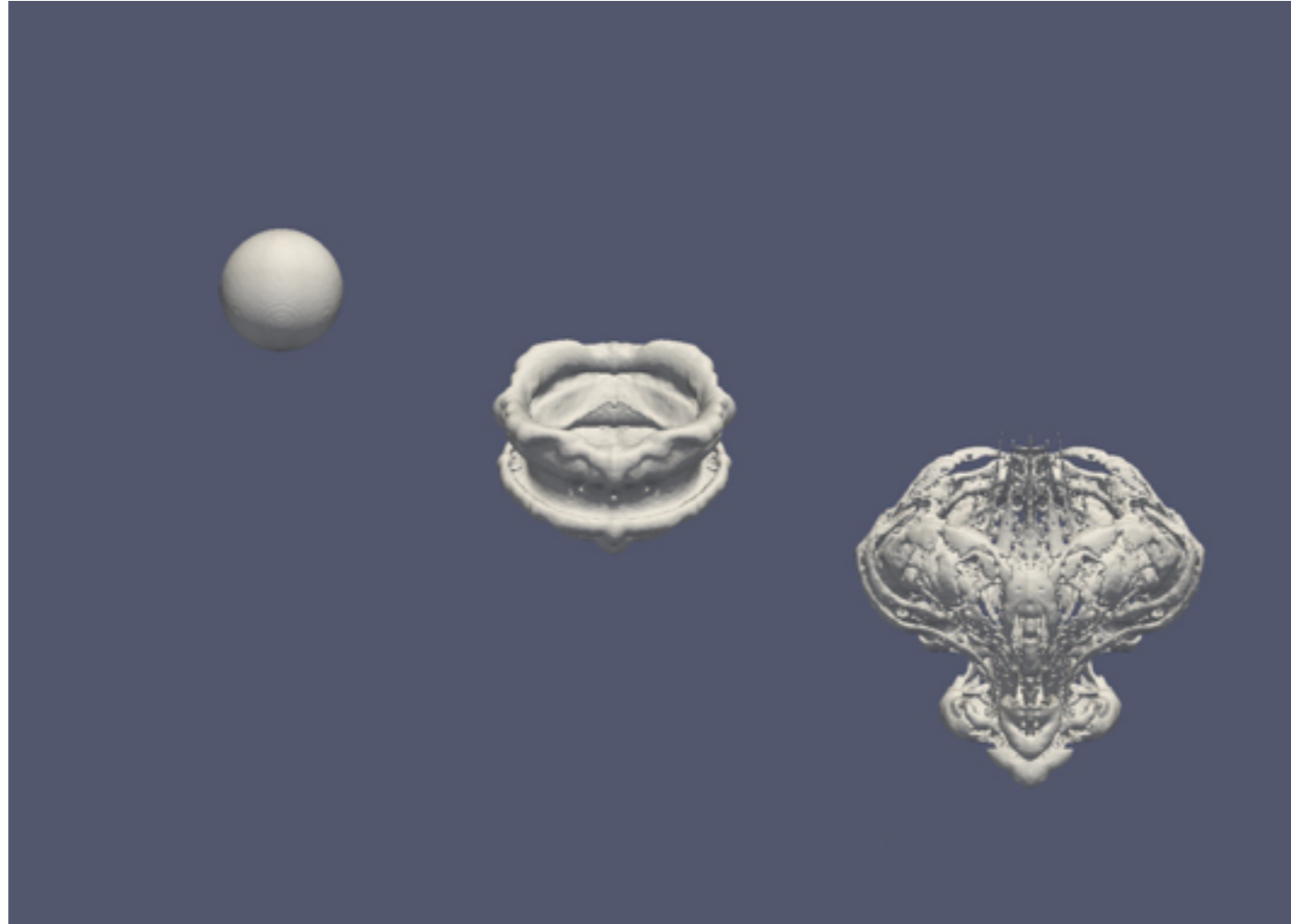


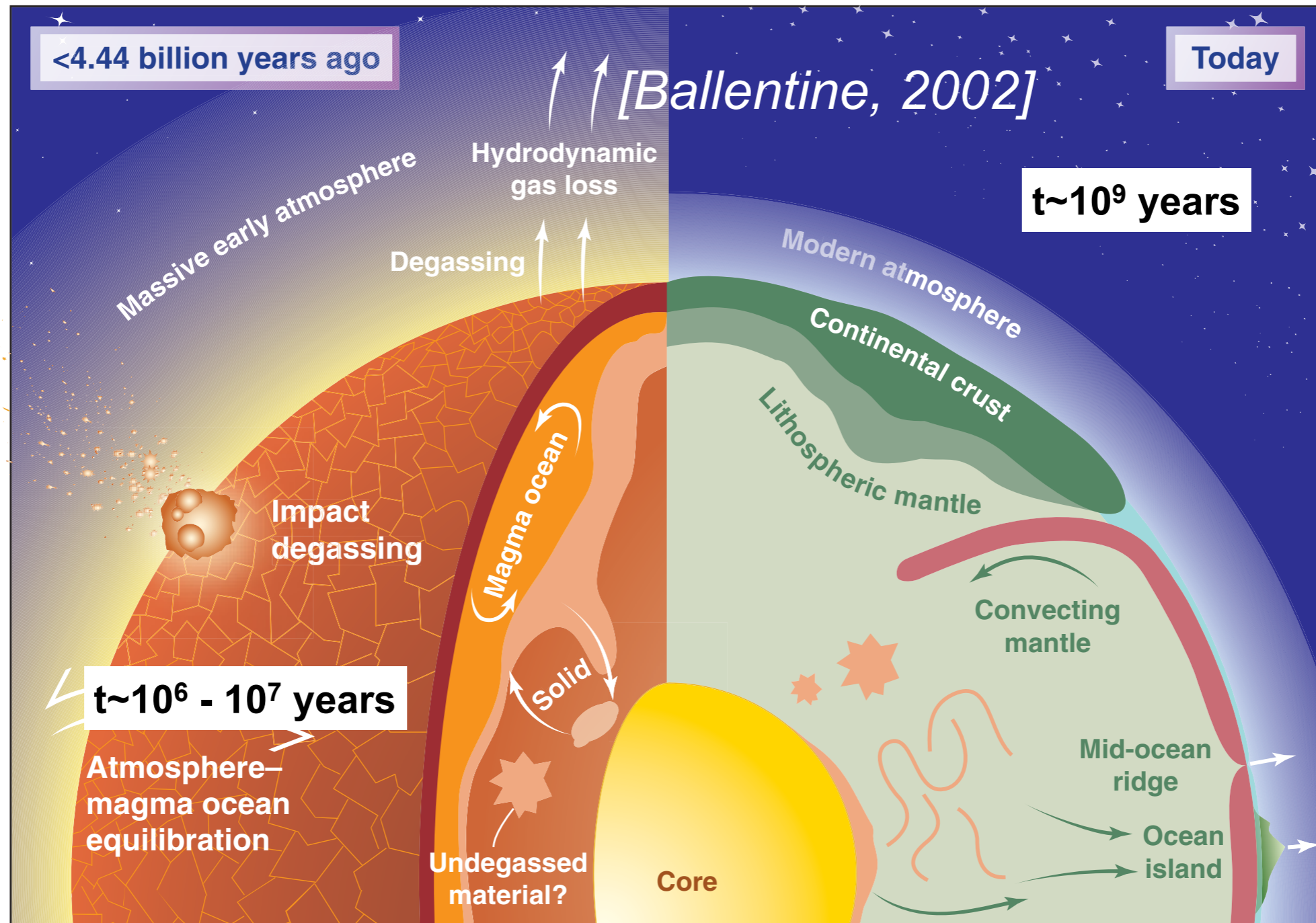
Iron flow in Earth's molten silicate proto-mantle



Henri Samuel



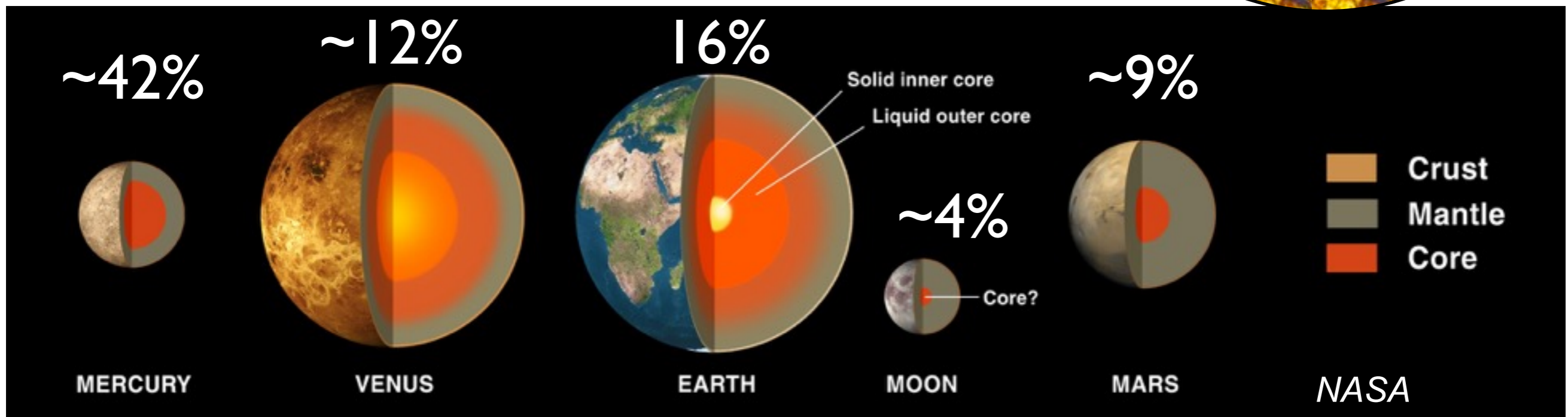
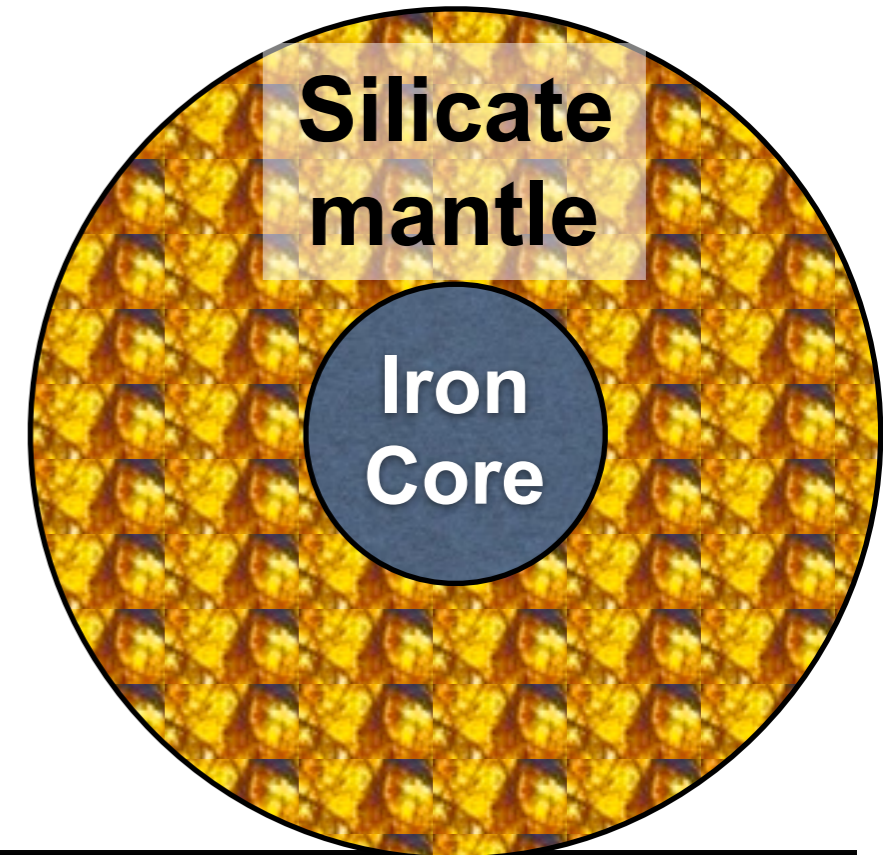
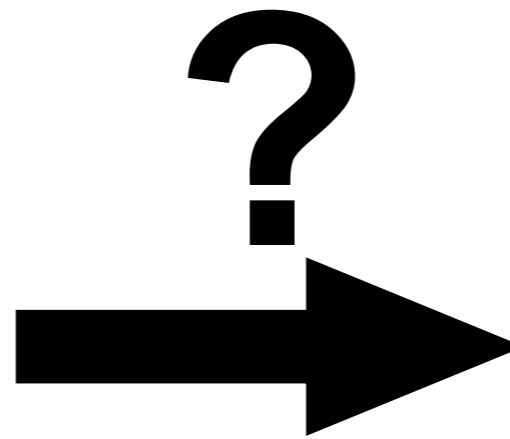
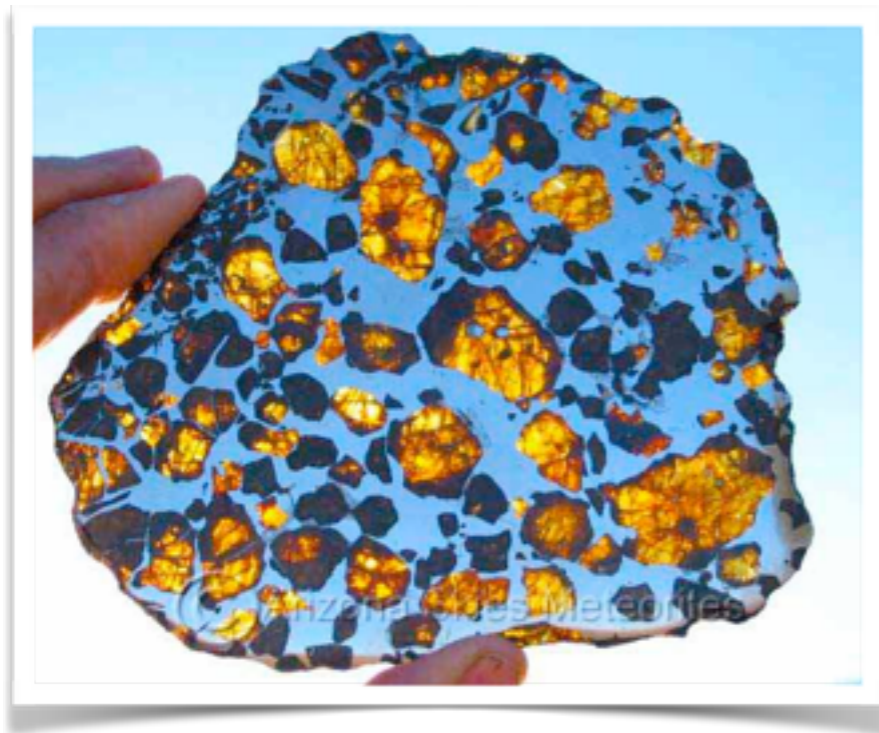
The early stages of planetary evolution



Early stages = Initial condition \Rightarrow long term evolution

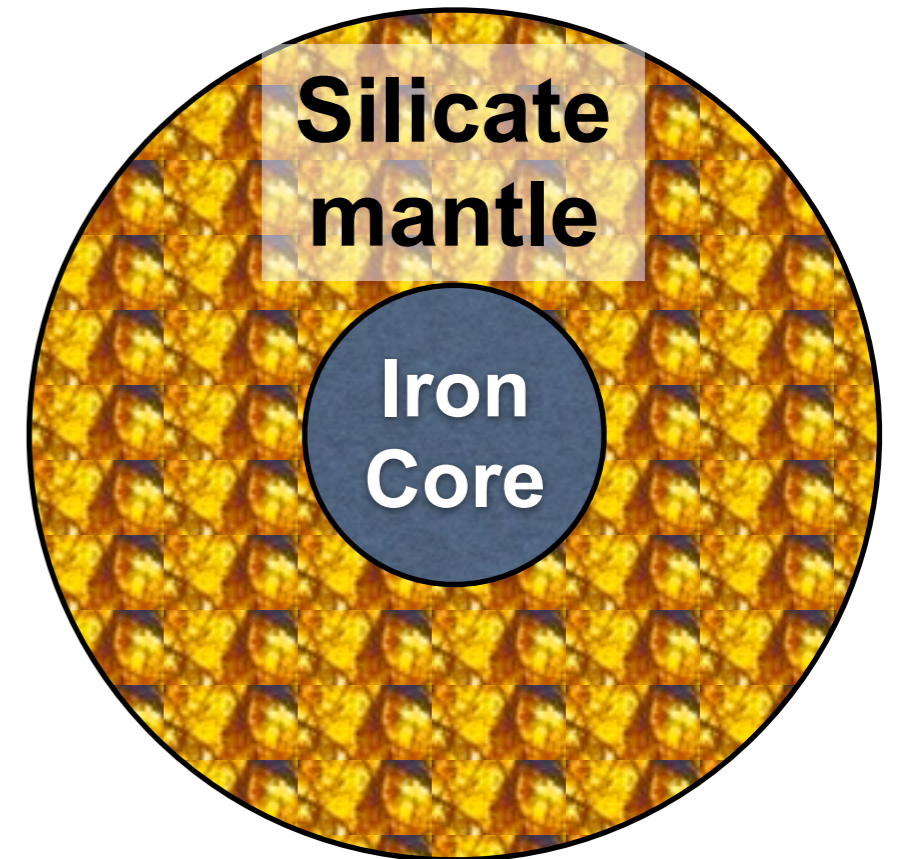
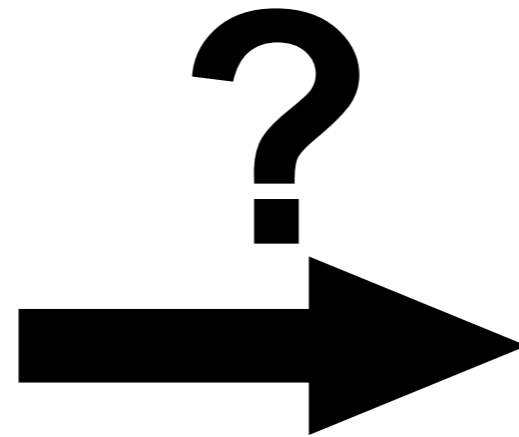
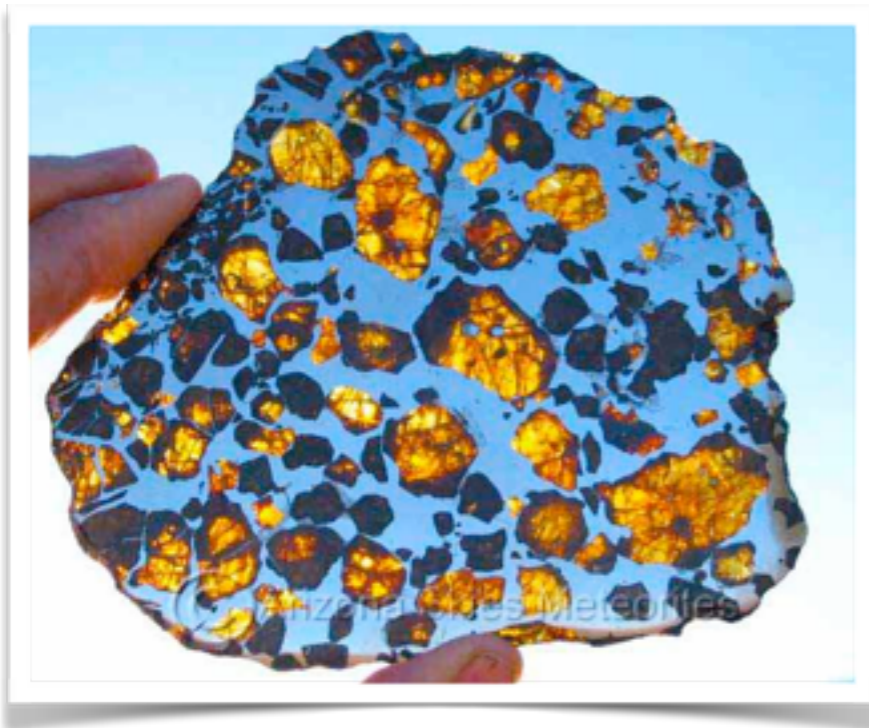
Early differentiation: Core Formation

- ✓ Metallic core present on several terrestrial bodies
- ✓ Core formation: First major differentiation event in terrestrial planets



What are the constraints?

Constraints on core formation: Summary



✓ Hf/W chronometry

⇒ Fast process: $t < 100$ Myrs

✓ Overabundance of siderophile elements (Ni, Co...) in mantle

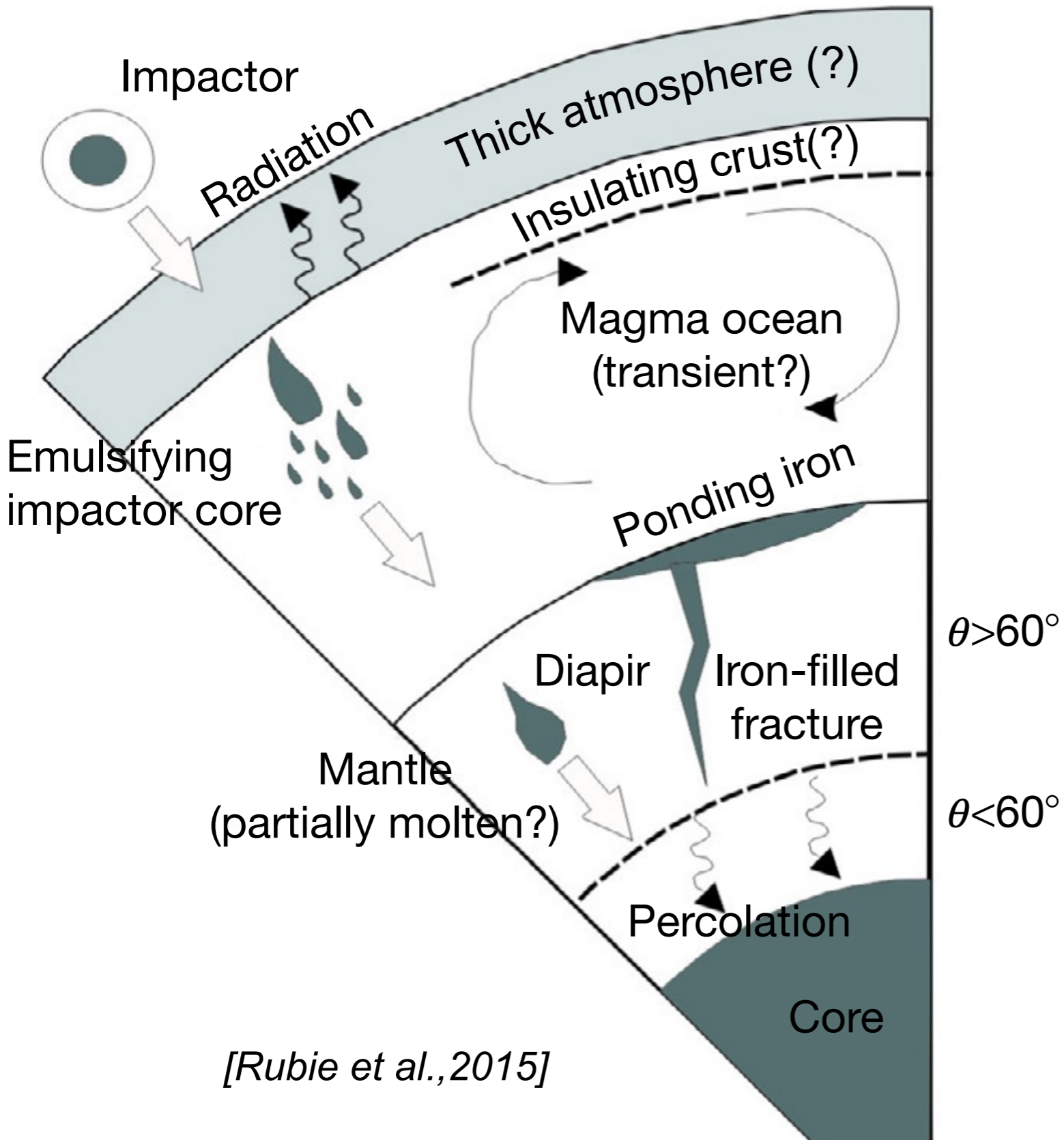
⇒ Requires time for Fe-Si equilibration

✓ High T process ("Si-Fe" separation)

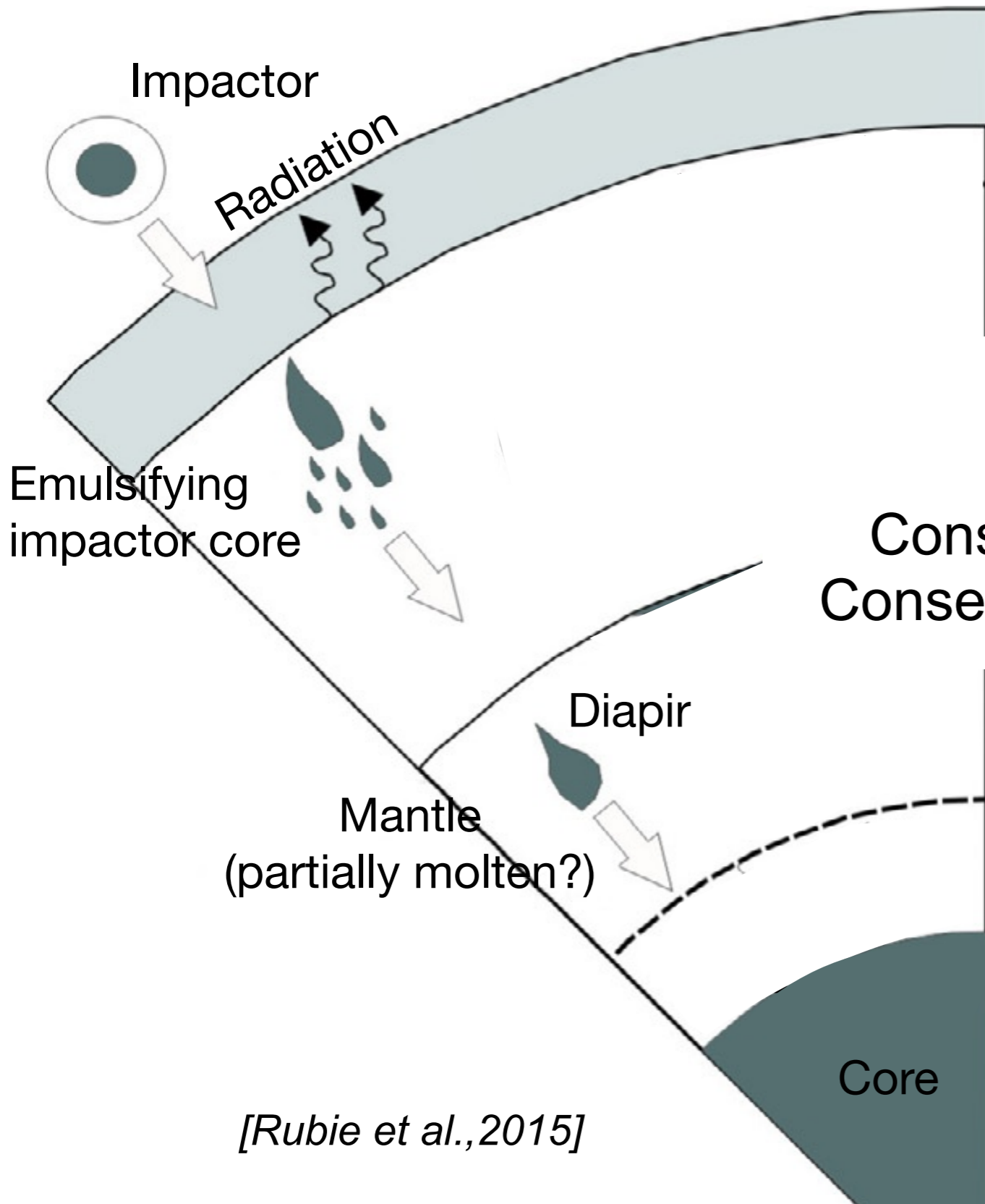
⇒ Melting

How did it happen?

Several possible core formation scenarios



Several possible core formation scenarios



[Rubie et al., 2015]

Focus on negative diapirism in:
✓ partially molten proto-mantle
✓ fully molten magma ocean

Do diapirs breakup?
Timing for fragmentation?
Consequences for Fe-Si equilibration?
Consequences for Fe-Si heat partitioning?

- 1. Setup and parameter space**
- 2. Influence of the parameters**
- 3. Implications**

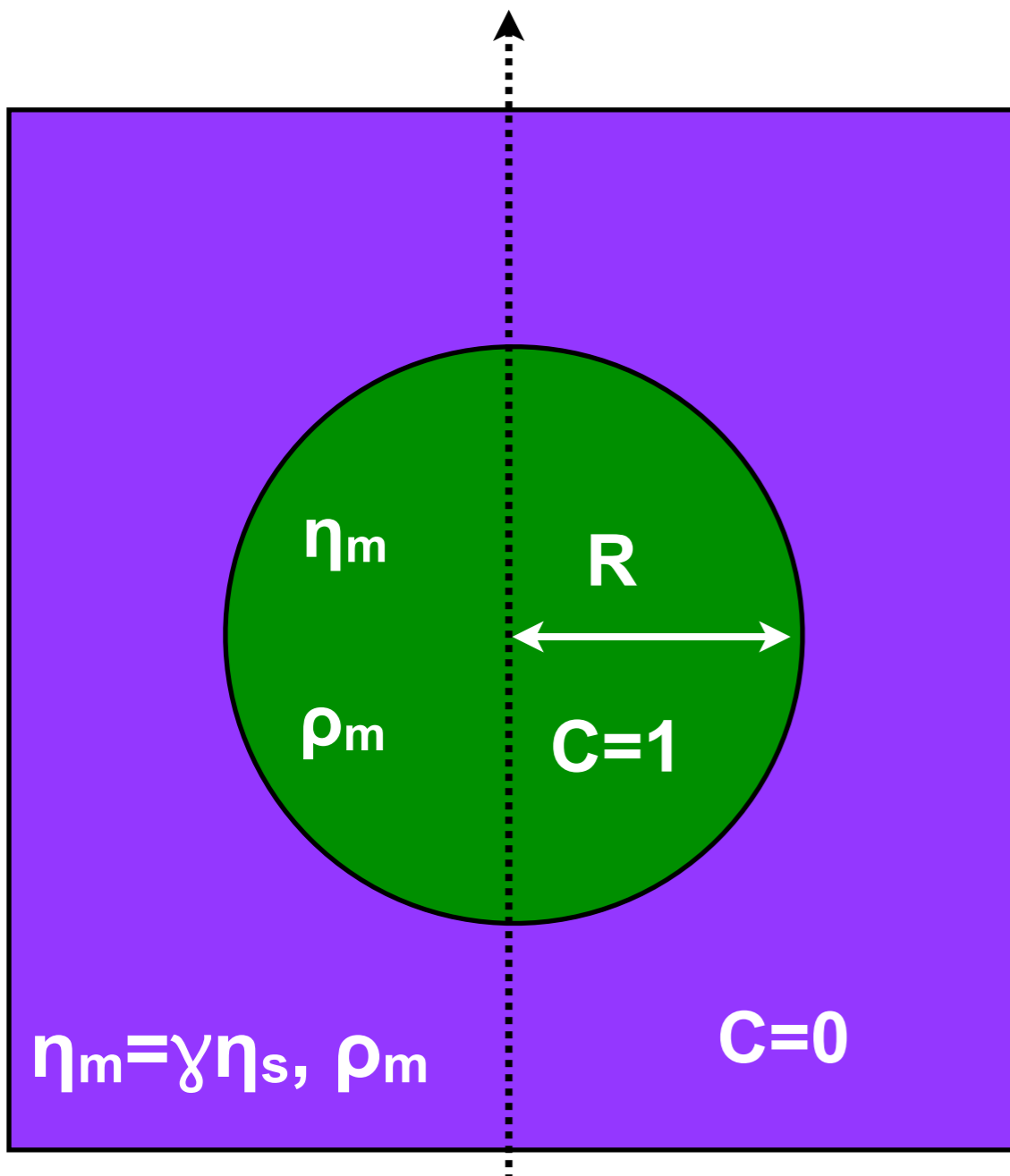
Fluid dynamics description of negative diapirism

Governing conservation equations

Momentum: $\rho D_t \mathbf{u} = -\nabla p + Re^{-1} \nabla \cdot (\eta \sigma) + Fr^{-1} C \mathbf{e}_g + We^{-1} \kappa \delta(d) \mathbf{n} - Ro^{-1} \boldsymbol{\Omega} \times \mathbf{u}$

Mass: $\nabla \cdot \mathbf{u} = 0$

Composition: $D_t C = 0$



Governing parameters

Re = Inertia / Viscous effects: $\frac{\rho_s V_\infty R}{\eta_s}$

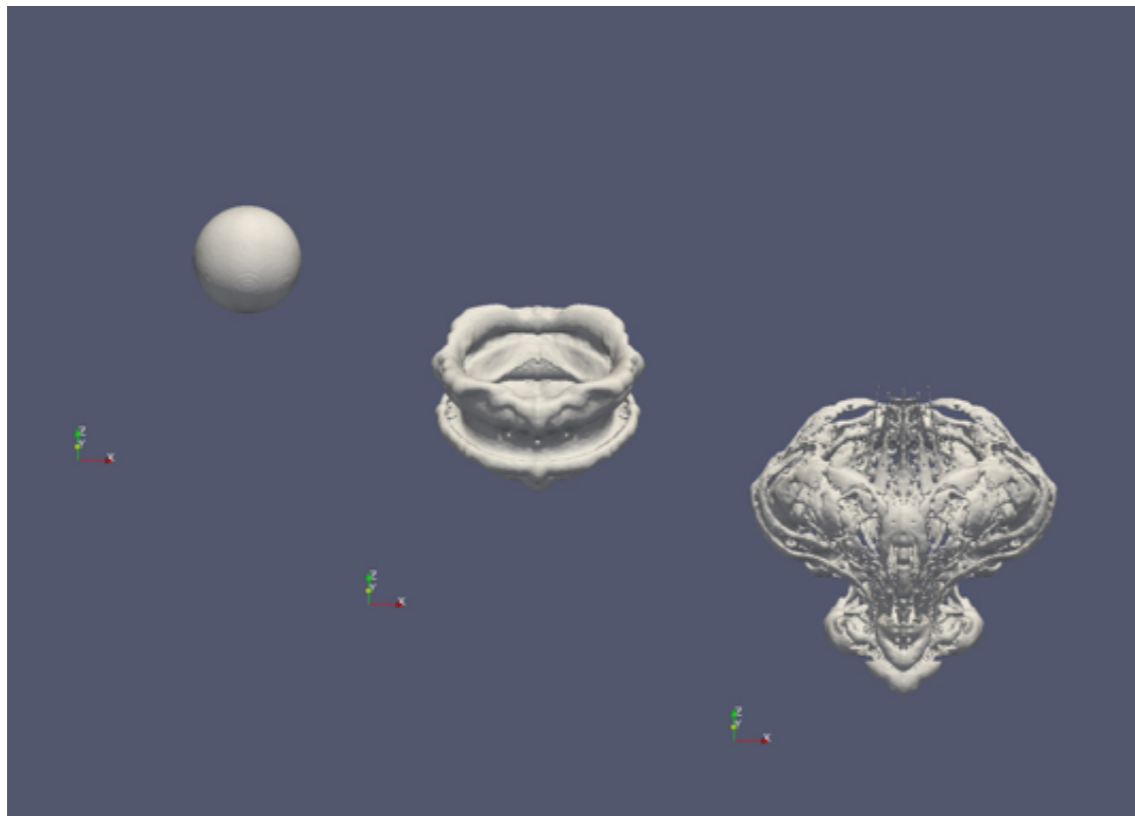
Fr = Inertia / Effective Buoyancy: $\frac{V_\infty^2}{gR}$

We = Inertia / Surface tension: $\frac{\rho_s V_\infty^2 R}{\sigma}$

+ rheological parameters ($n, \eta_s / \eta_m$)

