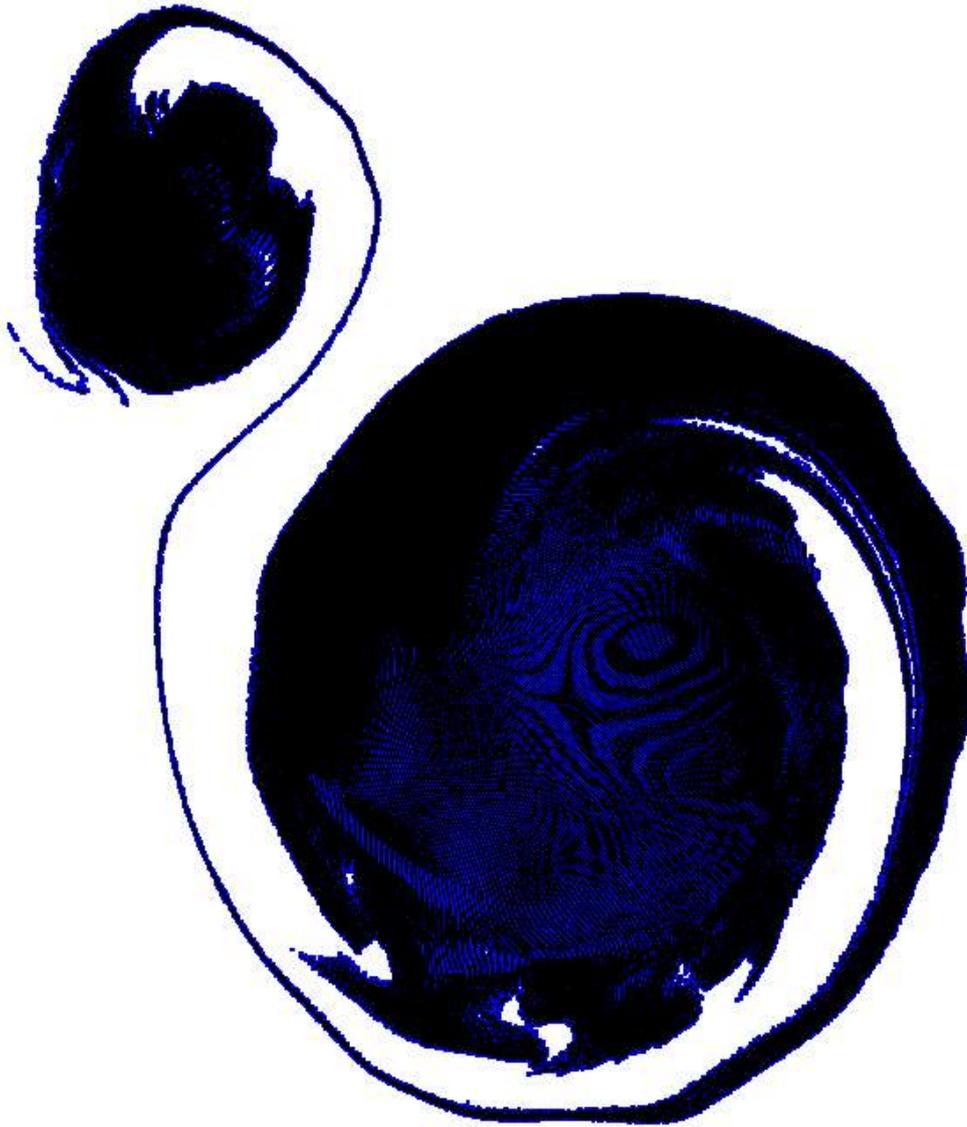


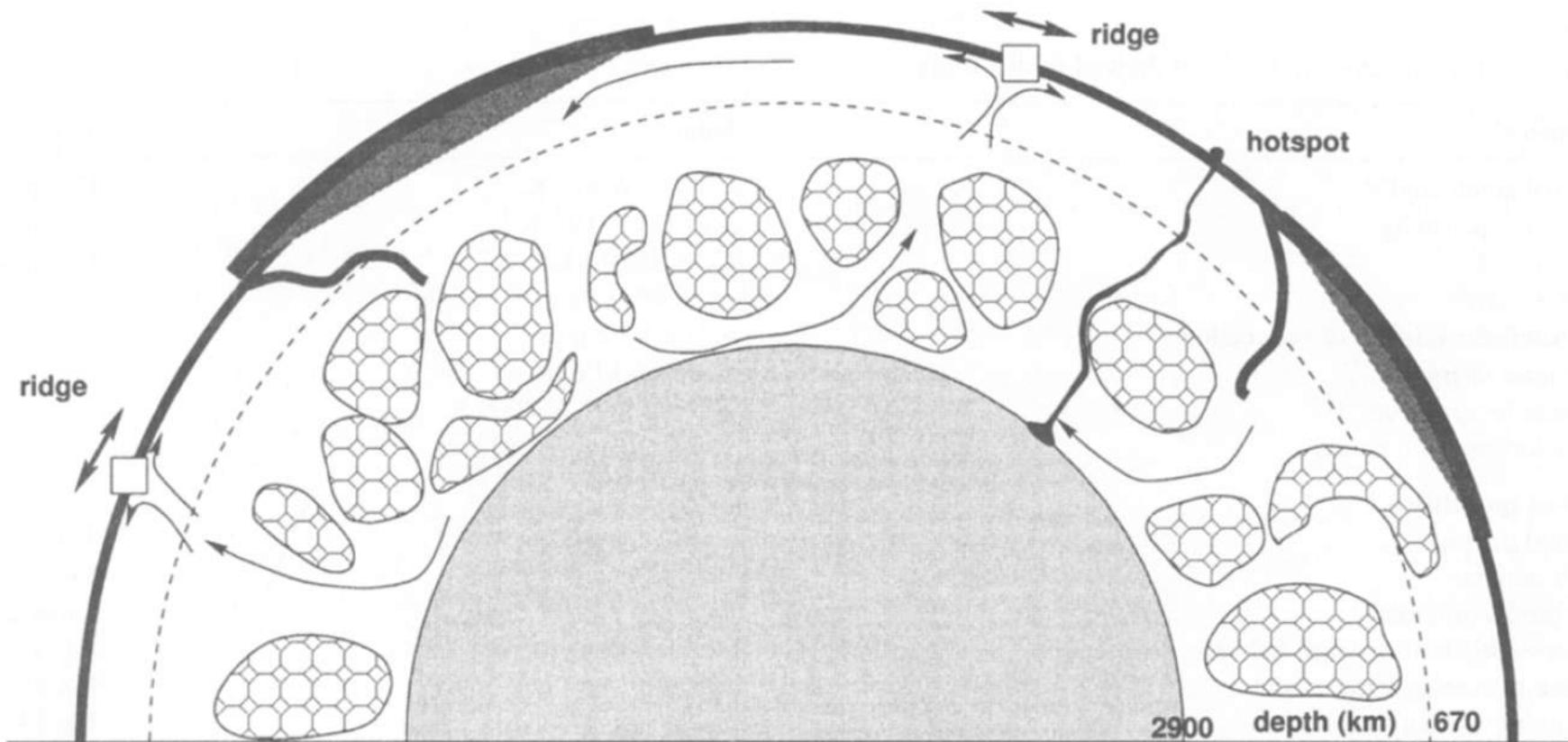
The flow of viscous heterogeneities in mantle plumes

Cinzia G. Farnetani

**IPGP et Université Diderot
Paris, France**



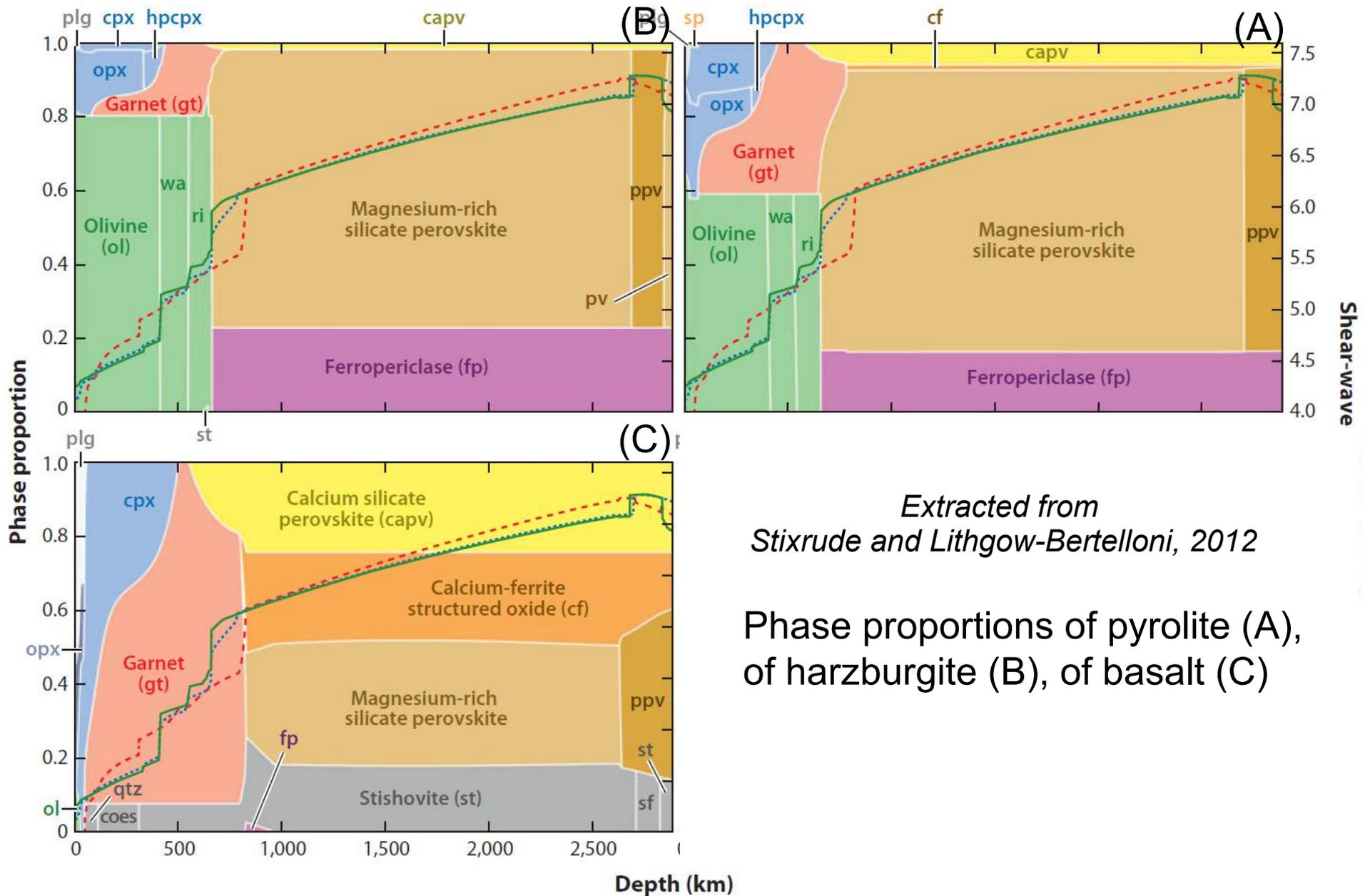
Viscous heterogeneities: Conceptual model by Becker et al., 1999



High-viscosity blobs could persist in the convective mantle for long time without substantial mixing and deformation.

Origin of viscous heterogeneities?

Grain size ($\eta \propto d^2$ for diffusion creep), water content, rock composition

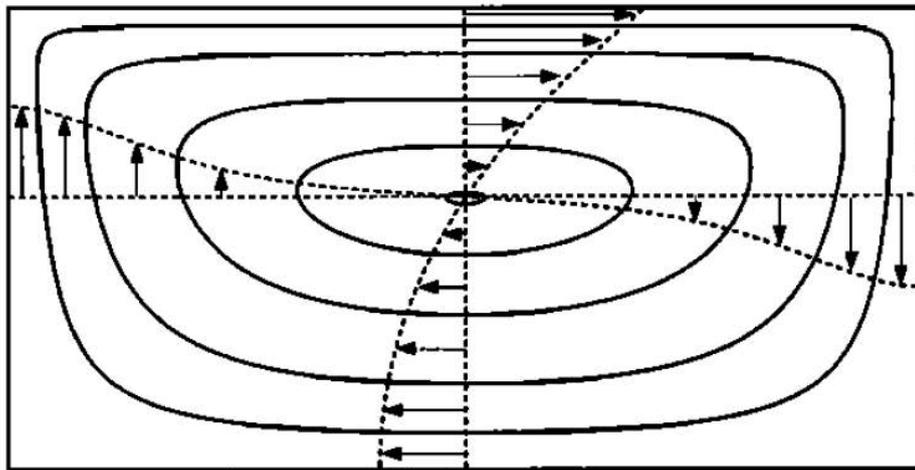
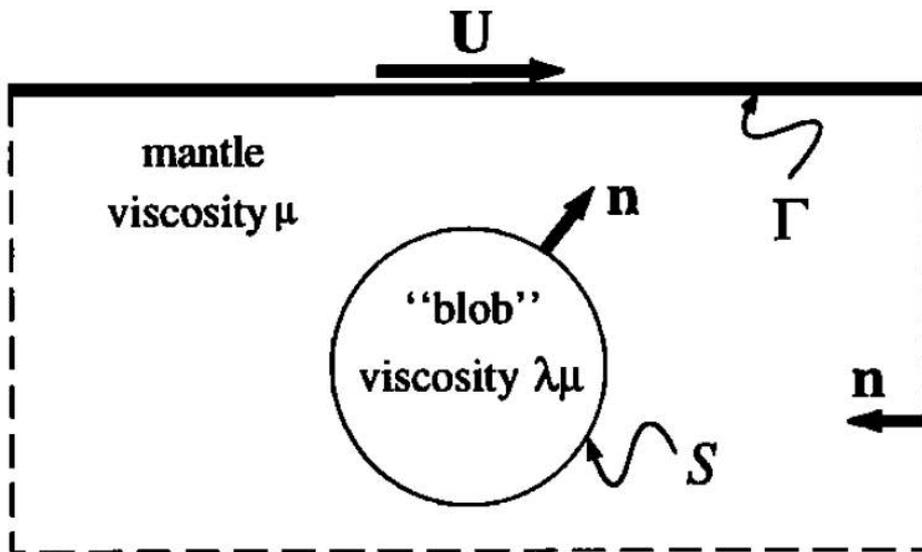


Extracted from
Stixrude and Lithgow-Bertelloni, 2012

Phase proportions of pyrolite (A),
of harzburgite (B), of basalt (C)

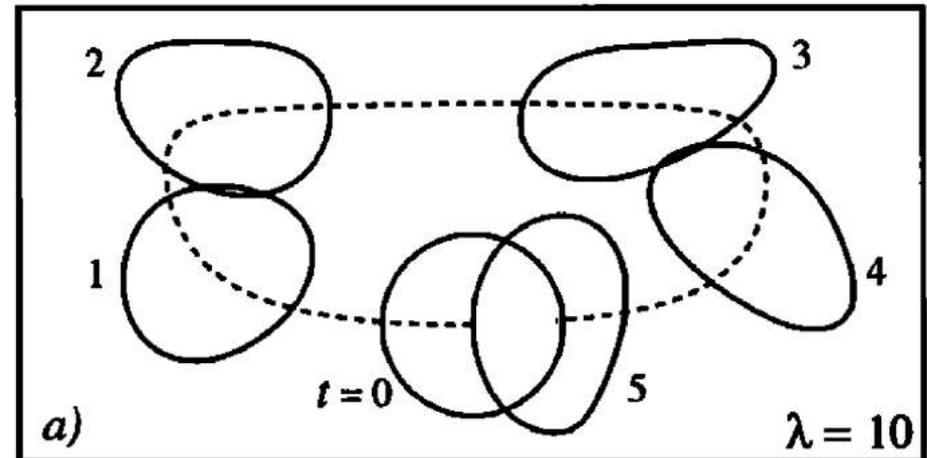
Viscous heterogeneities are modeled with a "fluid dynamics perspective",
rather than with a "mineral physics/compositional" perspective.

2D flow driven by surface motion



Manga, 1996

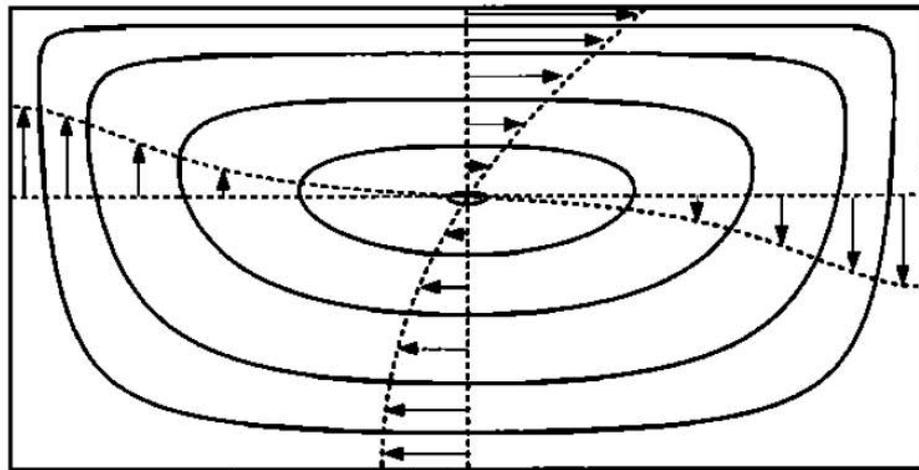
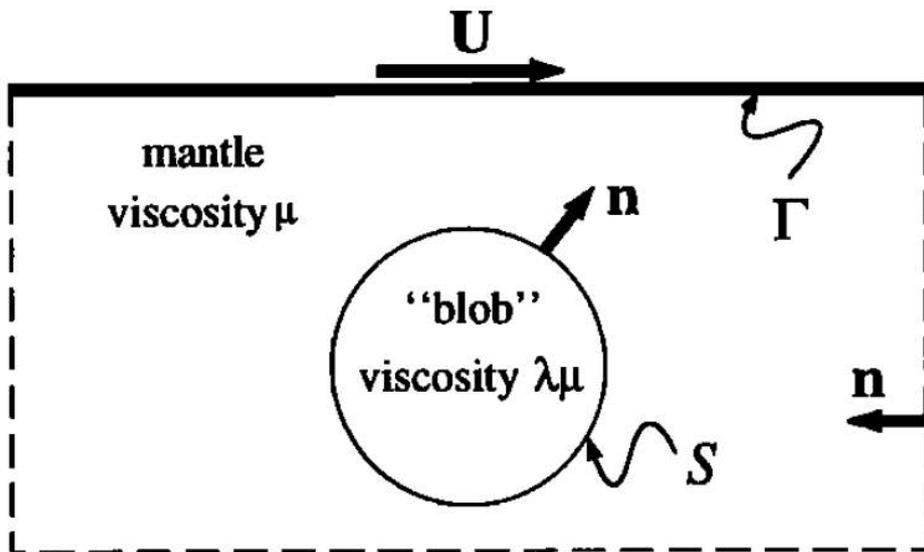
A viscous 'blob' ($\lambda=10$) experiences little deformation



Viscosity ratio

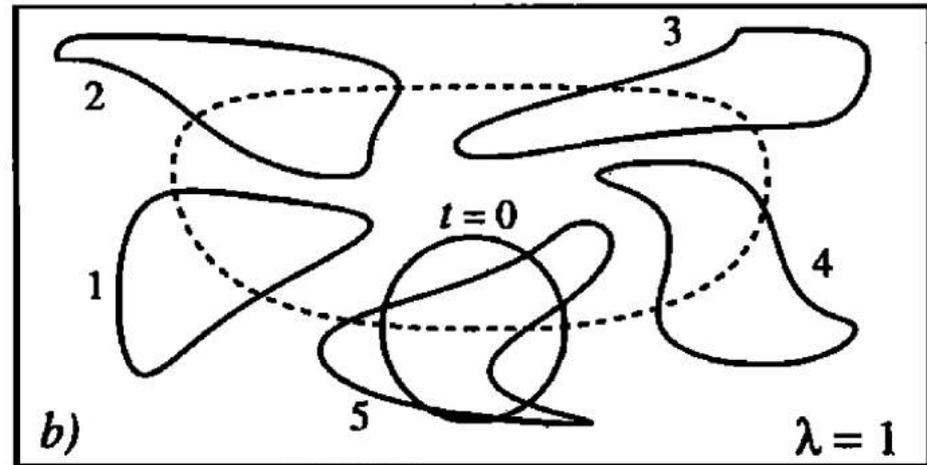
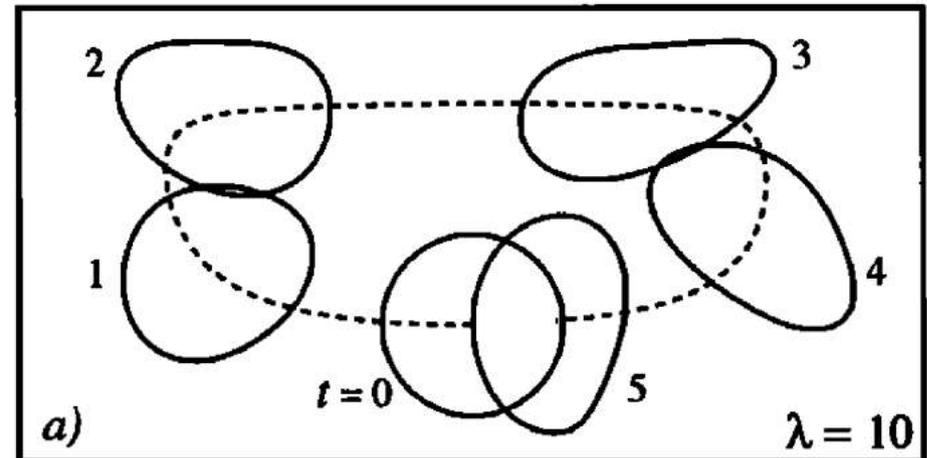
$$\lambda = \eta_{\text{heterogeneity}} / \eta_{\text{surrounding fluid}}$$

2D flow driven by surface motion



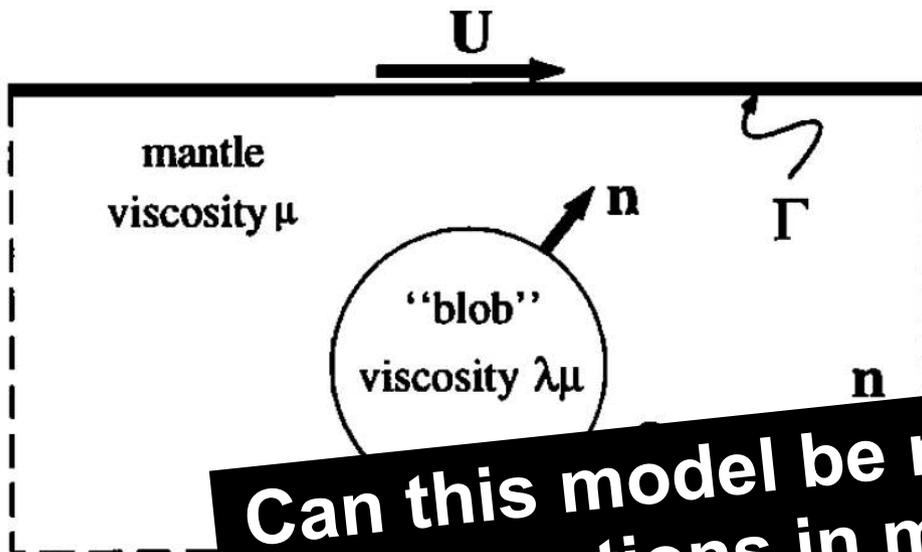
Manga, 1996

A viscous 'blob' ($\lambda=10$) experiences little deformation

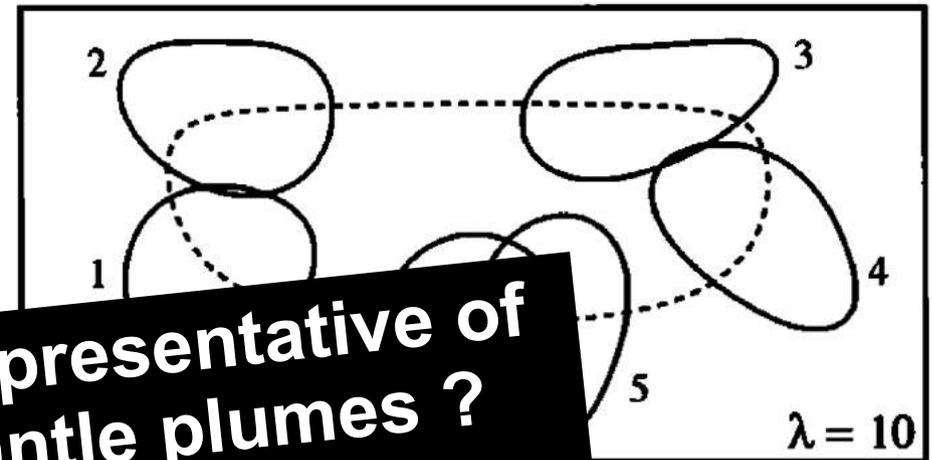


...but also for $\lambda=1$ the deformation is quite modest.

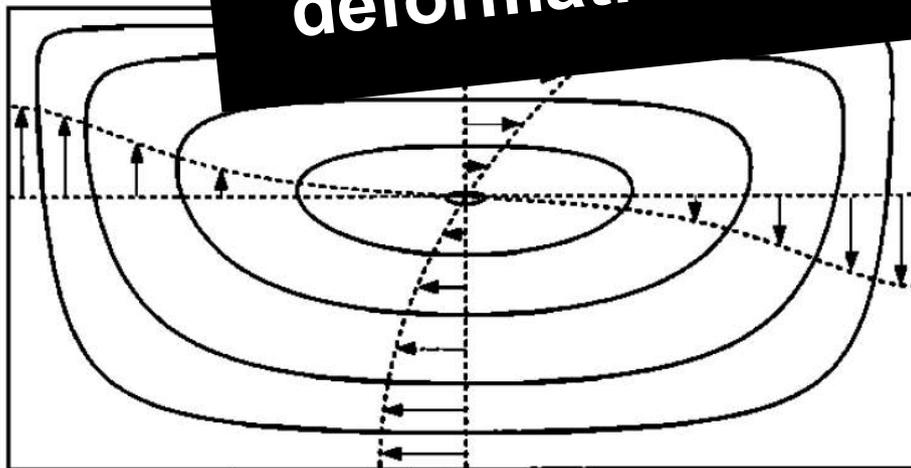
2D flow driven by surface motion



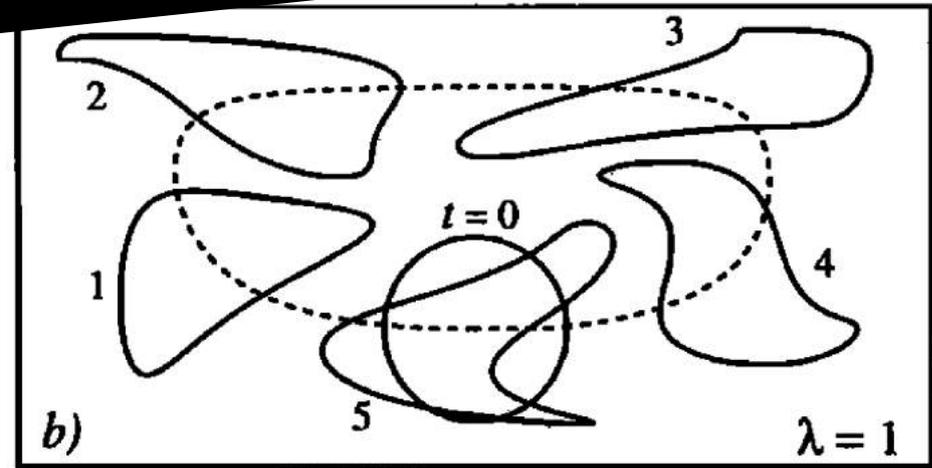
A viscous 'blob' ($\lambda=10$) experiences little deformation



Can this model be representative of deformations in mantle plumes?



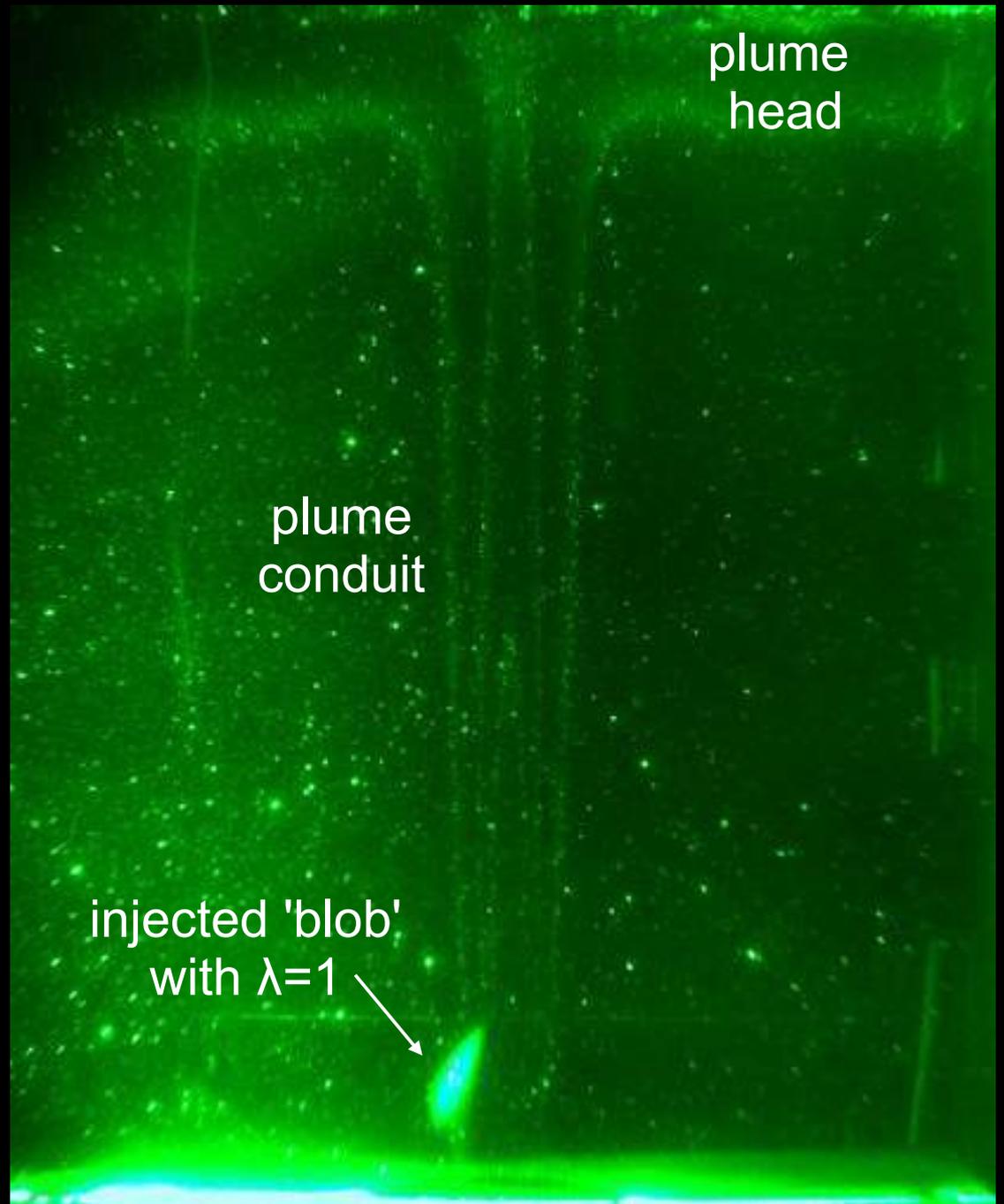
Manga, 1996



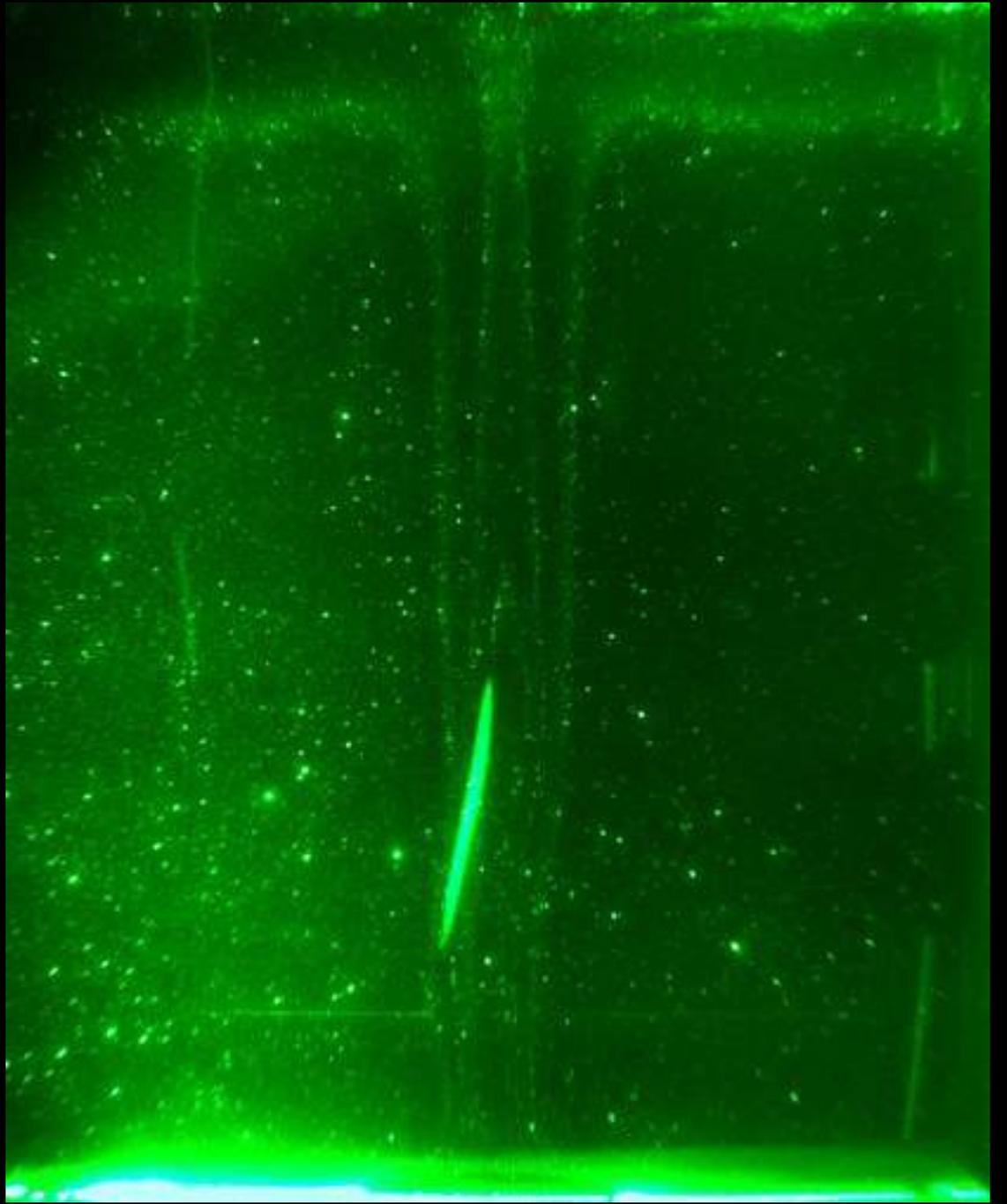
...but also for $\lambda=1$ the deformation is quite modest.

