

Compartmentalizing the cuprate strange metal

- 1) Introduction
- 2) 'Boltzmann' transport in the cuprate strange metal (ADMR, Hall)
- 3) 'non-Boltzmann' transport in the cuprate strange metal (in-plane MR)
- 4) MR scaling across p^* and p_{SC}
- 5) Superconductivity within strange metal regime

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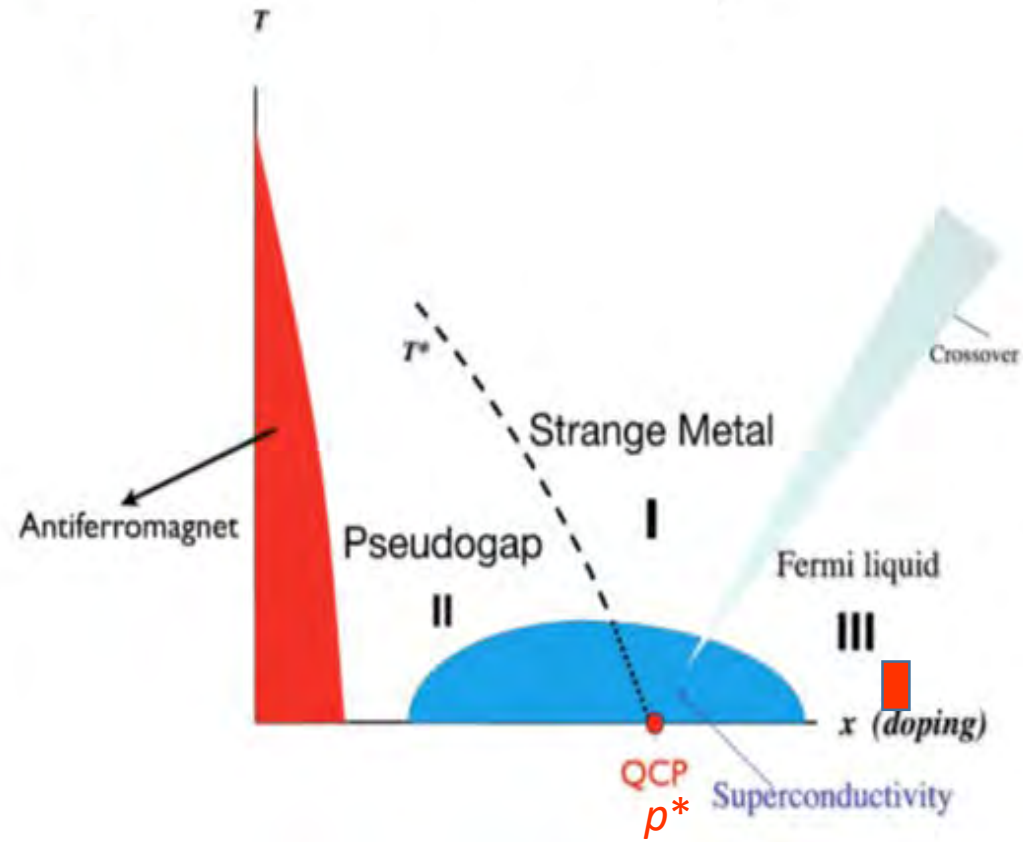
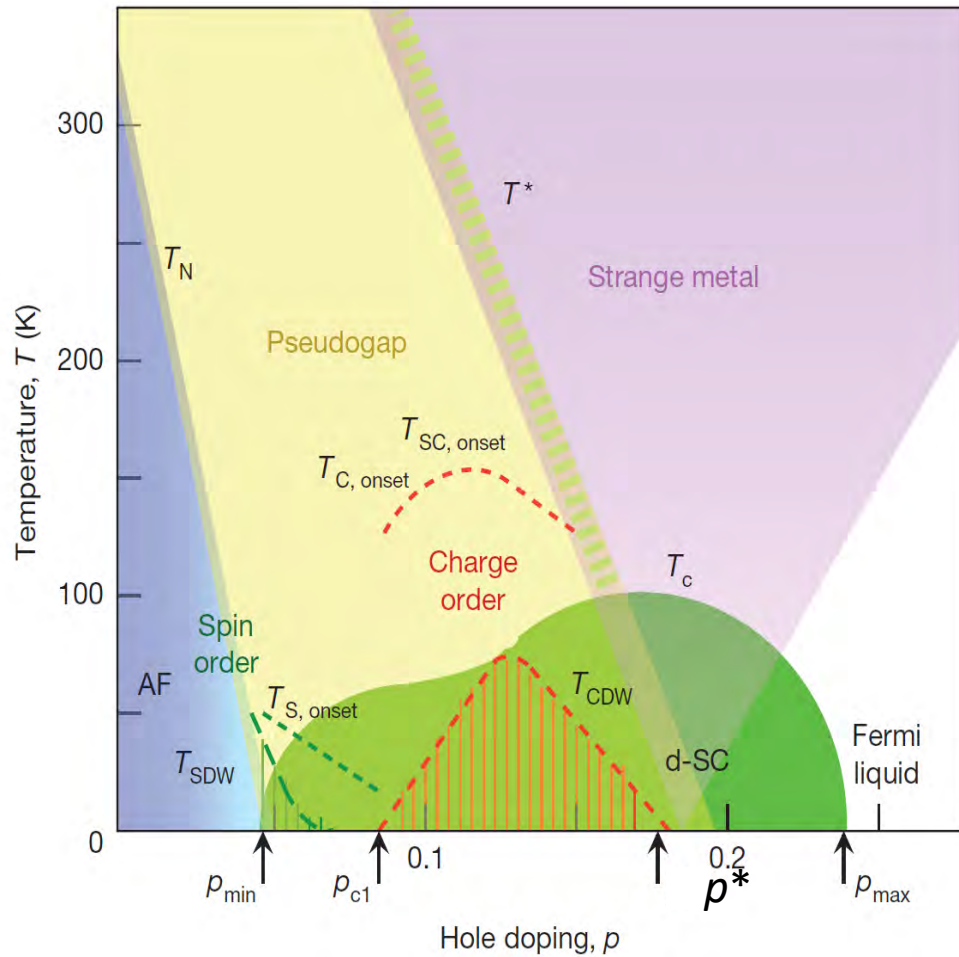
Radboud University



Introduction

Keimer *et al.*, *Nature* **518** 179 (15)

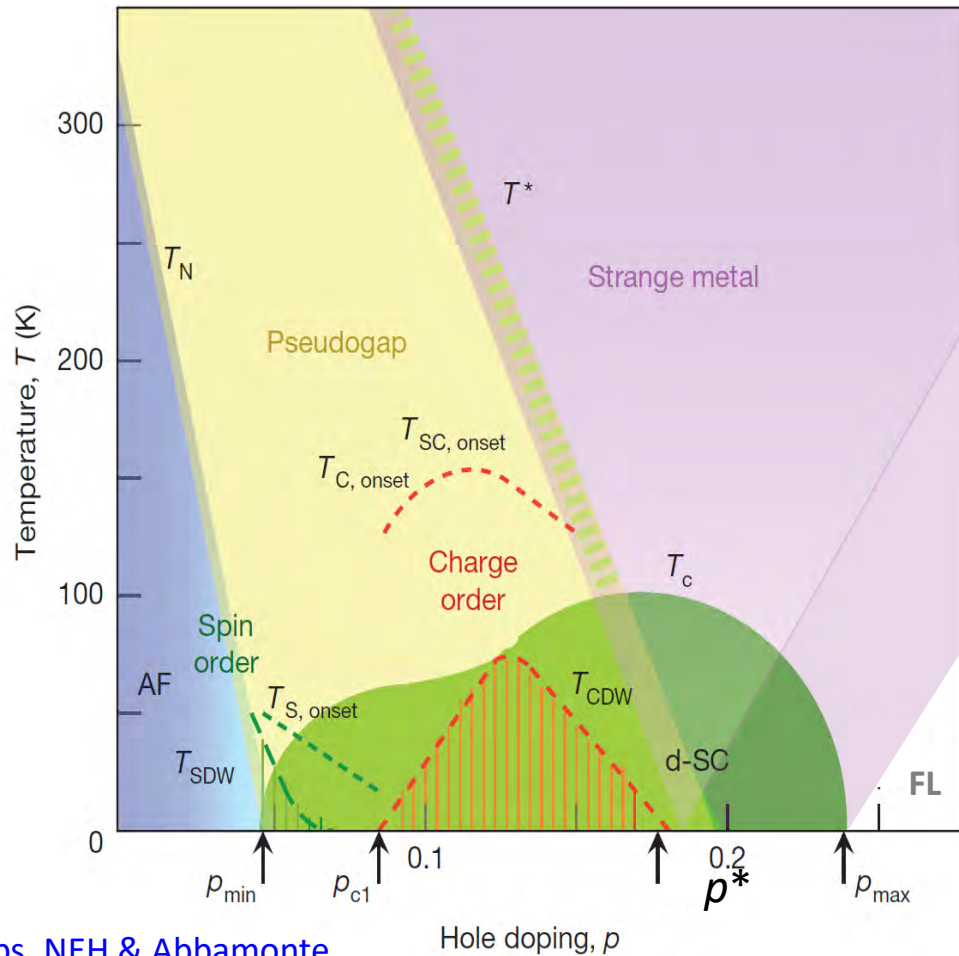
Varma, *RMP* **92** 031001 (20)



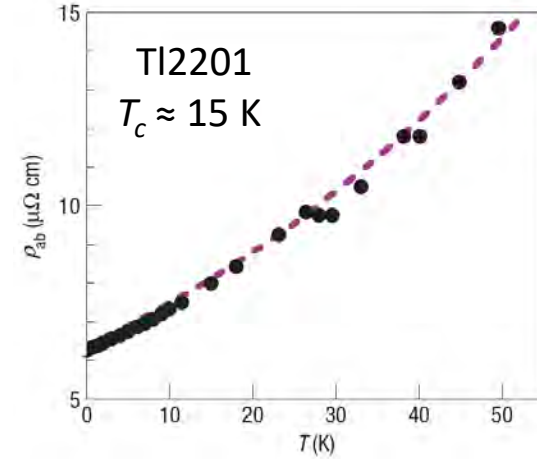
- Hole-doped cuprate phase diagram often depicted as though overdoped regime beyond p^* is a Fermi-liquid

Introduction

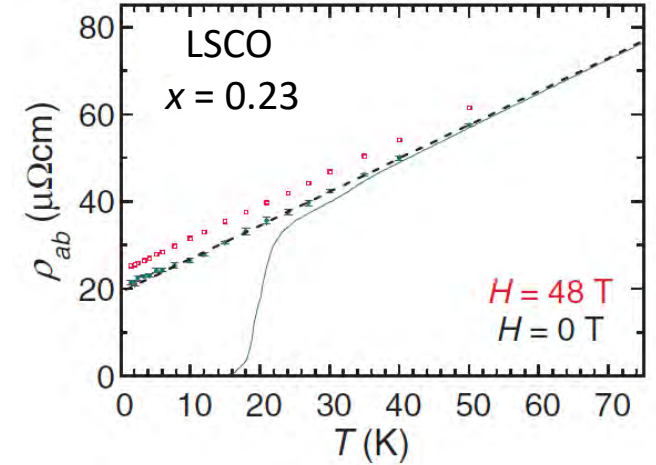
Keimer *et al.*, *Nature* **518** 179 (15)



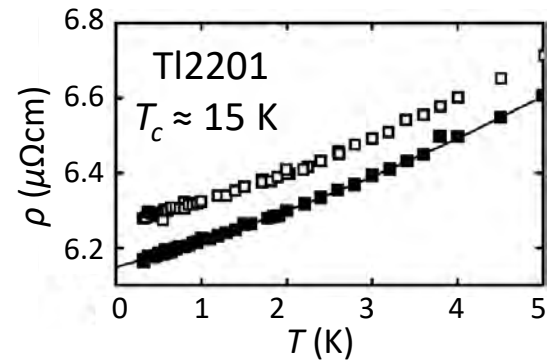
Phillips, NEH & Abbamonte, *2205.12979* (22)



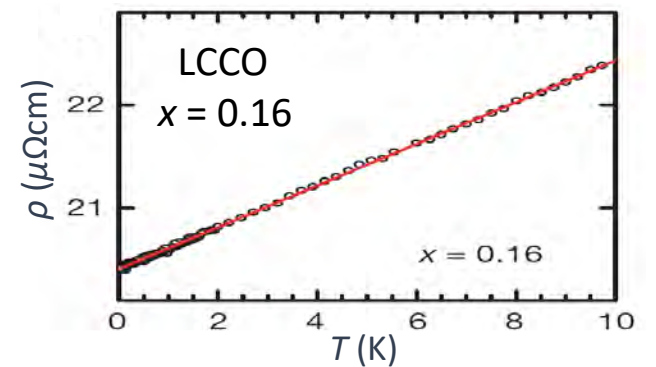
Mackenzie *et al.*, *PRB* **53** 5848 (96)



Cooper *et al.*, *Science* **323** 603 (09)



Proust *et al.*, *PRL* **89** 147003 (02)

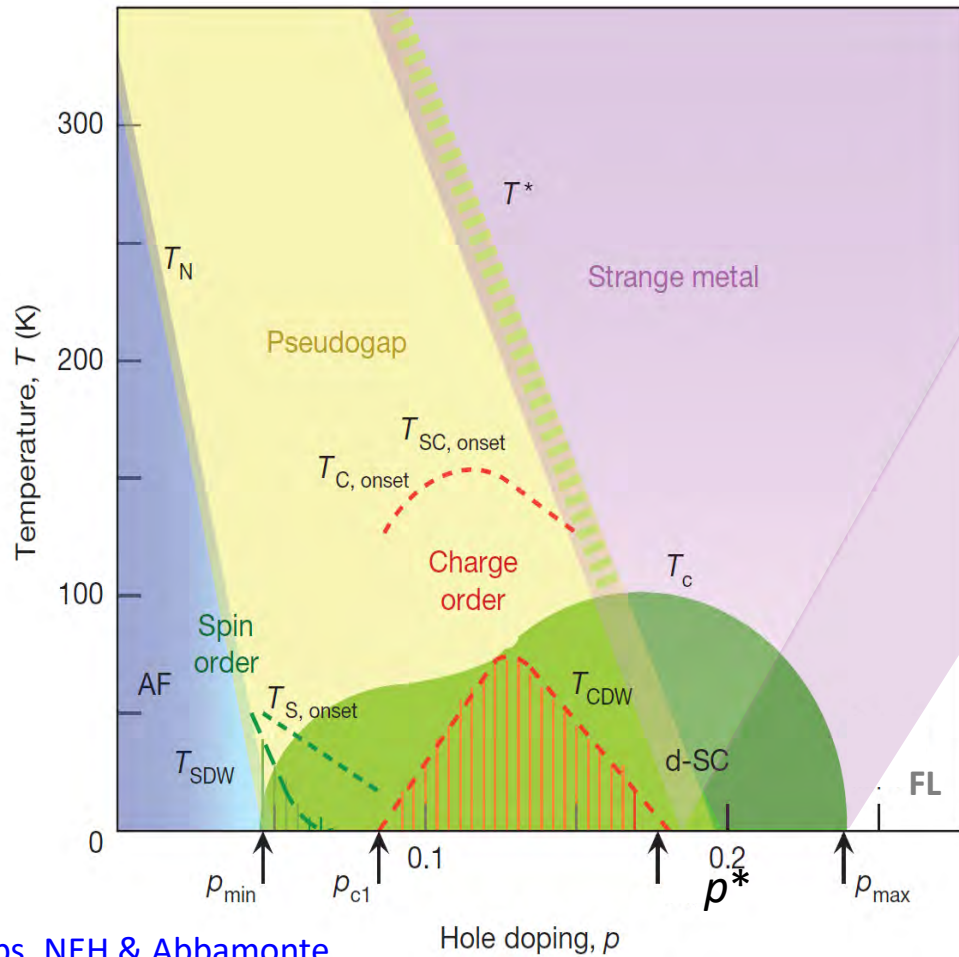


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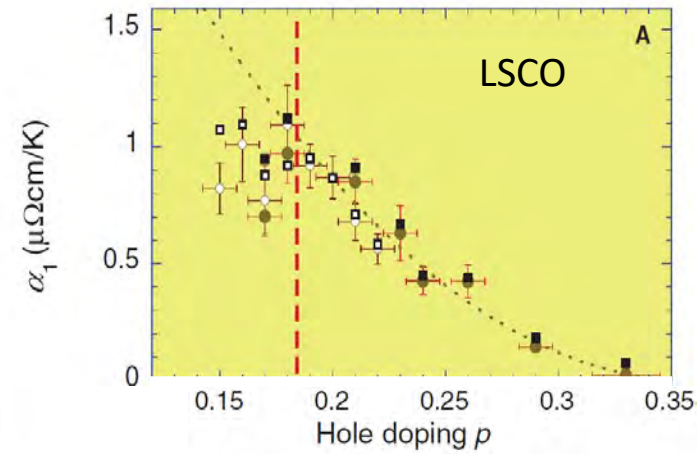
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Introduction

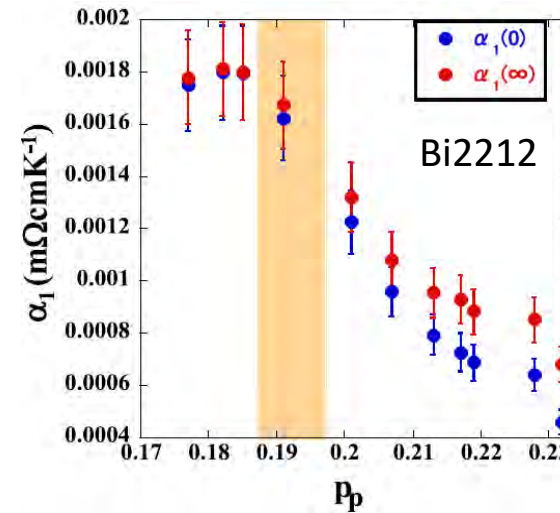
Keimer et al., *Nature* **518** 179 (15)



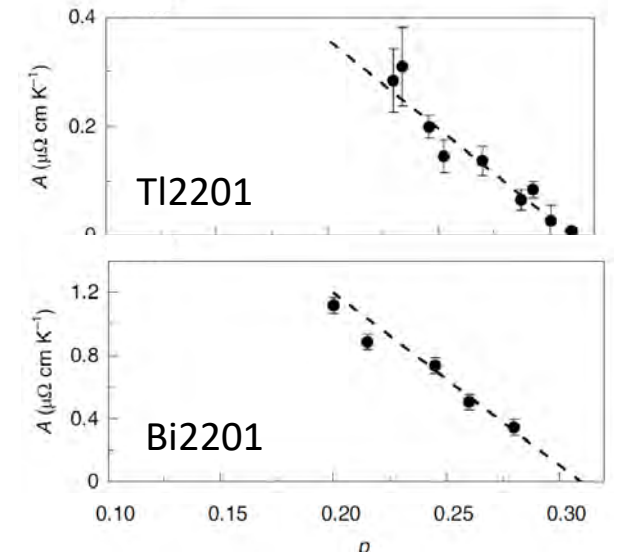
Phillips, NEH & Abbamonte, *2205.12979* (22)



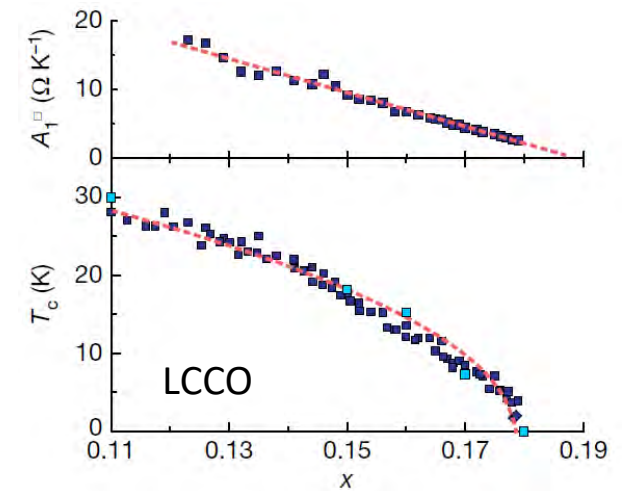
Cooper et al., *Science* **323** 603 (09)



Harada et al., *PRB* **105** 085131 (22)
Legros et al., *Nat. Phys.* **15** 142 (19)