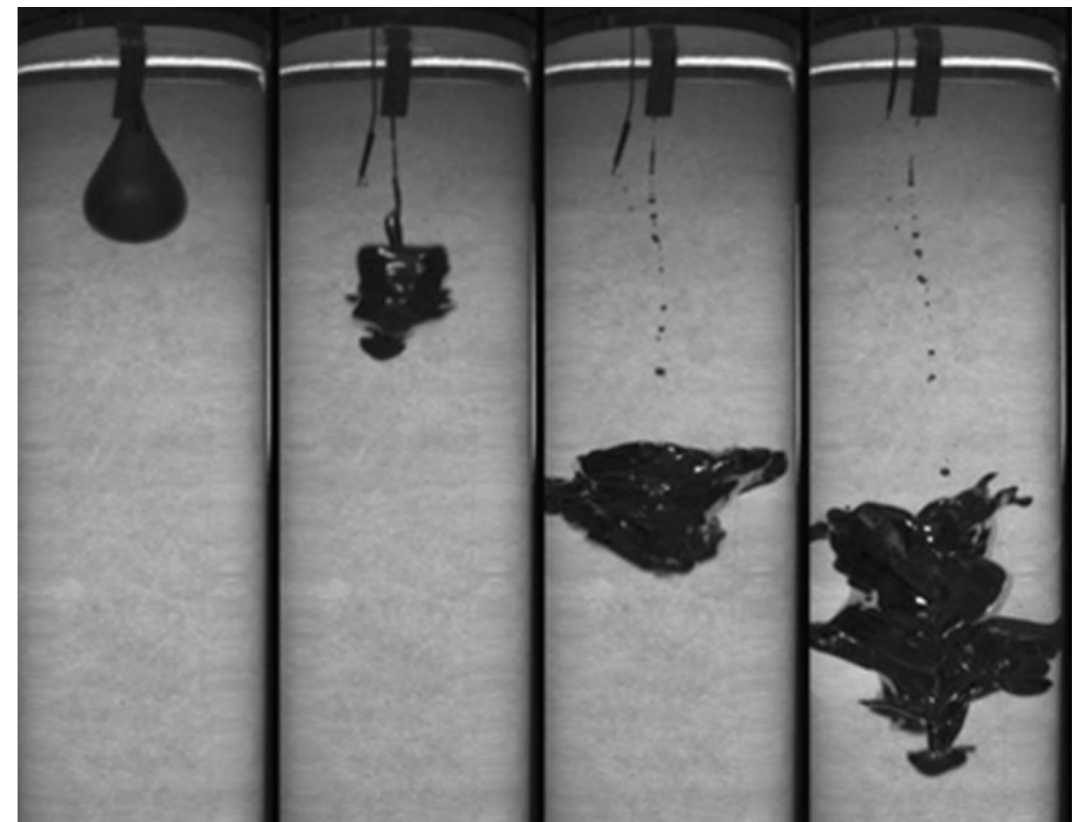
Modelling approach

Numerical experiments



[Ichikawa et al., 2010]
[Samuel, 2012]

Analog/“Tank” experiments

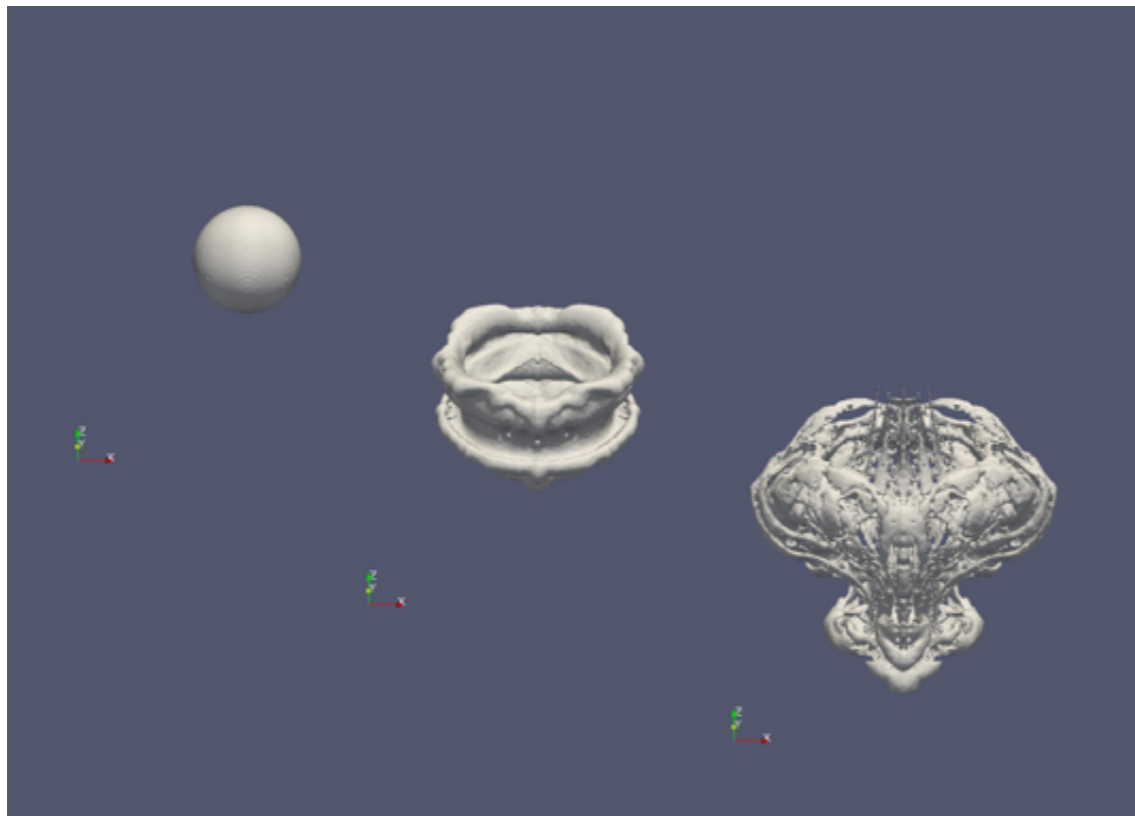


[Villermaux, 2007]
[Wacheul et al., 2014]

Modelling approach

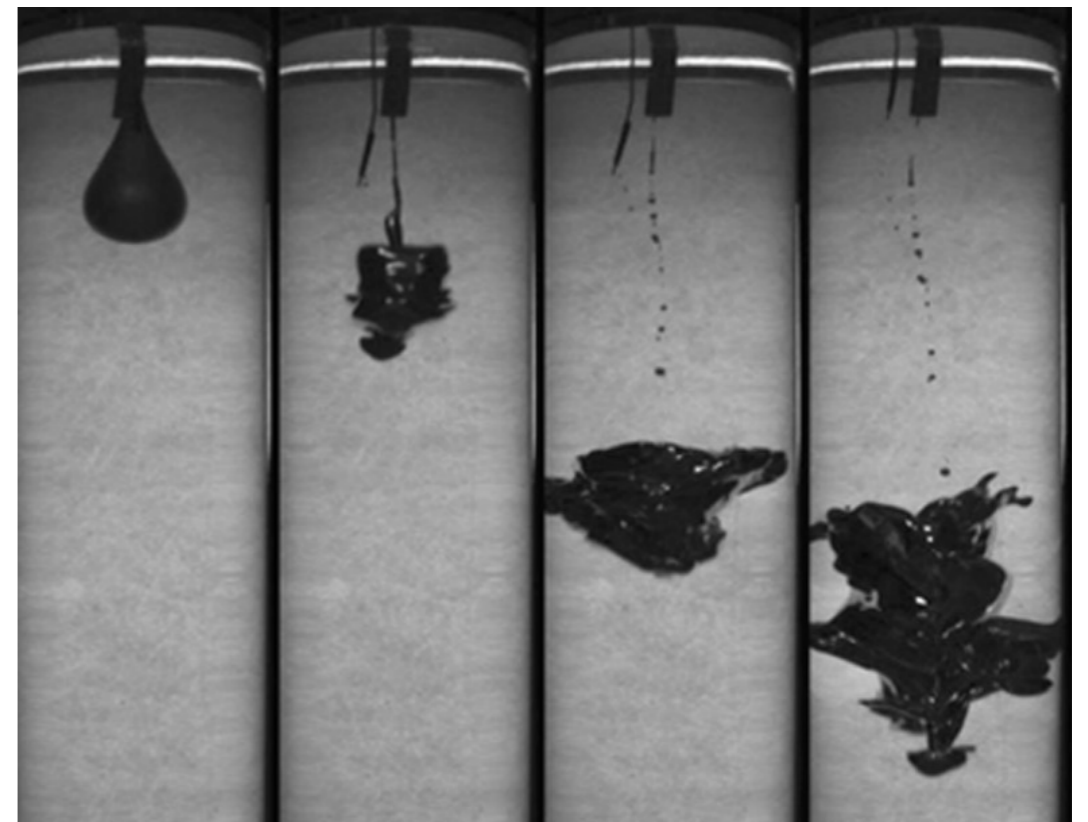
“A theory is something nobody believes, except the person who made it. An experiment is something everybody believes, except the person who made it.” —Albert Einstein

Numerical experiments



[Ichikawa et al., 2010]
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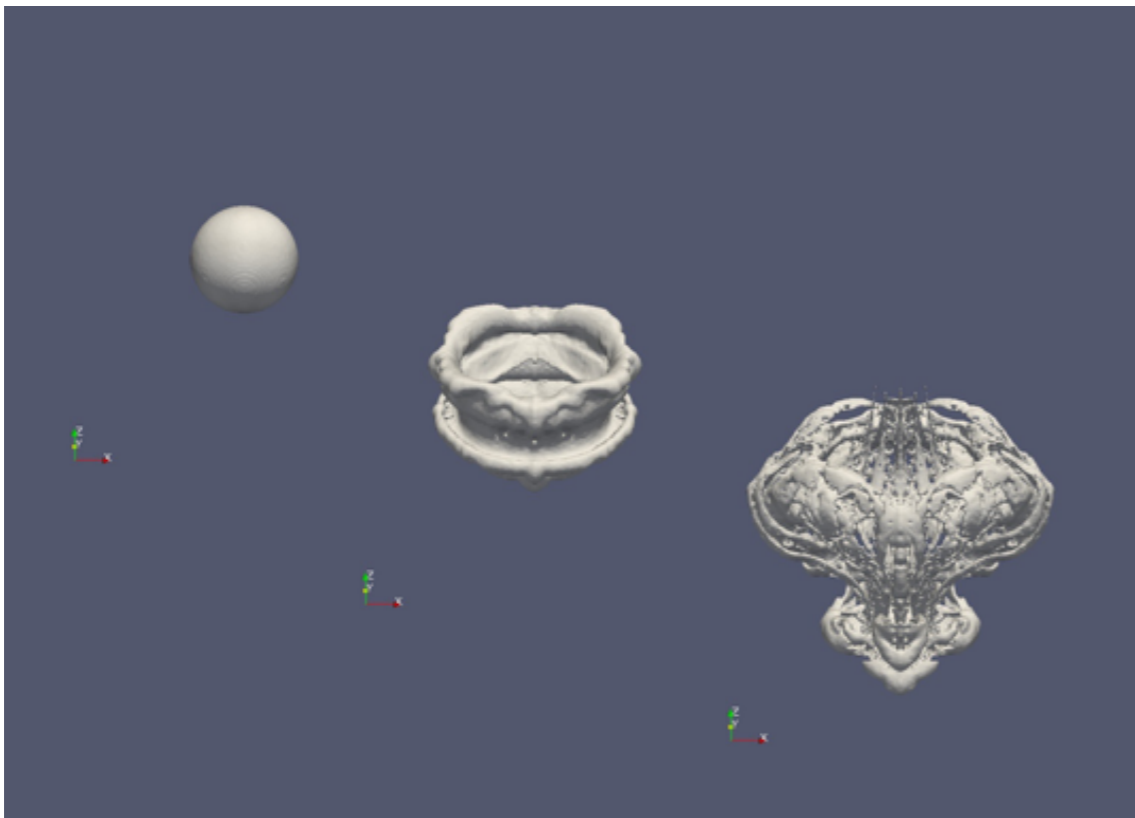


[Villermaux, 2007]
[Wacheul et al., 2014]

Modelling approach

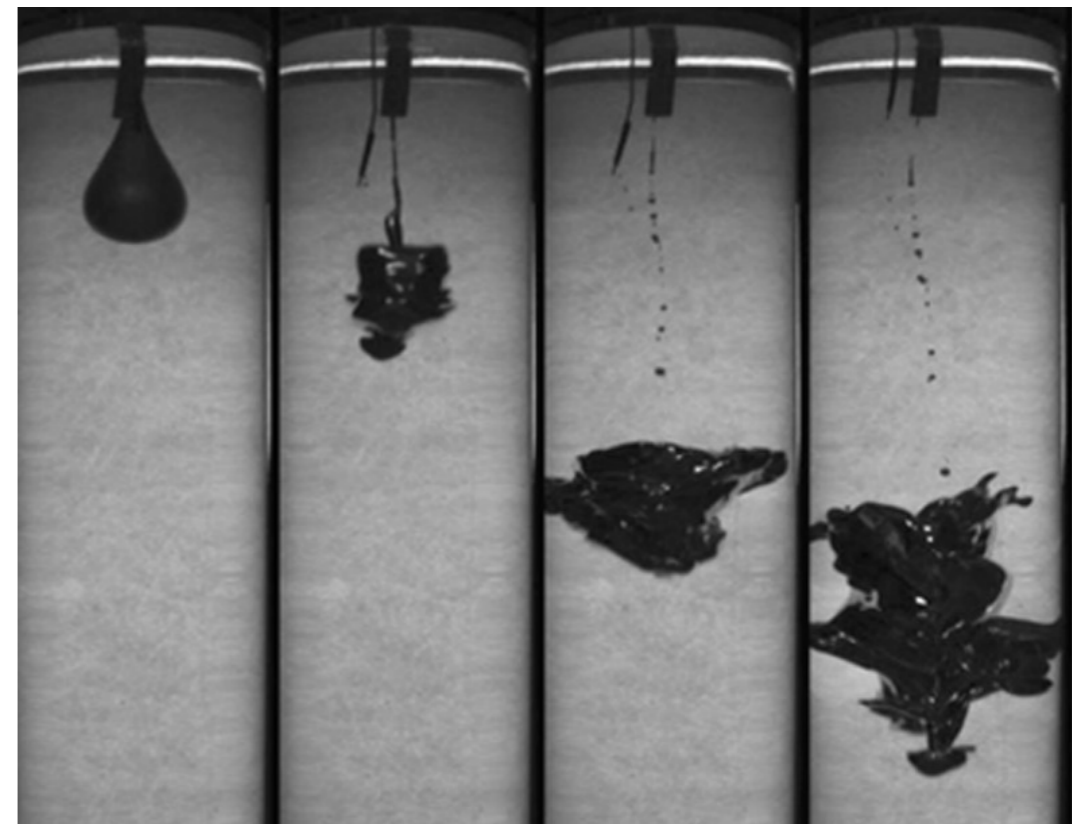
“A numerical experiment is something nobody believes, except the person who made it. A laboratory experiment is something everybody believes, except the person who made it.”

Numerical experiments



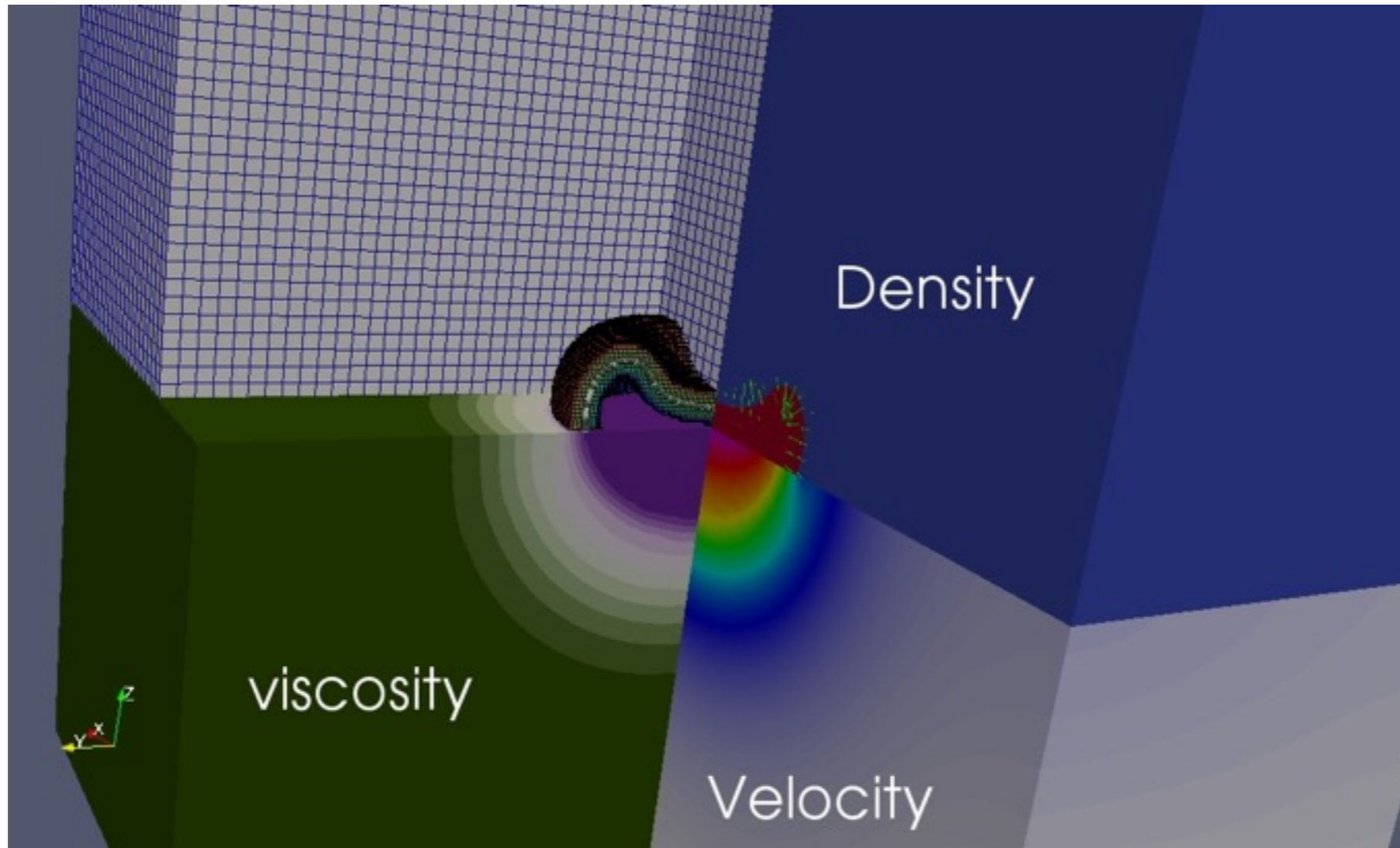
*[Ichikawa et al., 2010]
[Samuel, 2012]*

Analog/“Tank” experiments



*[Villermaux, 2007]
[Wacheul et al., 2014]*

3D Eulerian-Lagrangian Finite-Volume modeling



✓ Momentum & continuity: Implicit with exponential scheme / TVD RK explicit projection scheme with 3rd order WENO discretisation of non-linear advection terms

⇒ Essentially monotone, efficient for both large and small Reynolds number values

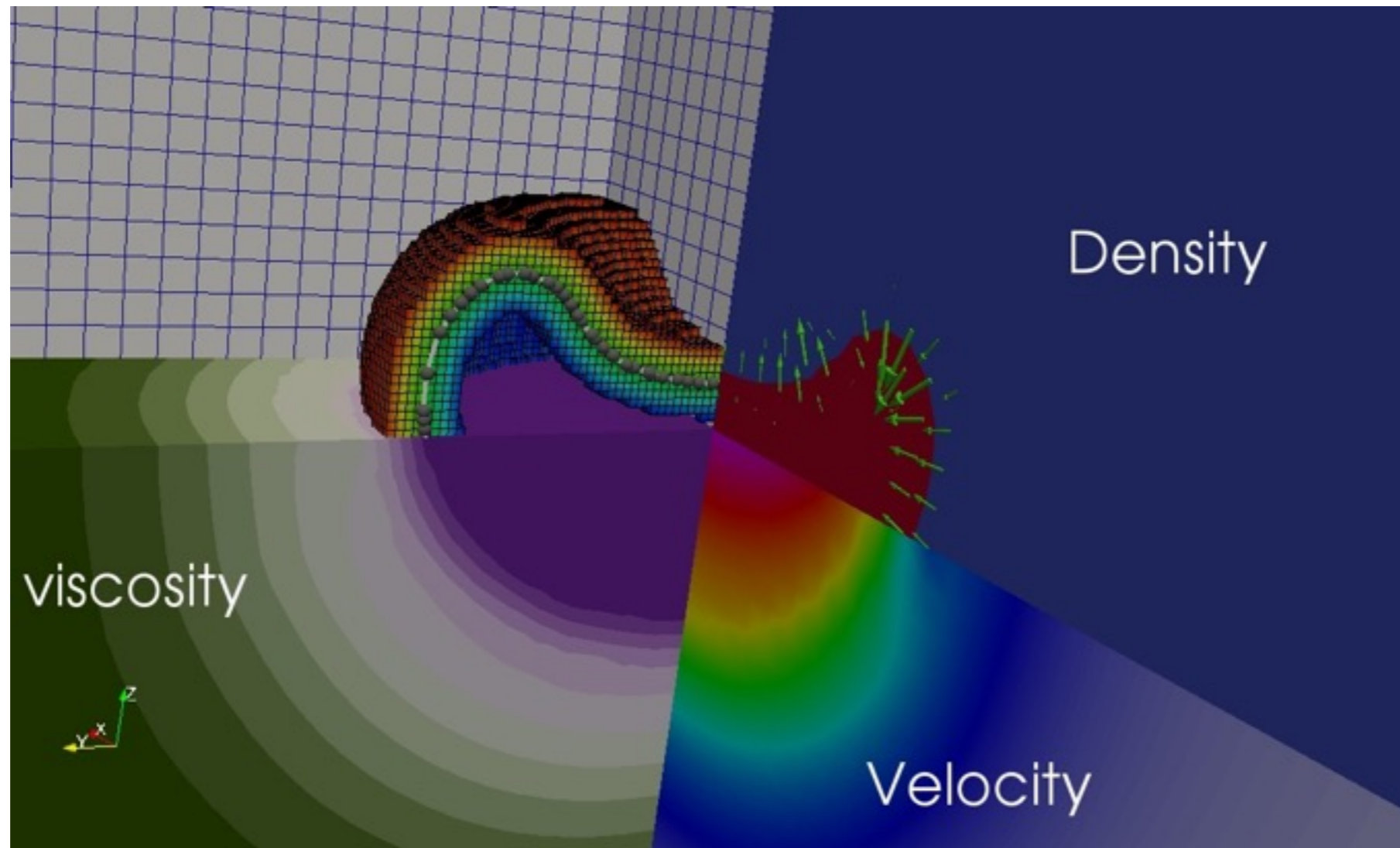
✓ Cons. composition: Particle-Marker two-way [Samuel, 2014] refined narrow-band Level-set

⇒ Sub-grid-scale resolution with good mass preservation at all times (error < 1%)

⇒ Surface tension accurately accounted for via a Continuum Surface Force Model

✓ Benchmarked against analytical and numerical solutions

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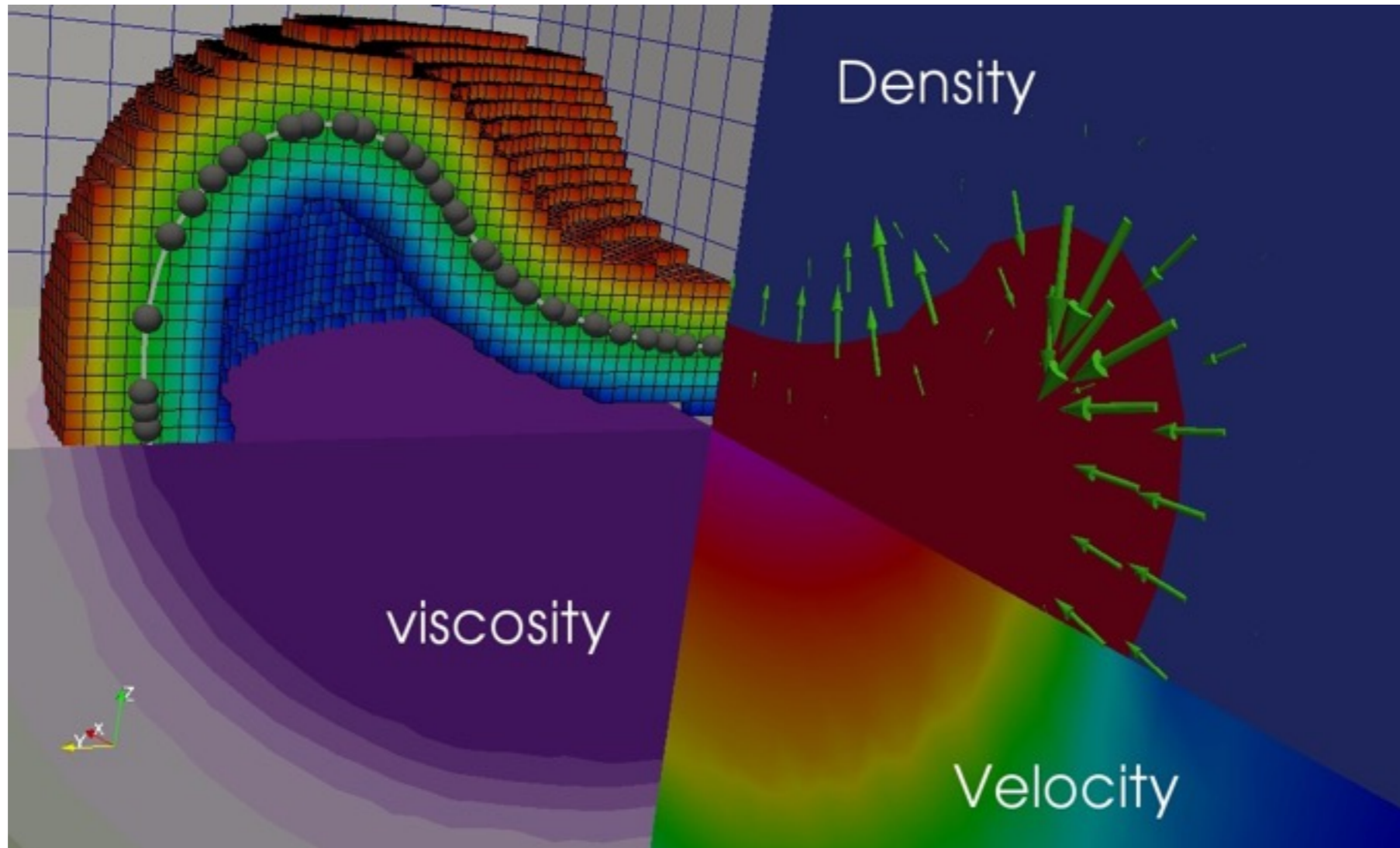
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Parameter space

$$\mathbf{Re} = \text{Inertia / Viscous effects: } \frac{\rho_s V_\infty R}{\eta_s} \quad \mathbf{We} = \text{Inertia / Surface tension: } \frac{\rho_s V_\infty^2 R}{\sigma}$$

✓ diapir radius, $R = 10^{-3} - 10^5$ m

✓ silicate viscosity, $\eta_s = 10^{-4} - 10^{14}$ Pa s

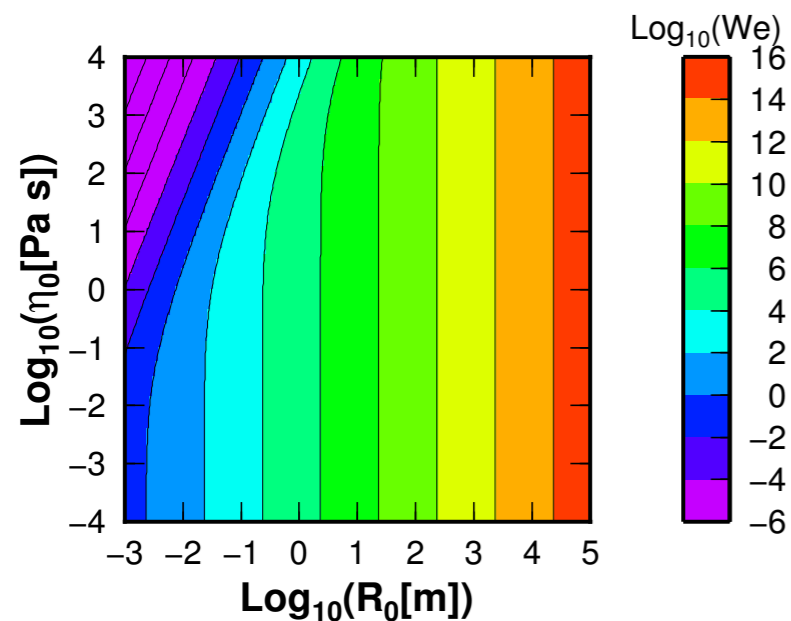
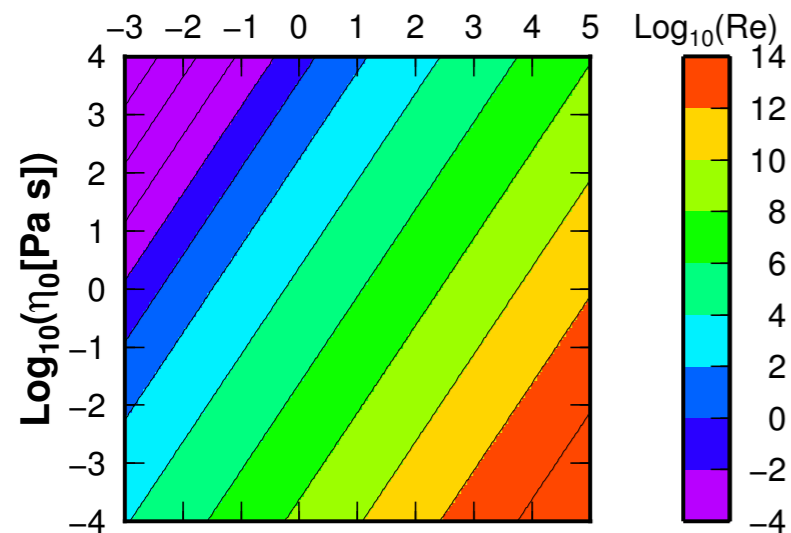
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Essentially molten



Parameter space

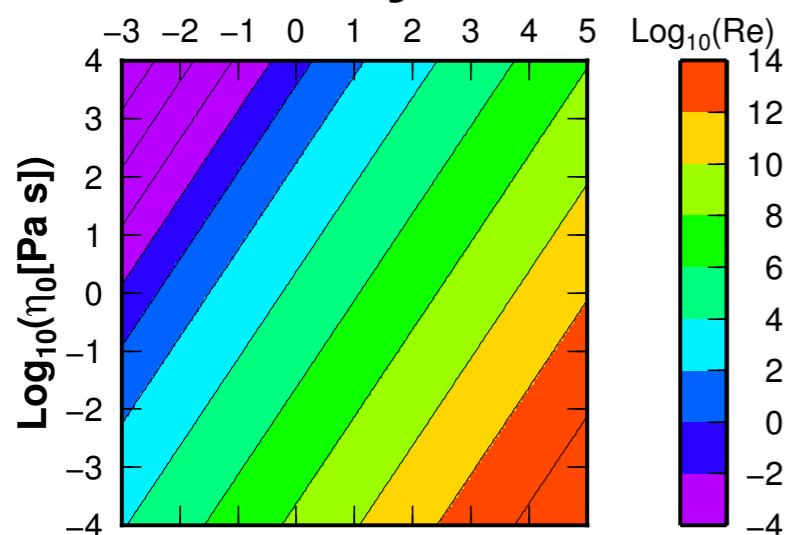
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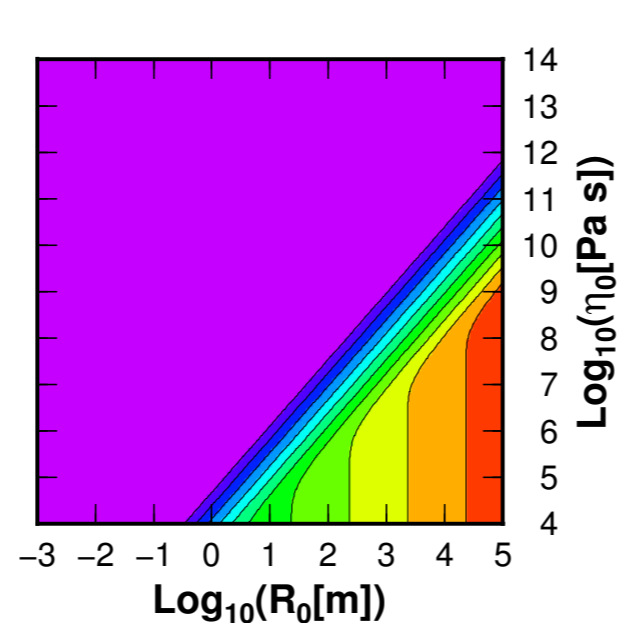
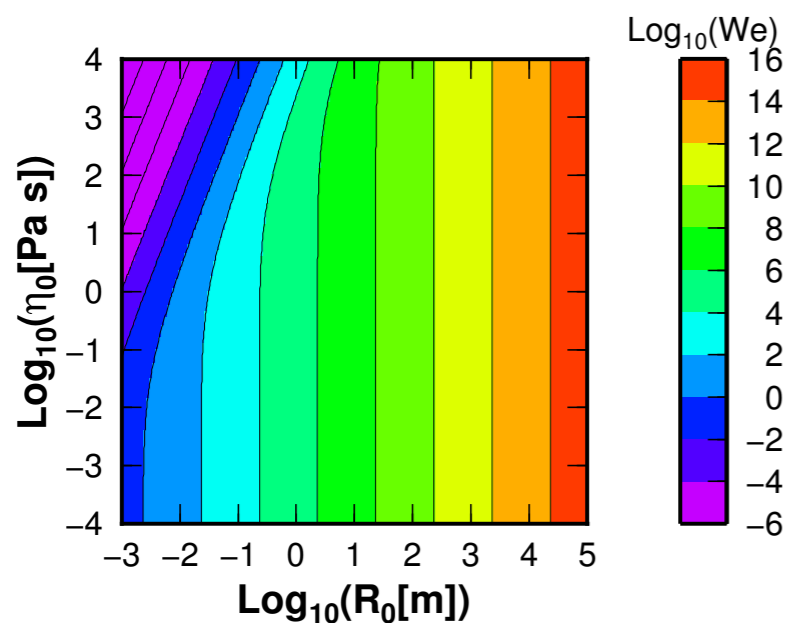
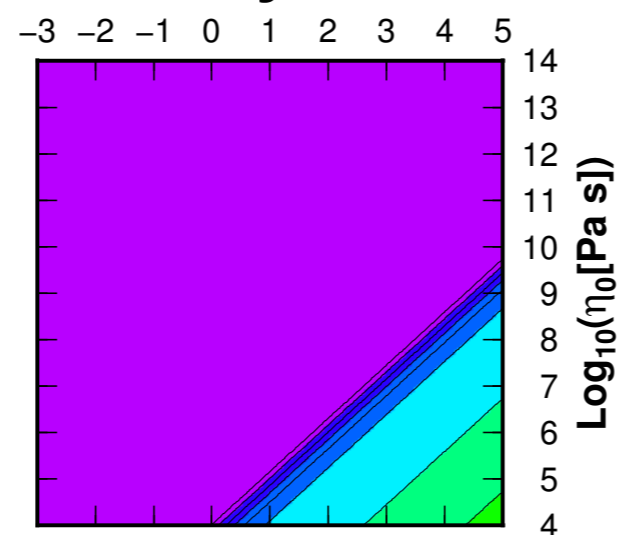
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Partially molten