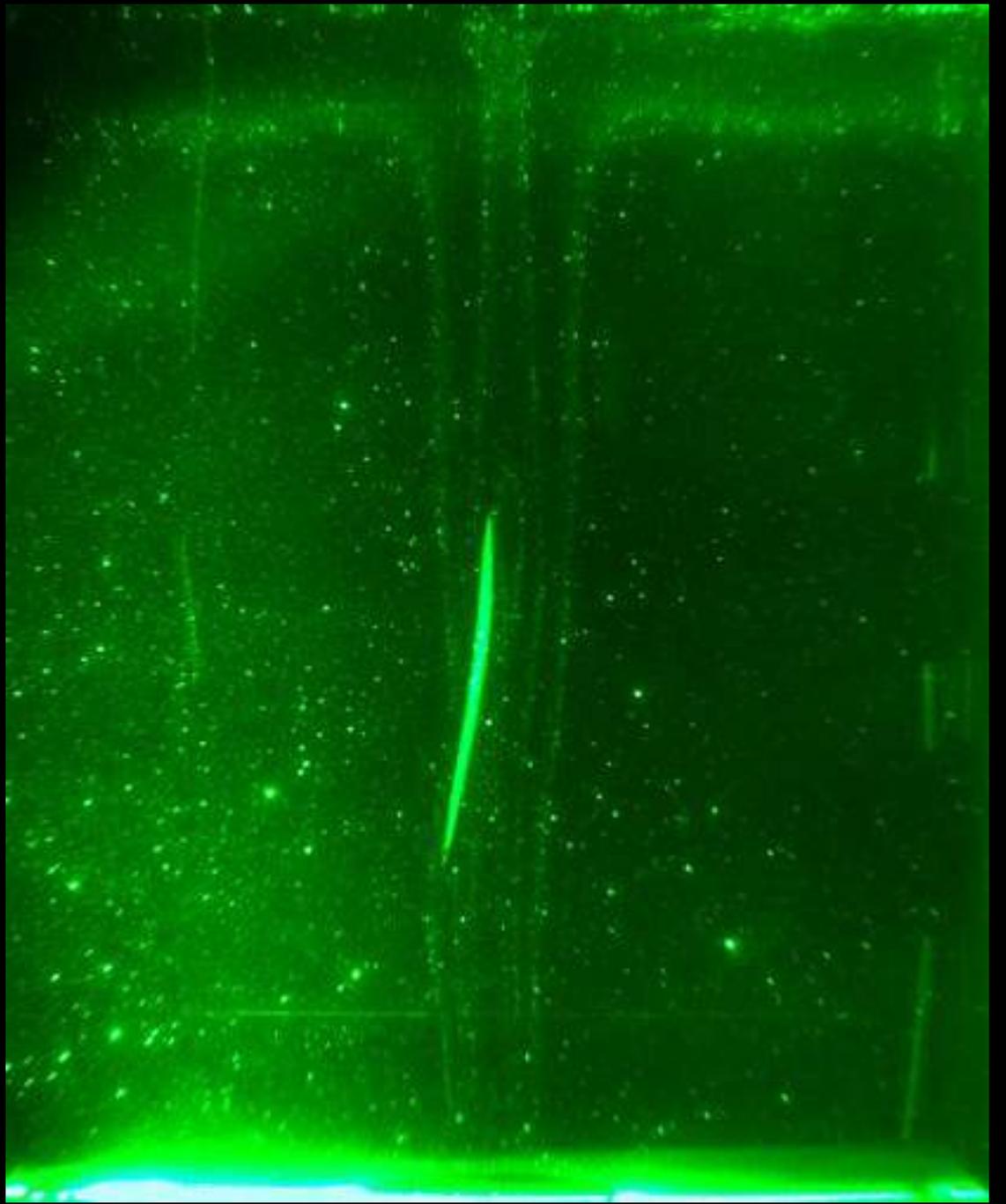
**In a plume conduit
for $\lambda = 1$
we obtain filaments**

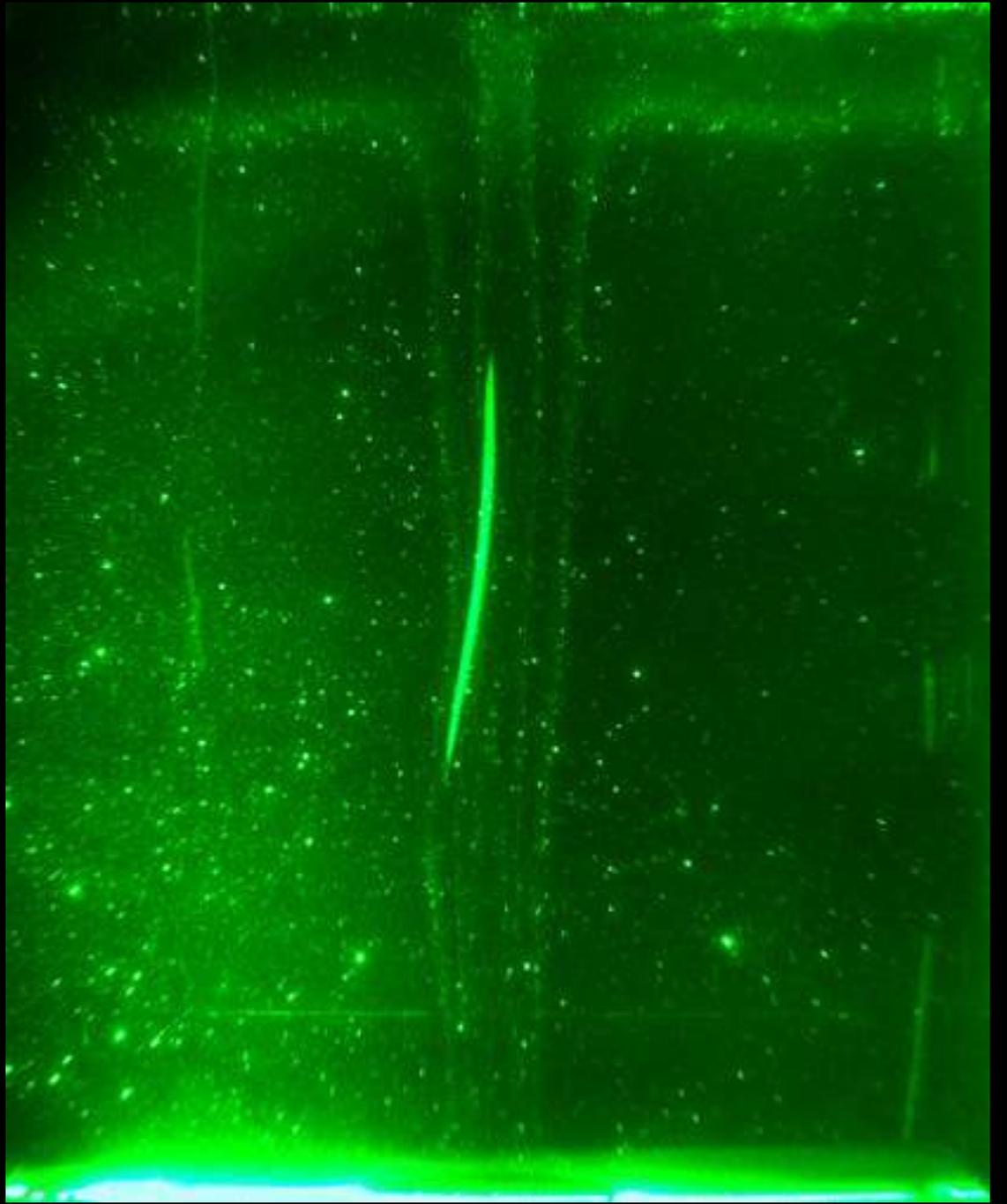
[Farnetani and Hofmann, 2009]

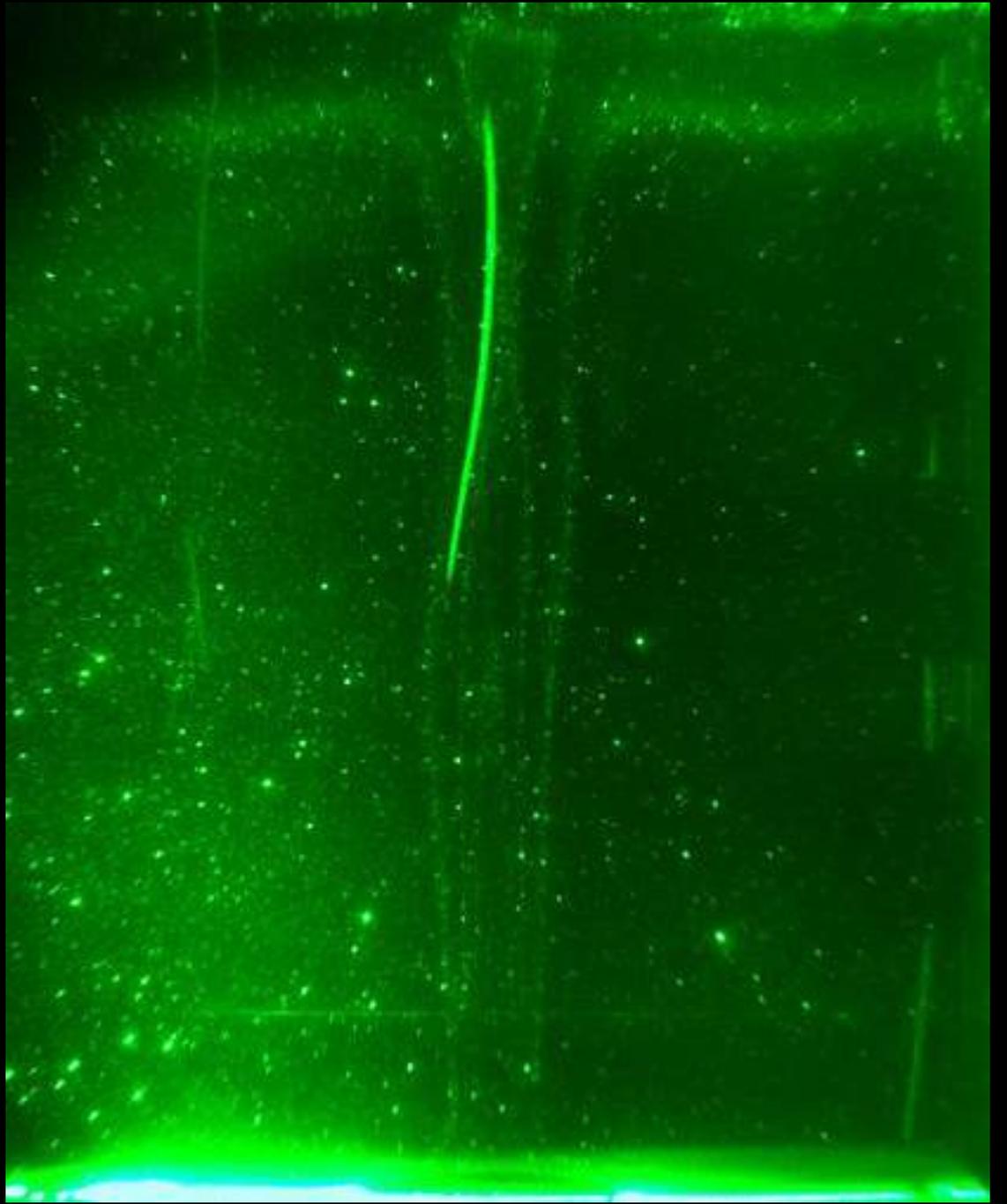


Experiments by A. Limare

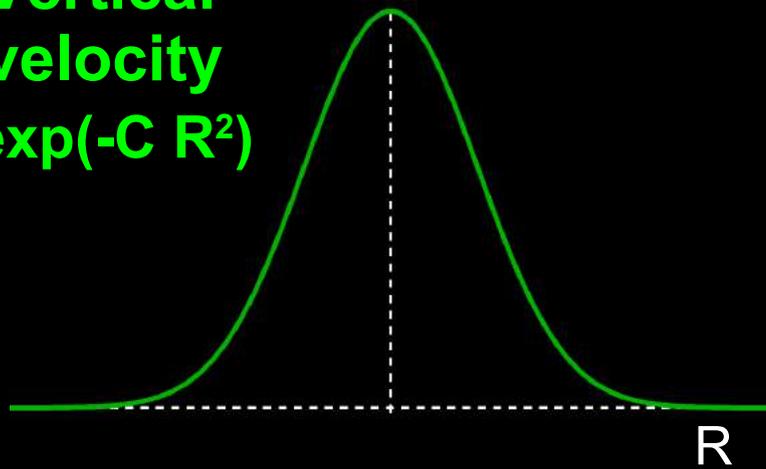




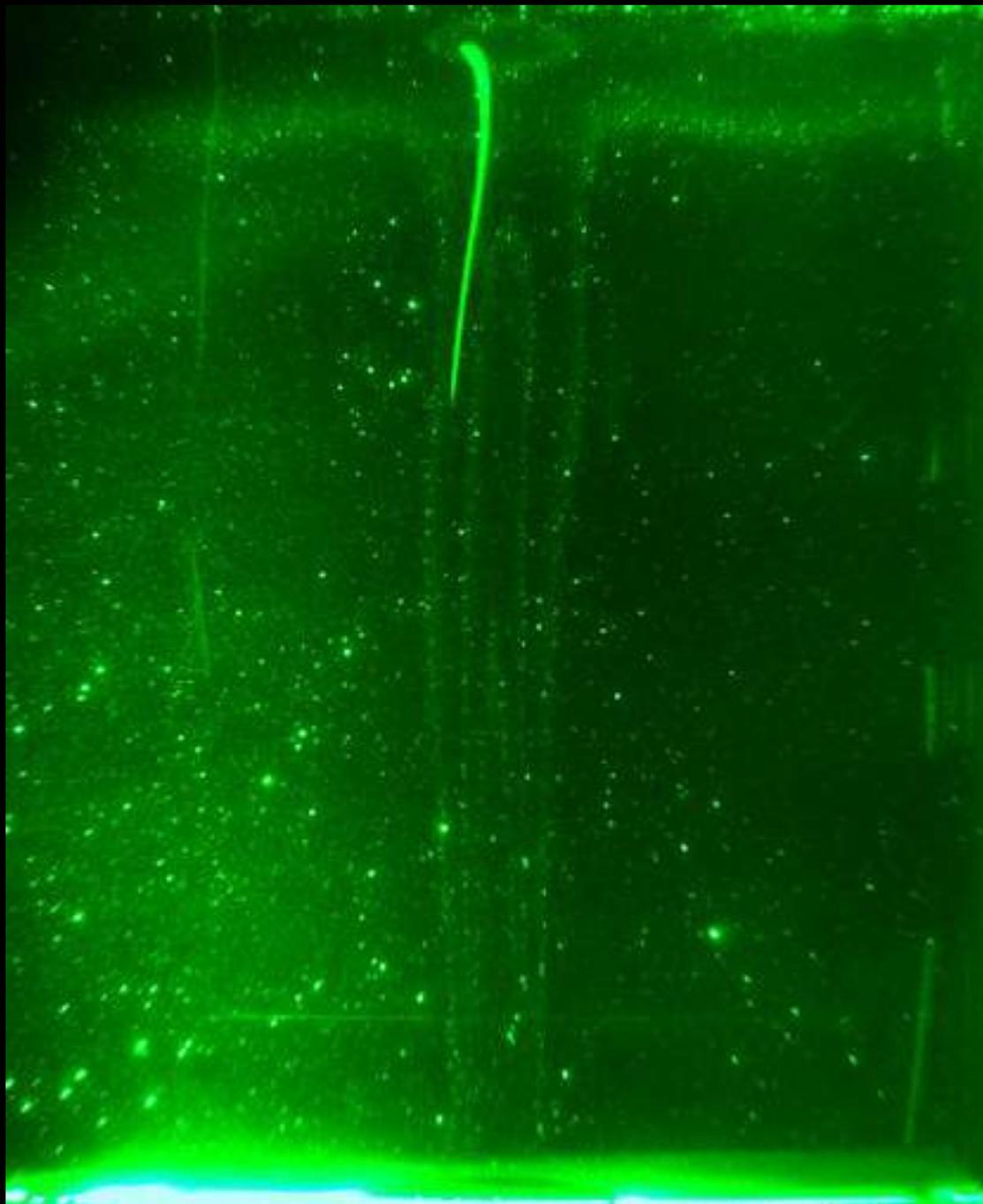
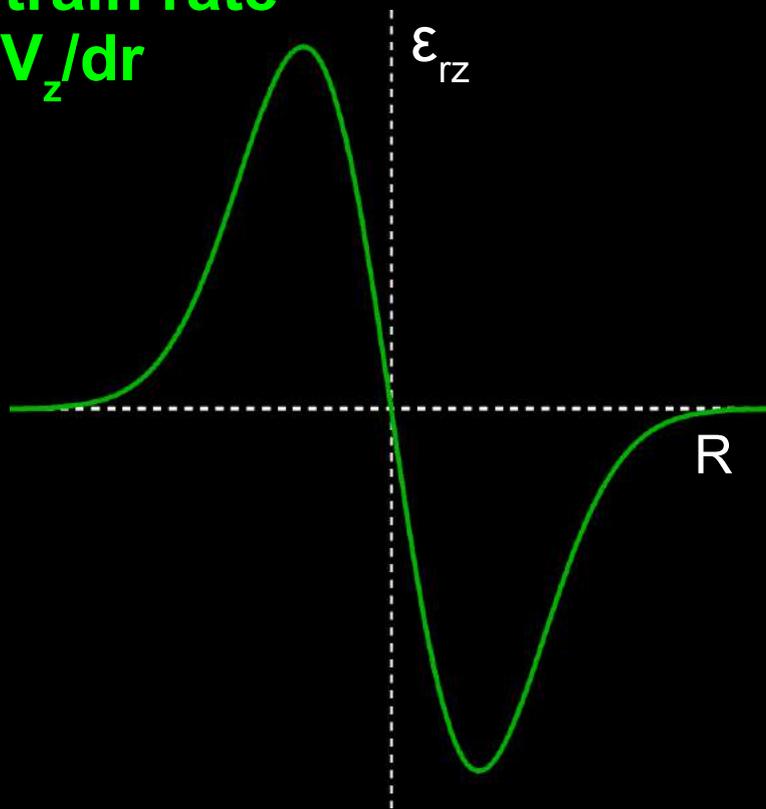




Vertical
velocity
 $\exp(-C R^2)$



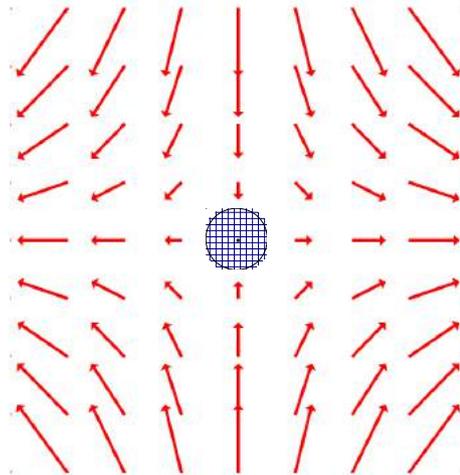
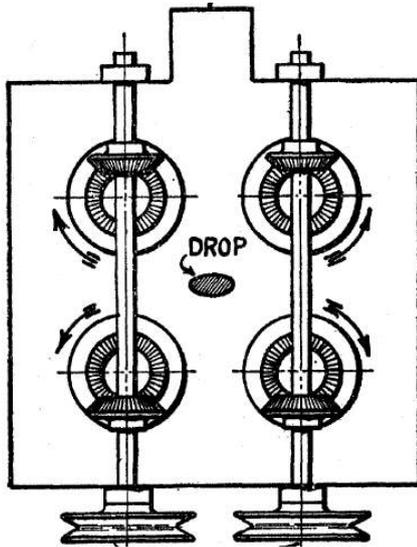
Strain rate
 dV_z/dr



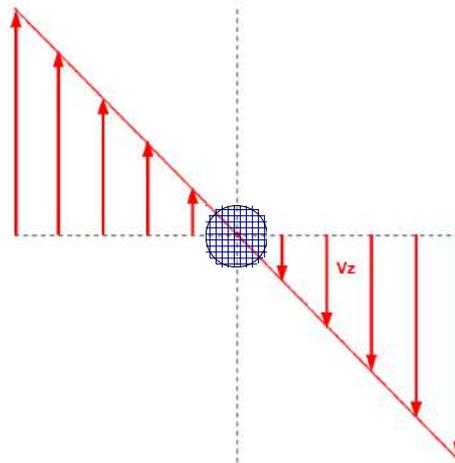
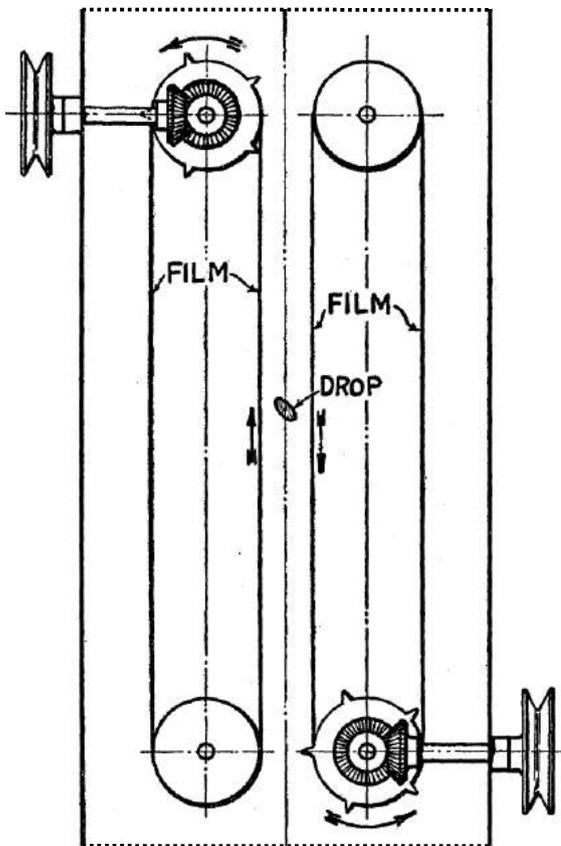
Interesting aspects of the flow within a mantle plume

- § The flow is often characterized by high strain rates (10^{-13} - 10^{-14} s⁻¹) and high deformations
- § The deformation history is complex, two types of flow coexist
 - Pure shear dominates in the basal part of the plume
 - Simple shear dominates in the plume conduit.
- § The "plume flow" rules out commonly used assumptions:
"Low deformations, Low and linearly varying strain rates, The same type of flow over time....."

Laboratory experiments by Taylor, 1934



Pure shear flow
a viscous drop $\lambda=20$
gets highly deformed



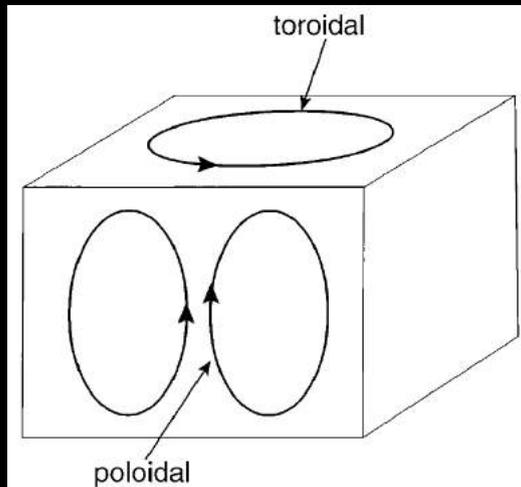
Simple shear flow
a viscous drop $\lambda=20$
merely rotates, with
minor deformations

Constant strain rate
throughout the fluid

Key questions about viscous heterogeneities in plumes

§ How is a viscous heterogeneity deformed by the plume flow ?

§ How is the plume flow perturbed by a viscous heterogeneity ?



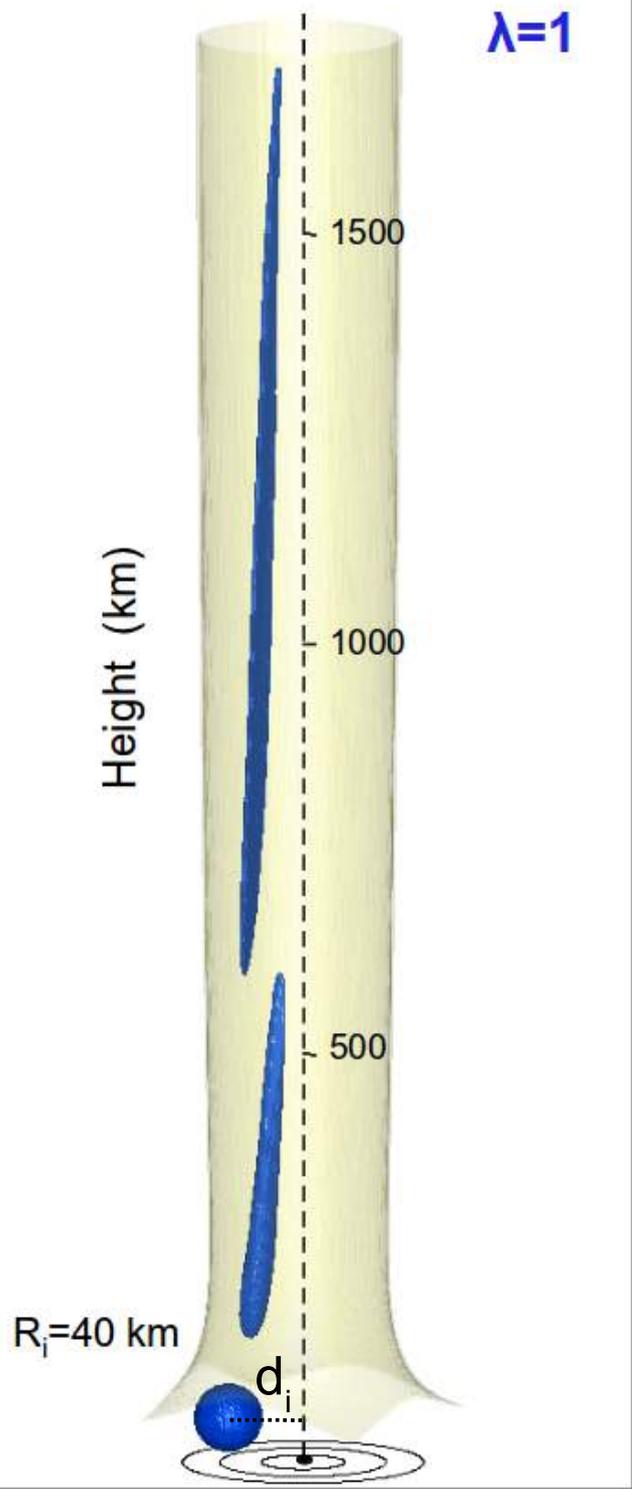
Lateral viscosity variations can induce a toroidal component within a poloidal, buoyancy driven flow

*[Ferrachat and Ricard 1998]
[Bercovici et al., 2000]*

§ If the plume carries viscous heterogeneities, can a toroidal flow component appear ?

§ In such a case, are radial mixing and/or azimuthal mixing enhanced ?

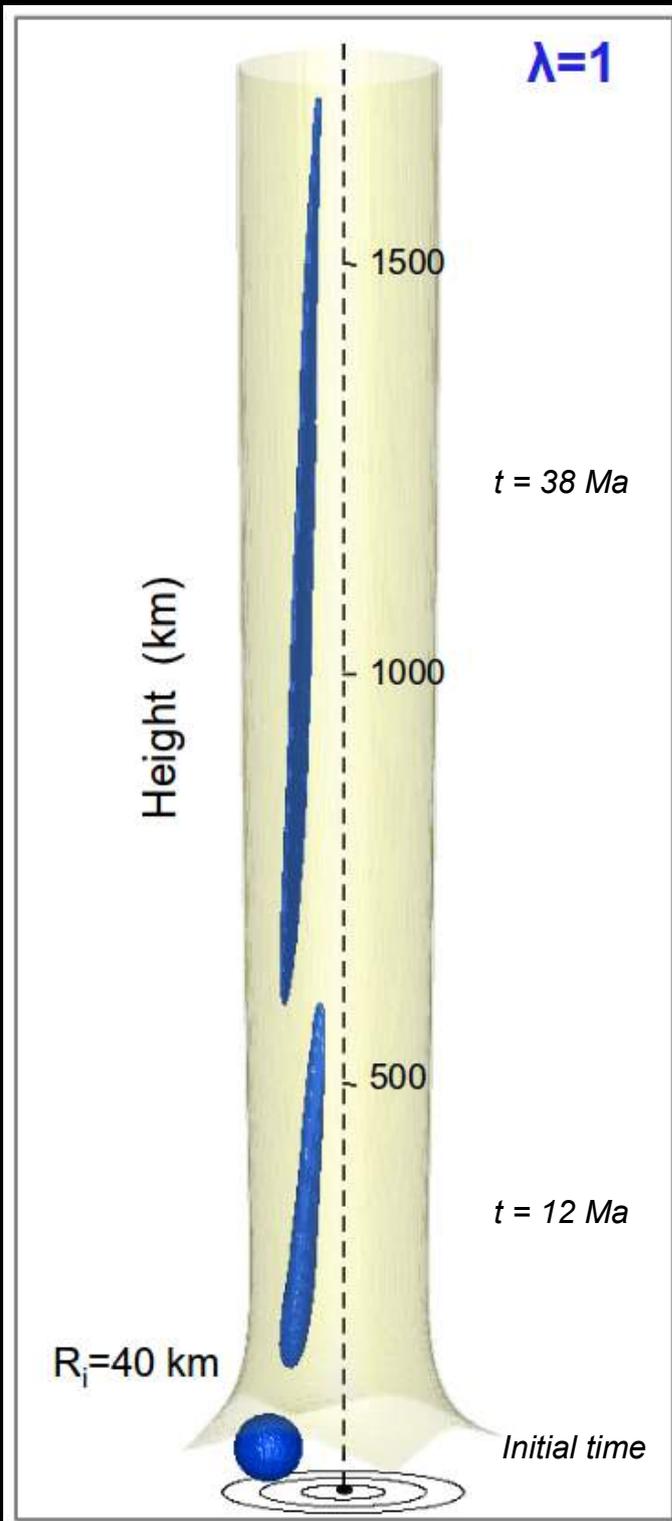
[Blichert-Toft and Albarède, 2009]



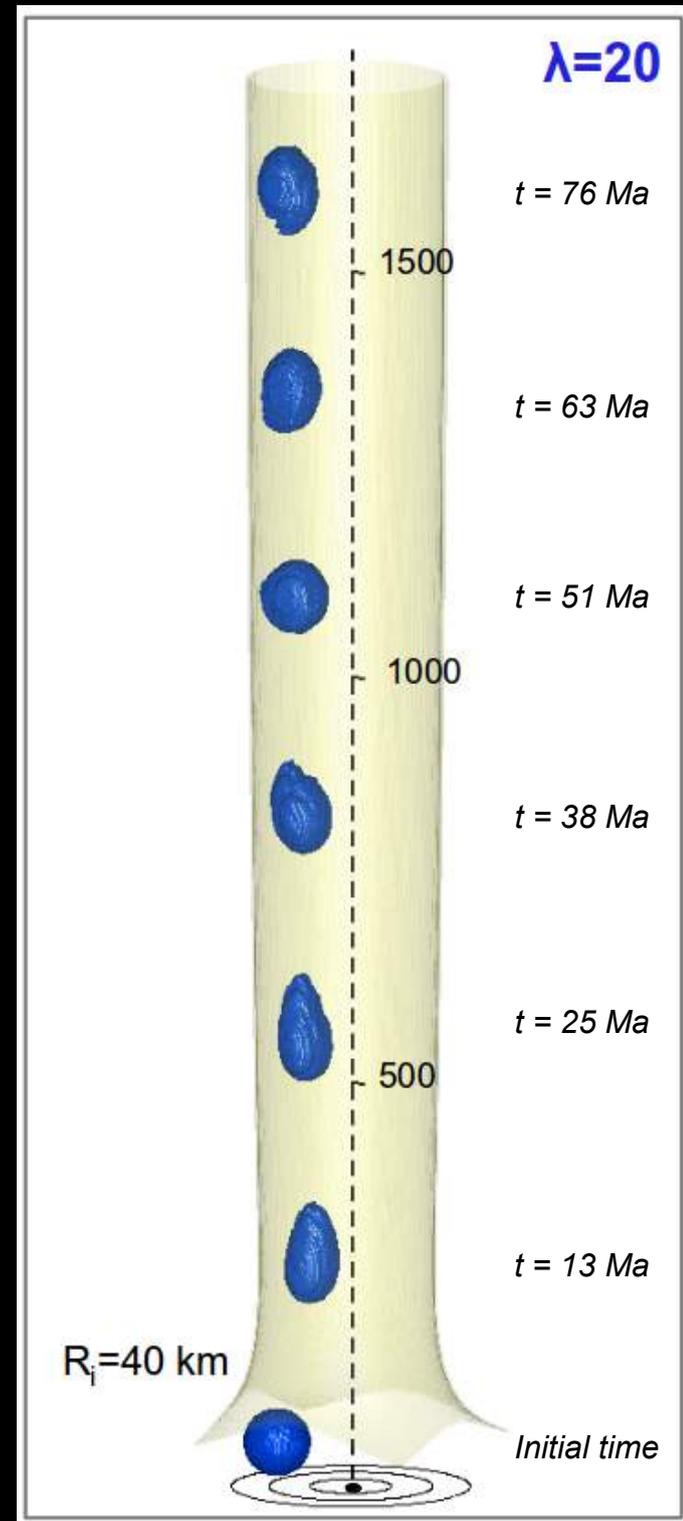
3D simulations of a mantle plume
with temperature dependent viscosity

Code Stag3D by *Paul Tackley*

Millions of active tracers model a single
more viscous ($1 < \lambda < 20$) heterogeneity
with an initial spherical shape of variable
radius ($30 < R_i < 50$ km), at initial axial
distance $d_i = 100$ km

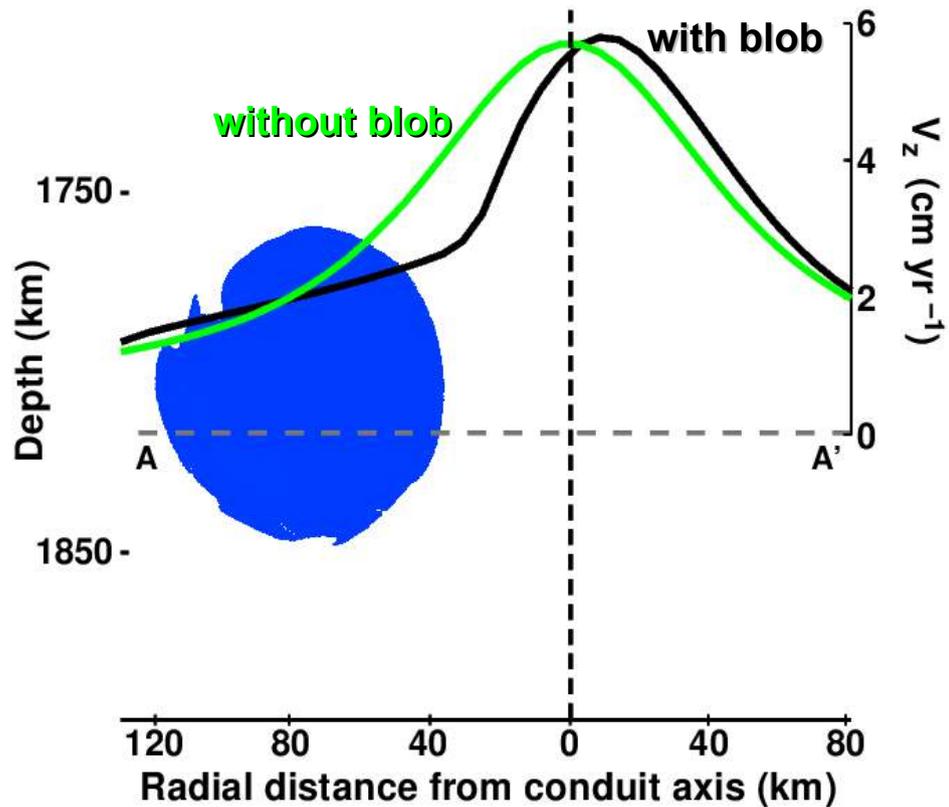


For $\lambda = 20$ $R_i = 40$ km
the heterogeneity
undergoes a modest
deformation