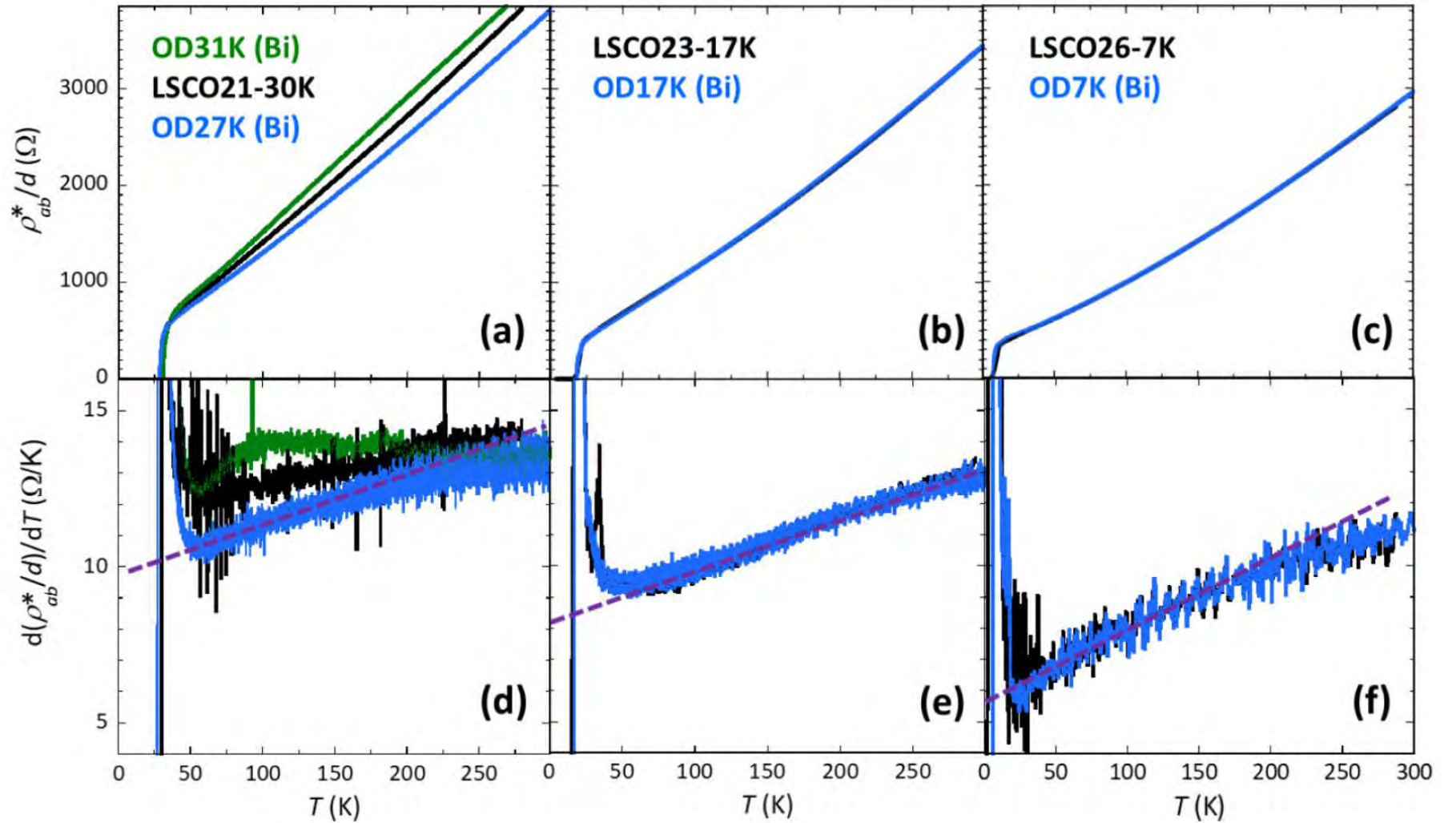
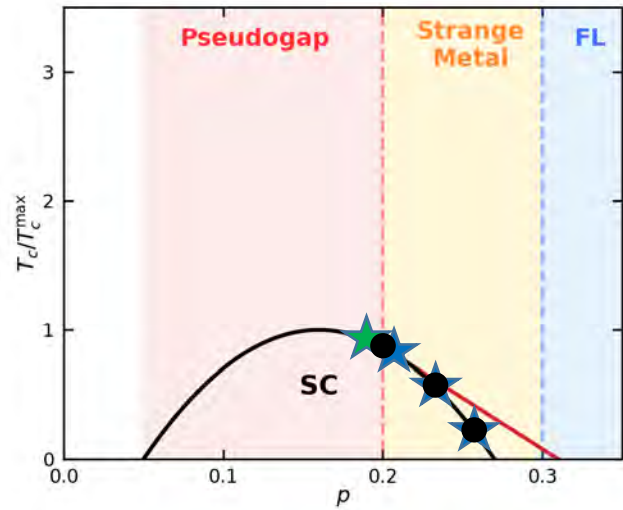
Putzke et al., *Nat. Phys.* **17** 826 (21)



Yuan et al., *Nature* **602** 431 (22)
Jin et al., *Nature* **476** 73 (11)

Introduction

Berben *et al.*, *PRM* 6 044804 (22)

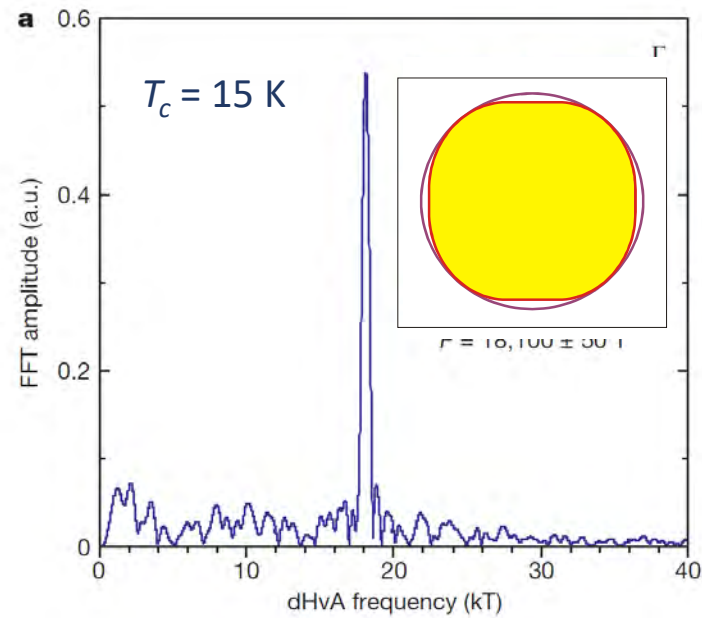


Fermiology of overdoped cuprates

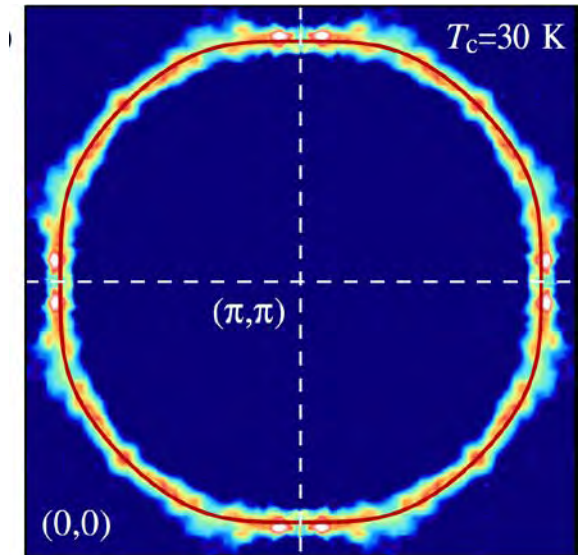
NEH *et al.*, *Nature* **425** 813 (03)



Vignolle *et al.*, *Nature* **455** 952 (08)



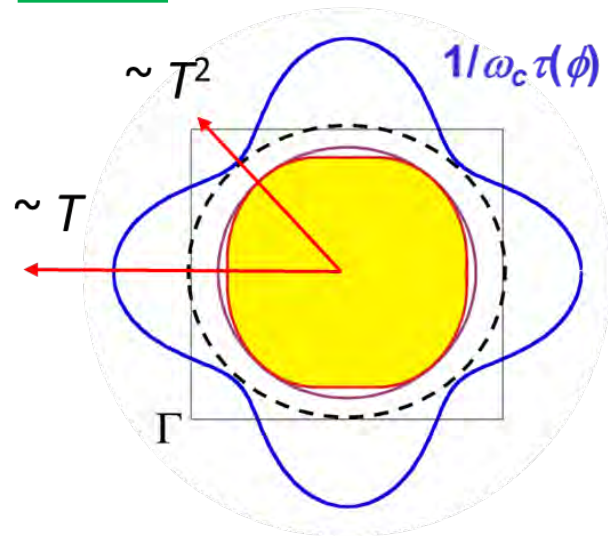
Platé *et al.*, *PRL* **95** 077001 (05)



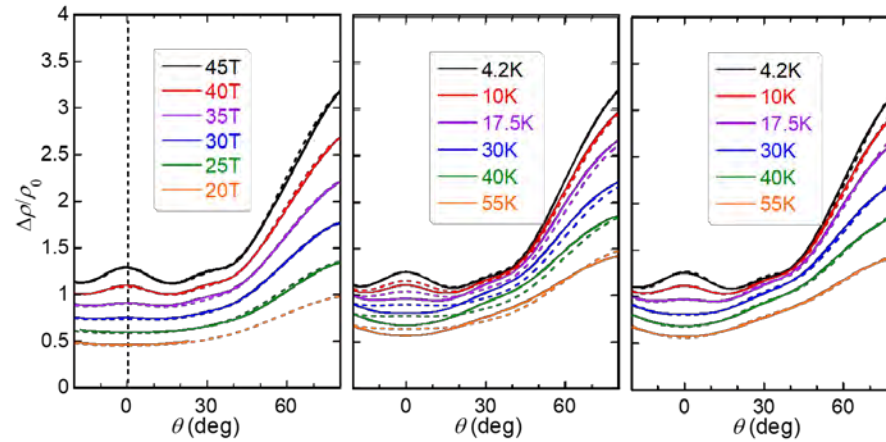
- ADMR, QO and ARPES measurements on OD Tl2201 all indicate large FS containing $1 + p$ holes

Boltzmann transport within SM regime

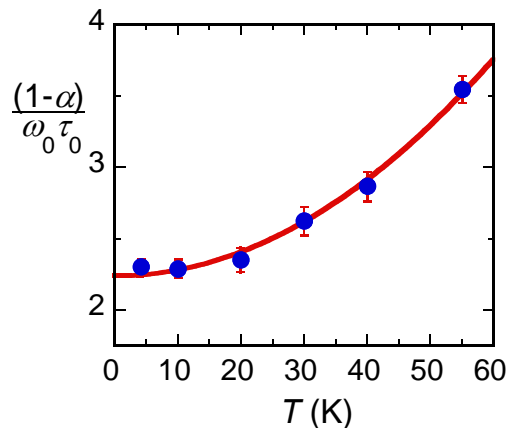
TI2201 $T_c \approx 15$ K



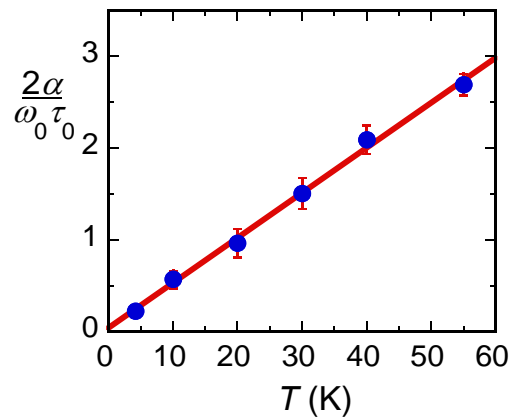
Abdel-Jawad *et al.*, *Nat. Phys.* **2**, 821 (06)



- T -dependent ADMR provided evidence of anisotropy in T -linear scattering rate



$\Gamma_{\text{iso}}(T)$ at the nodes



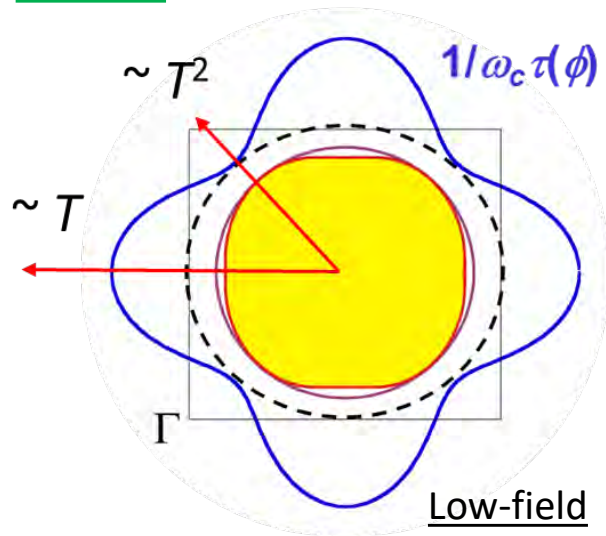
$\Gamma_{\text{aniso}}(T)$ at anti-nodes

Boltzmann / Shockley-Chambers

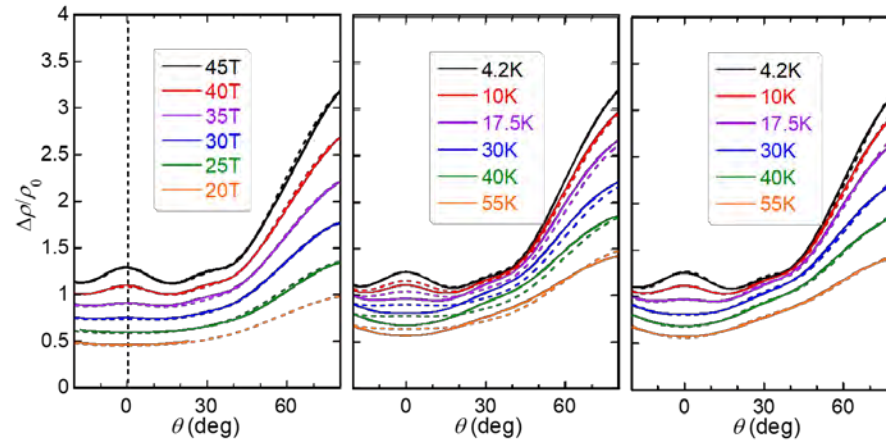
$$\sigma_{ij} = \frac{e^3 B}{2\pi^2 \hbar^2 c} \int_0^{2\pi} d\phi \int_0^\infty d\phi' \frac{v_i(\phi) v_j(\phi - \phi')}{\omega_c(\phi) \omega_c(\phi - \phi')} \exp\left(\int_\phi^{\phi'} \phi'' / \omega_c(\phi'') \tau(\phi'') d\phi''\right)$$

Boltzmann transport within SM regime

Tl2201 $T_c \approx 15$ K

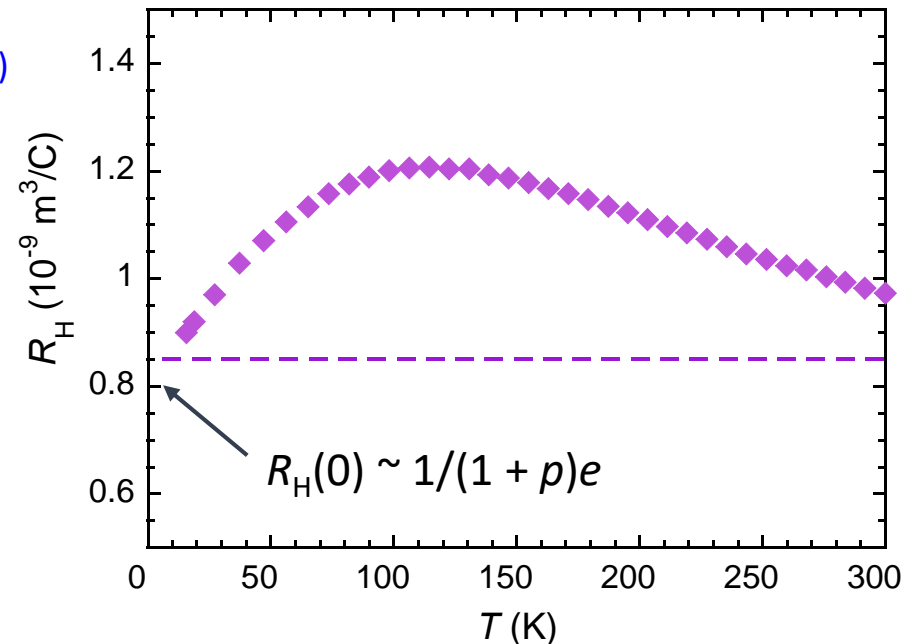
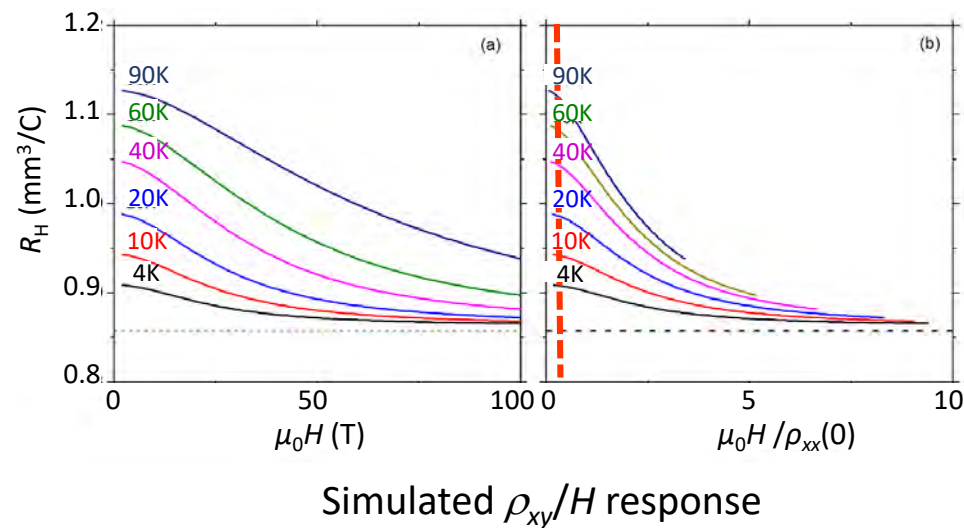


Abdel-Jawad *et al.*, *Nat. Phys.* **2**, 821 (06)



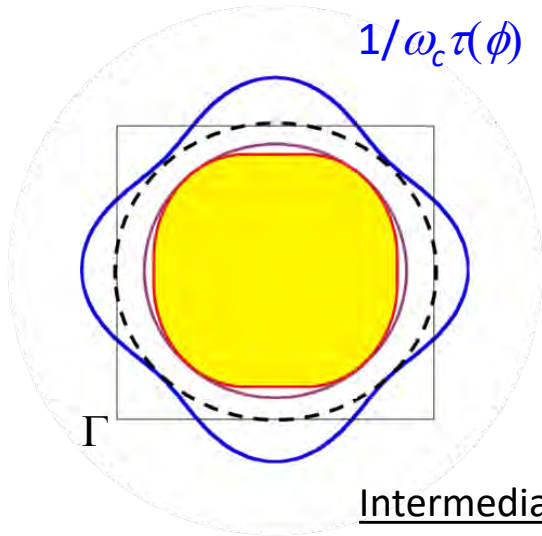
- T -dependent ADMR provided evidence of anisotropy in T -linear scattering rate
- ADMR parameterization reproduces $R_H(T)$ reasonably well.
- Same parameterization should also govern field-dependence of $R_H(T)$

Putzke *et al.*,
Nat. Phys. **17**, 826 (21)

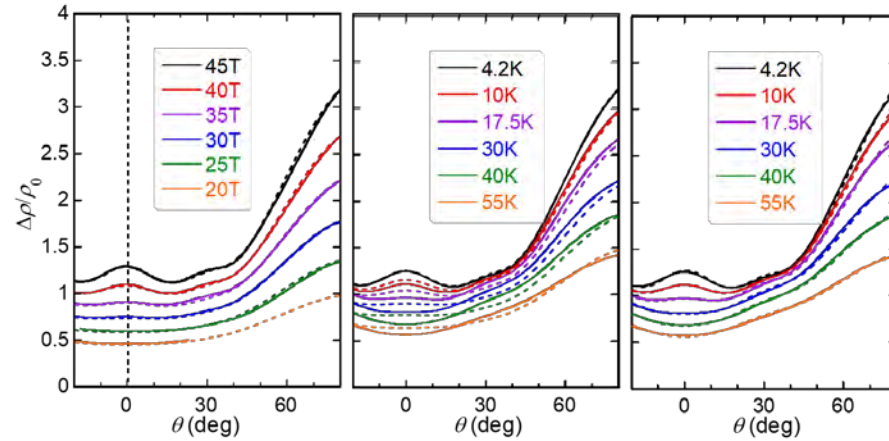


Boltzmann transport within SM regime

TI2201 $T_c \approx 15$ K

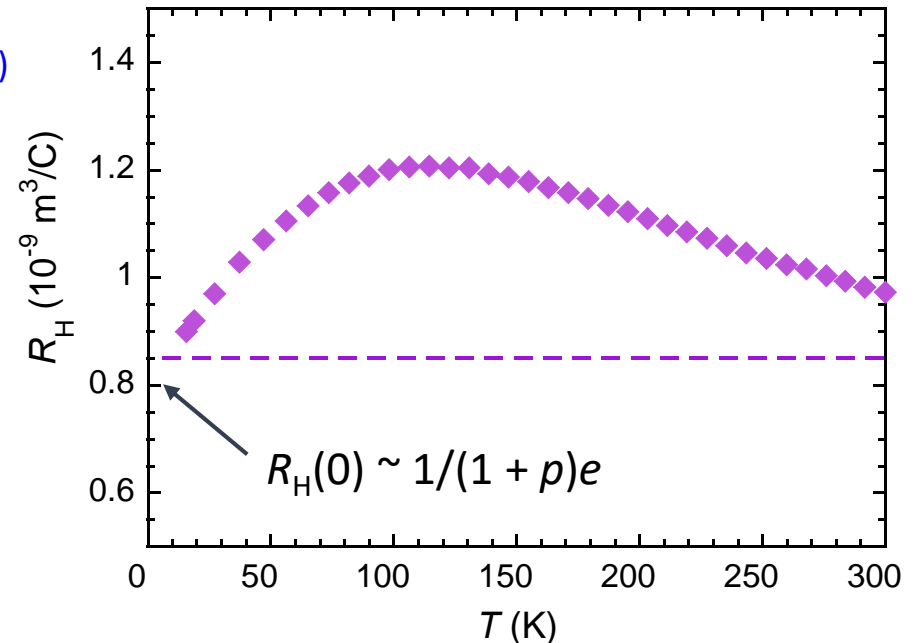
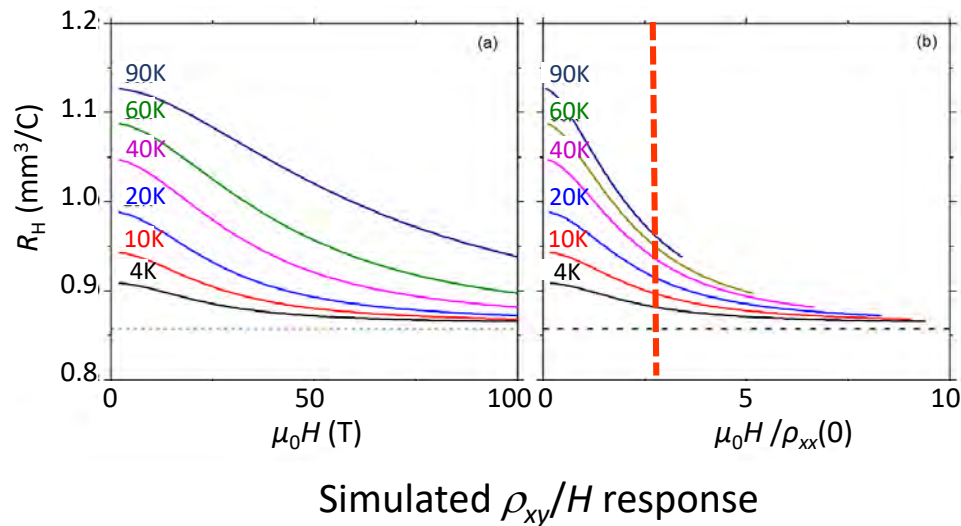