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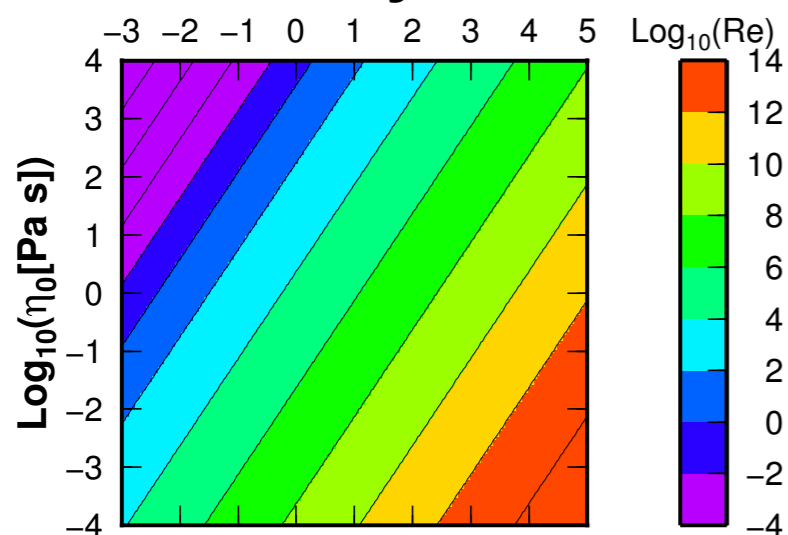
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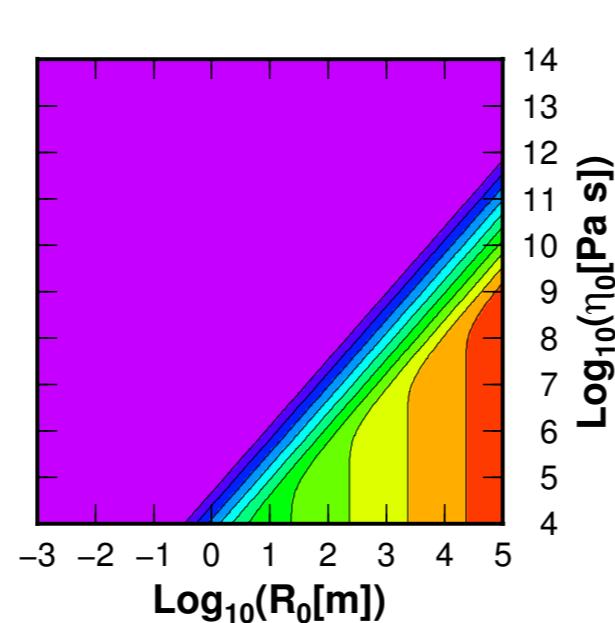
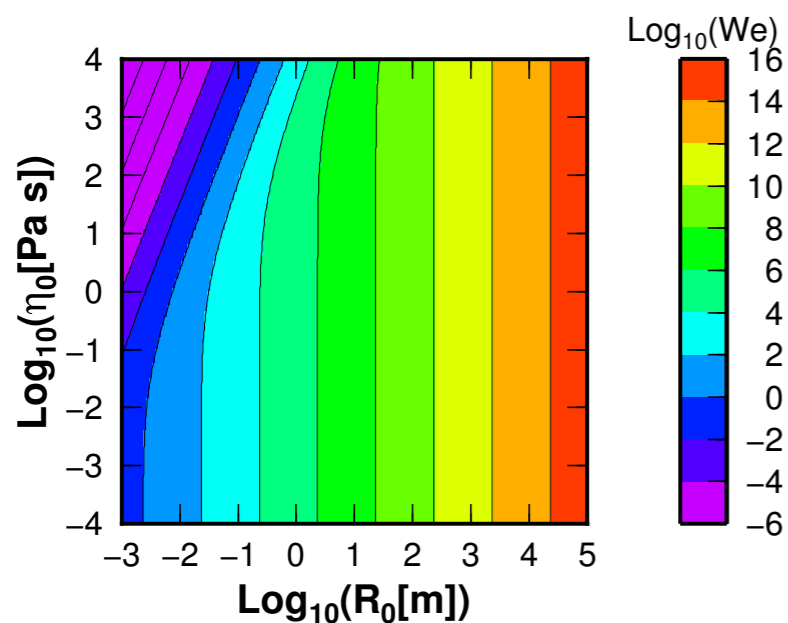
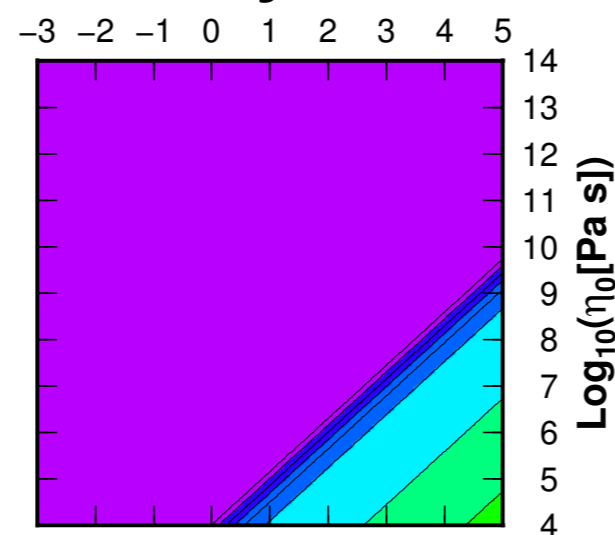
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Large Plausible range of rheology and diapir sizes

$$\text{Re} = [10^{-97} - 10^{16}]$$

$$\text{We} = [10^{-100} - 10^{15}]$$

⇒ Huge parameter space

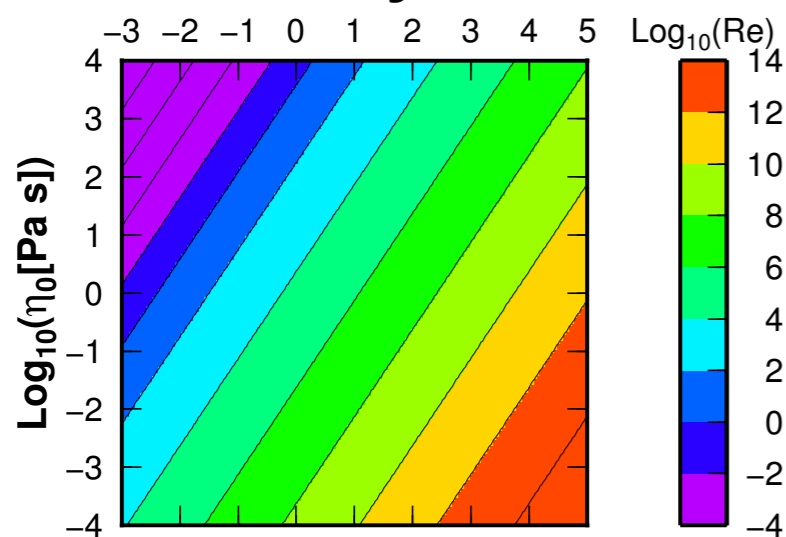
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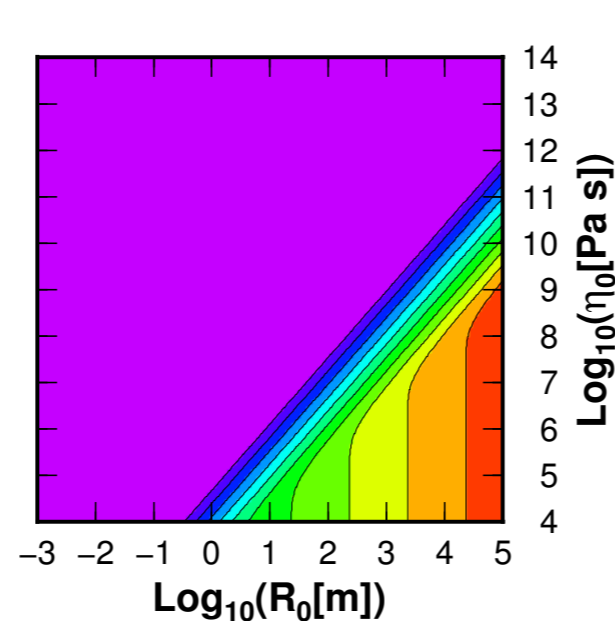
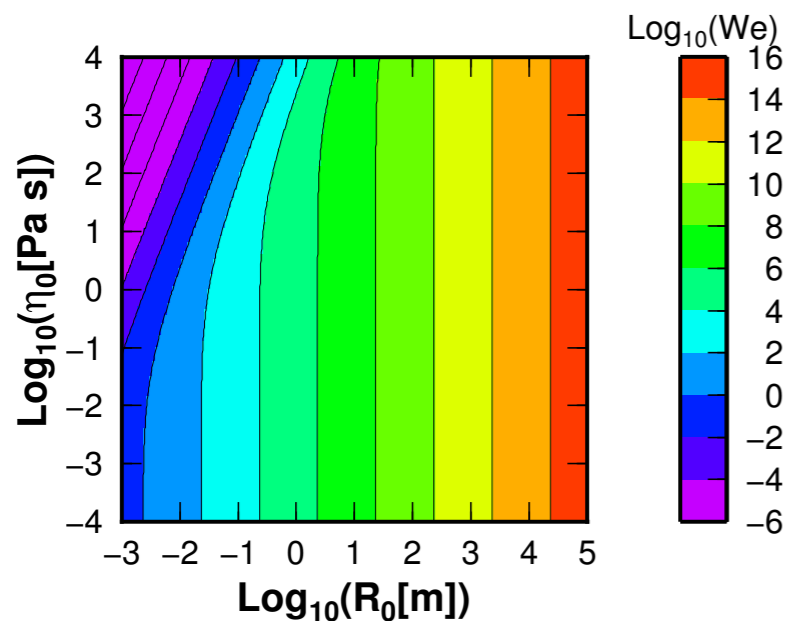
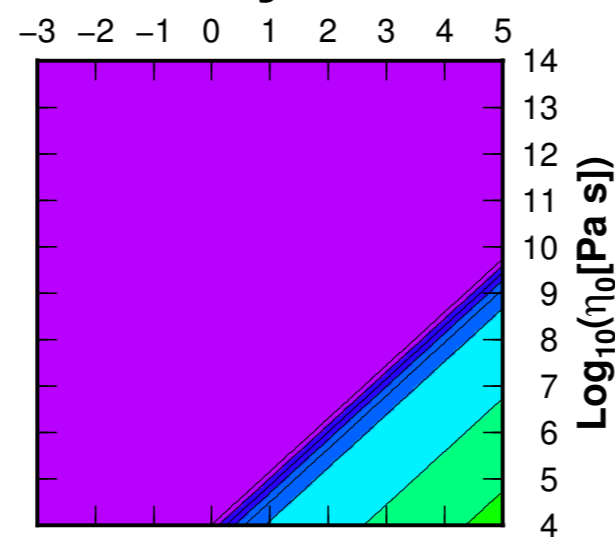
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Large, **small** and **intermediate** values must be considered

Parameter space

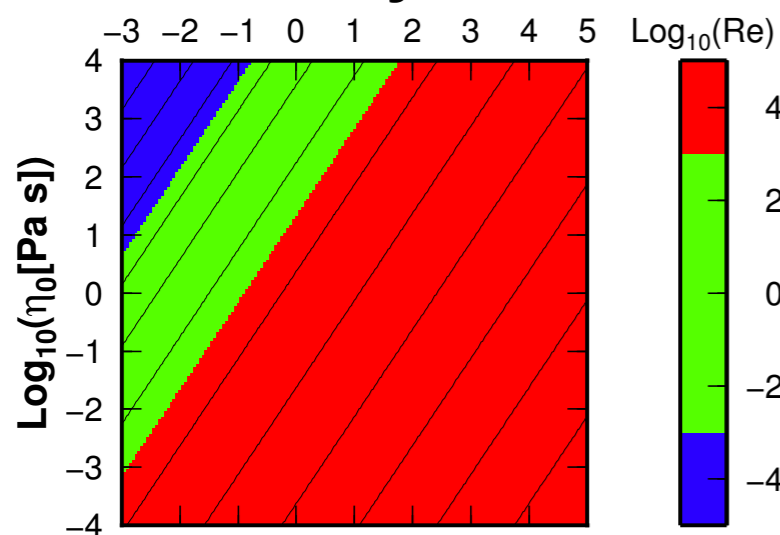
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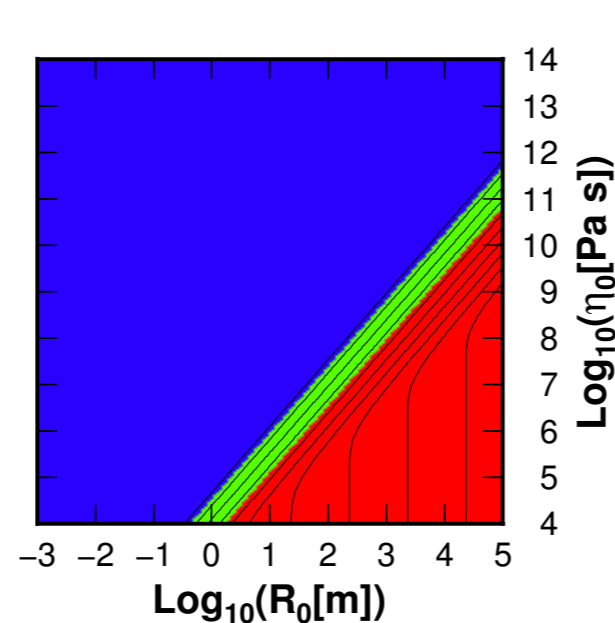
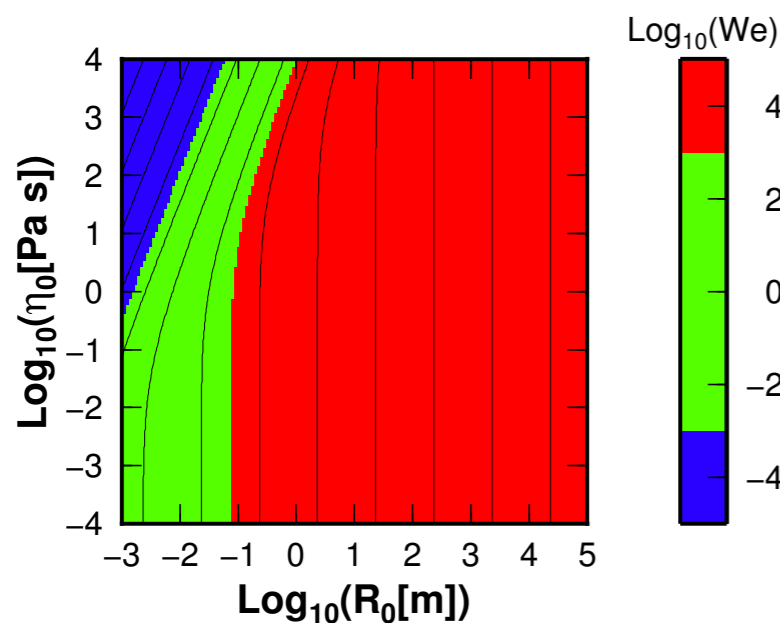
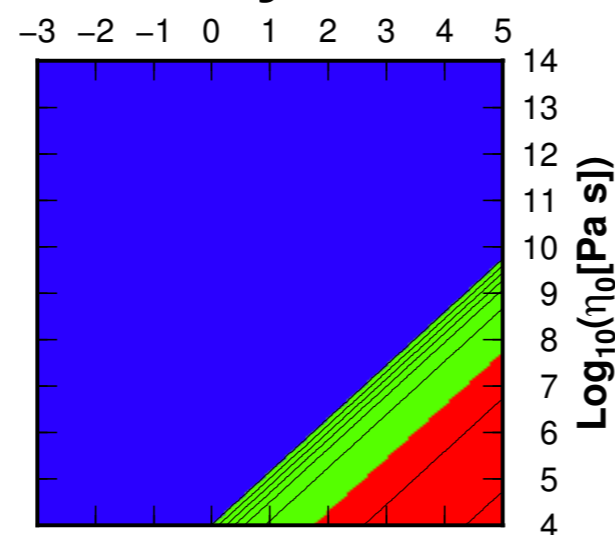
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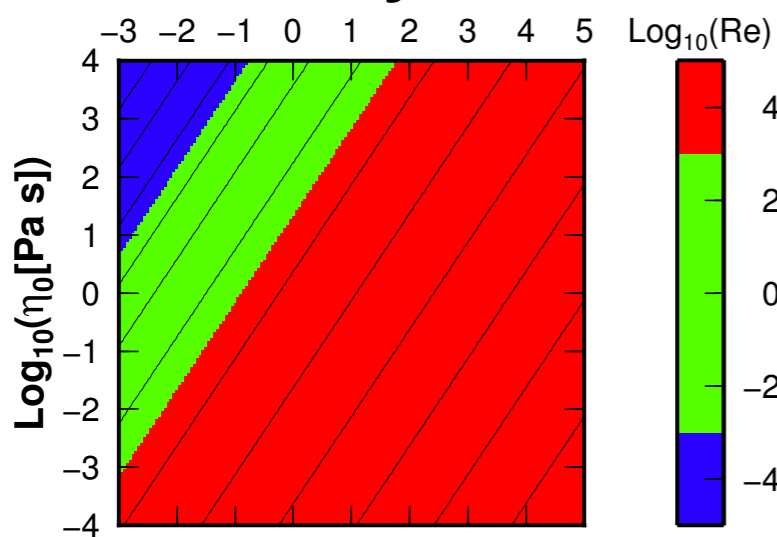
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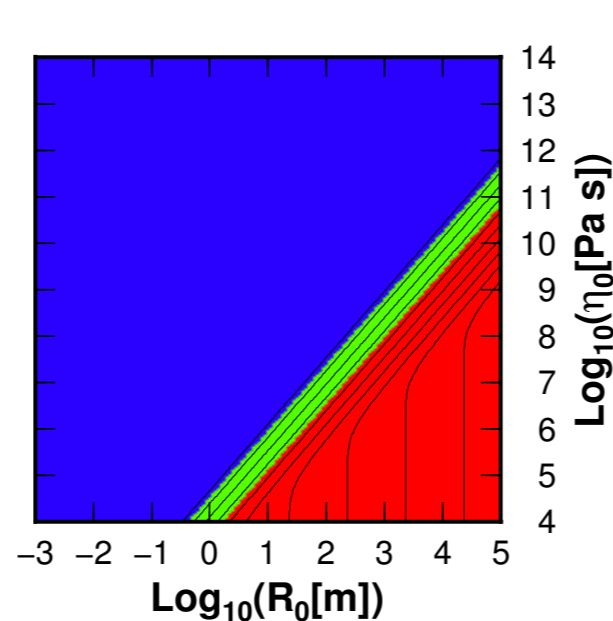
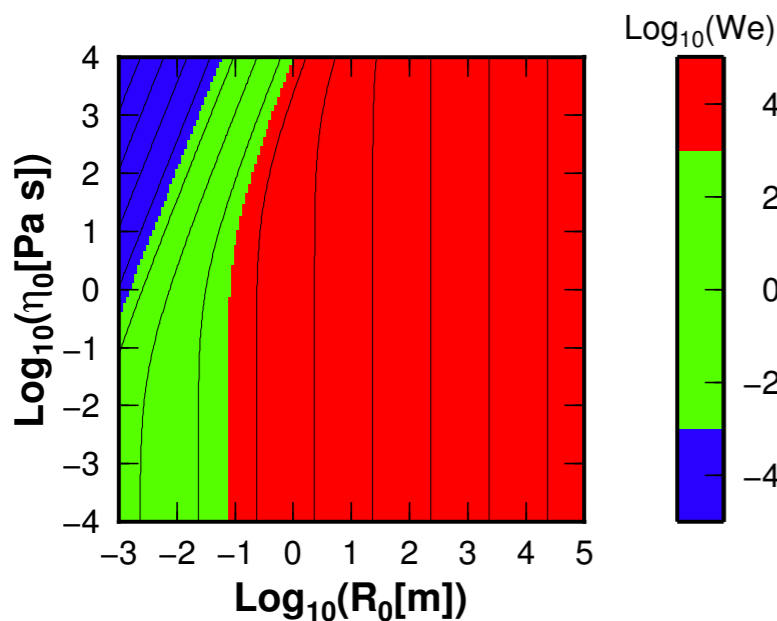
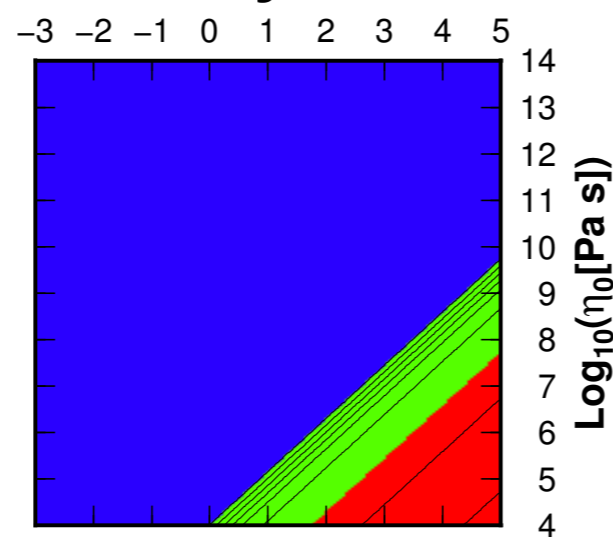
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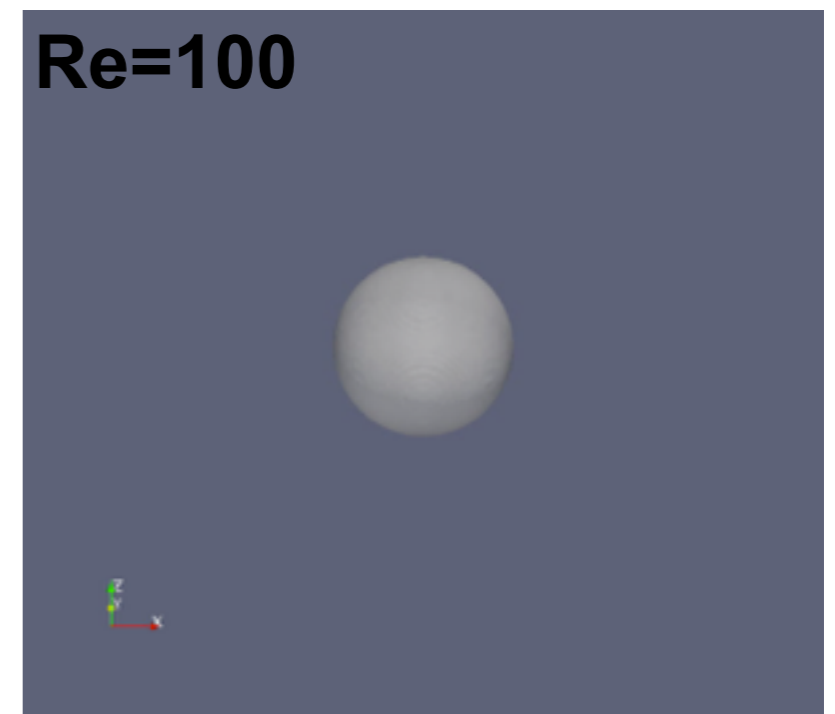
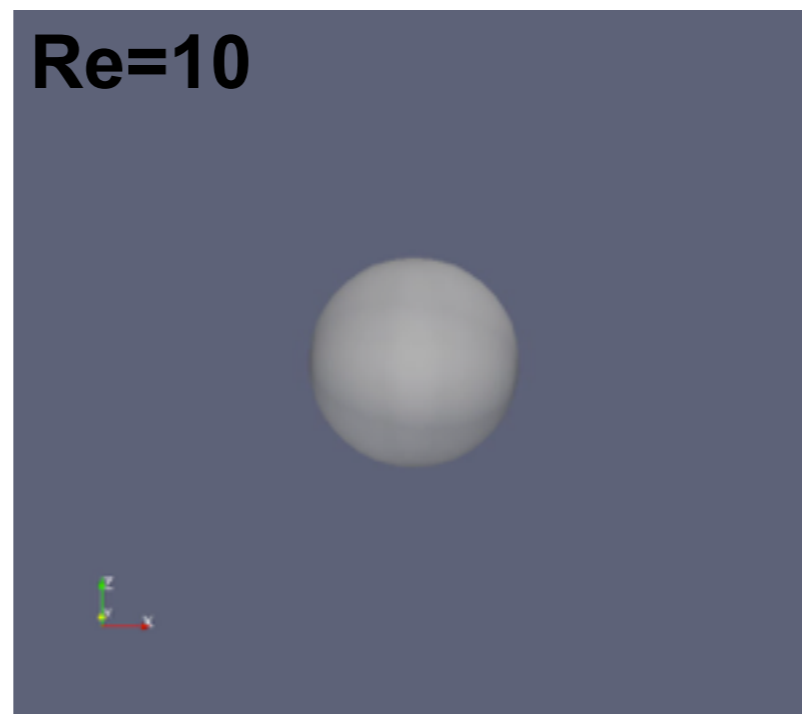
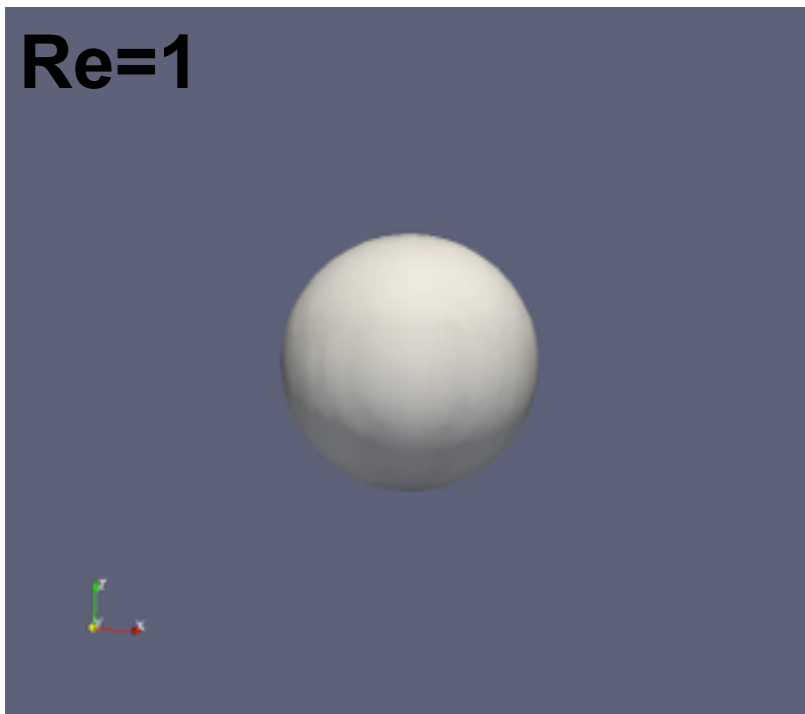
Systematic exploration for $(\text{Re}, \text{We}) = [10^{-3} - 10^3]$ and beyond:

⇒ **~200+ experiments**

Influence of inertia vs. viscous effects (Re)

$We \rightarrow \infty$ (no surface tension)

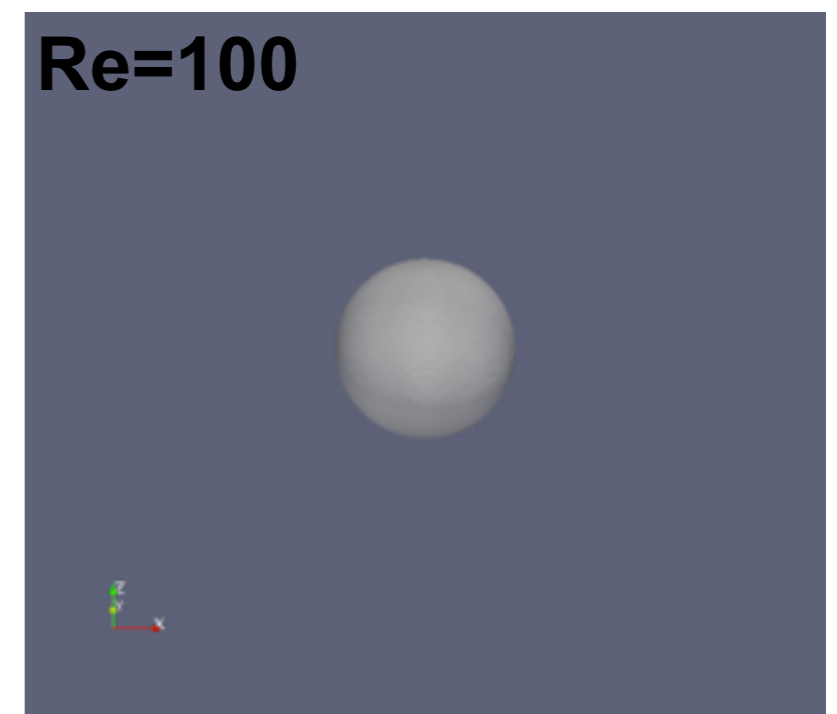
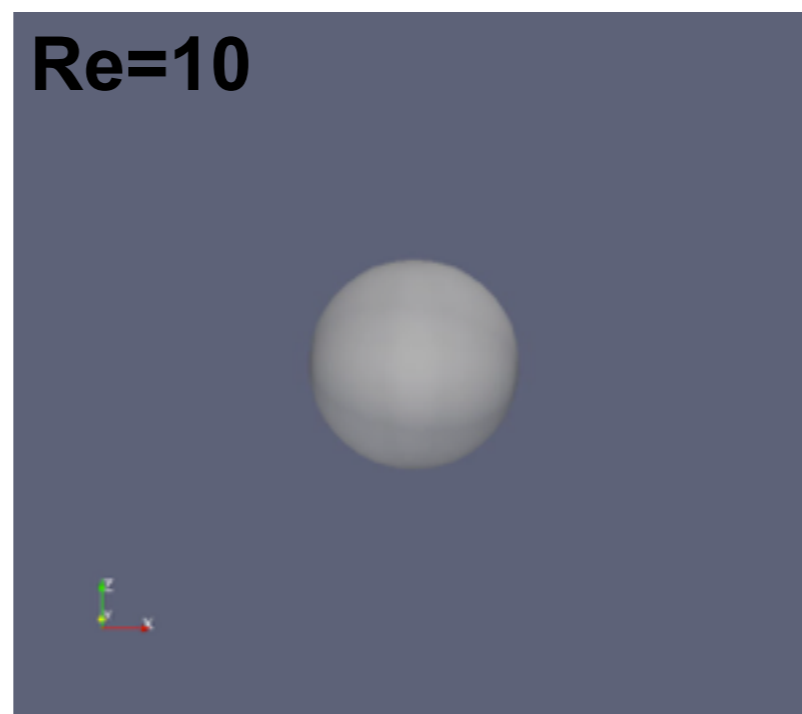
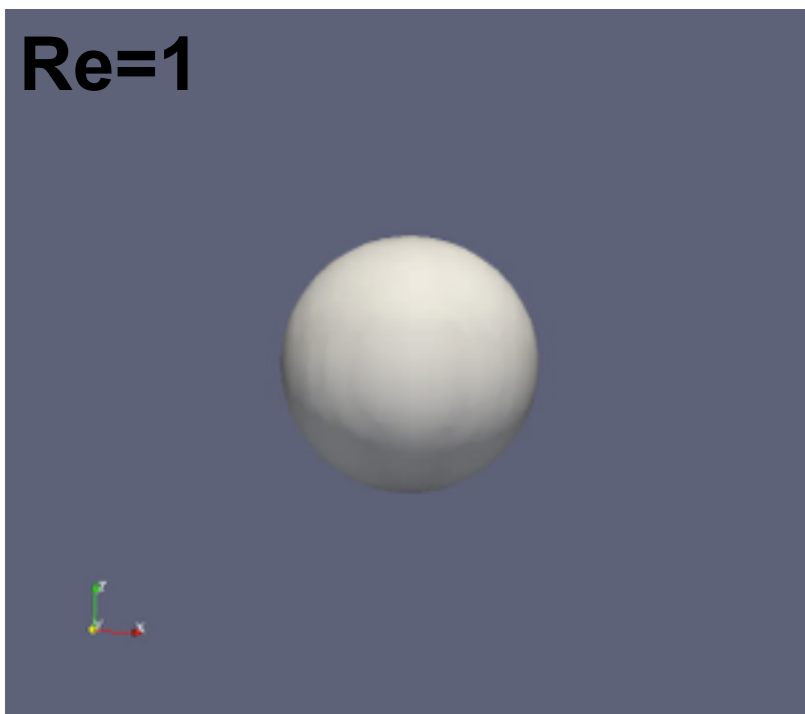
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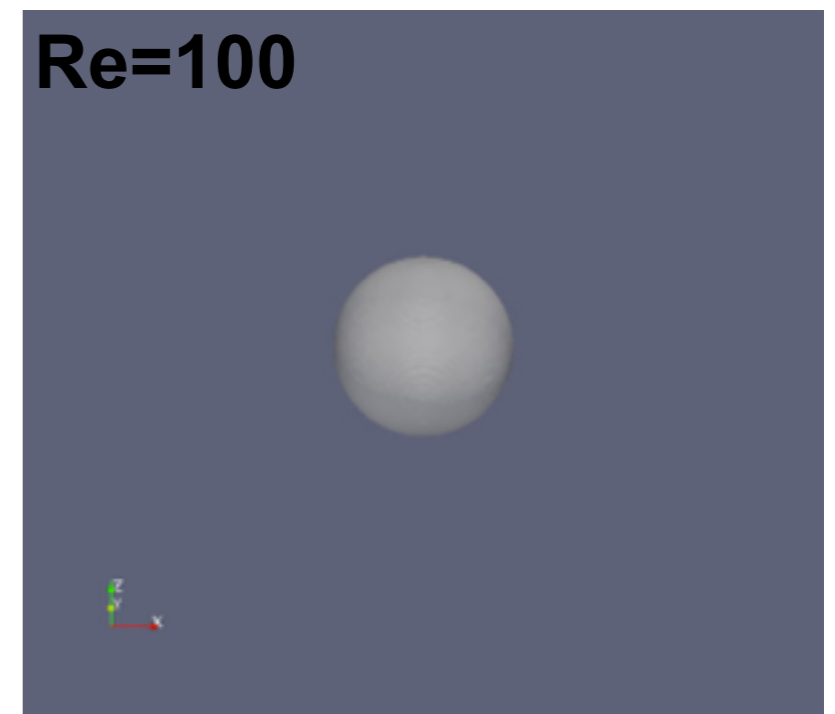
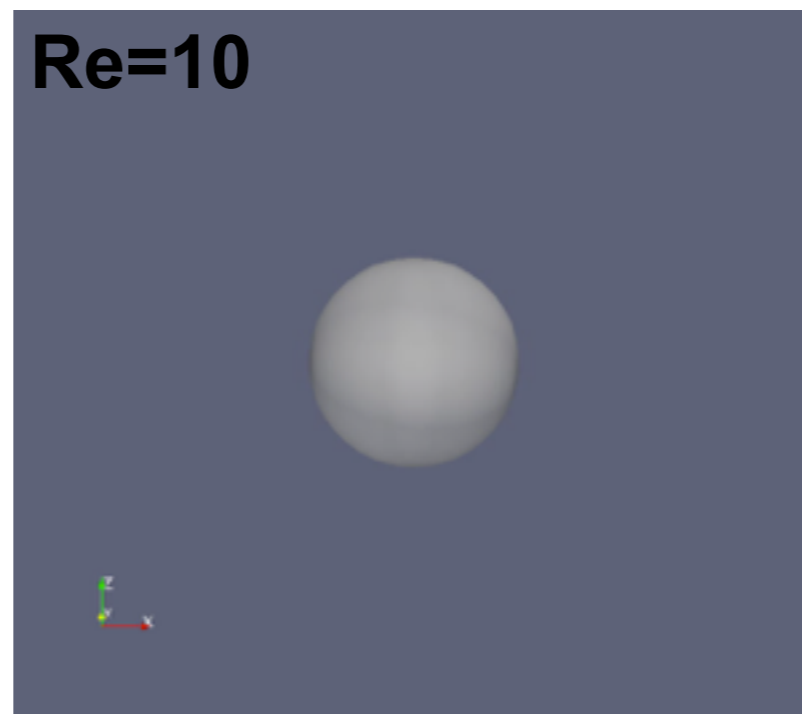
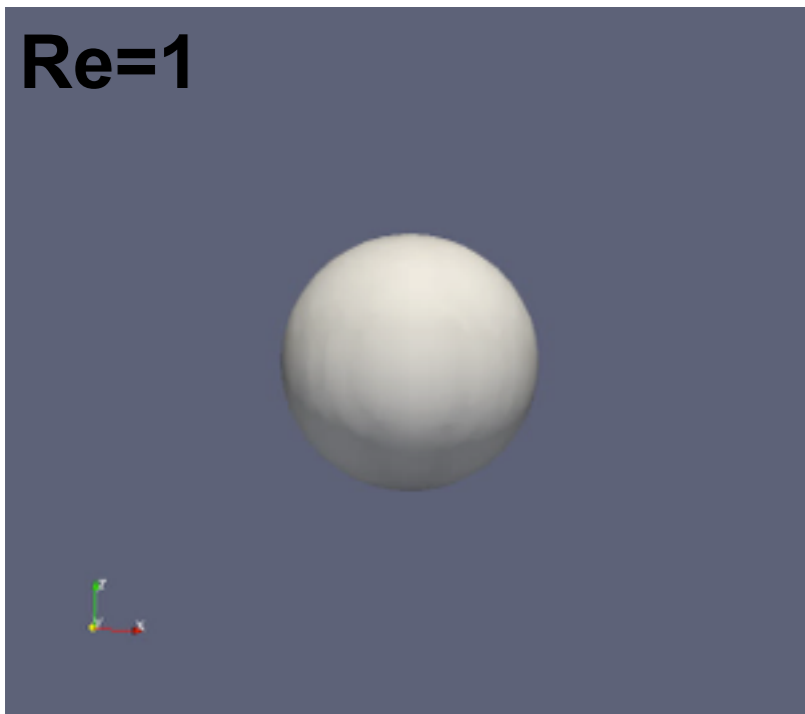
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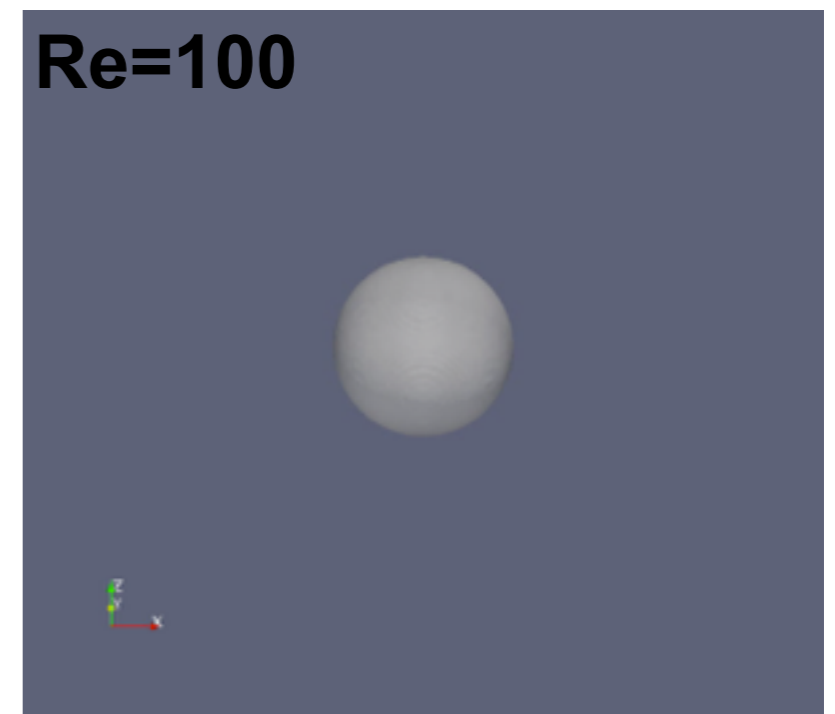
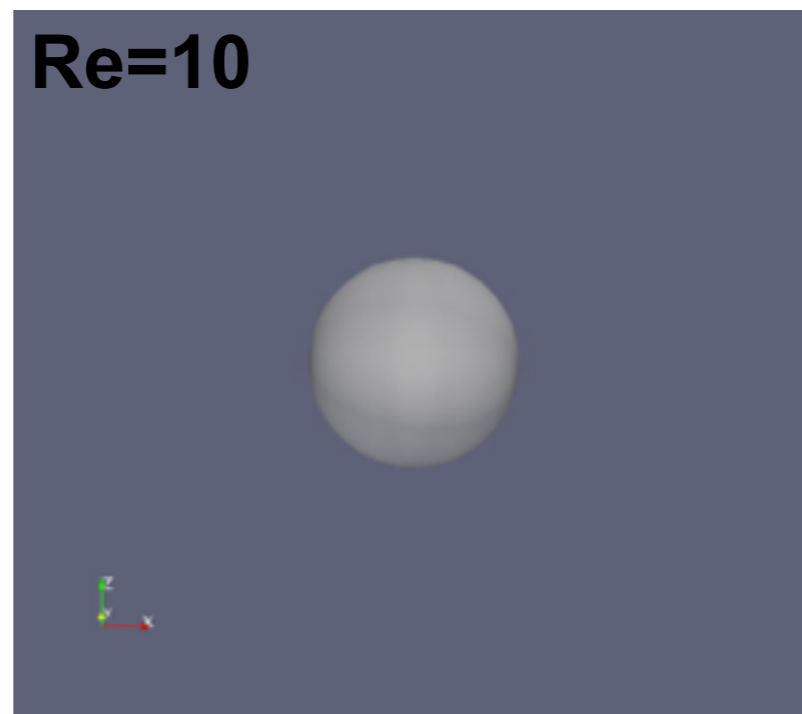
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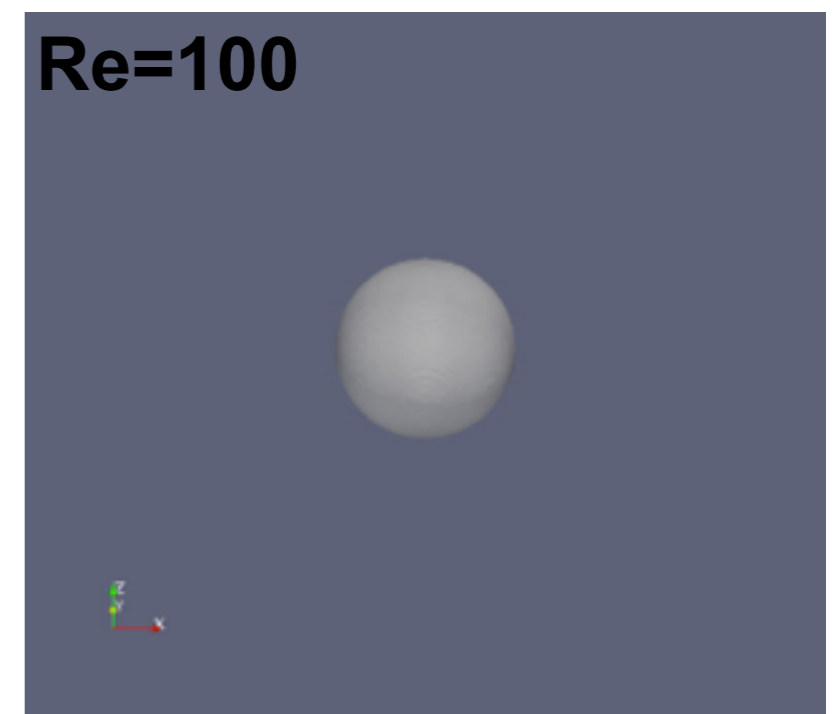
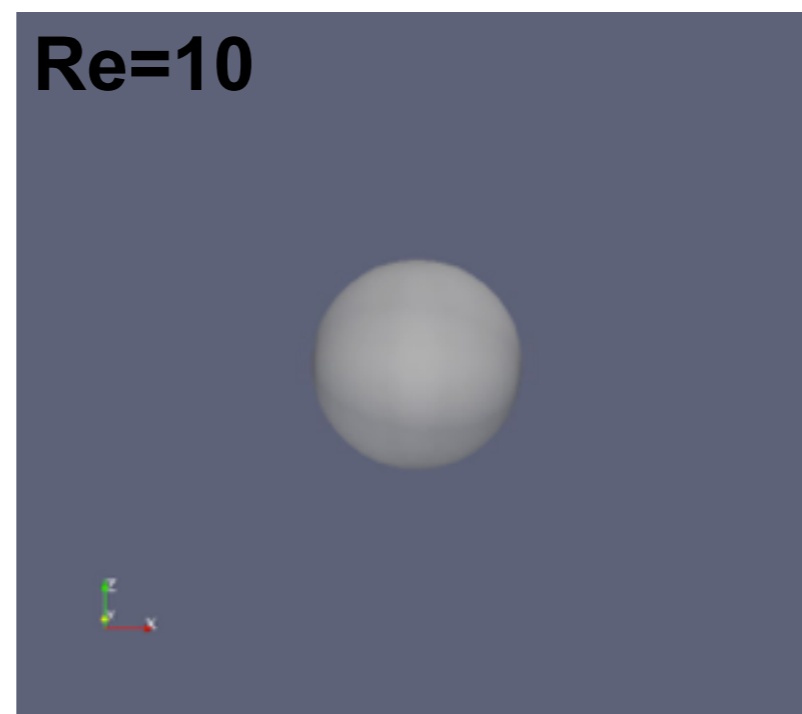
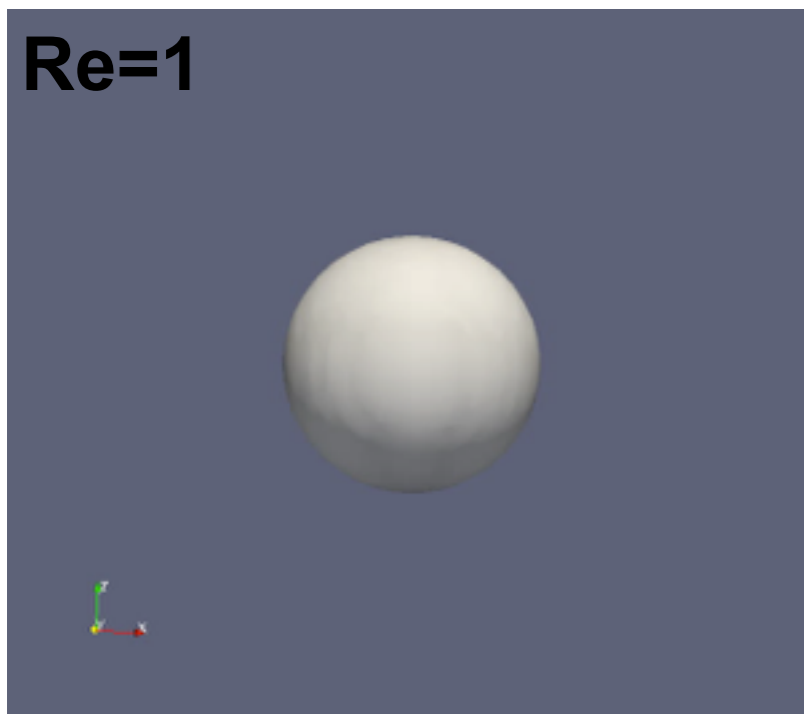
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Influence of inertia vs. viscous effects (Re)

