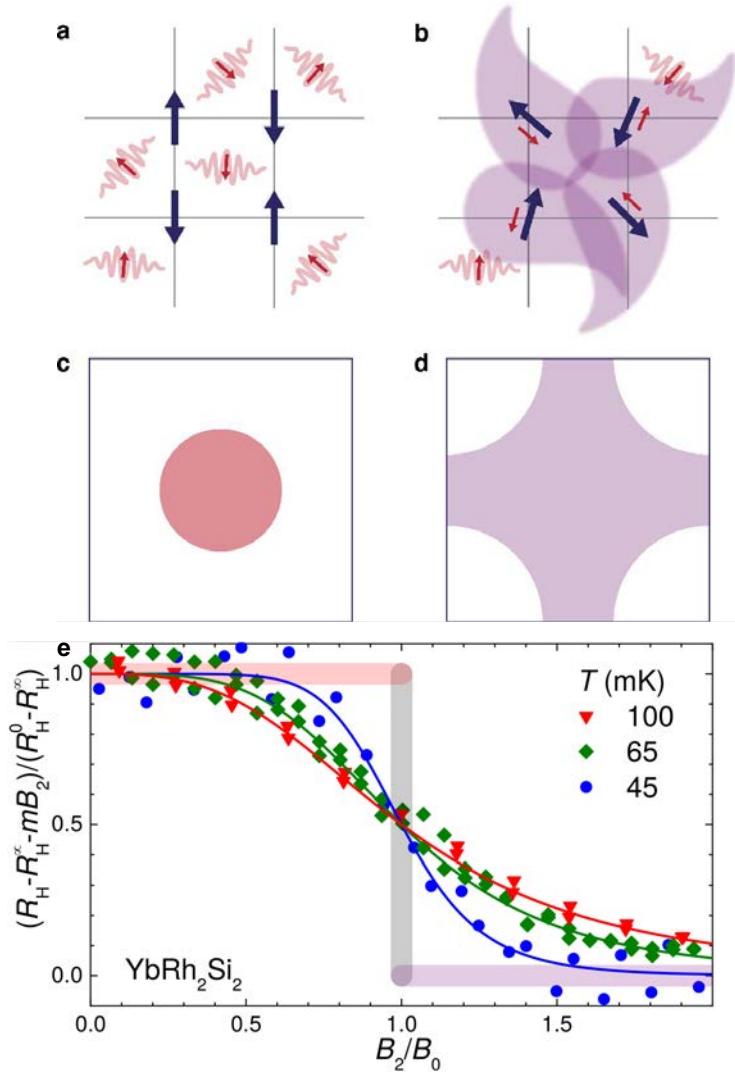
# Kondo destruction QCP scenario



(SP & Si, Nat. Rev. Phys. 3 (2021) 9) ↑

(Coleman et al., JPCM 13 (2001) R723; Schröder et al., Nature 407 (2000) 351)

# Kondo destruction QCP scenario

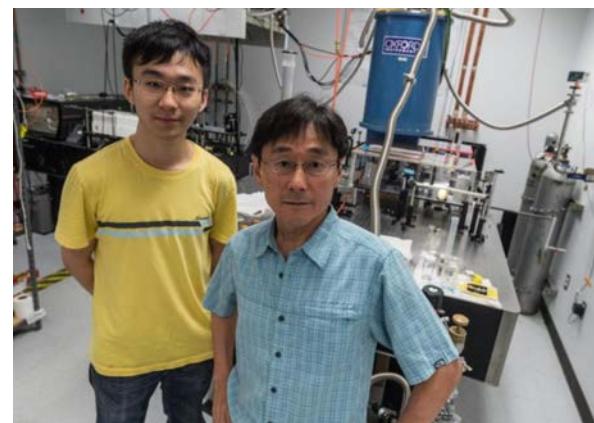


(SP & Si, Nat. Rev. Phys. 3 (2021) 9) ↑

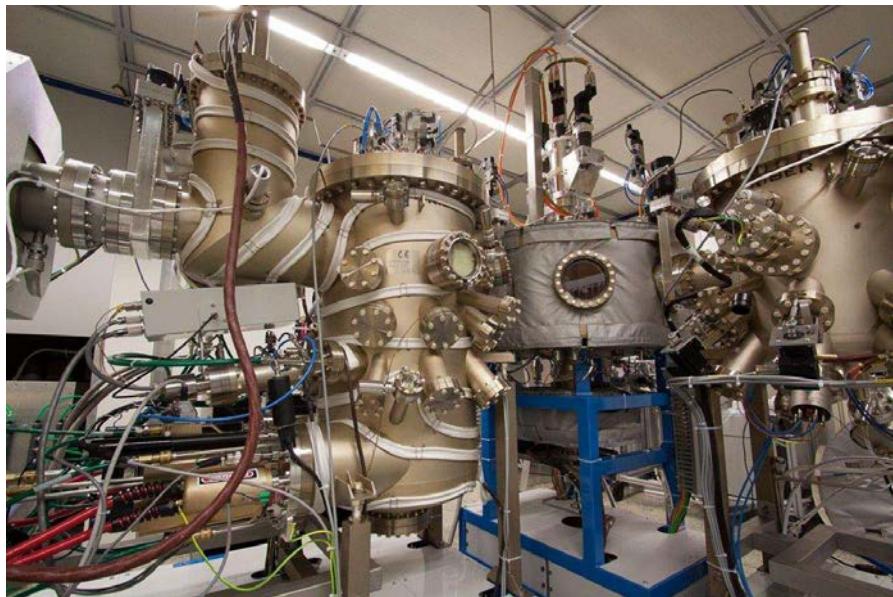
(Coleman et al., JPCM 13 (2001) R723; Shishido et al, JPSJ 74 (2005) 1103)

# Dynamical response: THz time-domain transmission spectroscopy

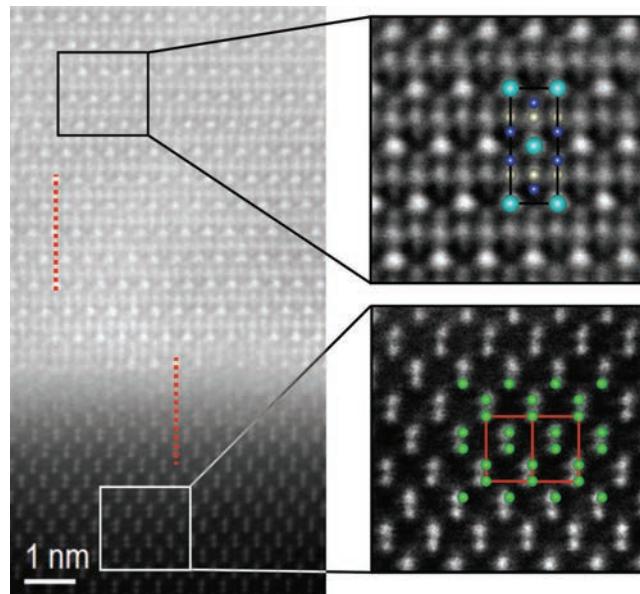
- Real and imag. part of  $\sigma(\omega)$
- No Kramers-Kronig transformation
- Thin films needed!



Molecular beam epitaxy system



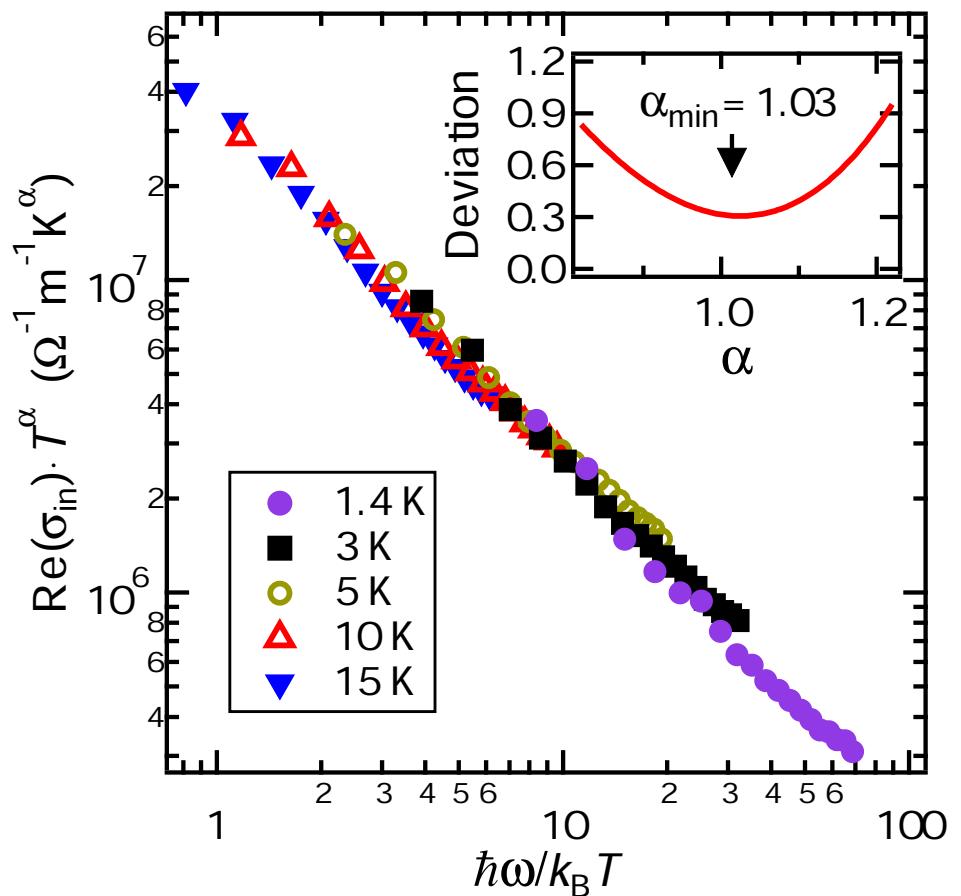
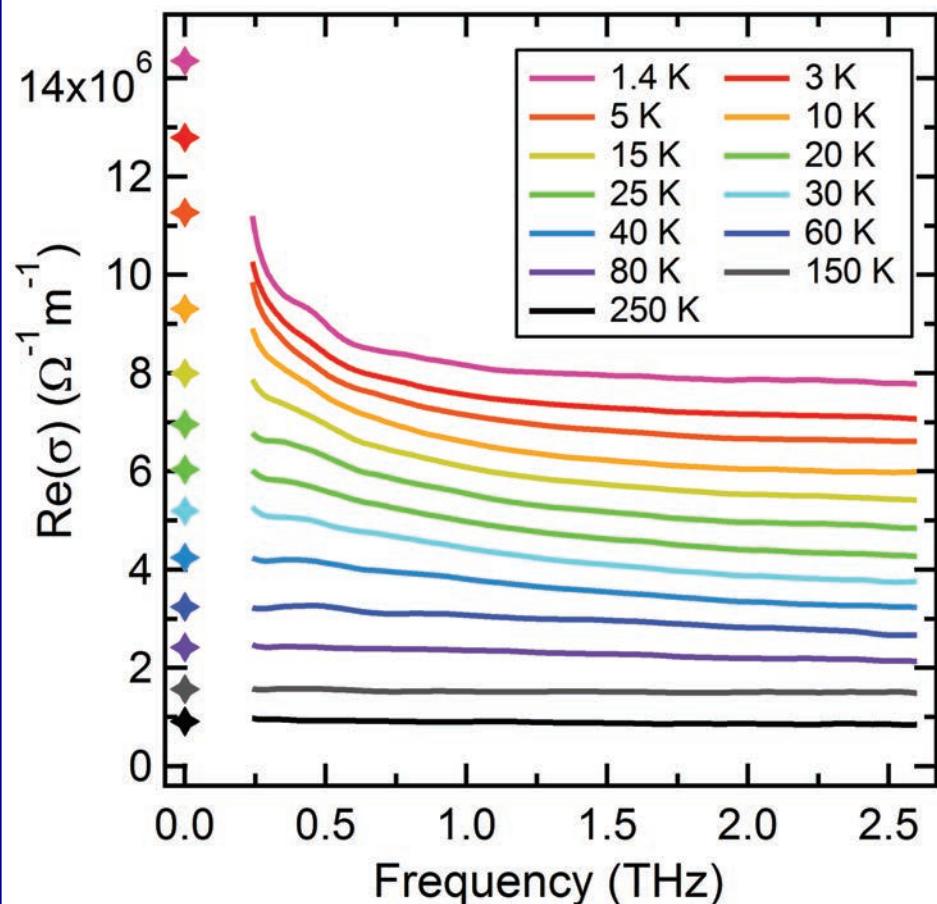
HAADF-STEM image