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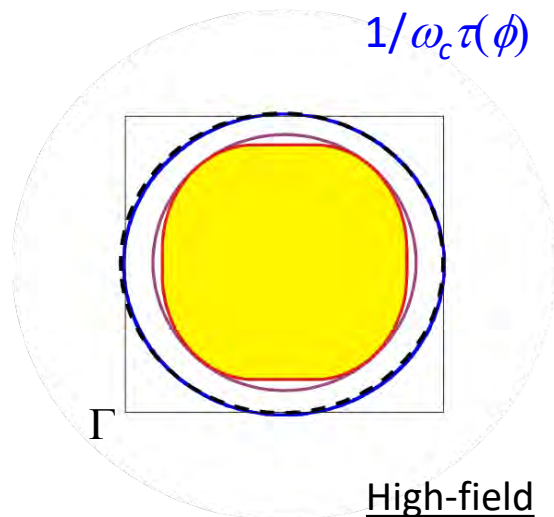
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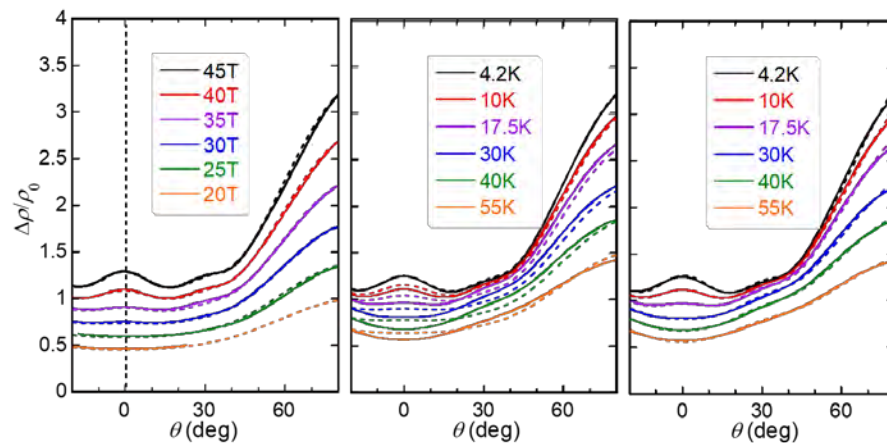


Boltzmann transport within SM regime

TI2201 $T_c \approx 15$ K

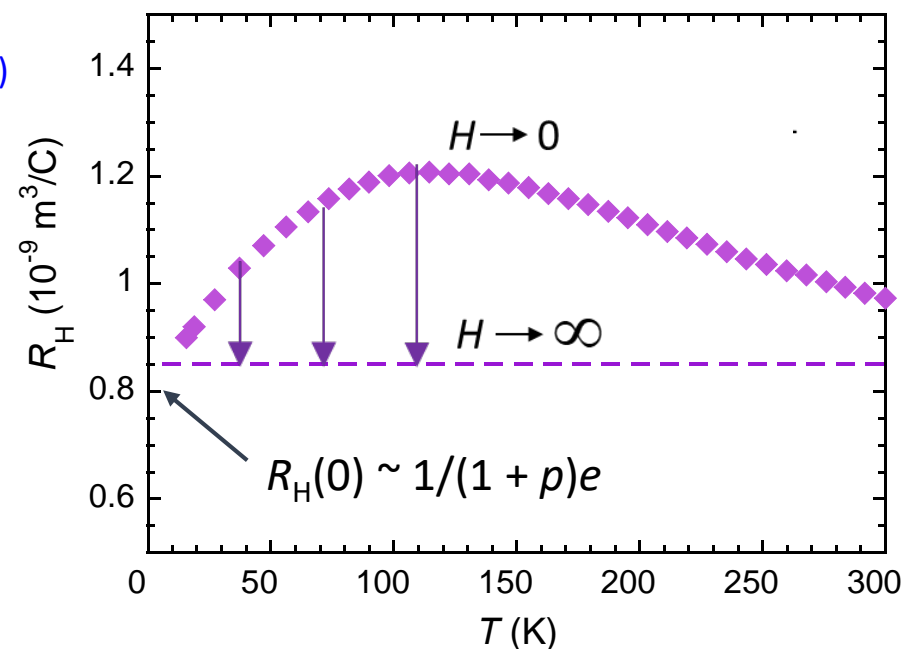
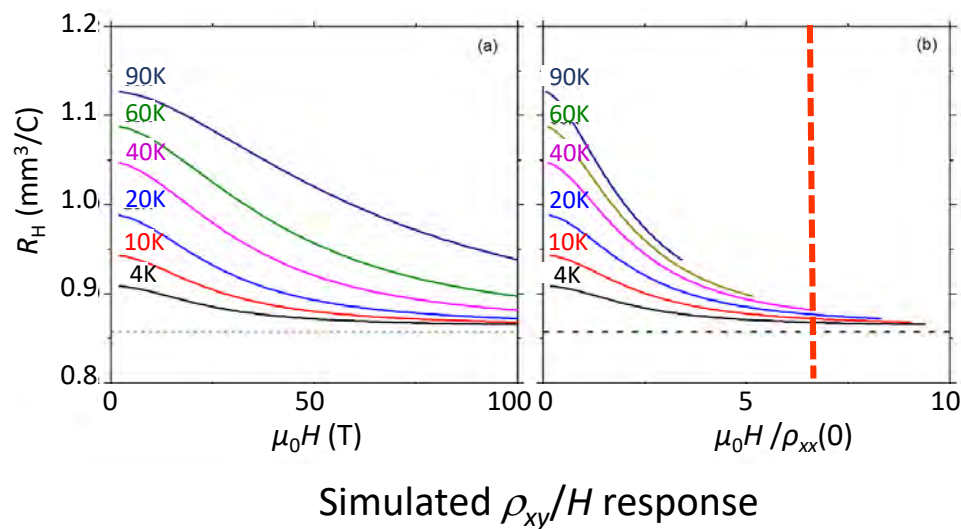


Abdel-Jawad *et al.*, *Nat. Phys.* **2**, 821 (06)



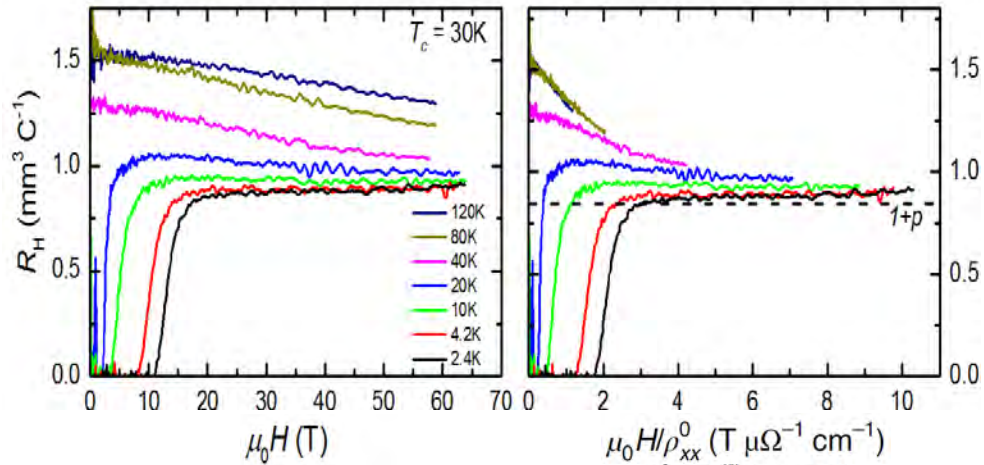
- T -dependent ADMR provided evidence of anisotropy in T -linear scattering rate
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Putzke *et al.*,
Nat. Phys. **17**, 826 (21)



Boltzmann transport within SM regime

TI2201 $T_c \approx 30$ K

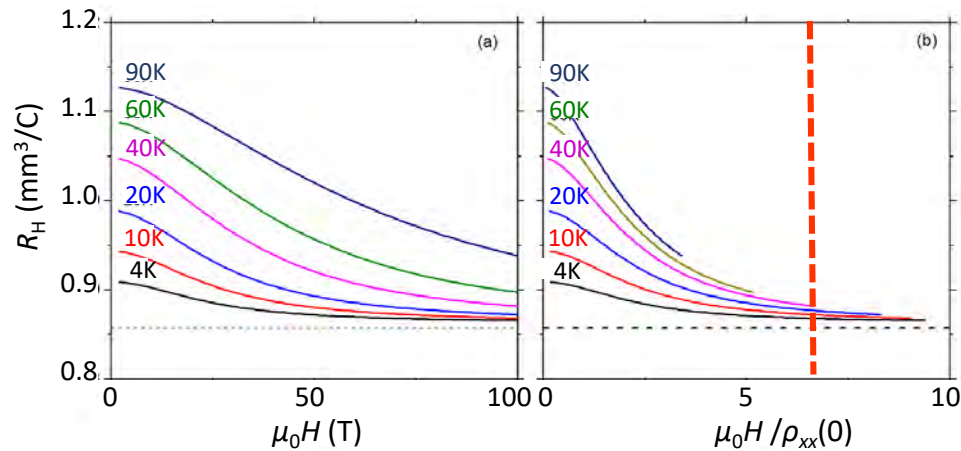


Note that R_H is H -independent at lowest T , indicating recovery of isotropic Γ

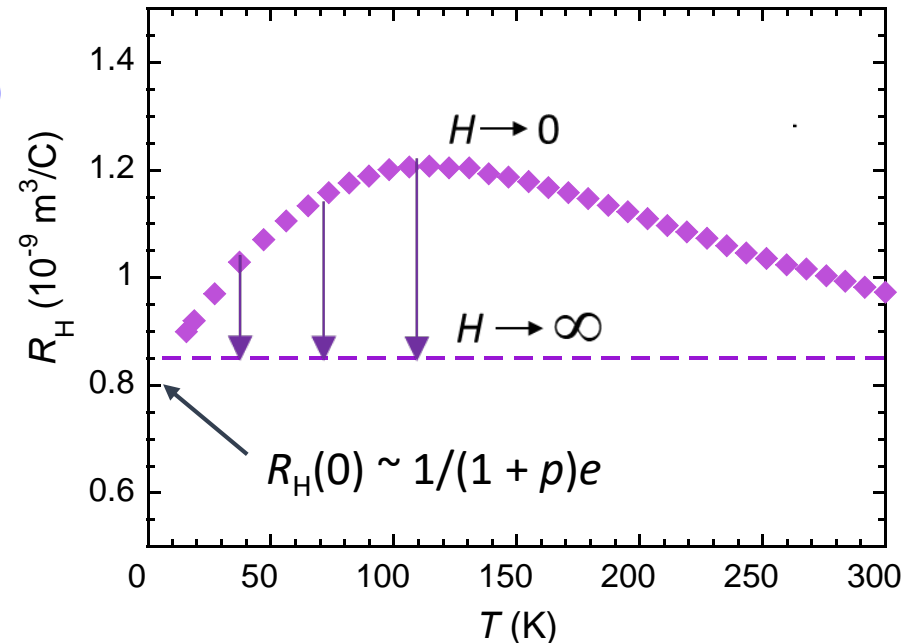
- T -dependent ADMR provided evidence of anisotropy in T -linear scattering rate
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Actual ρ_{xy}/H response

Putzke et al., Nat. Phys. 17, 826 (21)

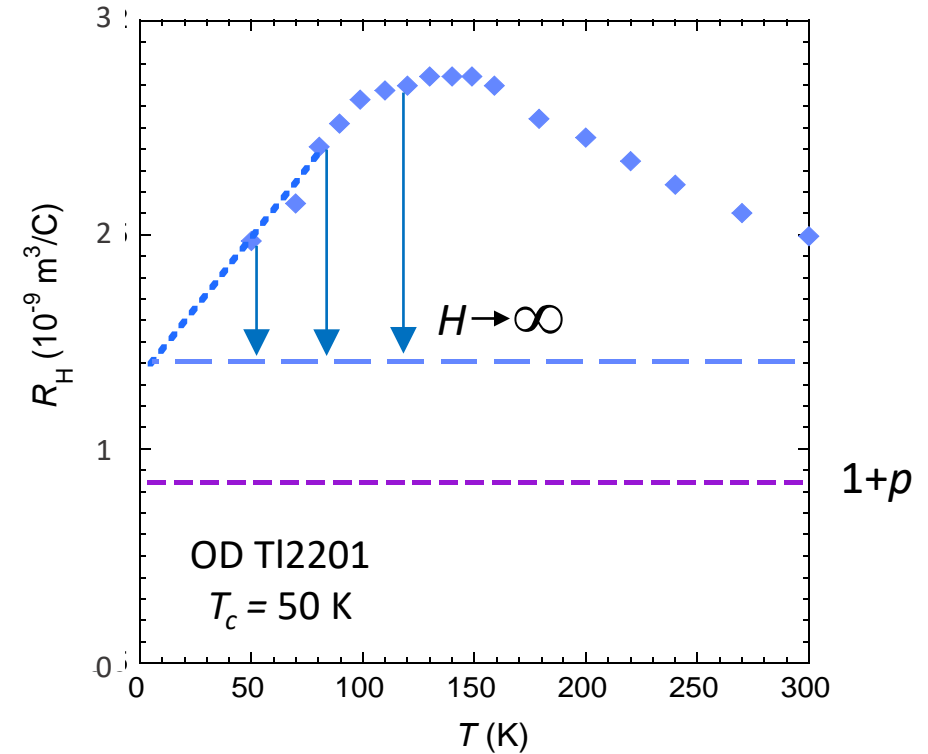
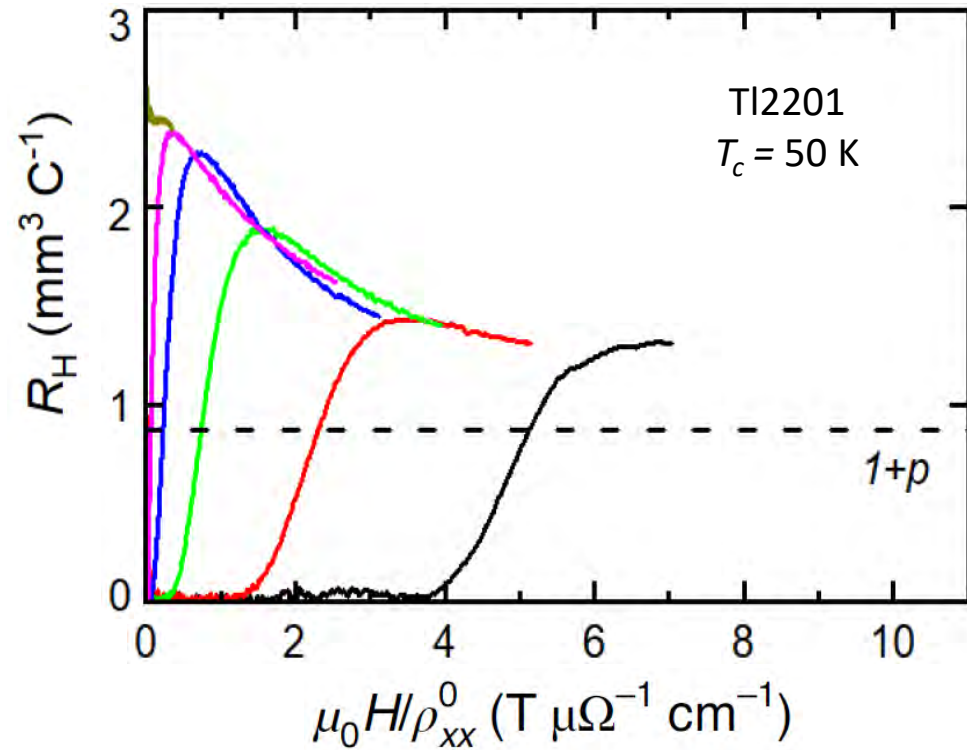


Simulated ρ_{xy}/H response



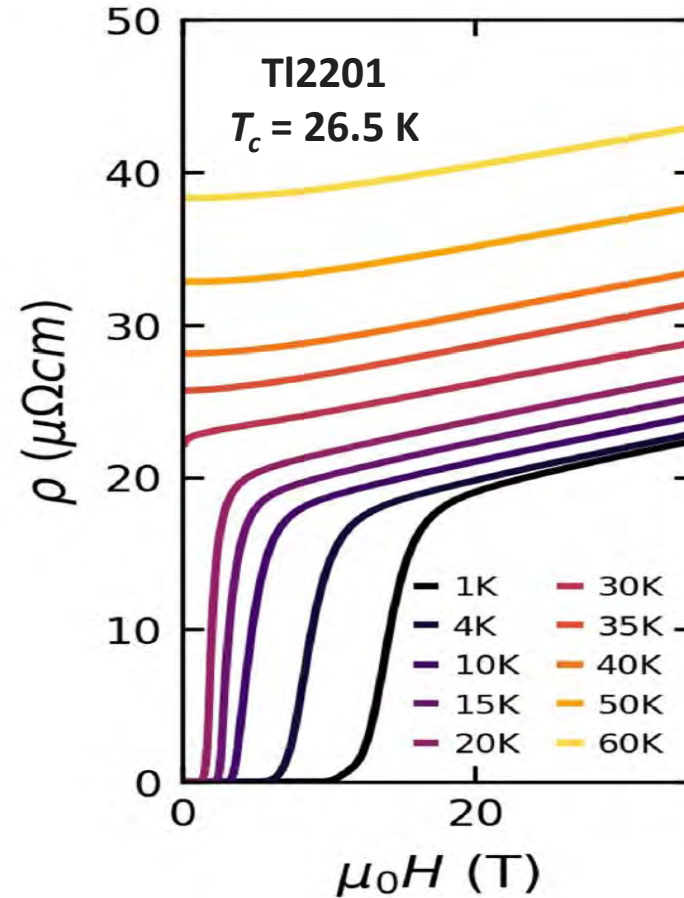
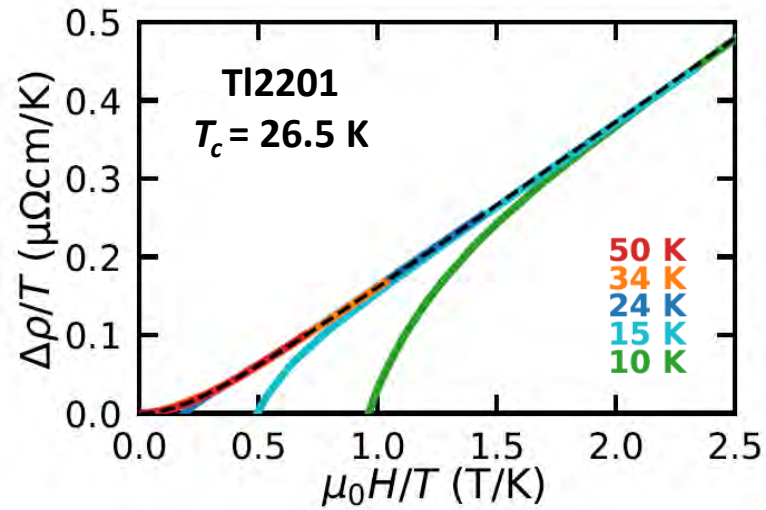
Boltzmann transport within SM regime

Putzke et al., Nat. Phys. 17, 826 (21)



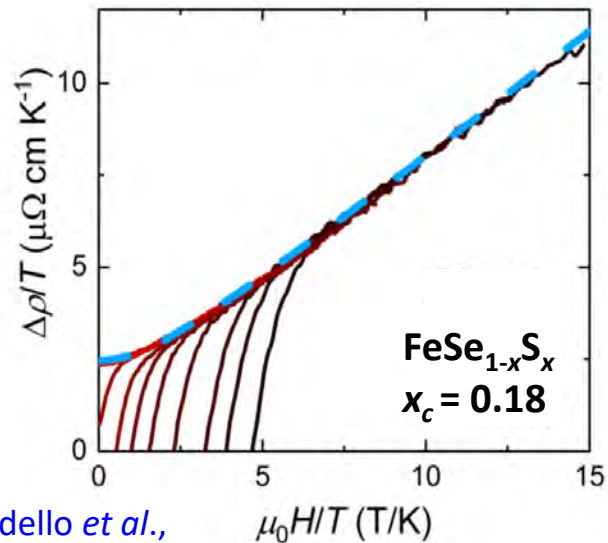
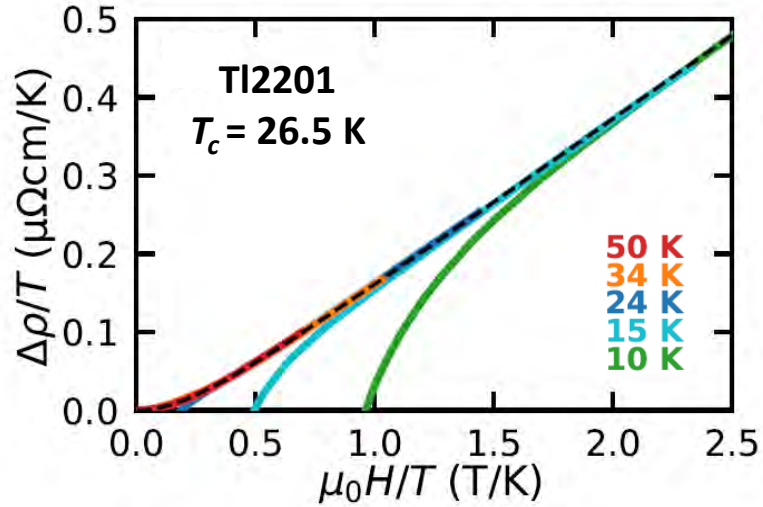
- In higher T_c TI2201 samples, drop in R_H with field also seen implying anisotropic scattering still responsible for H - and T -dependent $R_H(T)$. However, absolute value of $R_H(0)$ is now shifted up, suggesting loss of states *at all* T .