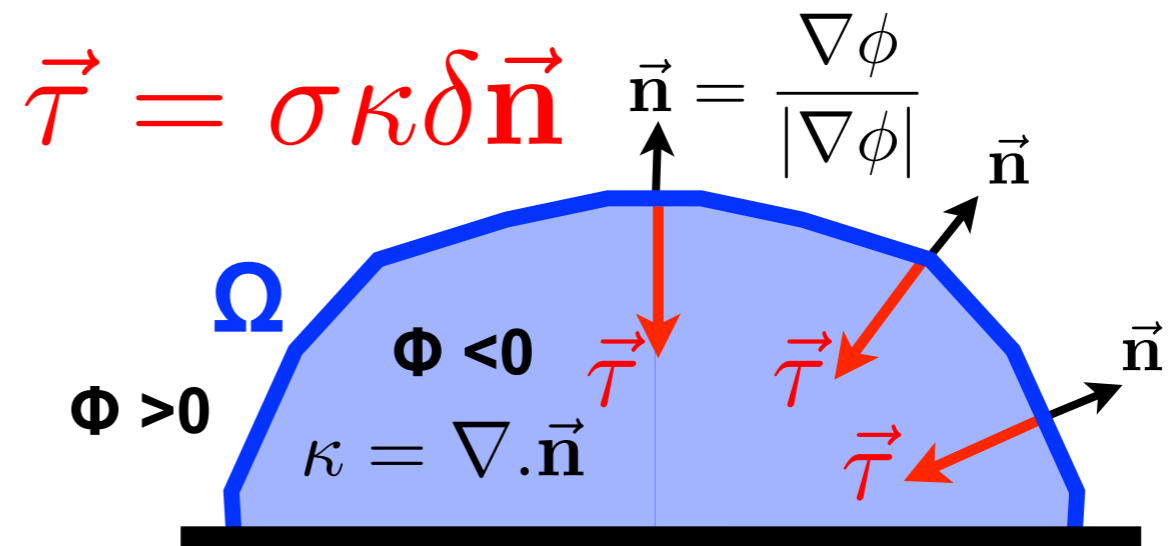
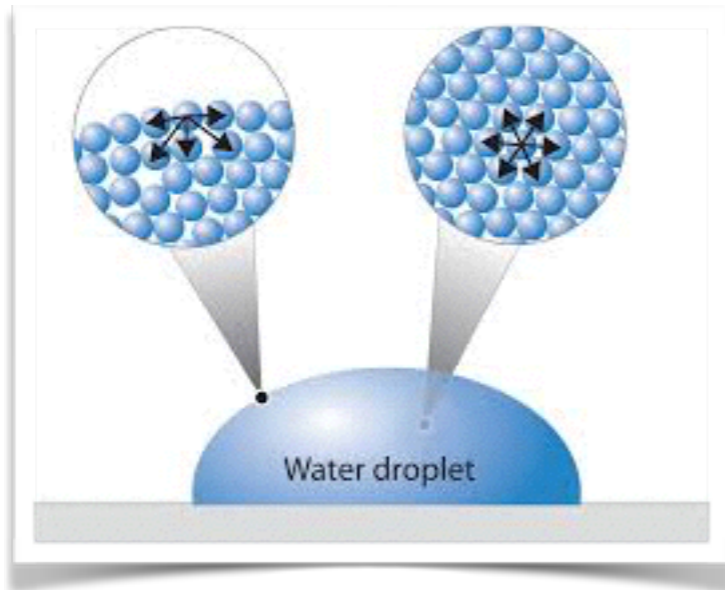
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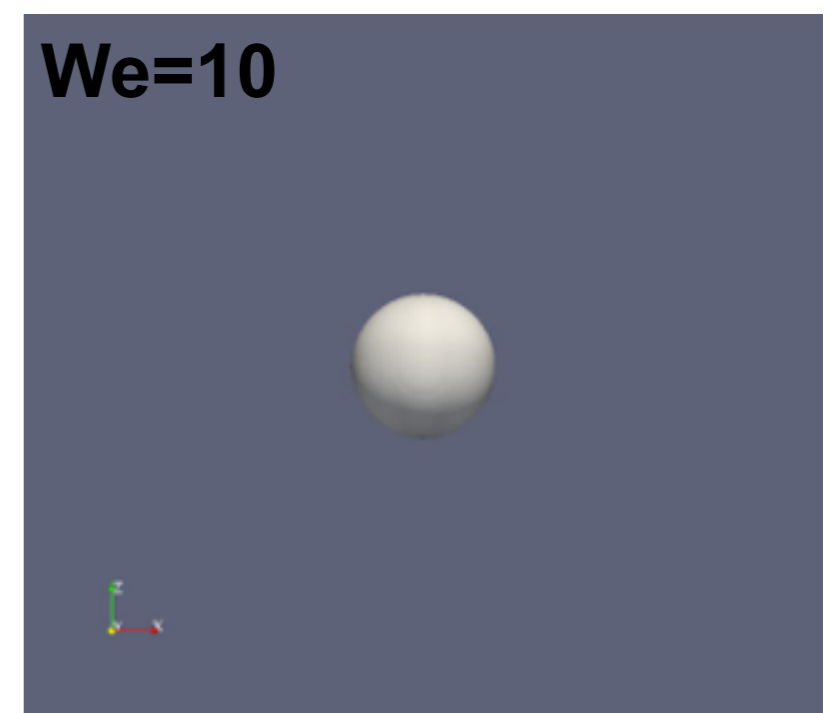
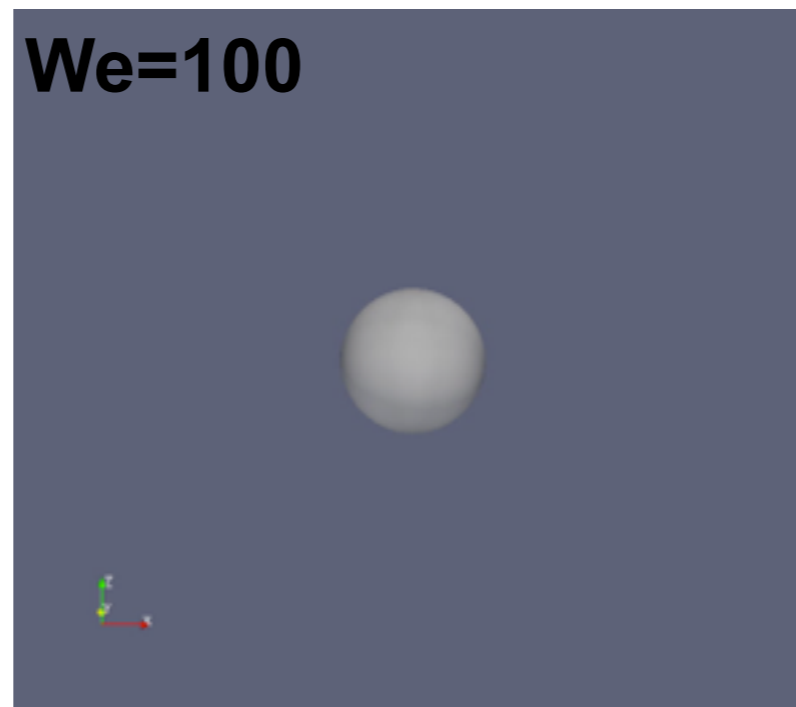
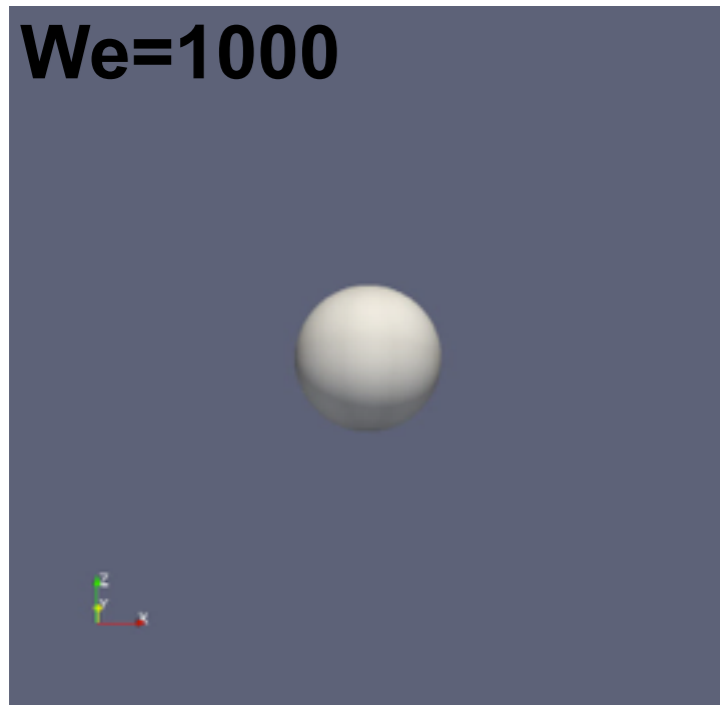
Large Re (small viscous effects) favour breakup
Post-breakup diapir sizes decrease with increasing Re

Influence of surface tension (We)

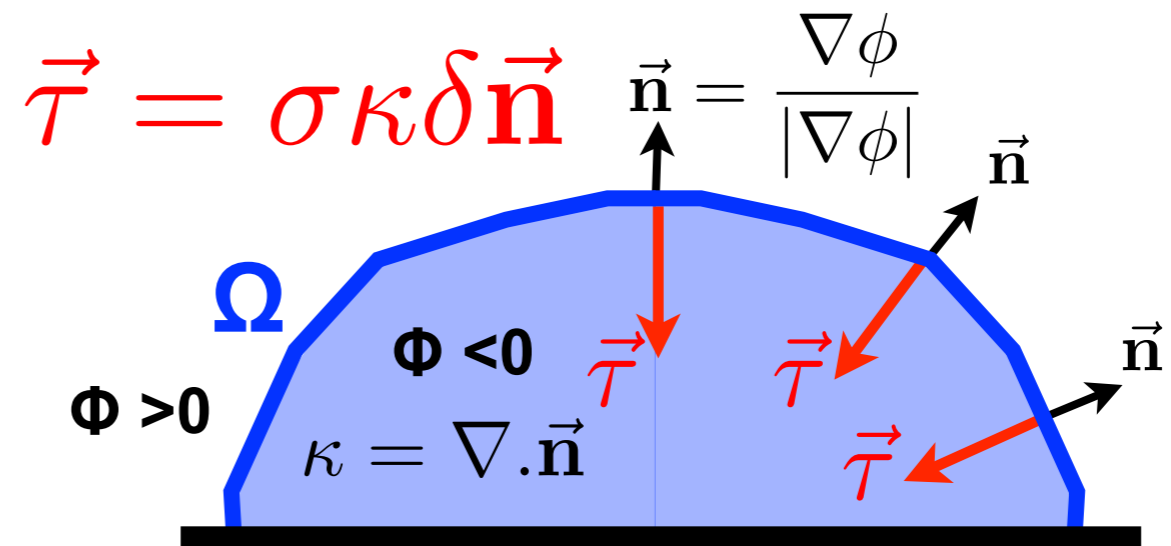
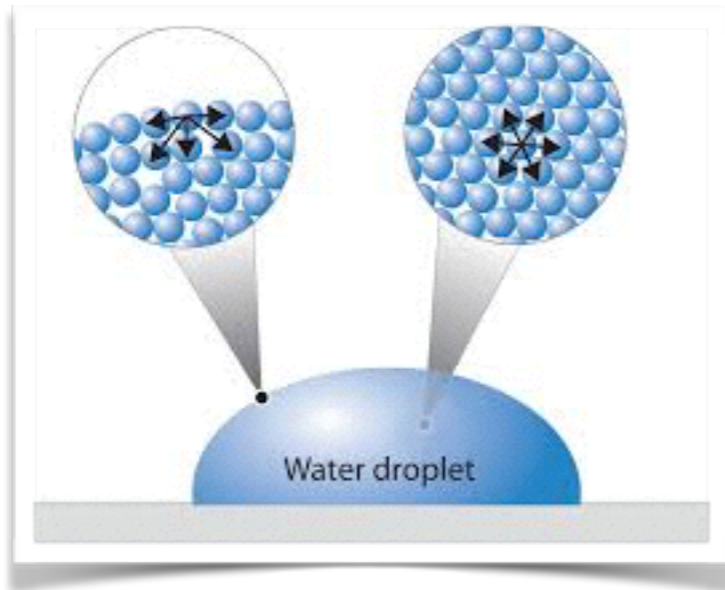


We = Inertia / Surface tension: $\frac{\rho_s V_\infty^2 R}{\sigma}$

$Re=100$

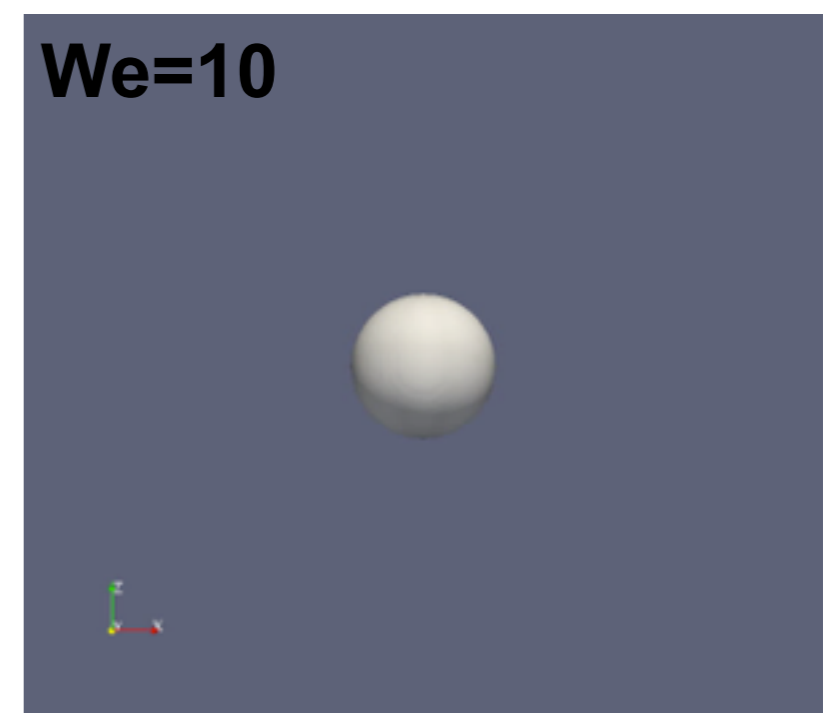
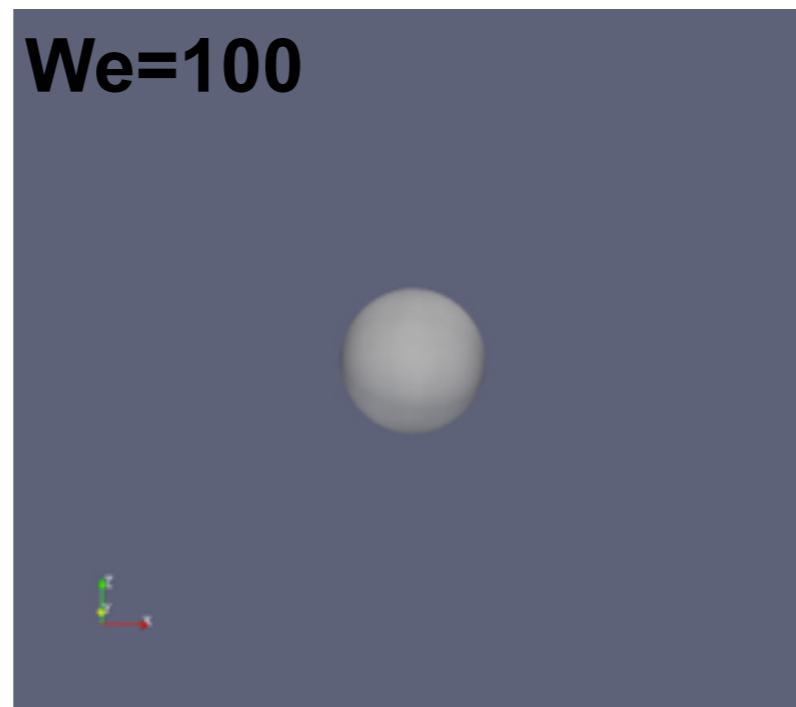
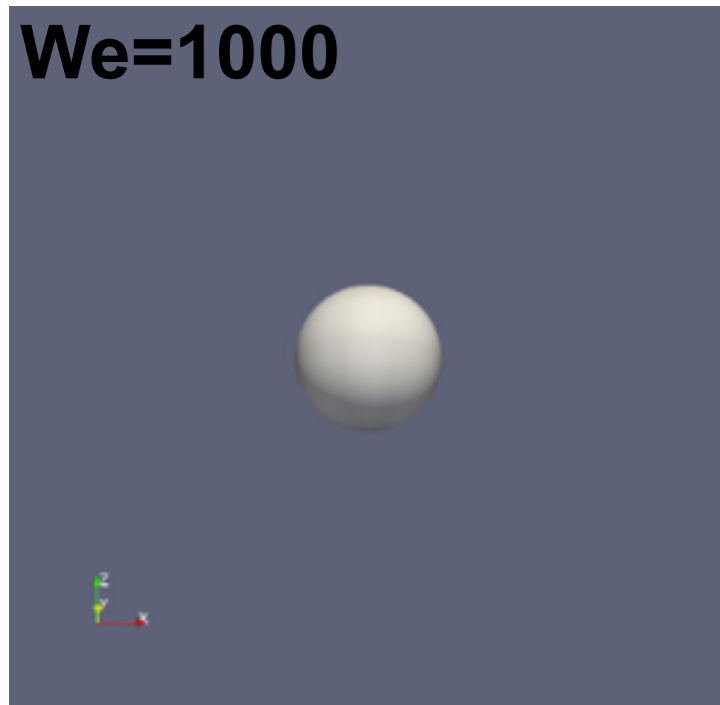


Influence of surface tension (We)

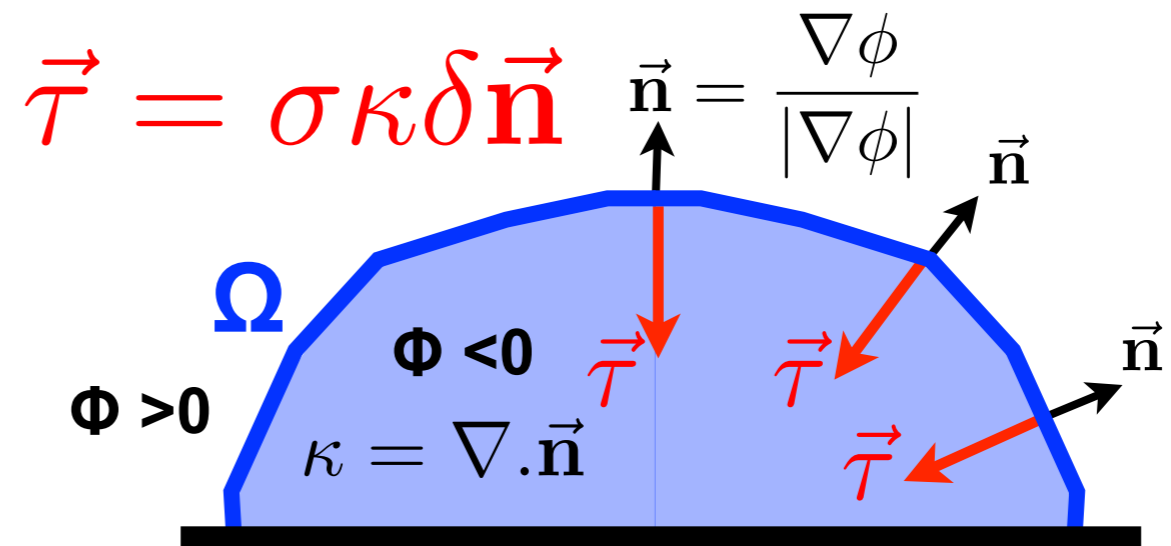
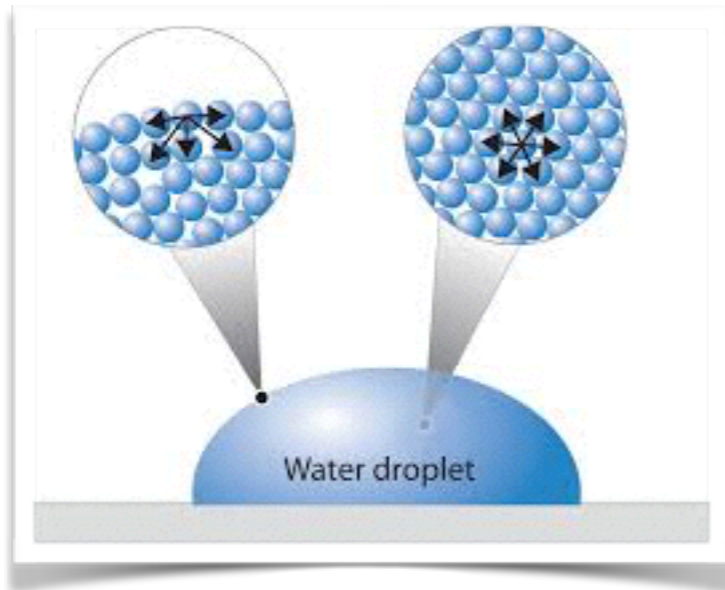


We = Inertia / Surface tension:
$$\frac{\rho_s V_\infty^2 R}{\sigma}$$

Re=100

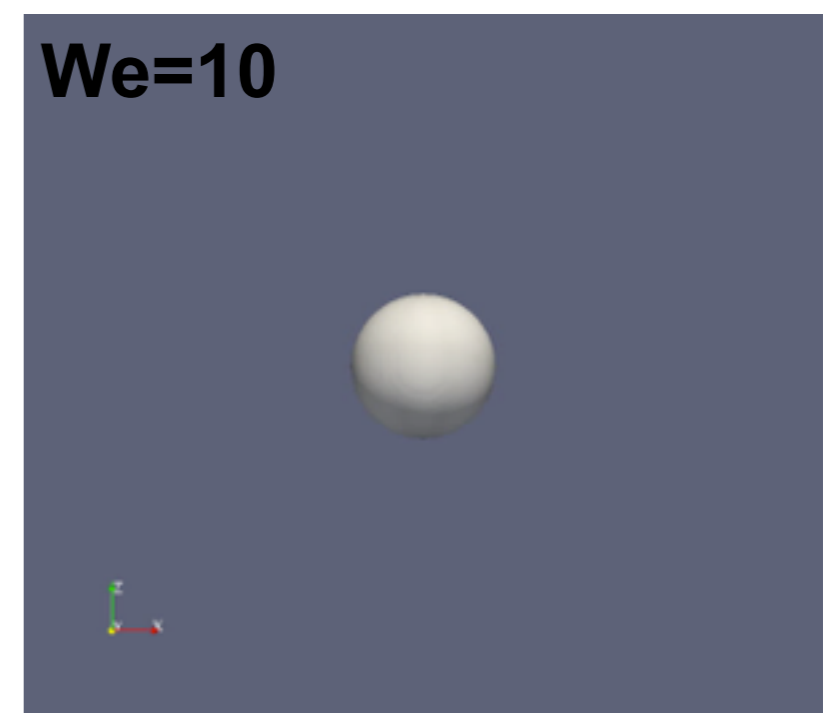
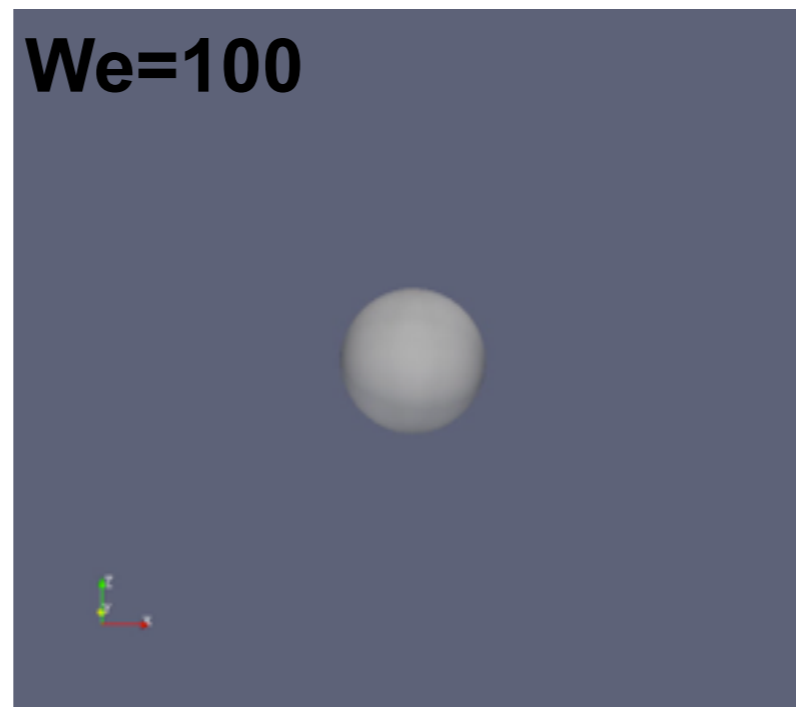
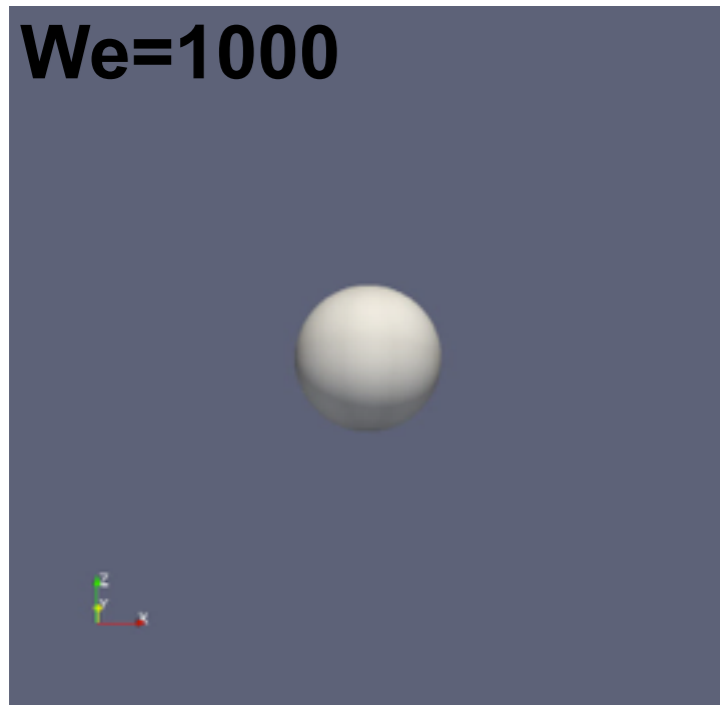


Influence of surface tension (We)