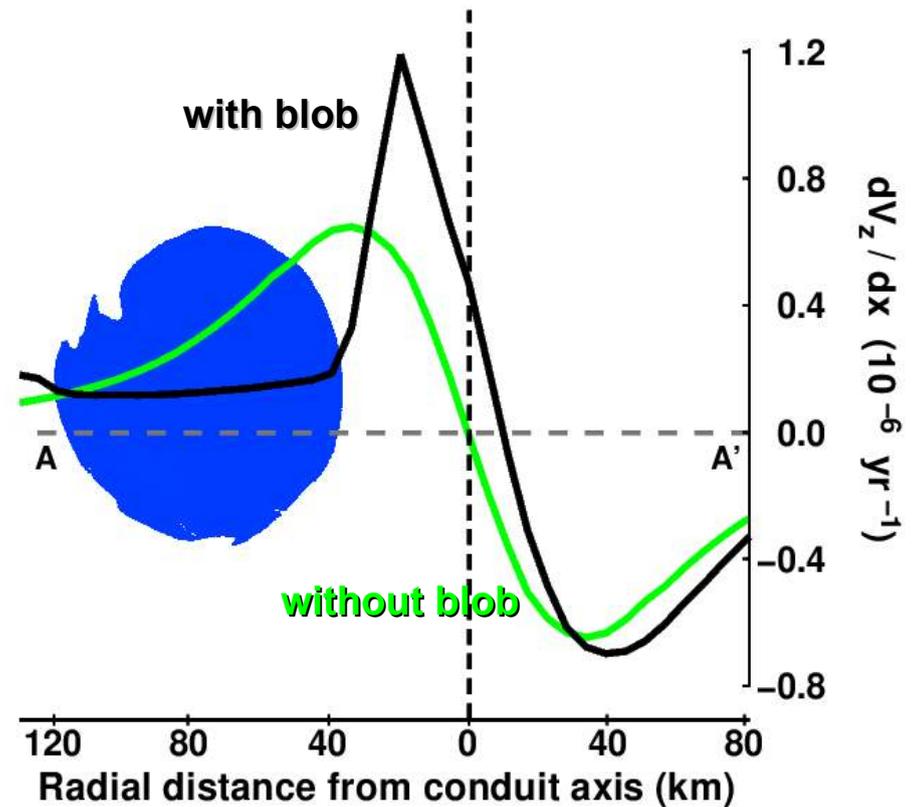


Viscous blob $\lambda = 20$

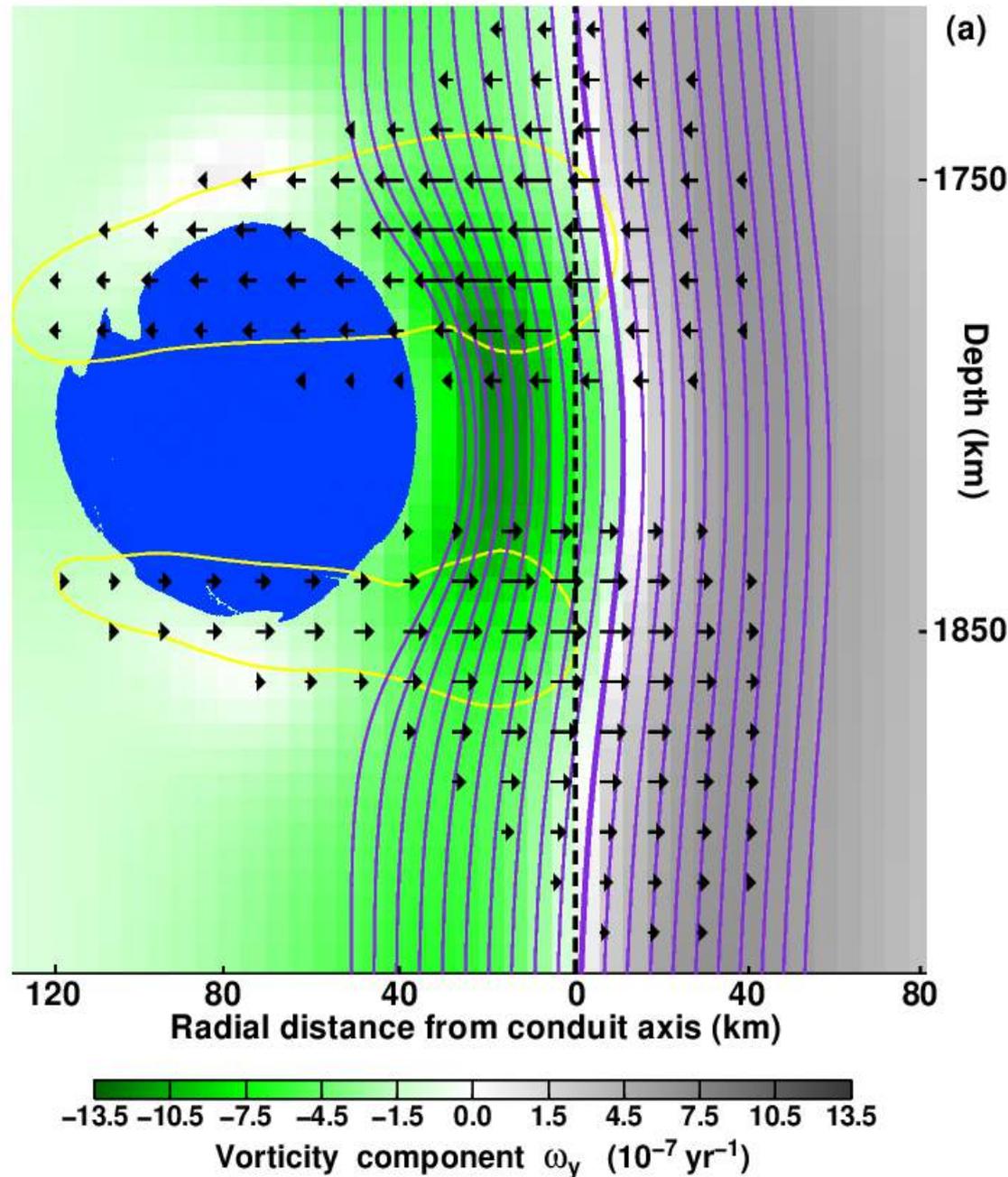
Vertical velocity profile



Strain rate profile



Vertical cross section



Horizontal velocity v_x (black)

Contour $v_x \geq 0.1 v_z$ (yellow)

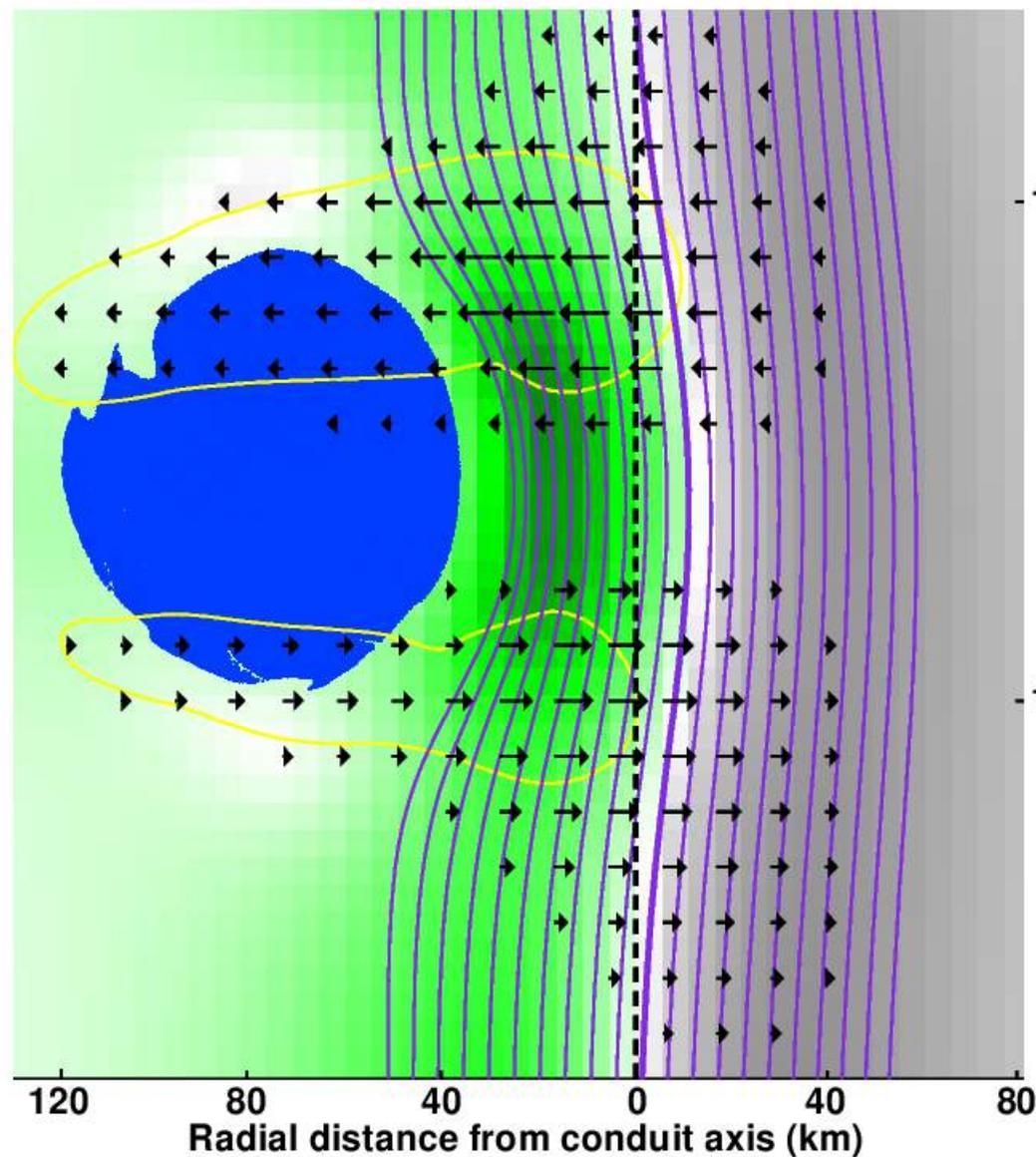
Vorticity component (shades)

$$\omega_y = \left(\frac{\partial v_x}{\partial z} - \frac{\partial v_z}{\partial x} \right)$$

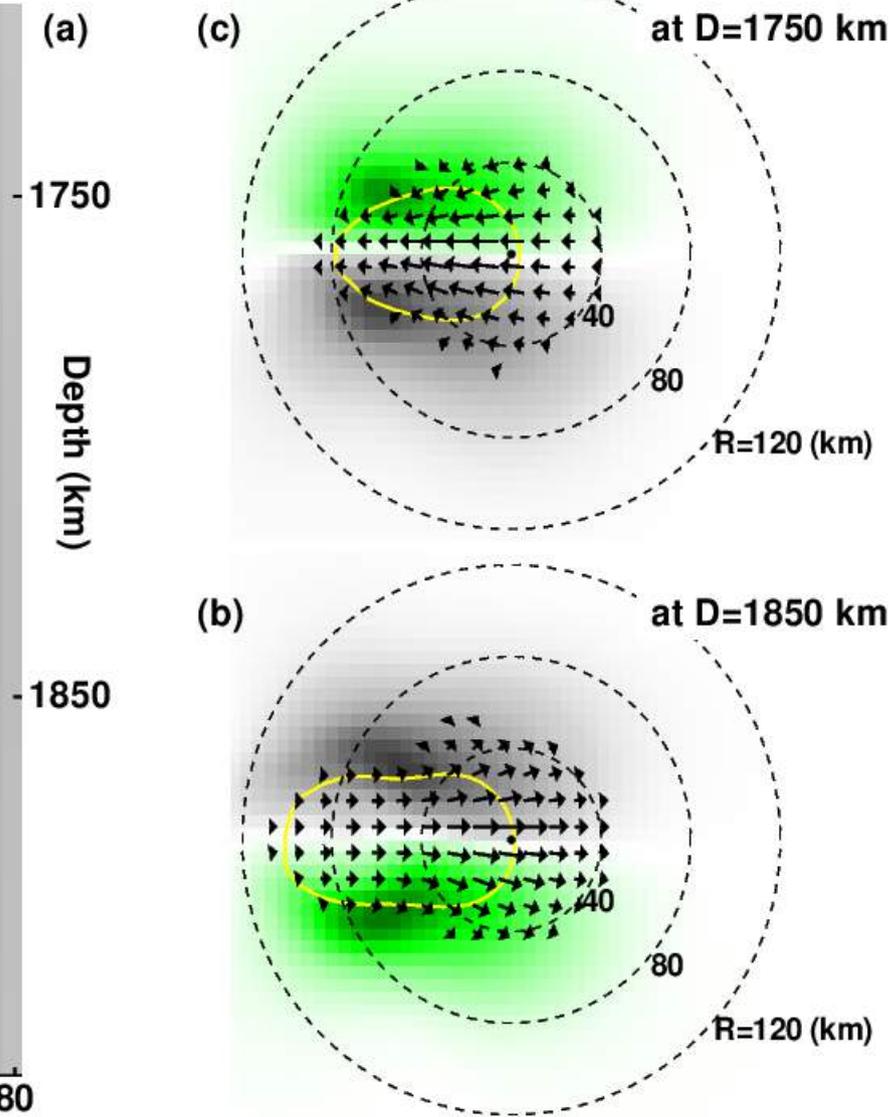
$$\omega_z = \left(\frac{\partial v_y}{\partial x} - \frac{\partial v_x}{\partial y} \right)$$

Flow trajectories (violet) are deviated and locally cross the plume axis (dashed line)

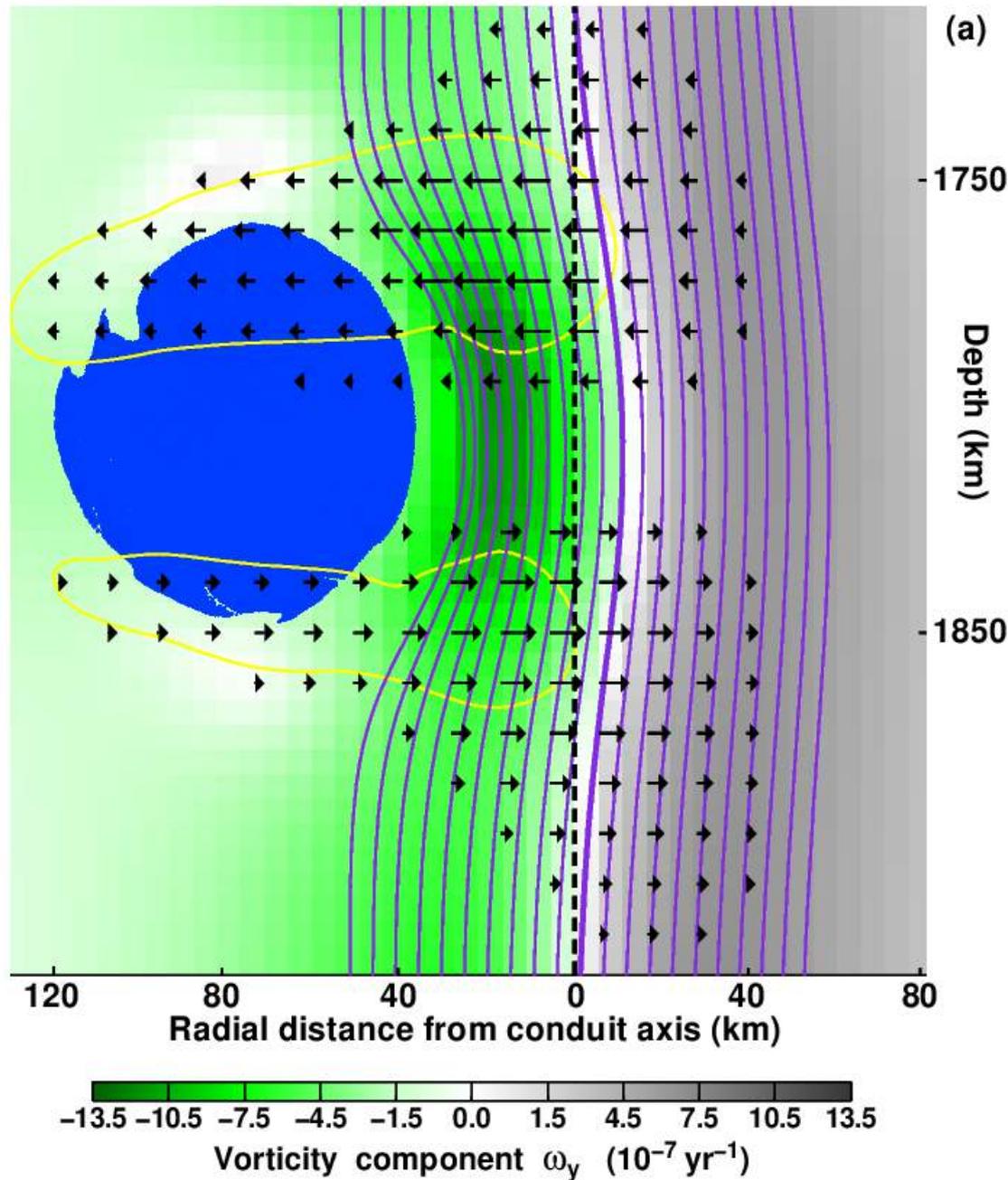
Vertical cross section



Horizontal cross sections

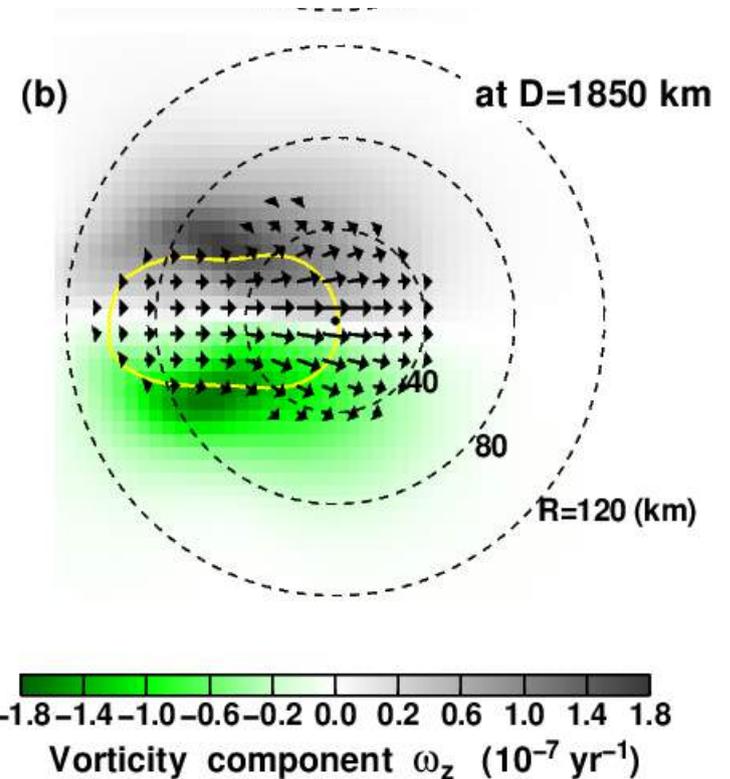


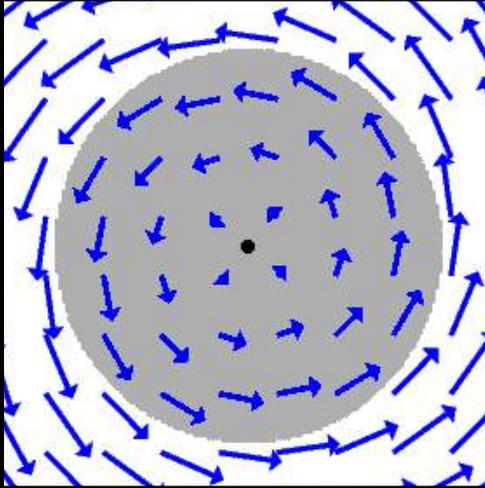
Vertical cross section



The flow is perturbed over a vertical distance 3 times the blob diameter.

The perturbation has a local character, without permanent inter-conduit mixing

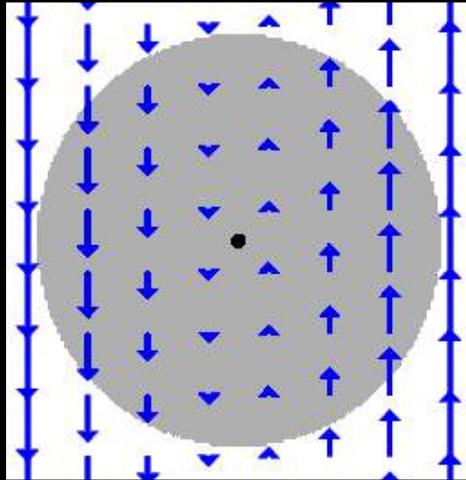




Solid-body rotation

$$V_x = -Cz, \quad V_z = Cx$$

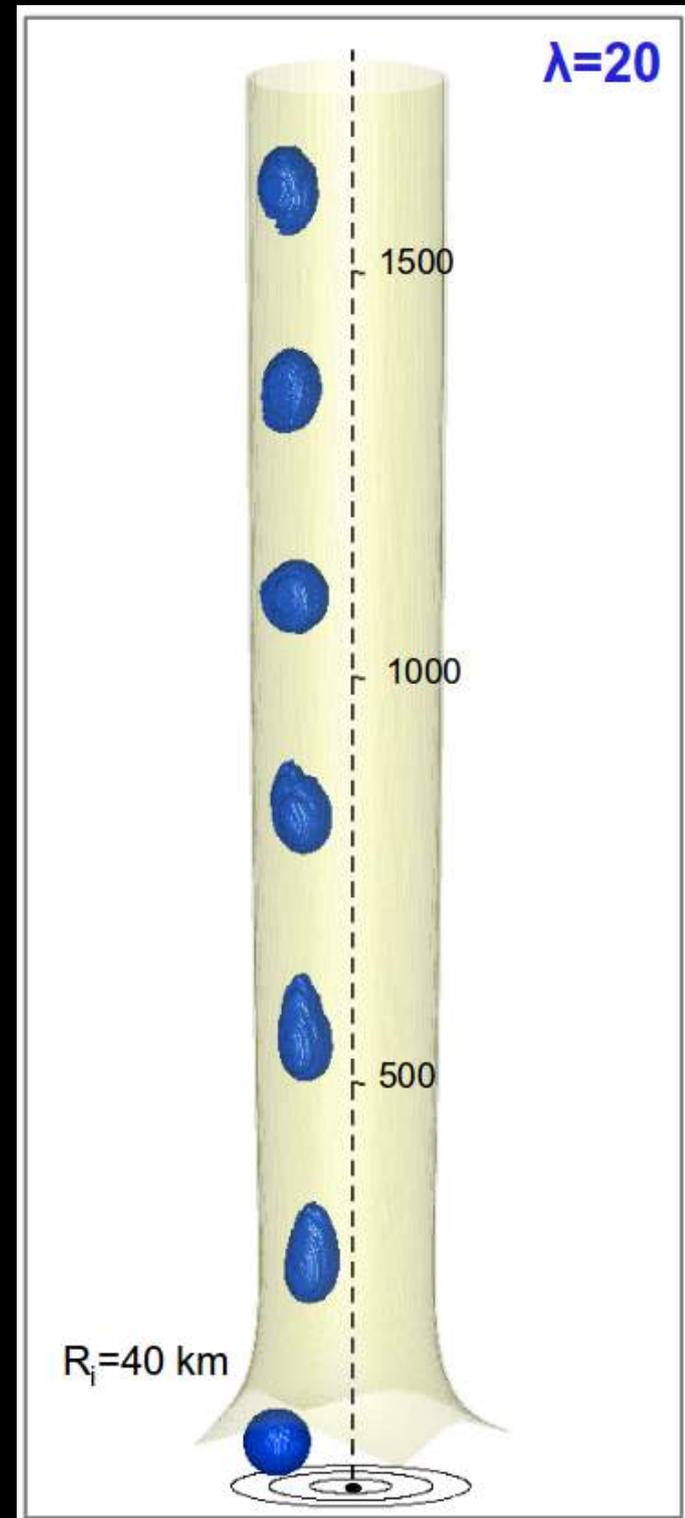
$$\omega_y = -2C, \quad \varepsilon_{xz} = 0$$

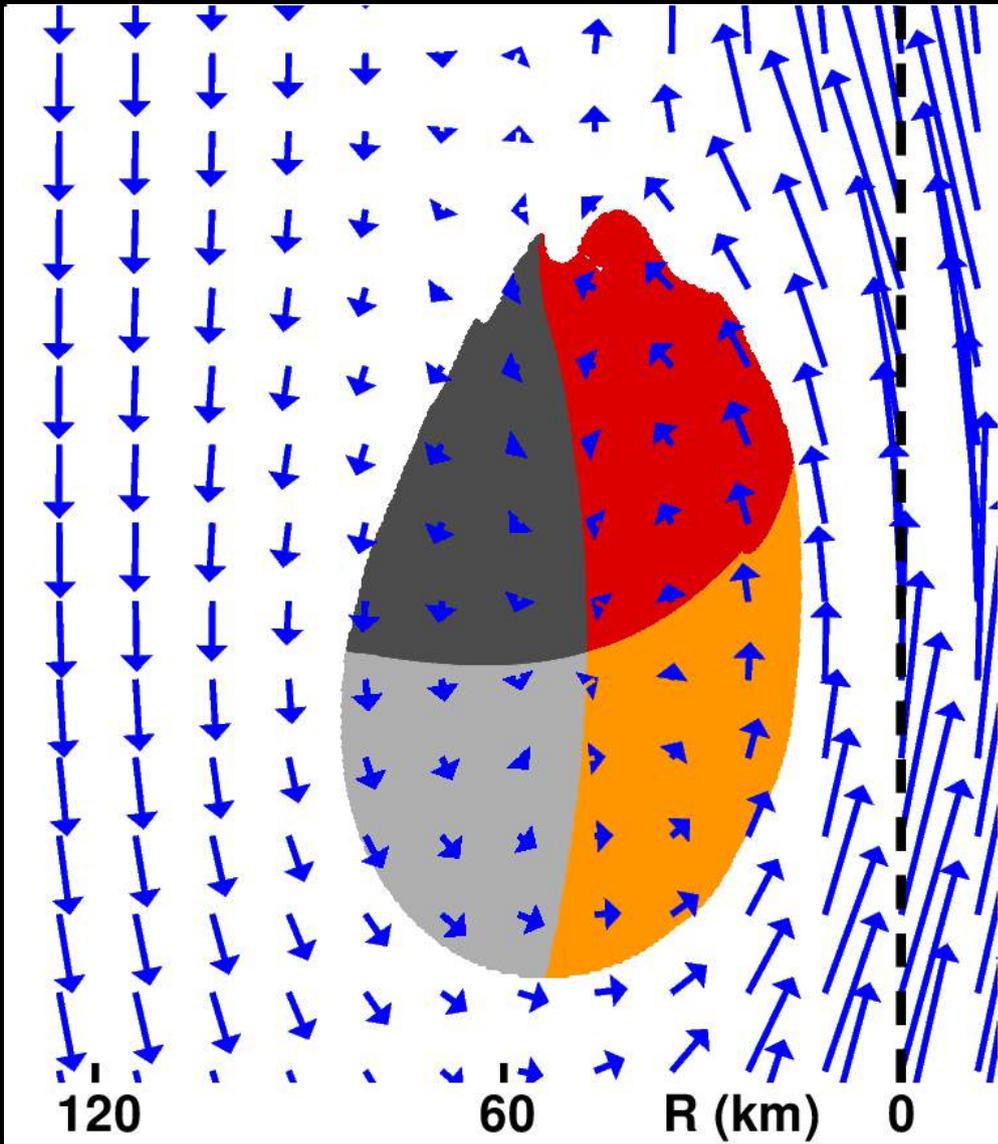


Simple shearing

$$V_x = 0, \quad V_z = Cx$$

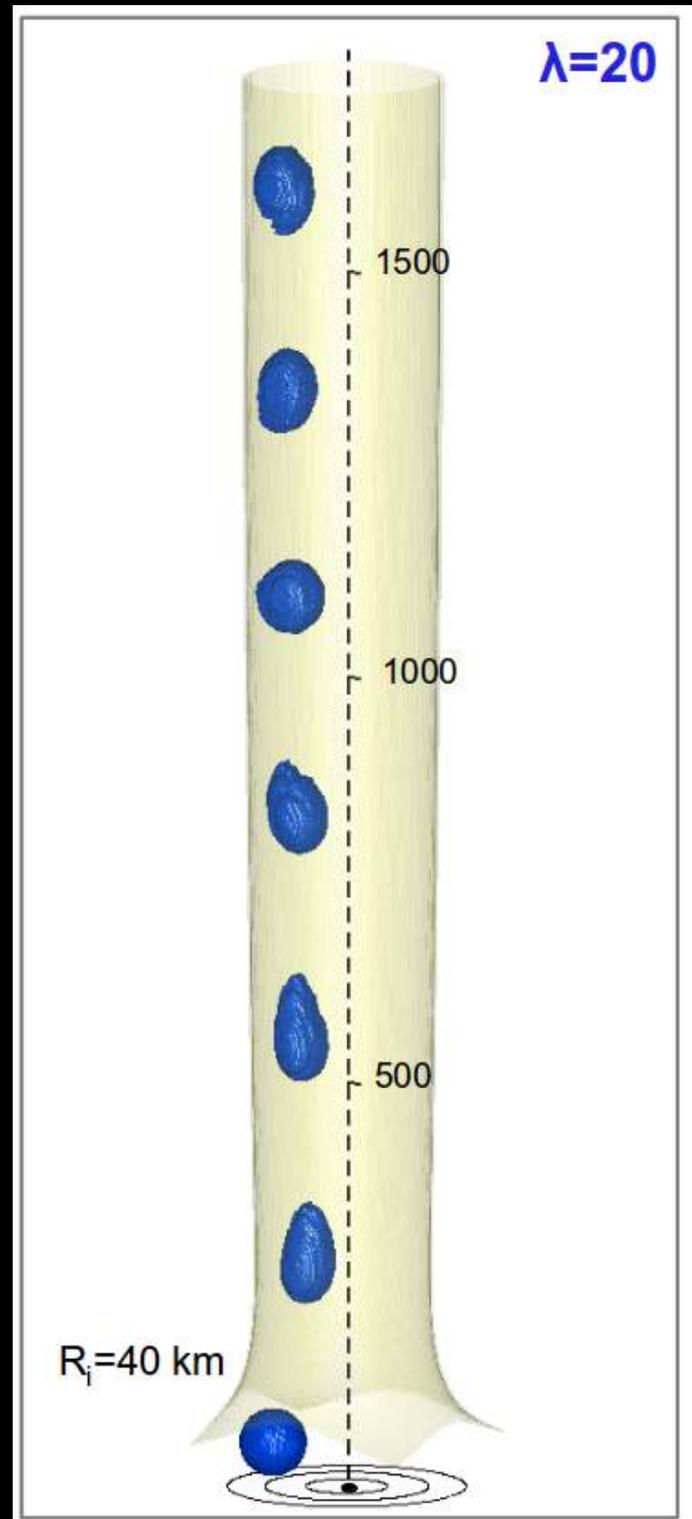
$$\omega_y = -C, \quad \varepsilon_{xz} = C/2$$

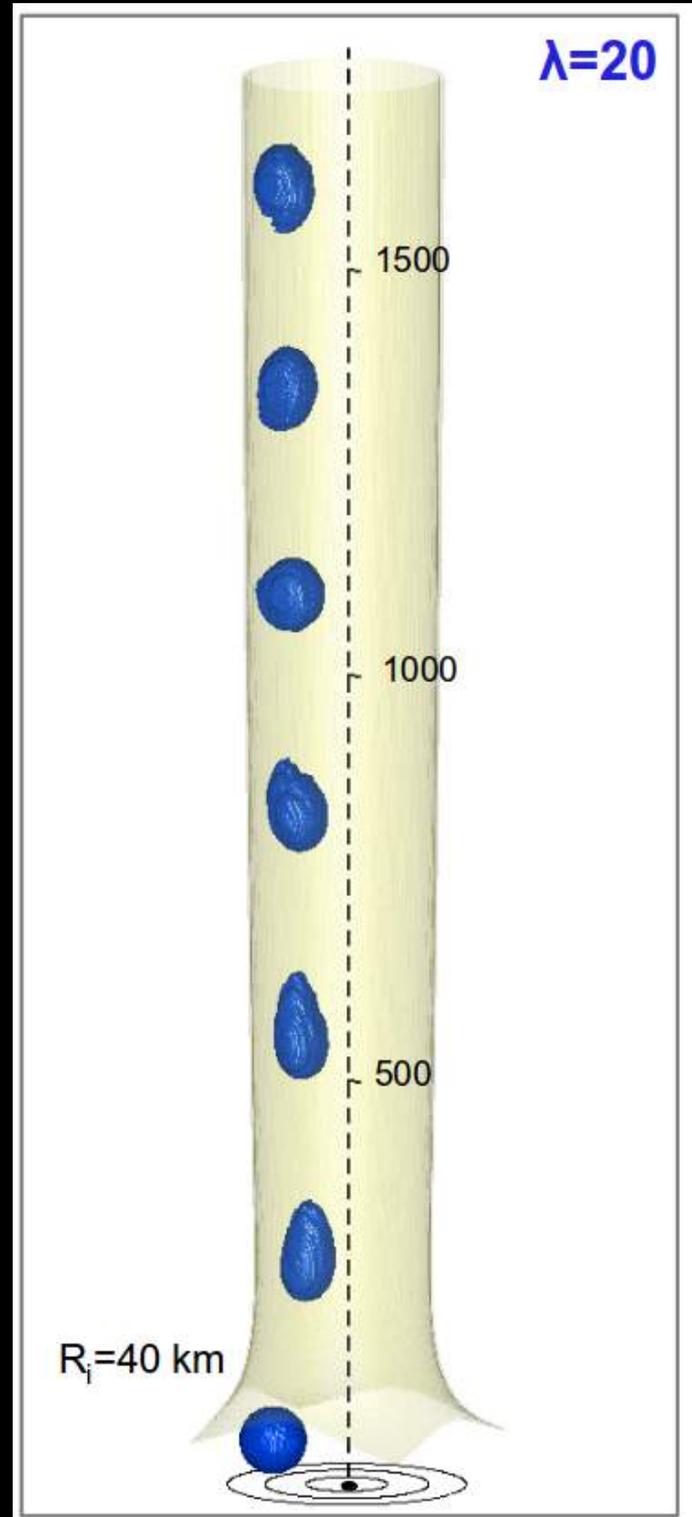
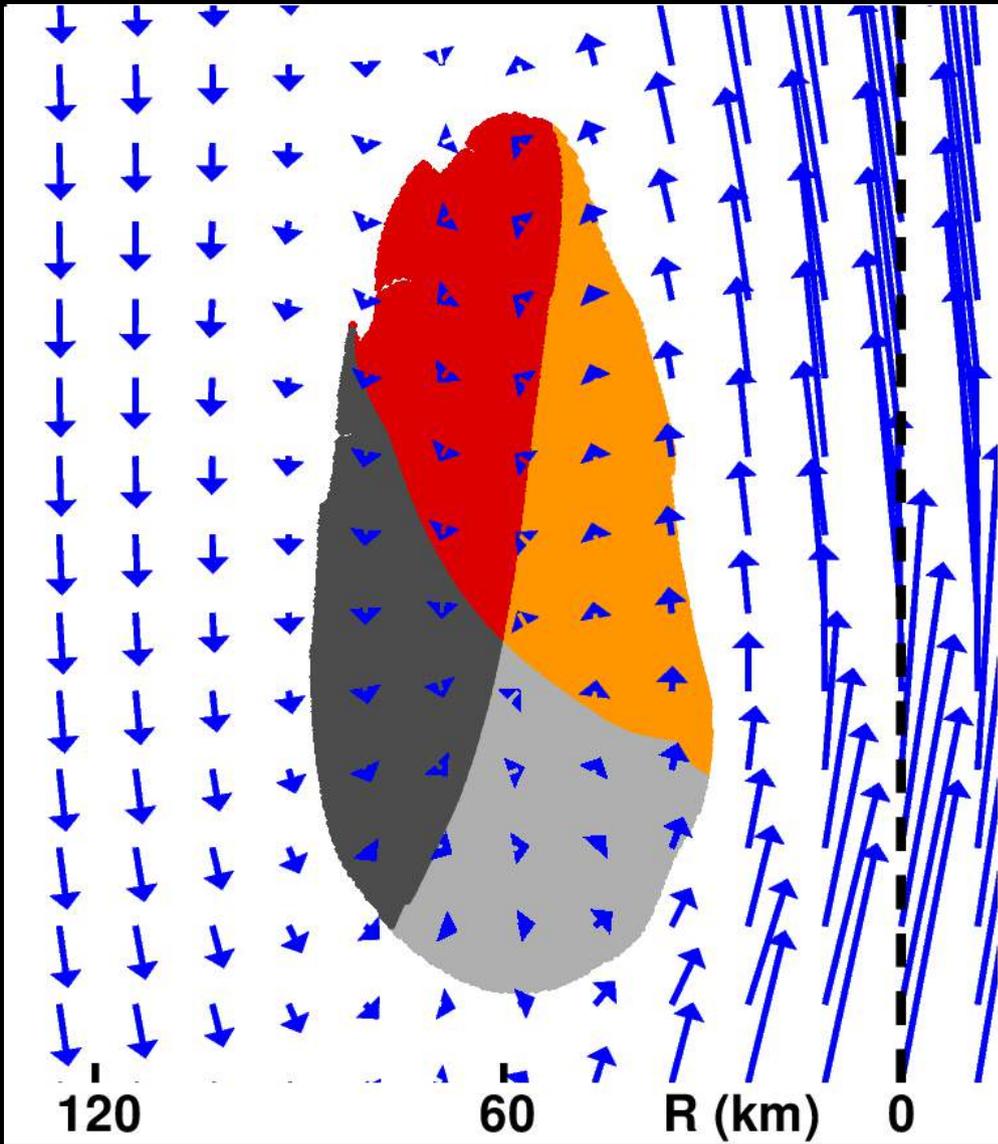