- With decreasing hole doping (increasing T_c), $R_H(H)$ does not asymptotically reach the value consistent with $n_H = 1 + p$



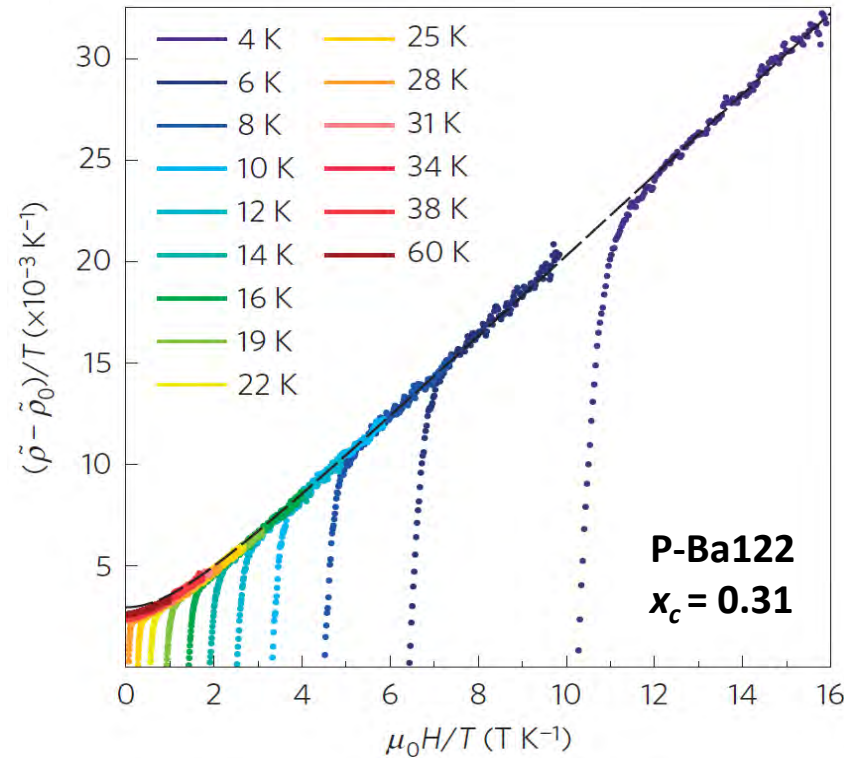
- In-plane MR shows crossover to H -linearity at highest fields with T -independent slope
- $\Delta\rho/T$ scales with H/T

non-Boltzmann transport in SM regime

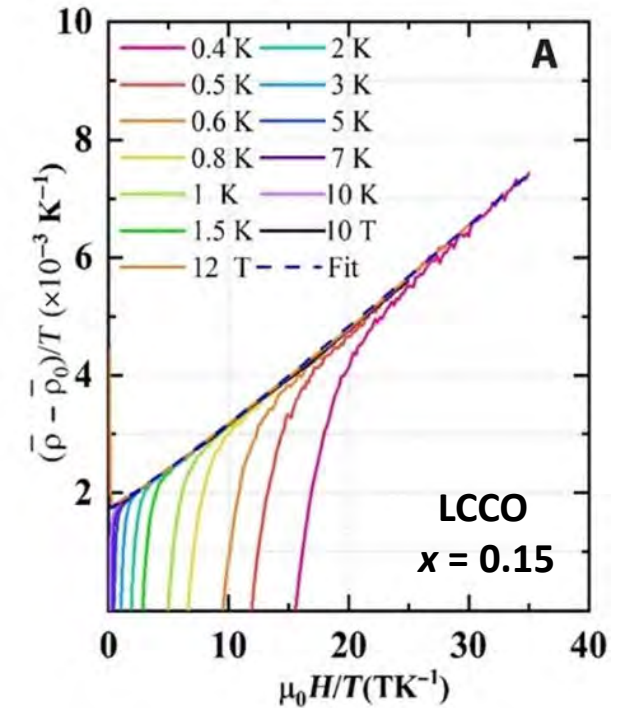


Licciardello *et al.*,
PRR **1**, 023011 (19)

Hayes *et al.*, *Nat. Phys.* **12**, 916 (16)



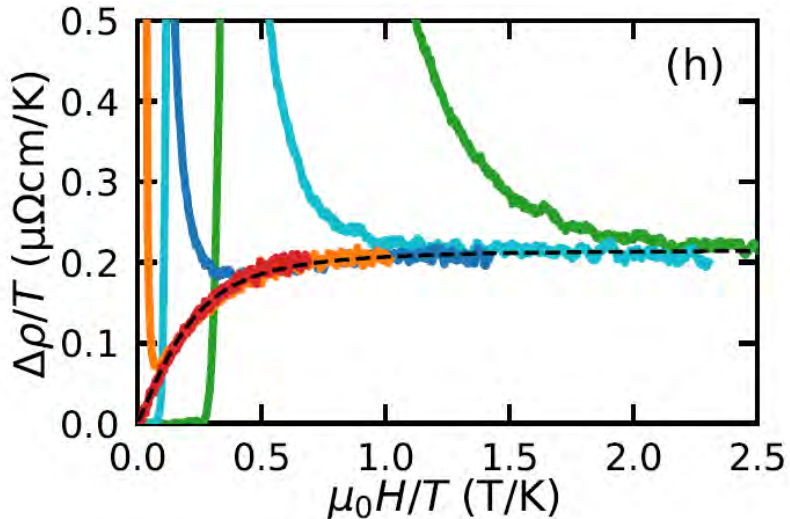
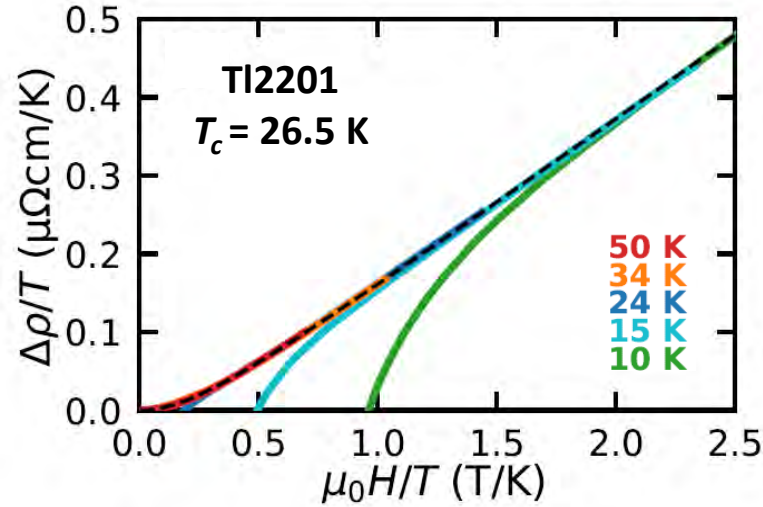
Sarkar *et al.*, *Sci. Adv.* **5**, eaav6753 (19)



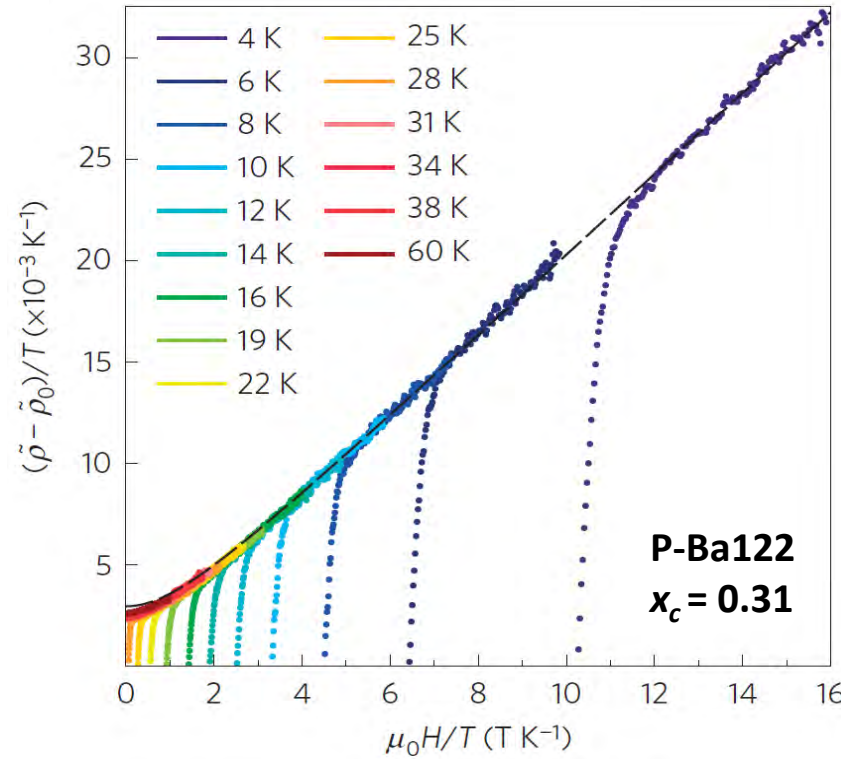
$$\rho(H, T) = \rho(0, 0) + \sqrt{(\alpha k_B T)^2 + (\gamma \mu_B \mu_0 H)^2}$$

- $\Delta\rho/T$ scales with H/T and follows quadrature form similar to that seen in pnictides, chalcogenides and n -doped cuprates near their respective magnetic and nematic QCPs.

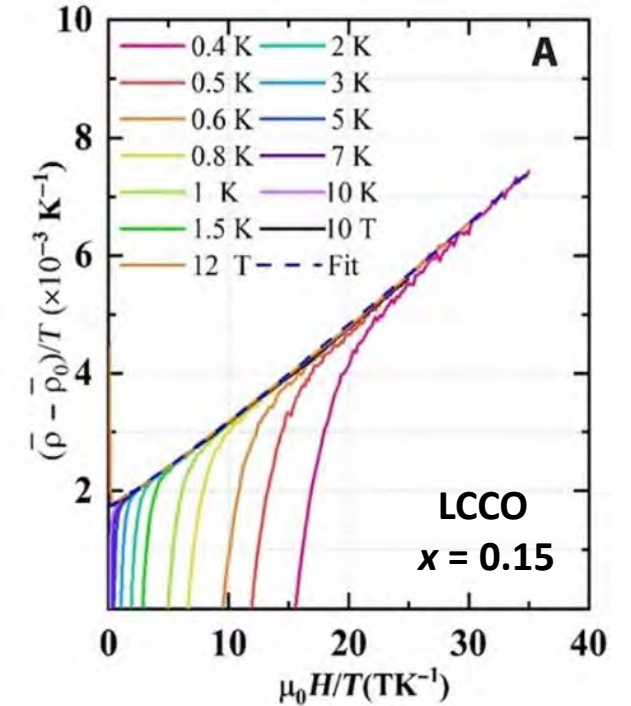
non-Boltzmann transport in SM regime



Hayes *et al.*, *Nat. Phys.* **12**, 916 (16)

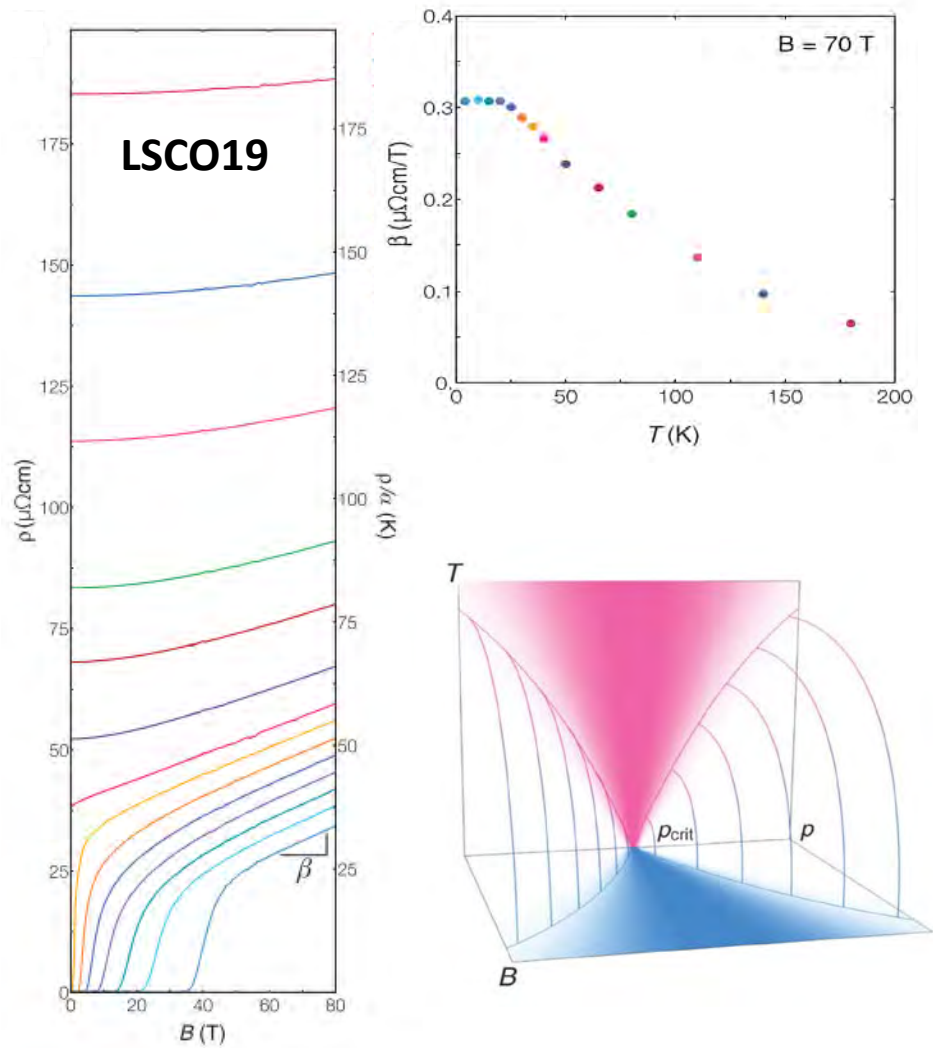


Sarkar *et al.*, *Sci. Adv.* **5**, eaav6753 (19)

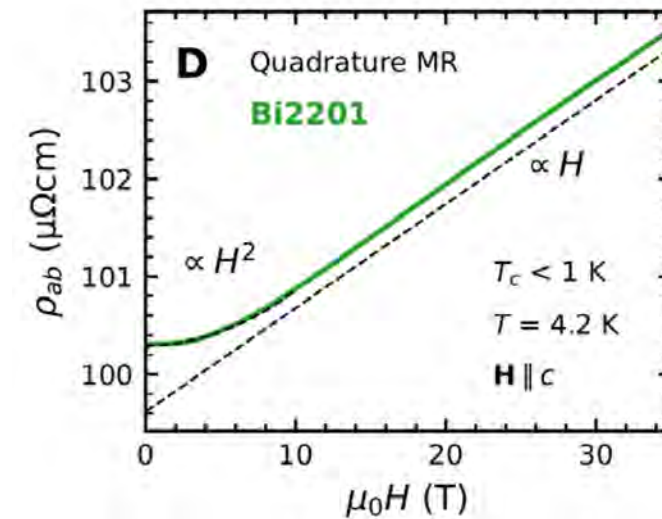
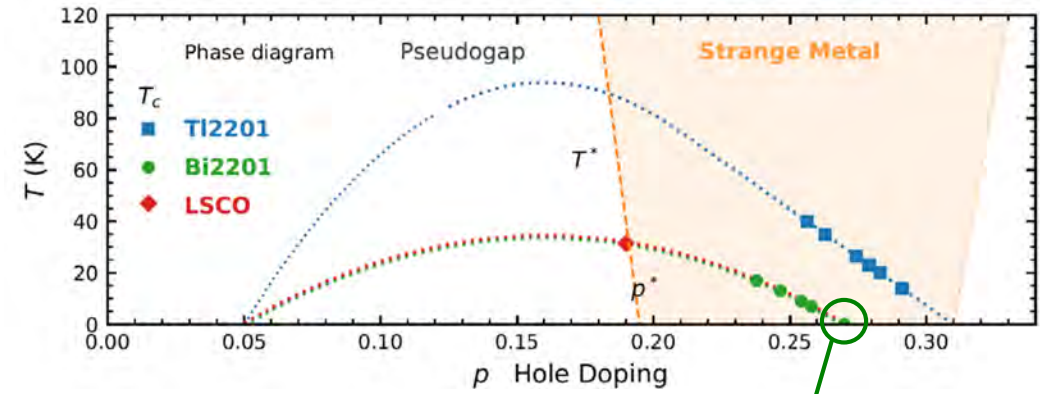


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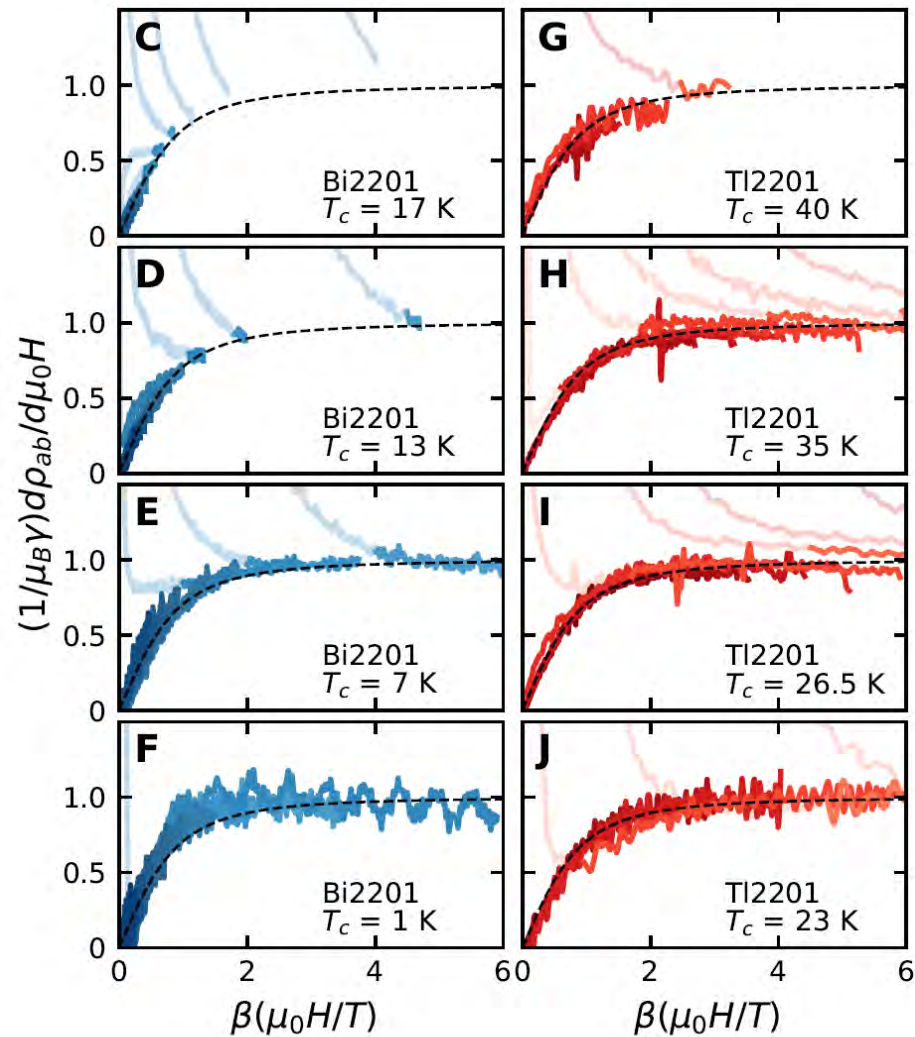
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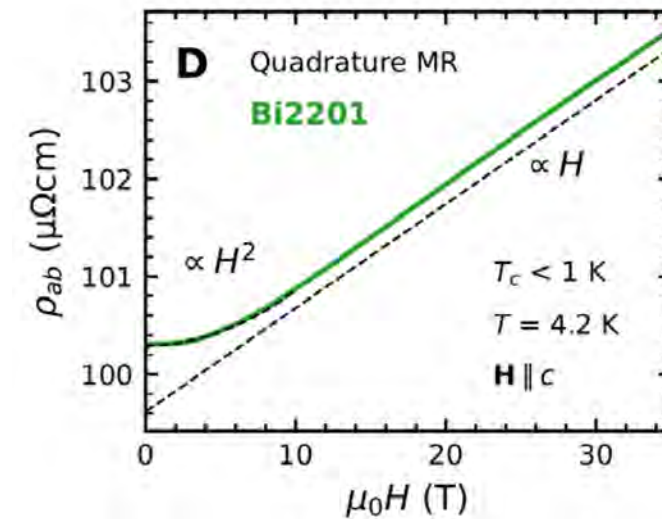
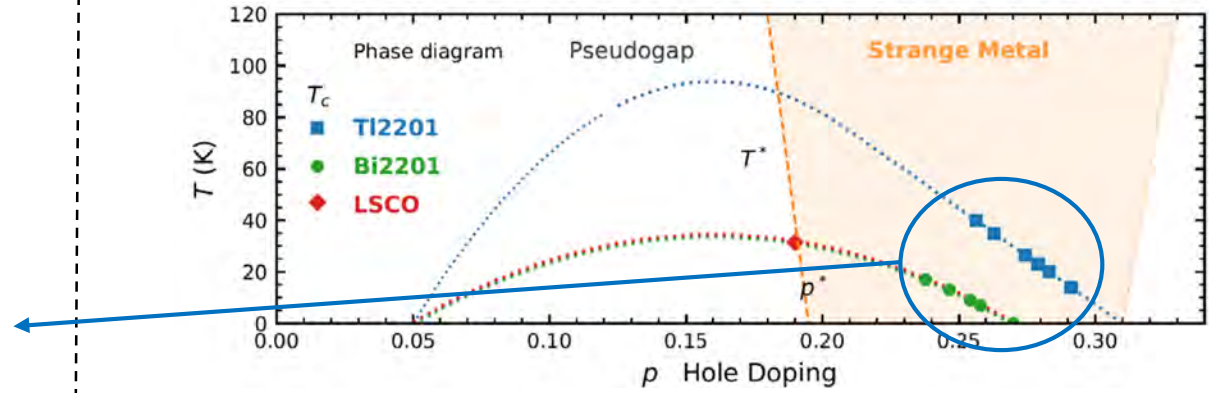
Giraldo-Gallo *et al.*, *Science* 361 479 (18)