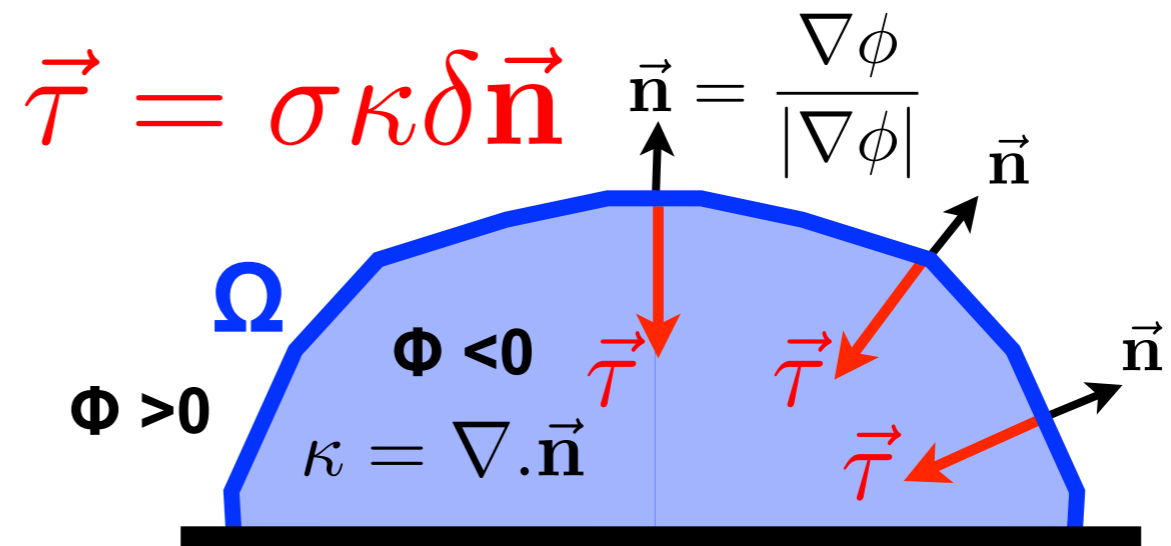
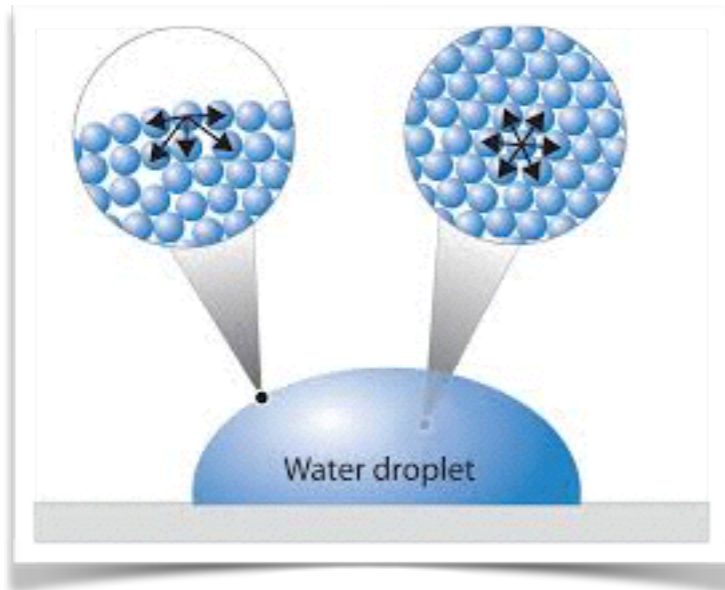


We = Inertia / Surface tension: $\frac{\rho_s V_\infty^2 R}{\sigma}$

$Re=100$

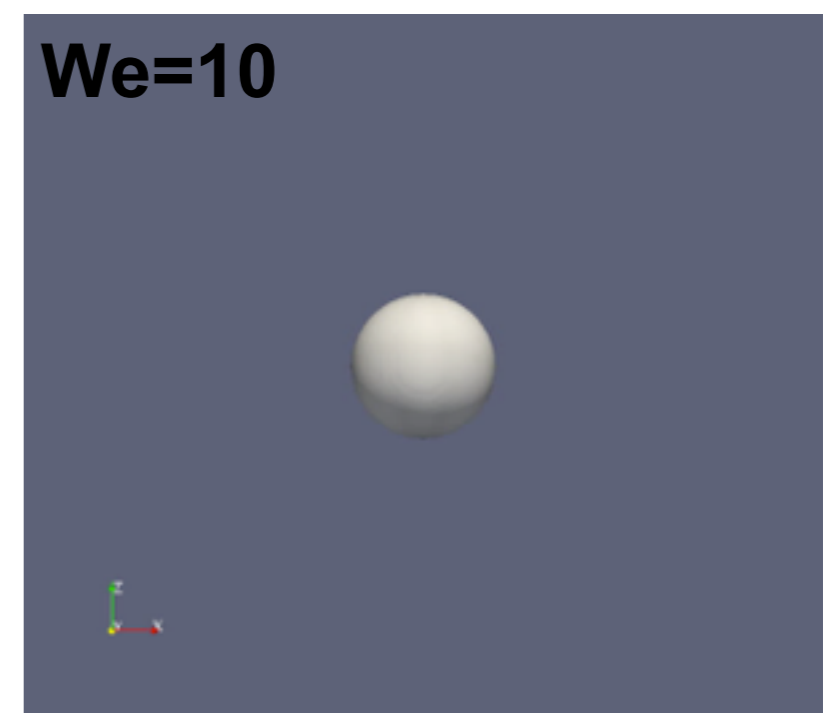
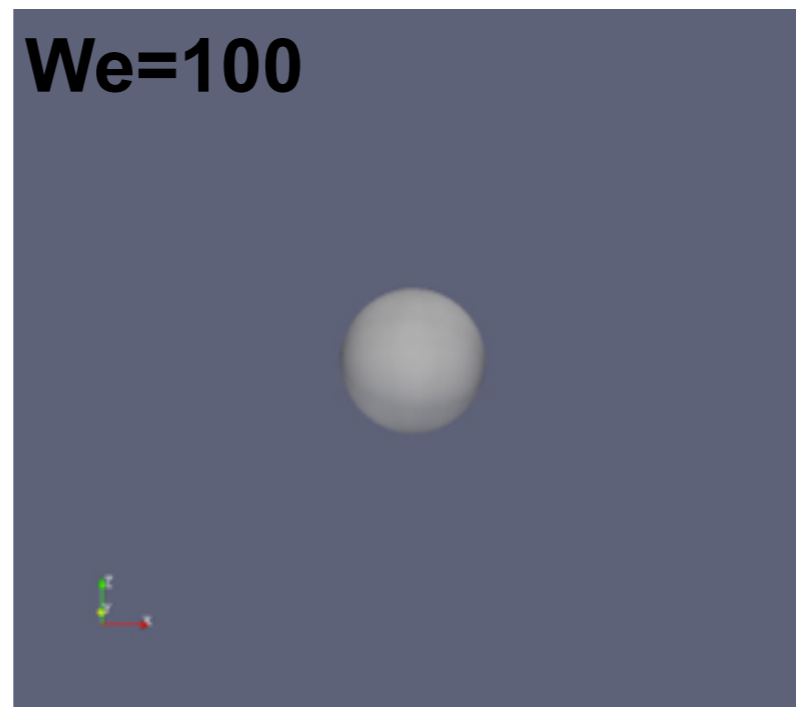
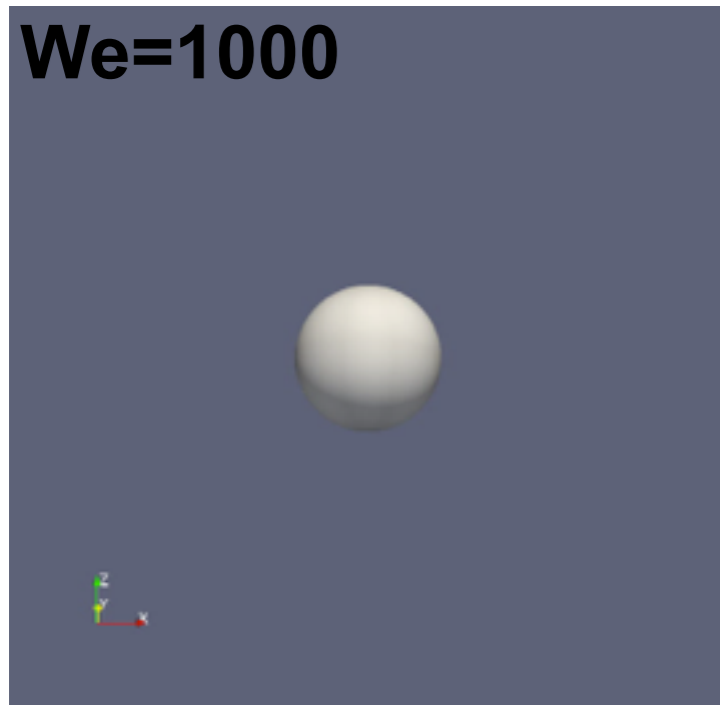


Influence of surface tension (We)

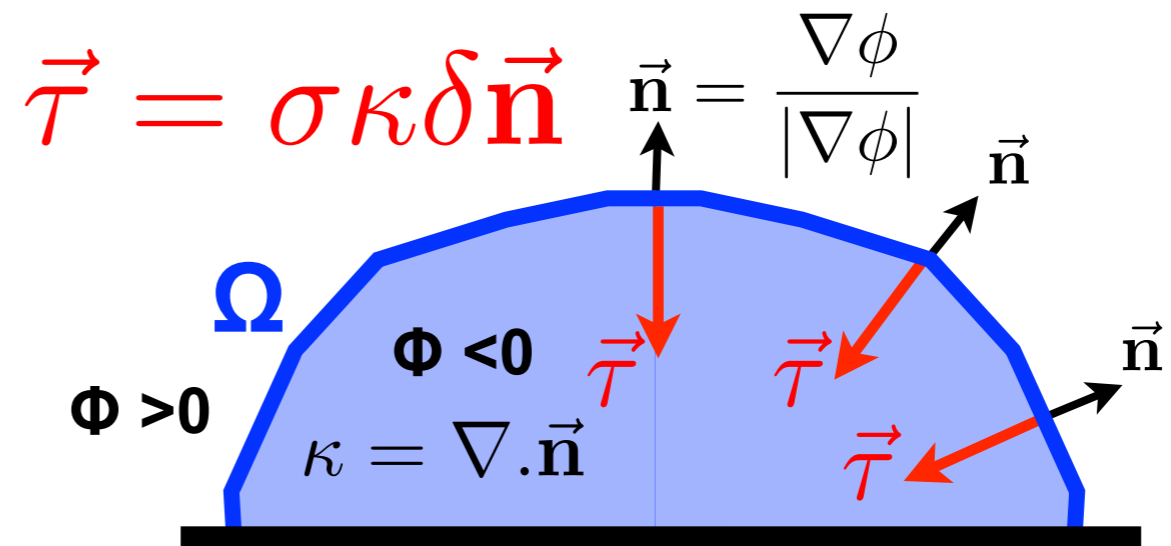
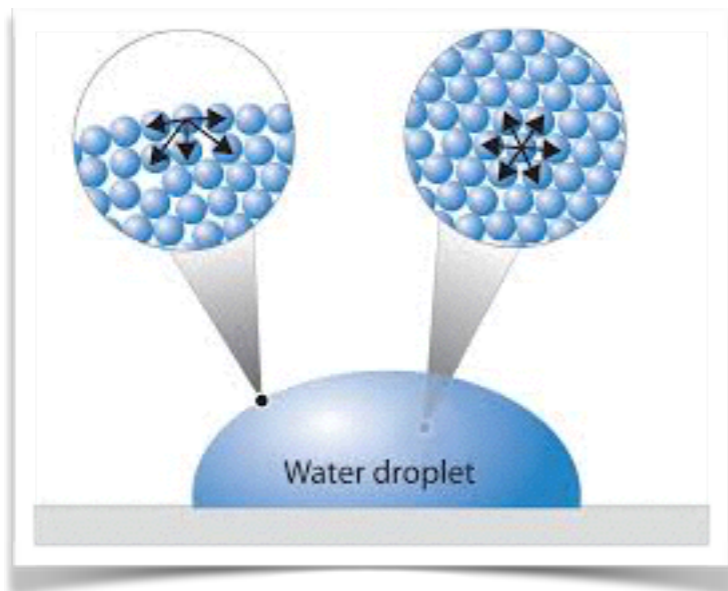


We = Inertia / Surface tension: $\frac{\rho_s V_\infty^2 R}{\sigma}$

Re = 100

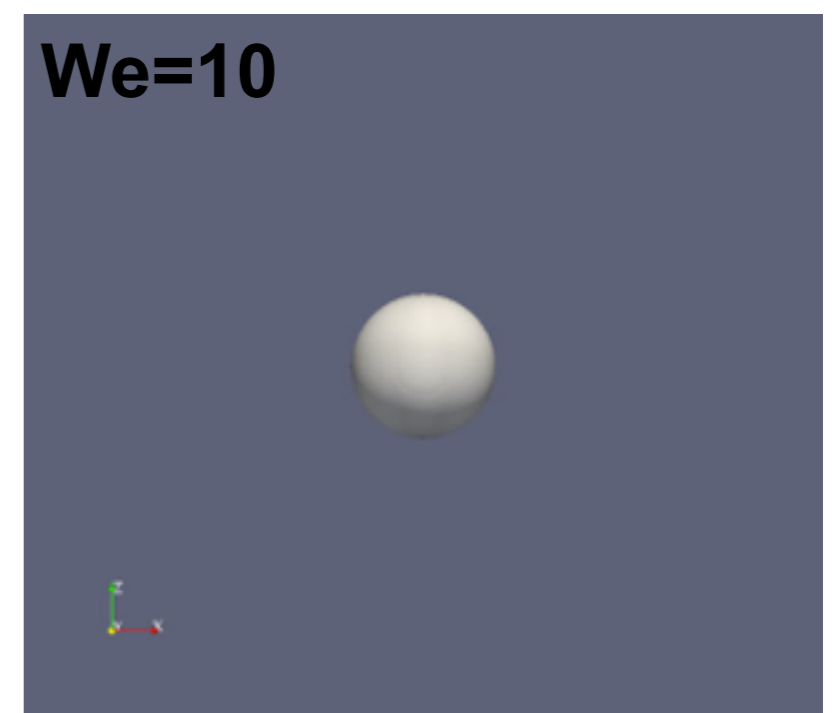
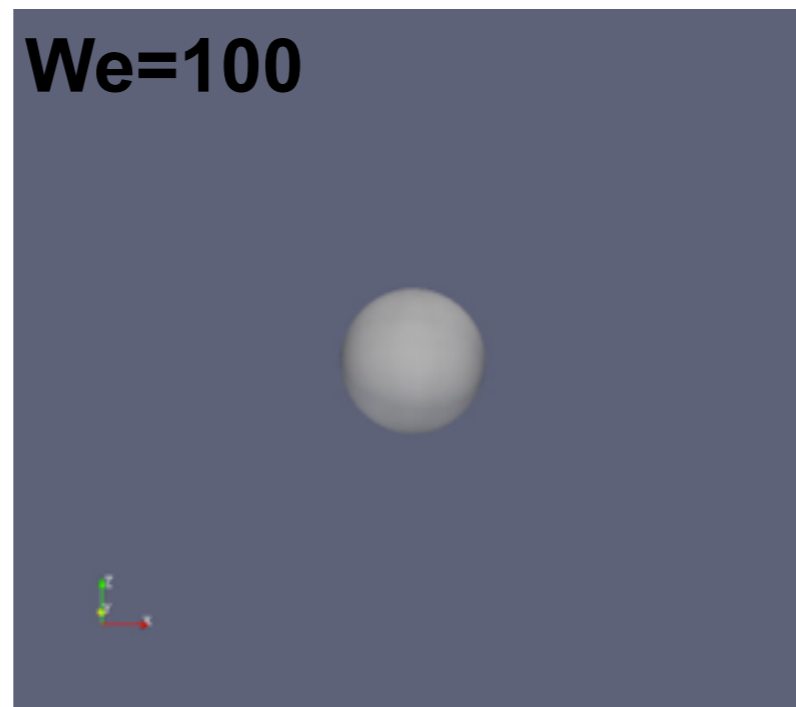
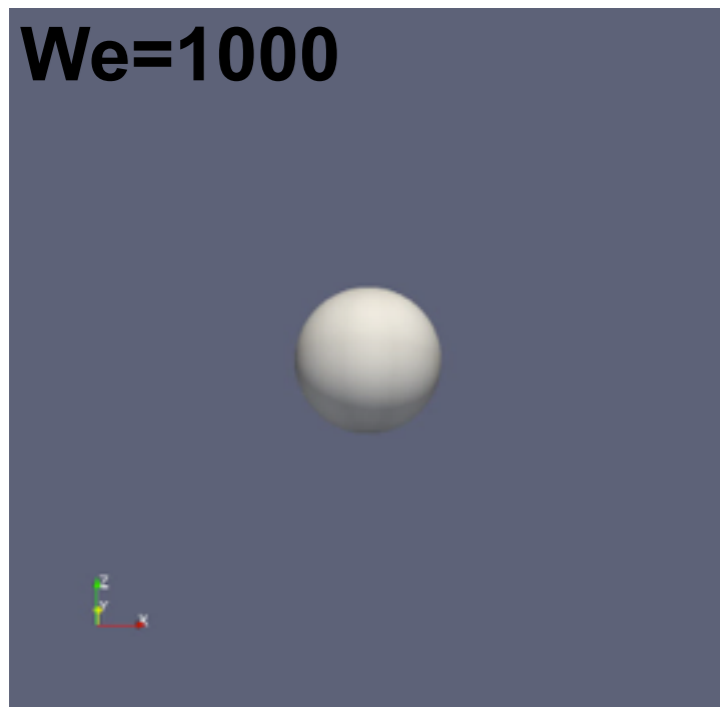


Influence of surface tension (We)



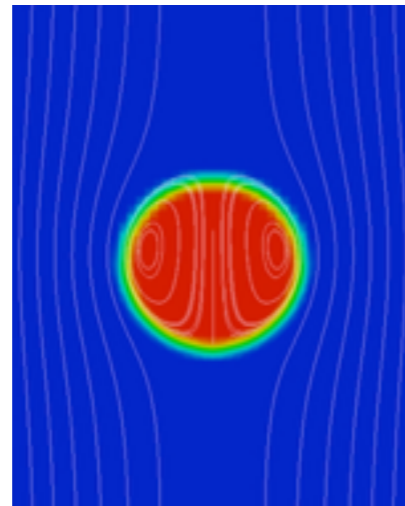
We = Inertia / Surface tension: $\frac{\rho_s V_\infty^2 R}{\sigma}$

Re=100



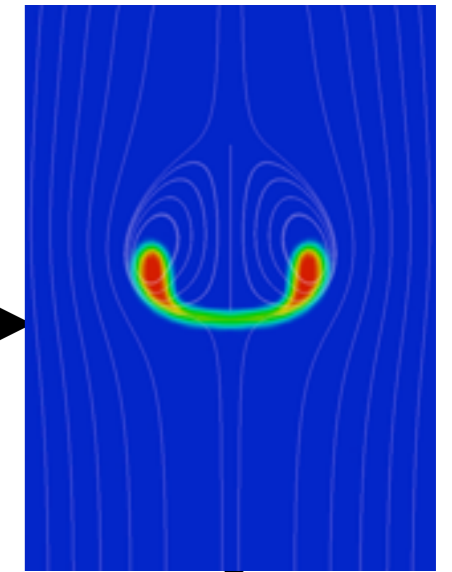
Small We (strong surface tension) efficiently reduces/prevents breakup