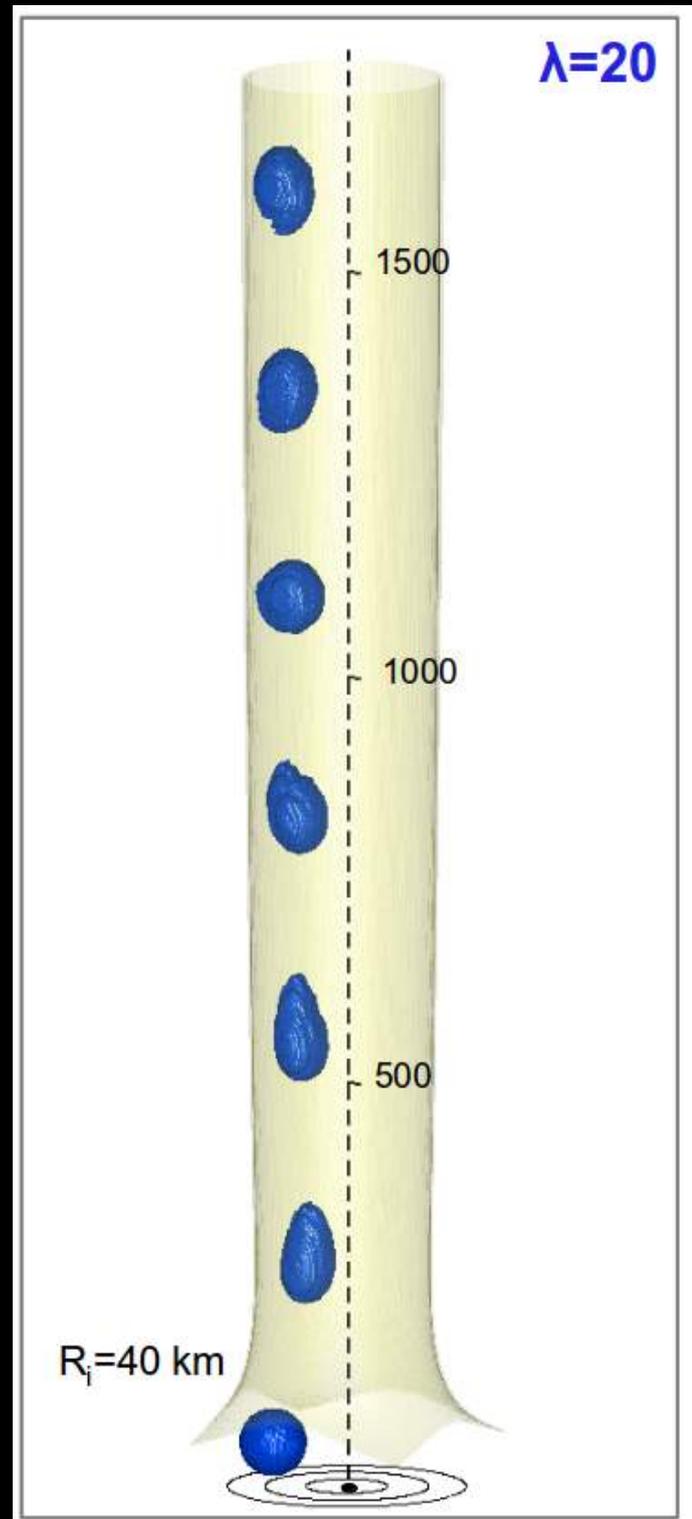
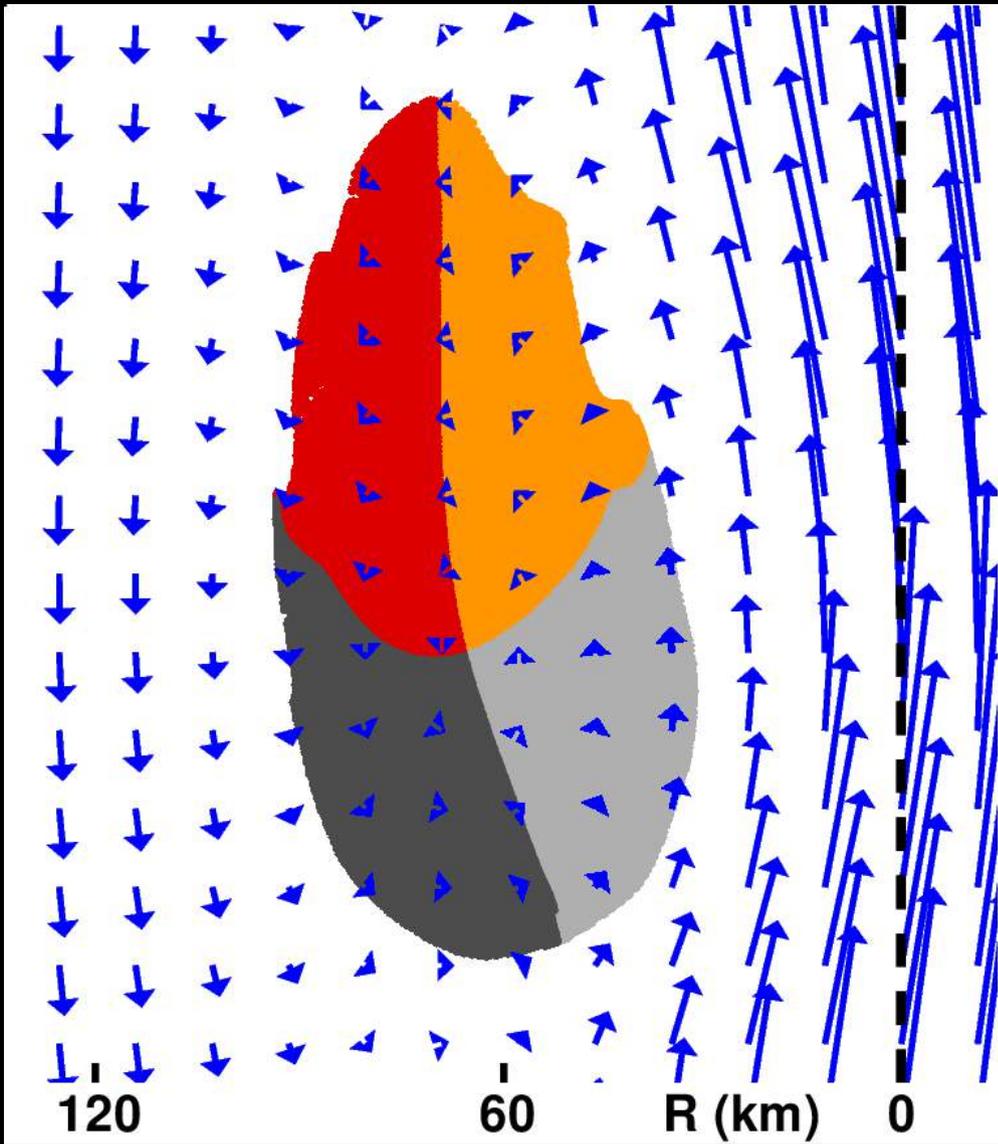


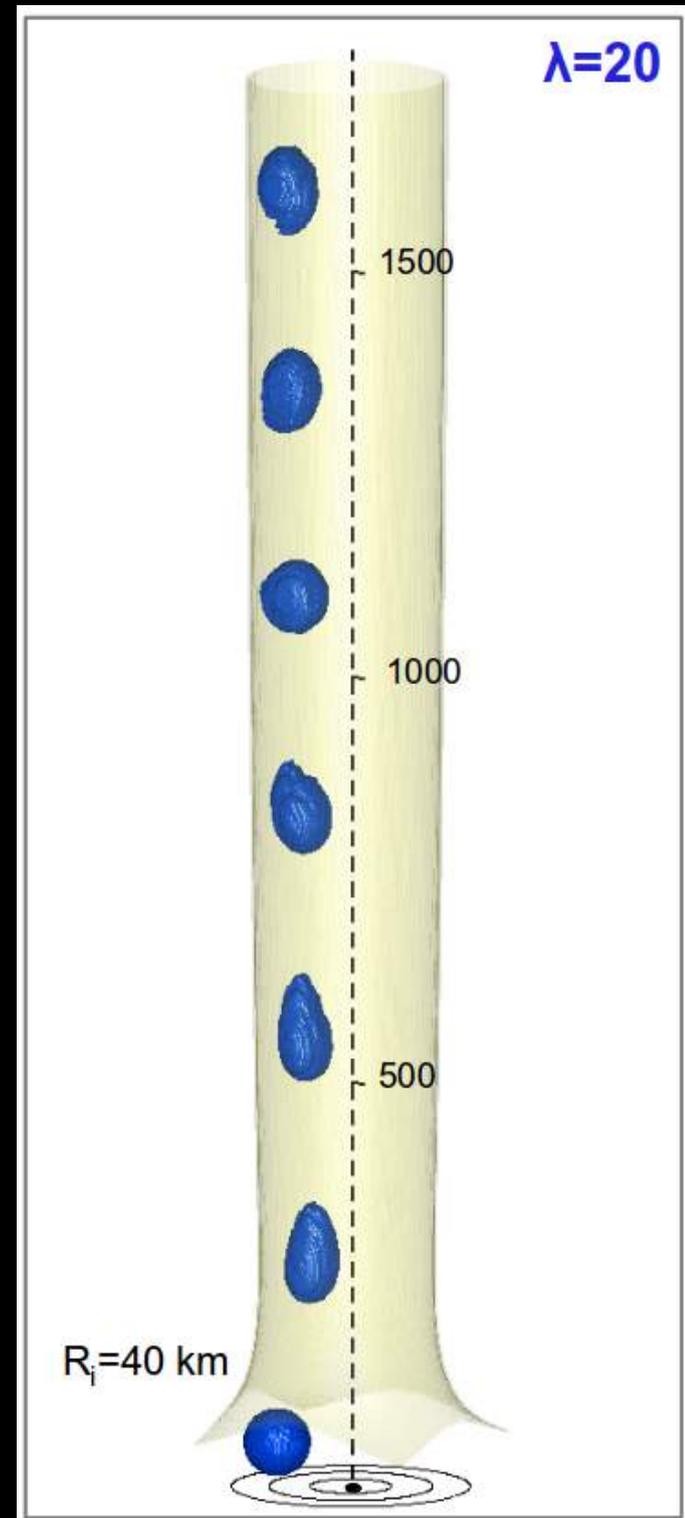
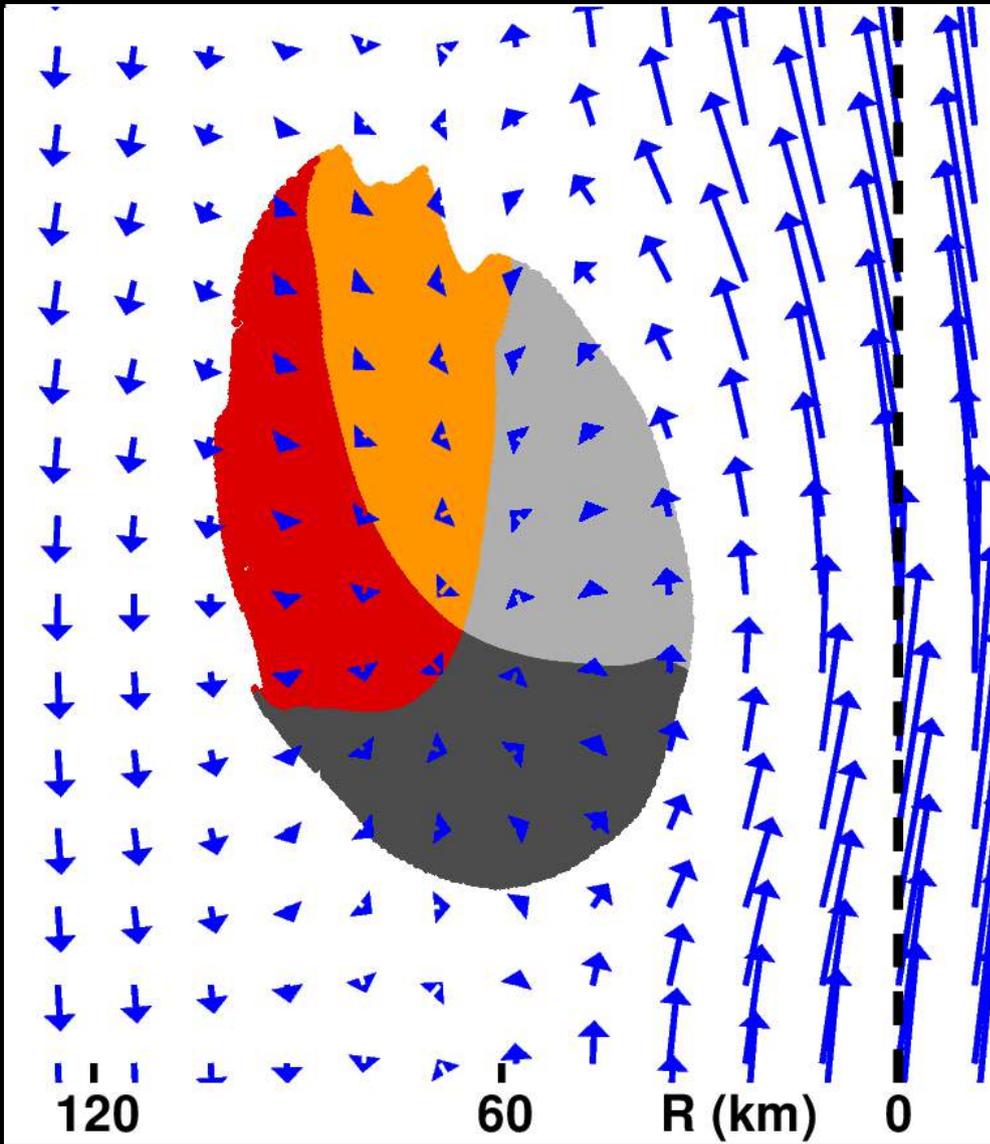
$$\mathbf{V}_x = \mathbf{V}_x - \mathbf{V}_x^{\text{center blob}}$$

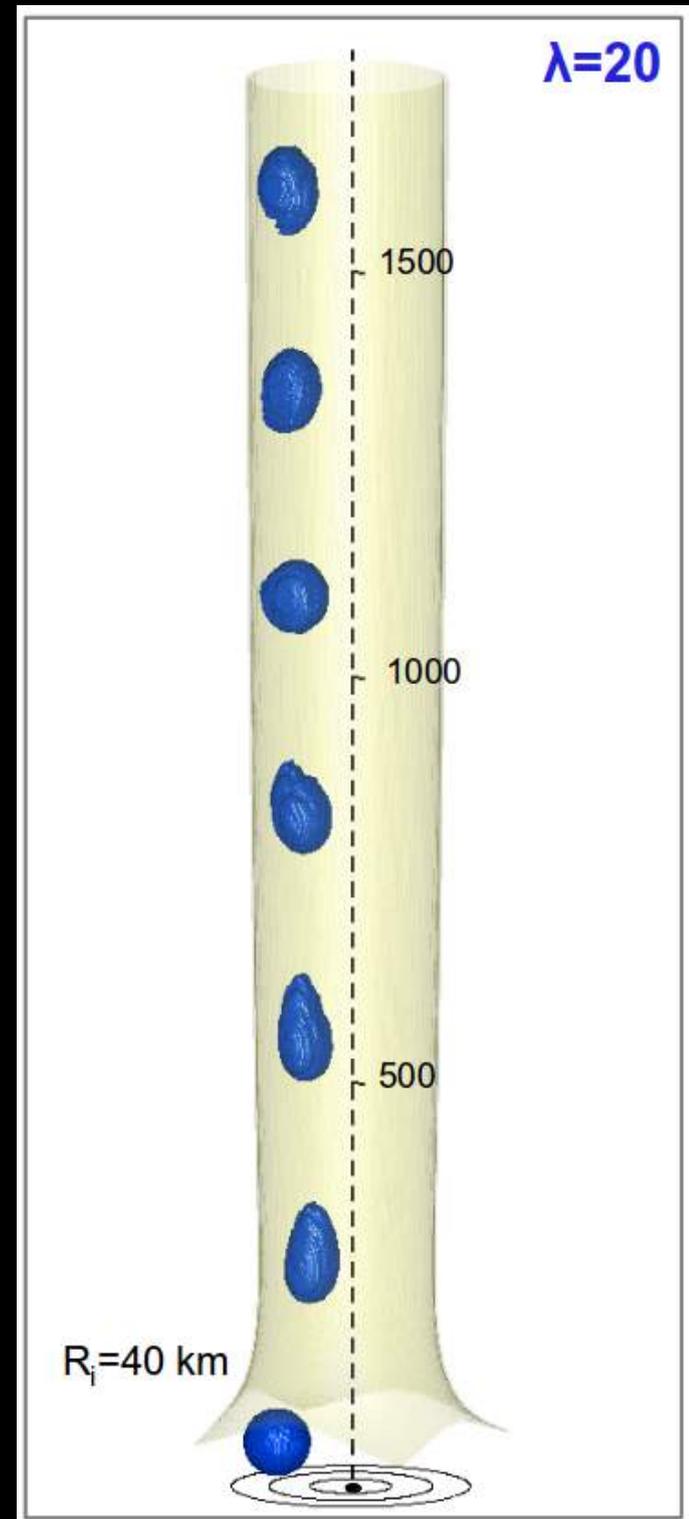
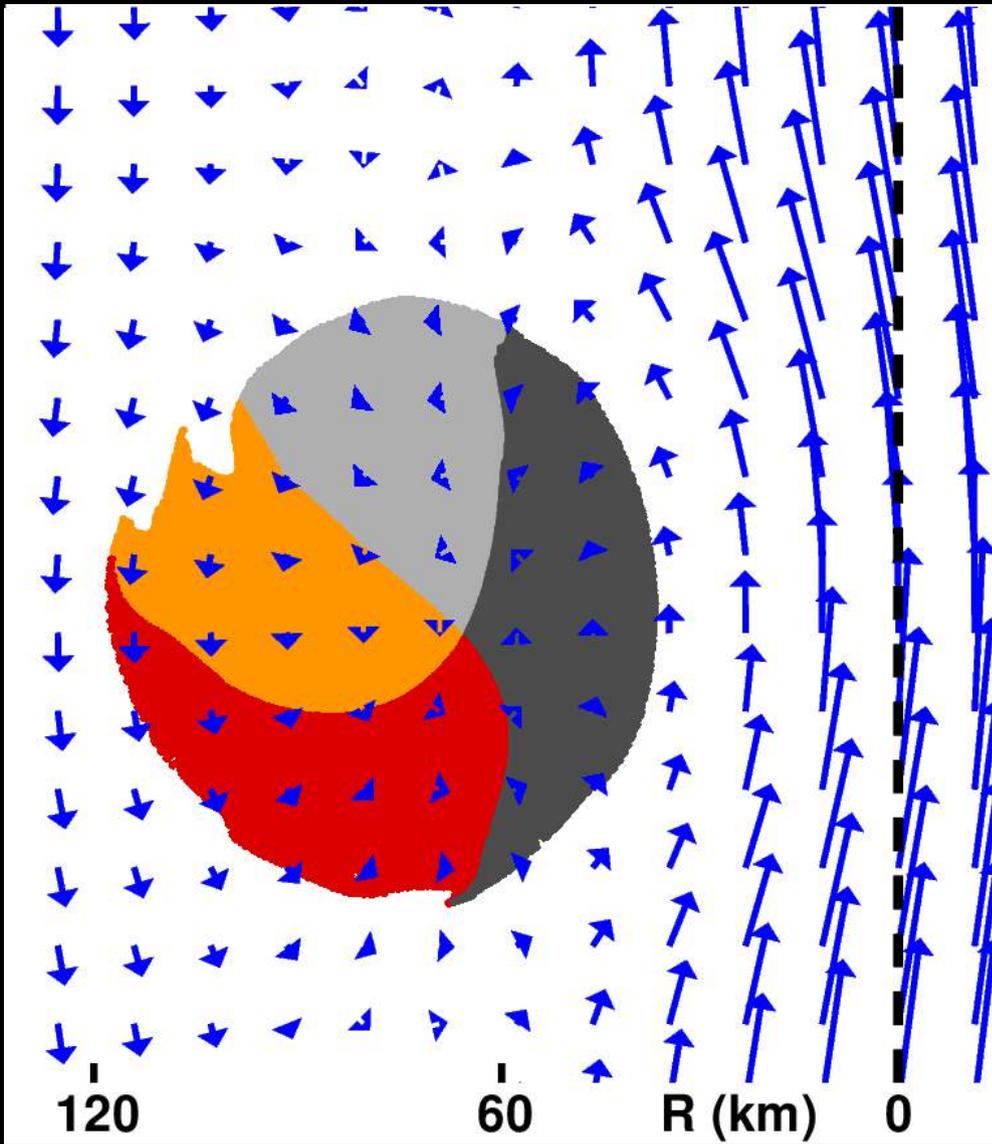
$$\mathbf{V}_z = \mathbf{V}_z - \mathbf{V}_z^{\text{center blob}}$$

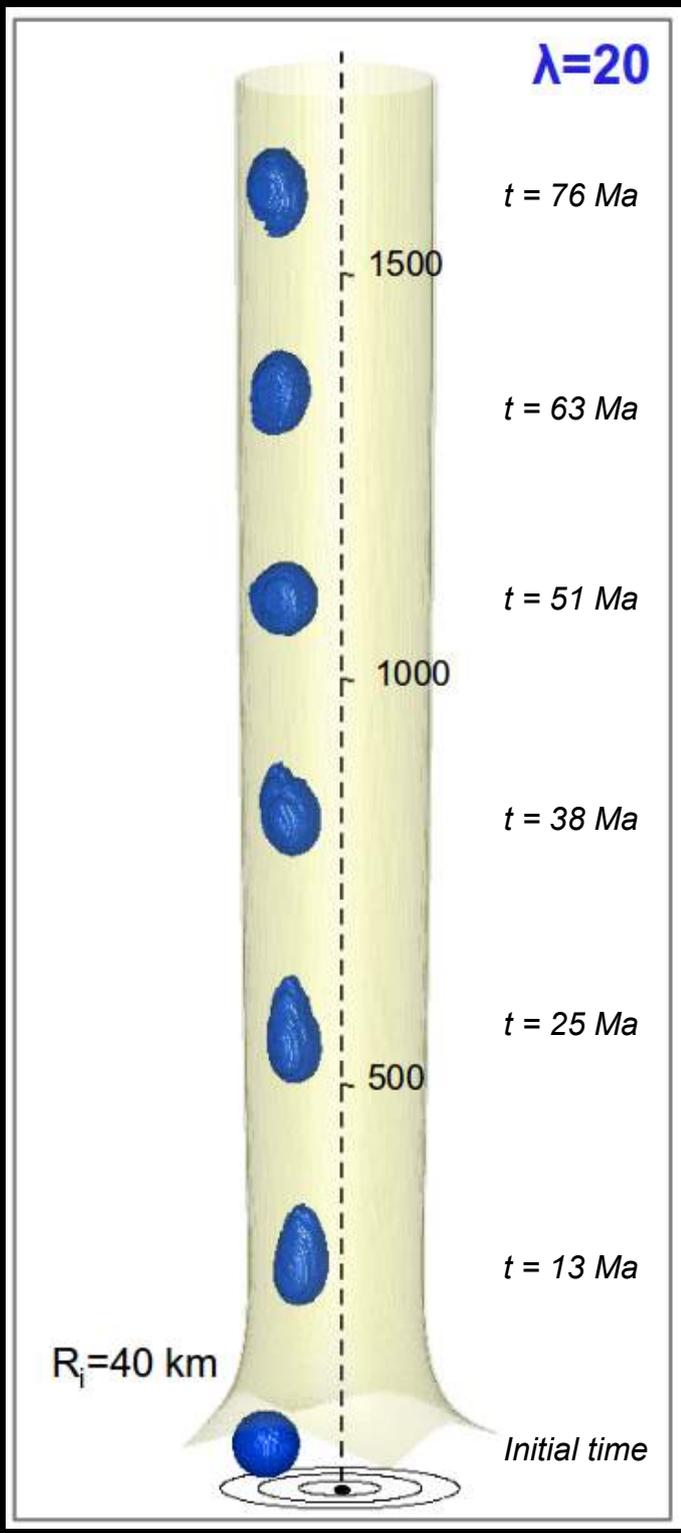
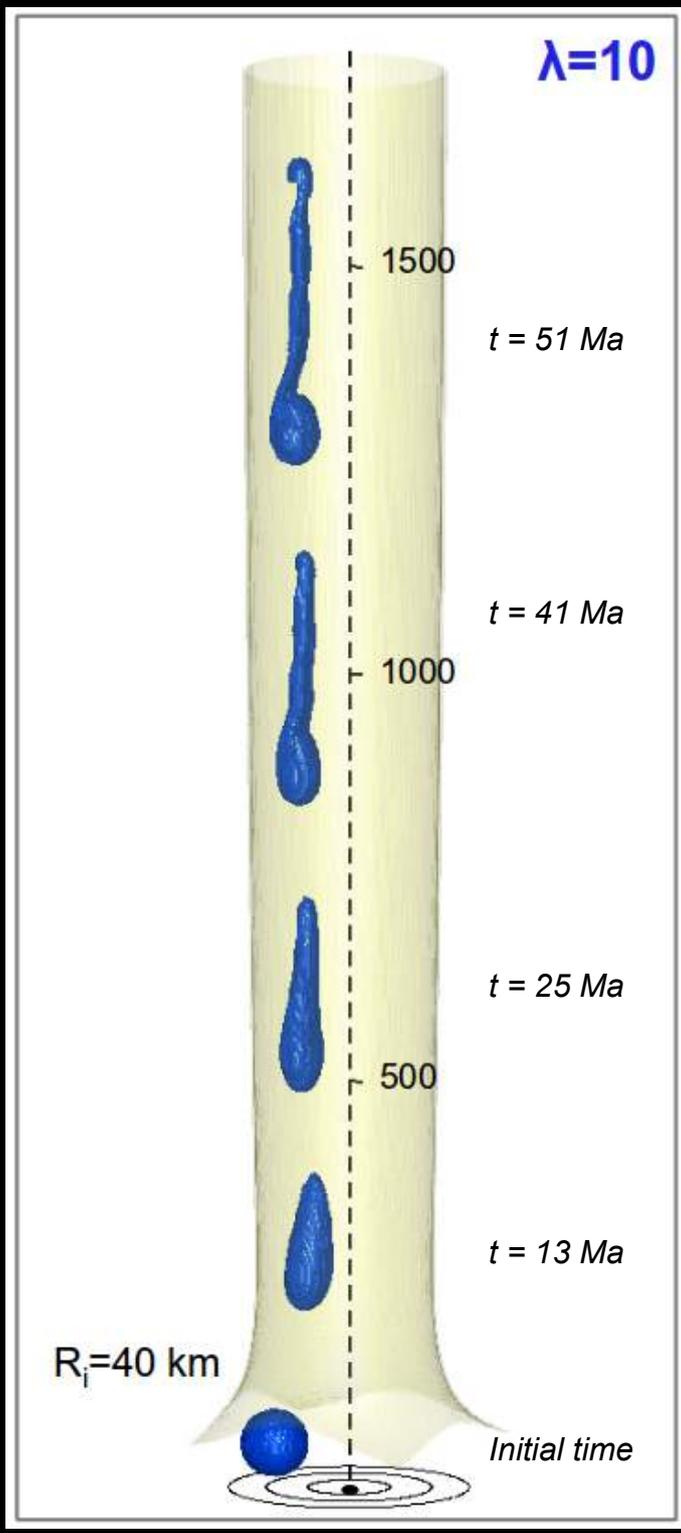
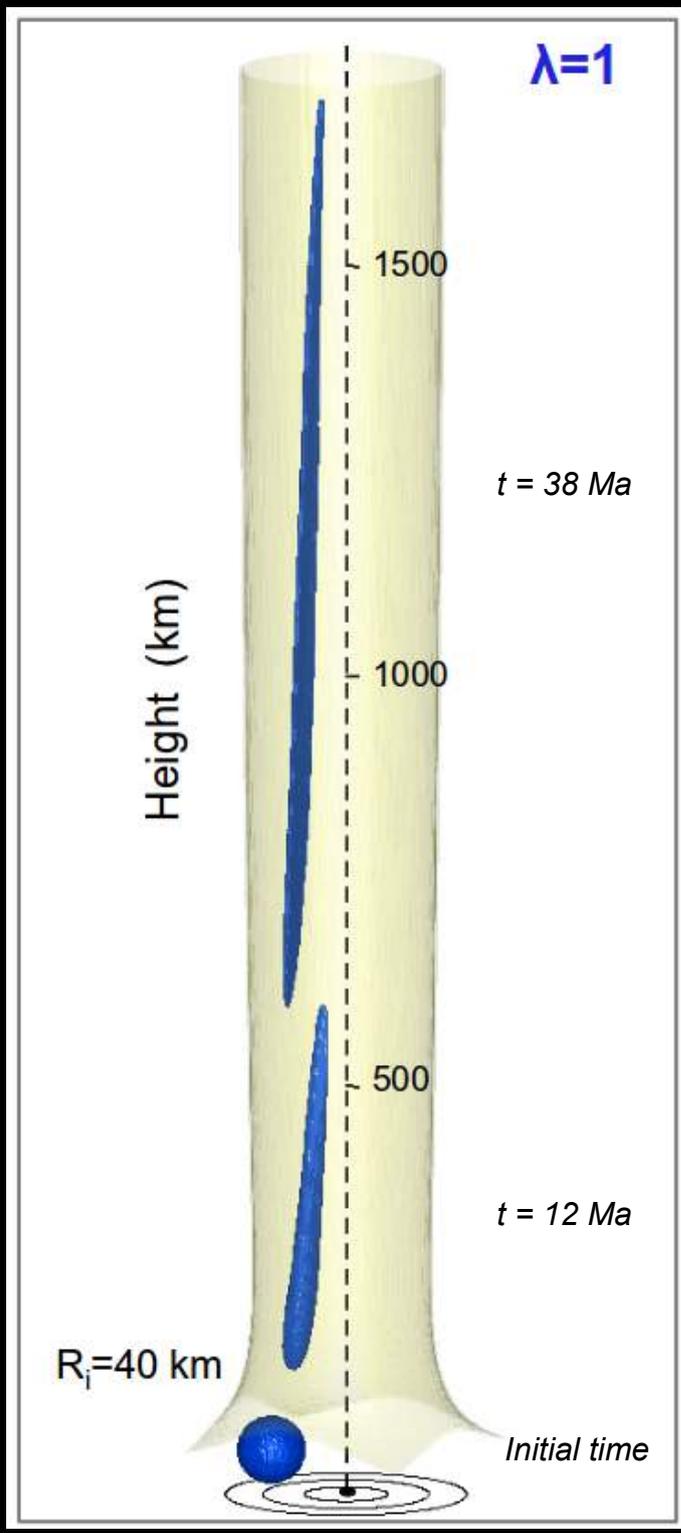




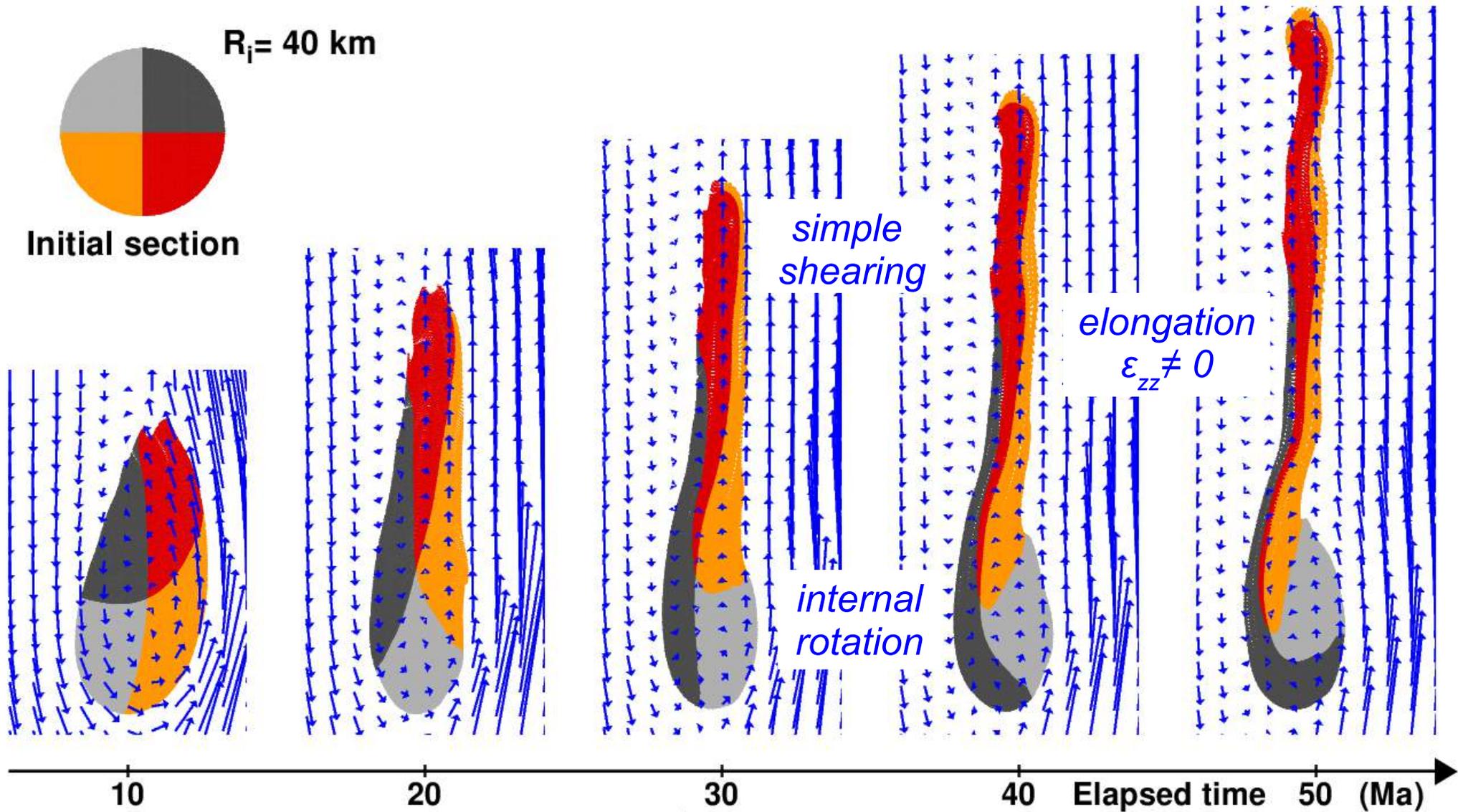




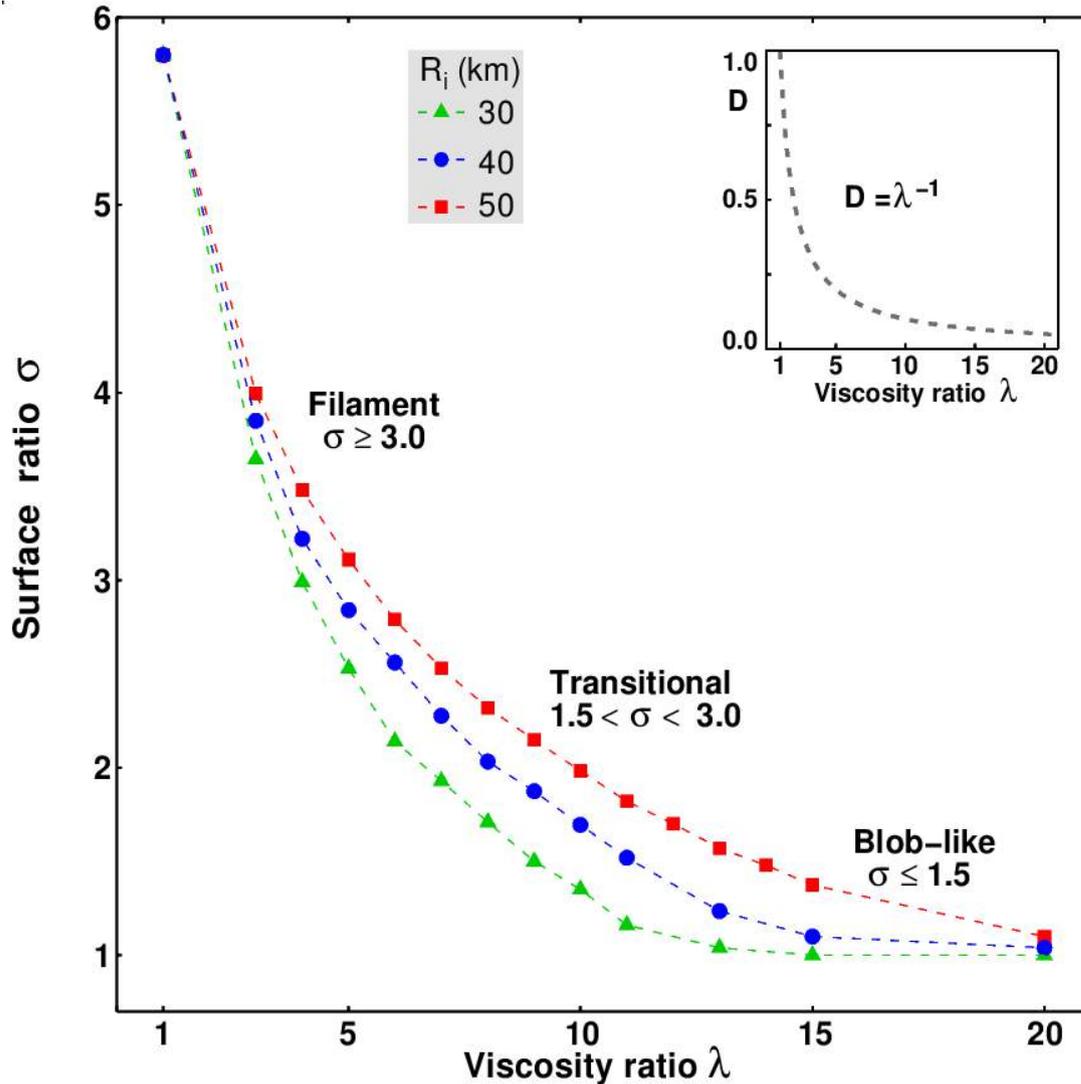




For $\lambda=10$ we find a "transitional" shape



Quantifying the deformation of a 3D body with an irregular shape



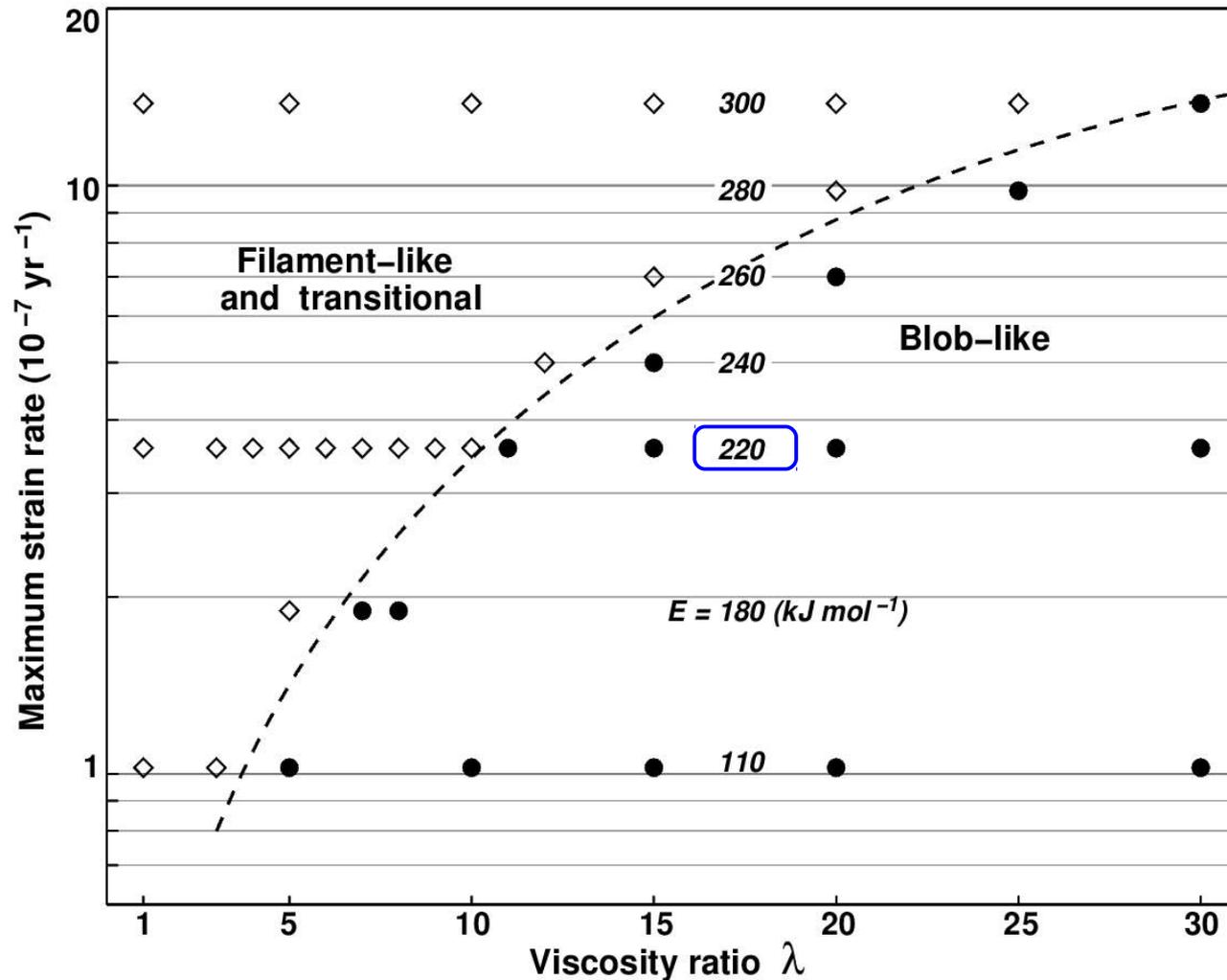
$$\sigma = \frac{\text{Surface heterogeneity at time } t}{\text{Surface initial sphere}}$$

σ decreases with increasing λ

For a given λ , a small size ($R_i = 30$ km) heterogeneity is less deformed than a larger ($R_i = 50$ km) one.