- Same H -linear MR found very far from p^*

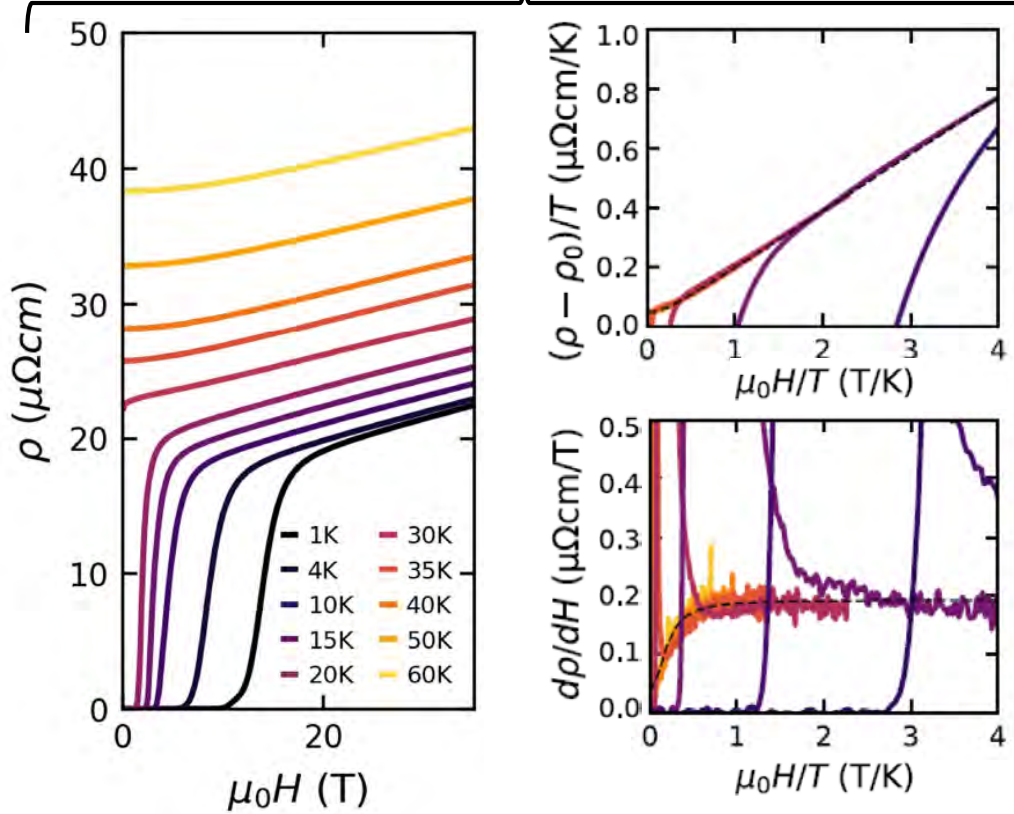


- Same behaviour observed across broad doping range

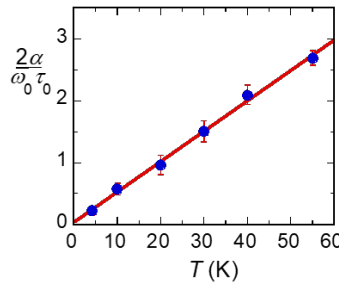
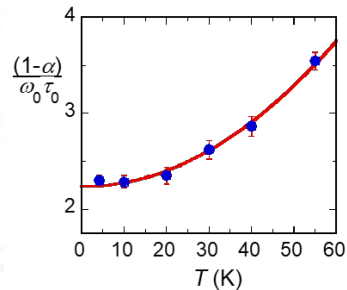
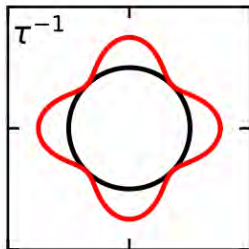
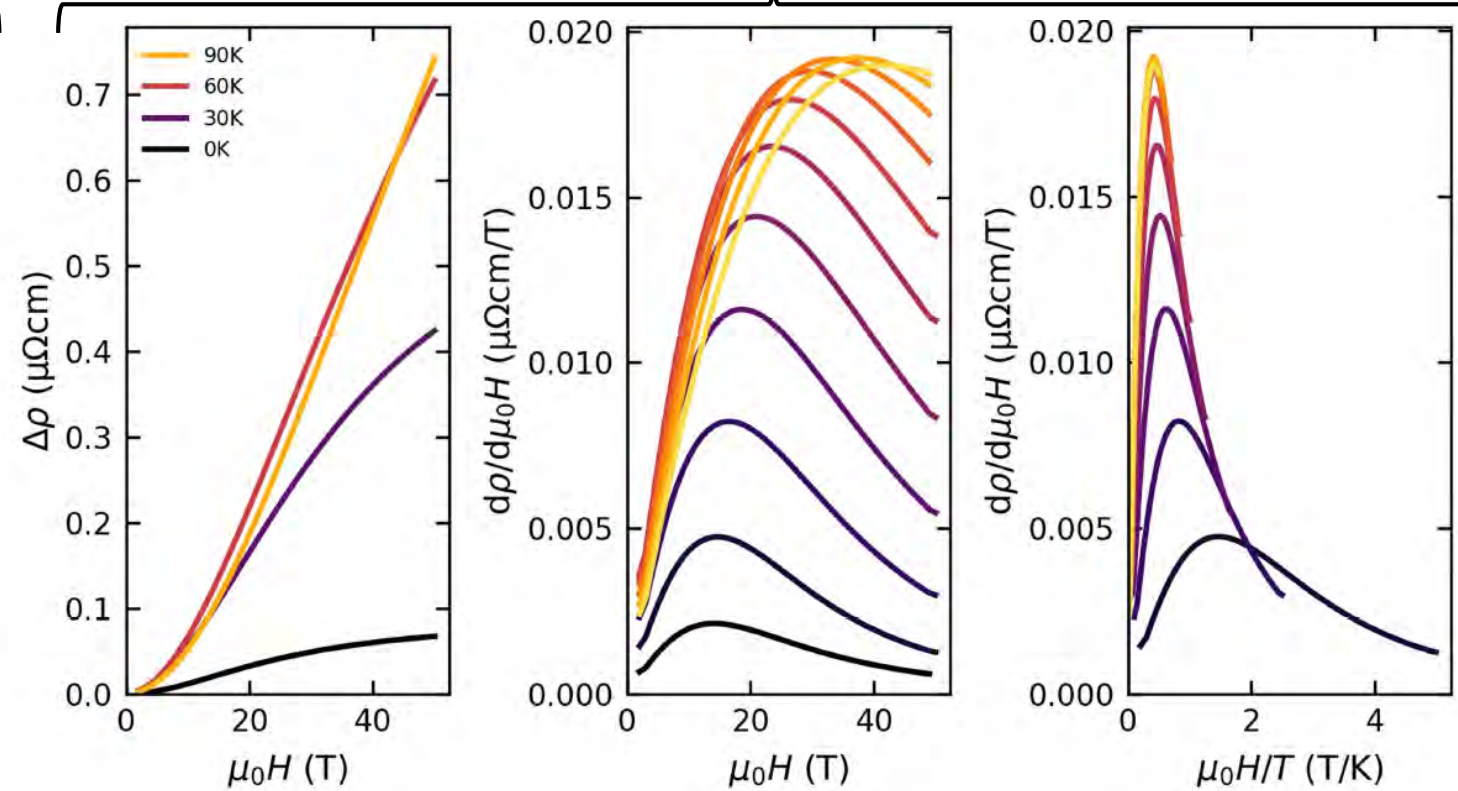


- Same H -linear MR found very far from ρ^*

Data



ADMR/Hall parameterization



Simulated MR:

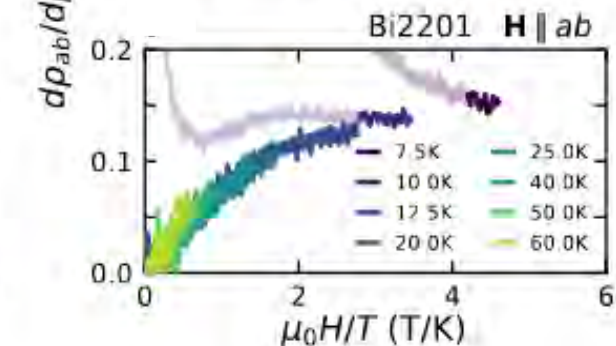
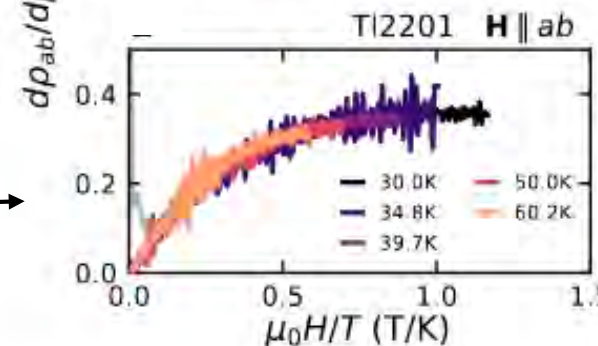
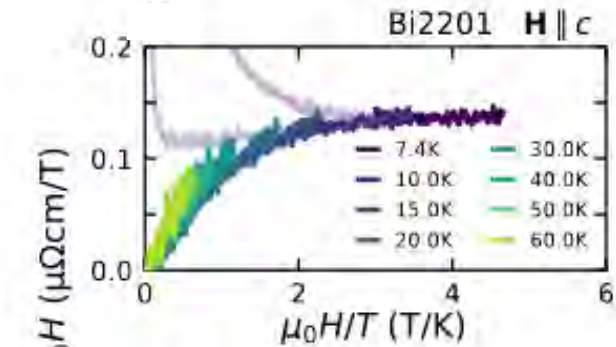
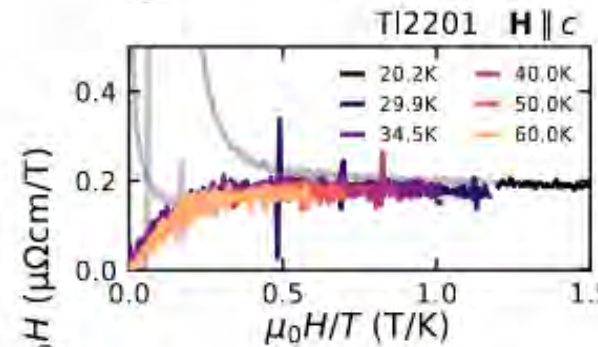
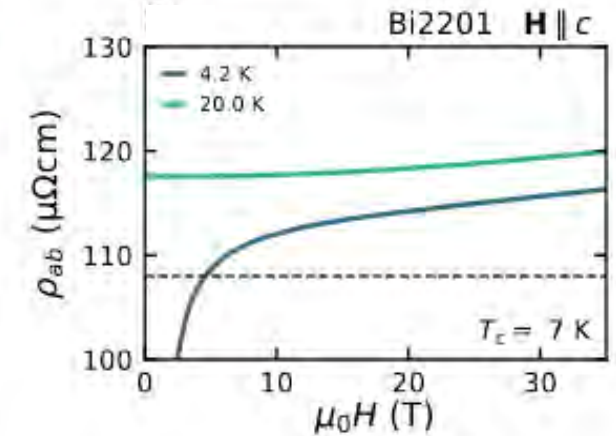
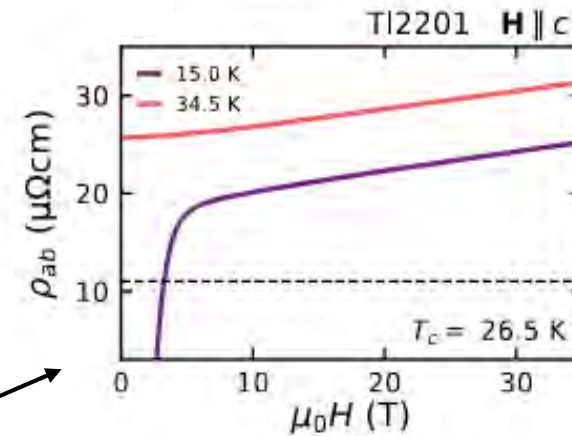
- More than an order of magnitude smaller than the actual MR
- Shows tendency to saturate at relatively modest fields.
- No quadrature H/T scaling

Boltzmann transport in SM regime

Recall Kohler's rule

$$\frac{\Delta\rho}{\rho(0)} \approx (\omega_c\tau)^2 \propto \left(\frac{H}{\rho(0)}\right)^2$$

- MR orders of magnitude larger than expected from estimate of $\omega_c\tau$
- MR of same magnitude for Tl2201 and Bi2201, despite 10 x larger ρ_0 in latter
- No angle dependence in MR

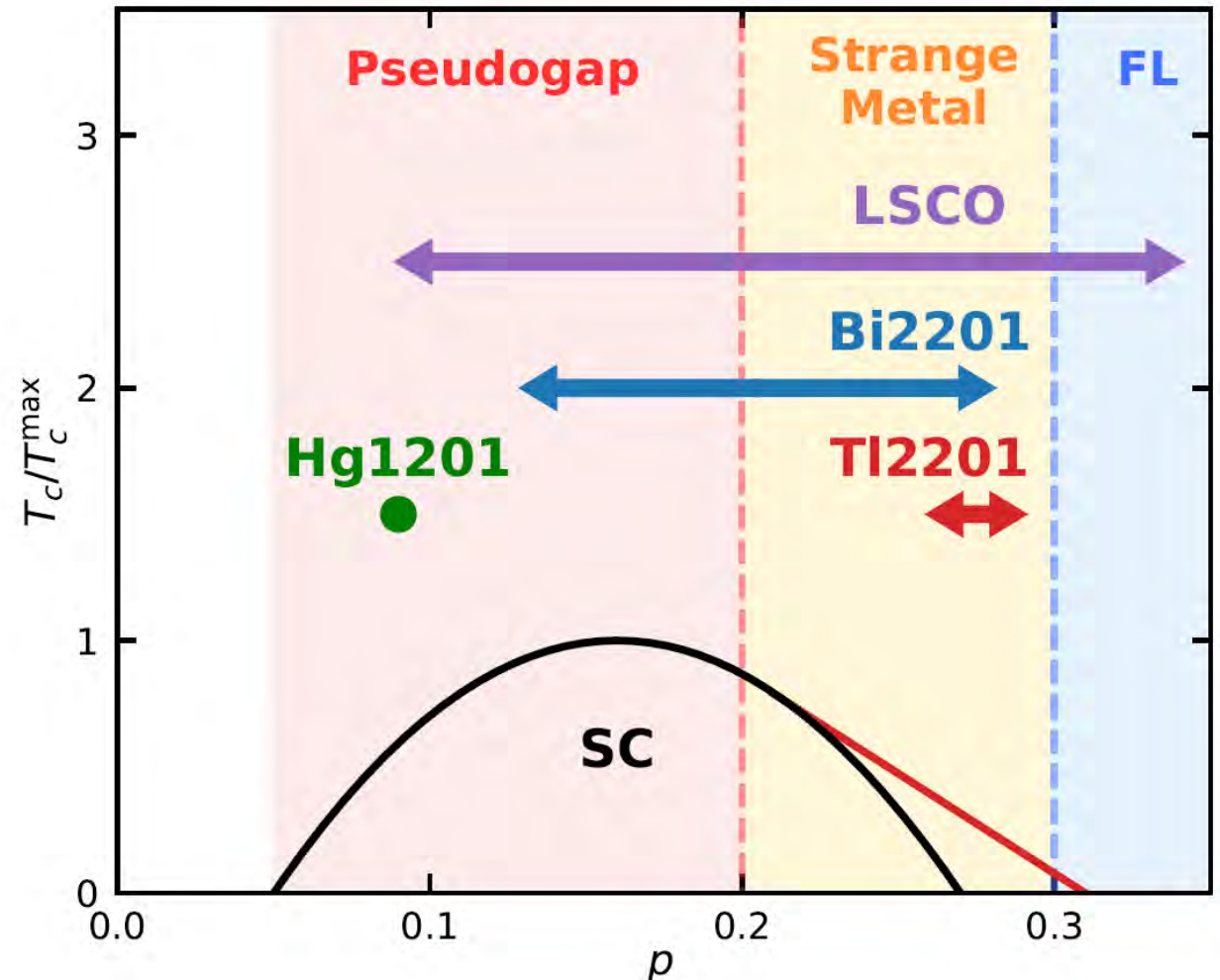


Q1: Does the H -linear slope have a dependence on T_c or p that can be linked to the T -linear component of $\rho_{ab}(T)$?

Q2: What happens to MR scaling below p^* as we enter into pseudogap regime?

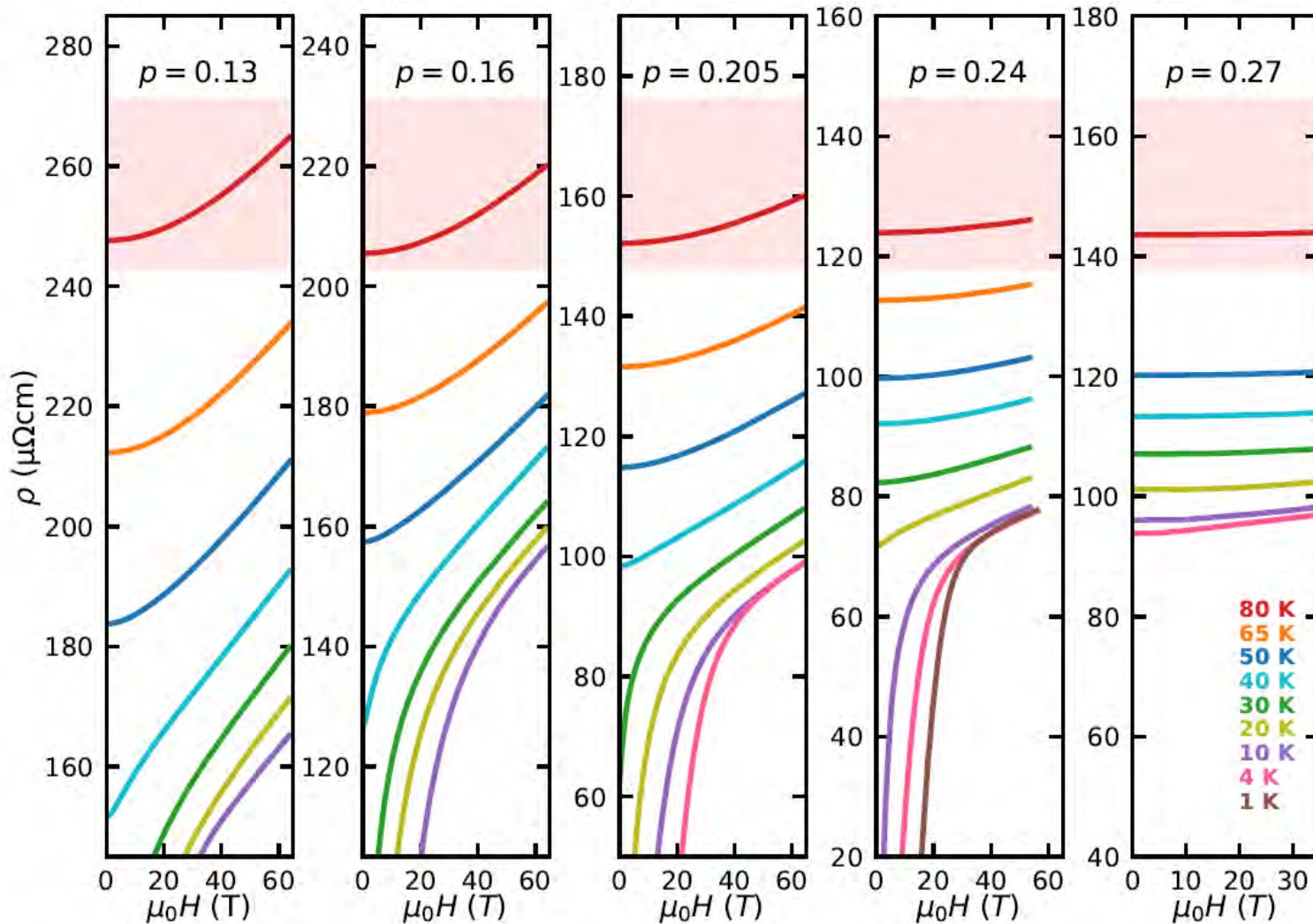
Q3: What happens beyond the superconducting dome? Does Kohler's scaling re-appear at high doping?

Q4: What is the link between H/T quadrature MR and modified Kohler scaling in optimally & under-doped cuprates?