(Prochaska et al., Science 367 (2020) 285)

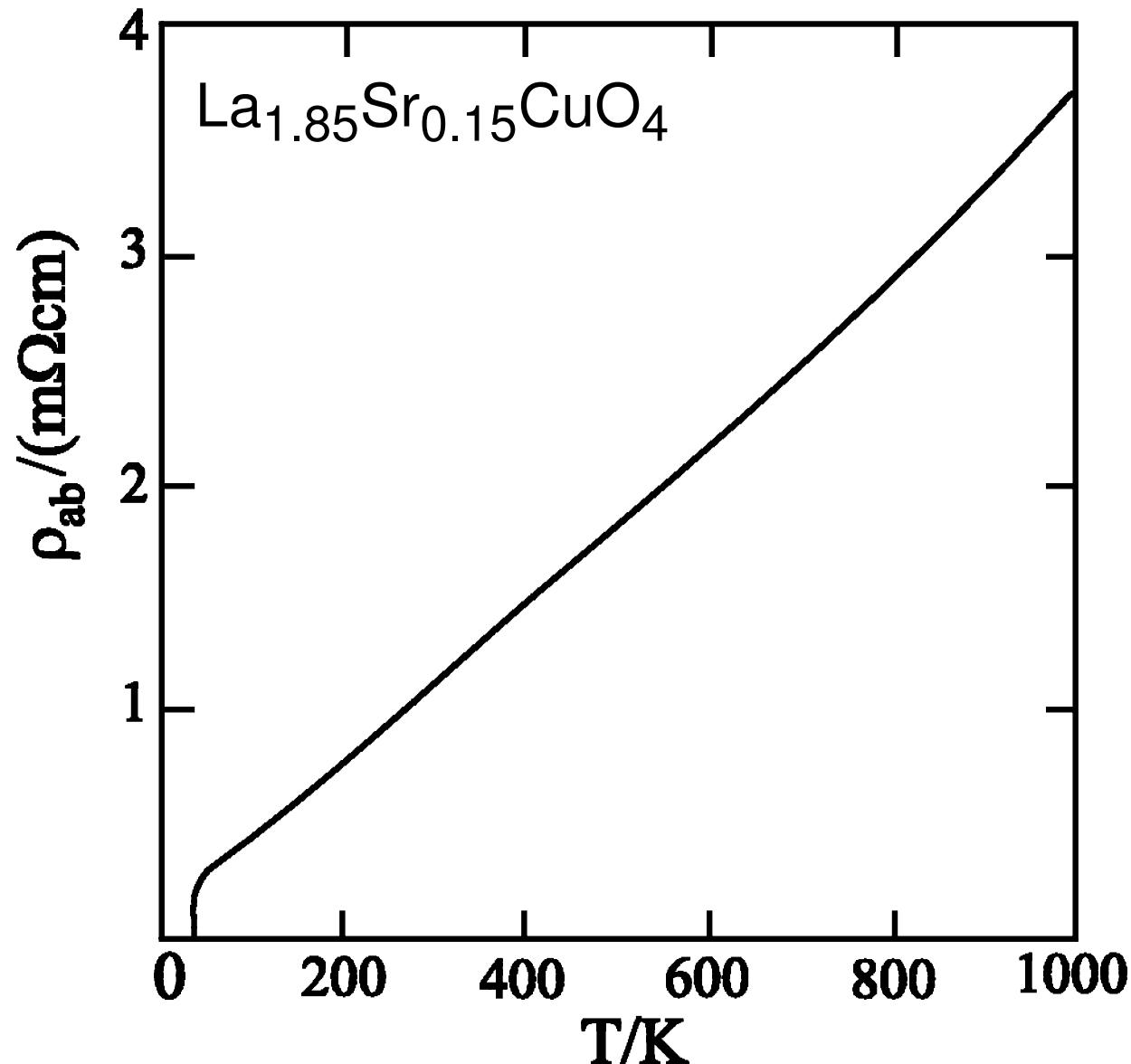
# Dynamical scaling in quantum critical YbRh<sub>2</sub>Si<sub>2</sub>

THz time-domain transmission spectroscopy on MBE films of YbRh<sub>2</sub>Si<sub>2</sub>



(Prochaska et al., Science 367 (2020) 285)

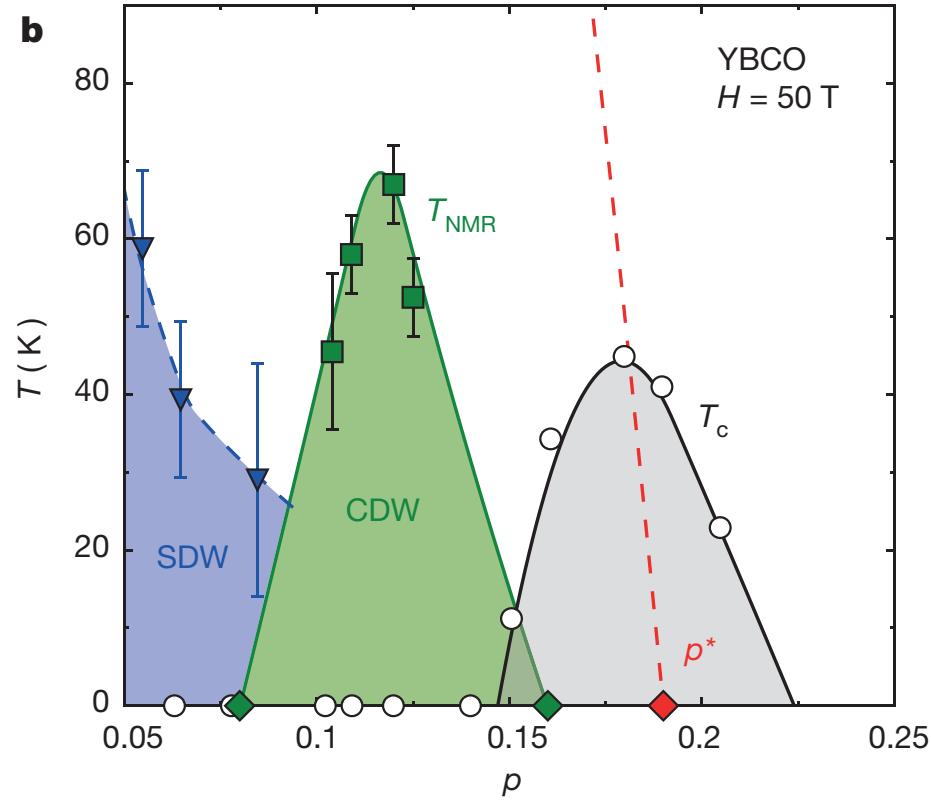
## Relation to the high- $T_c$ cuprates: Strange metal behavior



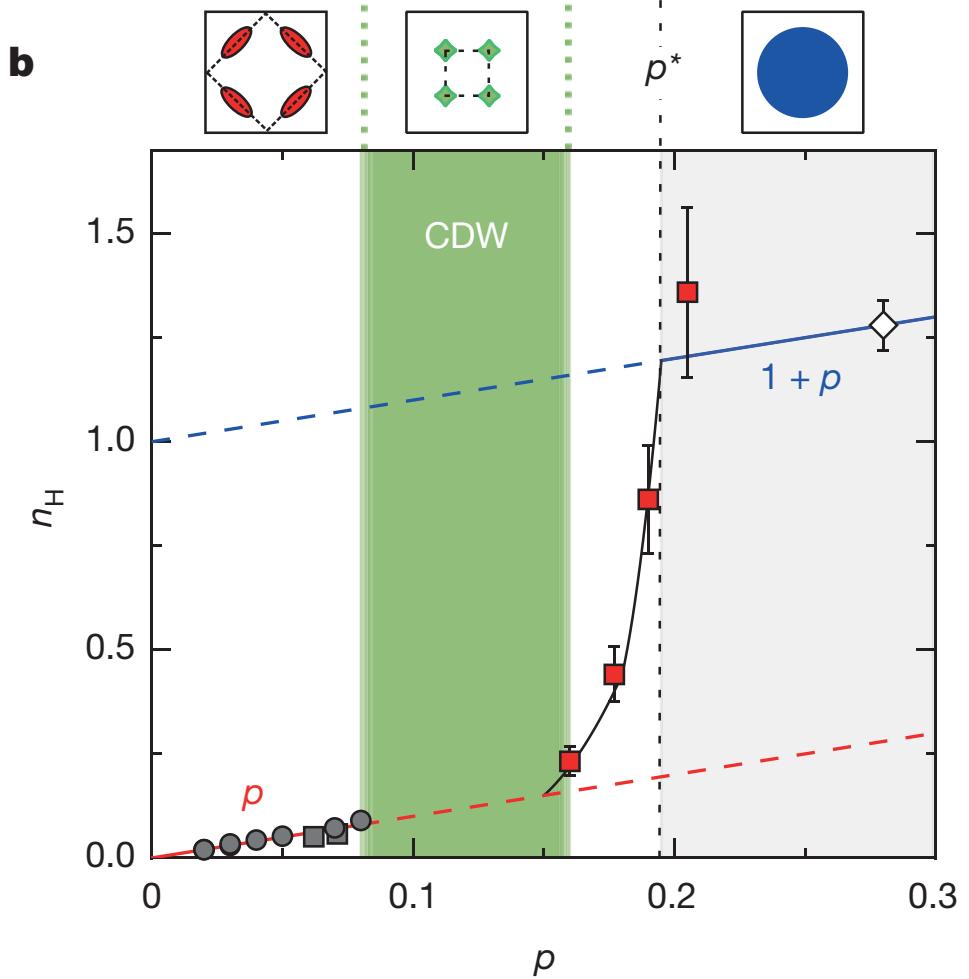
(Takagi et al., Phys. Rev. Lett. 69 (1992) 2975)