Albeit arbitrarily, σ is used to define shapes: filament-like, transitional and blob-like

Effect of the strain rate ($\epsilon_{rz} \sim dV_z/dr$) across the conduit



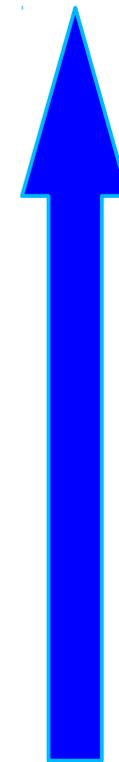
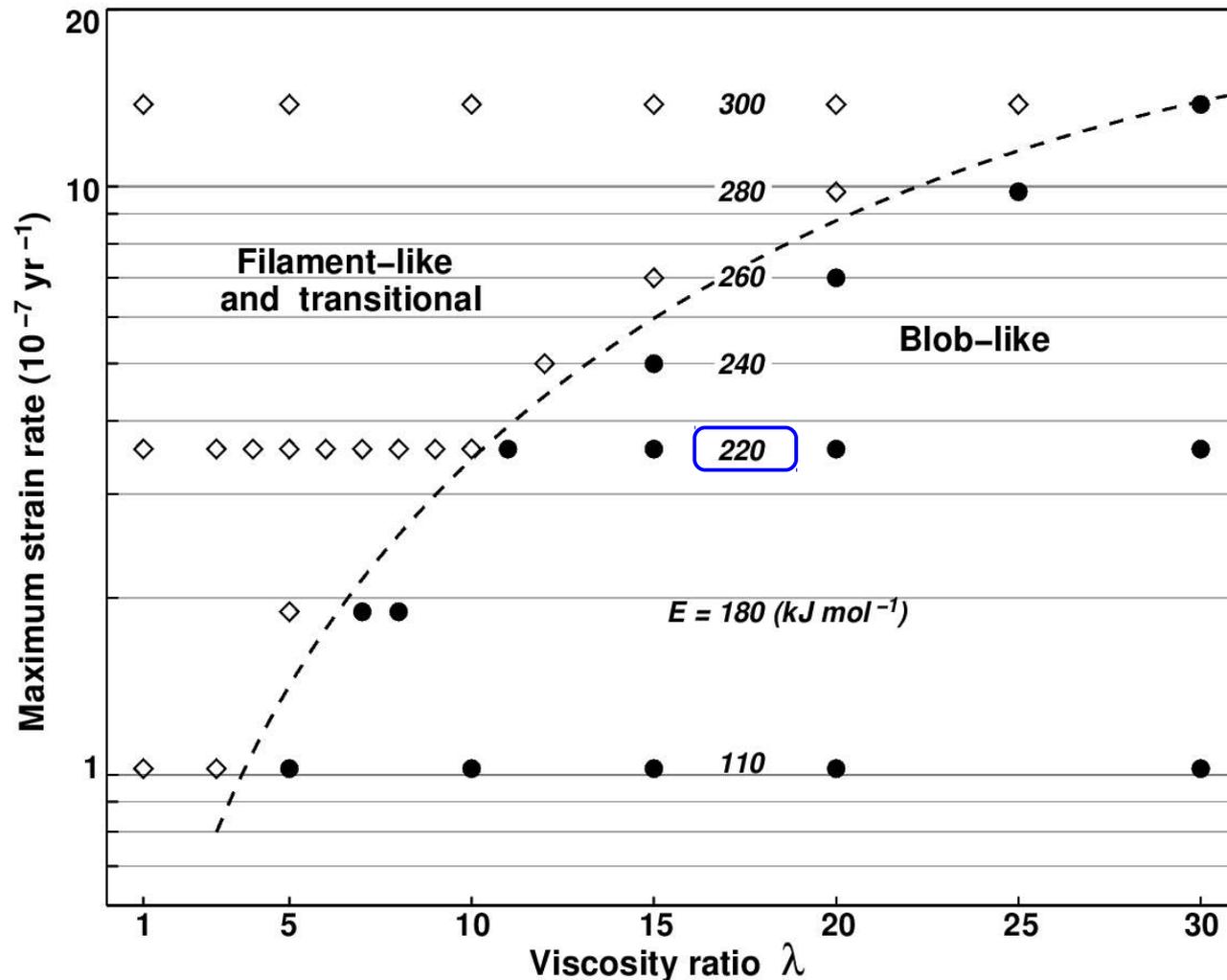
We span a range of ϵ_{rz} by varying the activation energy E .

$$\eta = \eta_m \exp \left[\frac{E}{R} \left(\frac{T_m - T}{T_m T} \right) \right]$$

At high ϵ_{rz} the blob-like shape is restricted to high λ (*i.e.*, $\lambda > 20$).

At low ϵ_{rz} the blob-like shape is stable at $\lambda = 4$, as in Manga [1996].

Effect of the strain rate ($\epsilon_{rz} \sim dV_z/dr$) across the conduit

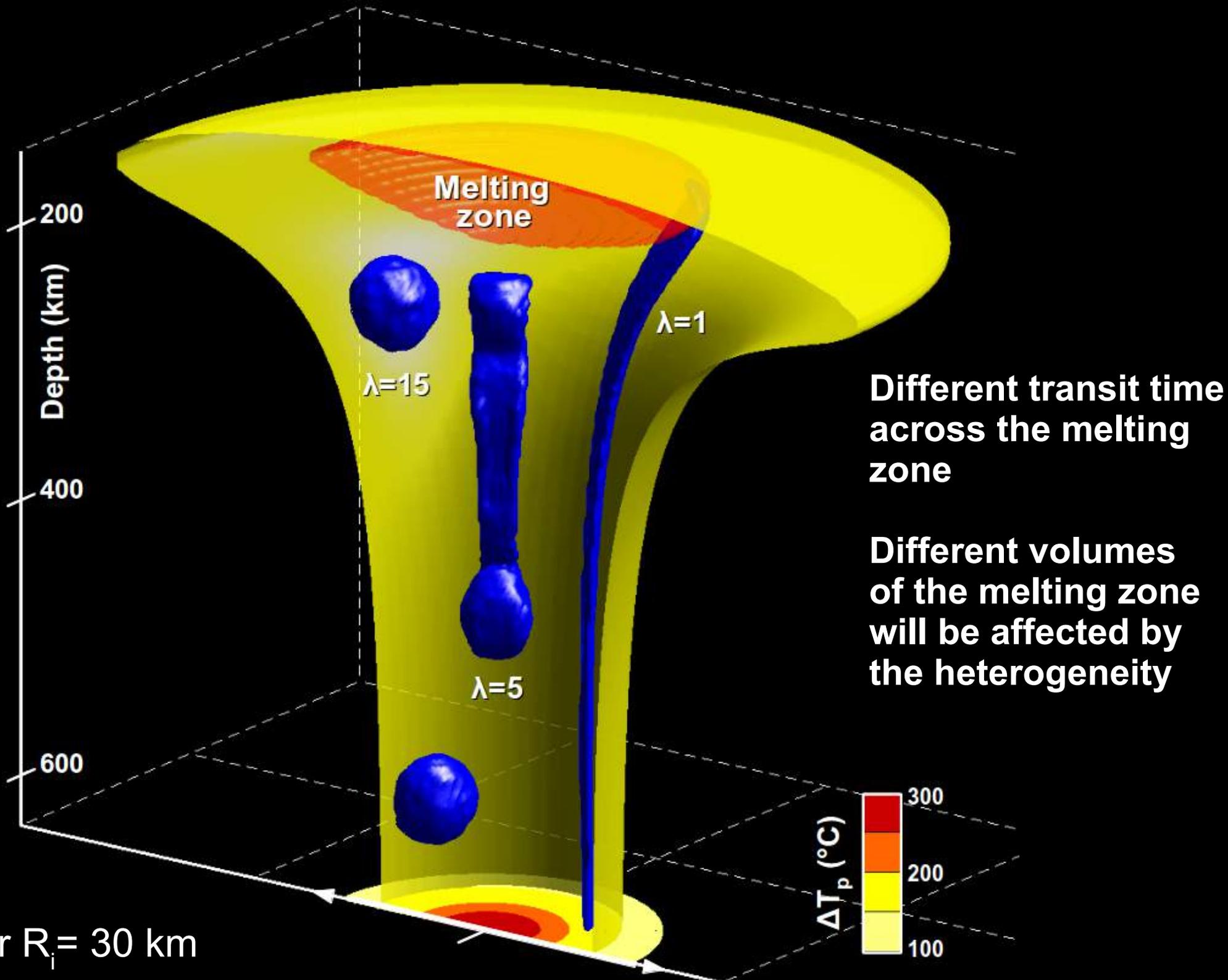


By increasing the activation energy E , the whole plume flow is modified :

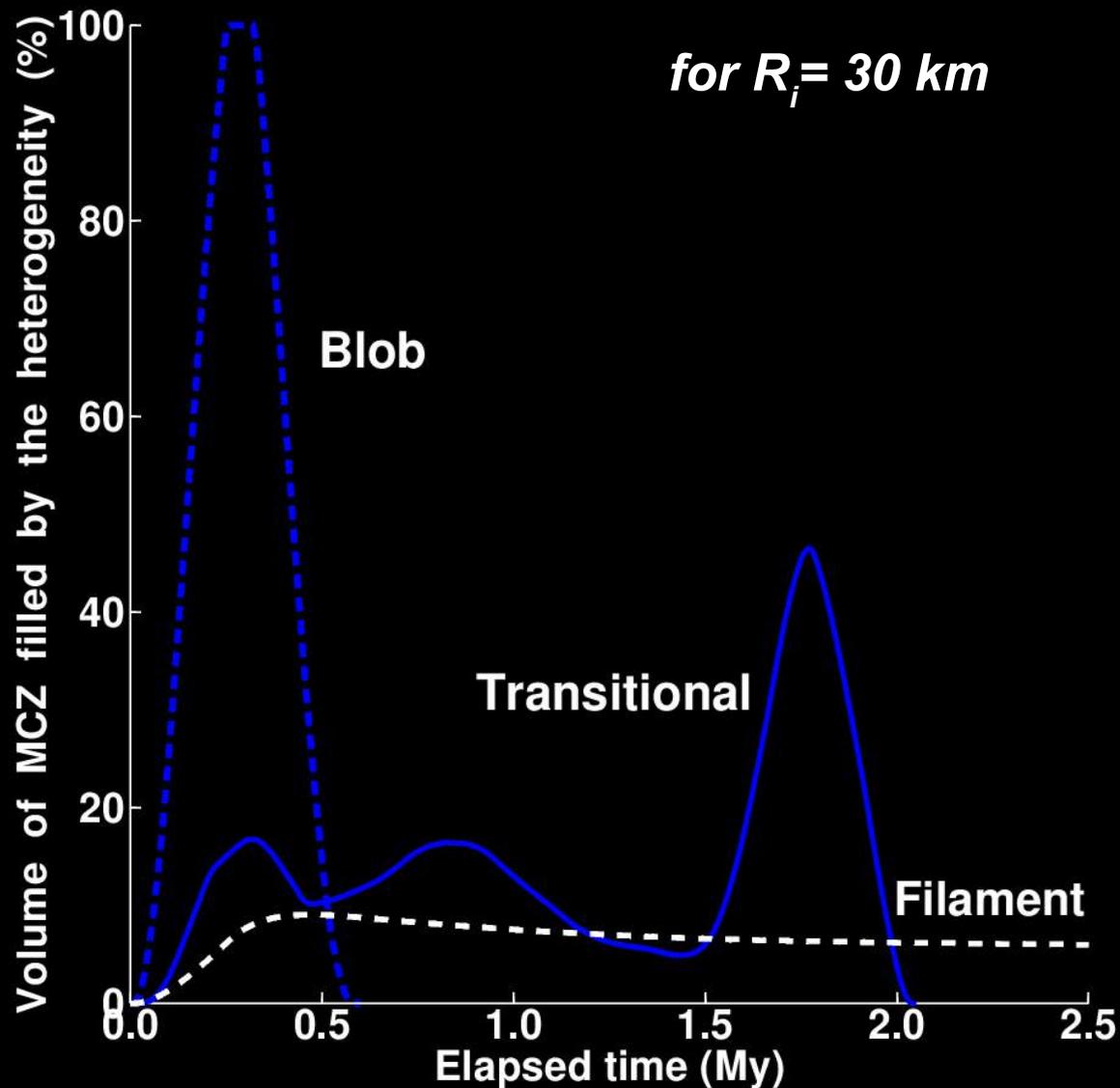
- the upwelling velocity increases
- the buoyancy flux B increases

Filament-like heterogeneities will prevail in **vigorous plumes** ($B_{\text{Hawaii}} = 8700 \text{ Kg/s}$)

Blob-like heterogeneities will be more easily preserved in **weaker plumes**
 ($B_{\text{Réunion}} = 1900 \text{ Kg/s}$; $B_{\text{Samoa}} = 1600 \text{ Kg/s}$)



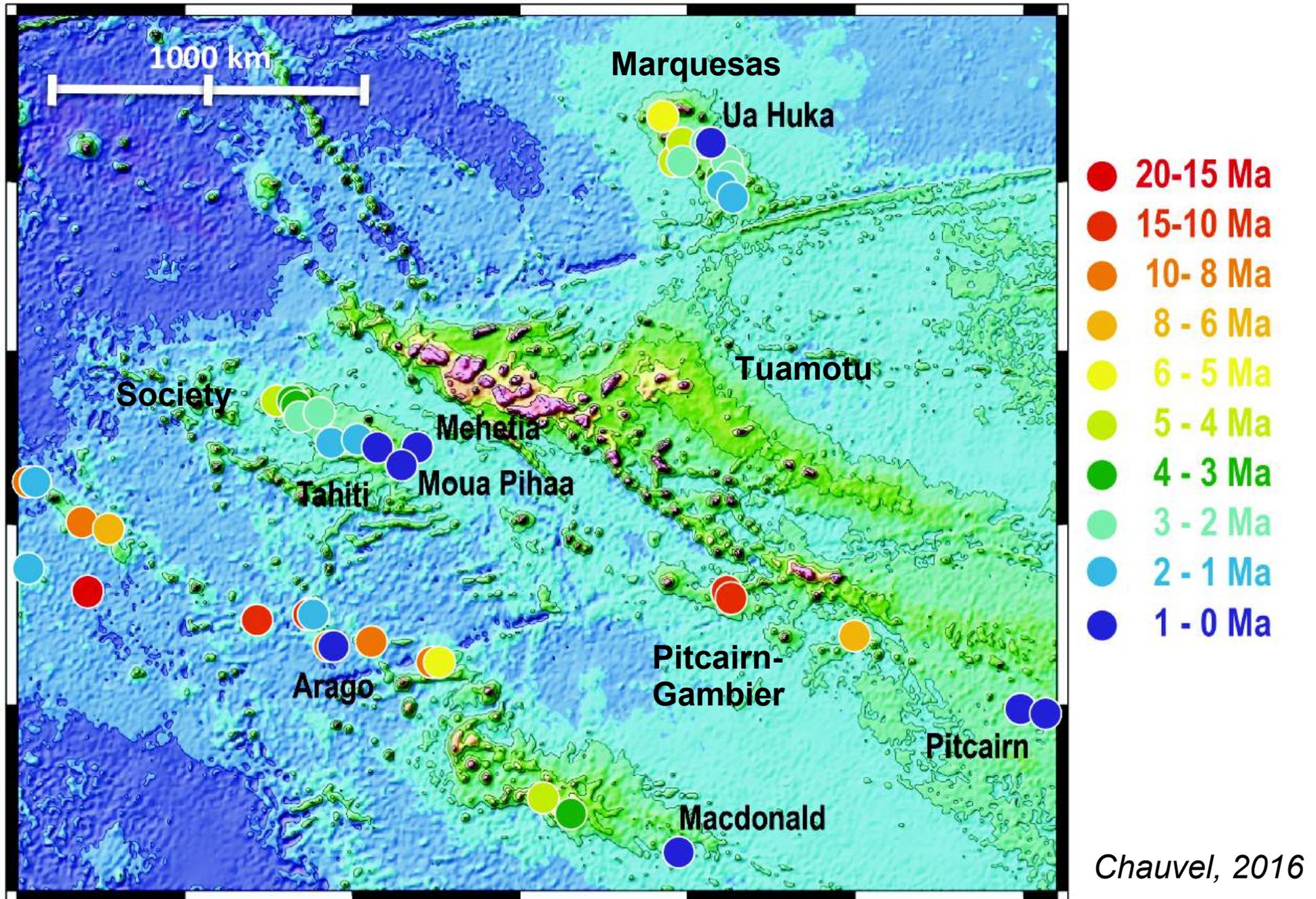
Are viscous blobs compositionally more (or less) fertile ?



If more fertile
their presence can enhance
melting and possibly leave a
distinct isotopic fingerprint
for time-scales of ~ 0.5 Ma.

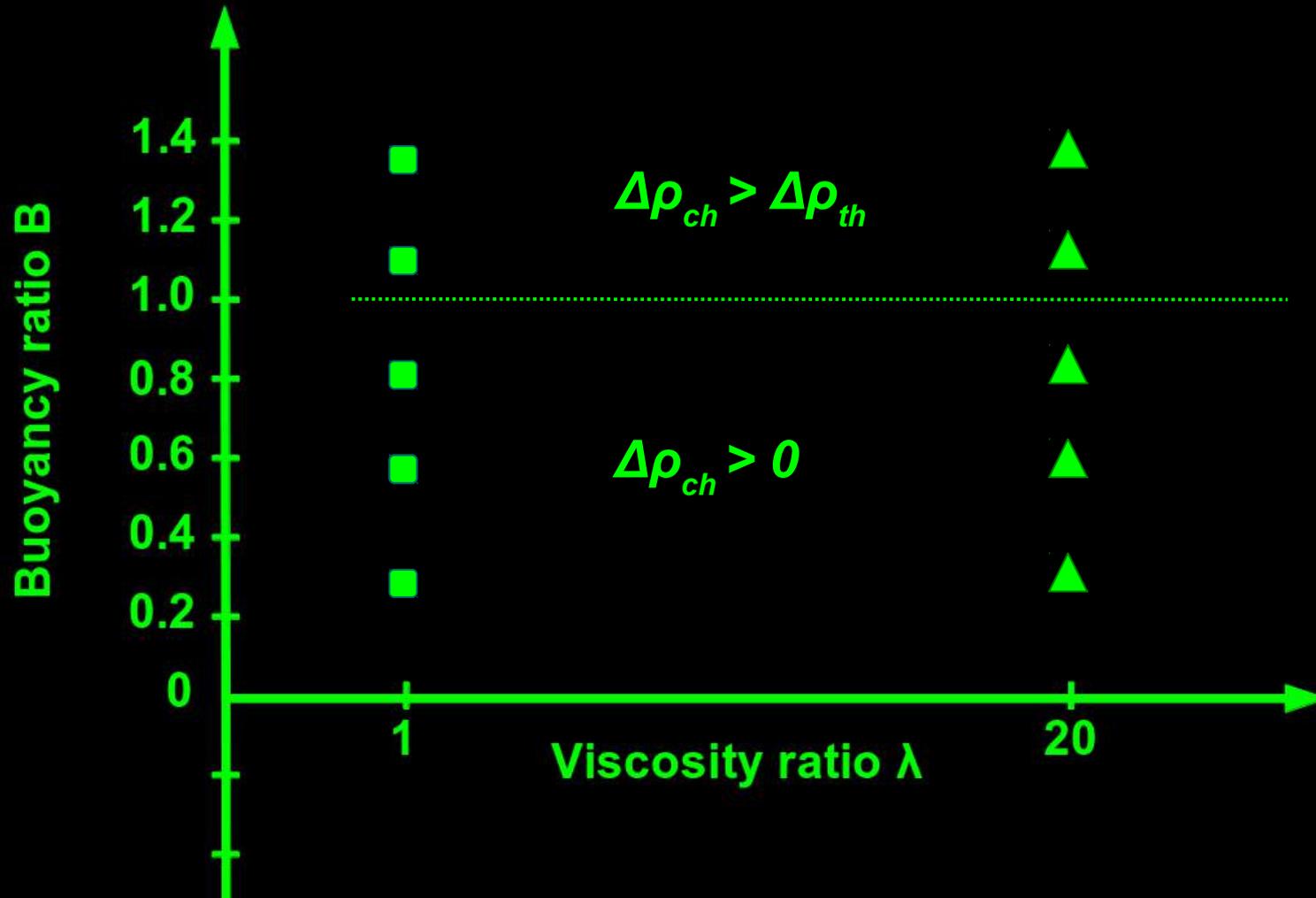
If less fertile
their presence can reduce
or shut-off melt production.

Volcanic activity through time for some Pacific hotspots



Exploring the effect of compositional buoyancy

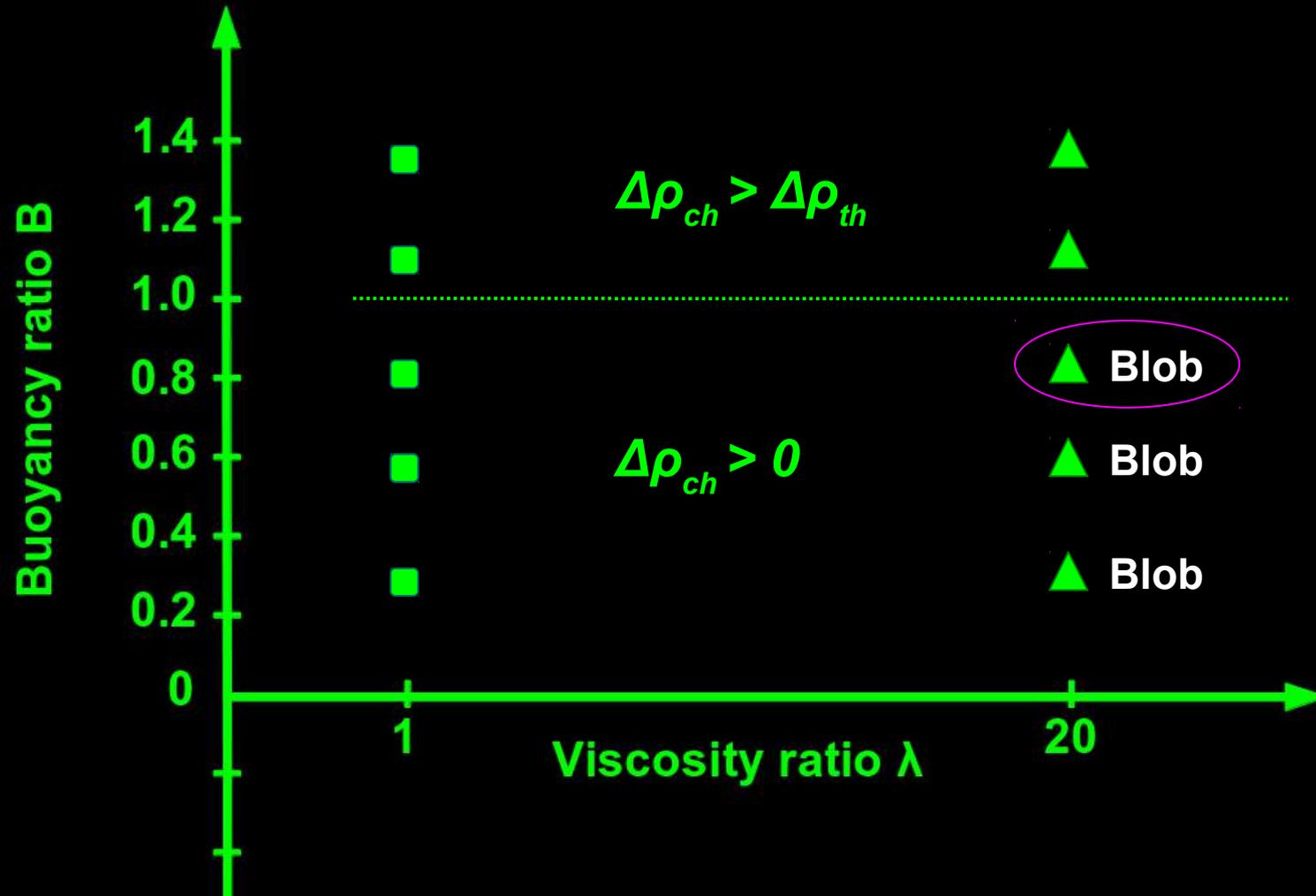
The buoyancy ratio $B = \Delta\rho_{ch} / \Delta\rho_{th}$



For $\lambda=20$ we conducted numerical simulations spanning a range of B values
For $\lambda=1$ numerical simulations and laboratory experiments by A. Limare, M. Geissmann

Exploring the effect of compositional buoyancy

$$\text{The buoyancy ratio } B = \Delta\rho_{ch} / \Delta\rho_{th}$$



Elapsed
time (Ma)

5

27

39

52

65

80

102

124

Melting
zone

149

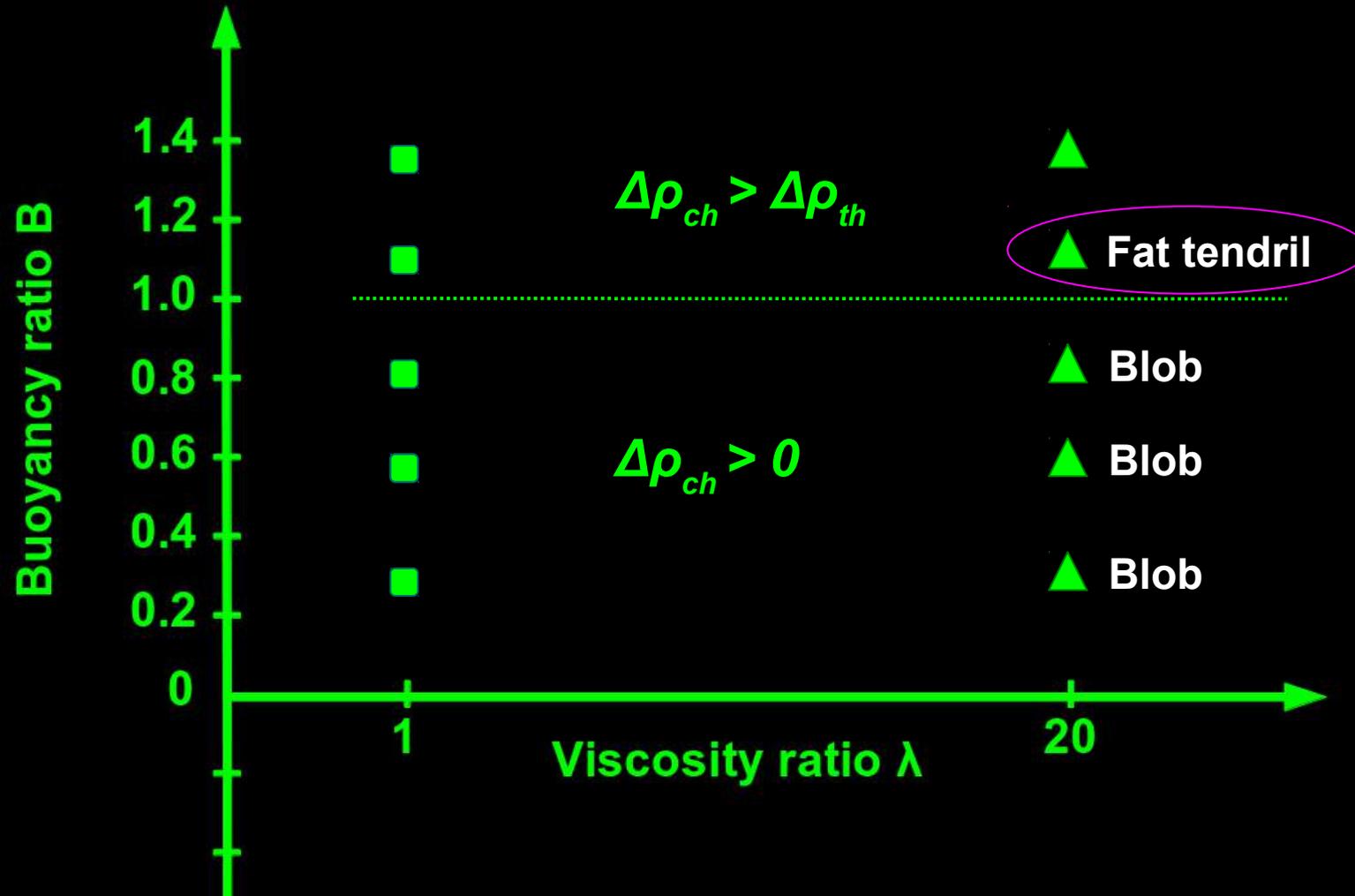
Viscous heterogeneity $\lambda = 20$
Compositionally denser $B = 0.8$

Plume axis



Exploring the effect of compositional buoyancy

$$\text{The buoyancy ratio } B = \Delta\rho_{ch} / \Delta\rho_{th}$$



Elapsed
time (Ma)

22

30

43

50

64

76

89

101

Melting
zone

114

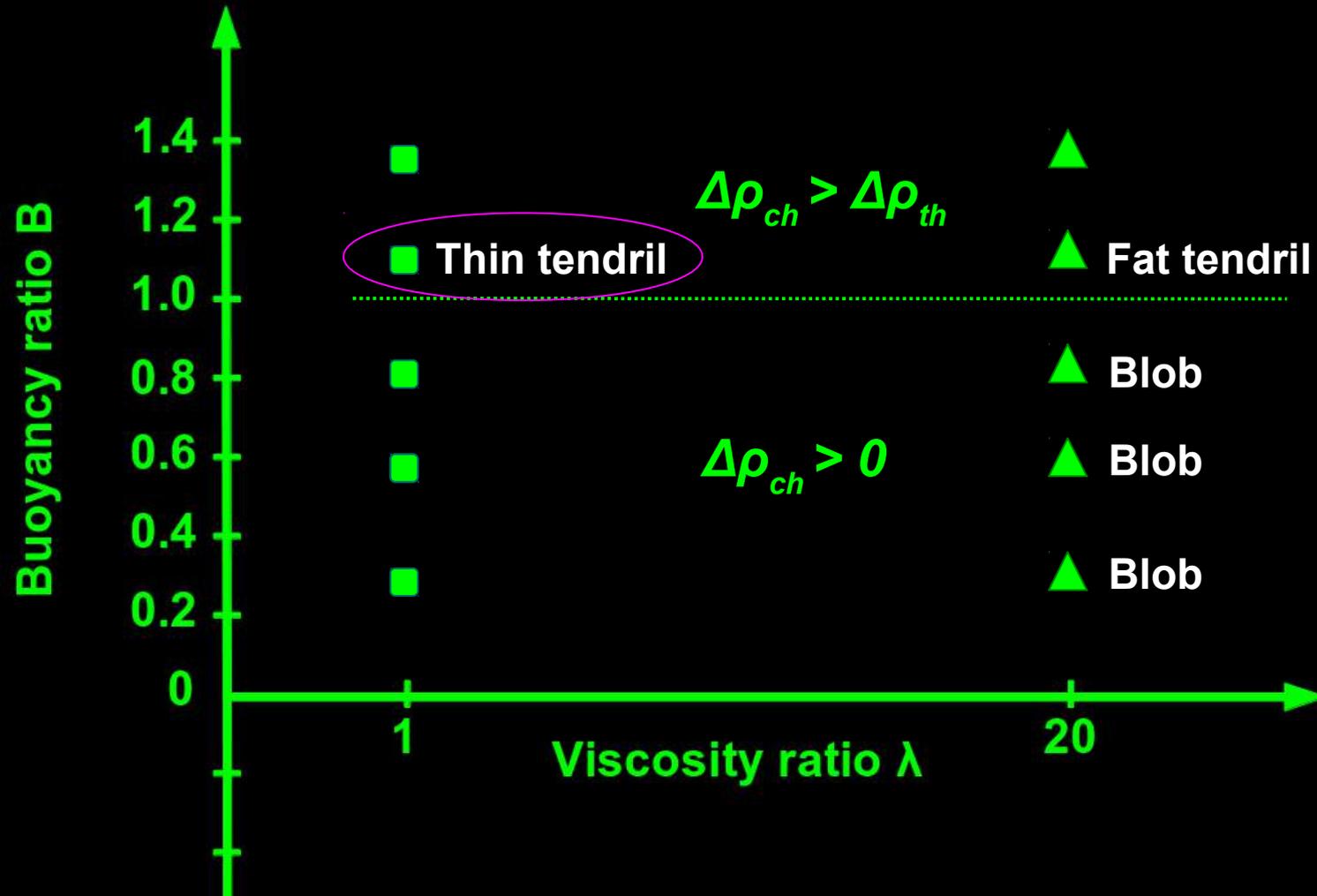
Viscous heterogeneity $\lambda = 20$
Compositionally denser $B = 1.1$