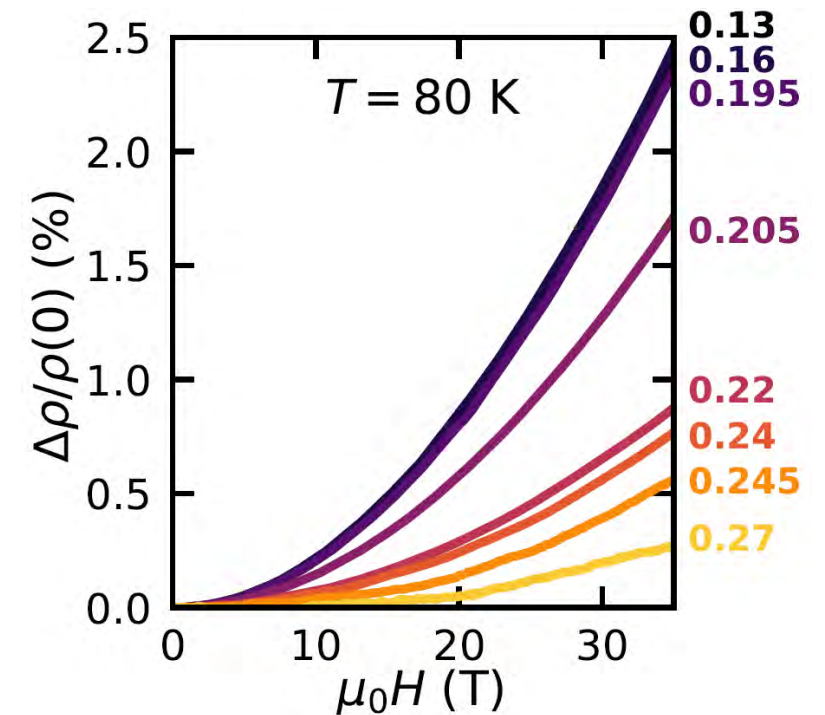


Q1: H -linear MR vs. p

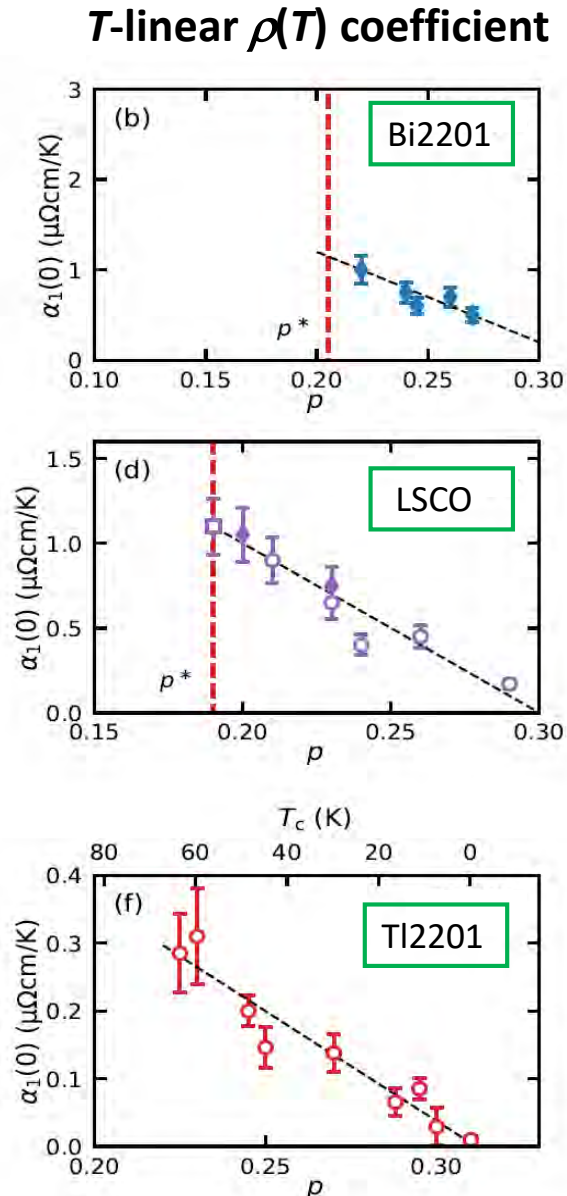
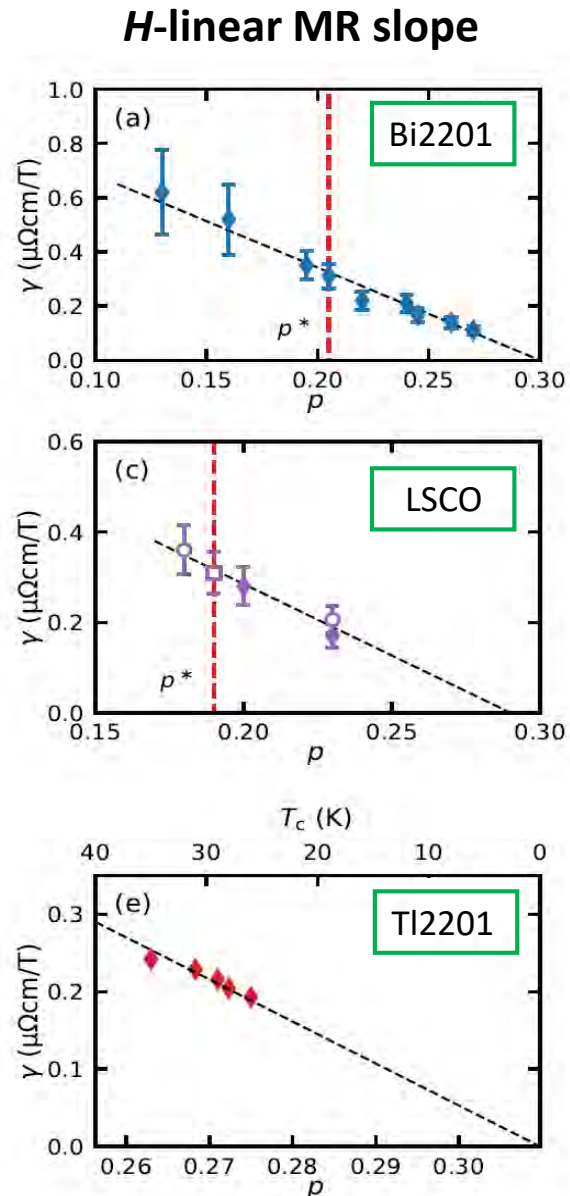
Bi2201



- At a fixed temperature, there is a clear doping dependence in the magnitude of the MR... even when normalized to $\rho(0)$.



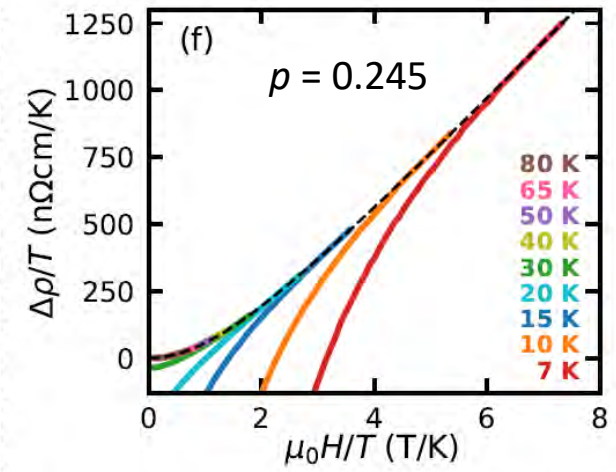
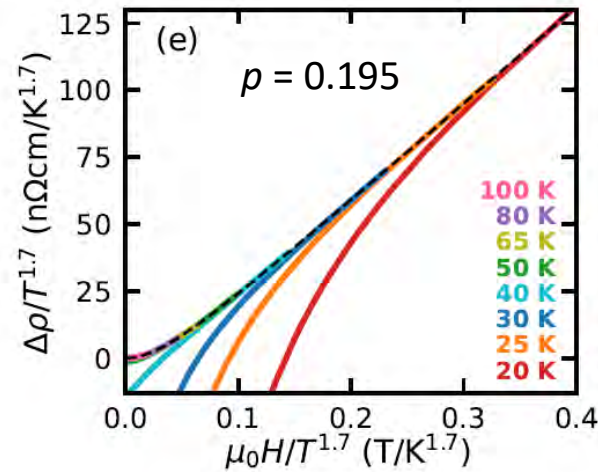
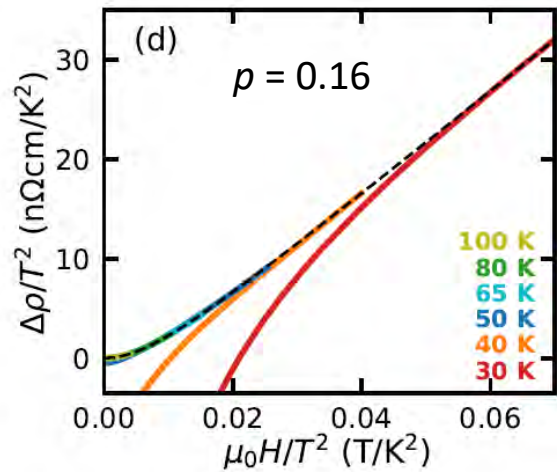
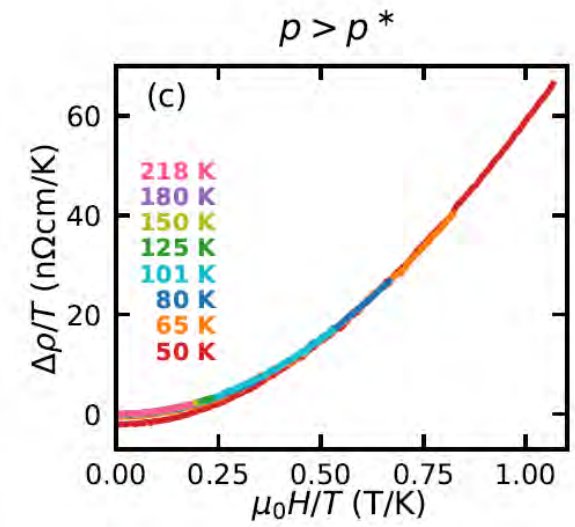
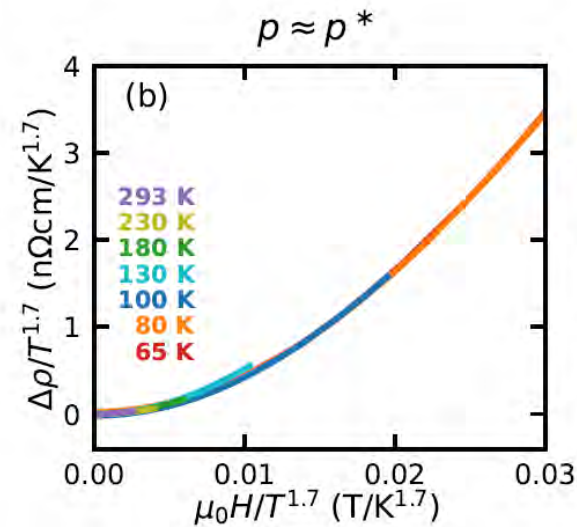
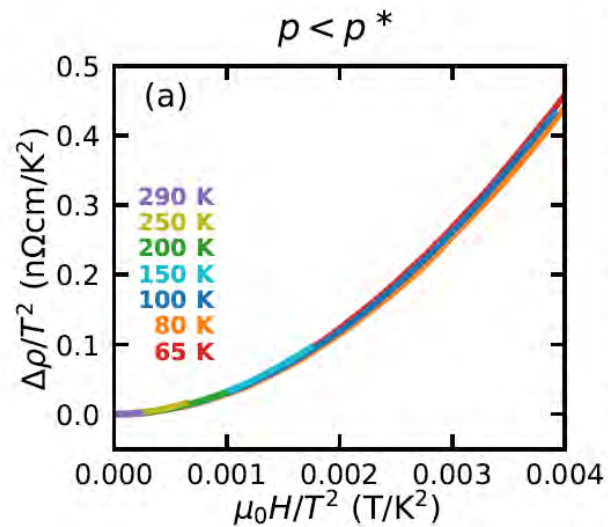
Q1: H -linear MR vs. p



- Beyond p^* , the H -linear MR slope found to show a similar variation with p (or T_c) as the coefficient of the T -linear zero-field resistivity for all three families.
- Below p^* , H -linear slope continues to rise with decreasing p , which we attribute to a loss of carriers inside the pseudogap regime.
- Suggests that within strange metal regime, T -linear resistivity and H -linear MR are indeed intrinsically linked.

Q2: MR scaling across p^*

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H/T^2 scaling

$H/T^{1.7}$ scaling

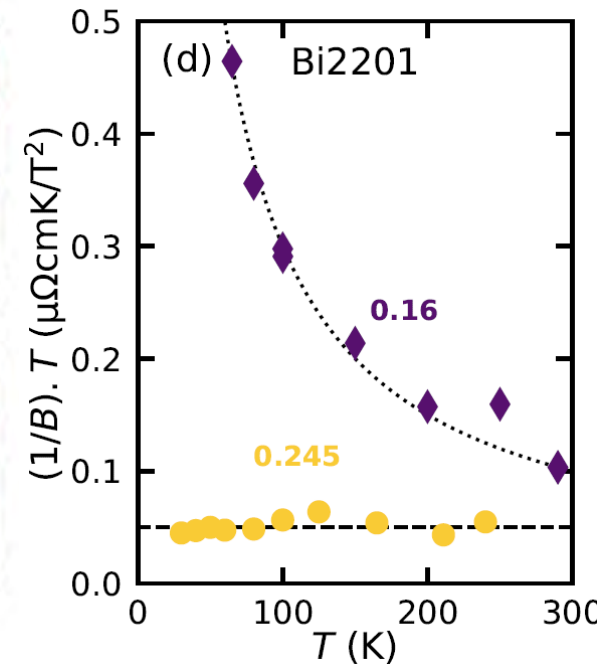
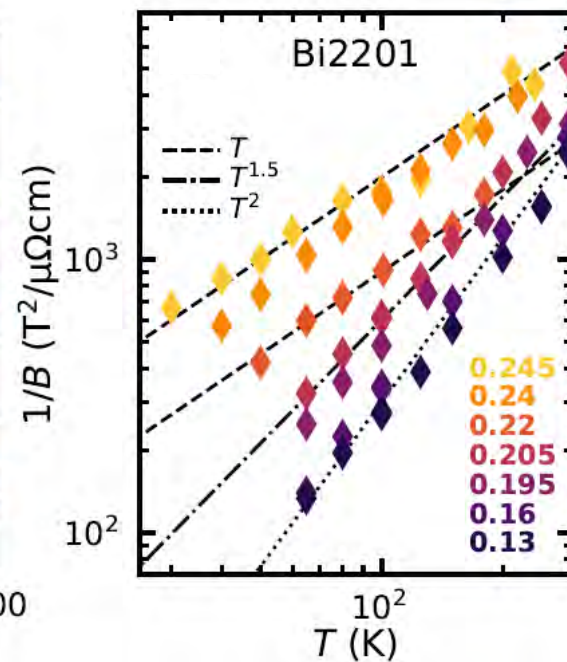
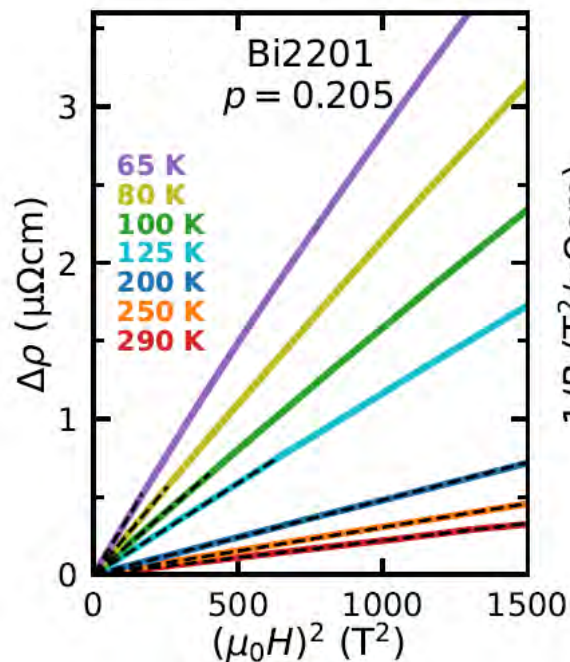
H/T scaling

Q2: MR scaling across p^*

Another way to reveal type of scaling behavior observed is to look at T -dependence of the slope B of the low-field MR

$$\Delta\rho(H, T) = B(T)(\mu_0 H)^2$$

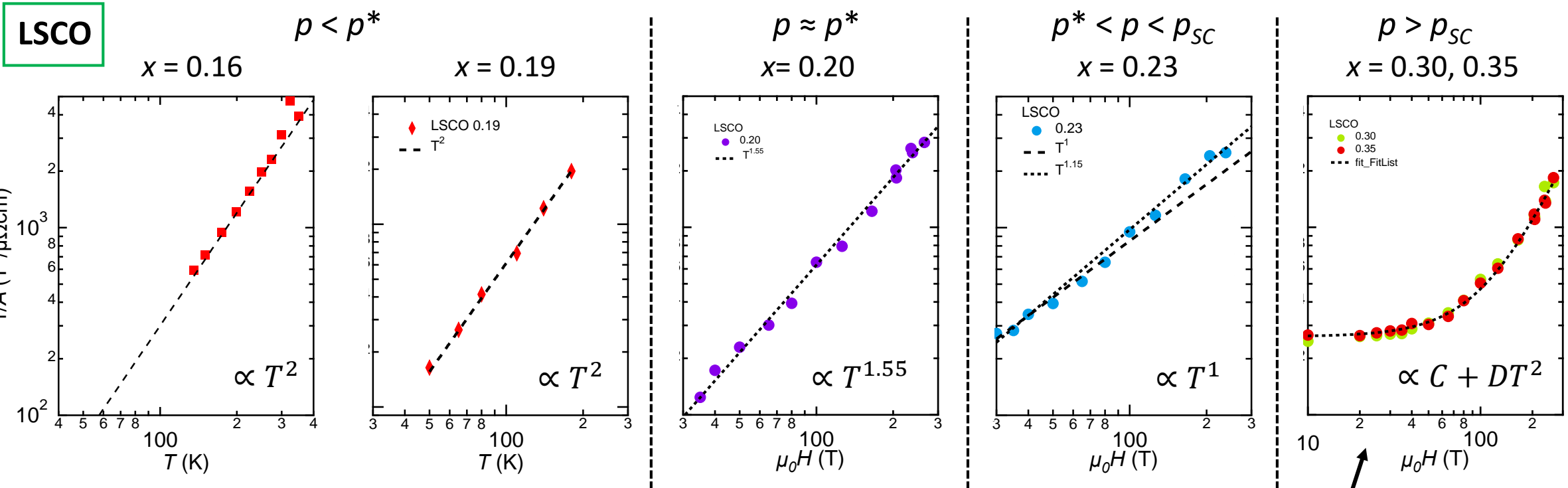
(Recall that for Kohler's or modified Kohler's rule, $\Delta\rho(H) = \frac{(\mu_0 H)^2}{\rho(0)}$ or $\Delta\rho(H) = \frac{\rho(0)}{\cot^2\theta_H} (\mu_0 H)^2$)



Power-law scaling observed in normal state of all SC samples with variable exponent m

Q3: MR scaling across p_{SC}

Only with LSCO can we access the non-SC state on the overdoped side ($p > 0.27$), but the advantage is we can compare directly across the different regimes. Here we plot the T -dependence of the inverse of the low- H H^2 coefficient within the different regimes:



Harris et al.,
PRL **75**, 1391 (95)

Giraldo-Gallo et al.,
Science **361**, 479 (18)

Recovery of Kohler scaling beyond strange metal regime.

MR scaling across p^* and p_{SC}

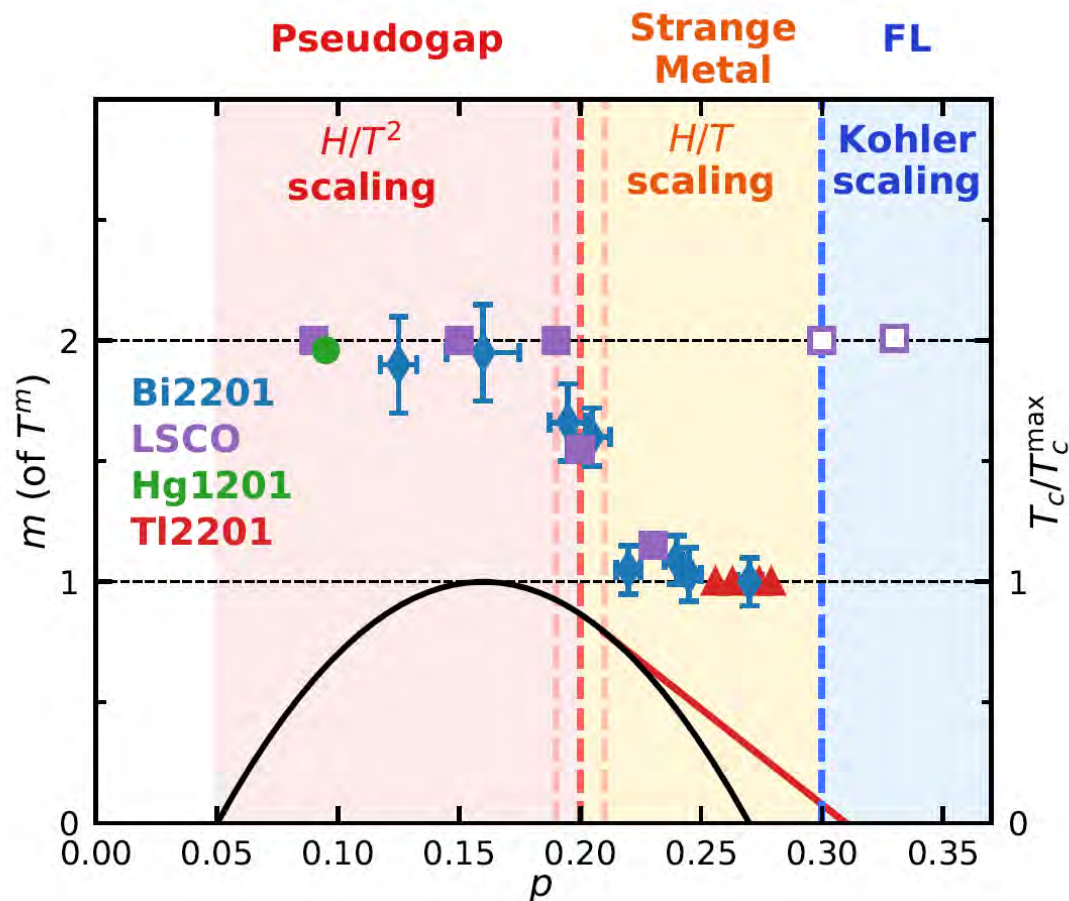
There are thus 3 types of scaling:

H/T^2 scaling below p^*
 H/T scaling for $p_{SC} > p > p^*$
 Kohler scaling for $p > p_{SC}$

$$\rho(H, T) = \underbrace{\mathcal{F}(T)}_{\text{'Some other Contribution'}} + \underbrace{\sqrt{(\alpha_m T^m)^2 + (\gamma \mu_0 H)^2}}_{\text{Quadrature MR}}$$

'Some other Contribution'

Quadrature MR

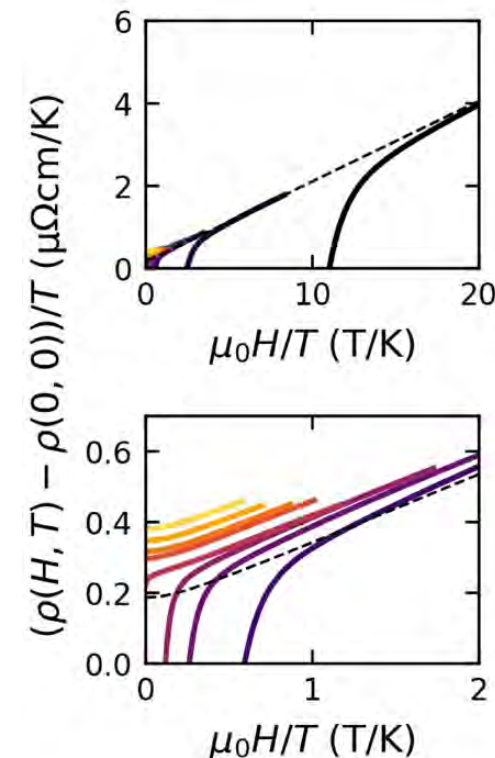


$$\mathcal{F}(T) = \rho_0 + A_1 T + A_2 T^2$$

$$A_1 T + \alpha k_B T = \alpha_1(0) T$$

Other component does not appear to contribute to in-plane MR, but is visible in the c-axis MR and in-plane Hall effect

- DUAL CHARACTER OF STRANGE METAL



4) Q₄: Power-law scaling and MKR

Modified Kohler scaling

$$\frac{\Delta\rho}{\rho(0)} \approx (\tan\theta_H)^2 \propto \left(\frac{H}{\cot\theta_H}\right)^2$$