# Relation to the high- $T_c$ cuprates: Carrier (de)localization

Phase diagram at 50 T



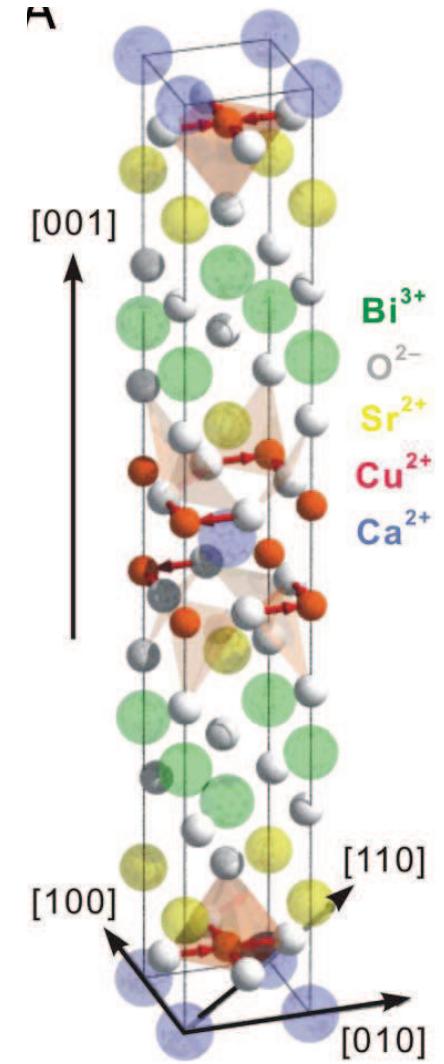
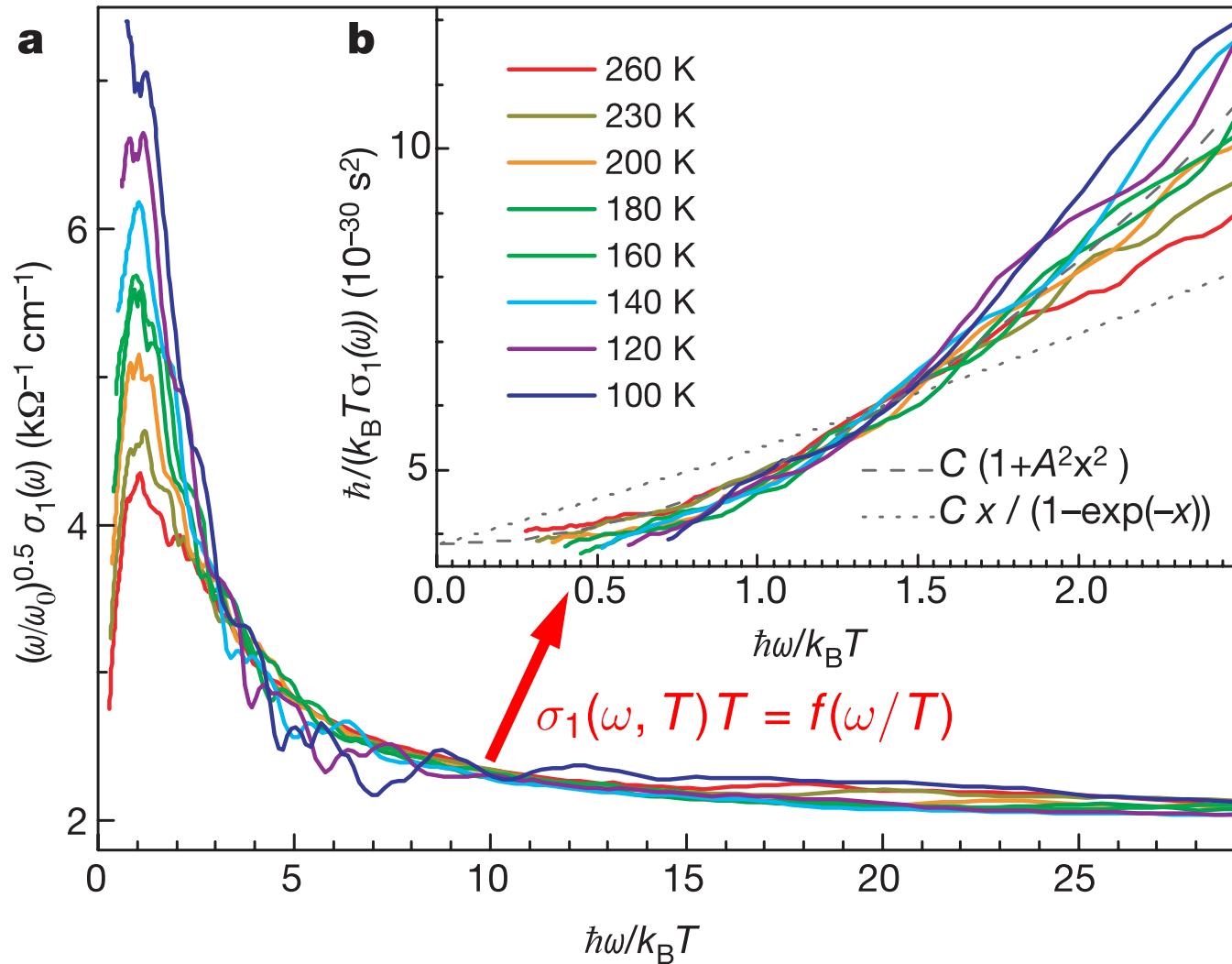
Change of carrier concentration



(Badoux et al., Nature 531 (2016) 210)

# Relation to the high- $T_c$ cuprates: Dynamical scaling in $\sigma(\omega)$

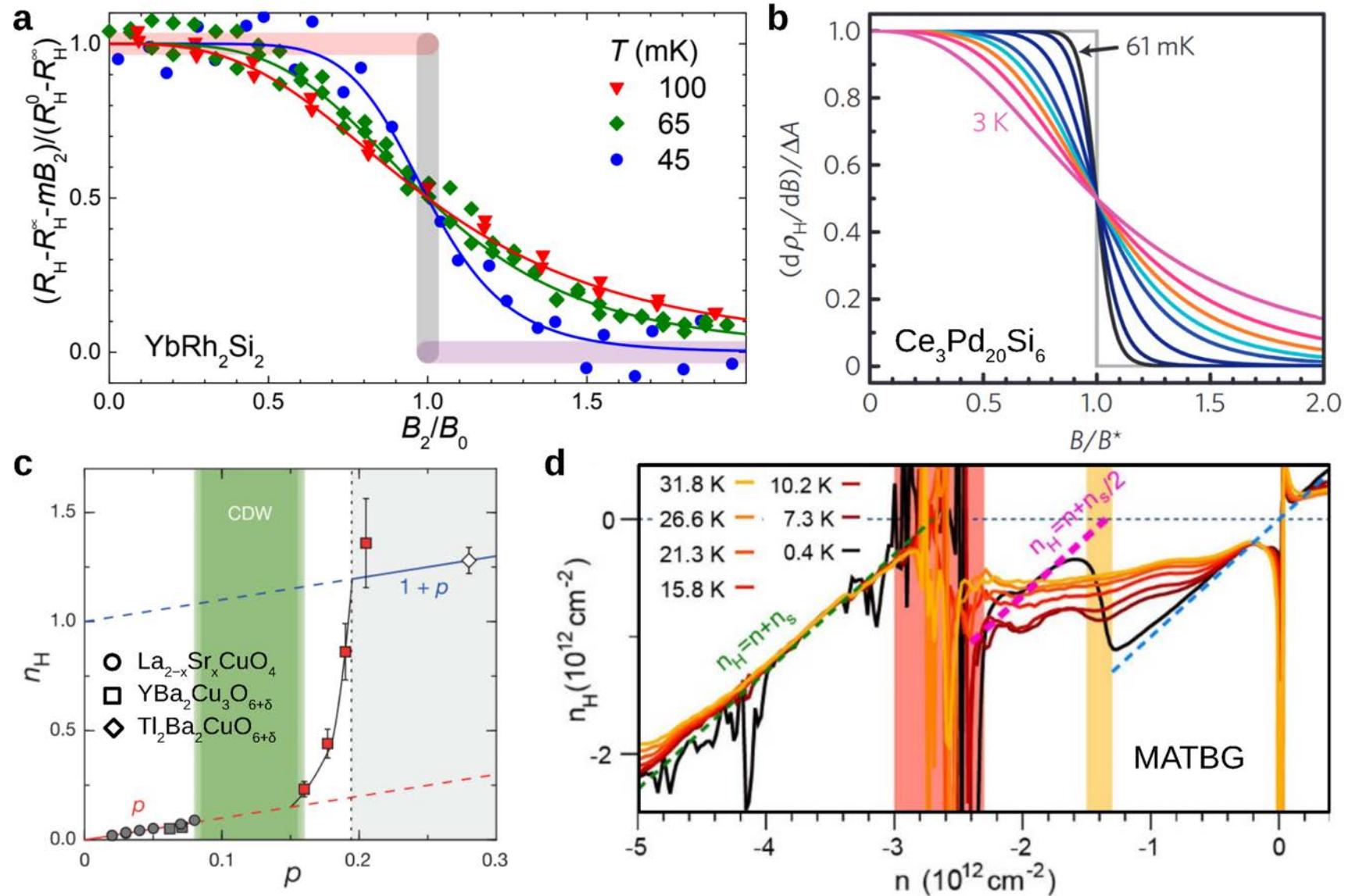
Optical conductivity of optimally doped  $\text{Bi}_{2.23}\text{Sr}_{1.9}\text{Ca}_{0.96}\text{Cu}_2\text{O}_{8+\delta}$



(van der Marel et al., Nature 425 (2003) 271)