Experimental breakup / Stability criterion



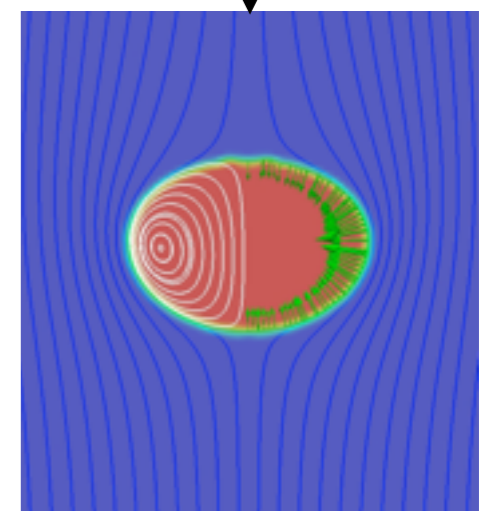
Increasing

$$Re = \frac{\rho v R}{\eta}$$



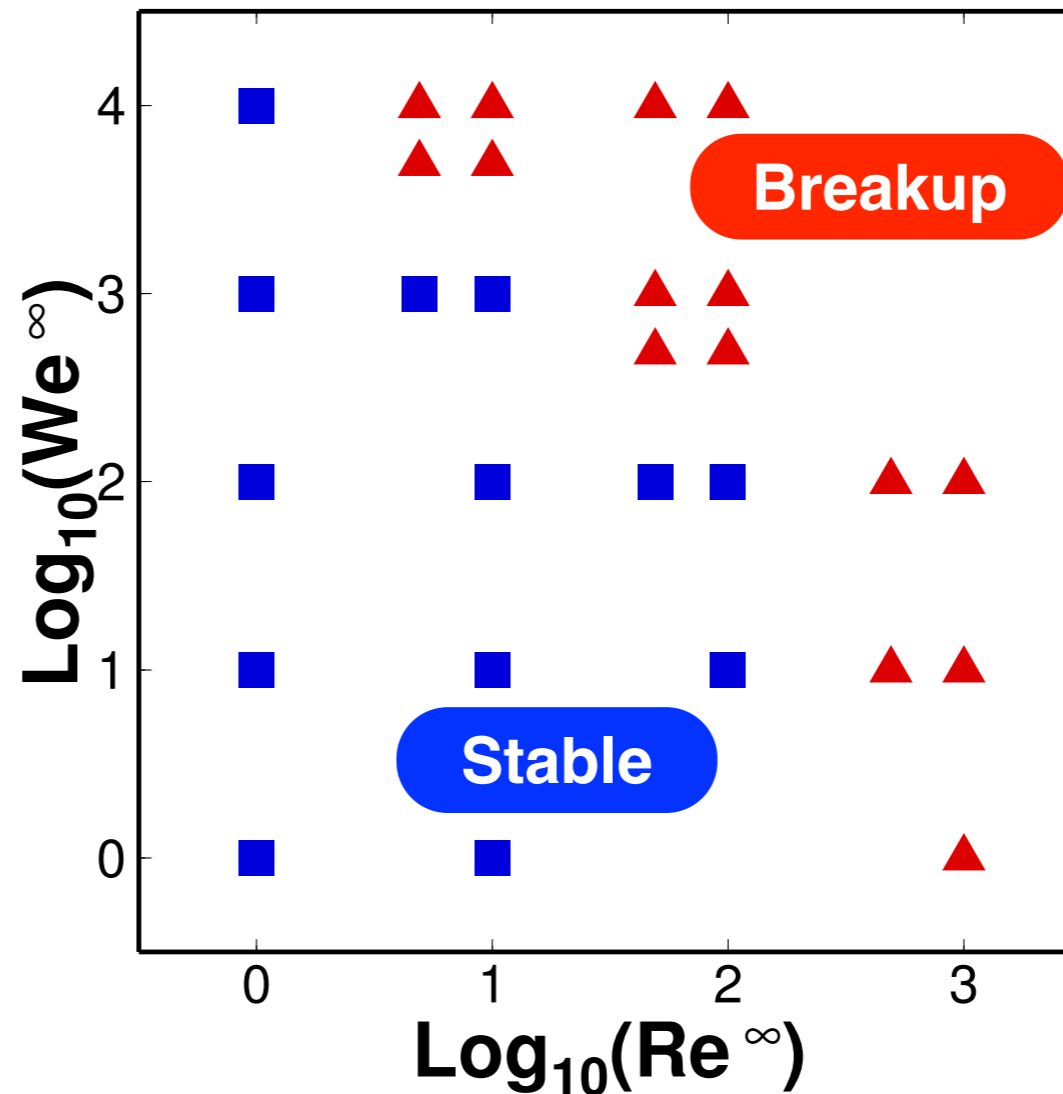
Decreasing

$$We = \frac{\rho v^2 R}{\gamma}$$

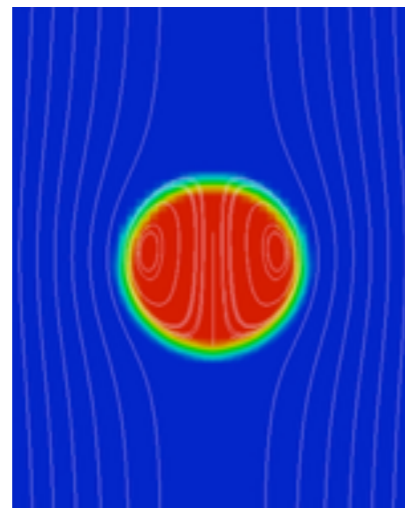


Theoretical breakup criterion

$$\frac{a_1}{Re^\infty} + \frac{a_2}{We^\infty} < C_D$$

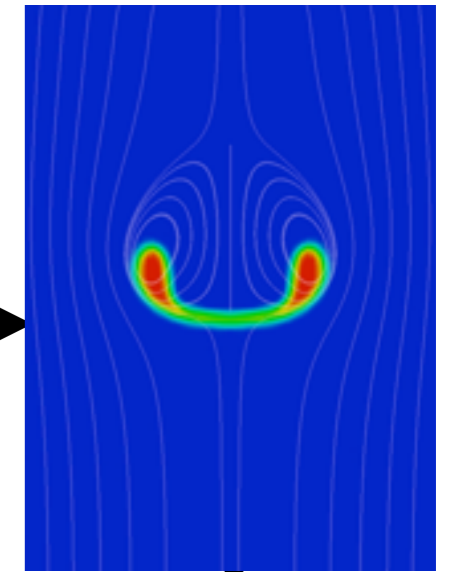


Experimental breakup / Stability criterion



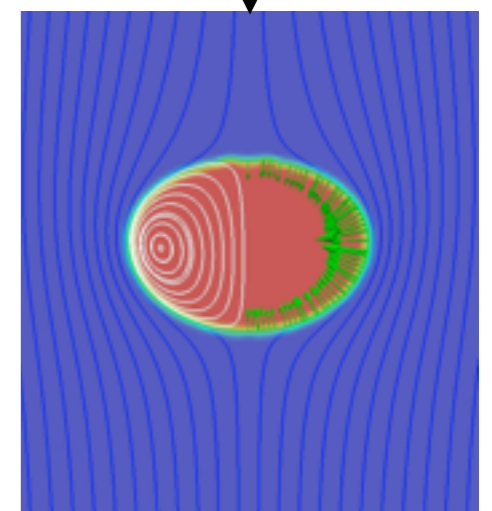
Increasing

$$Re = \frac{\rho v R}{\eta}$$



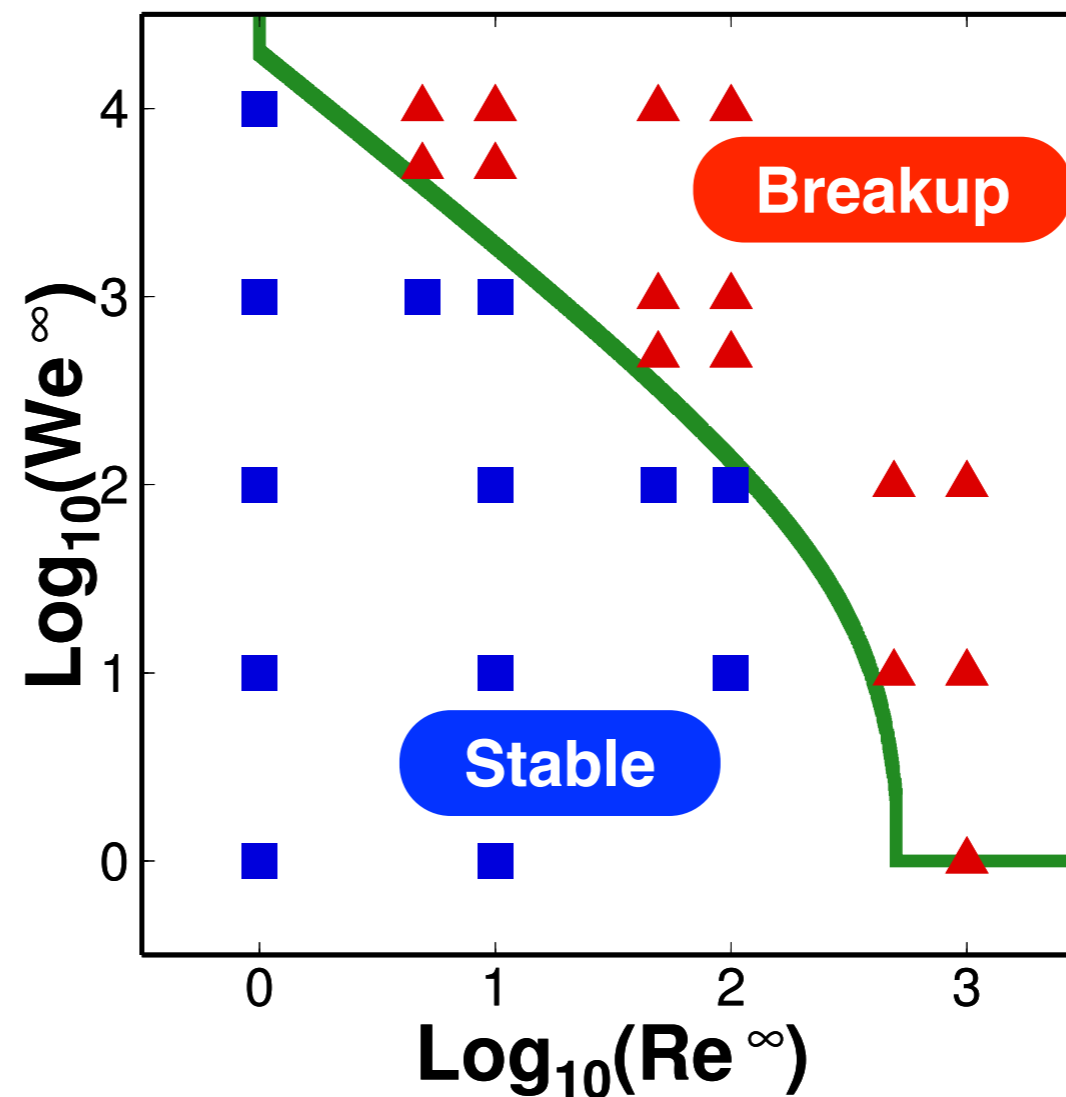
Decreasing

$$We = \frac{\rho v^2 R}{\gamma}$$

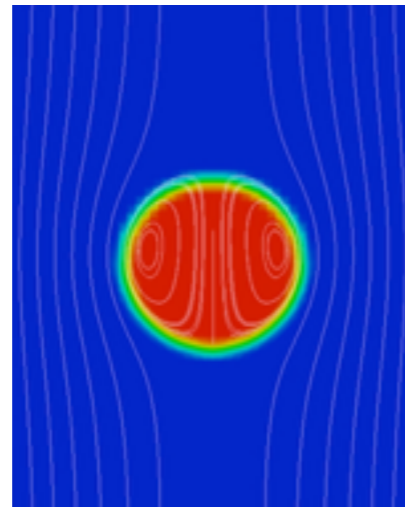


Theoretical breakup criterion

$$\frac{a_1}{Re^\infty} + \frac{a_2}{We^\infty} < C_D$$

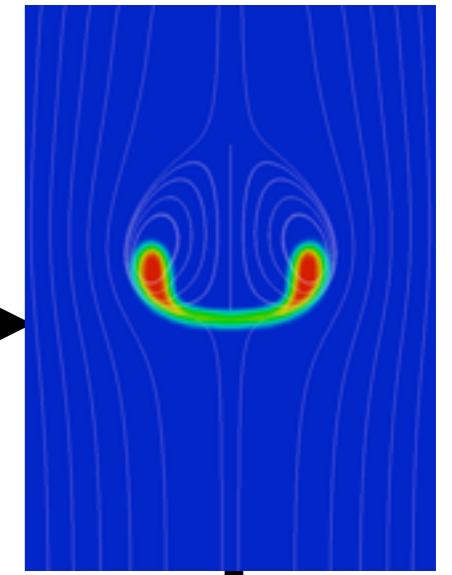


Experimental breakup / Stability criterion



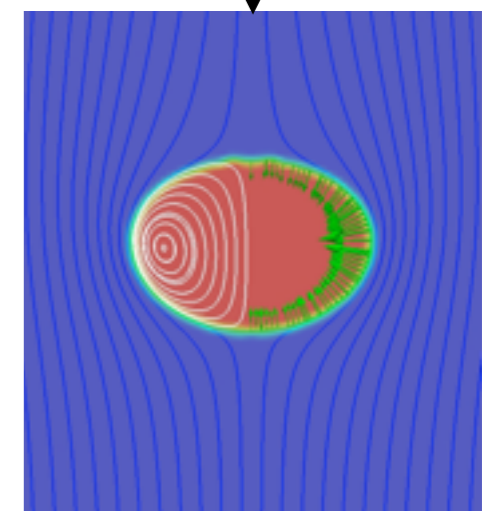
Increasing

$$Re = \frac{\rho v R}{\eta}$$



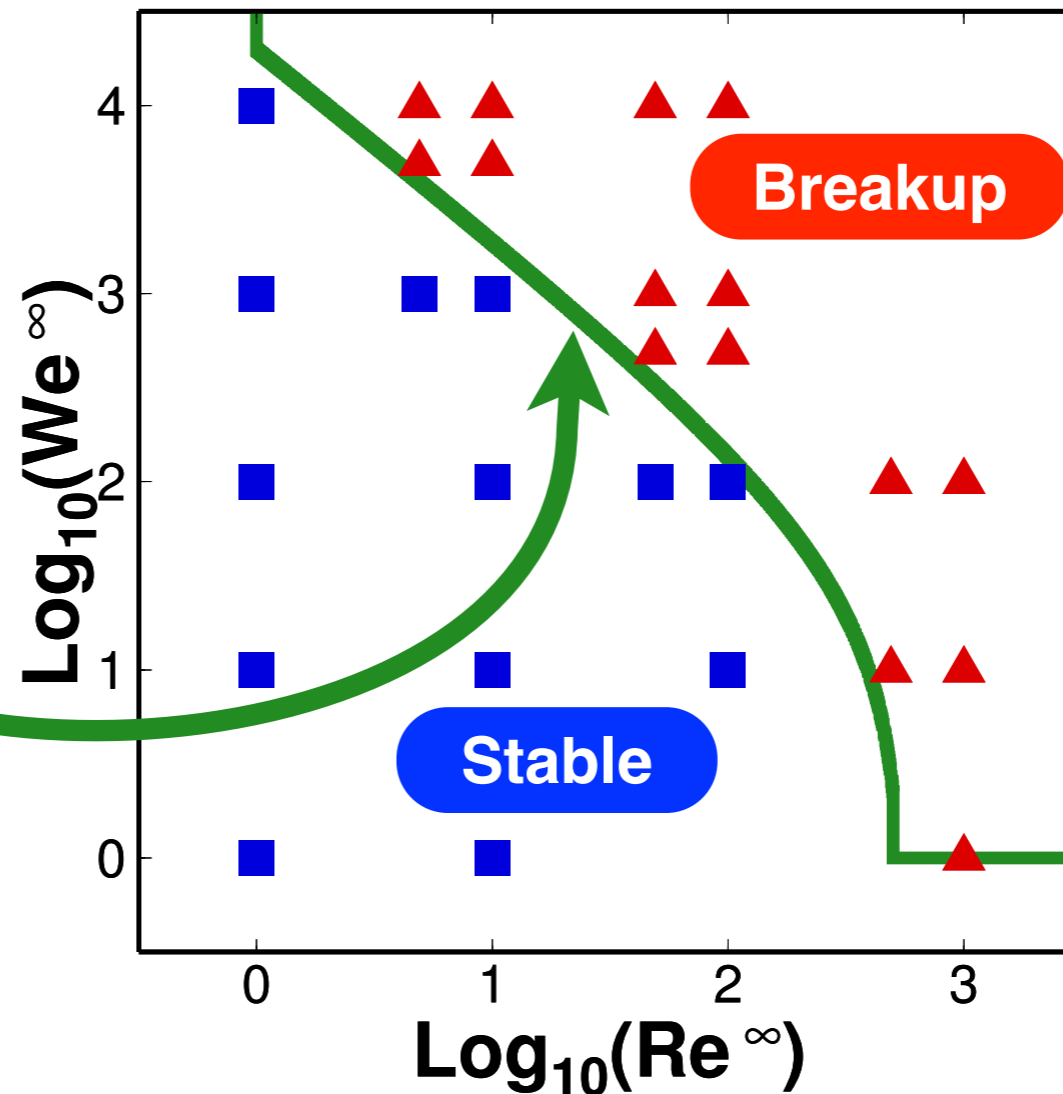
Decreasing

$$We = \frac{\rho v^2 R}{\gamma}$$

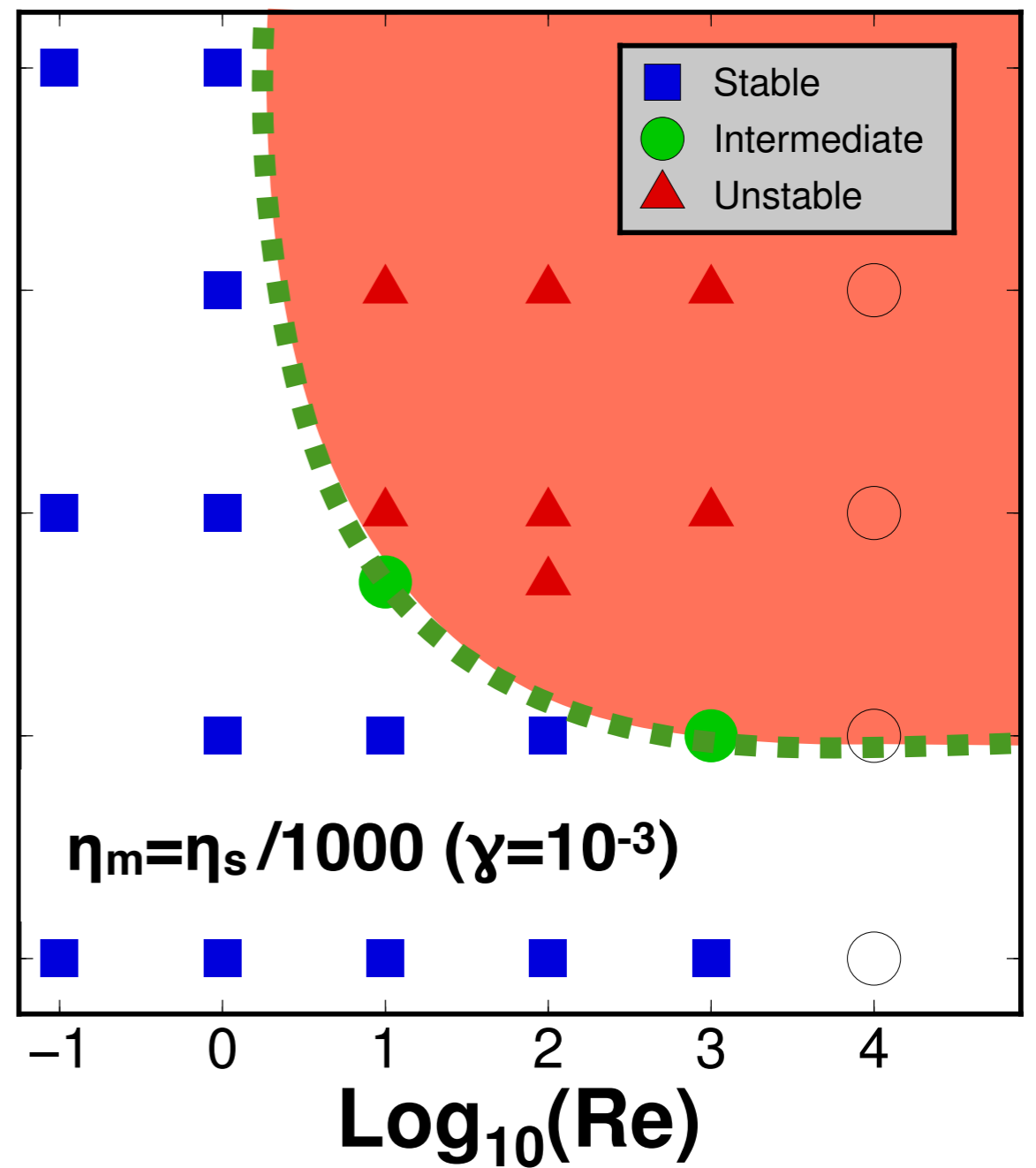
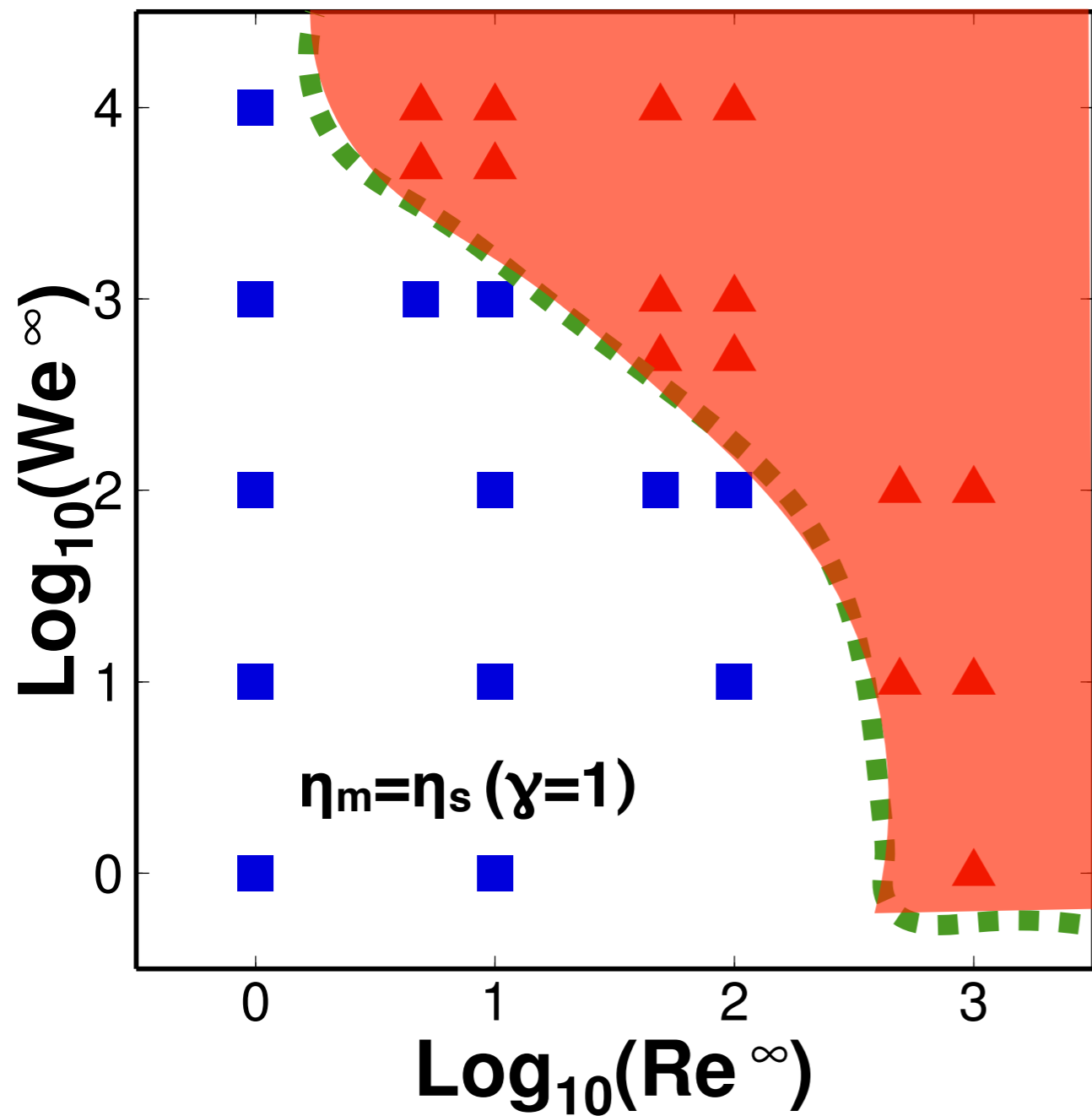


Theoretical breakup criterion

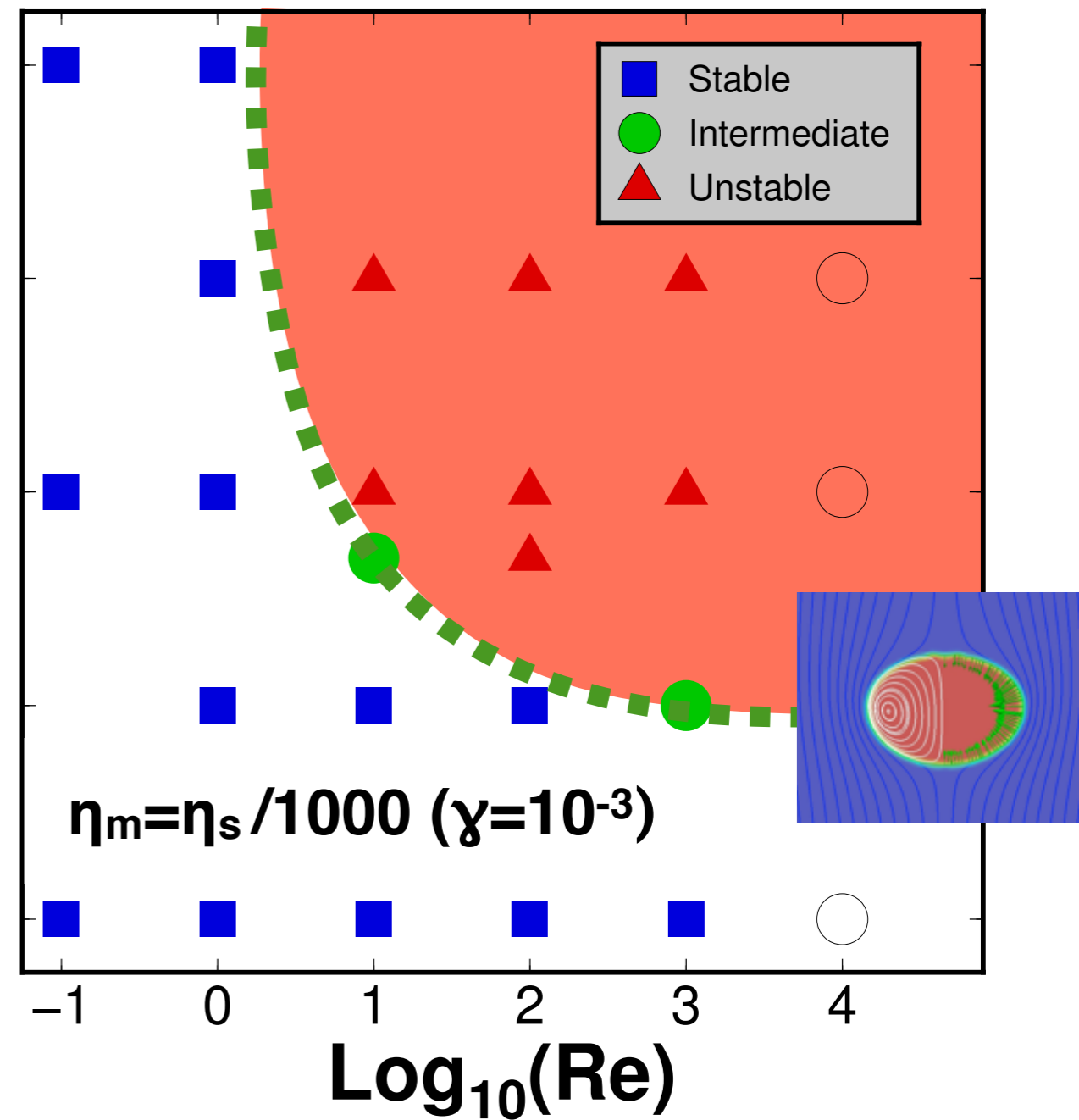
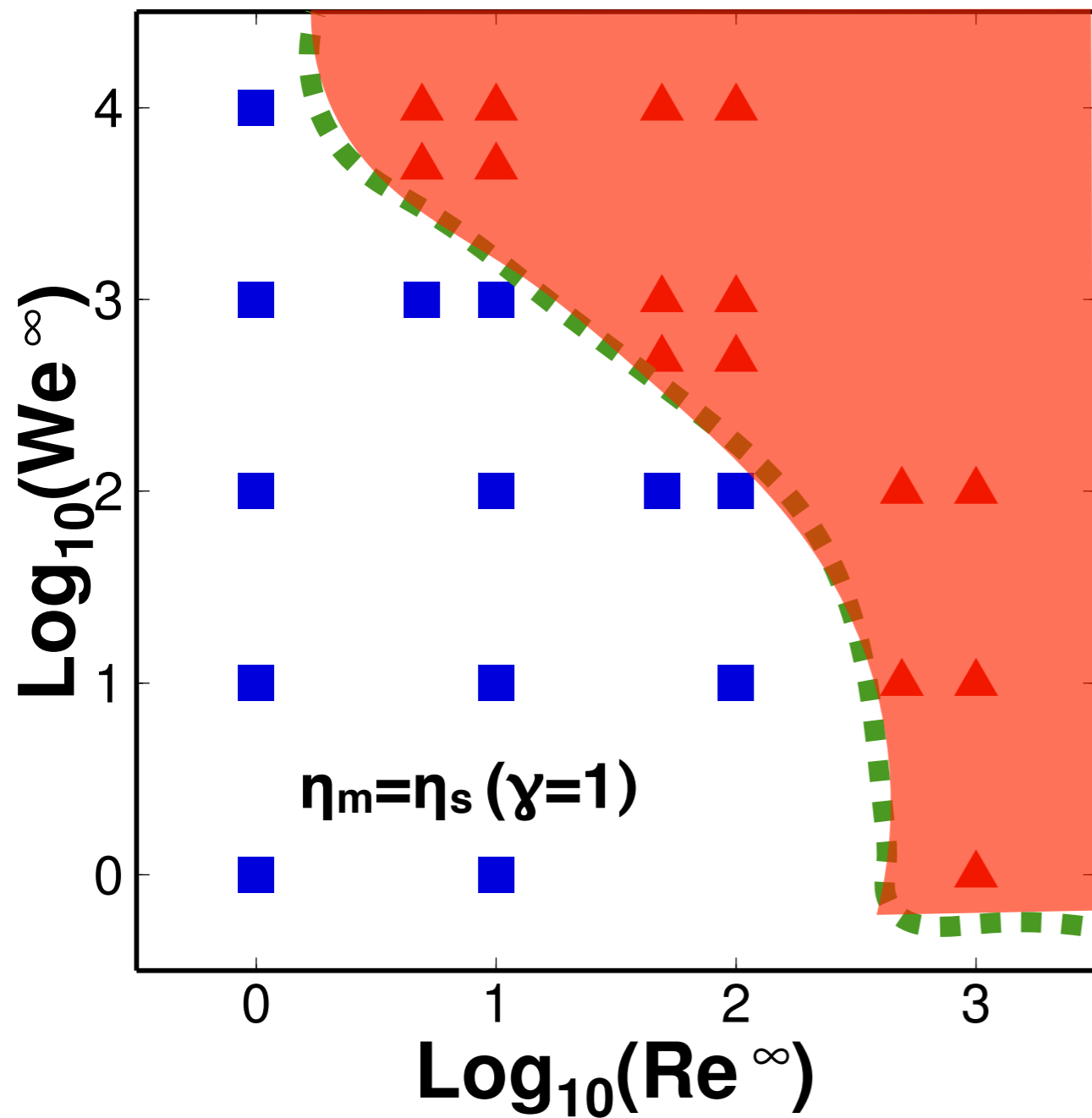
$$\frac{a_1}{Re^\infty} + \frac{a_2}{We^\infty} < C_D$$



Newtonian rheology: Influence of the Fe-Si viscosity contrast

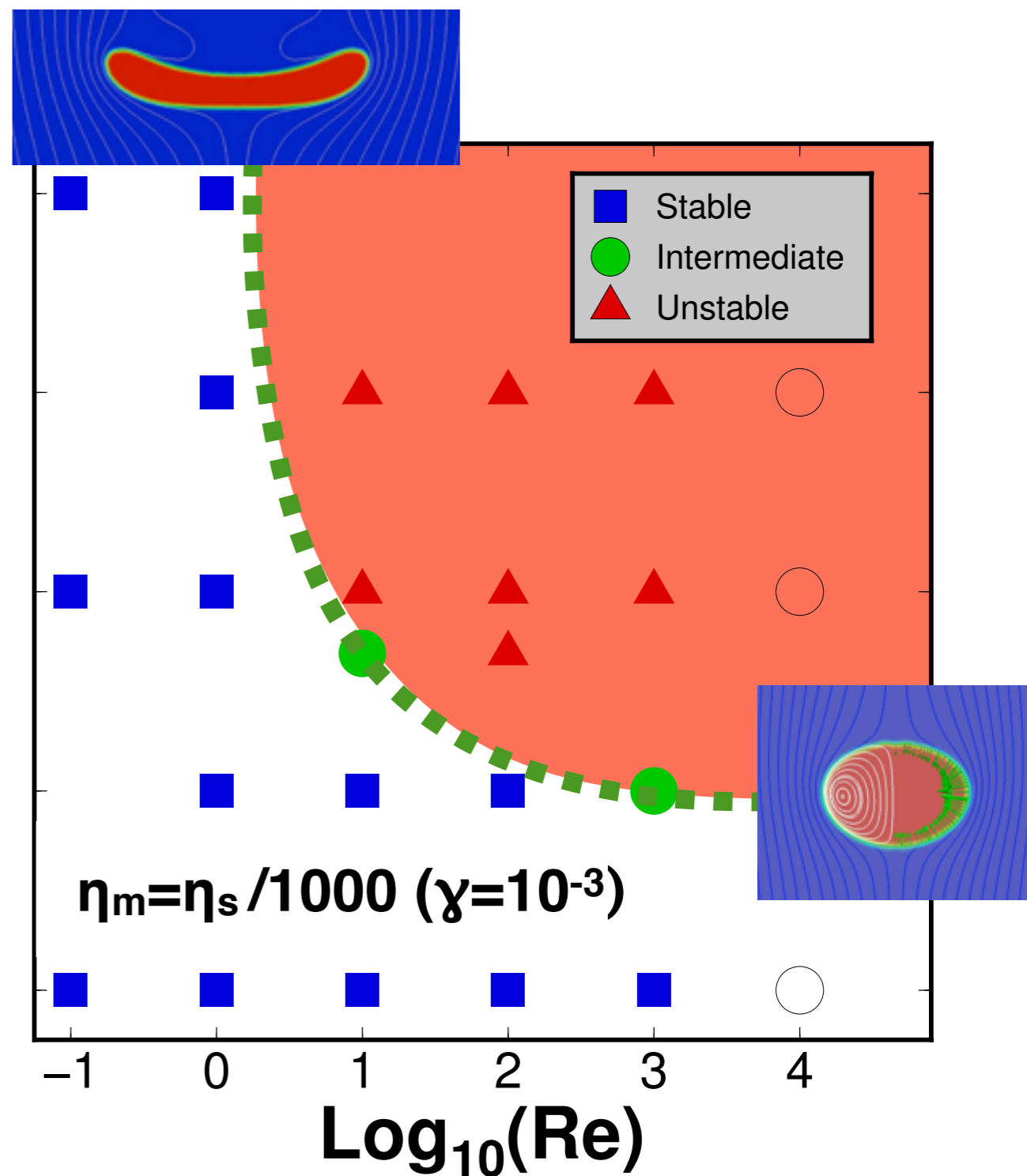
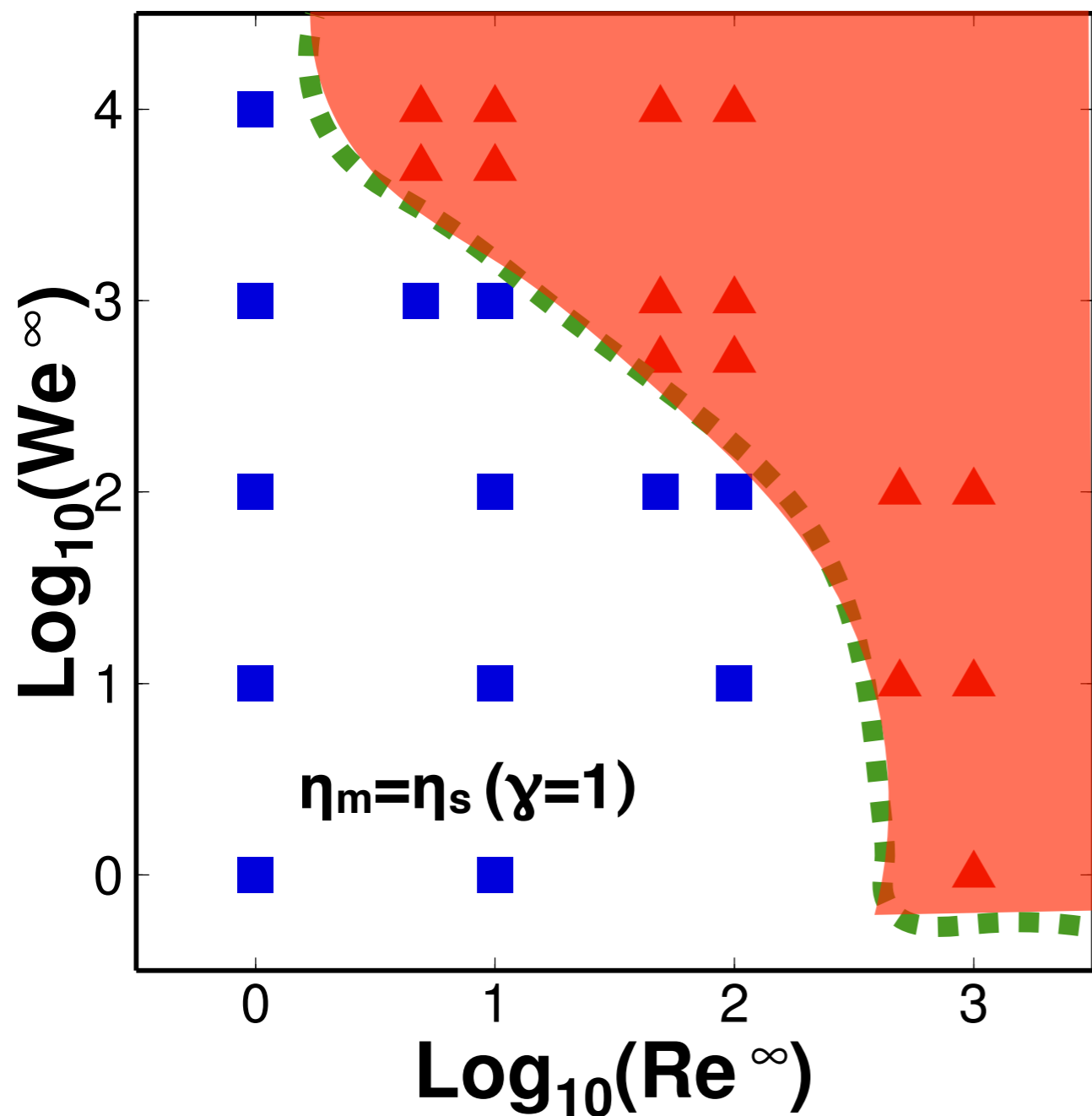


Newtonian rheology: Influence of the Fe-Si viscosity contrast



A high Re, internal circulation reduces breakup ([Wacheul et al., 2014])

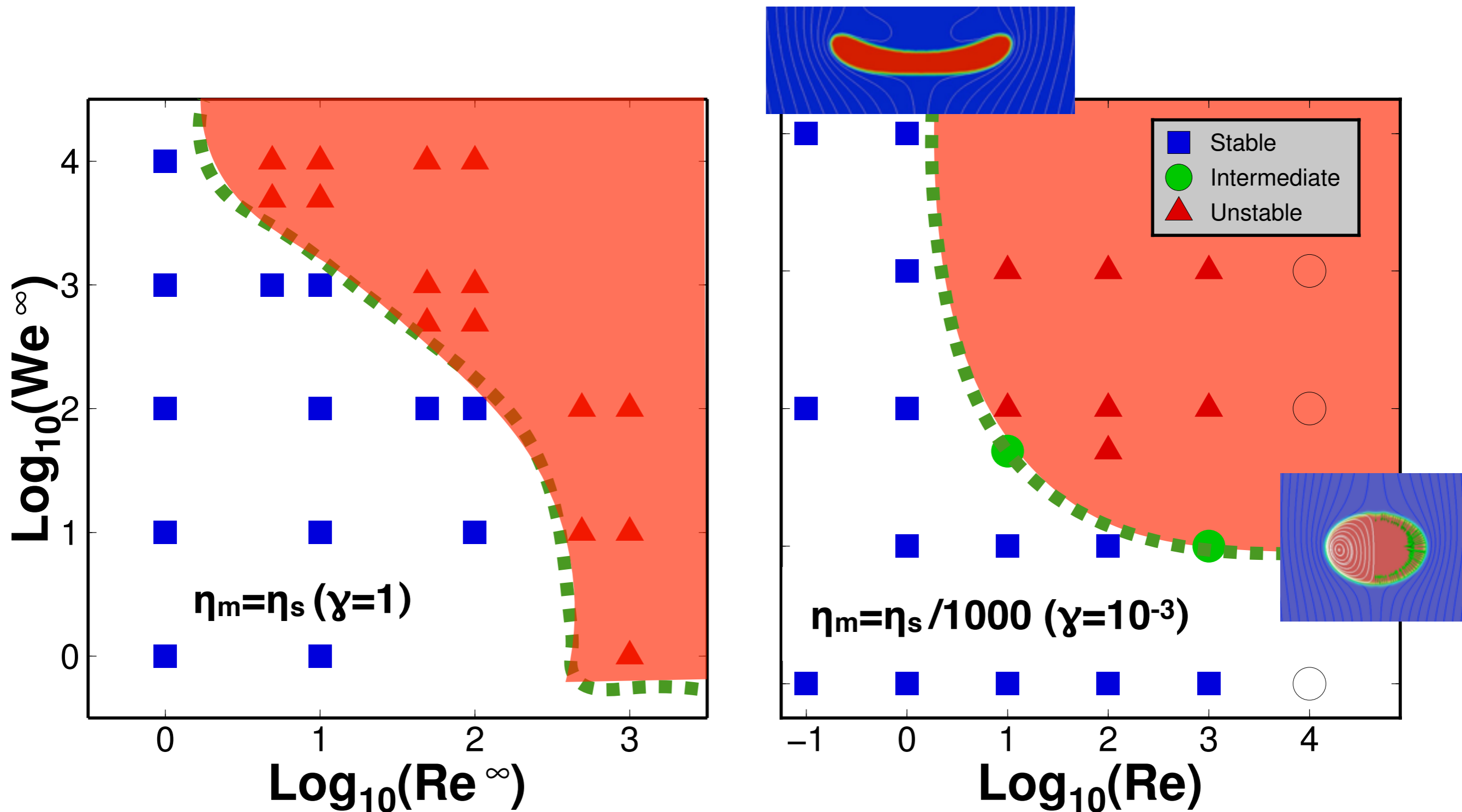
Newtonian rheology: Influence of the Fe-Si viscosity contrast



A high Re, internal circulation reduces breakup ([Wacheul et al., 2014])

At moderate and small Re, viscous resistance to deformation reduces breakup

Newtonian rheology: Influence of the Fe-Si viscosity contrast



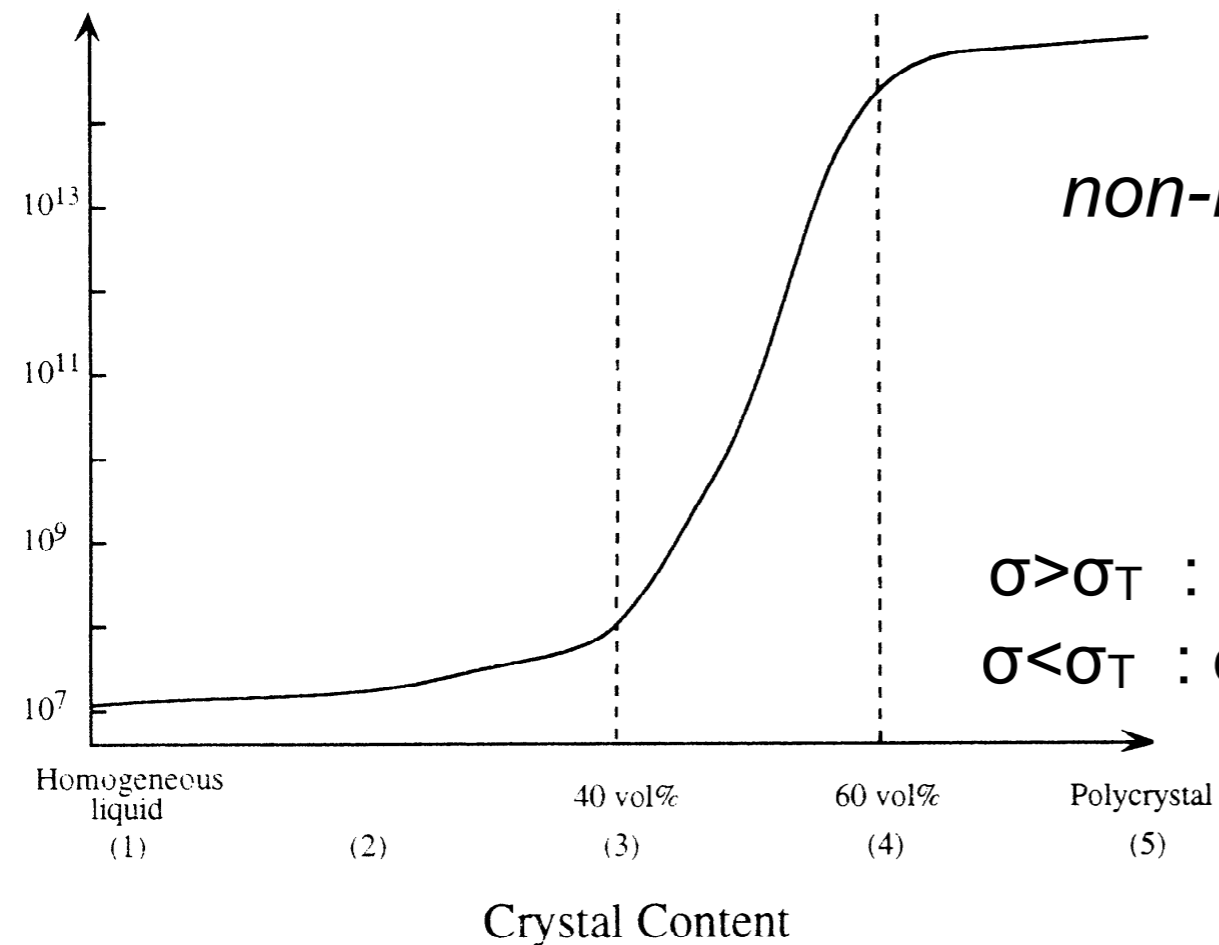
A high Re , internal circulation reduces breakup ([Wacheul et al., 2014])

At moderate and small Re , viscous resistance to deformation reduces breakup

Small $\gamma = \eta_s / \eta_m$ stabilises diapirs at high Re , but favours breakup at low Re

Rheological transitions & non-Newtonian rheology for partially molten silicates

LEJEUNE AND RICHTER: RHEOLOGY OF CRYSTAL-BEARING MELTS



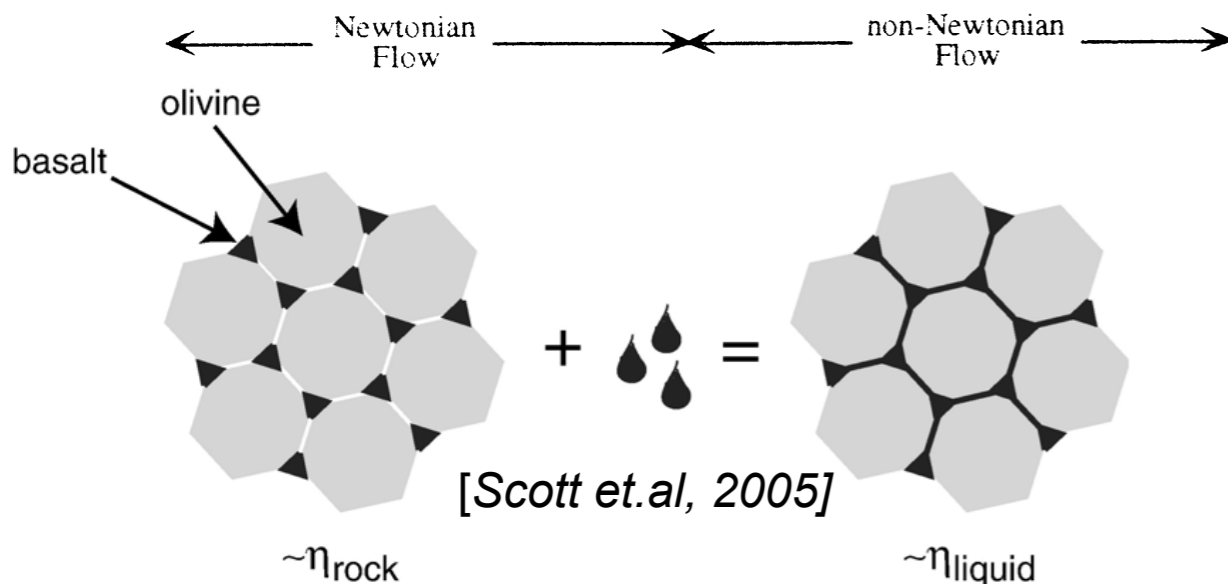
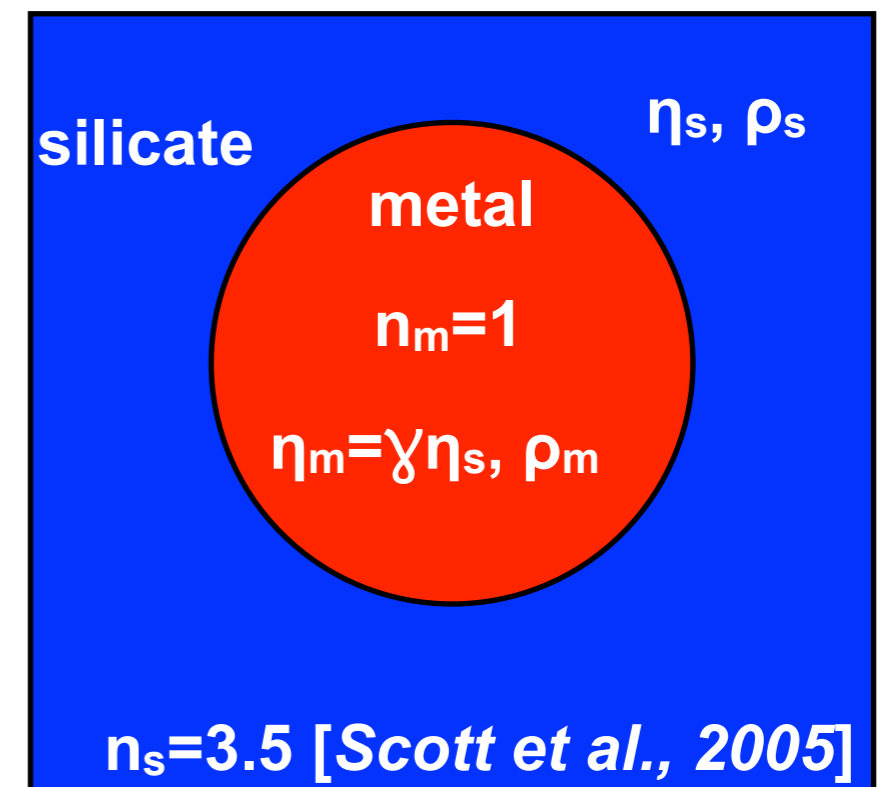
Newtonian case (fully molten diapir):

$$\eta = \eta_{0\text{diff}}$$

non-Newtonian case (partially molten silicates):

$$\eta = \eta_{0\text{diff}} \left[1 + \left(\frac{\sigma}{\sigma_T} \right)^{n-1} \right]^{-1}$$

$\sigma > \sigma_T$: dislocation creep (non-Newtonian) dominated
 $\sigma < \sigma_T$: diffusion creep (Newtonian) dominated