Plume axis



Exploring the effect of compositional buoyancy

$$\text{The buoyancy ratio } B = \Delta\rho_{ch} / \Delta\rho_{th}$$



Elapsed time (Ma)

4

21

27

33

46

59

72

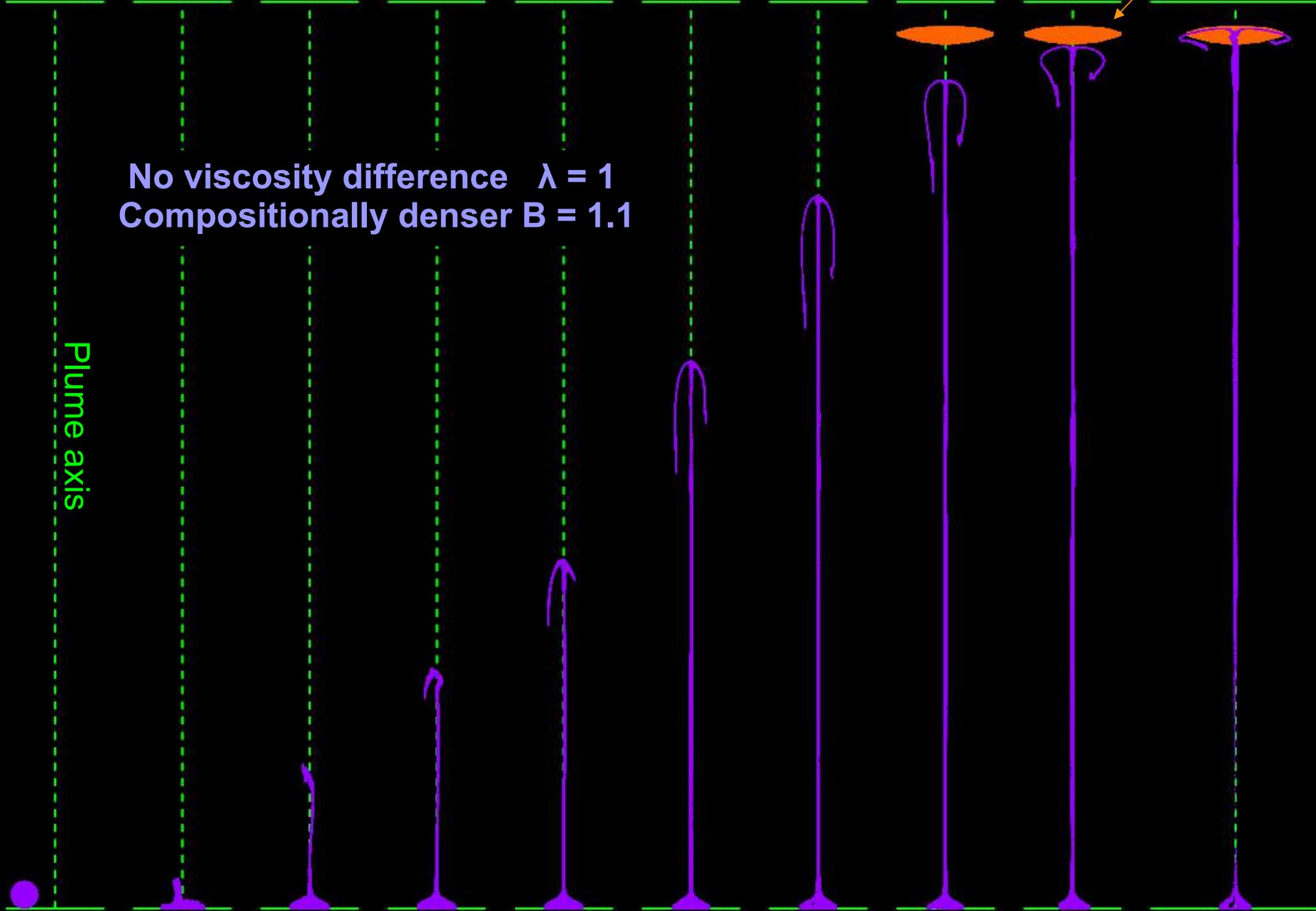
82

Melting zone

98

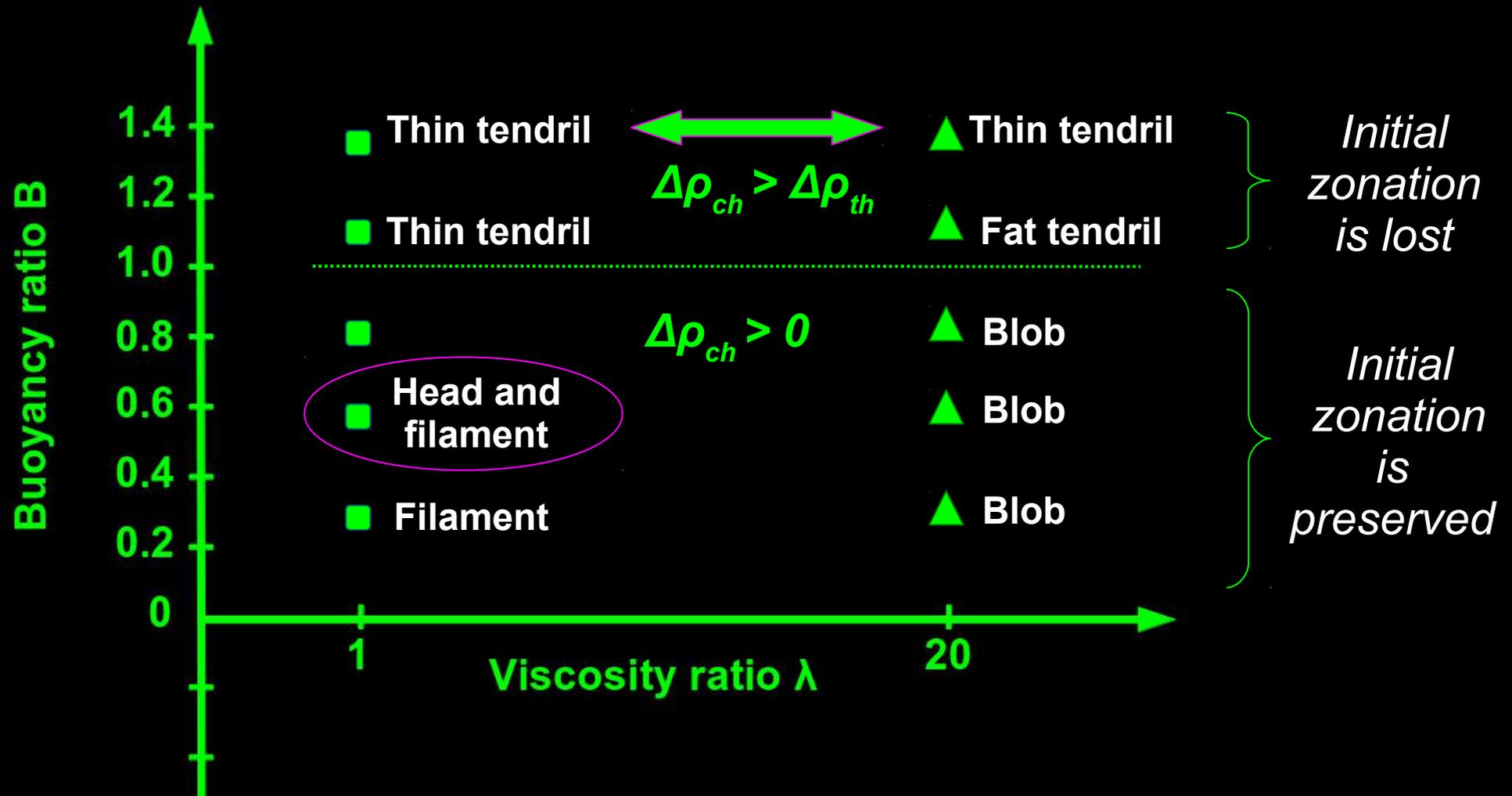
No viscosity difference $\lambda = 1$
Compositionally denser $B = 1.1$

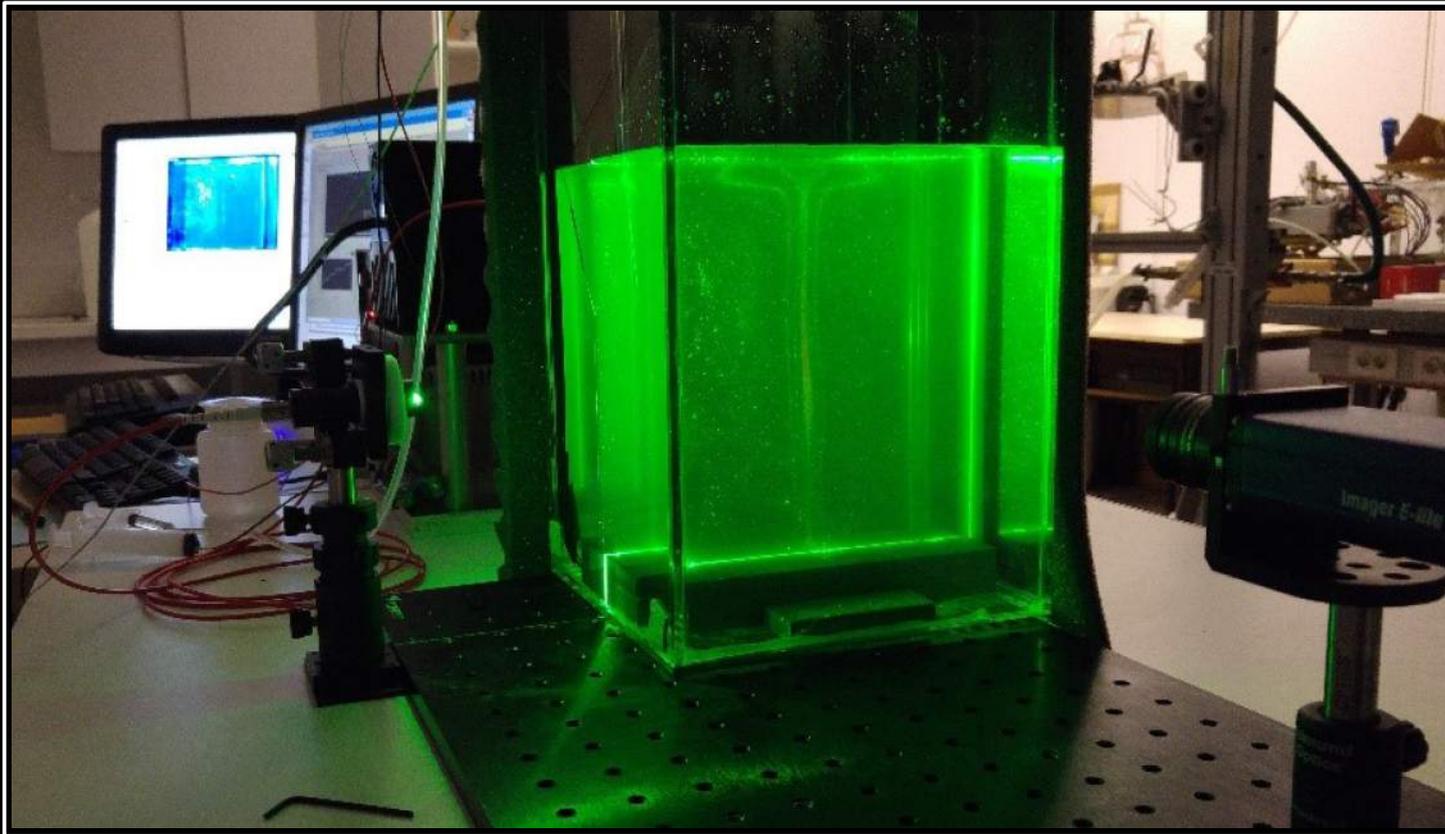
Plume axis



Exploring the effect of compositional buoyancy

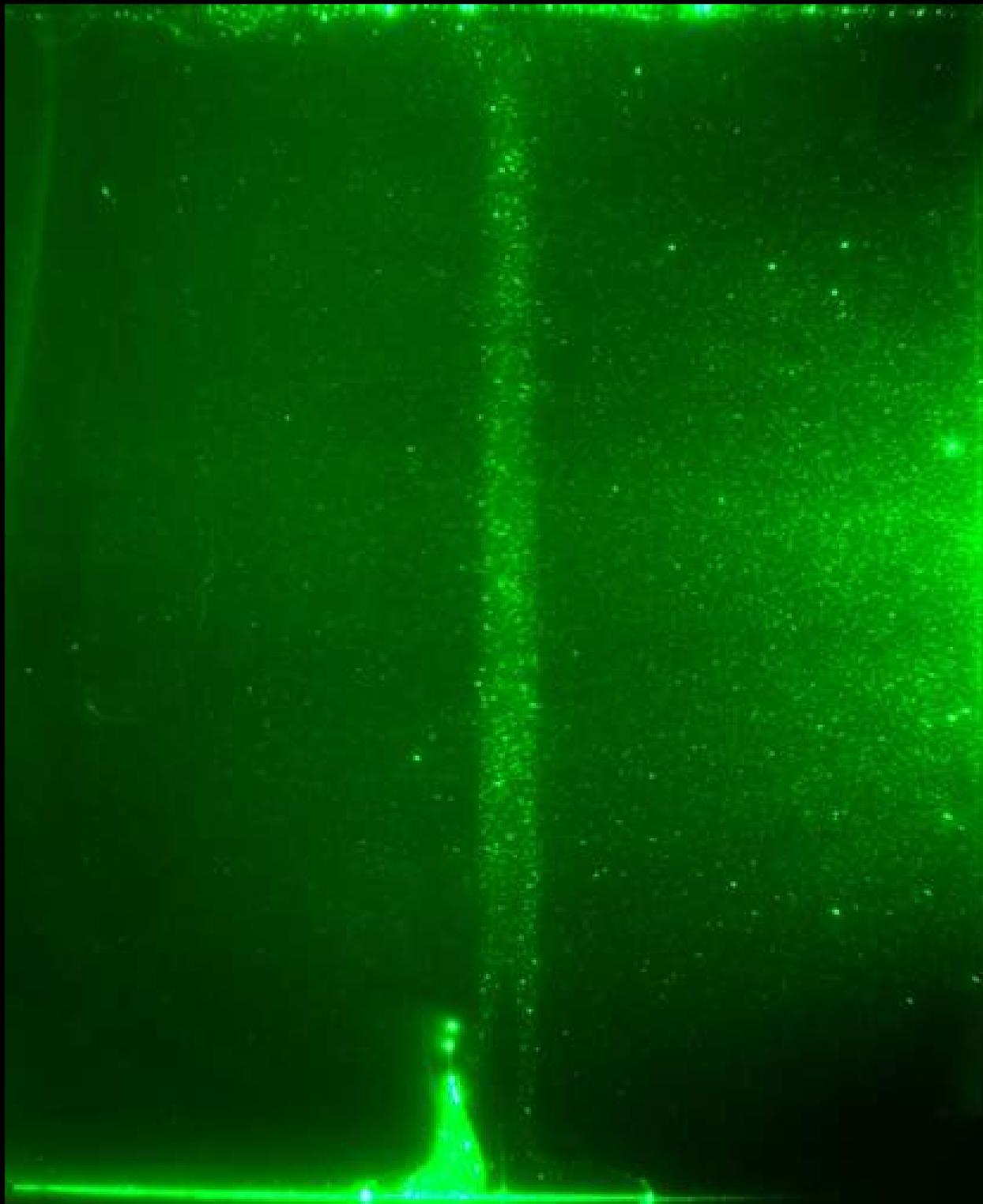
The buoyancy ratio $B = \Delta\rho_{ch} / \Delta\rho_{th}$

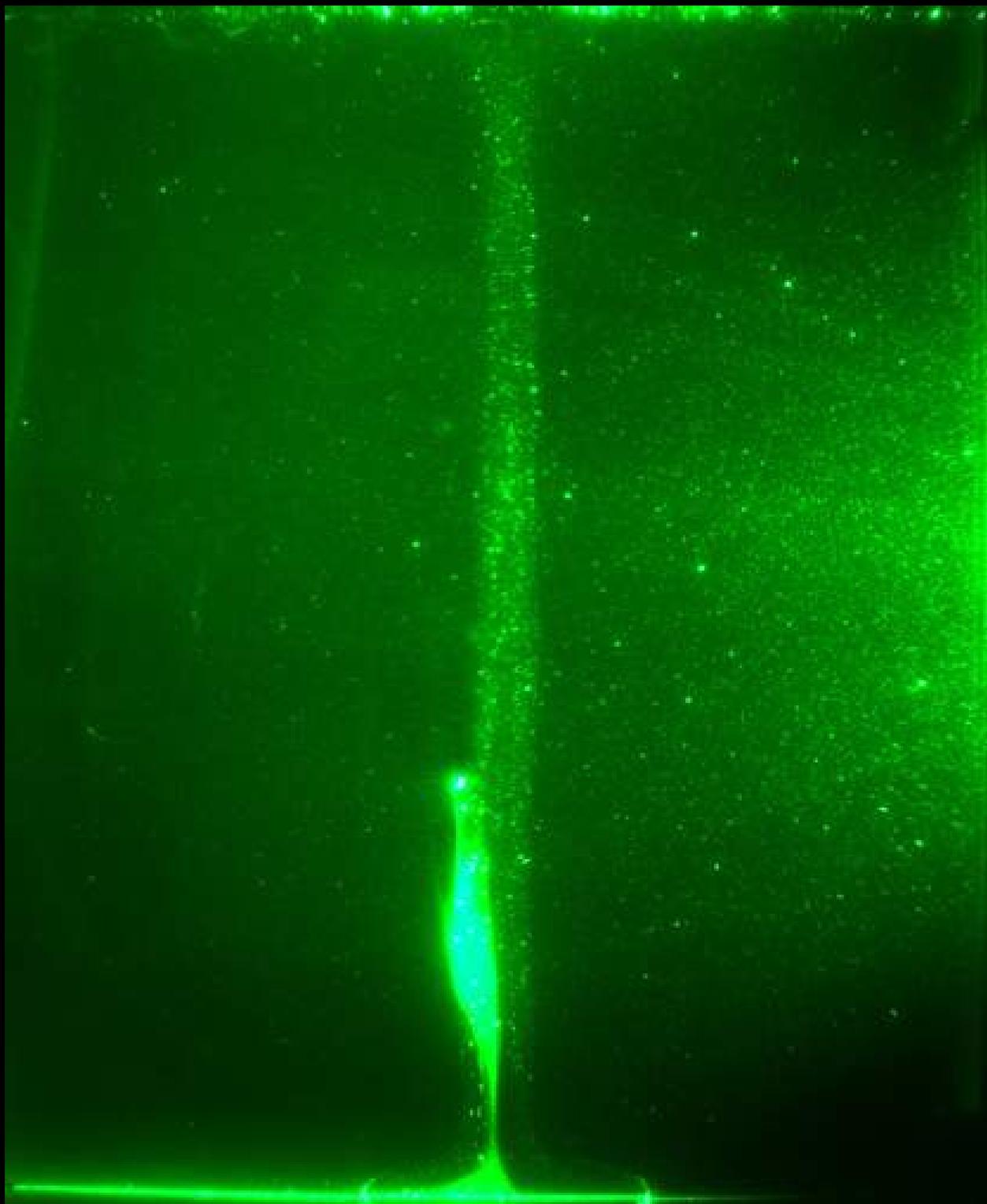


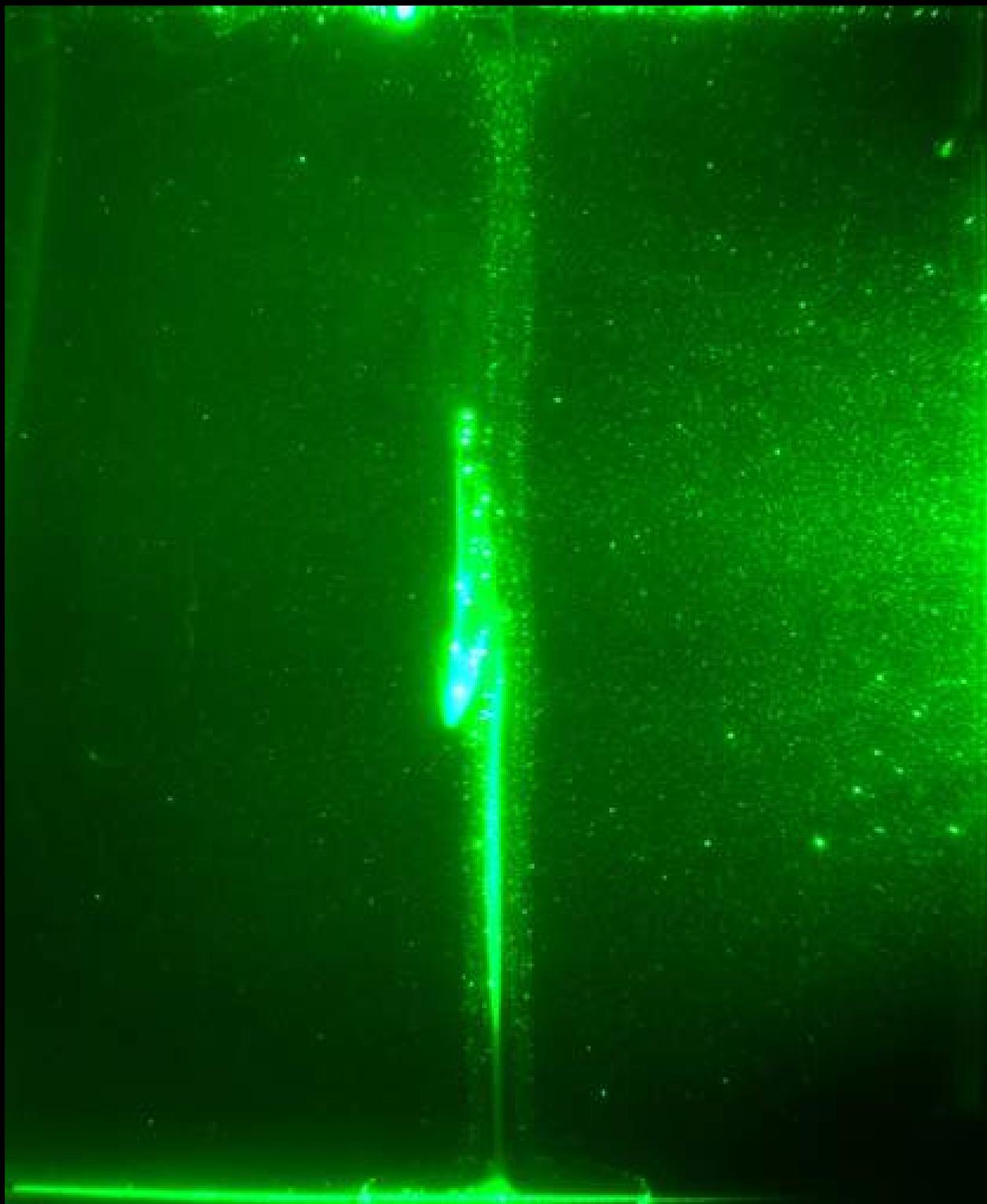


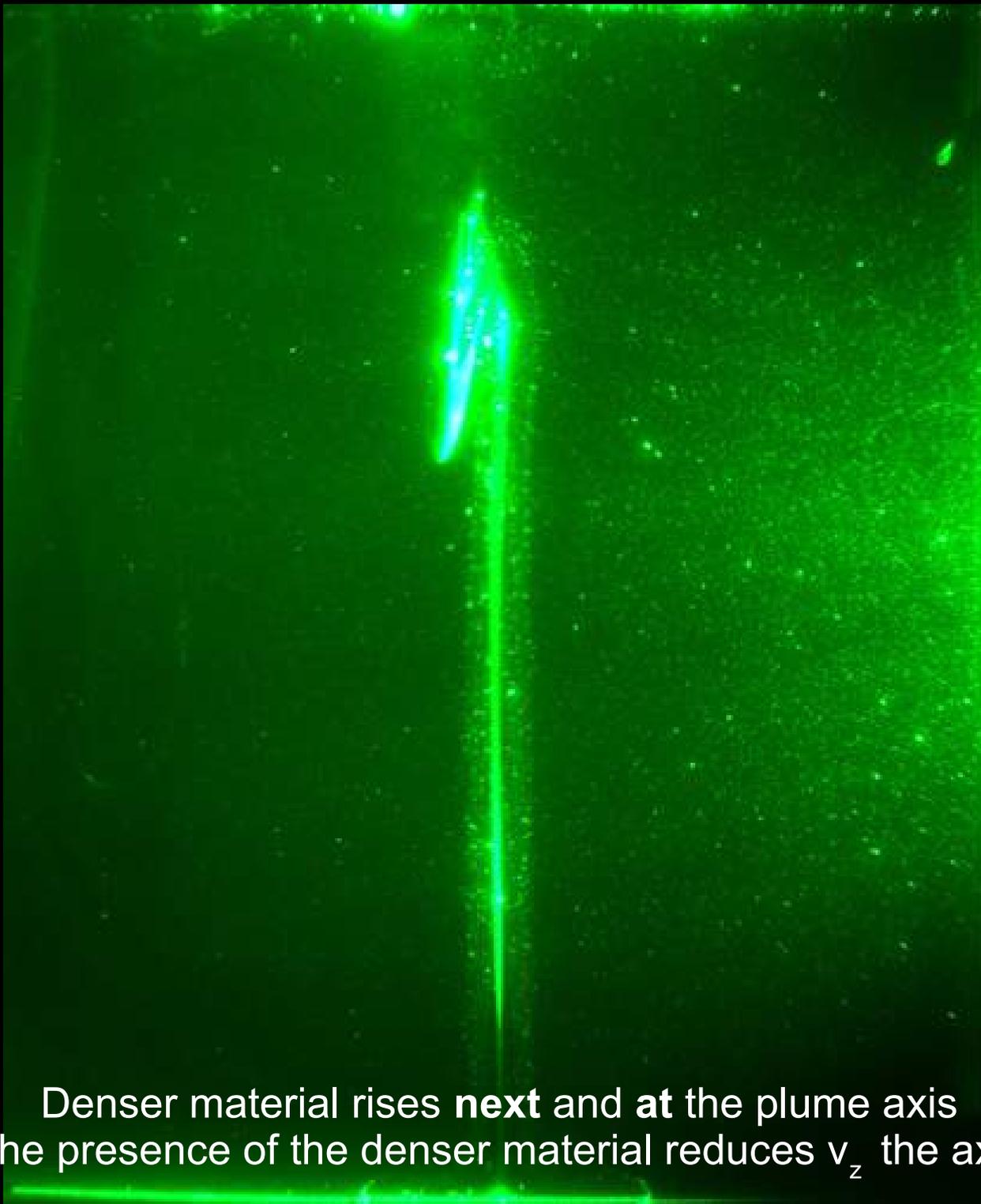
- Experimental tank filled with diluted Glucose syrup. $10^5 < Ra < 10^6$
- We inject chemically denser material at one side of the plume.
- We vary : the injected volume ($0.2-0.5 \cdot 10^{-3}$ l),
the distances from the plume axis,
the excess compositional density $\Delta\rho_{ch}$ and thus B.
- Thermochromic Liquid Crystals are used to measure temperature,
Particle Image Velocimetry to measure flow velocities.

B = 0.6

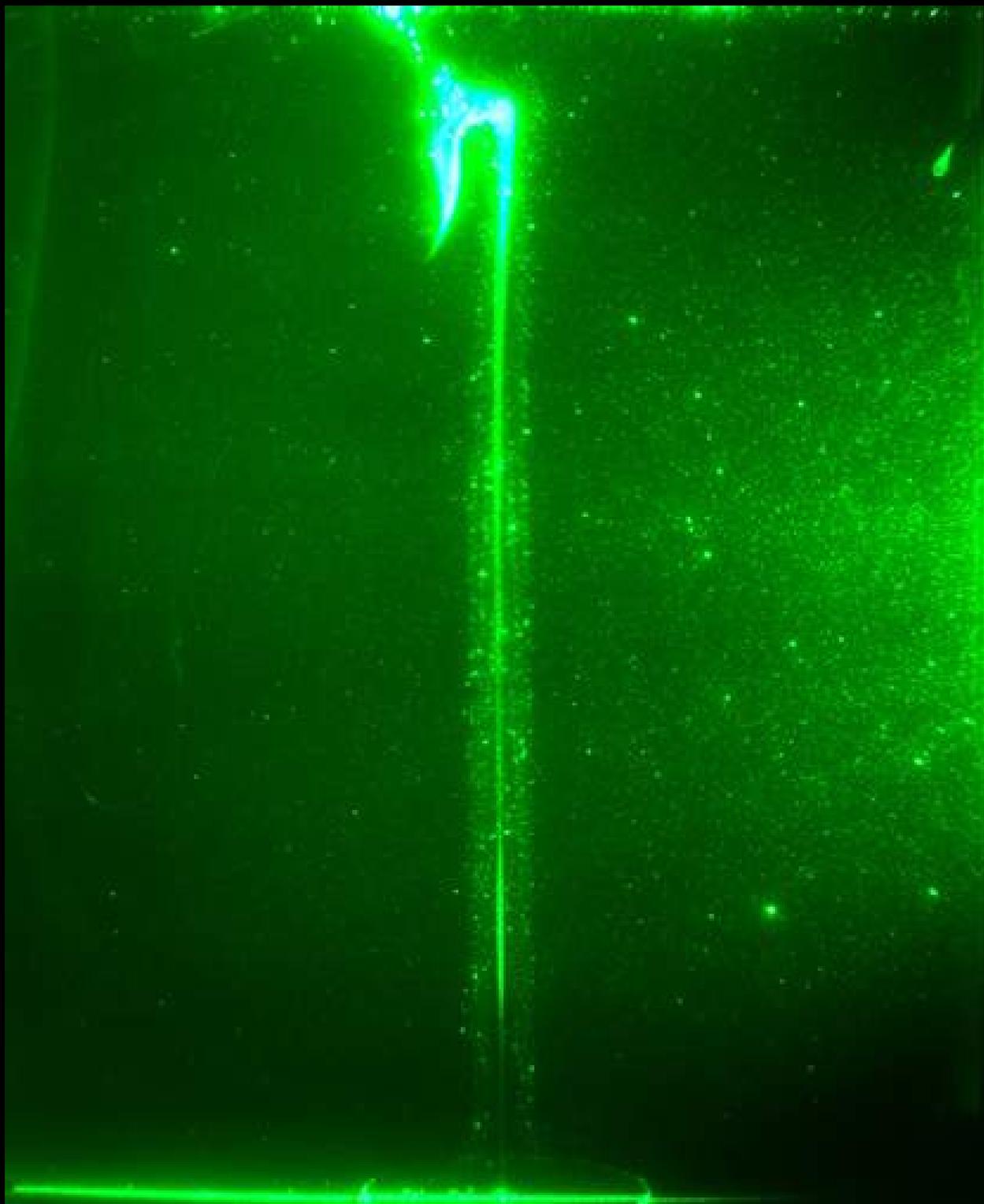


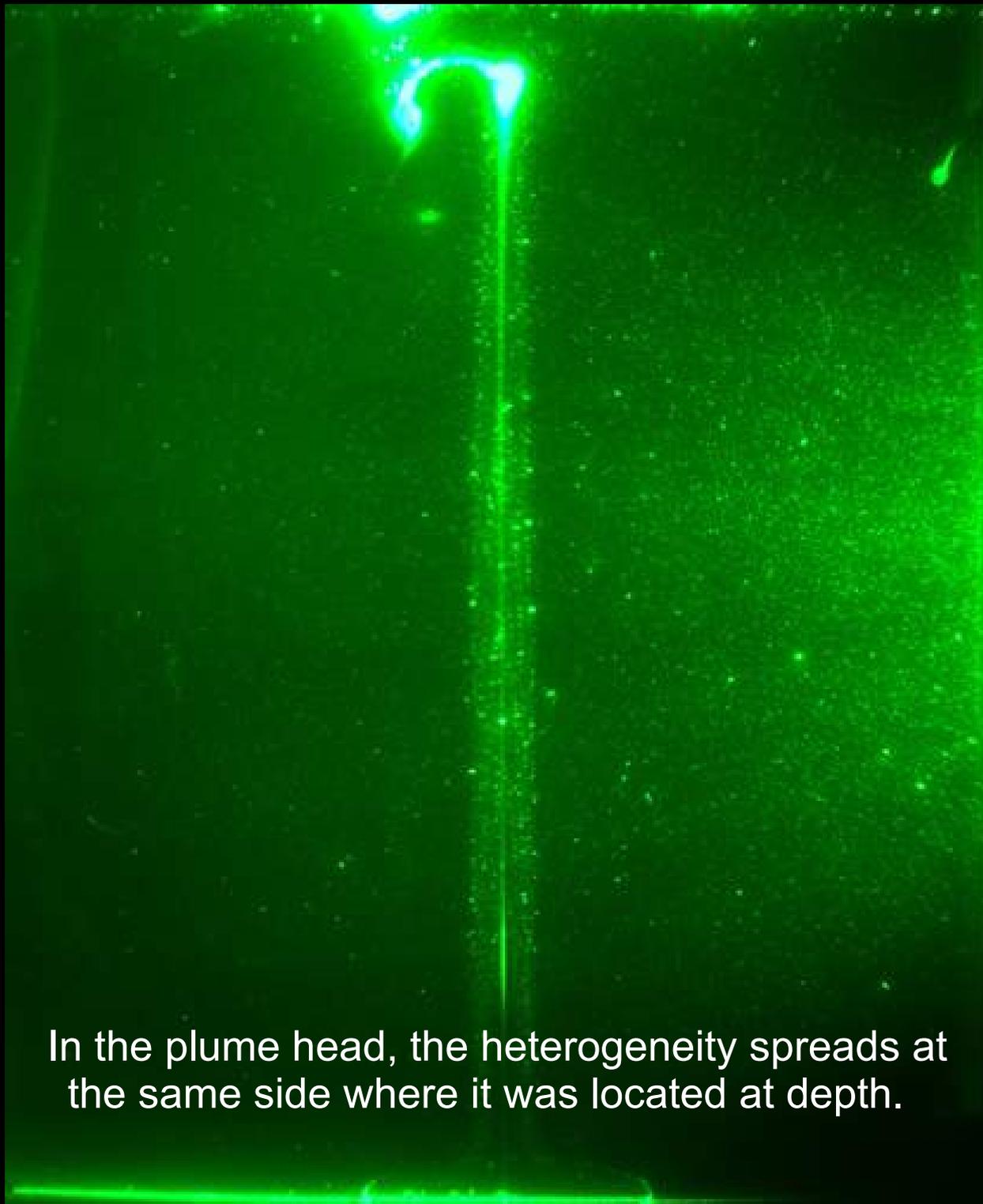






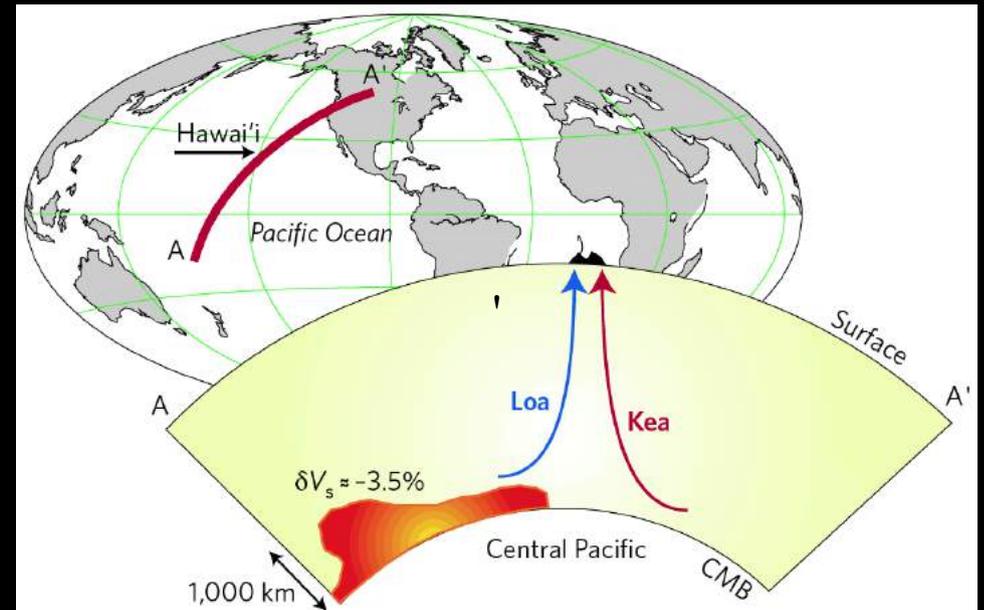
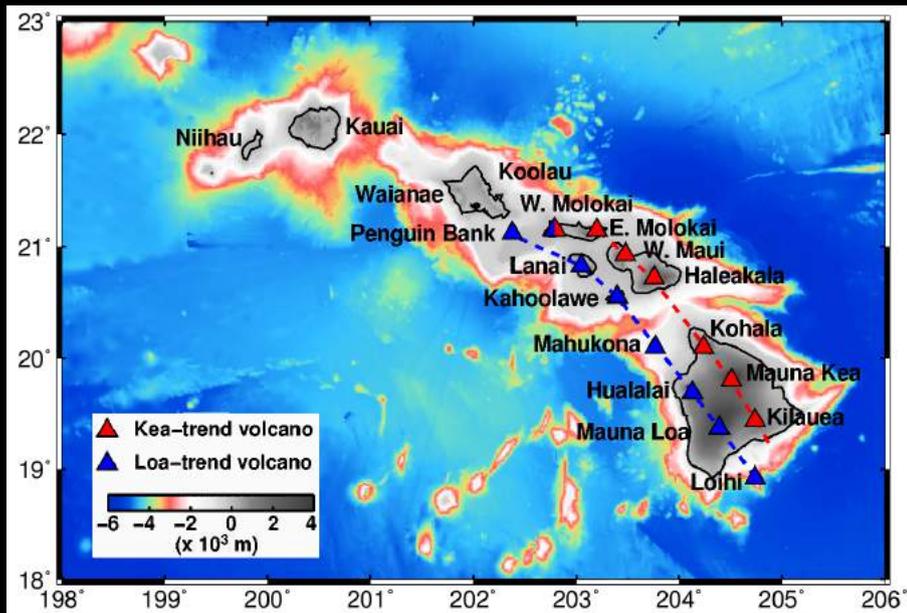
Denser material rises **next** and **at** the plume axis
The presence of the denser material reduces v_z the axis





In the plume head, the heterogeneity spreads at the same side where it was located at depth.