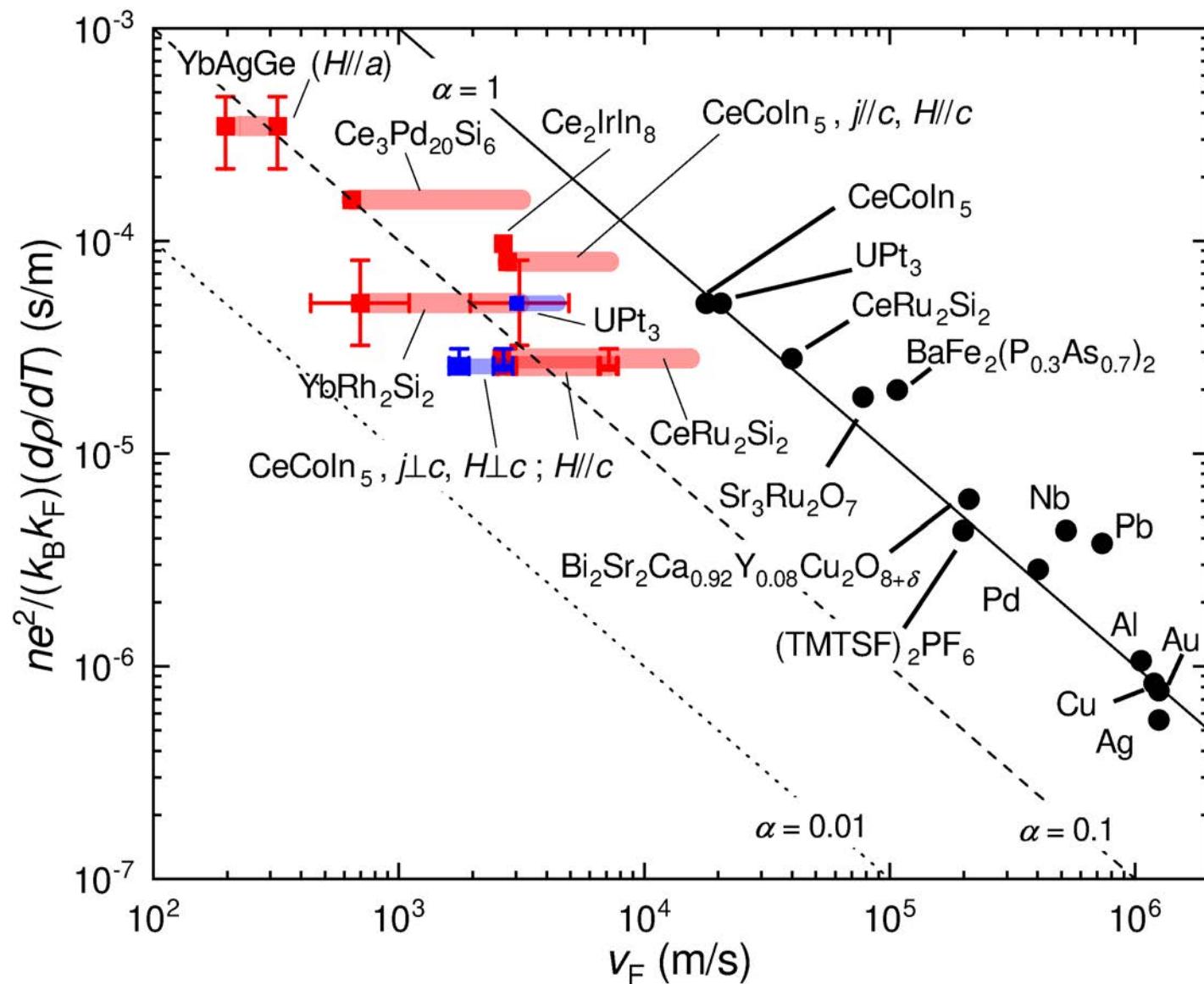
(Carbone et al., PNAS 2008)↑

# Carrier (de)localization in other SCES?



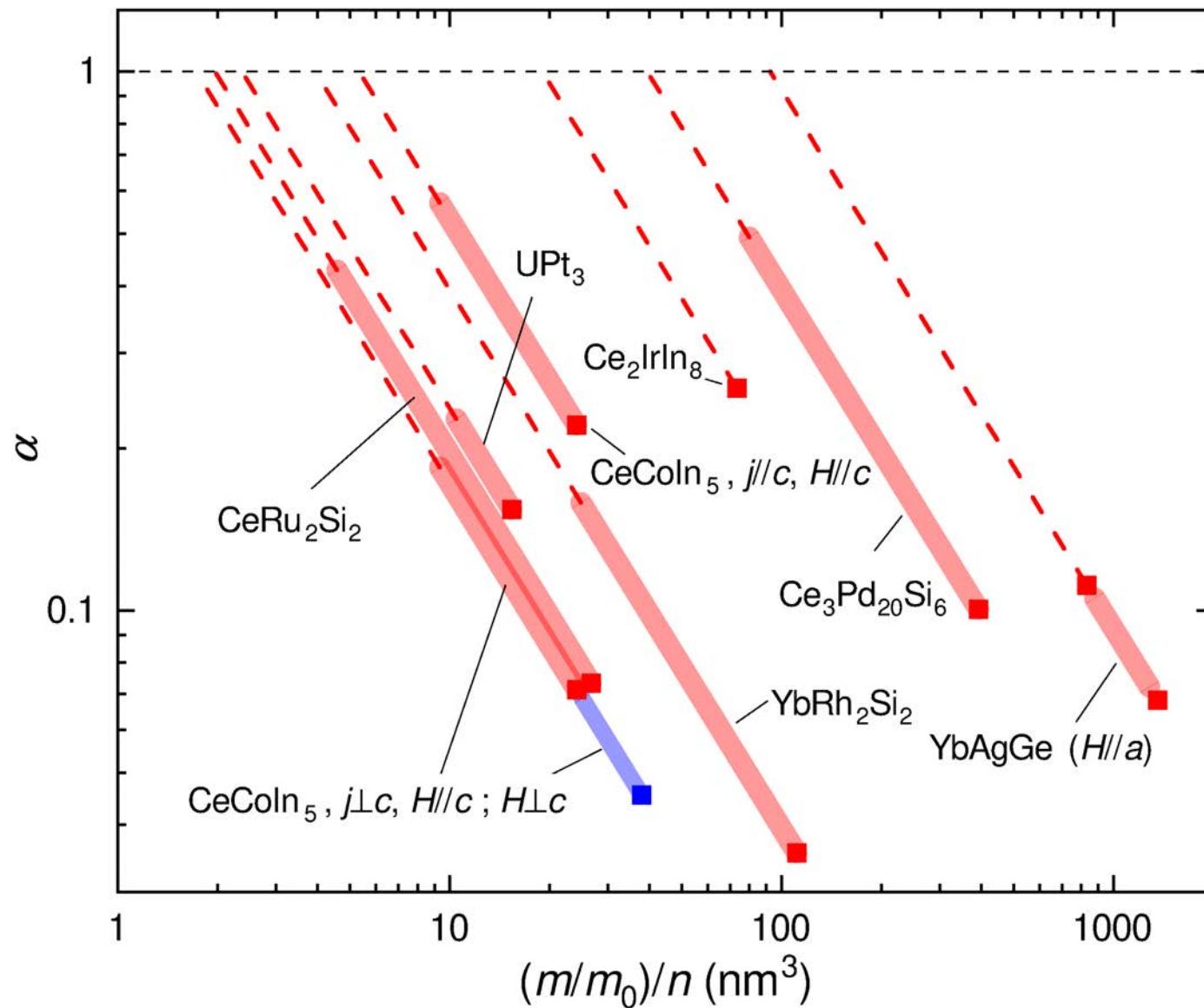
(Taupin & SP, Crystals 12 (2022) 251)

# Planckian dissipation in electrical transport?



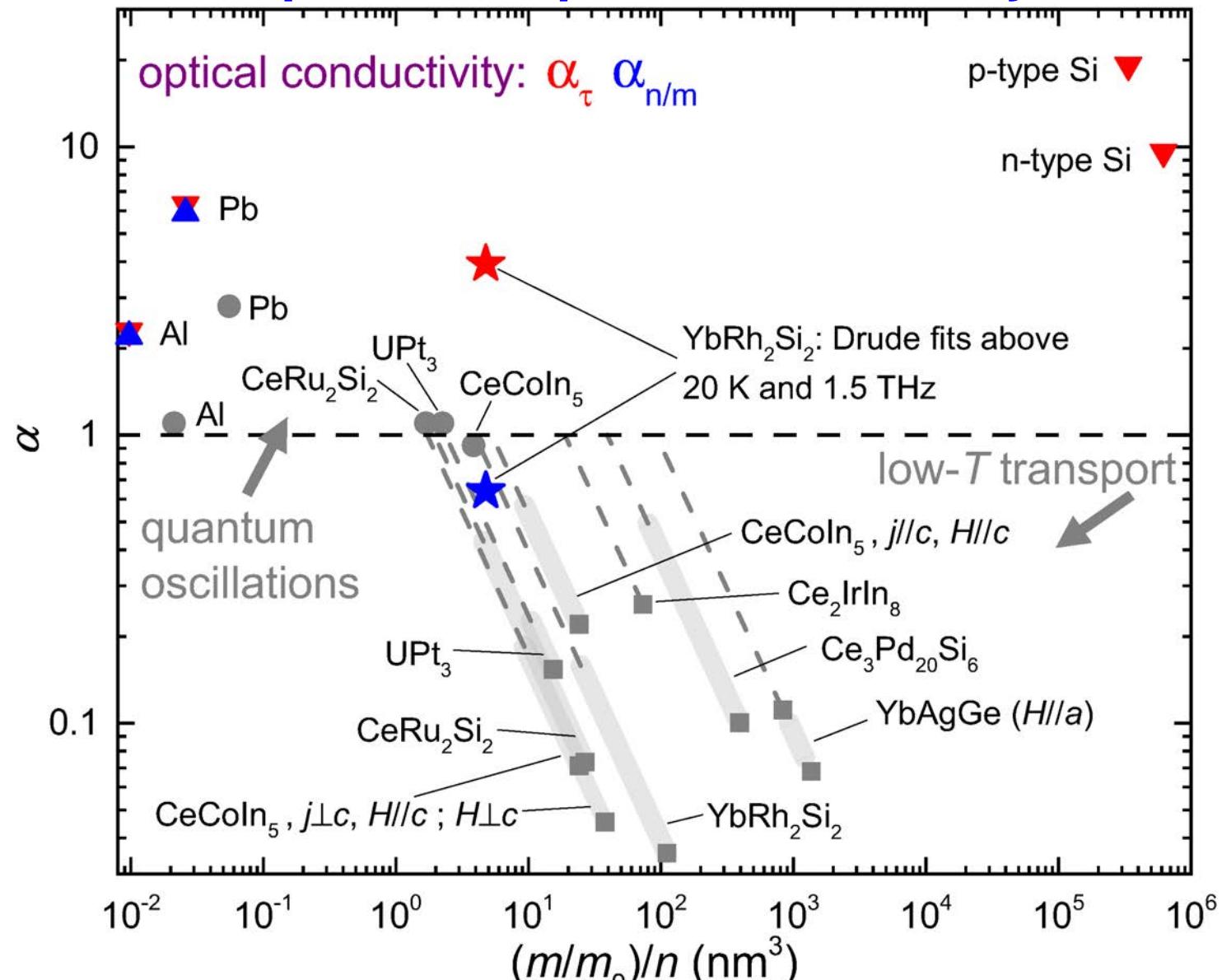
(Taupin & SP, Crystals 12 (2022) 251)

# Planckian dissipation in electrical transport?



(Taupin & SP, Crystals 12 (2022) 251)

# Planckian dissipation in optical conductivity?

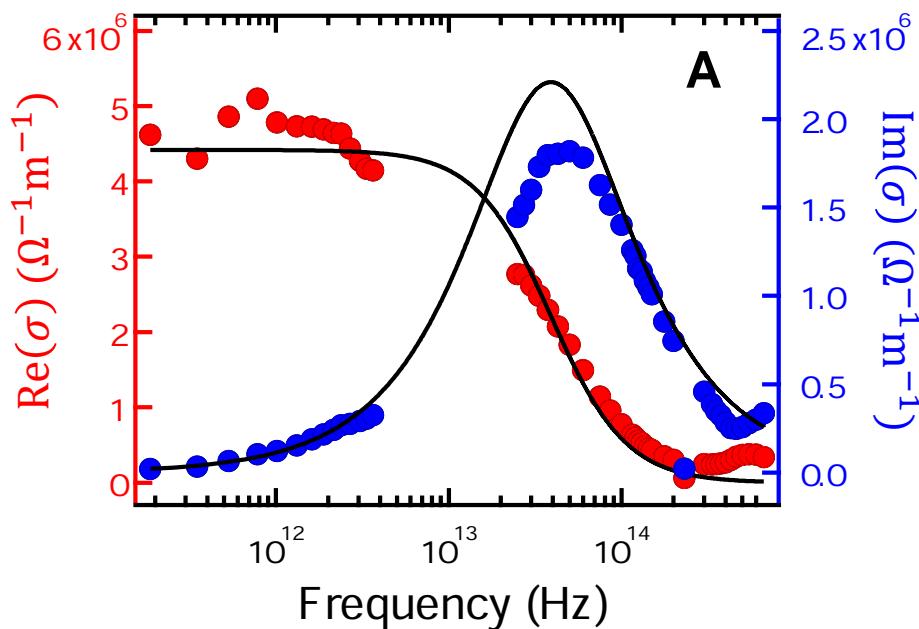


# Planckian dissipation in optical conductivity?

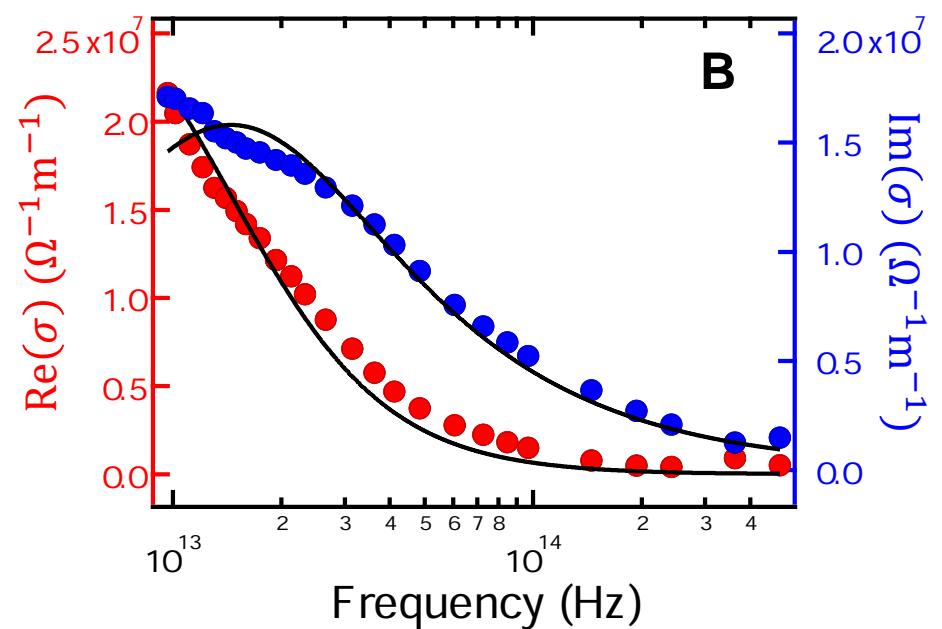
$$\text{Re}[\sigma(\omega)] = \sigma_1 = \frac{ne^2\tau}{m} \frac{1}{1 + \omega^2\tau^2}$$

$$\text{Im}[\sigma(\omega)] = \sigma_2 = \frac{ne^2\tau}{m} \frac{\omega\tau}{1 + \omega^2\tau^2}$$