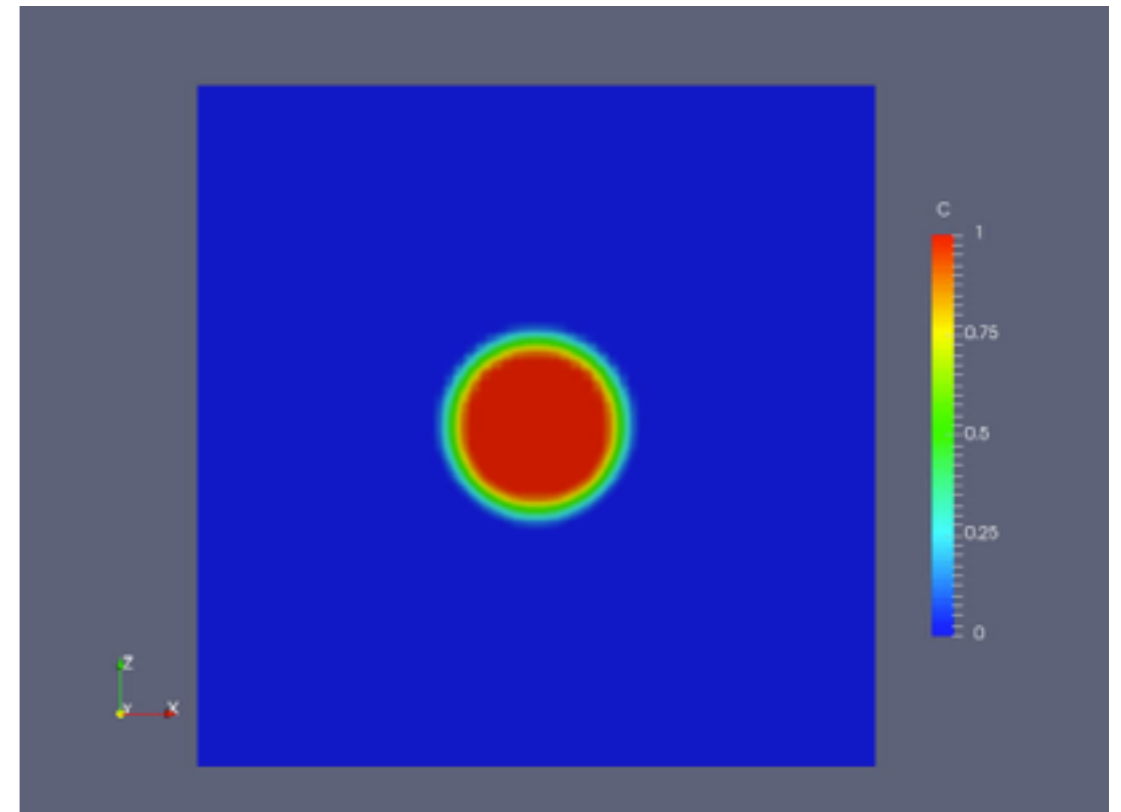
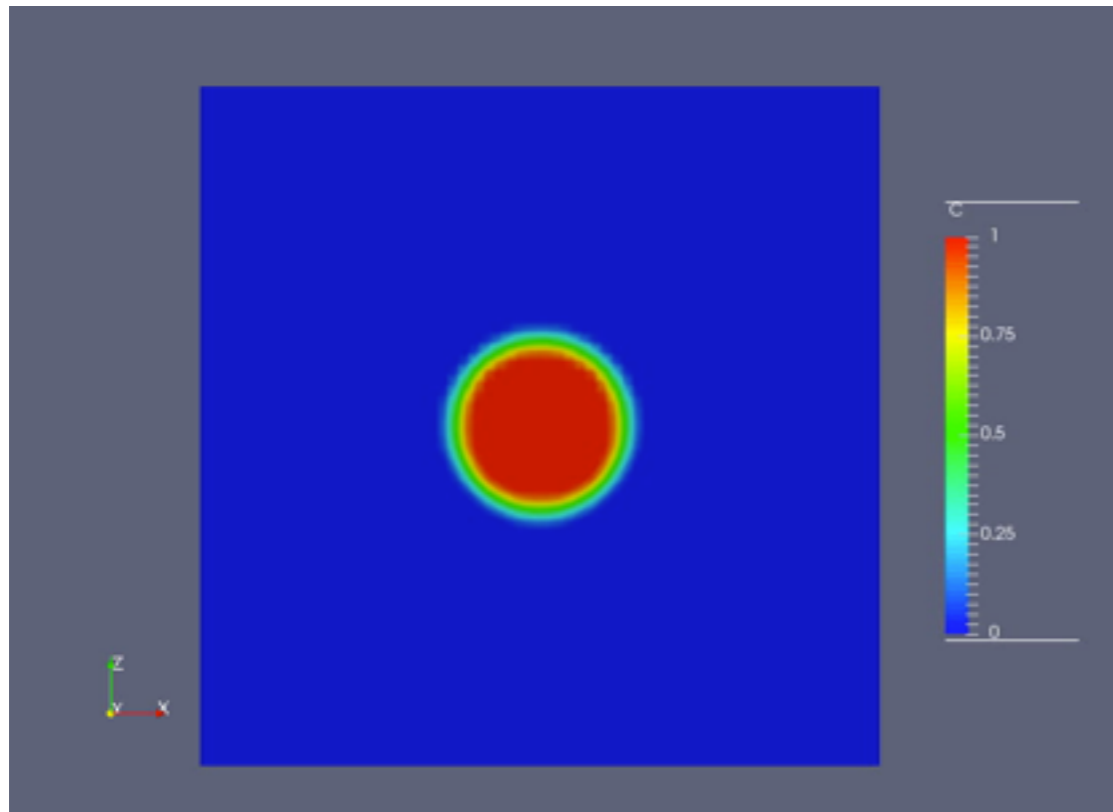


Newtonian vs. non-Newtonian rheology

$n=1$

$Re = 100$ $We=10$

$n=3.5$

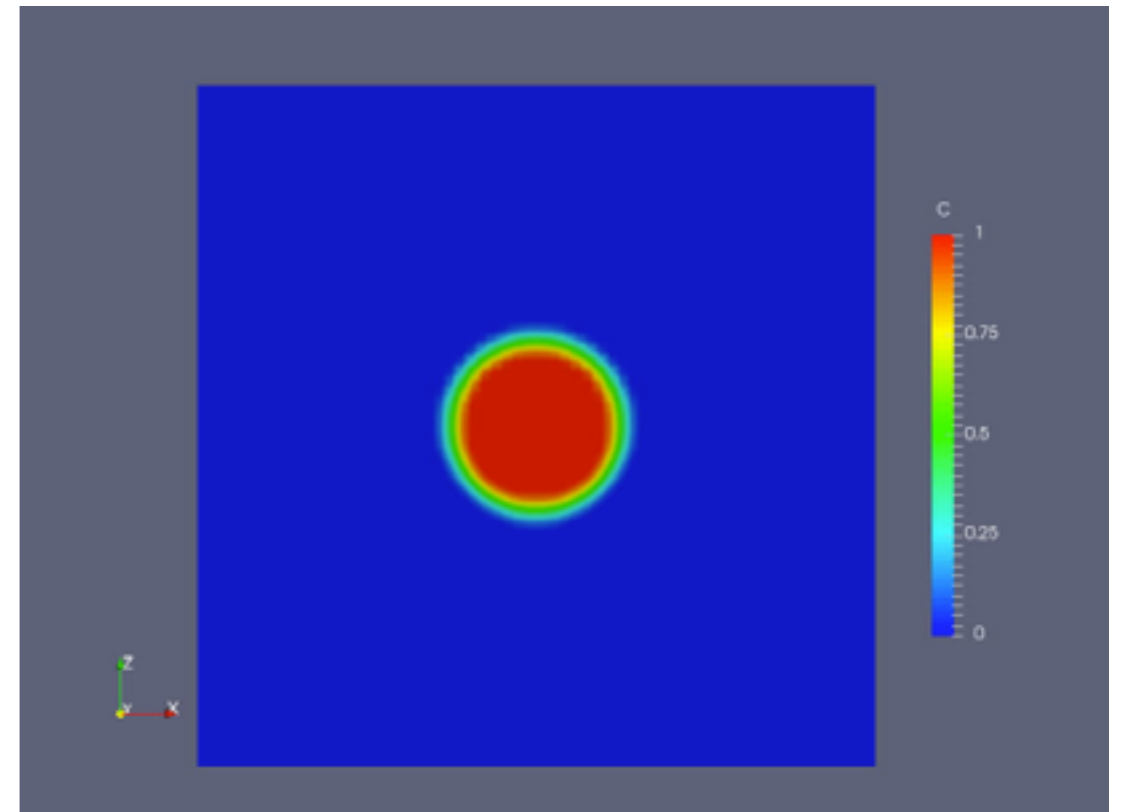
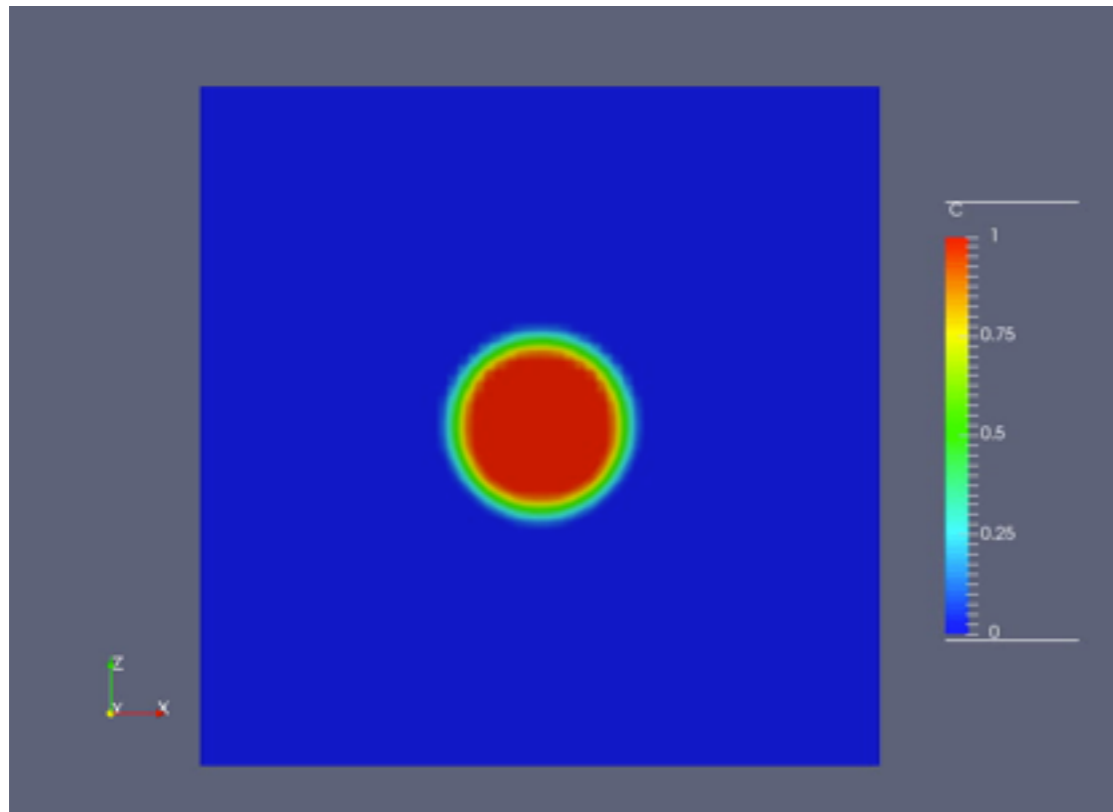


Newtonian vs. non-Newtonian rheology

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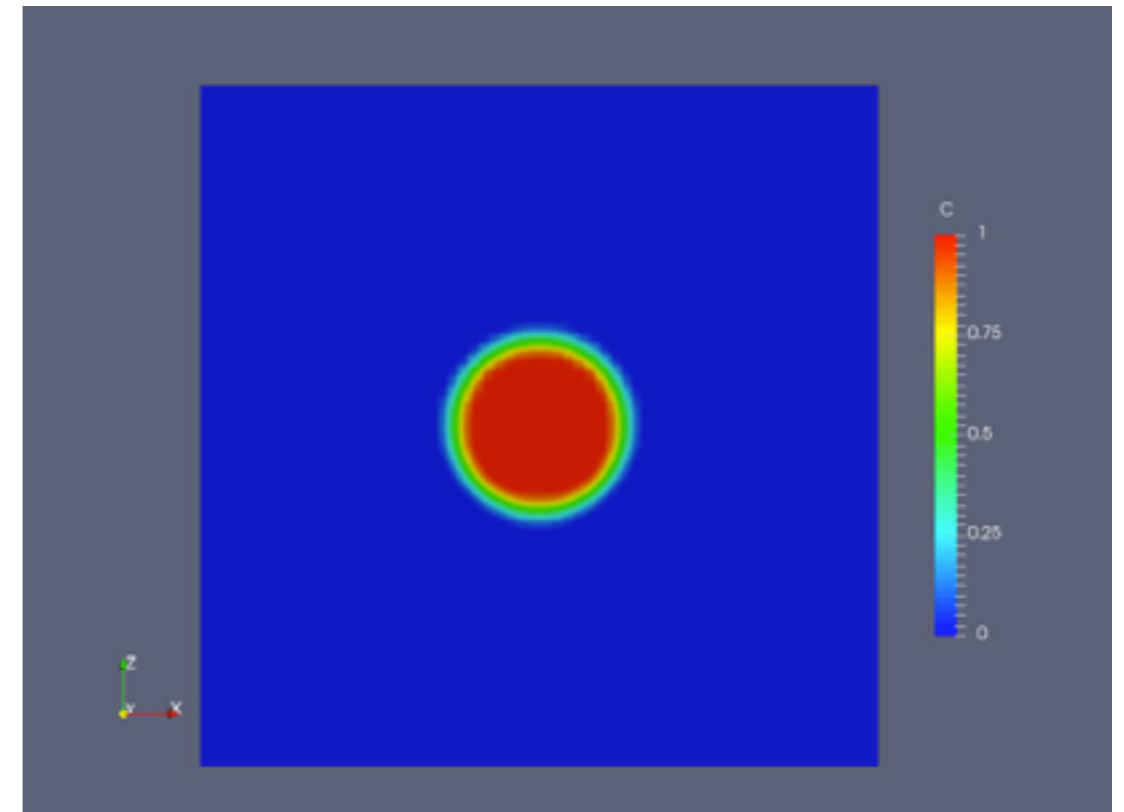
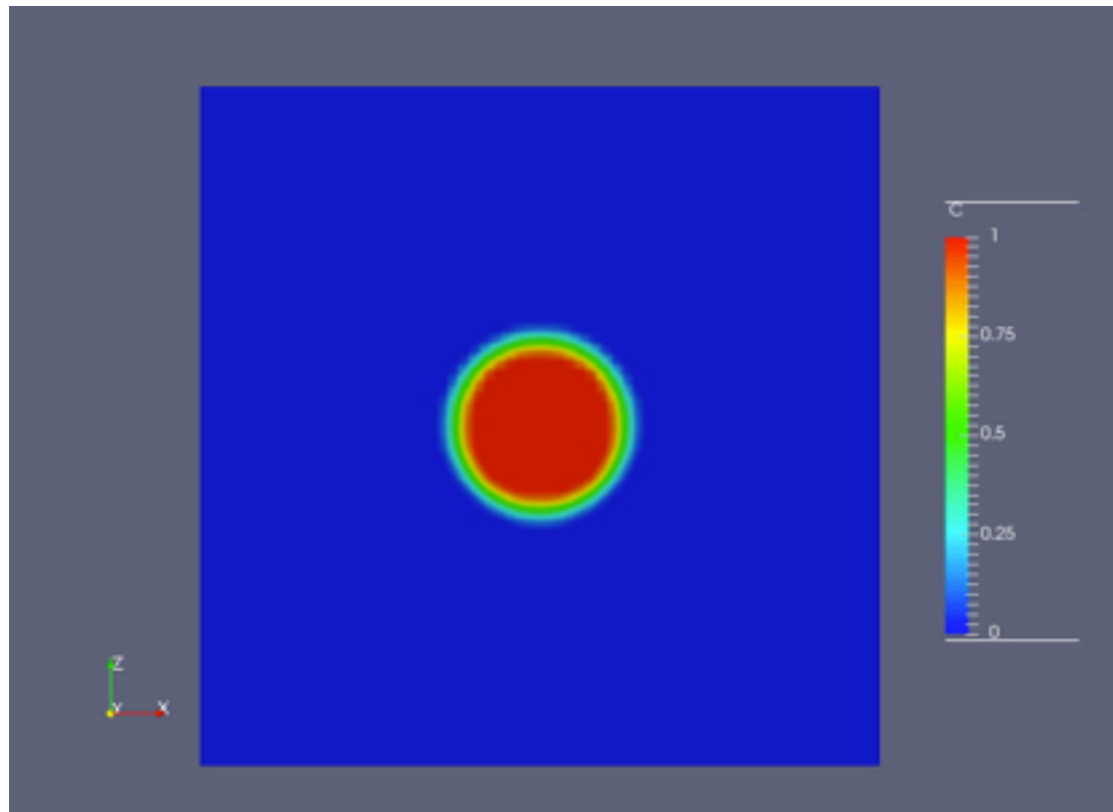


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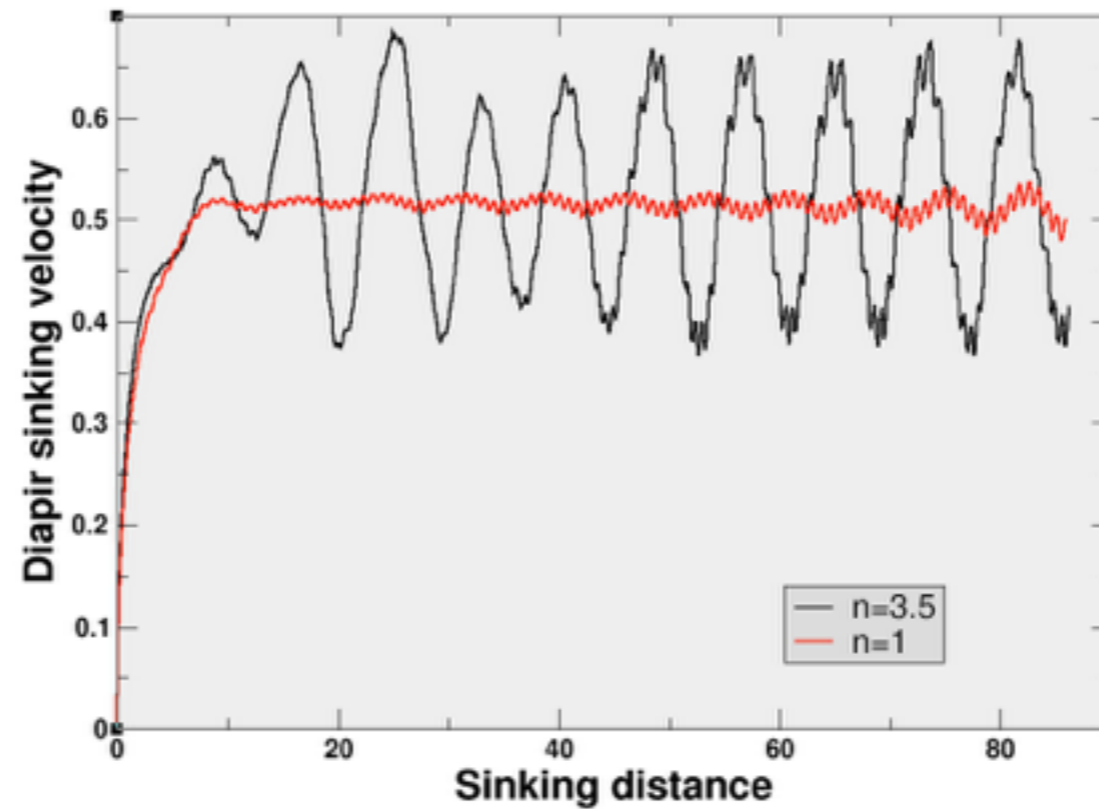
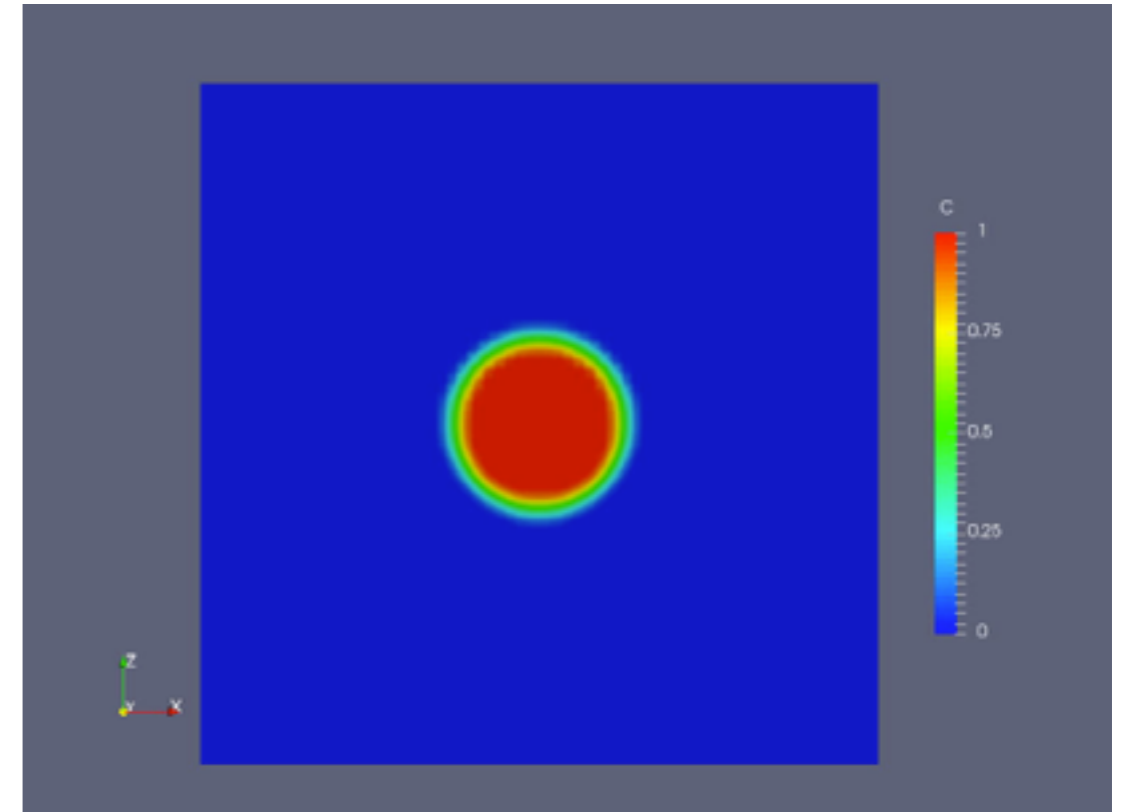
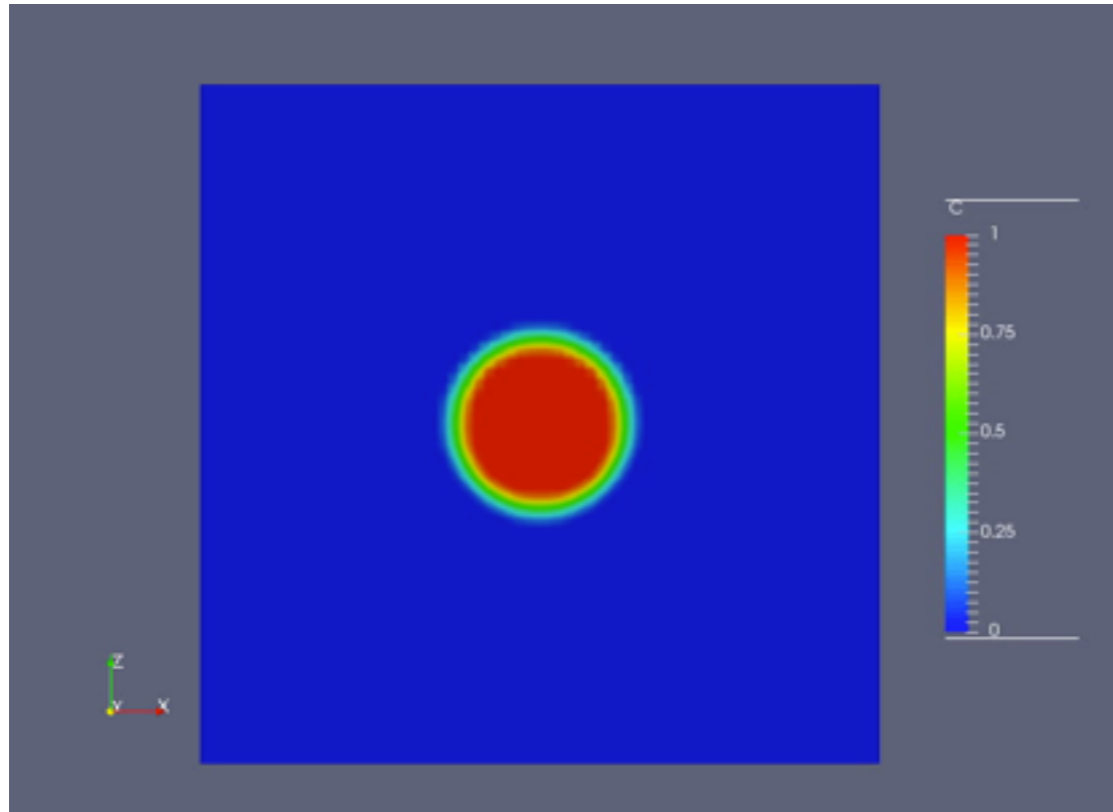


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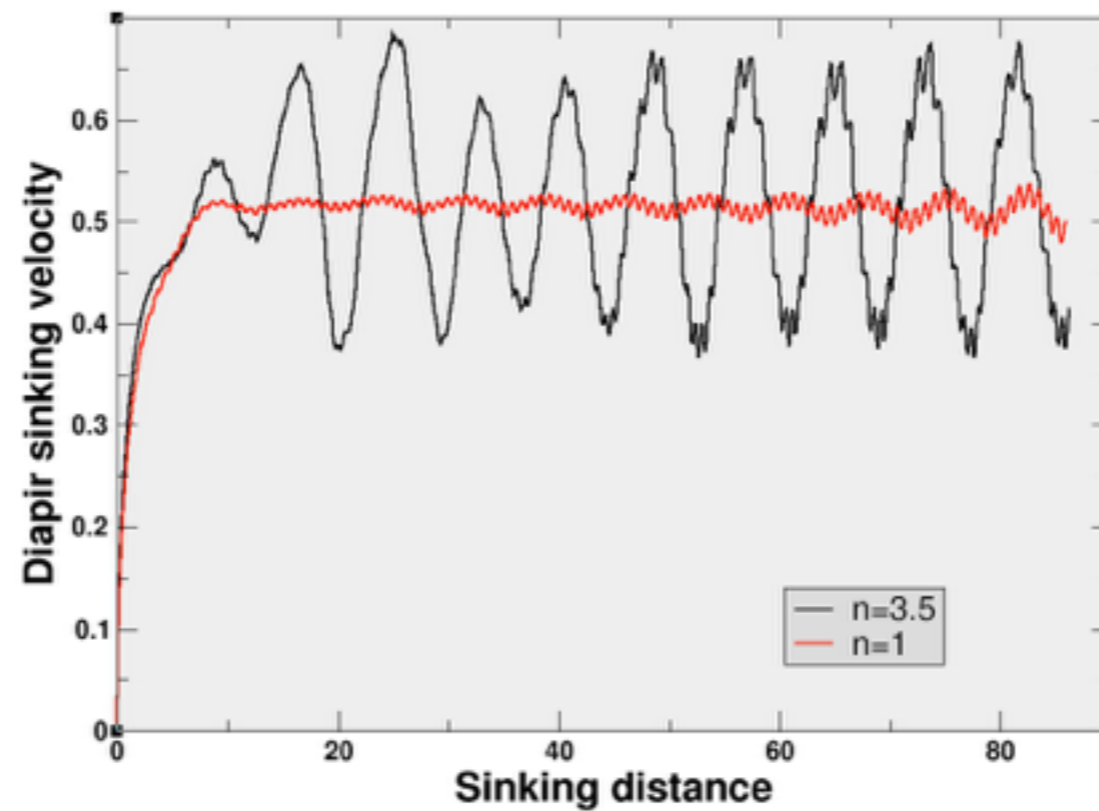
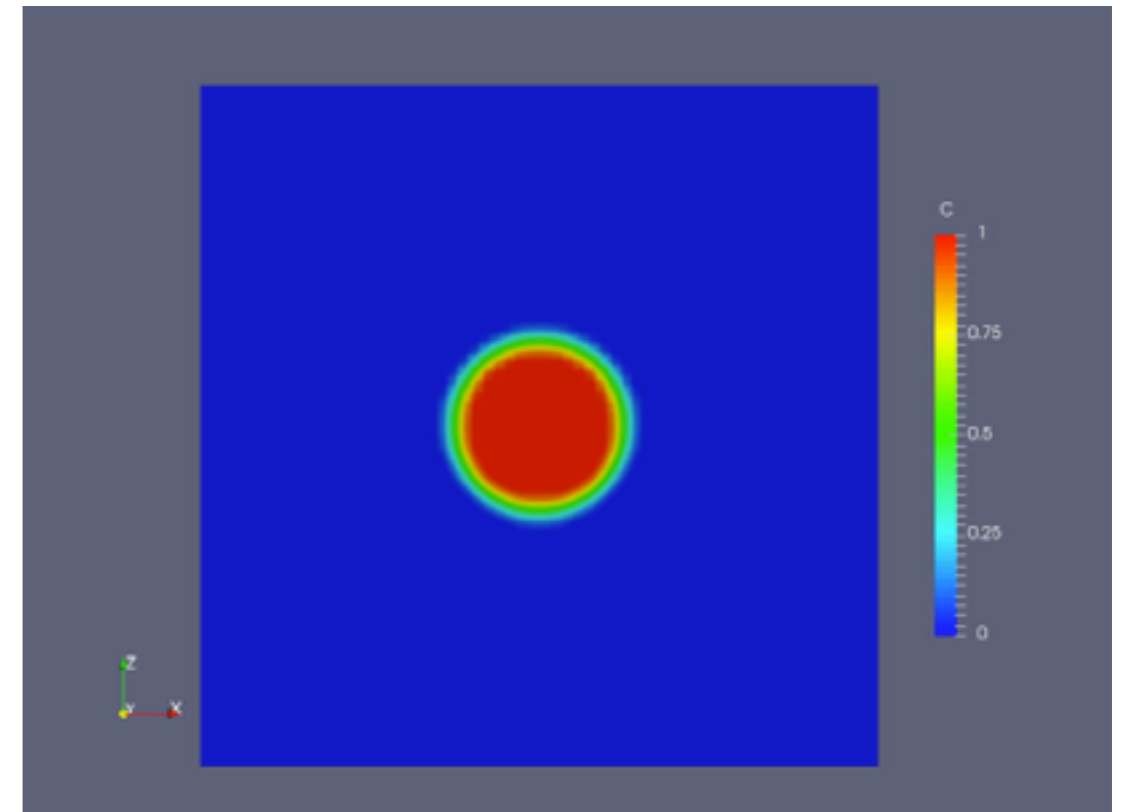
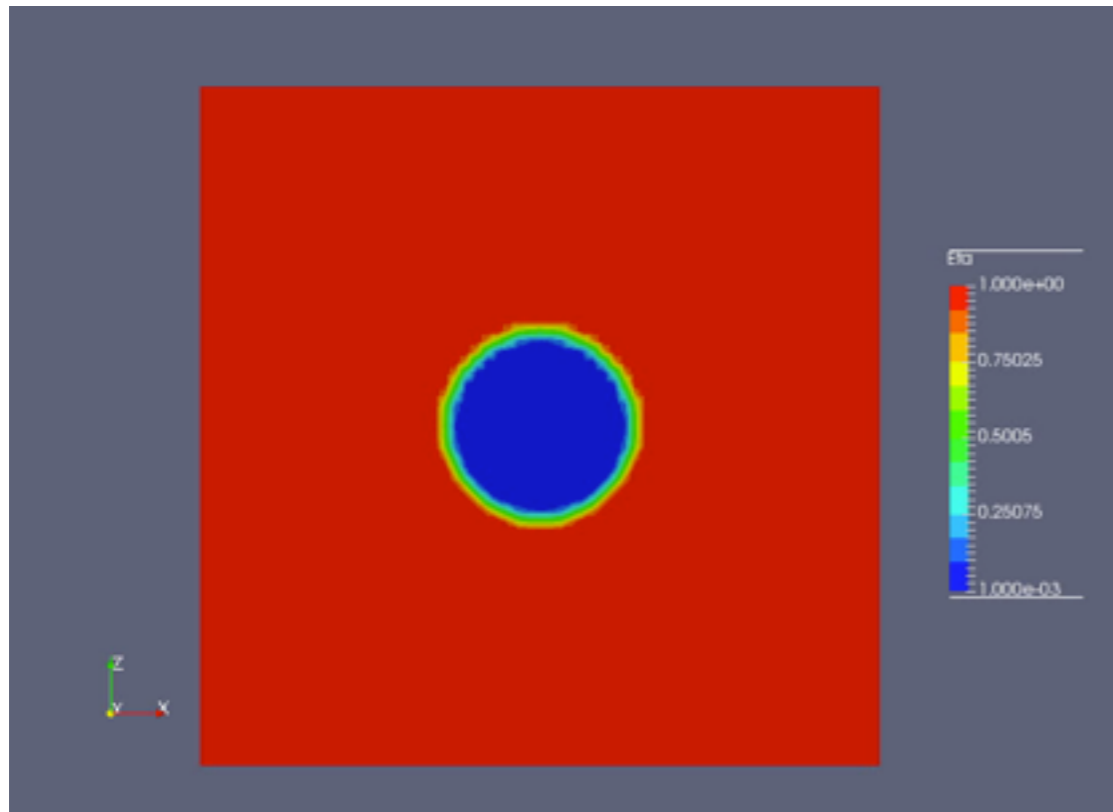