Why do we care about losing -or preserving- the initial zonation of deep heterogeneities?

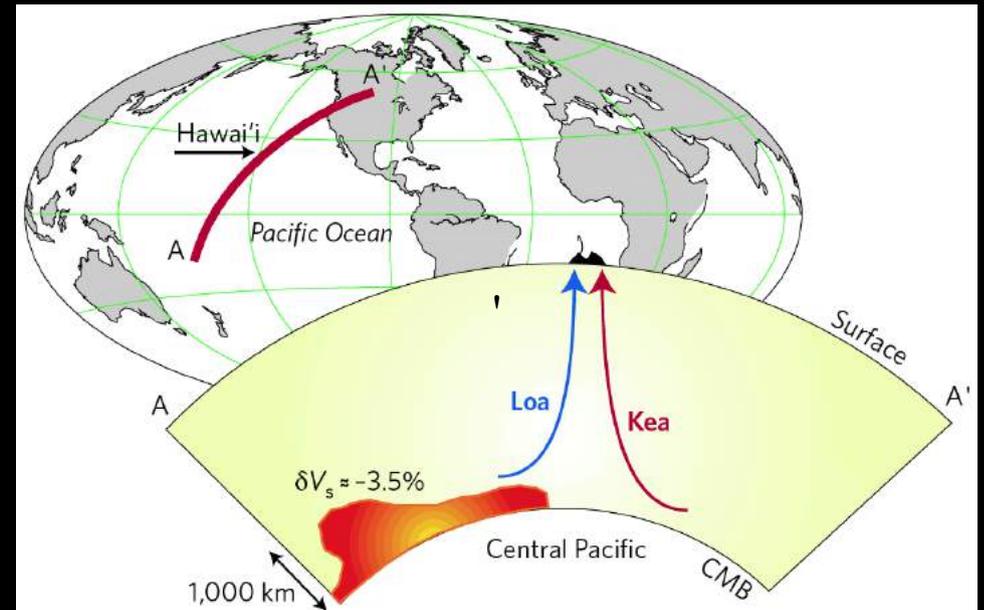
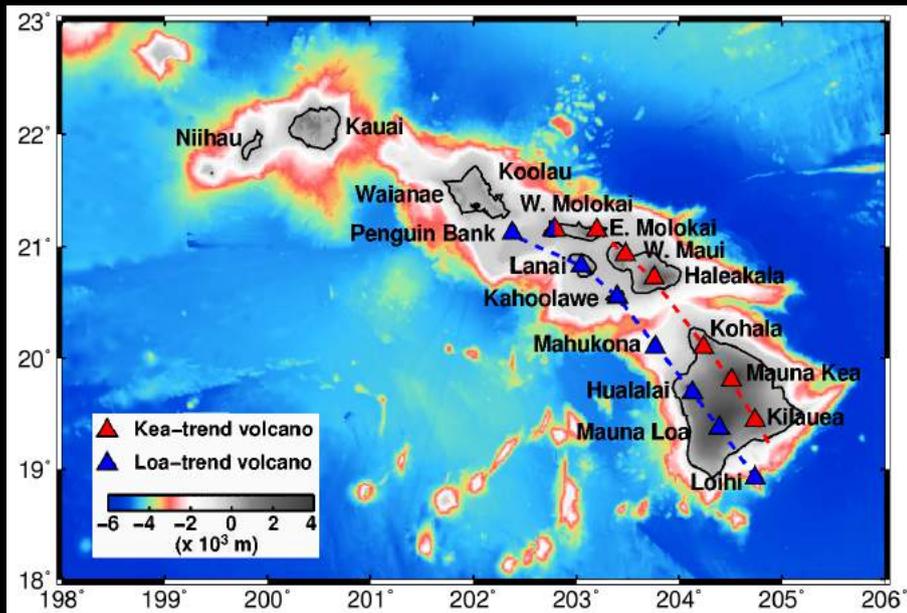


Weis et al., 2011

Spatial variations recorded in the geochemistry of hotspot lavas can reflect the heterogeneous composition of their deep-mantle source.

For passive heterogeneities (i.e., no density or rheological variations) plume flow does preserve the deep zonation.

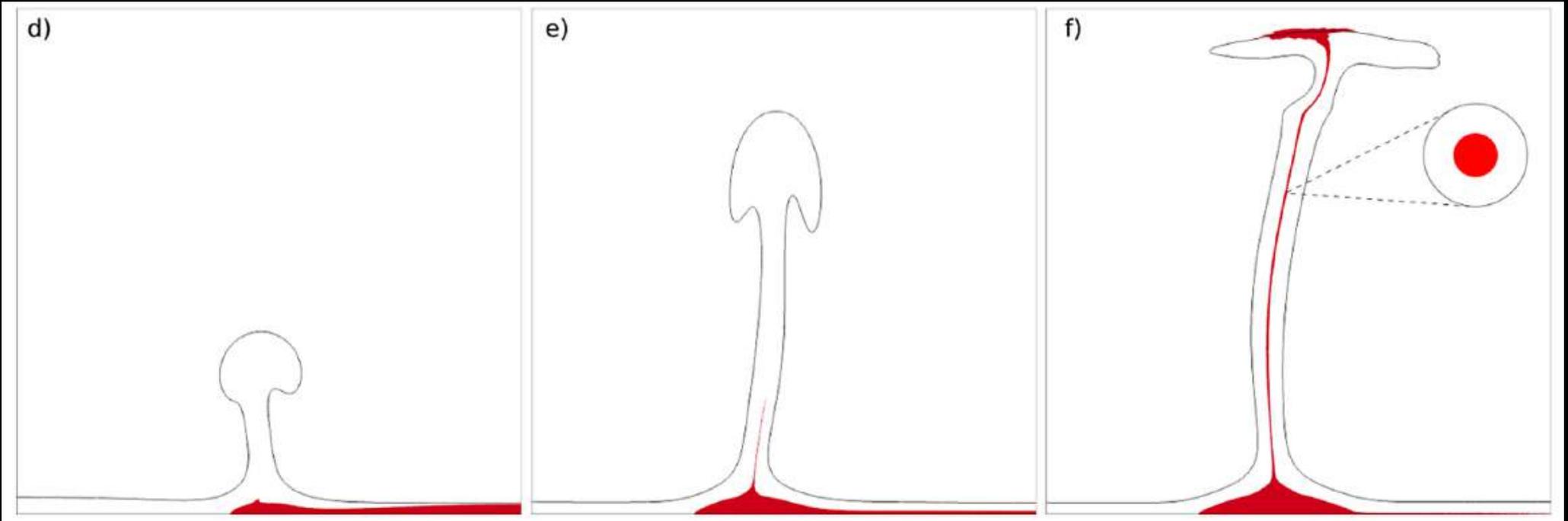
Why do we care about loosing -or preserving- the initial zonation of deep heterogeneities?



Weis et al., 2011

We find that the initial zonation is preserved if the finite-size heterogeneity is more viscous ($1 < \lambda < 20$) and with buoyancy ratio up to 0.8

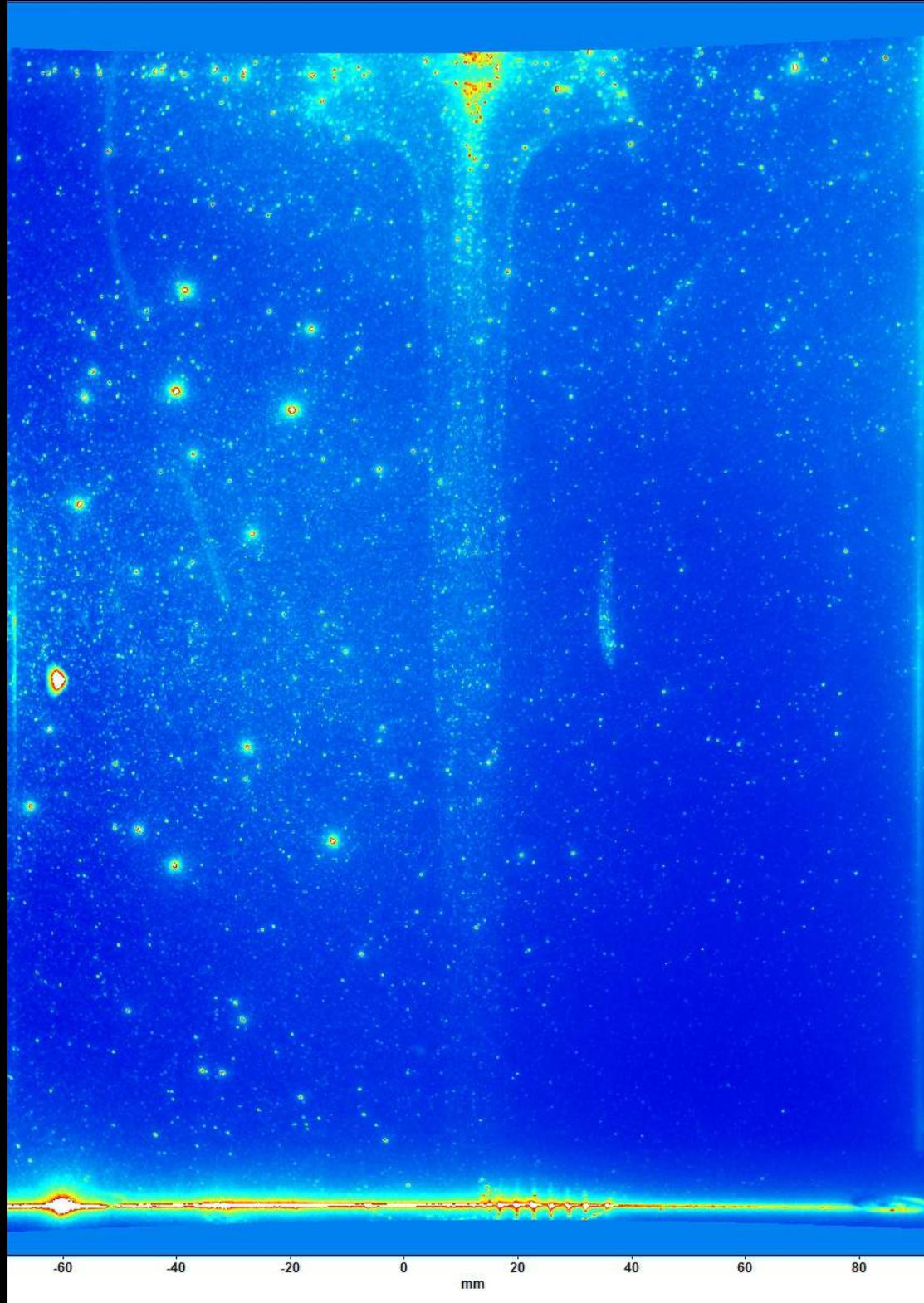
For buoyancy ratio $B > 1$, independently of the viscosity ratio, the heterogeneity spreads at the base of the plume. Only a tendril of denser material rises at the plume axis. The initial zonation is lost.



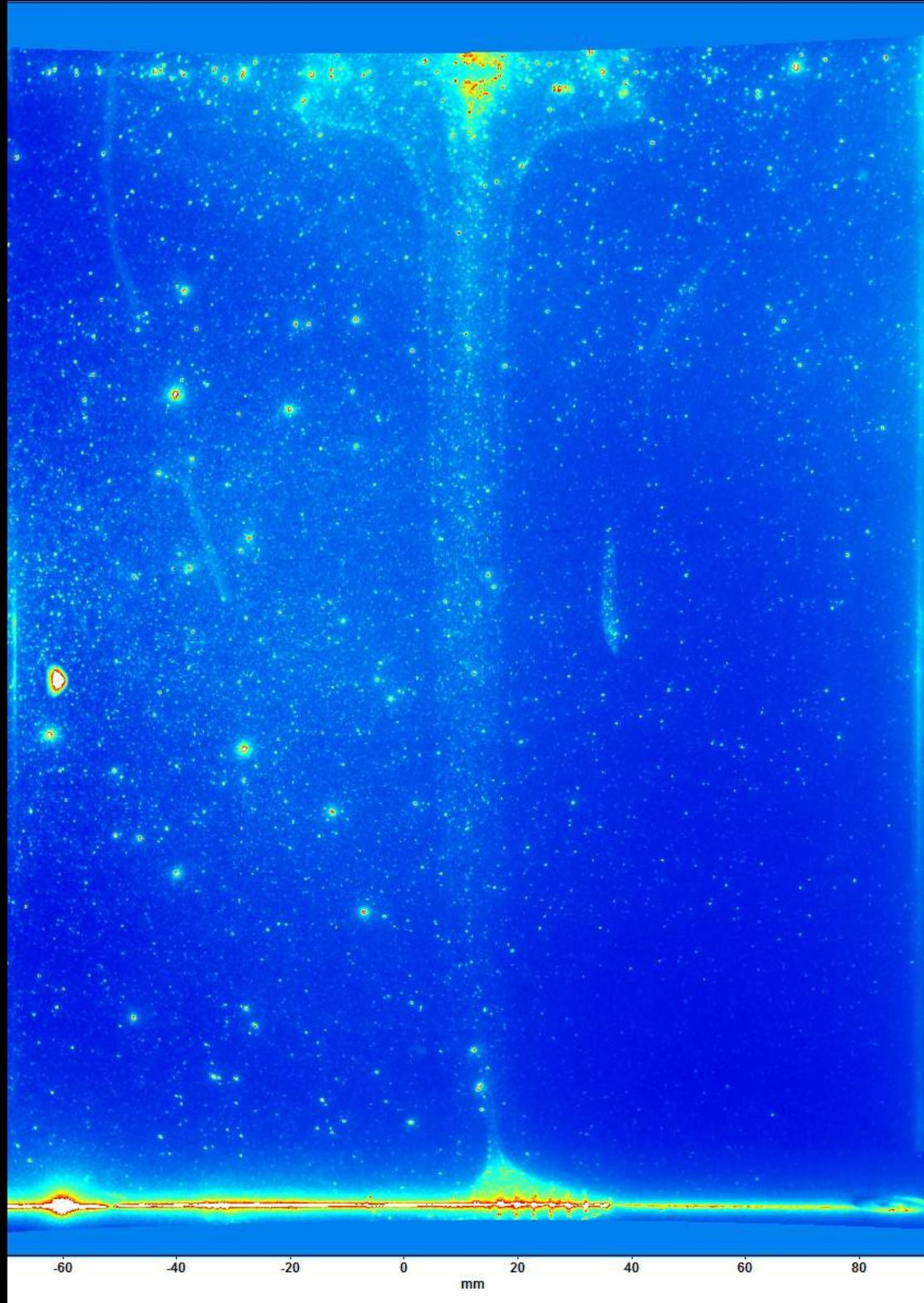
Numerical simulations by Jones et al., 2016 model an asymmetric distribution of denser material (red) at the base of a plume and find that the basal zonation is lost.

Experiments by
A. Limare and
T. Duvernay

0030

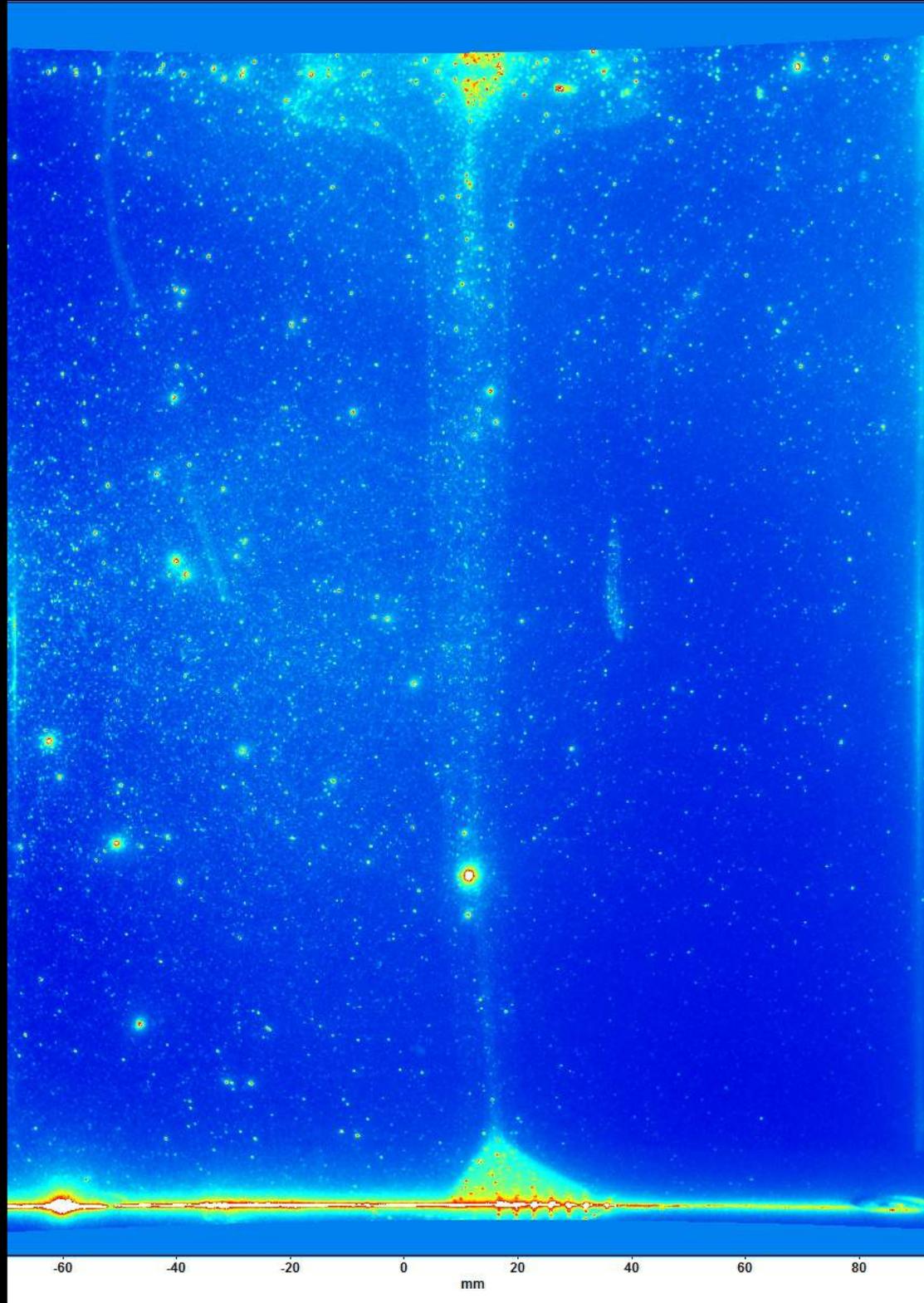


As soon as the
thermal plume is
established,
we inject (over
half of its base)
a compositionally
denser fluid



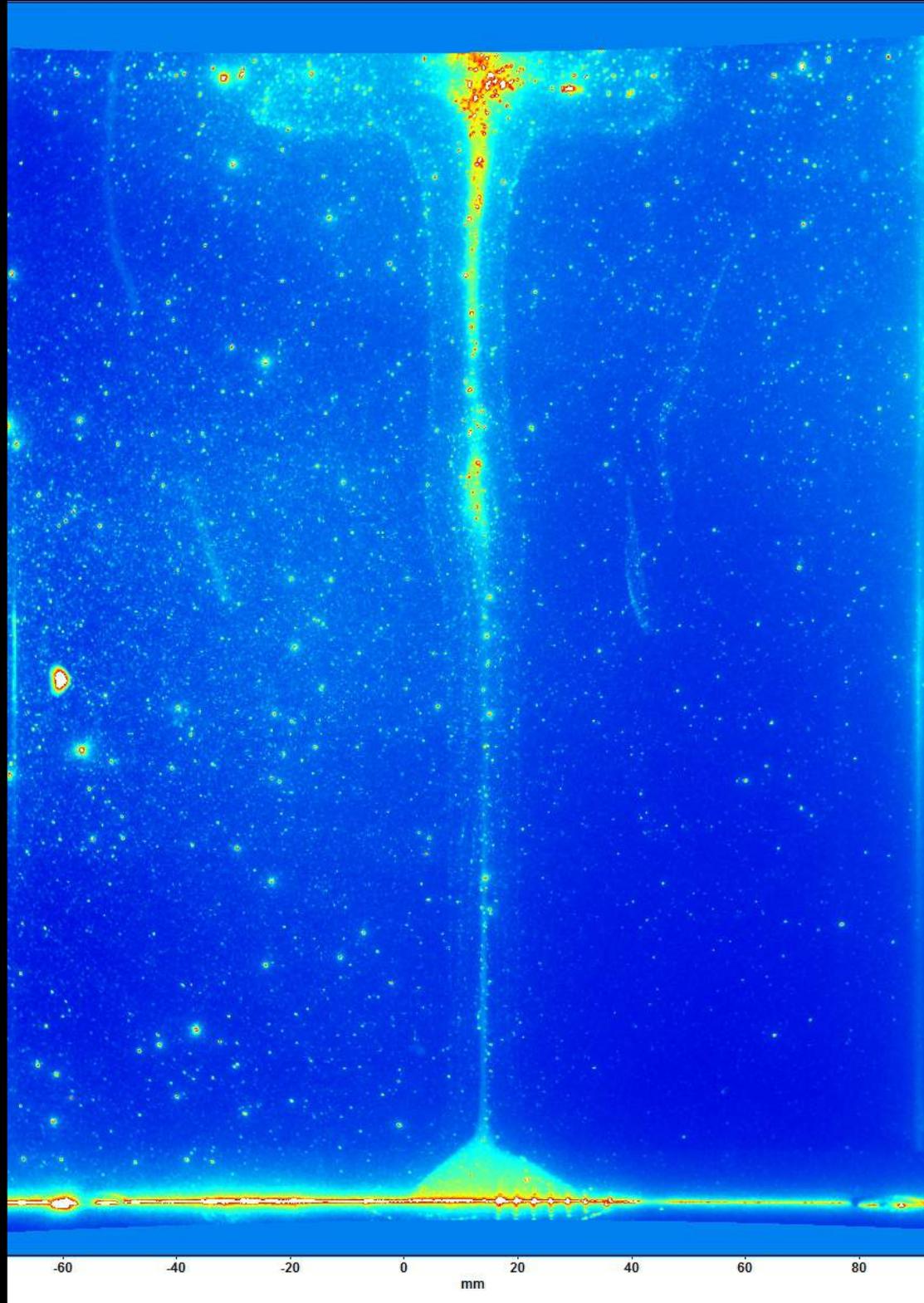
The buoyancy number is $B=1.2$

$$B = \frac{\Delta\rho_{ch}}{\rho \alpha \Delta T}$$



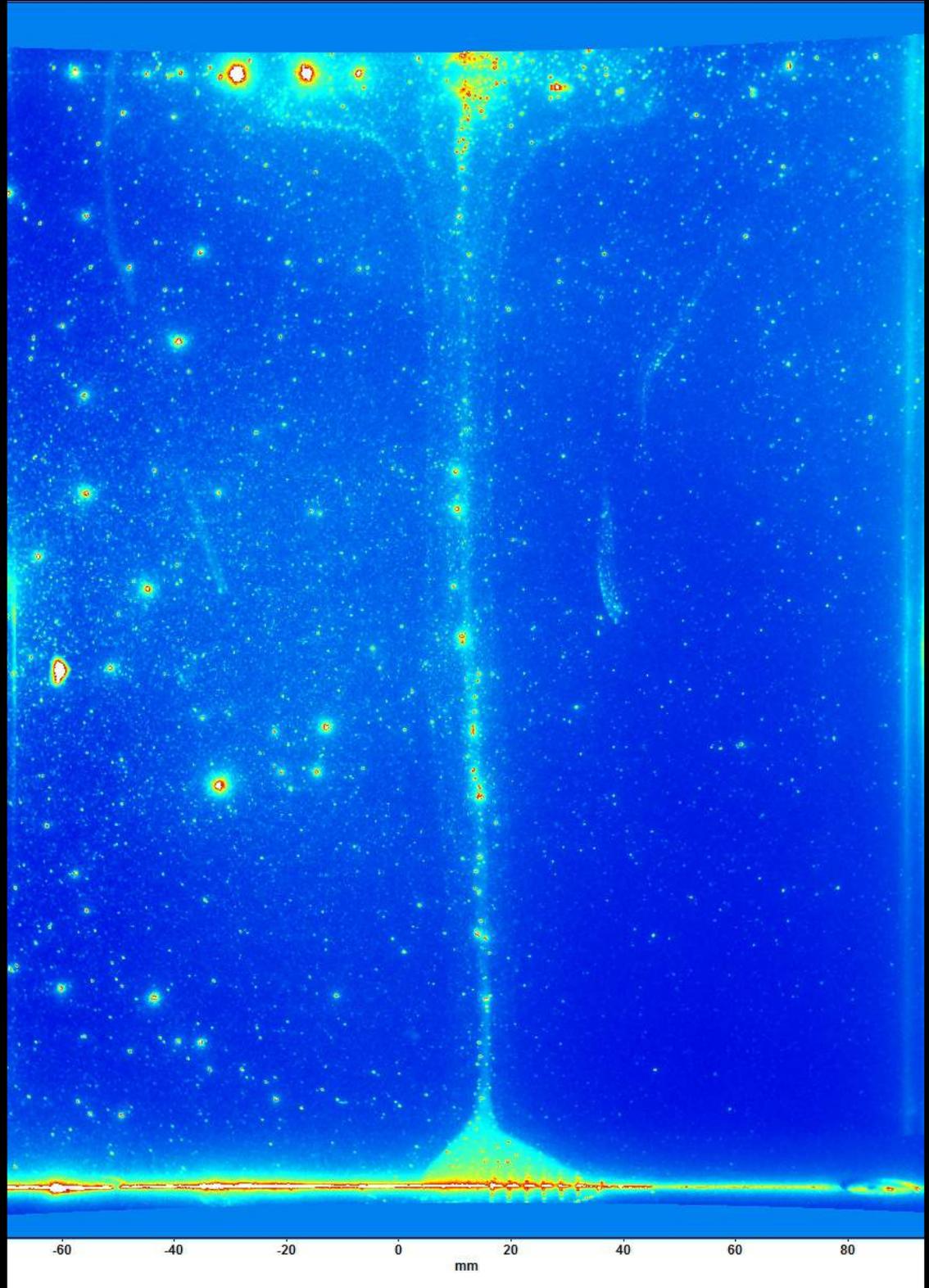
The denser fluid
piles up at the
base of the plume