Pb at room temperature



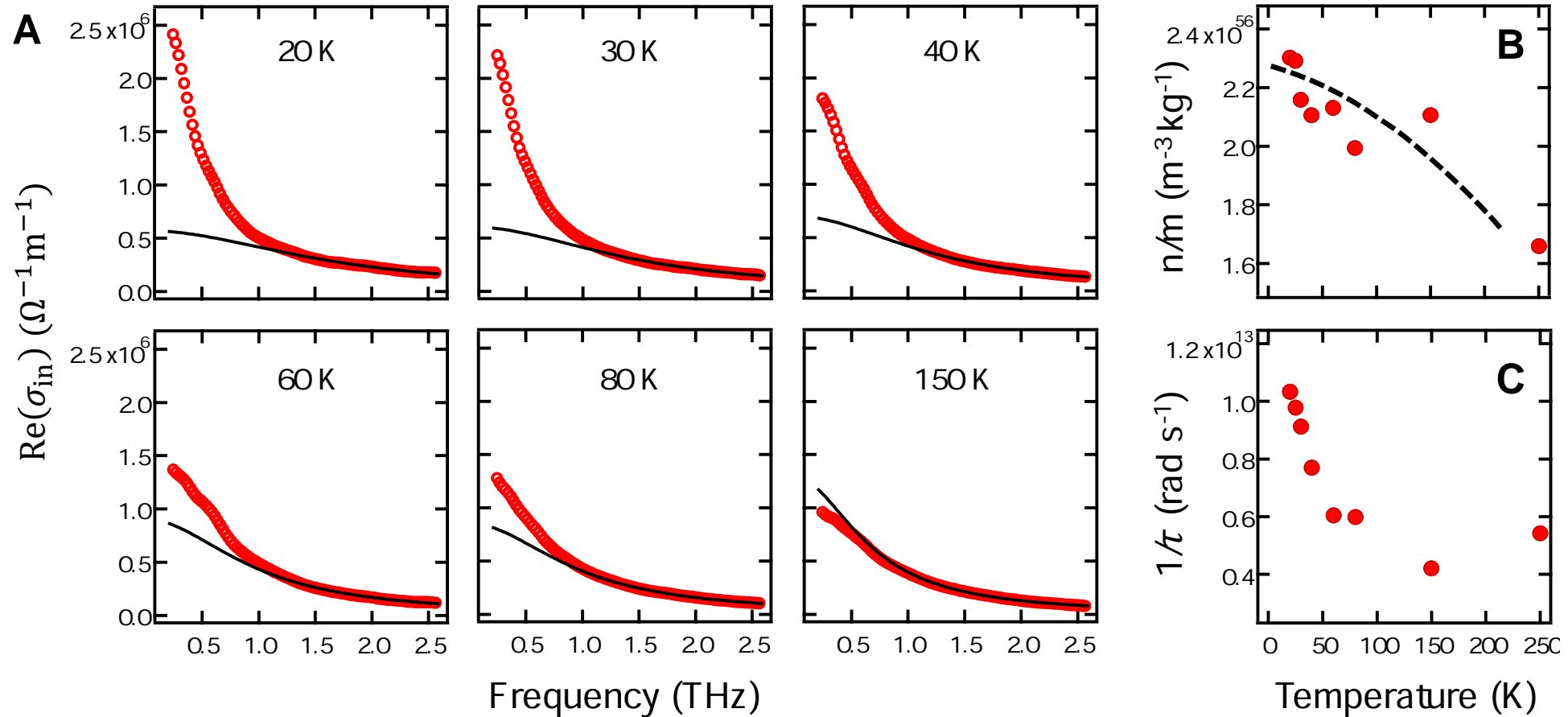
Al at room temperature



(Li, Kono, Si & SP, arXiv:2205.13382)

# Planckian dissipation in optical conductivity?

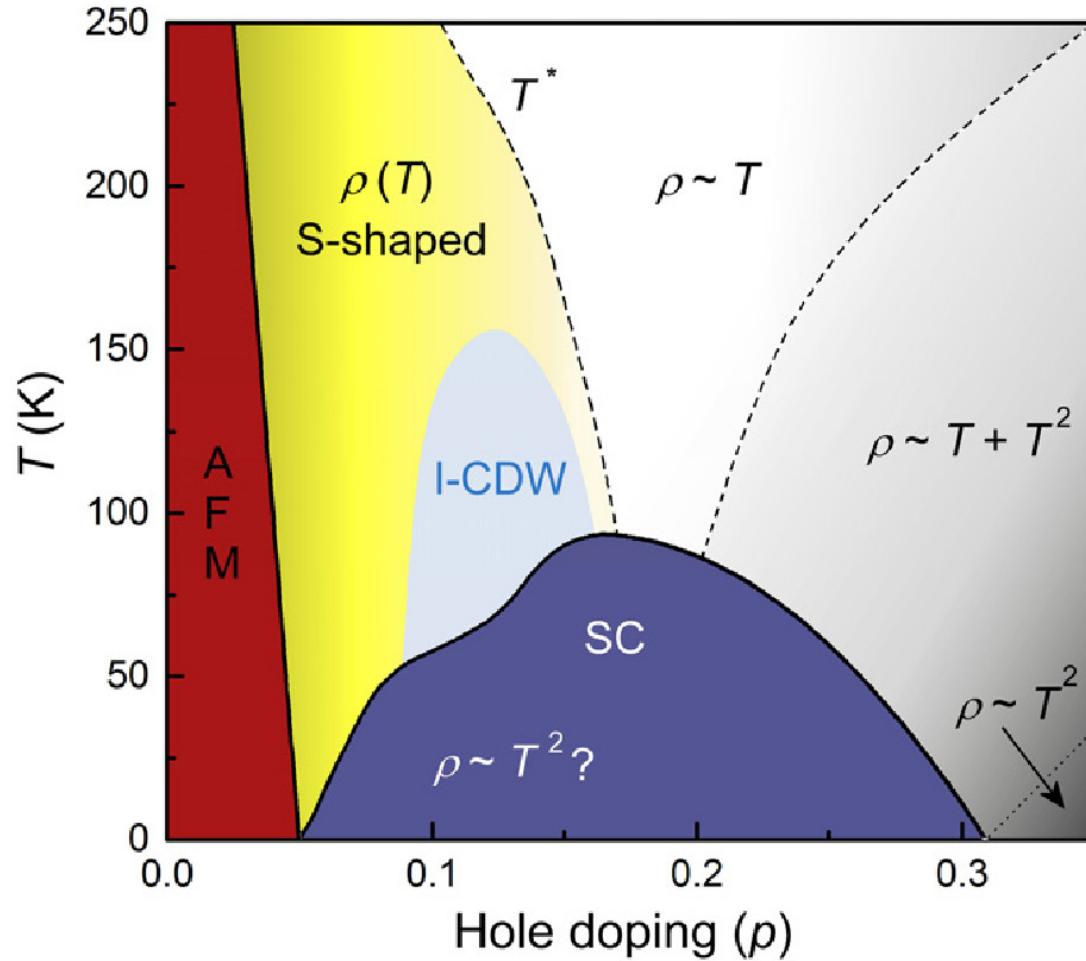
$\text{YbRh}_2\text{Si}_2$ : highly non-Drude behavior in strange metal regime



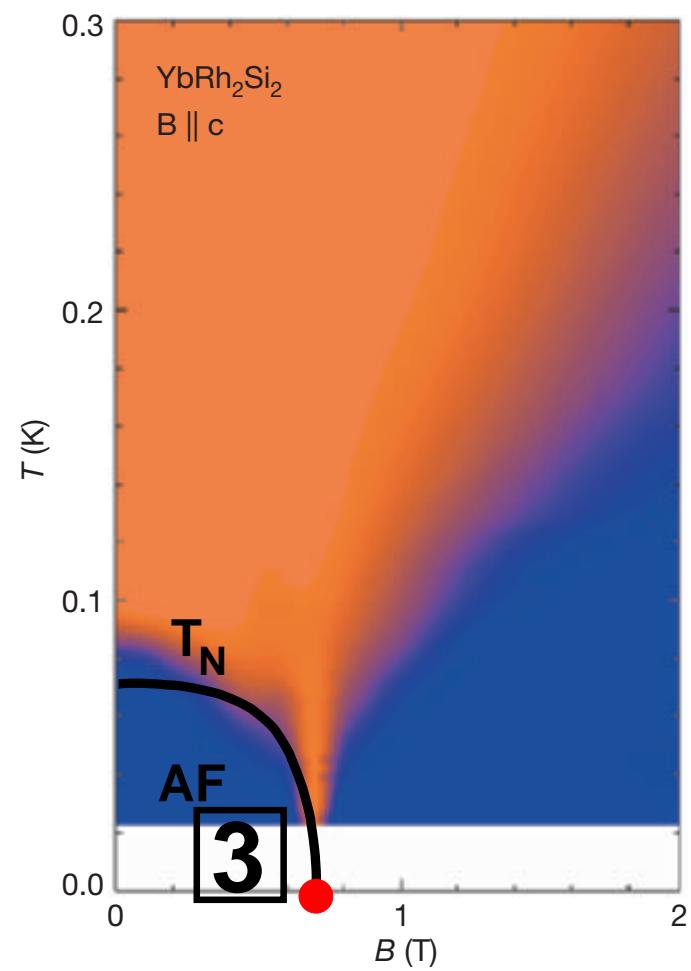
(Li, Kono, Si & SP, arXiv:2205.13382)