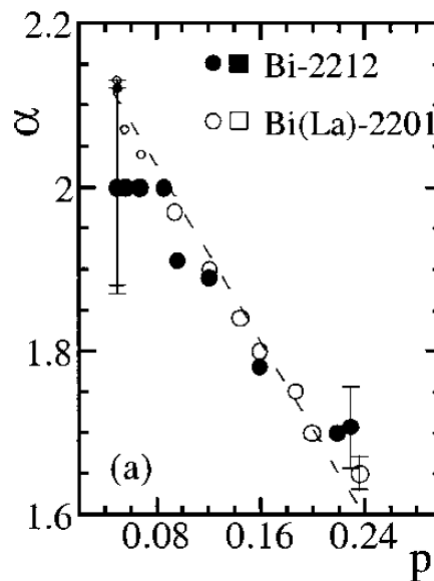
$$\cot\theta_H \propto A + BT^\alpha$$

$$\frac{\Delta\rho}{\rho(0)} \propto \left(\frac{1}{A + BT^\alpha}\right)^2$$

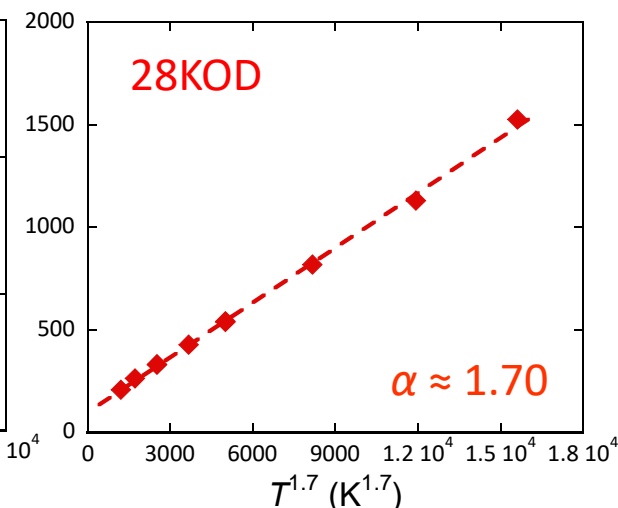
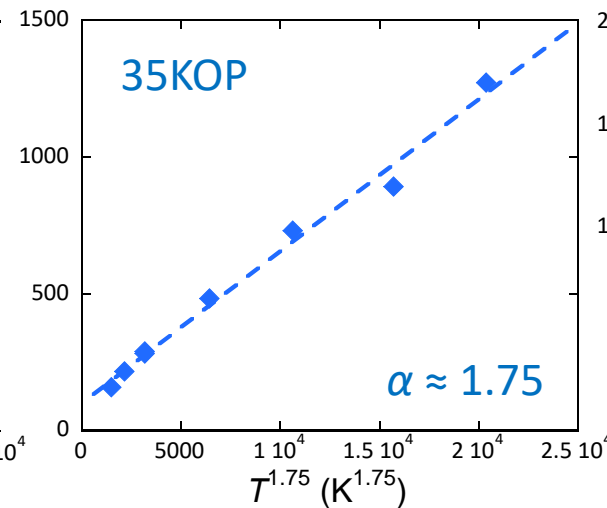
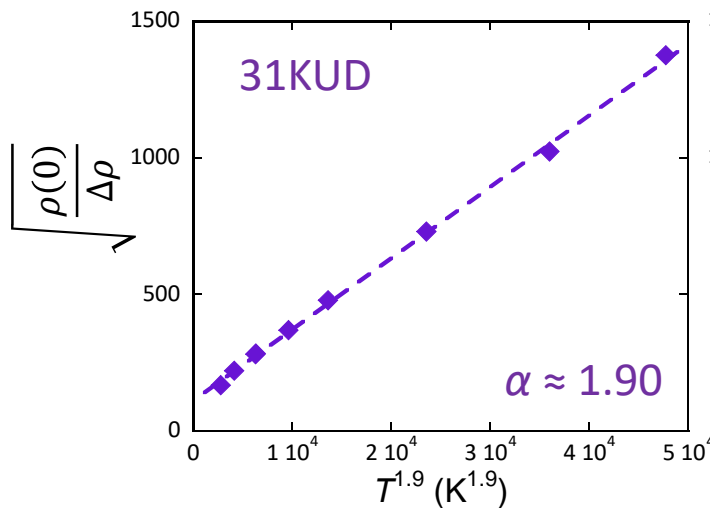
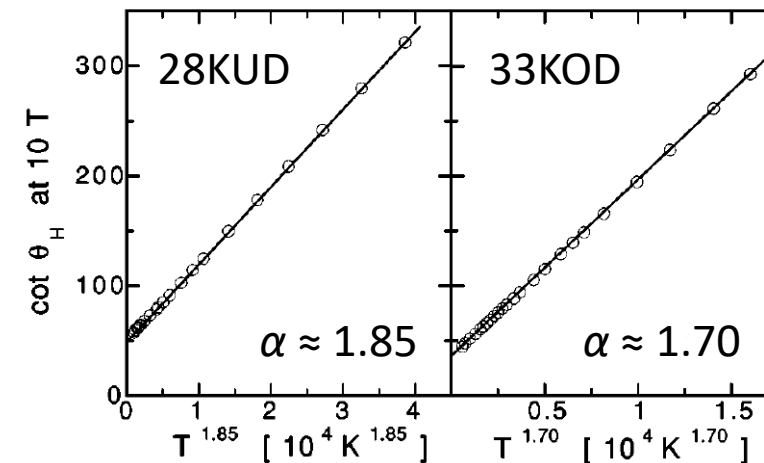
$$\Rightarrow \sqrt{\frac{\rho(0)}{\Delta\rho}} \propto A + BT^\alpha$$

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Konstantinovic *et al.*,
PRB 62 R11989 (00)



Ando + Murayama, PRB 60 R6991 (99)



4) Q₄: Power-law scaling and MKR

Modified Kohler scaling

Berben, Ayres *et al.*, 2203.04867

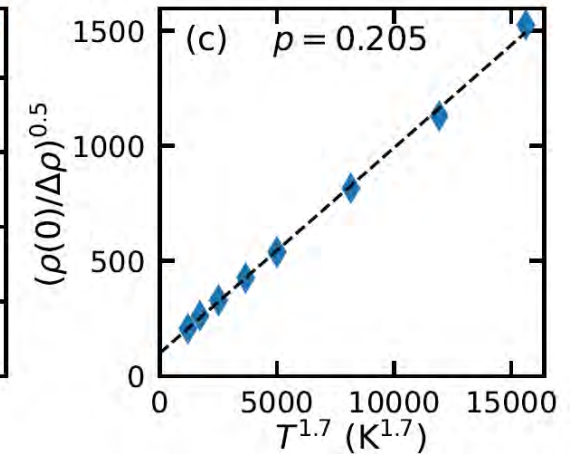
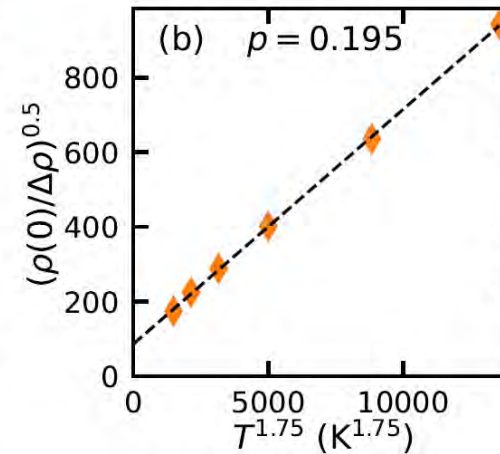
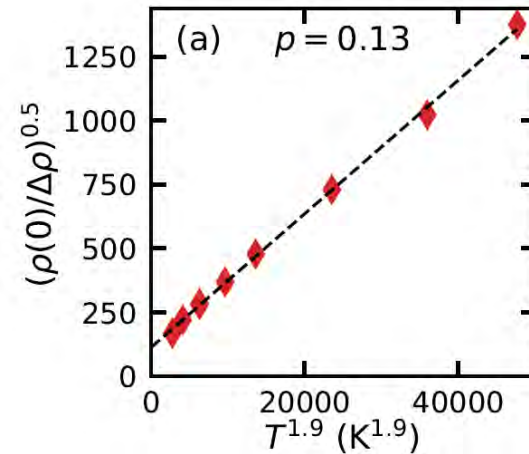
$$\frac{\Delta\rho}{\rho(0)} \approx (\tan\theta_H)^2 \propto \left(\frac{H}{\cot\theta_H}\right)^2$$

$$\cot\theta_H \propto A + BT^\alpha$$

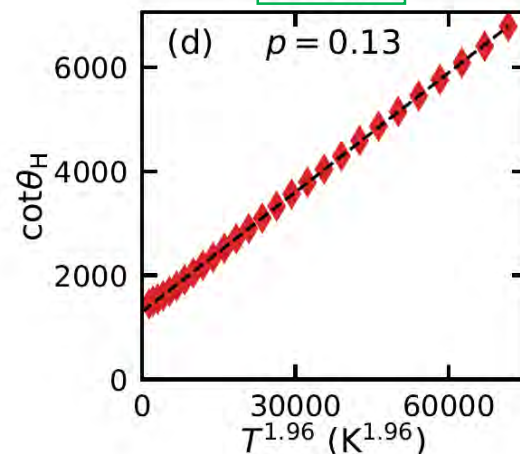
$$\frac{\Delta\rho}{\rho(0)} \propto \left(\frac{1}{A + BT^\alpha}\right)^2$$

$$\Rightarrow \sqrt{\frac{\rho(0)}{\Delta\rho}} \propto A + BT^\alpha$$

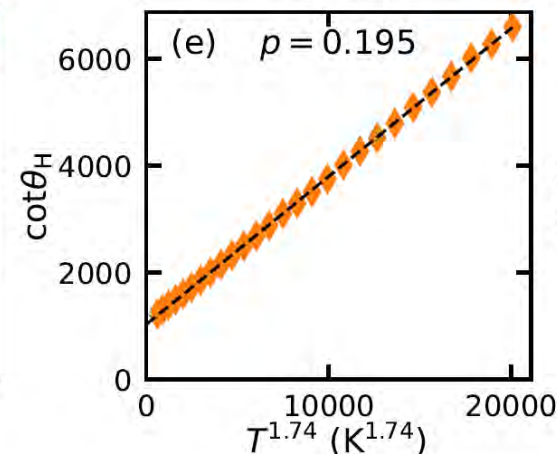
Although $\Delta\rho$ is a pure power law, the relative MR inherits a residual term from $\rho(T)$.



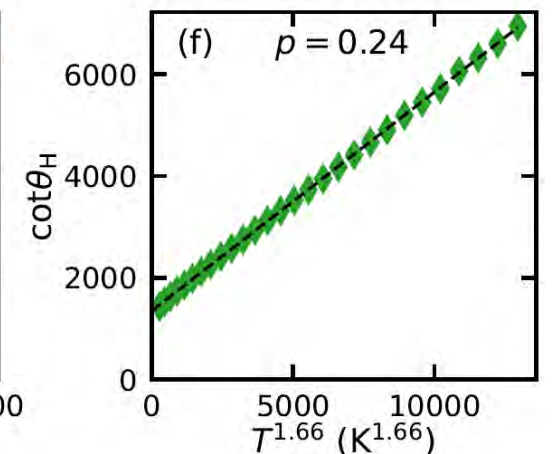
Bi2201



Bi2201



Bi2201

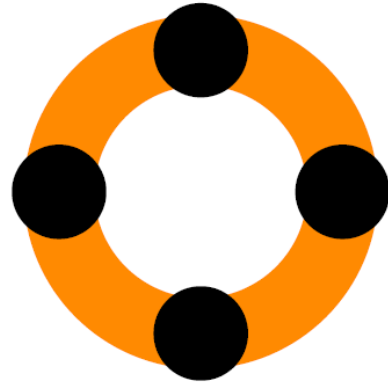


Possible sources of H -linear MR



Mesoscopic disorder

Singleton, *PRM* (20)
Boyd & Phillips, *PRB* (19)
Patel *et al.*, *PRX* (18)



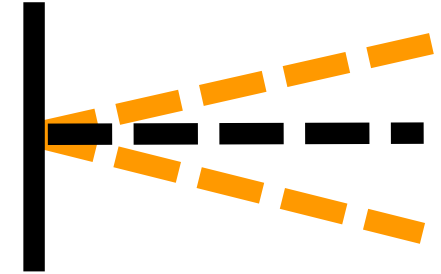
Hot spots

Koshelev, *PRB* (16)
Maksimovic *et al.*, *PRX* (20)
Grissonanche *et al.*, *Nature* (21)



Sharp FS corners

Koshelev, *PRB* (13)
Maksimovic *et al.*, *PRX*(20)
Grissonanche *et al.*, *Nature* (21)



Zeeman coupling

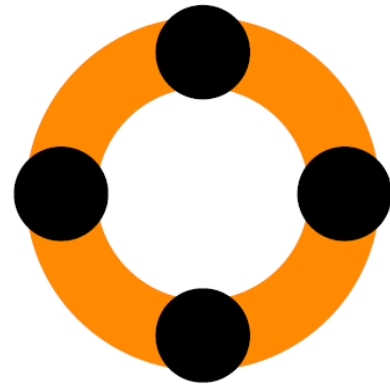
Banerjee *et al.*, *PRB* (21)
Marino & Arouca, *SST* (21)

Possible sources of H -linear MR



Mesoscopic disorder

Singleton, *PRM* (20)
Boyd & Phillips, *PRB* (19)
Patel *et al.*, *PRX* (18)



Hot spots

Koshelev, *PRB* (16)
Maksimovic *et al.*, *PRX* (20)
Grissonnanche *et al.*, *Nature* (21)



Sharp FS corners

Koshelev, *PRB* (13)
Maksimovic *et al.*, *PRX*(20)
Grissonnanche *et al.*, *Nature* (21)



Impeded cyclotron motion

Hinlopen *et al.* [2201.03292](#)

Many origins can be generalized by a modification of BTE incorporating a bound for cyclotron motion somewhere on the Fermi surface.

$$\sigma_{ij} = \frac{e^2}{4\pi^3\hbar} \int_{FS} d^2k \int_0^{\text{bound}} dt \frac{v_i(0)}{v_F(0)} v_j(-t) \exp\left(-\frac{t}{\tau_0}\right)$$

$$\sigma_{xx} = \frac{e^2 k_F^2}{2\pi^2 \hbar c} \int_0^{\pi/2} d\phi \int_0^{-\phi/\omega_c} dt \frac{v_x(0)}{v_F(0)} v_x(-t) \exp(-t/\tau_0)$$

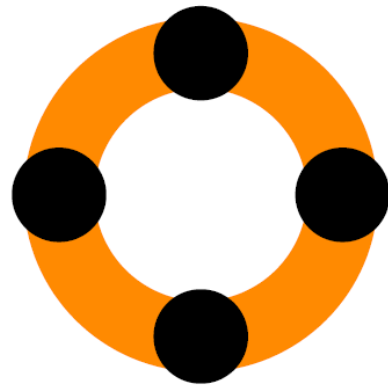
Unable to account for absence of $\rho(0)$ in MR scaling

Possible sources of H -linear MR



Mesoscopic disorder

Singleton, *PRM* (20)
 Boyd & Phillips, *PRB* (19)
 Patel *et al.*, *PRX* (18)



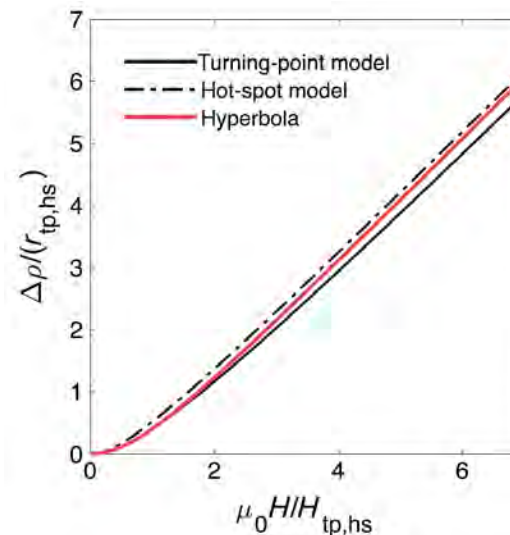
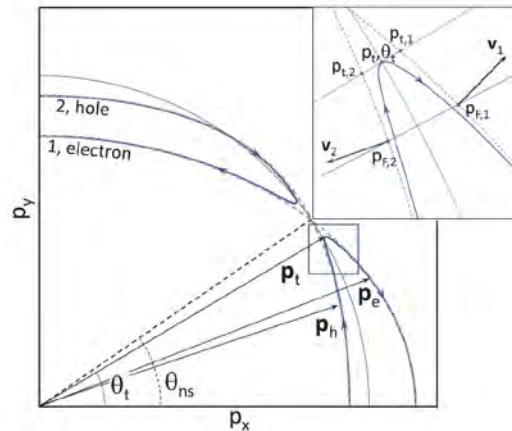
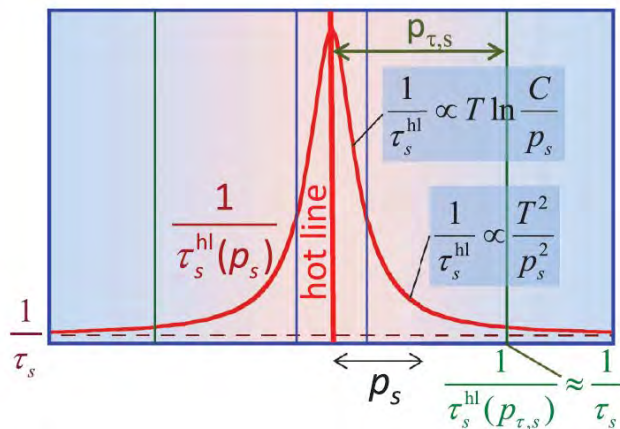
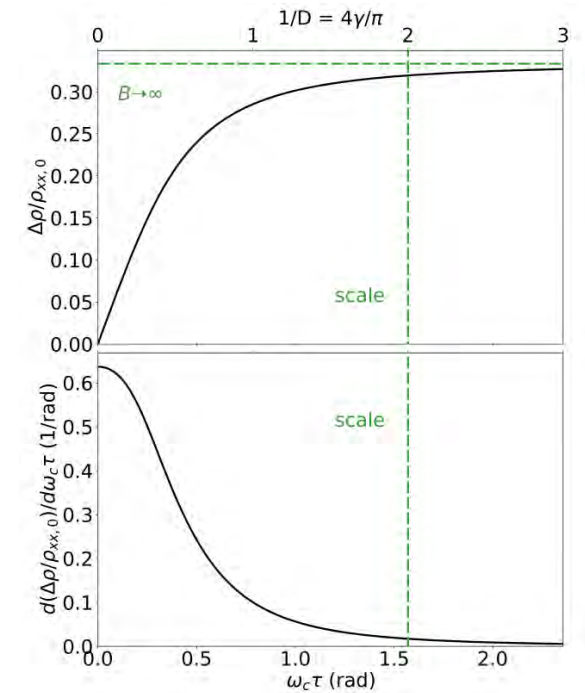
Hot spots

Koshelev, *PRB* (16)
 Maksimovic *et al.*, *PRX* (20)
 Grissonnanche *et al.*, *Nature* (21)



Sharp FS corners

Koshelev, *PRB* (13)
 Maksimovic *et al.*, *PRX*(20)
 Grissonnanche *et al.*, *Nature* (21)



Hinlopen *et al.*,
[2201.03292](https://arxiv.org/abs/2201.03292)

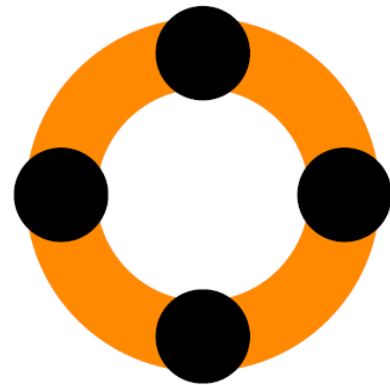
- Applied to pnictides
- H -linearity will eventually give way to saturation

Possible sources of H -linear MR



Mesoscopic disorder

Singleton, *PRM* (20)
 Boyd & Phillips, *PRB* (19)
 Patel *et al.*, *PRX* (18)



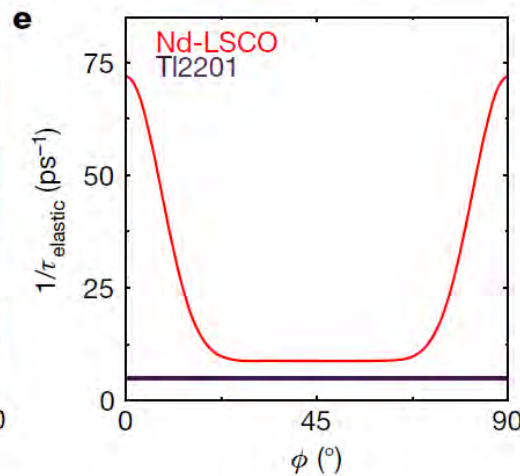
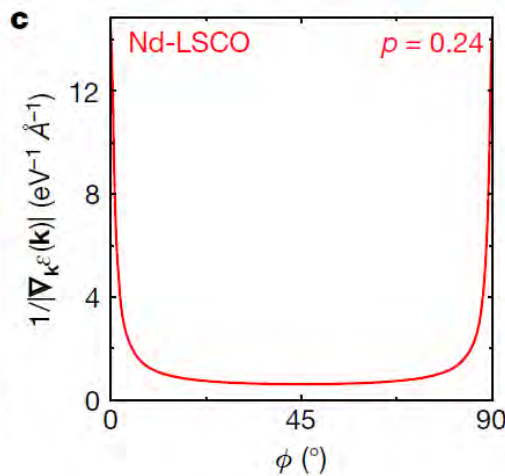
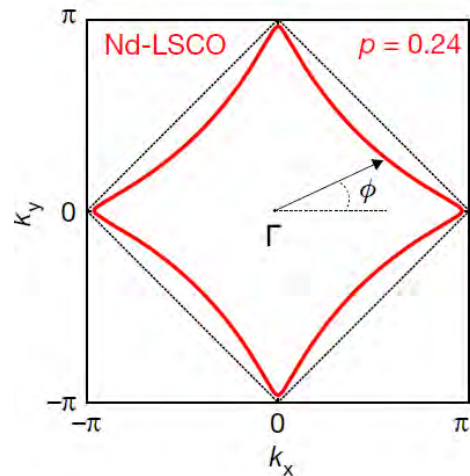
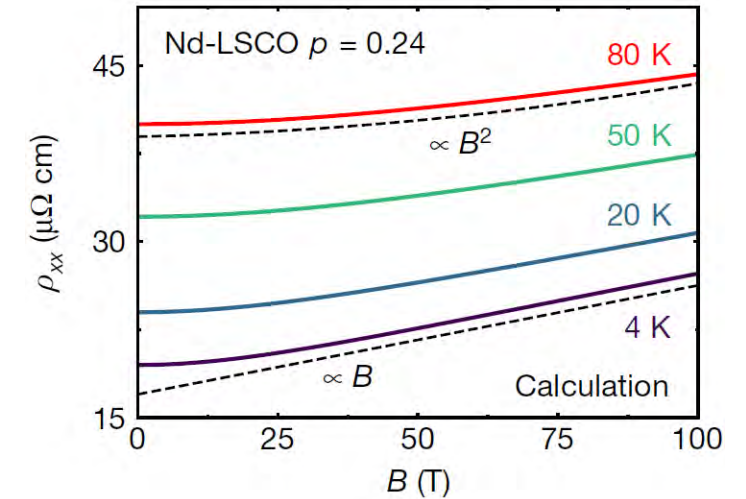
Hot spots