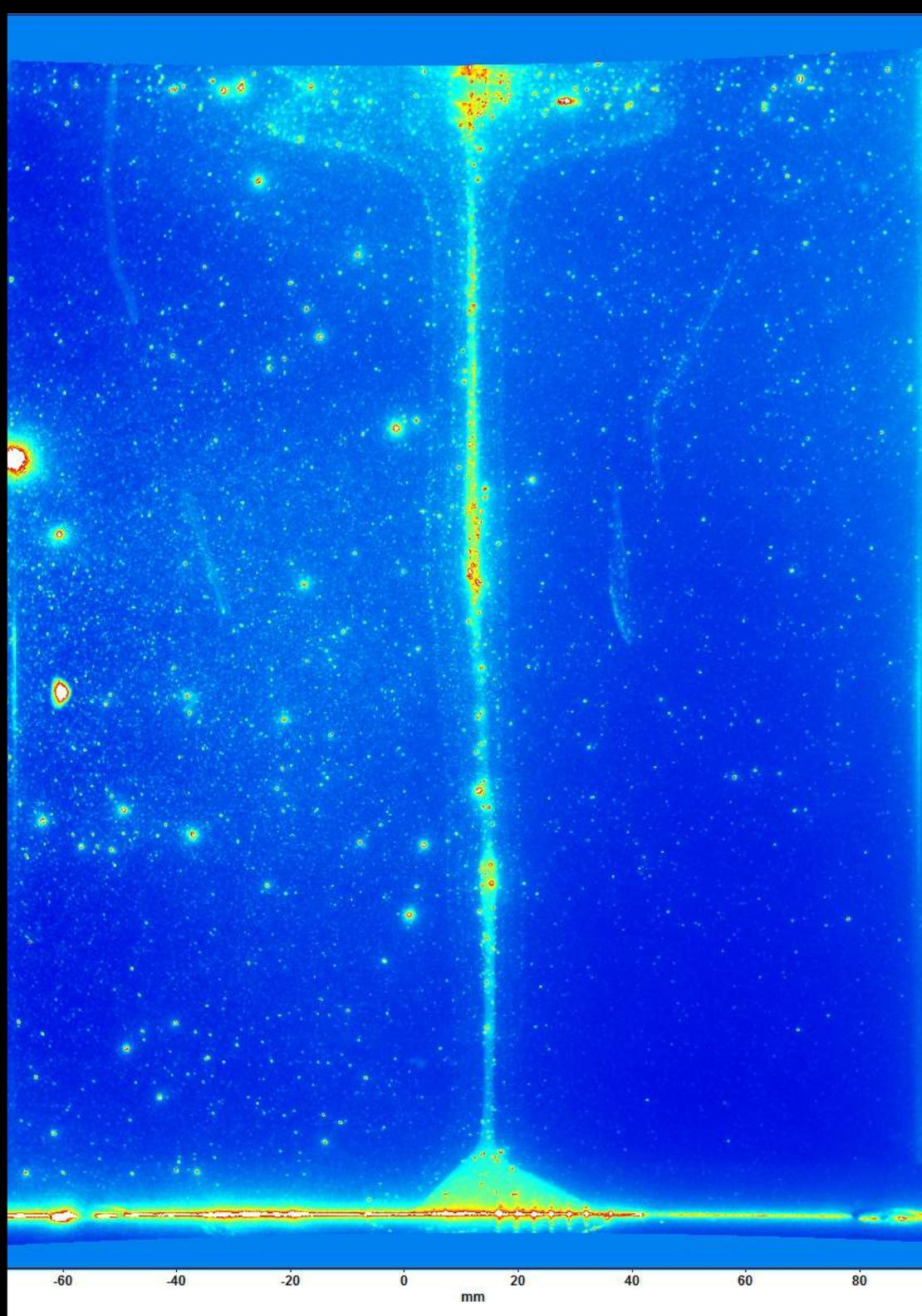
Injected volume:
5ml



The denser fluid rises by viscous coupling at the plume axis

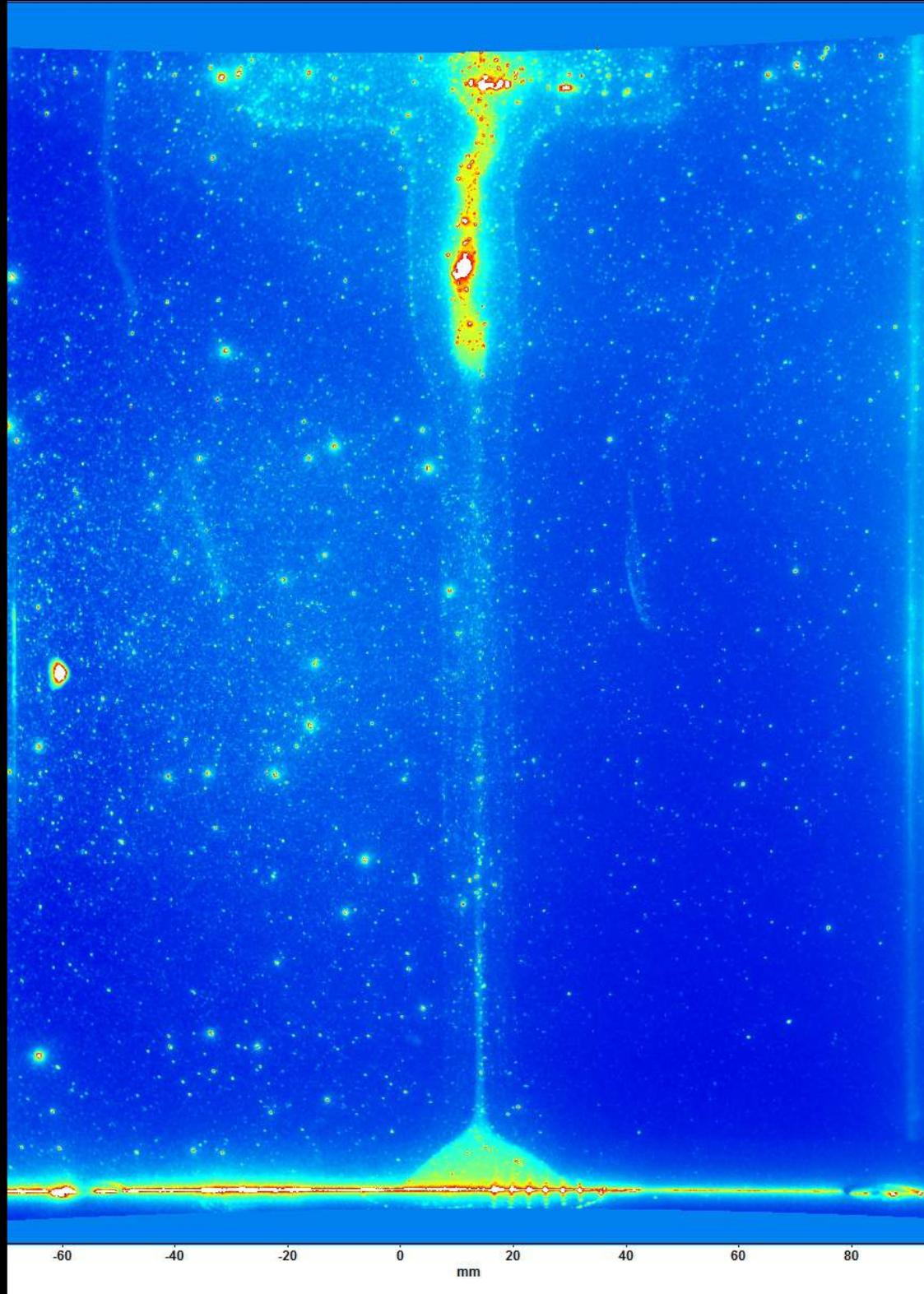
0110

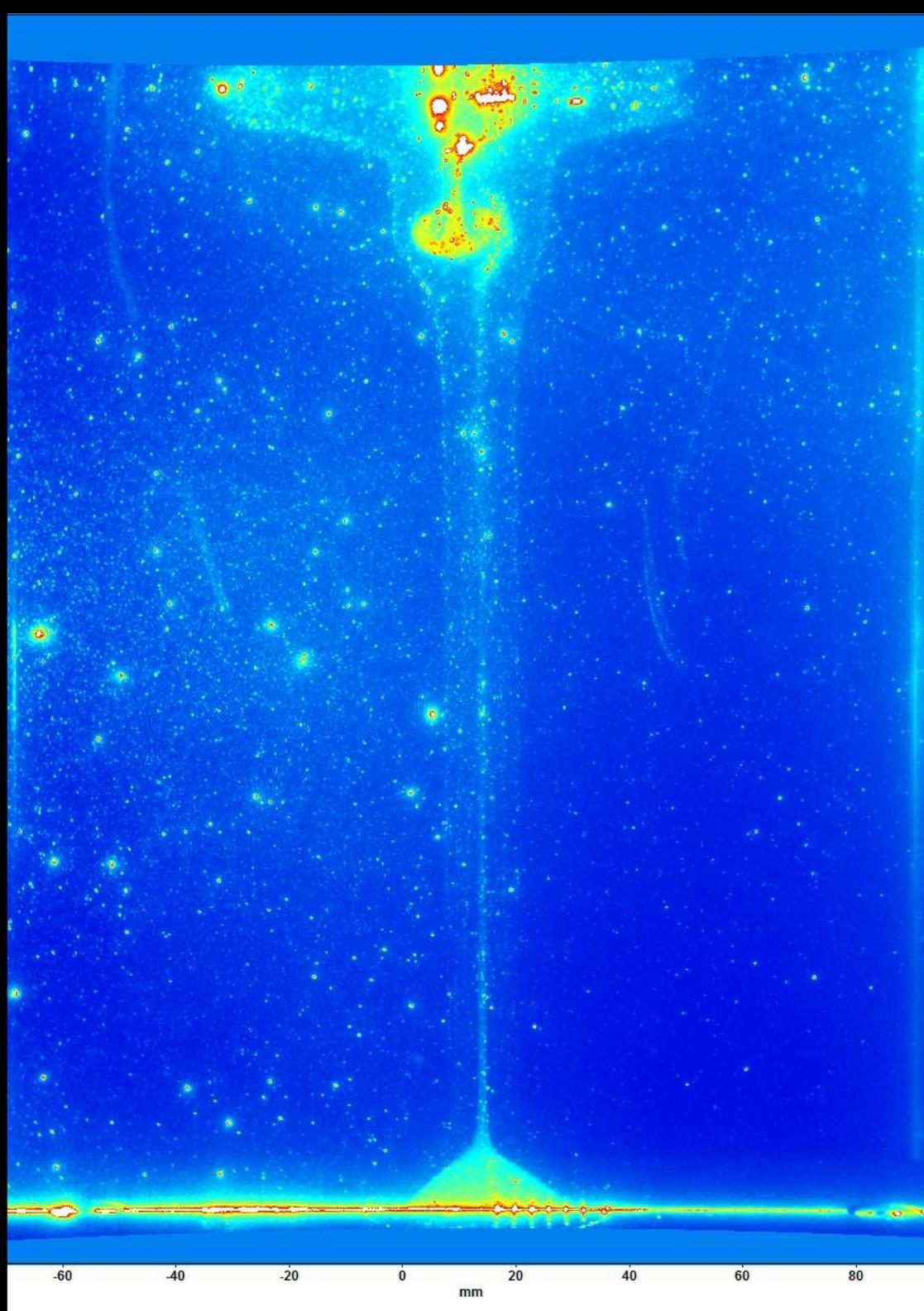




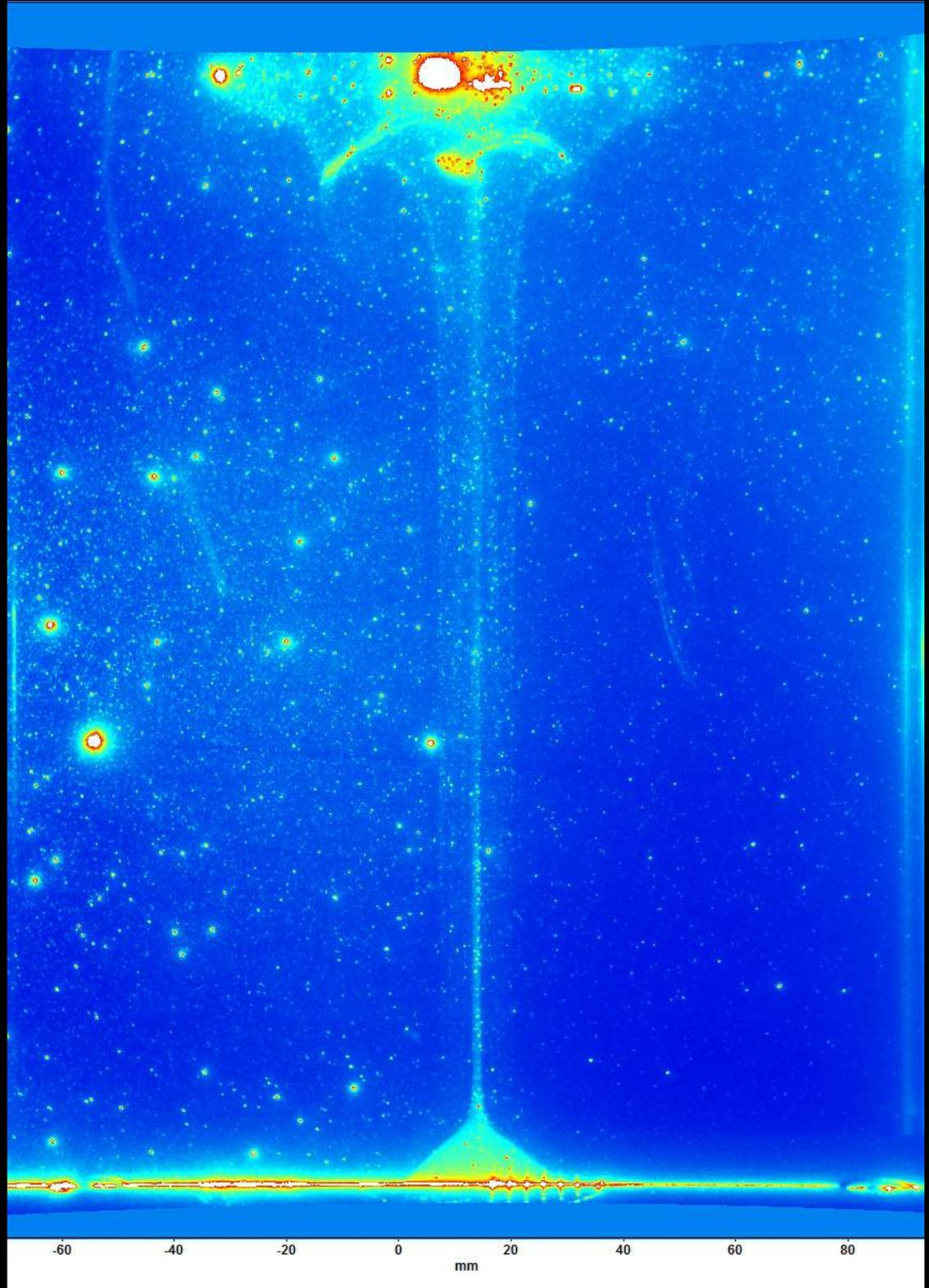
The denser fluid accumulates in the plume head, rather than spreading laterally

0230

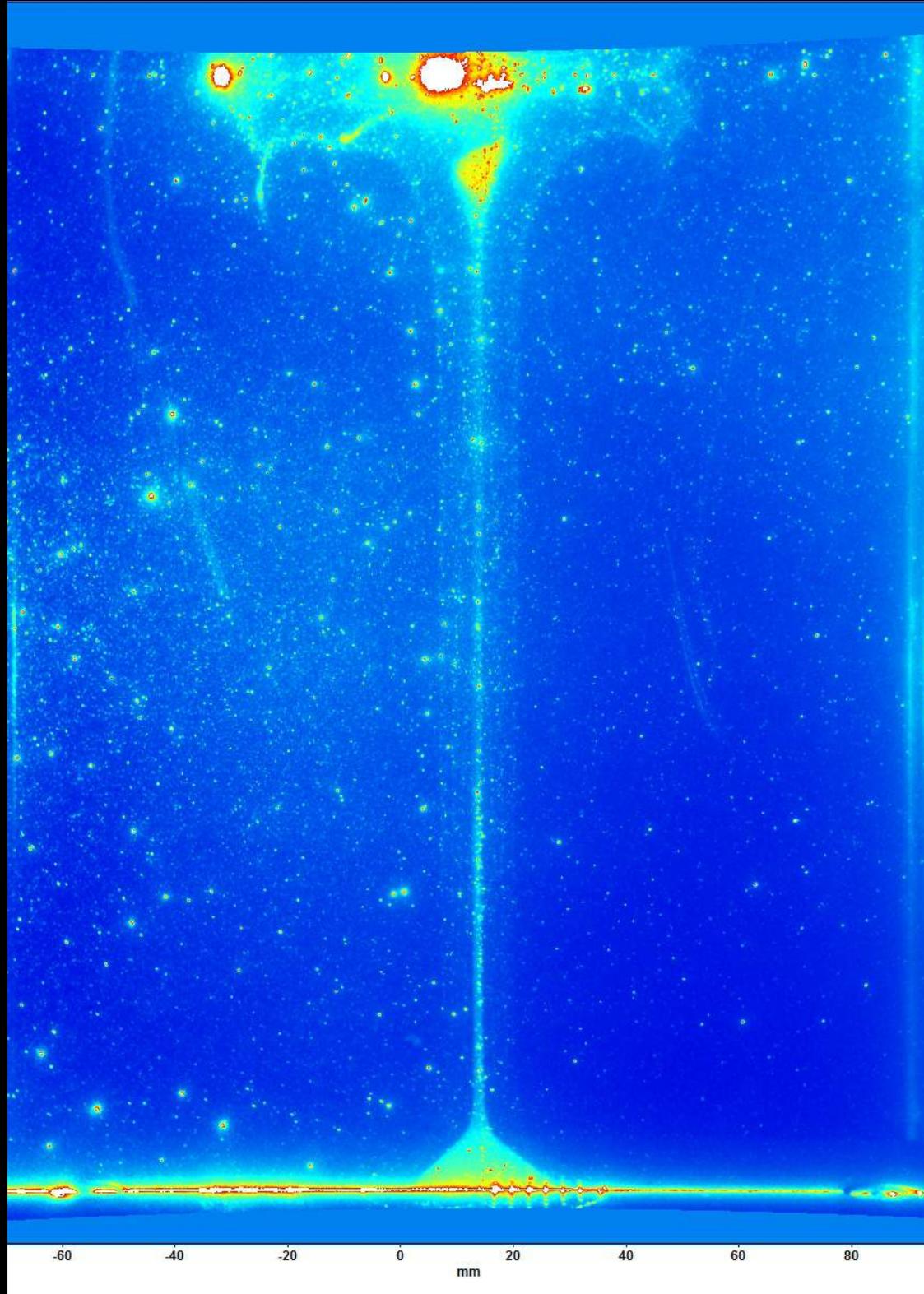


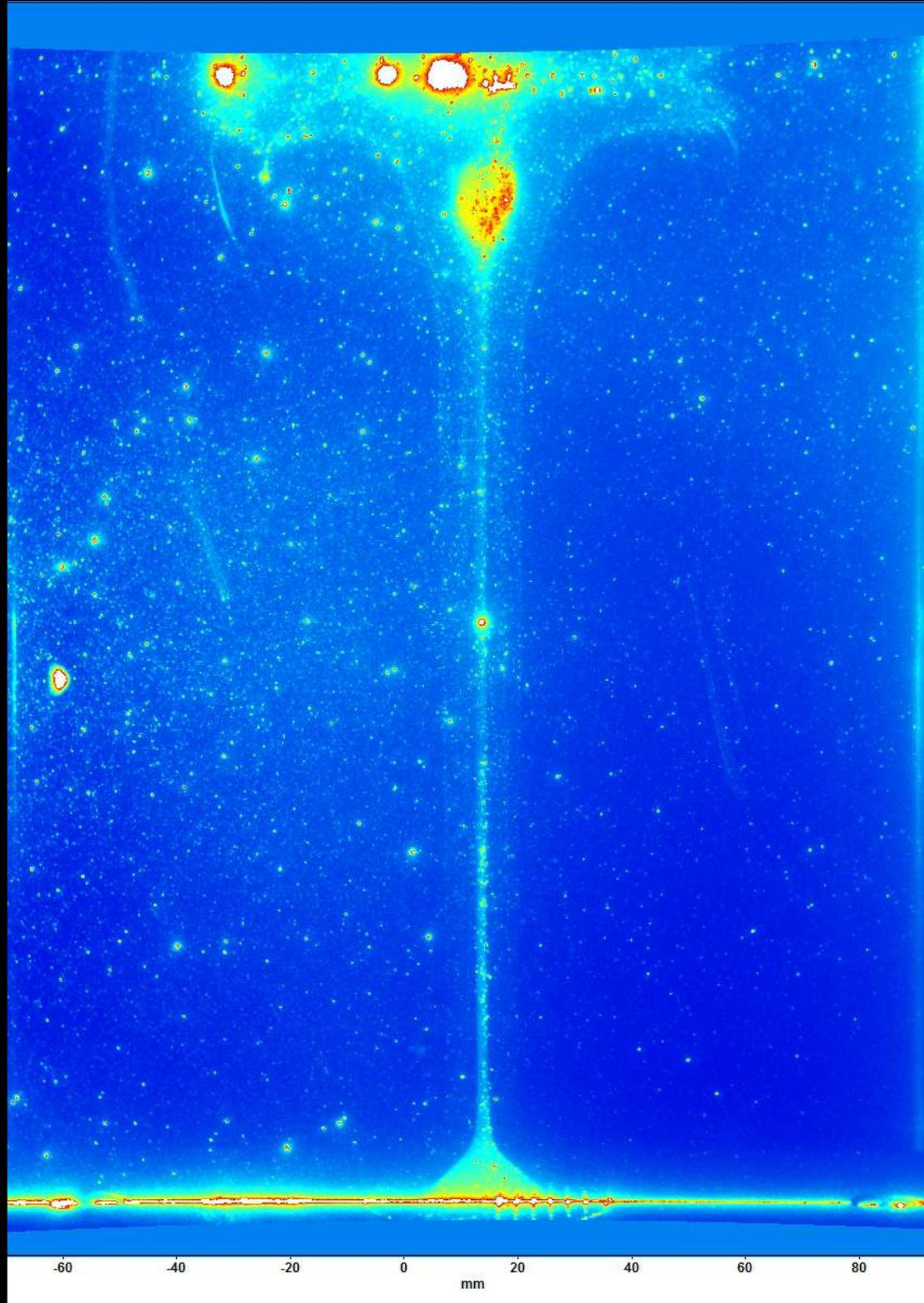


0430



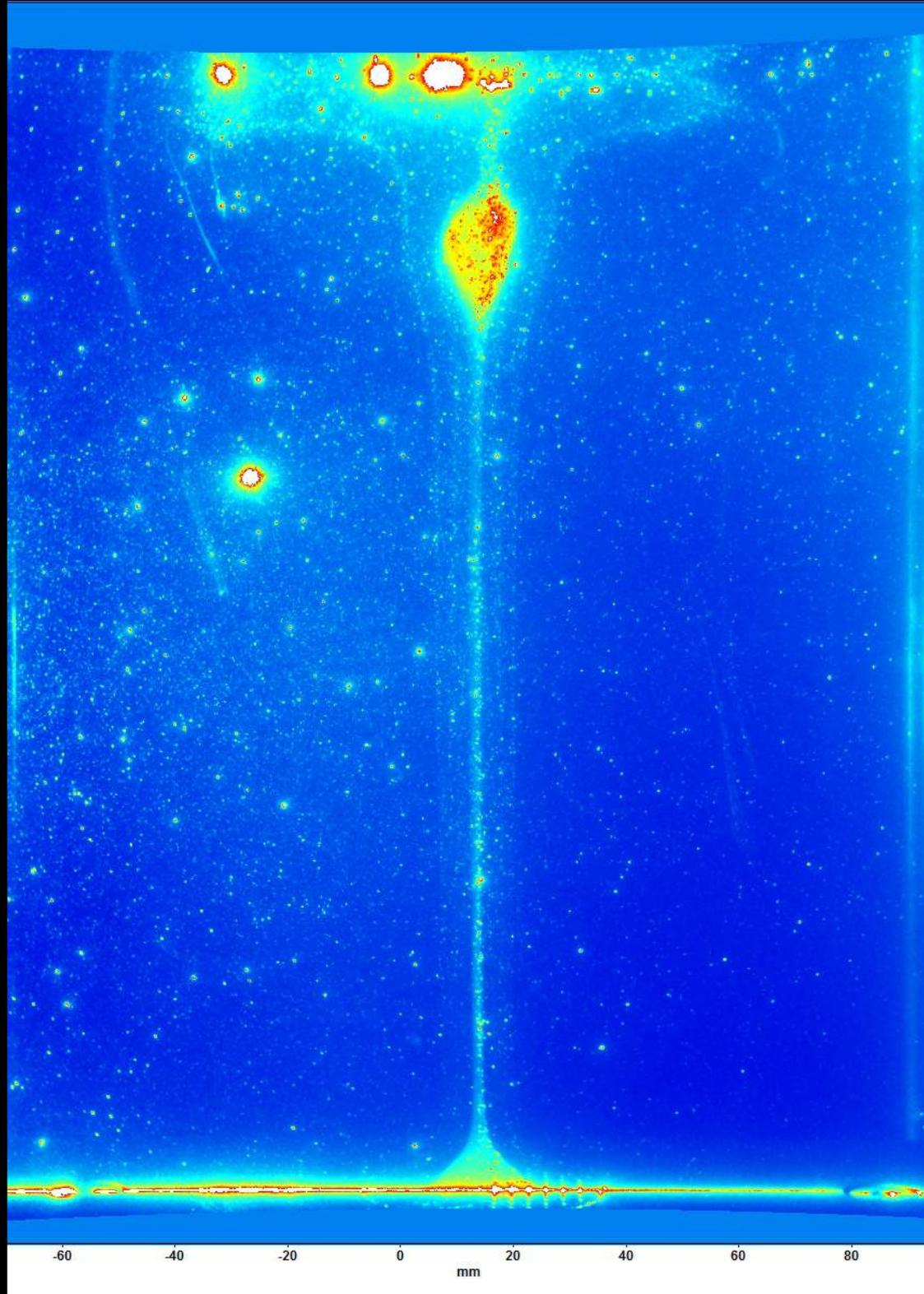
0530



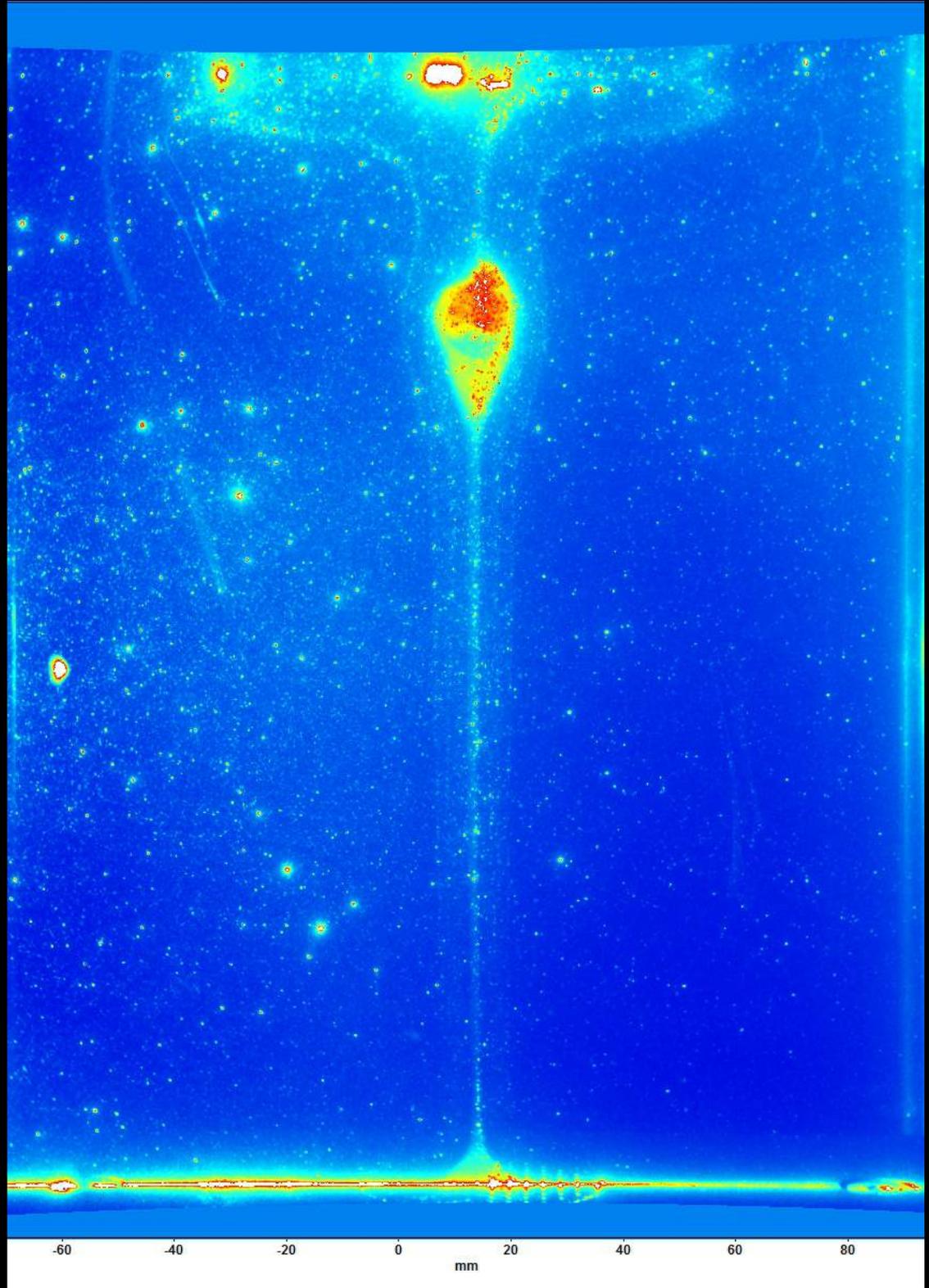


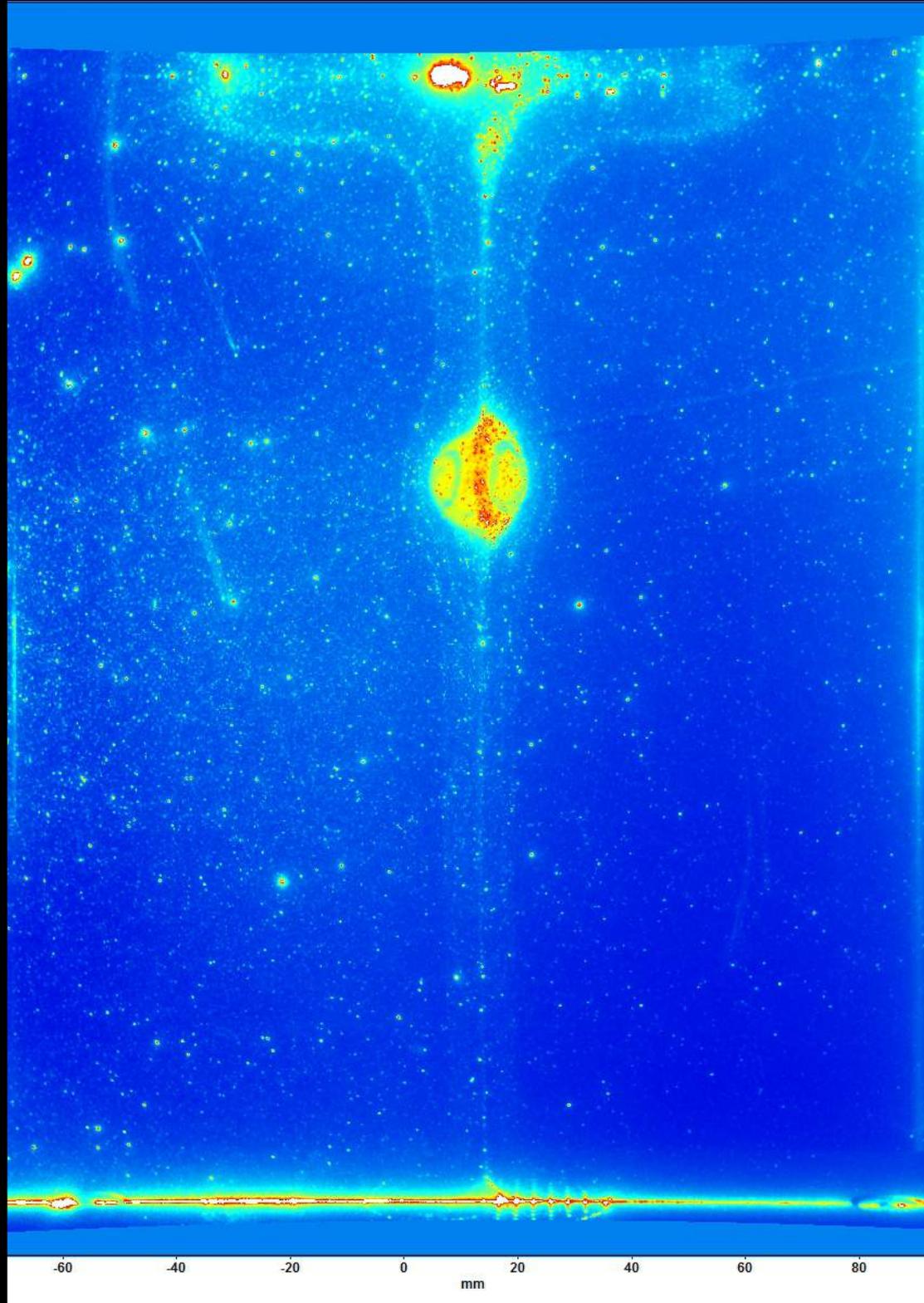
The denser fluid
cools and starts
to sink at the
conduit axis

0730

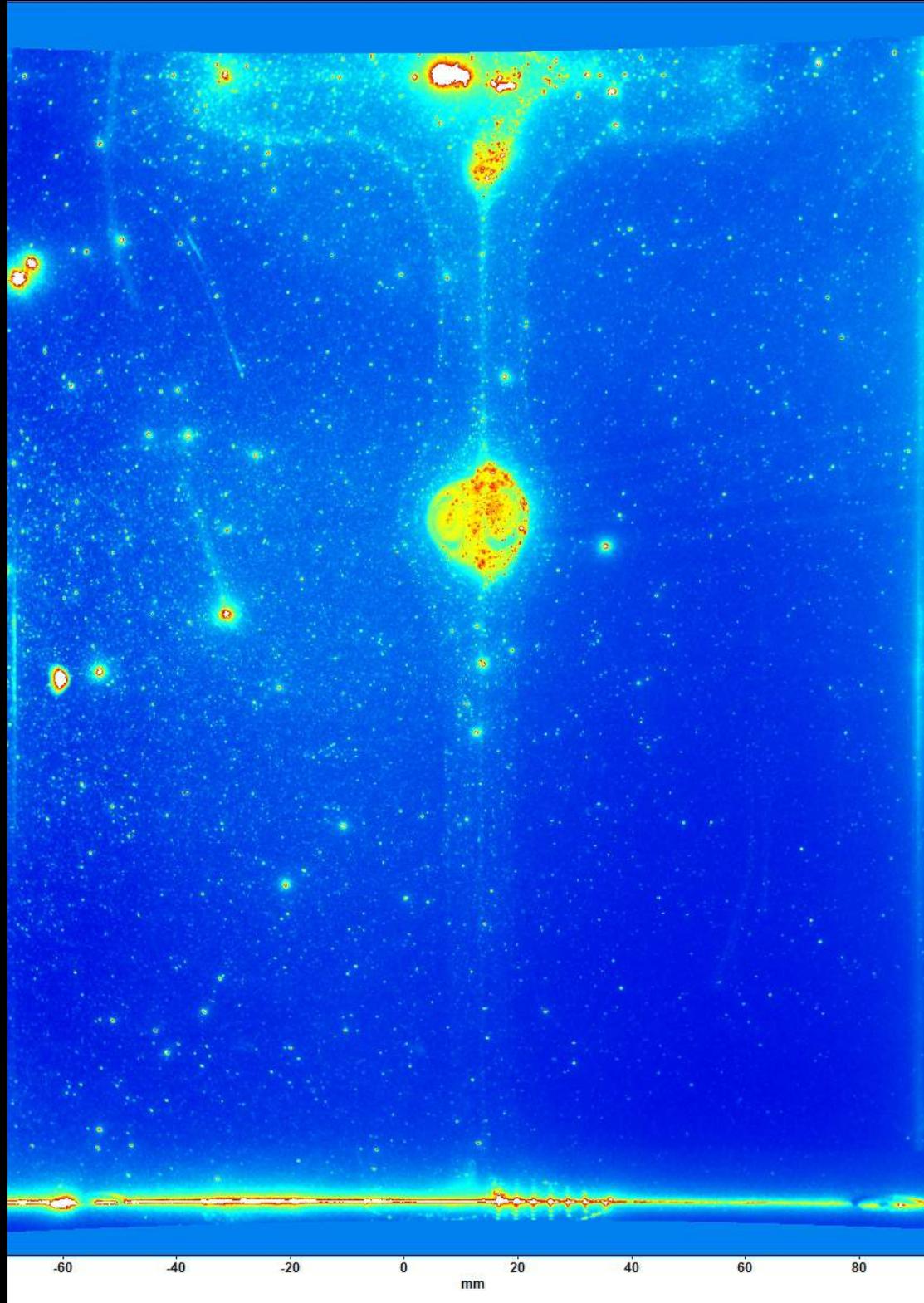


0830



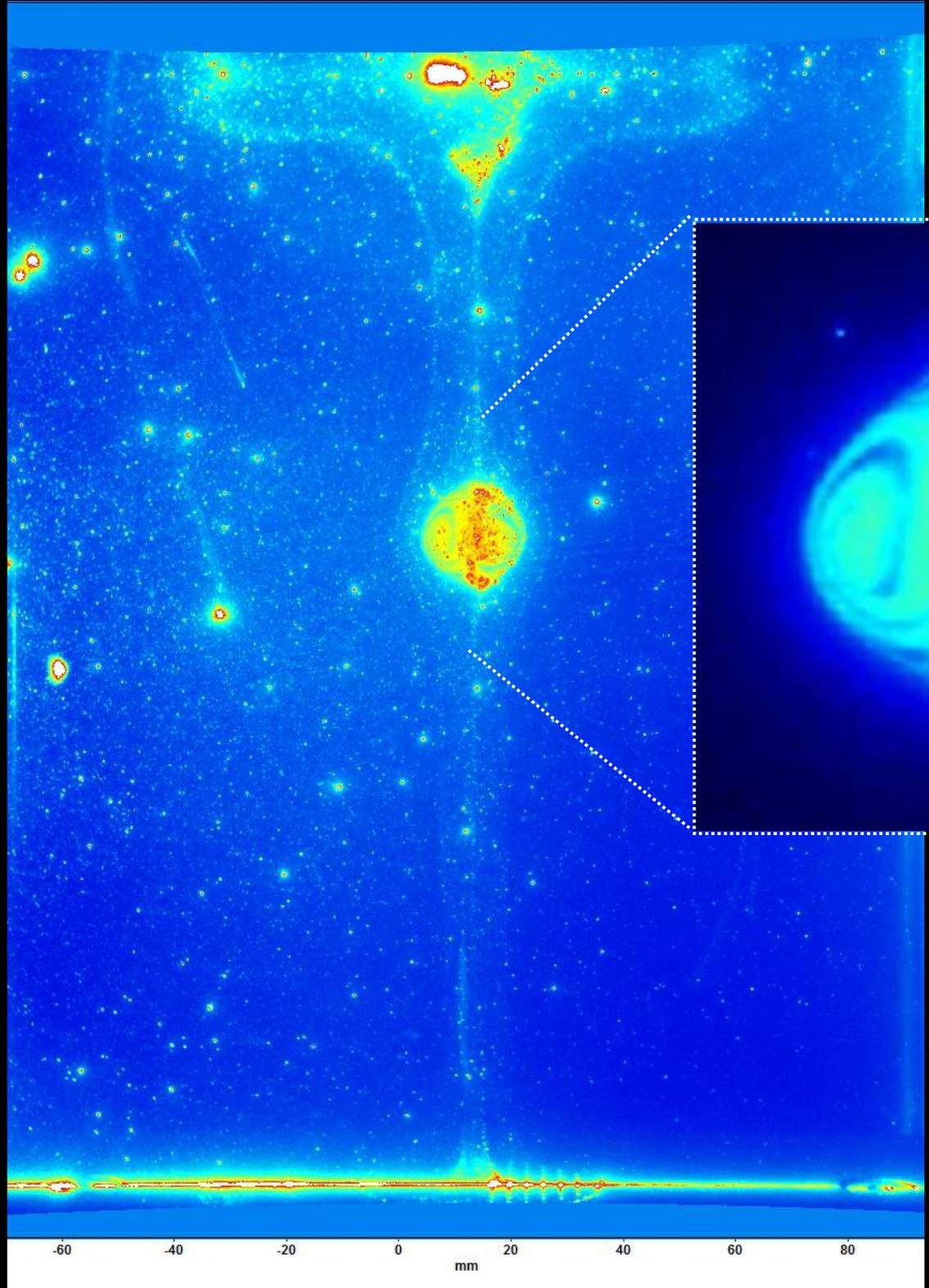


As it falls it grows
by entraining
surrounding fluid

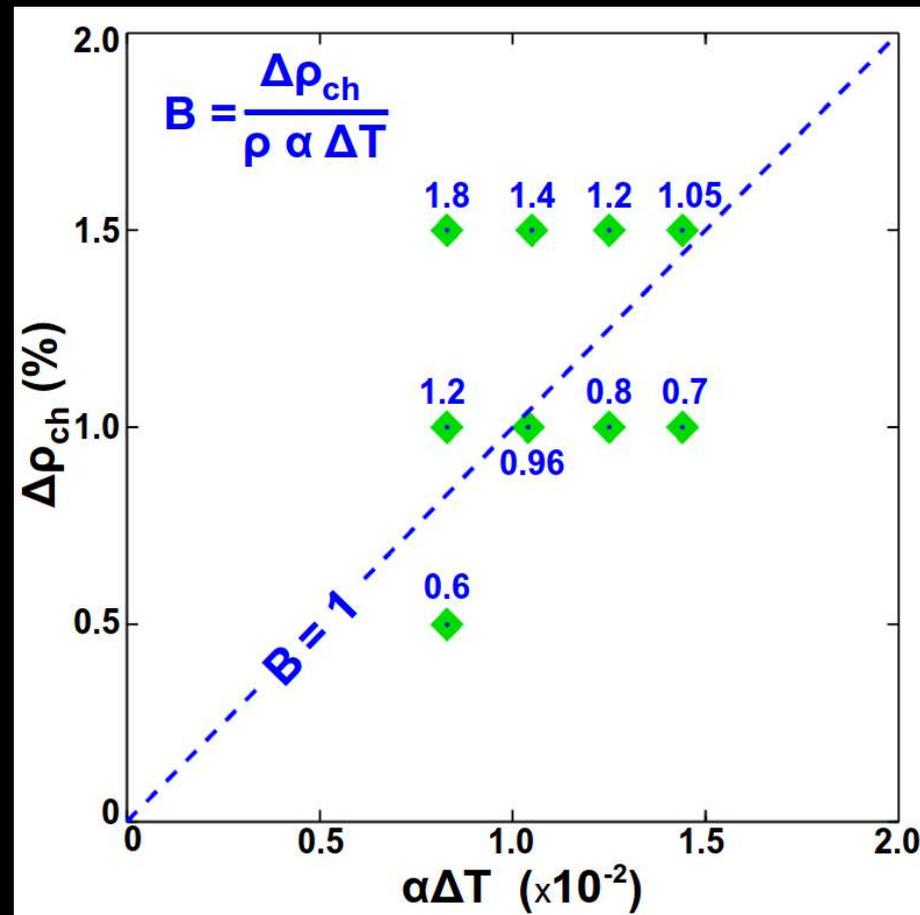


The upwelling
plume fluid has to
'circumvent' the
sinking denser
'blob'.
The flow lines are
perturbed

1000



Laboratory experiments with compositionally denser heterogeneities



How does a denser heterogeneity perturb the plume flow?

What is the evolving shape of an initially spherical denser heterogeneity?