# Is there superconductivity at the QCP of $\text{YbRh}_2\text{Si}_2$ ?

Generic phase diagram of the cuprates

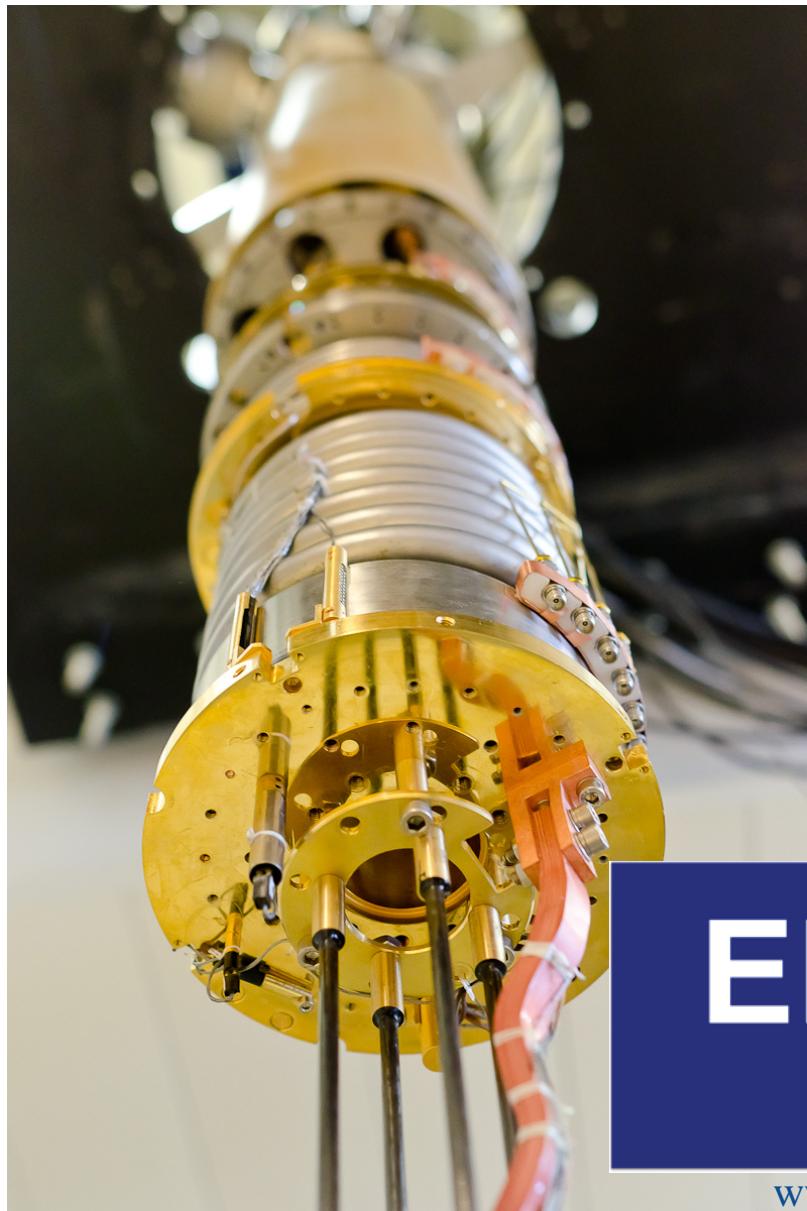


Phase diagram of  $\text{YbRh}_2\text{Si}_2$



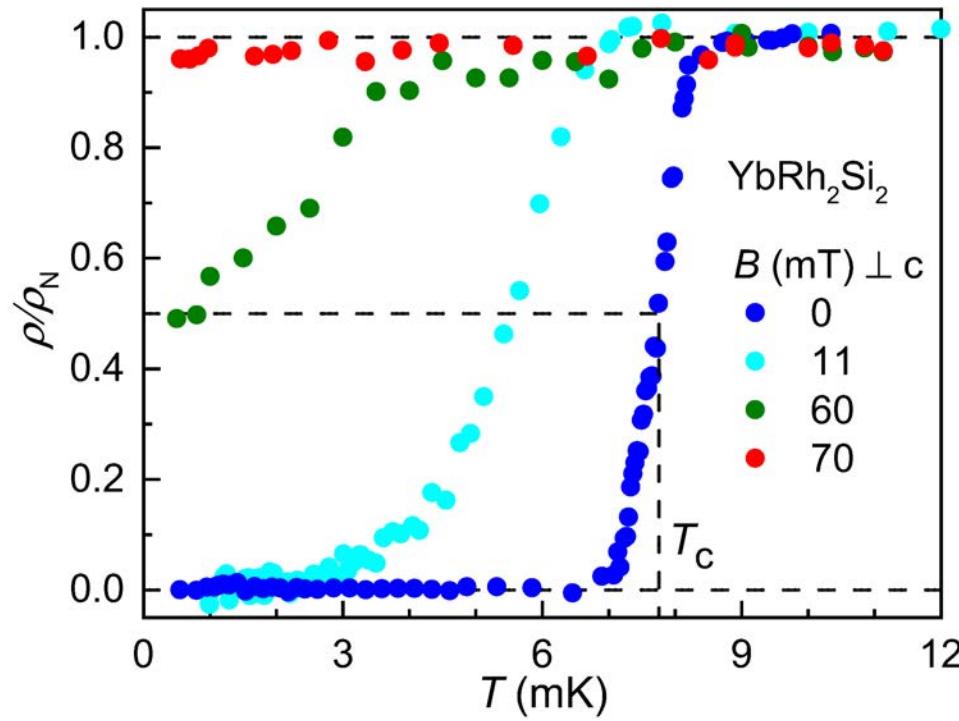
(Proust et al., PNAS 113 (2016) 13654) (Custers et al., Nature 424 (2003) 524)

# The Vienna Microkelvin Laboratory

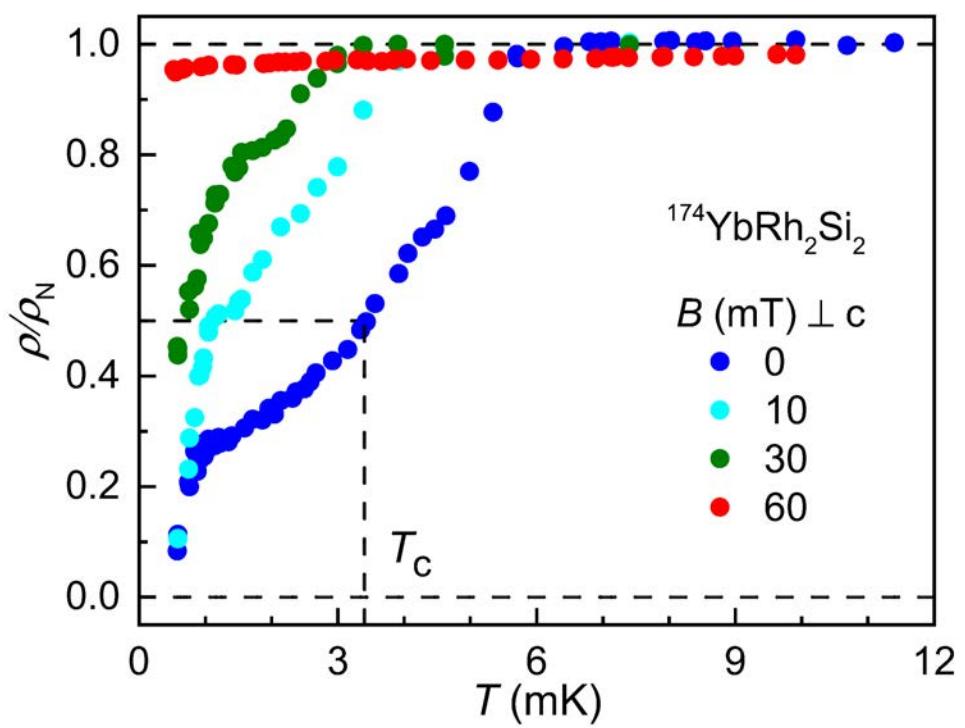


# Electrical resistivity at ultralow temperatures: Iso- $B$ curves

$\text{YbRh}_2\text{Si}_2$

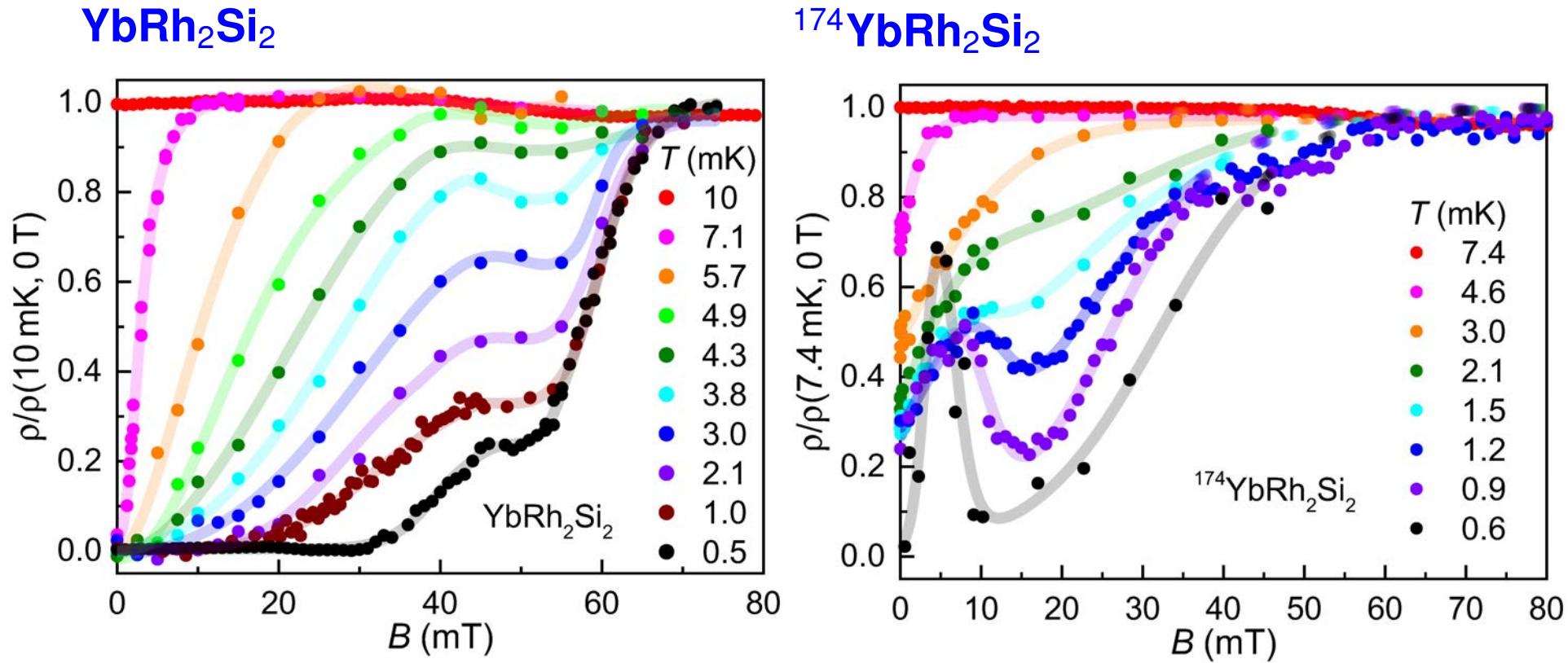


$^{174}\text{YbRh}_2\text{Si}_2$



(Nguyen et al., Nat. Commun. 12 (2021) 4341)

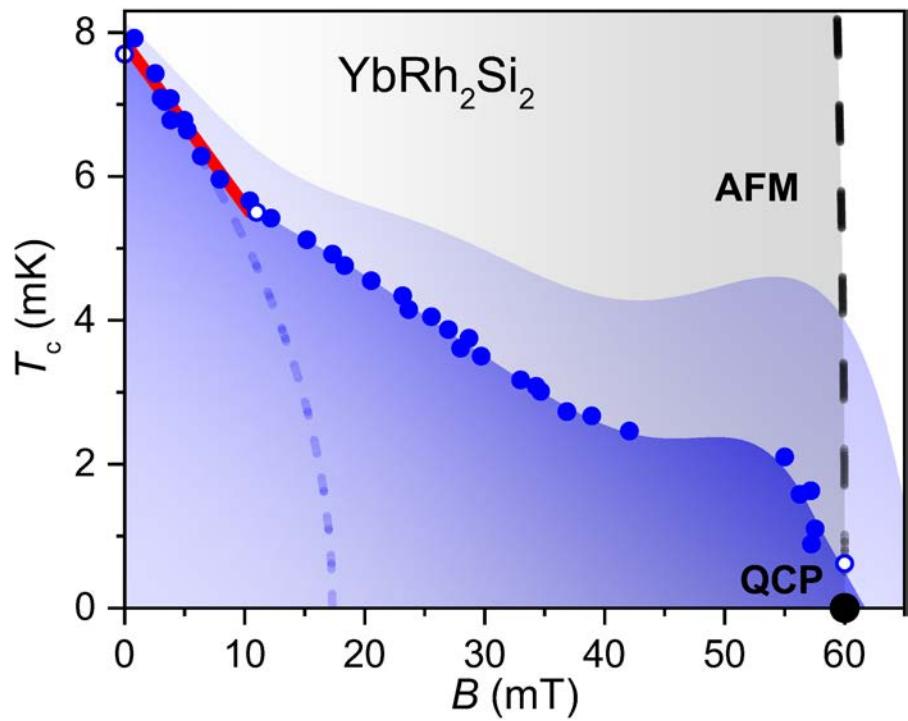
# Electrical resistivity at ultralow temperatures: Iso- $T$ curves