Koshelev, *PRB* (16)
 Maksimovic *et al.*, *PRX* (20)
Grissonnanche *et al.*, *Nature* (21)



Sharp FS corners

Koshelev, *PRB* (13)
 Maksimovic *et al.*, *PRX*(20)
Grissonnanche *et al.*, *Nature* (21)



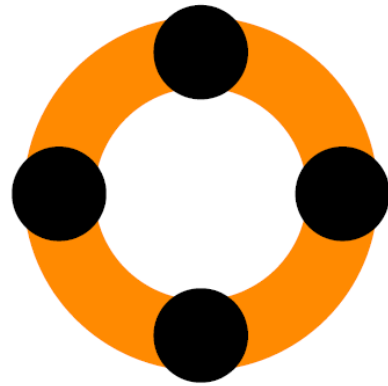
- Applied to cuprate near p^*
- Contains both sharp corners and extreme anisotropy.
- Not clear parameterization gives H/T scaling

Possible sources of H -linear MR



Mesoscopic disorder

Singleton, *PRM* (20)
 Boyd & Phillips, *PRB* (19)
 Patel *et al.*, *PRX* (18)



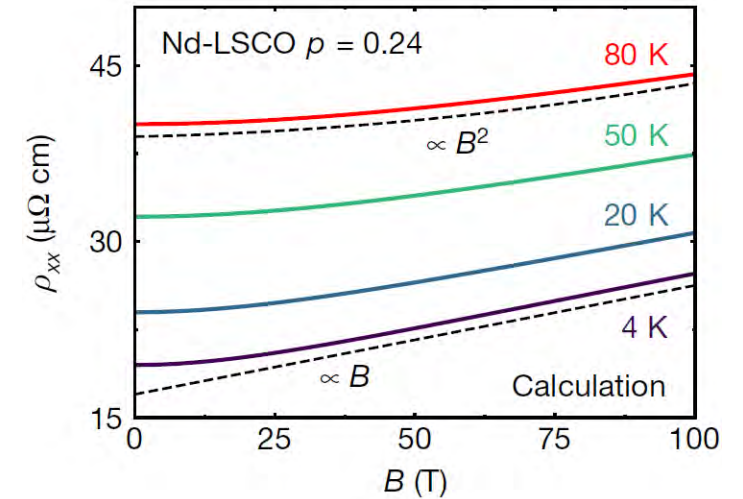
Hot spots

Koshelev, *PRB* (16)
 Maksimovic *et al.*, *PRX* (20)
Grissonnanche *et al.*, *Nature* (21)



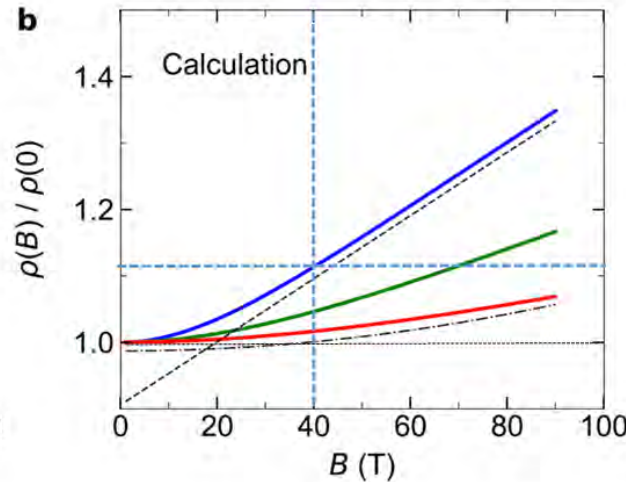
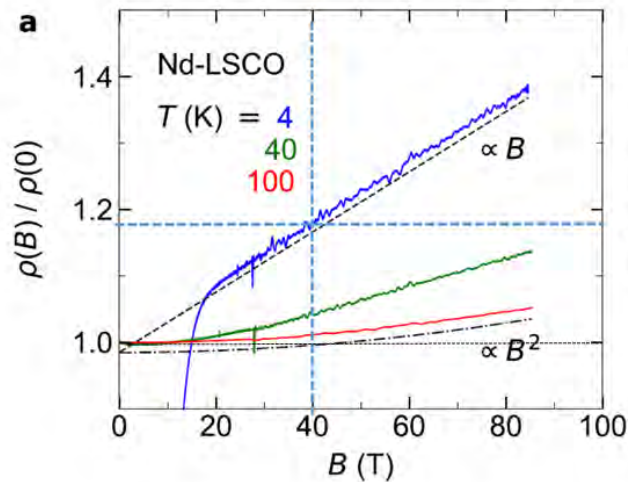
Sharp FS corners

Koshelev, *PRB* (13)
 Maksimovic *et al.*, *PRX*(20)
Grissonnanche *et al.*, *Nature* (21)

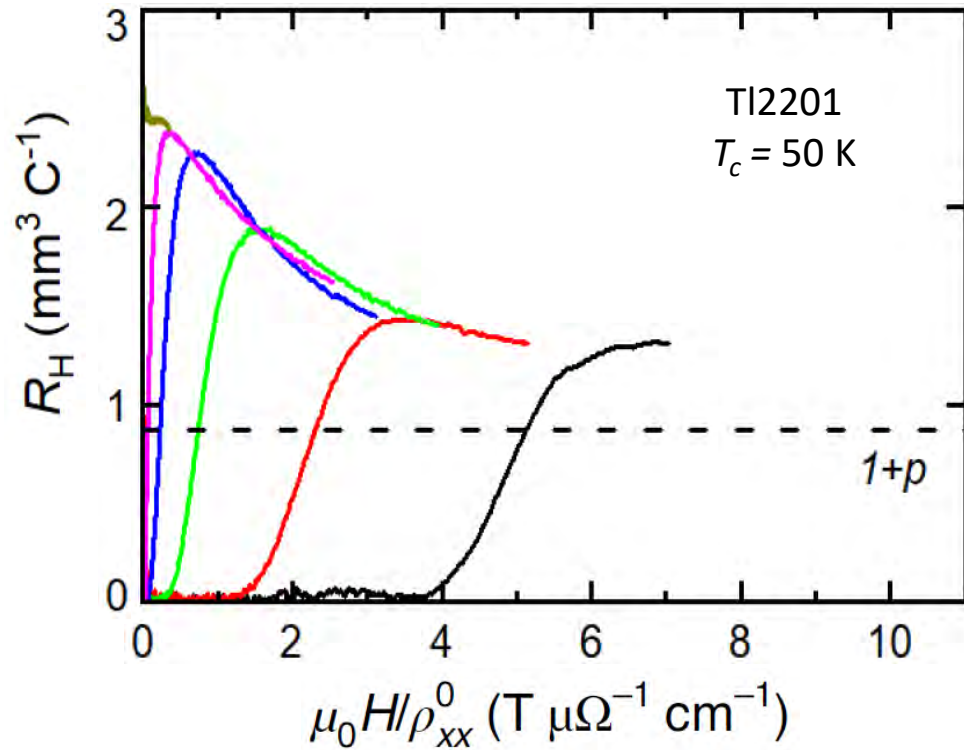


- Applied to cuprate near p^*
- Contains both sharp corners and extreme anisotropy.
- Not clear parameterization gives H/T scaling
- Similar parameterization cannot work for TI2201

Ataei *et al.*,
 2203.05035 (22)

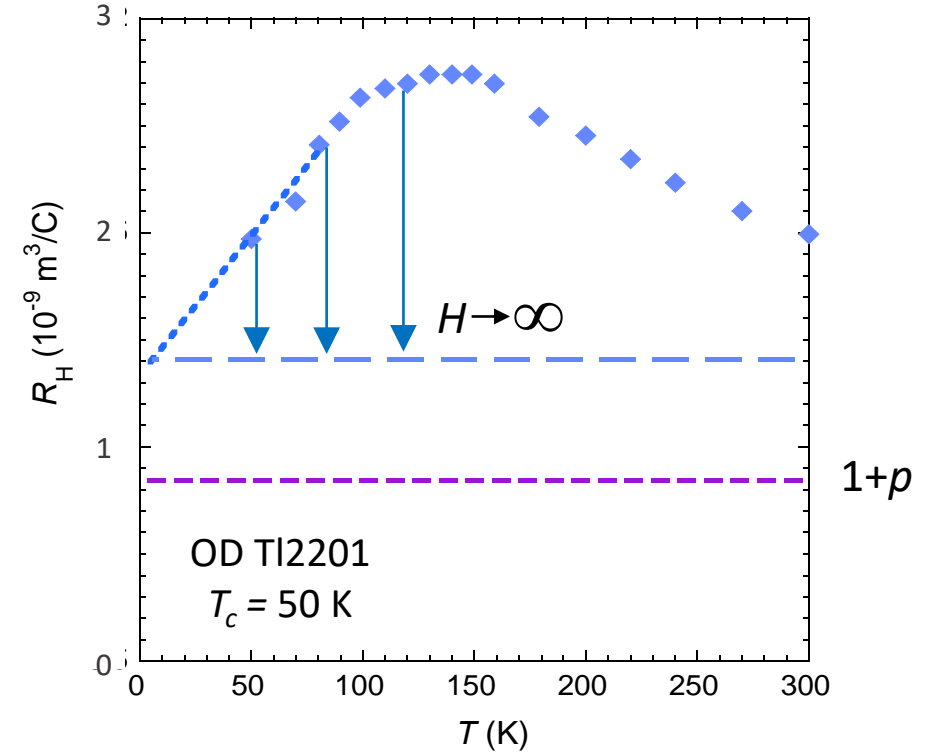


Superconductivity within SM regime



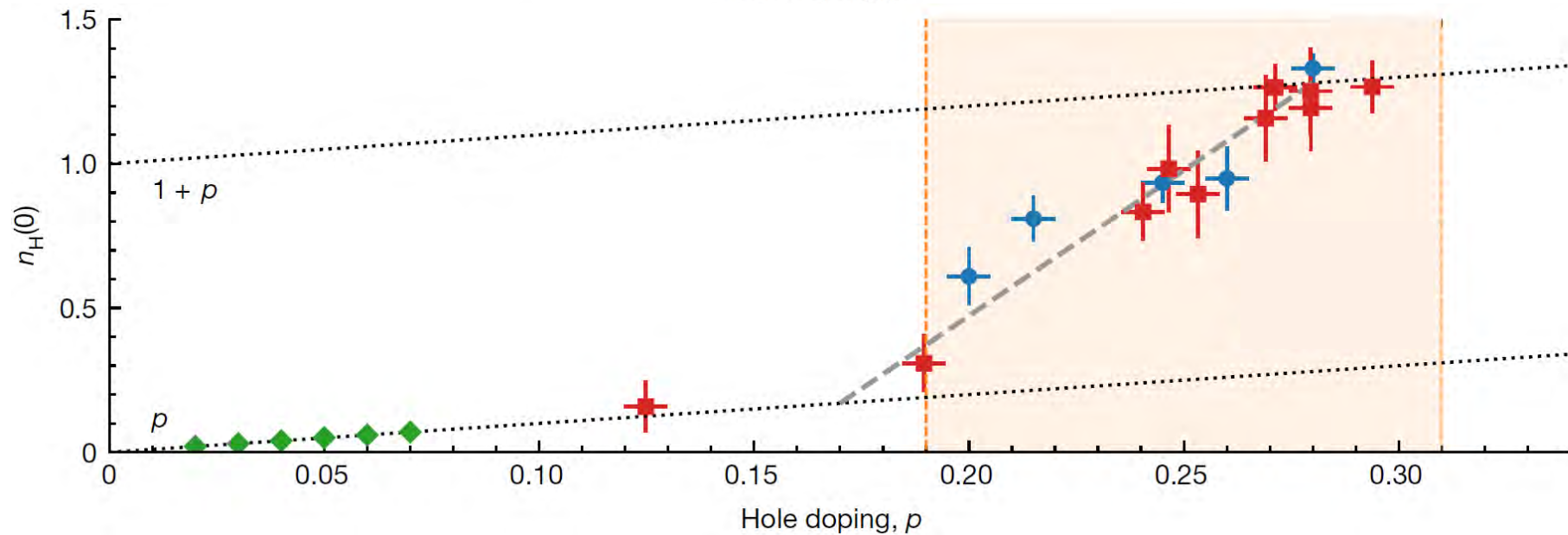
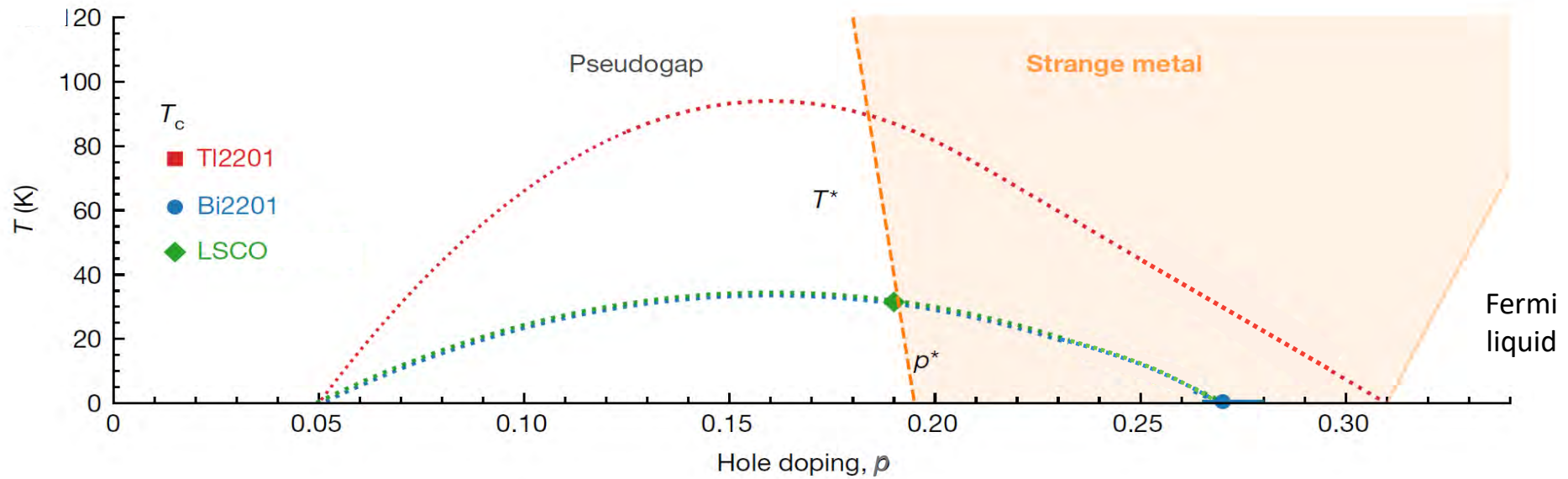
- In higher T_c TI2201 samples, drop in R_H with field also seen implying anisotropic scattering still responsible for H - and T -dependent $R_H(T)$. However, absolute value of $R_H(0)$ is now shifted up, suggesting loss of states *at all* T .

Putzke et al., Nat. Phys. 17, 826 (21)



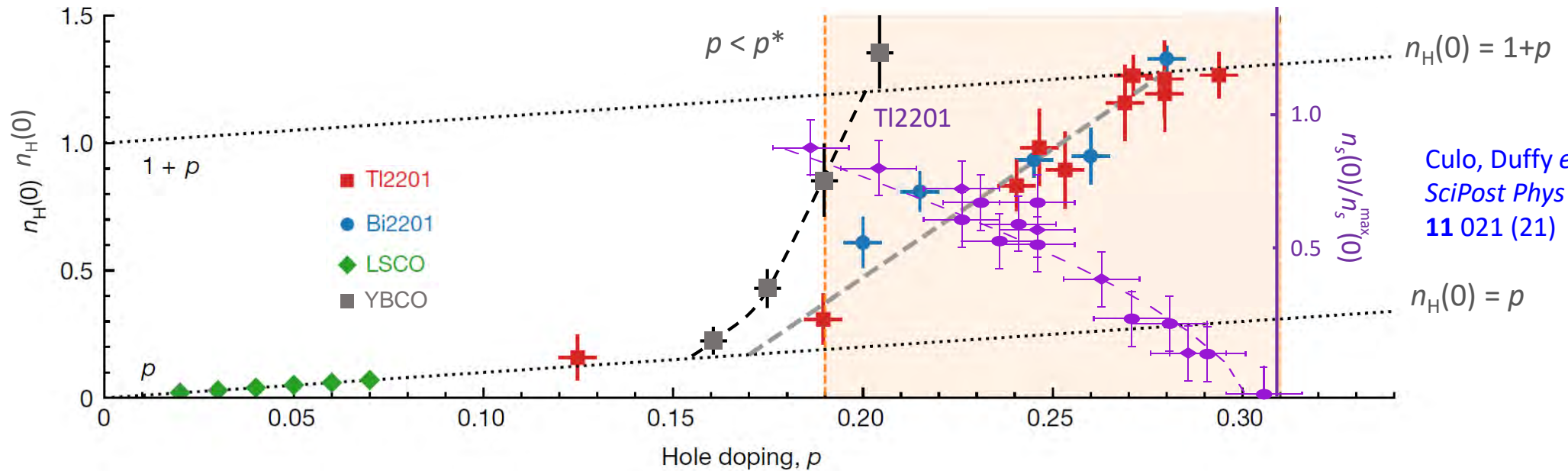
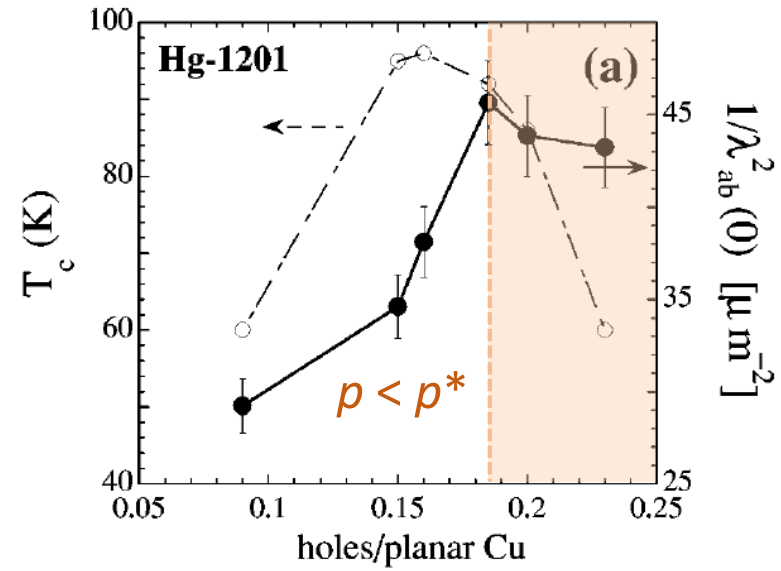
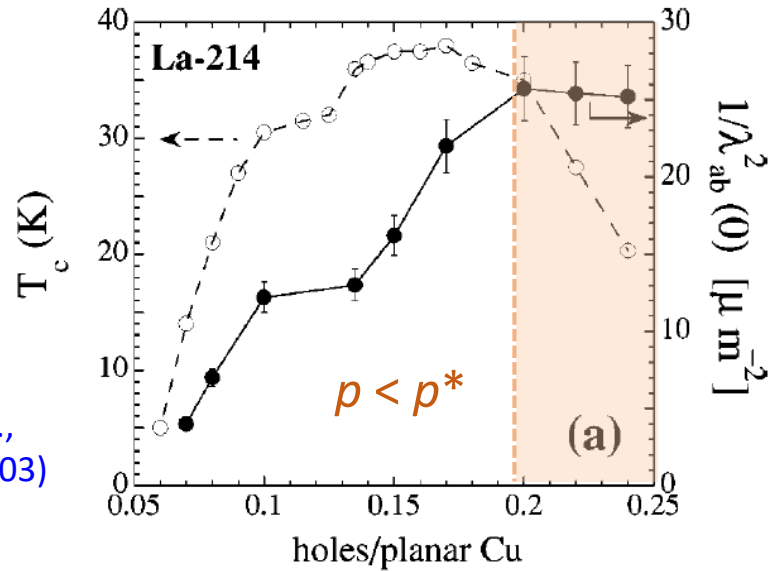
- With decreasing hole doping (increasing T_c), $R_H(H)$ does not asymptotically reach the value consistent with $n_H = 1 + p$

Superconductivity within SM regime



Superconductivity within SM regime

Panagopoulos *et al.*,
PRB 67 220502(R) (03)



Culo, Duffy *et al.*,
SciPost Phys
11 021 (21)

Summary

- New features in the transport properties of the strange metal of hole-doped cuprates
- (Anti)-correlation between the drop in $n_H(0)$ and the growth of the T -linear component of $\rho(T)$
- Low- T MR H -linear at high field and shows H/T scaling and signatures of incoherence
- Evidence for two-components in the conductivity – one Boltzmann-like, the other non-Boltzmann
- Pseudogap likely gaps out ‘Planckian’ carriers, leading to crossover to H/T^2 scaling in the MR
- HTS borne out of strange metal phase with dual character – but which one is responsible?