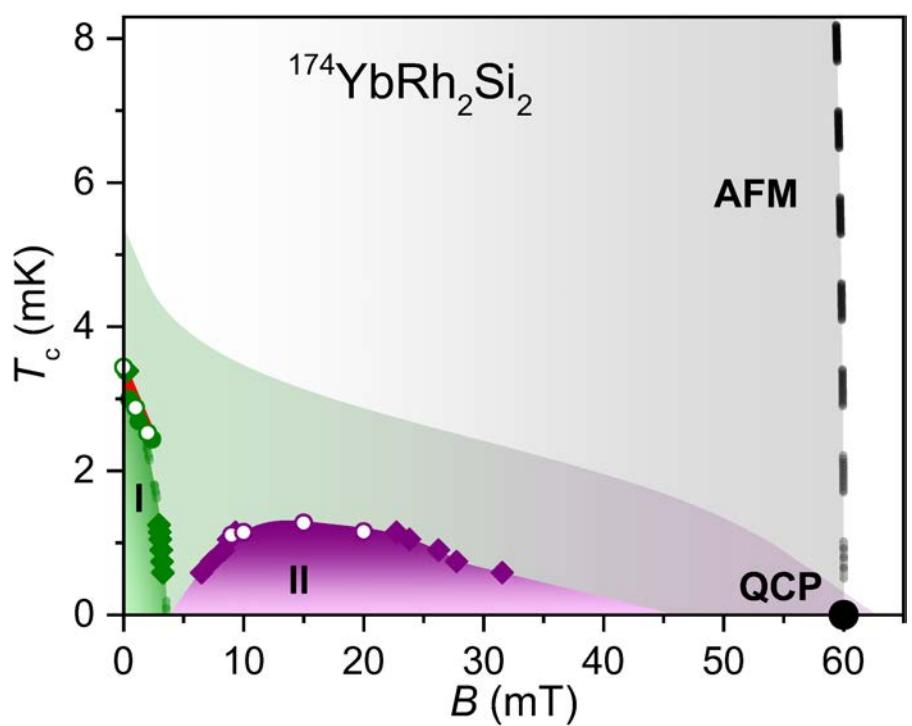
(Nguyen et al., Nat. Commun. 12 (2021) 4341)

# Temperature–magnetic field phase diagrams

$\text{YbRh}_2\text{Si}_2$



$^{174}\text{YbRh}_2\text{Si}_2$

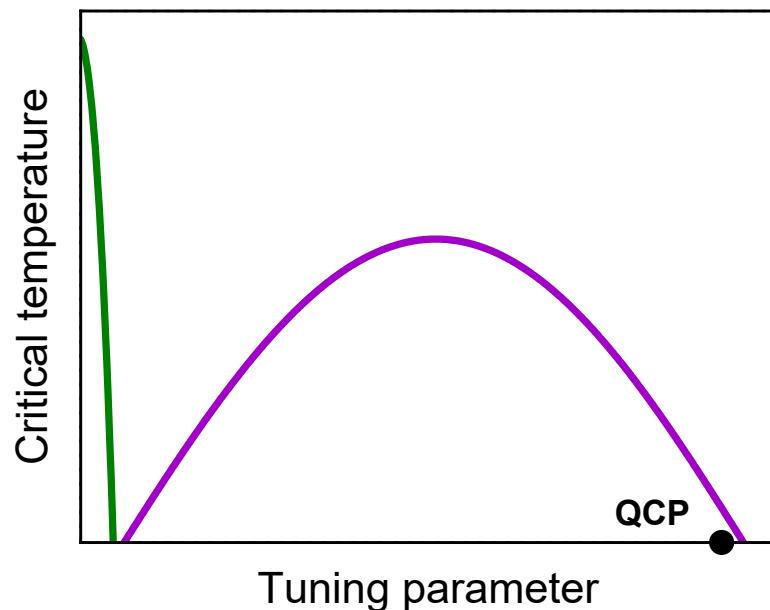
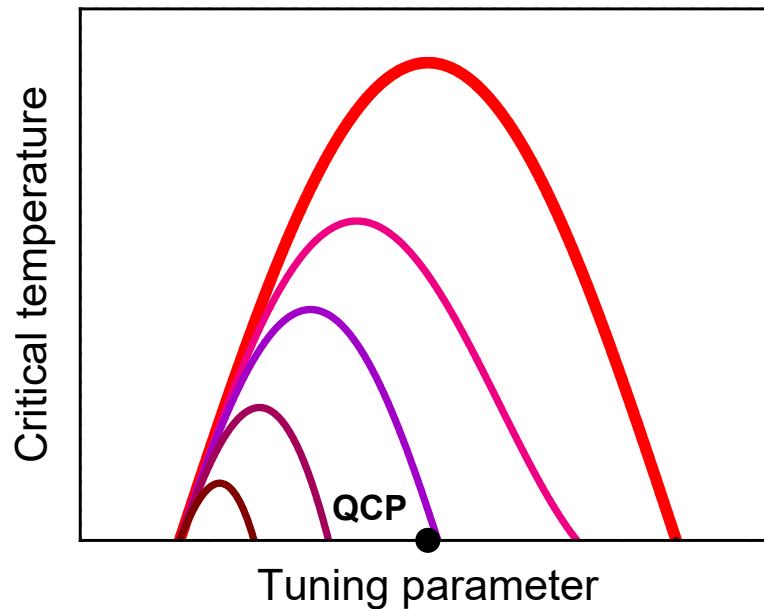
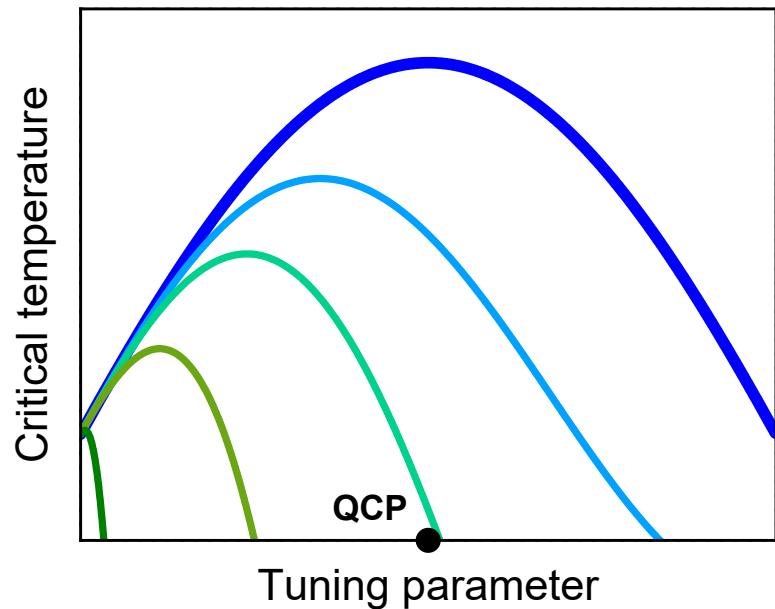


Orbital-limiting fields: 24 mT (5 mT)

Pauli-limiting fields: 15 mT (6.4 mT)

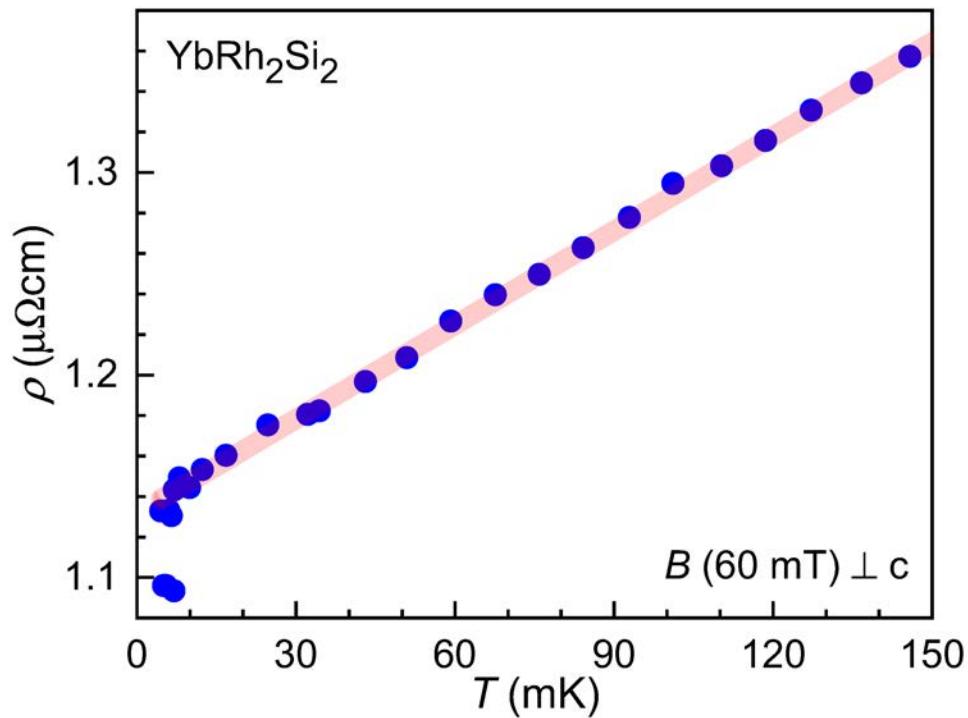
(Nguyen et al., Nat. Commun. 12 (2021) 4341)

# Magnetic field effect on “dome” structure

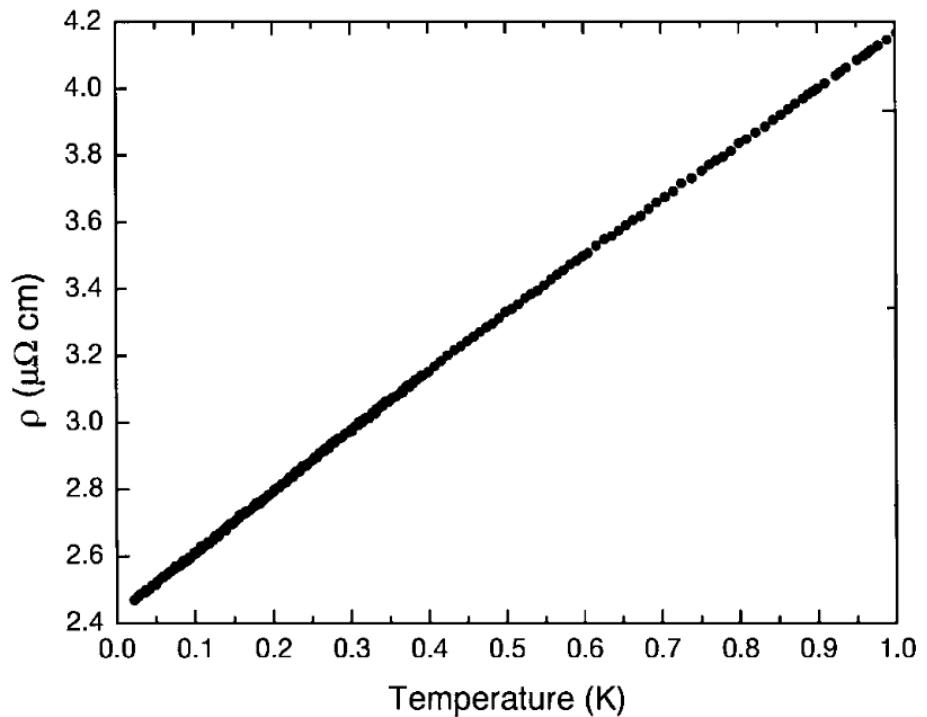


# Linear-in- $T$ electrical resistivity down to $T_c$ at QCP

**YbRh<sub>2</sub>Si<sub>2</sub>**



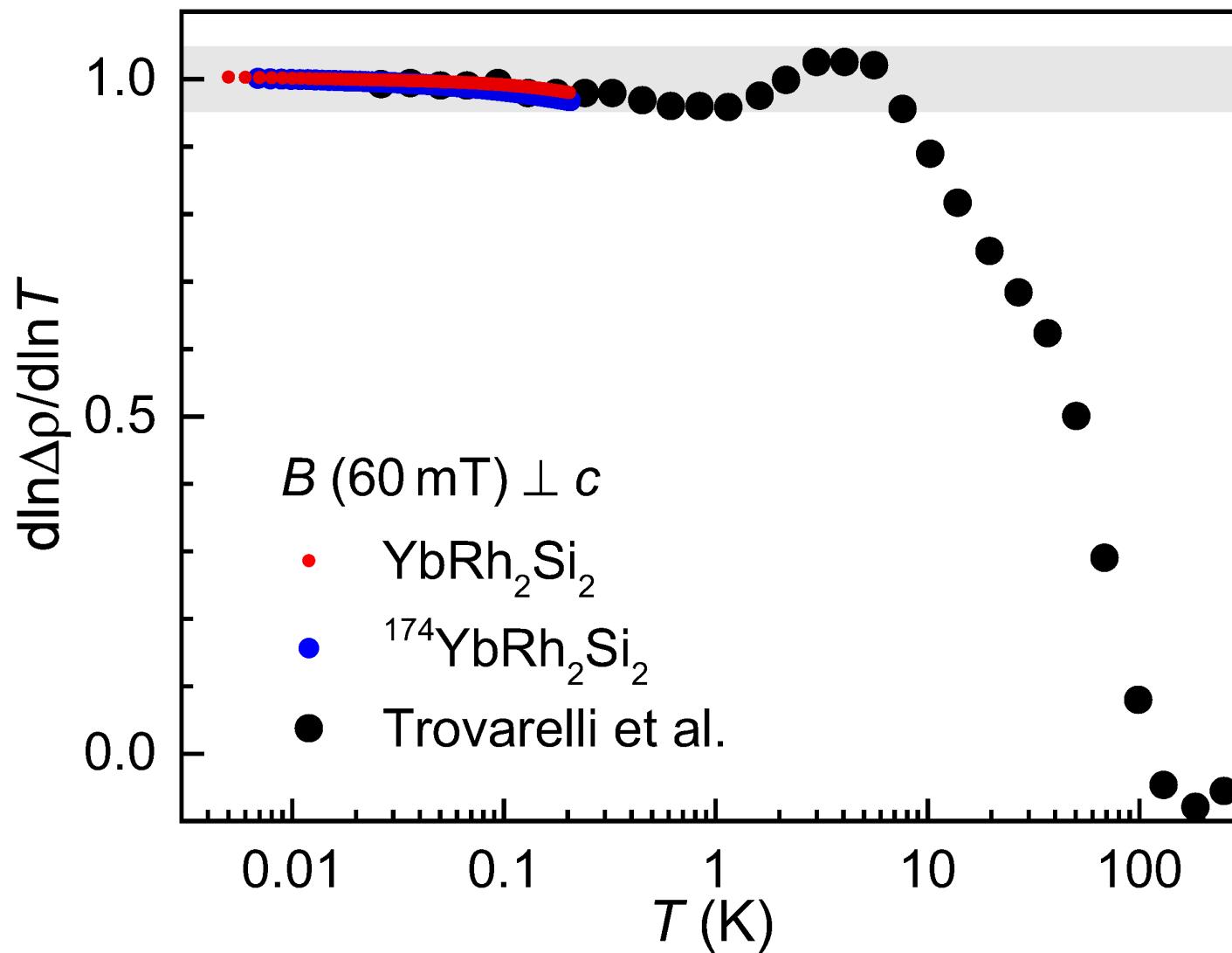
**YbRh<sub>2</sub>Si<sub>2</sub> (earlier batch)**



(Nguyen et al., Nat. Commun. 12 (2021) 4341)

(Trovarelli et al., Phys. Rev. Lett. 85 (2000) 626)

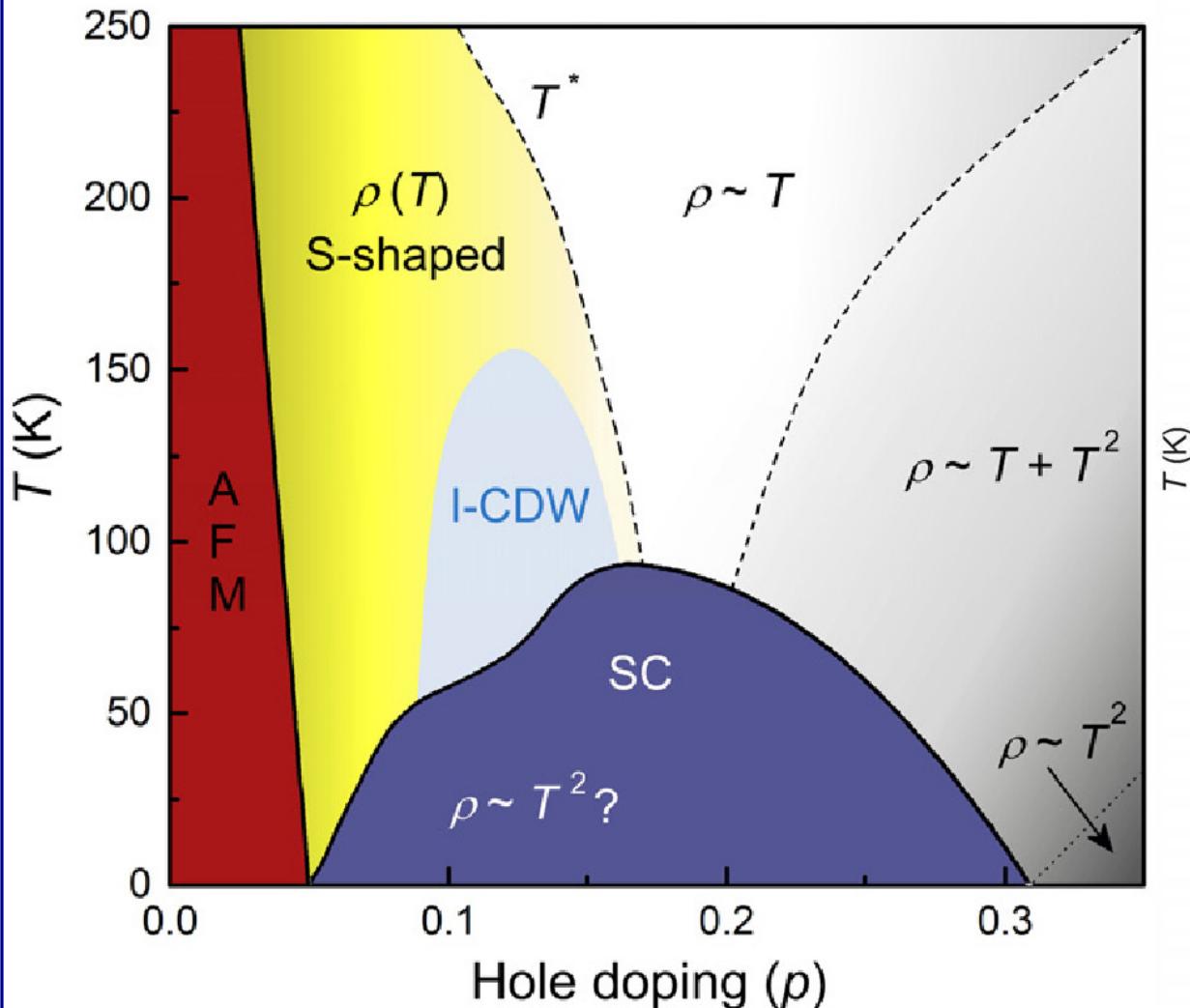
# $\text{YbRh}_2\text{Si}_2$ : An extreme strange metal (3.5 order of magnitude)



(Nguyen et al., Nat. Commun. 12 (2021) 4341)

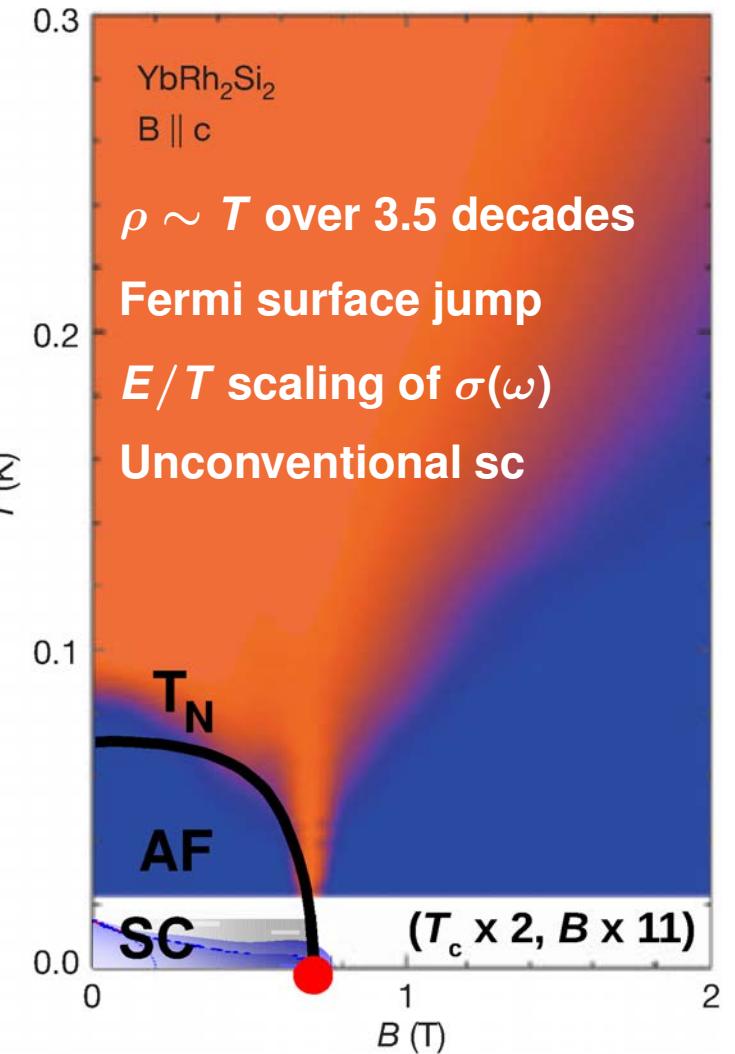
# Advance understanding by connecting the various platforms!

Generic phase diagram of the cuprates



(Proust et al., PNAS 113 (2016) 13654)

Phase diagram of  $\text{YbRh}_2\text{Si}_2$



(Refs. in this talk)

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