Newtonian vs. non-Newtonian rheology

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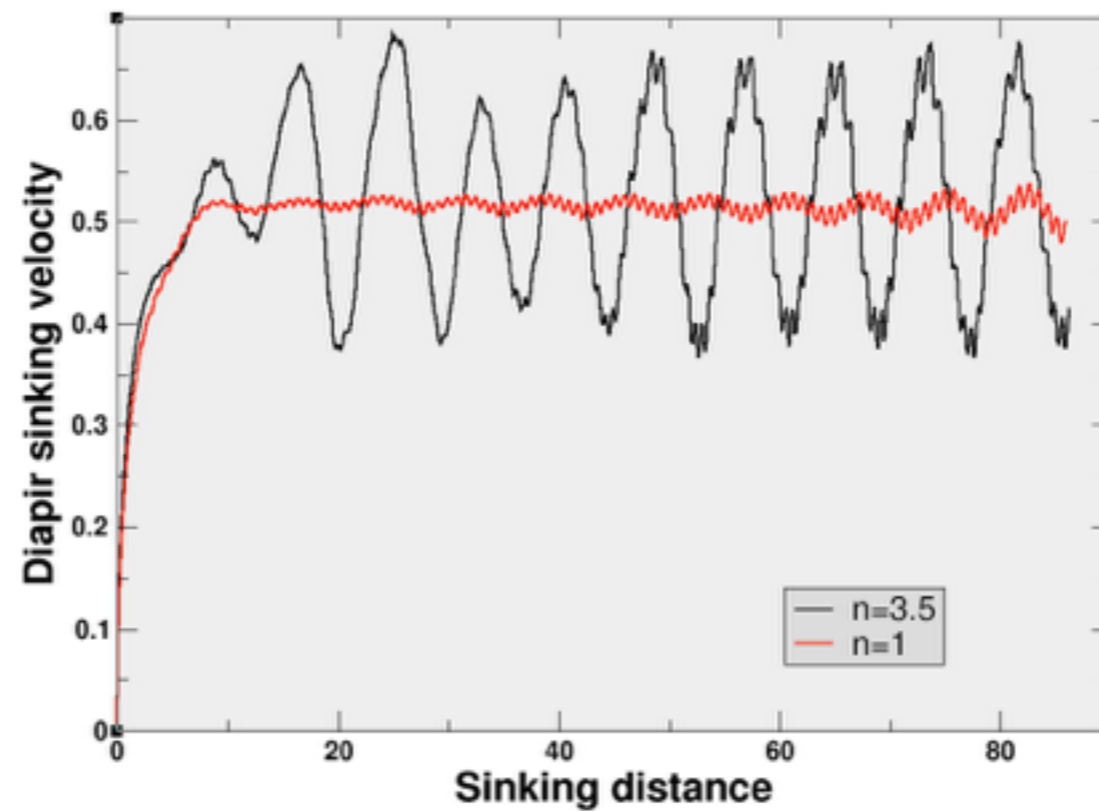
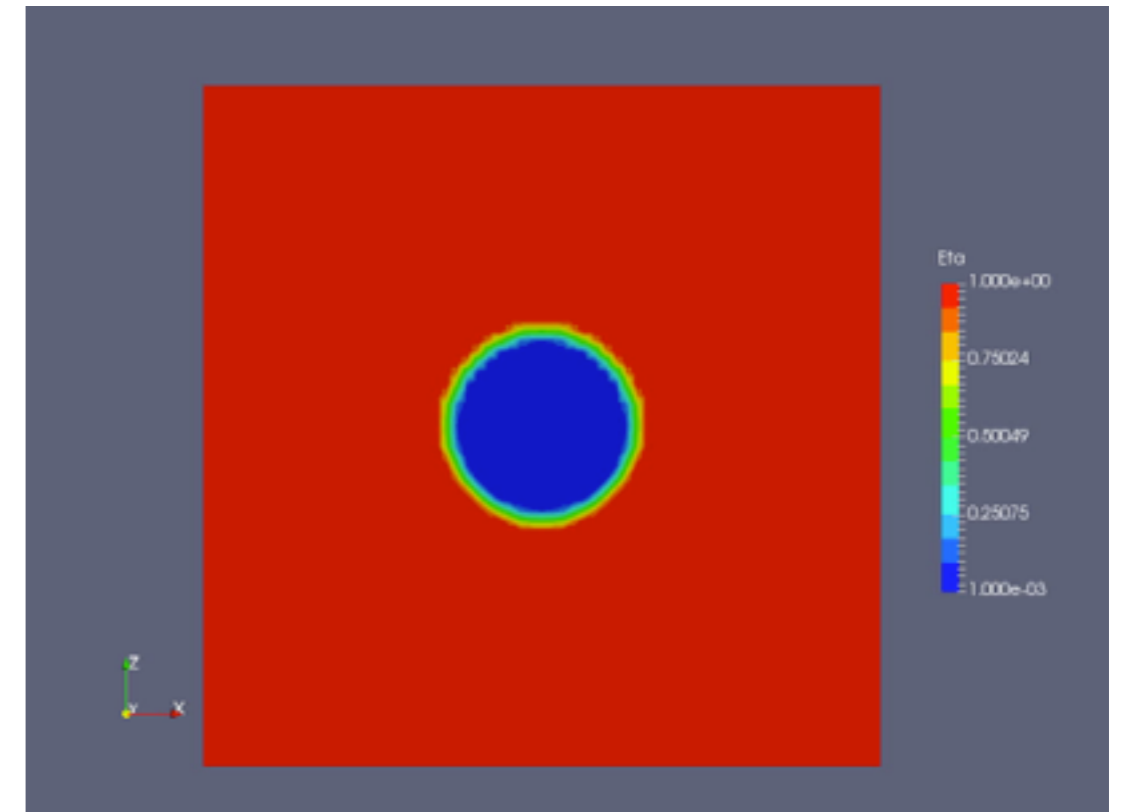
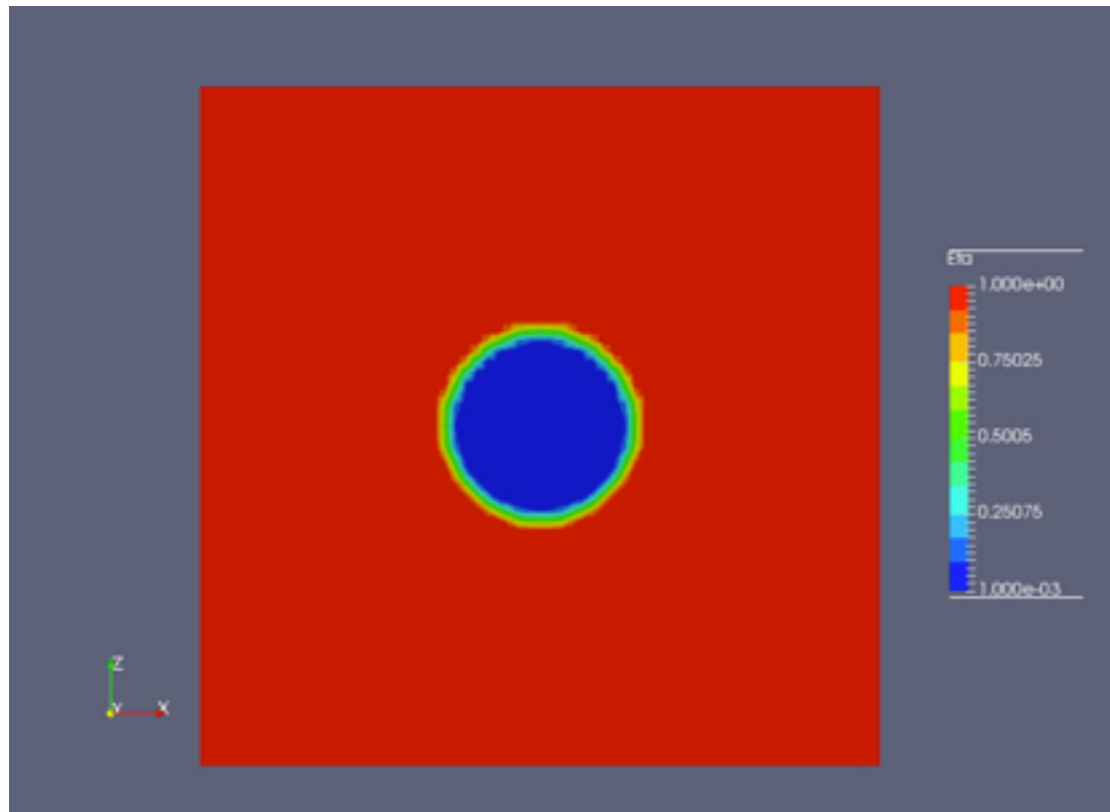


Newtonian vs. non-Newtonian rheology

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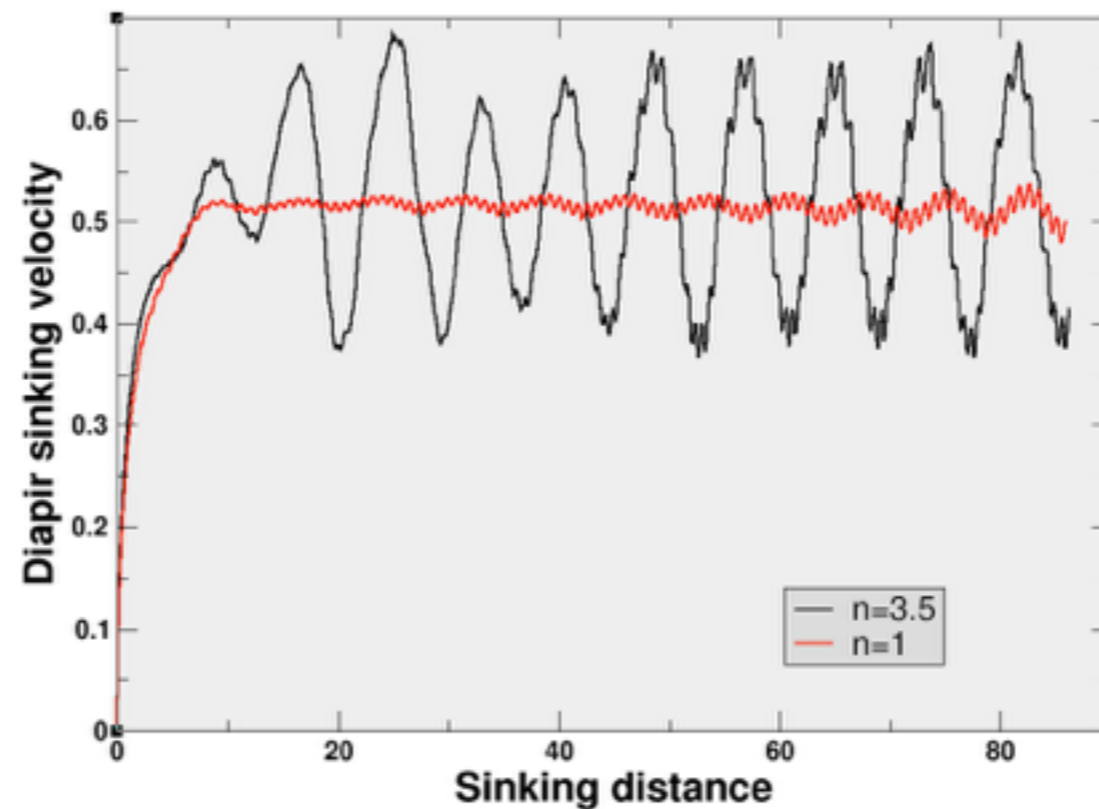
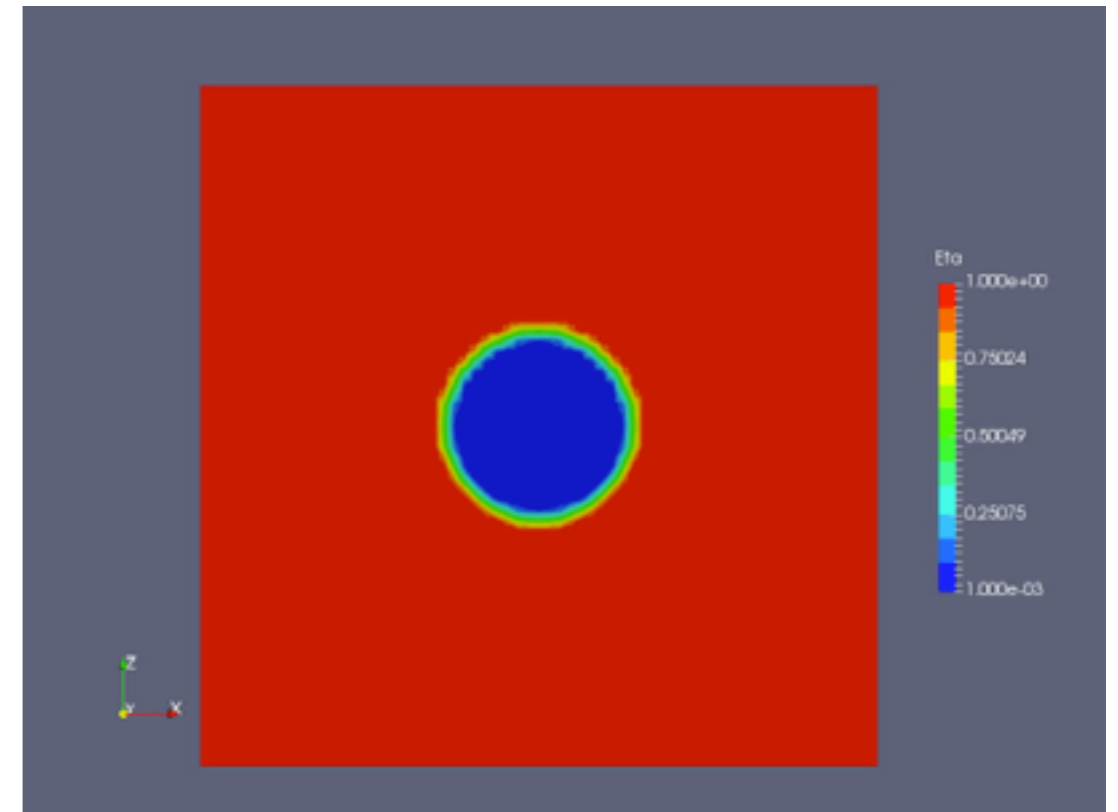
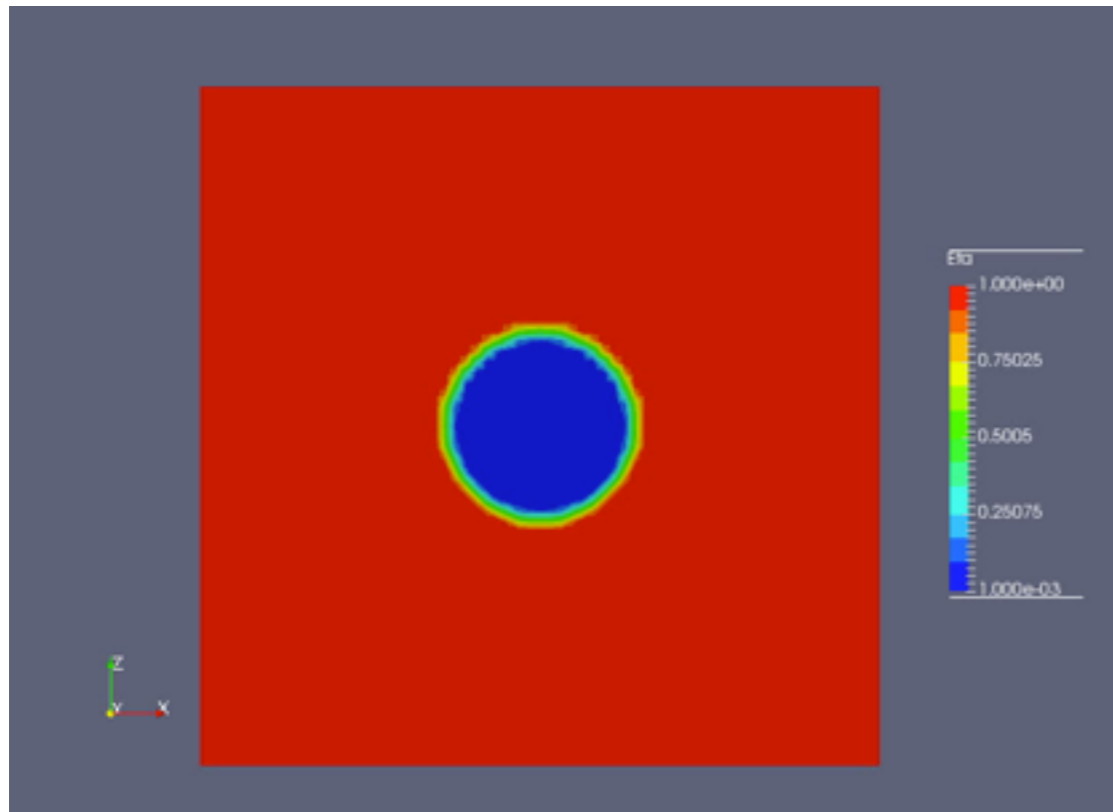


Newtonian vs. non-Newtonian rheology

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$Re = 100$ $We=10$

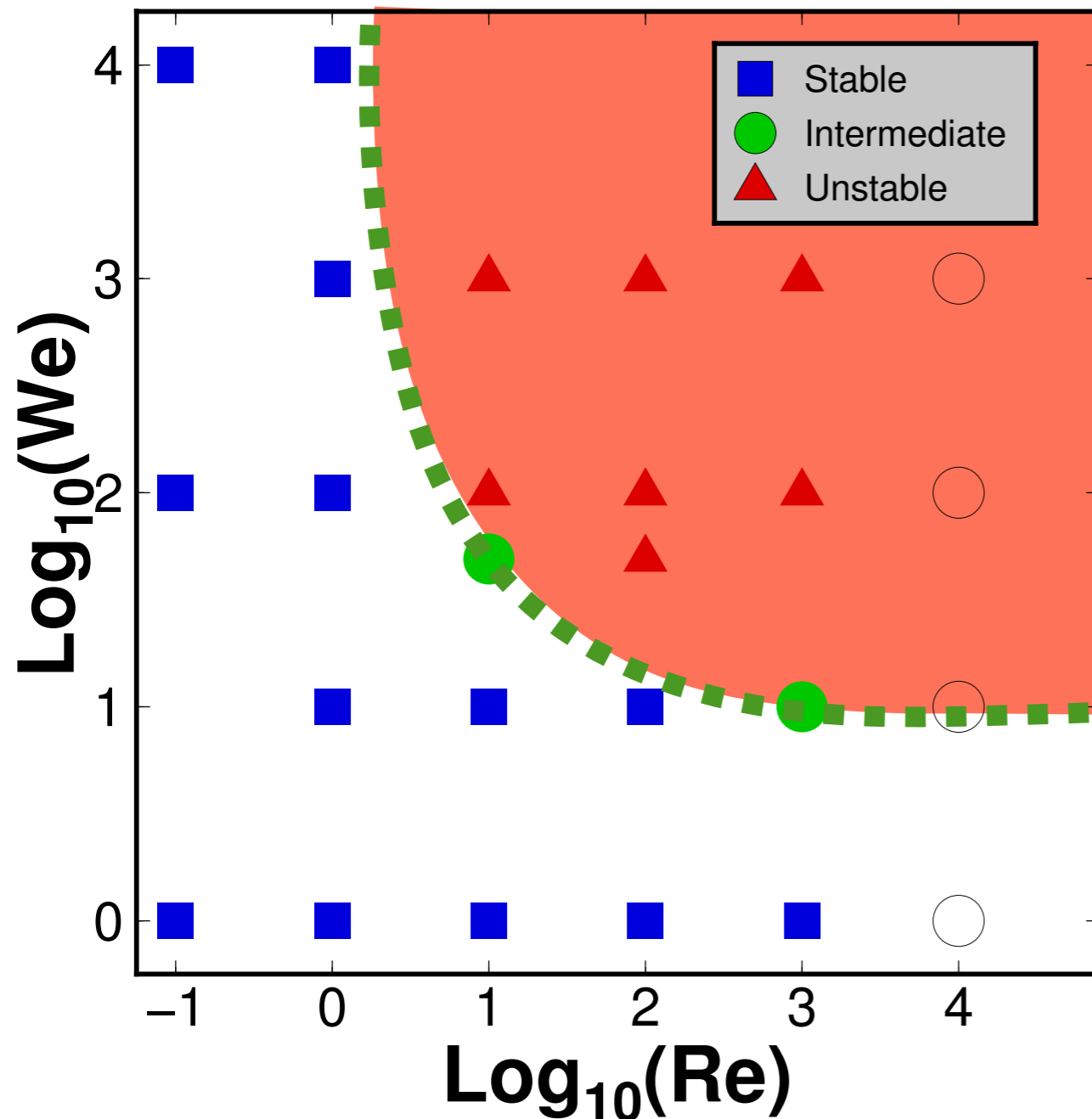
$n=3.5$



**non-Newtonian
rheology favours
breakup**

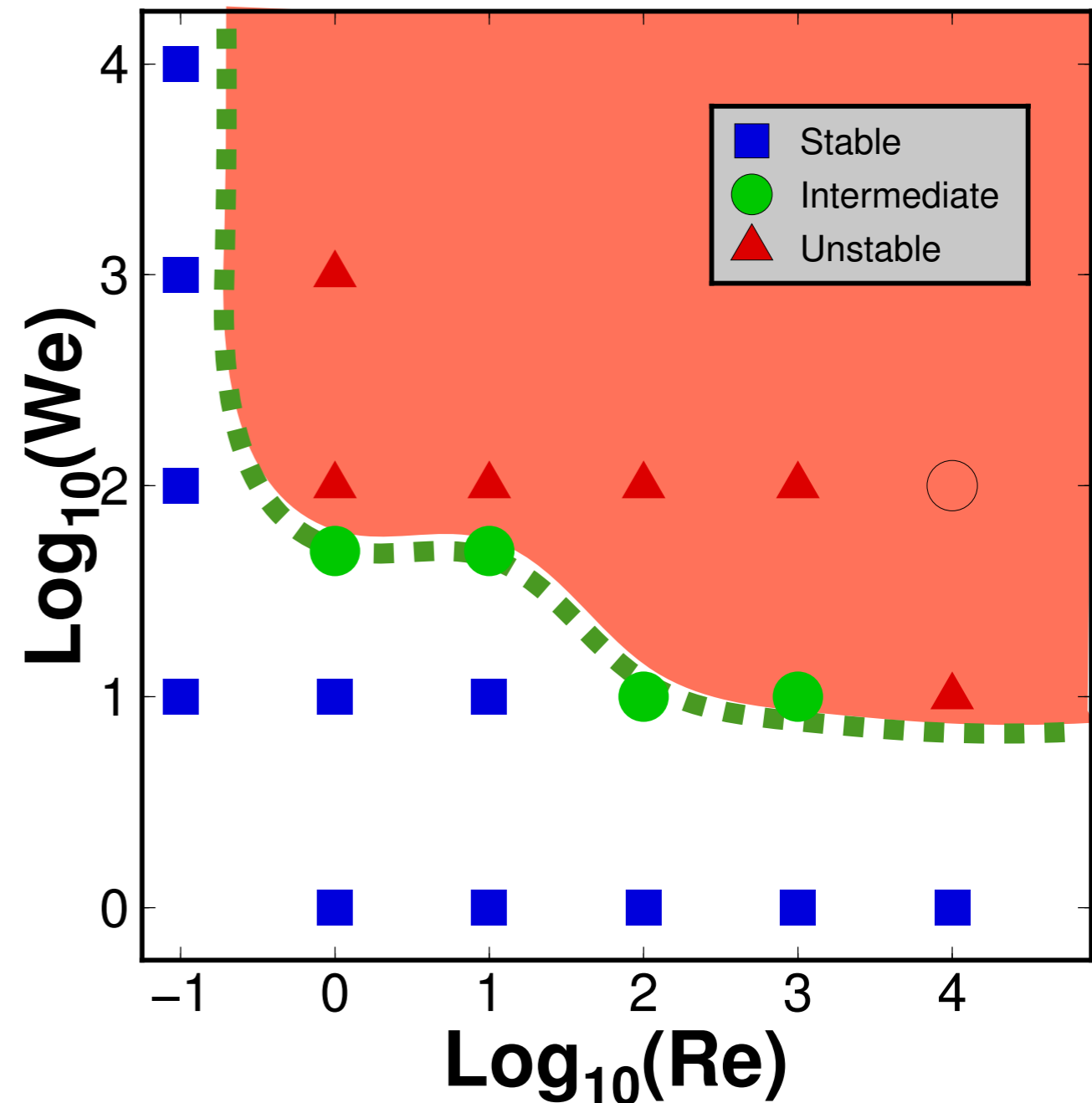
Newtonian ($n=1$) vs. Non-Newtonian rheology ($n=3.5$) stability diagrams

$n=1, \gamma=10^{-3}$



non-Newtonian rheology influence is stronger for smaller Re values

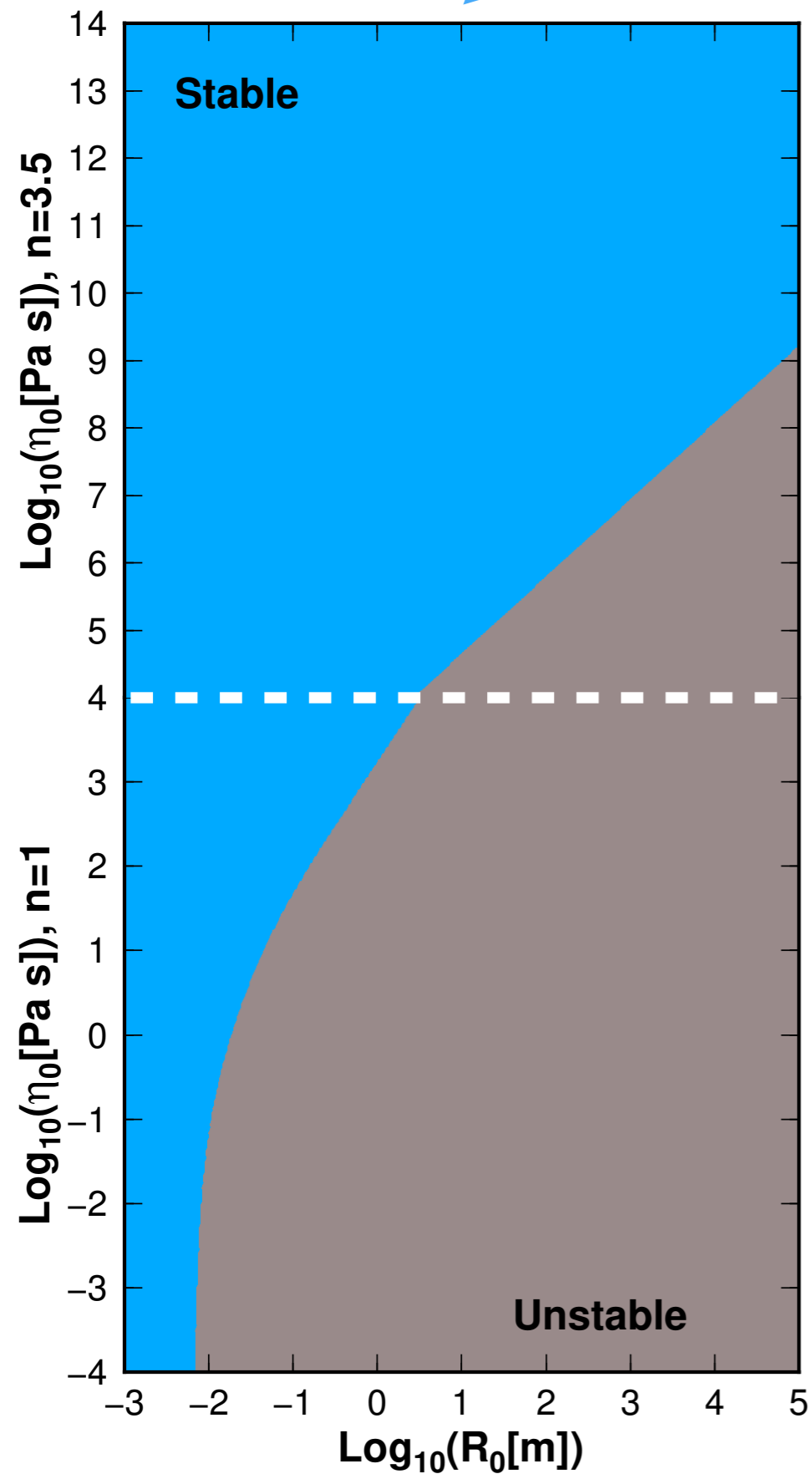
$n=3.5, \gamma=10^{-3}$



non-Newtonian rheology favours breakup

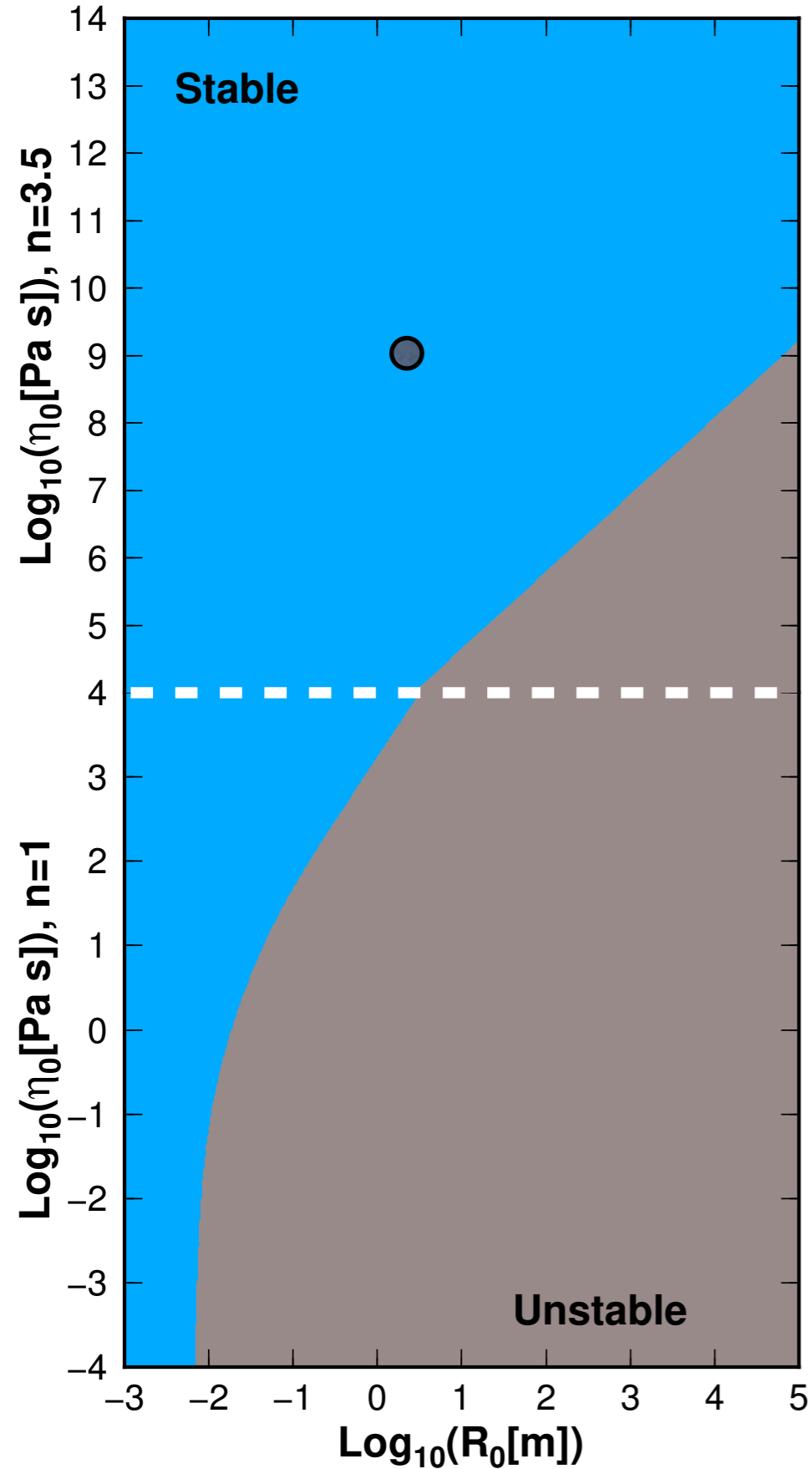
Summary: stability region

We-Re stability condition: $a_1/Re + a_2/We < C_D$



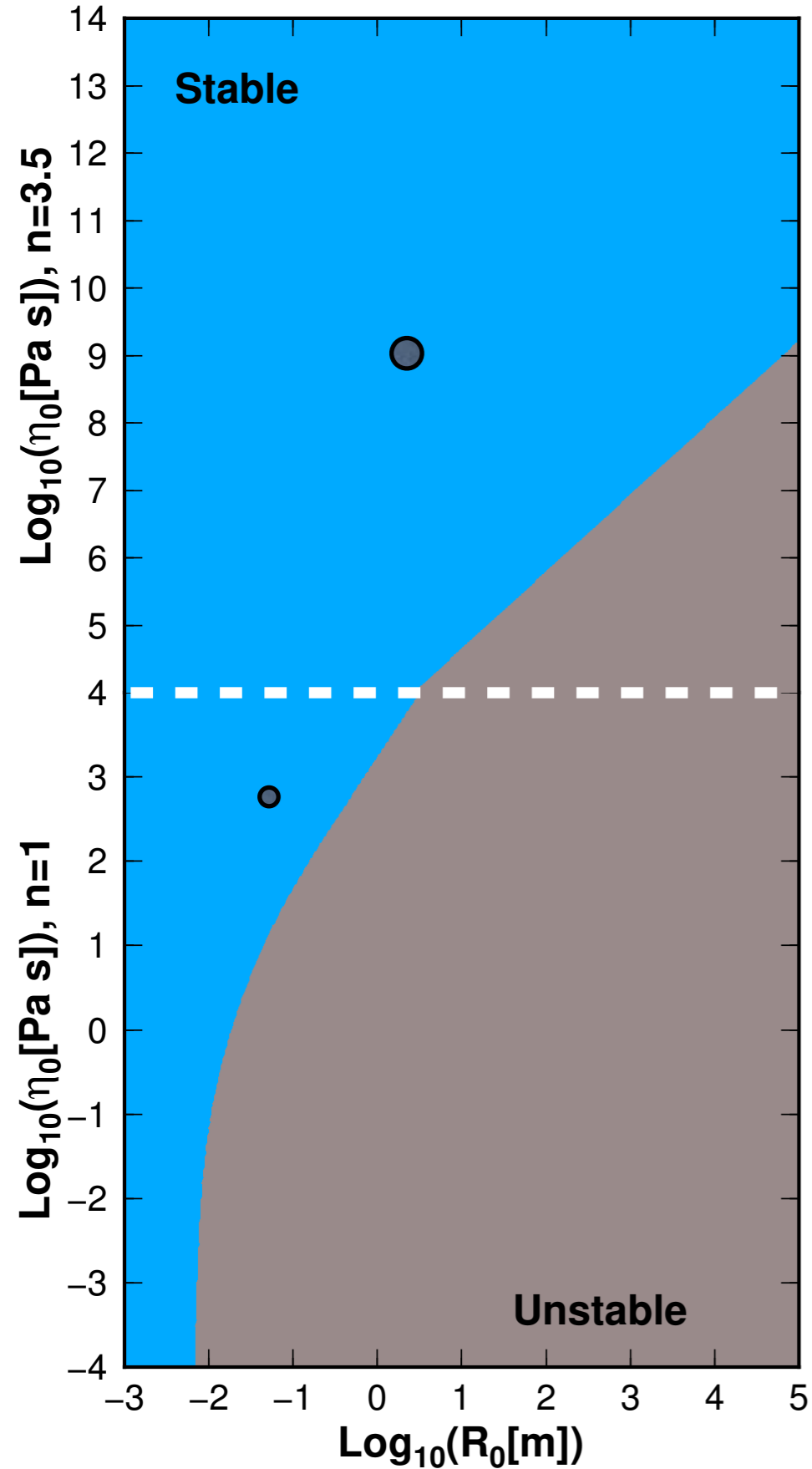
Summary: stability region

We-Re stability condition: $a_1/Re + a_2/We < C_D$



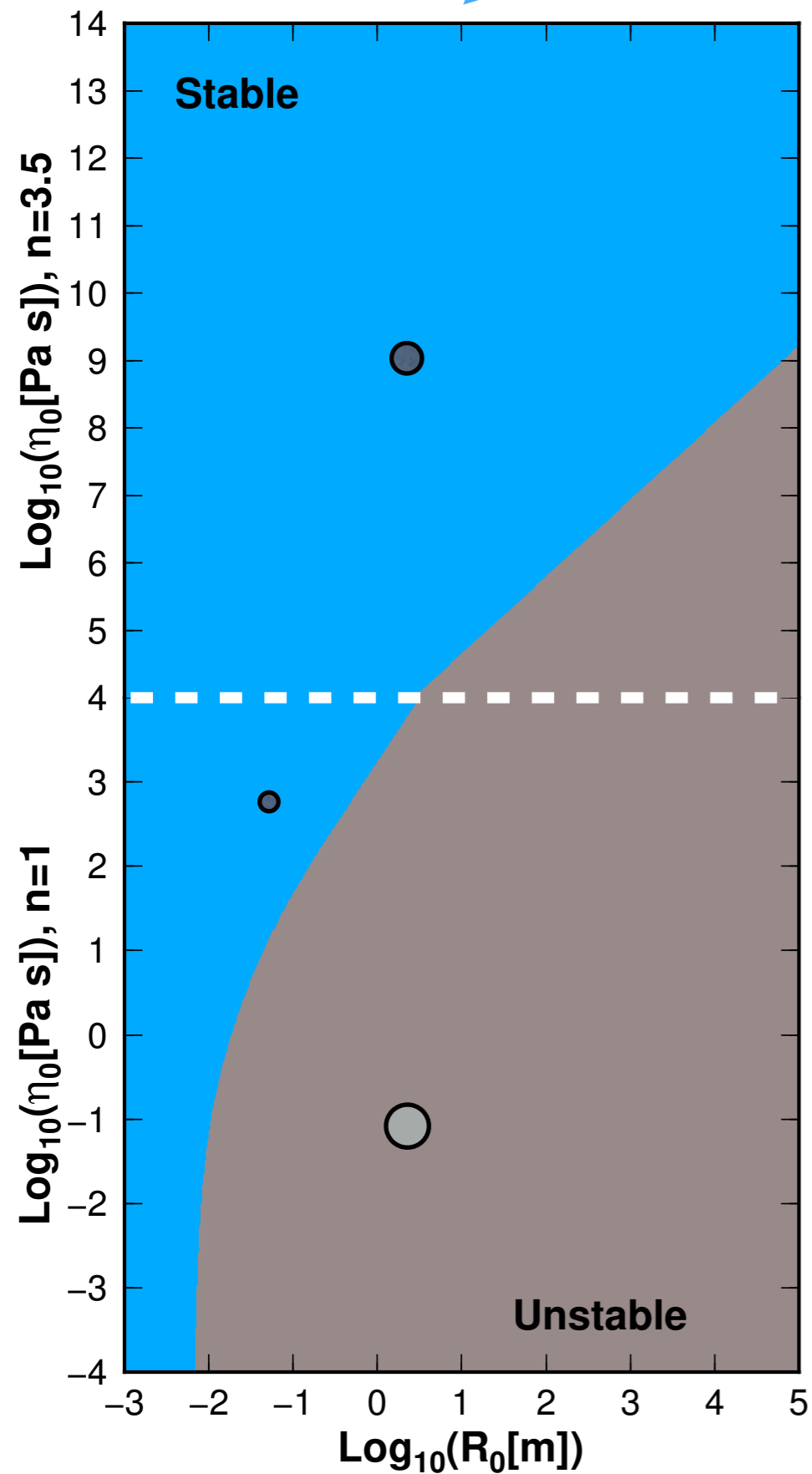
Summary: stability region

We-Re stability condition: $a_1/\text{Re} + a_2/\text{We} < C_D$



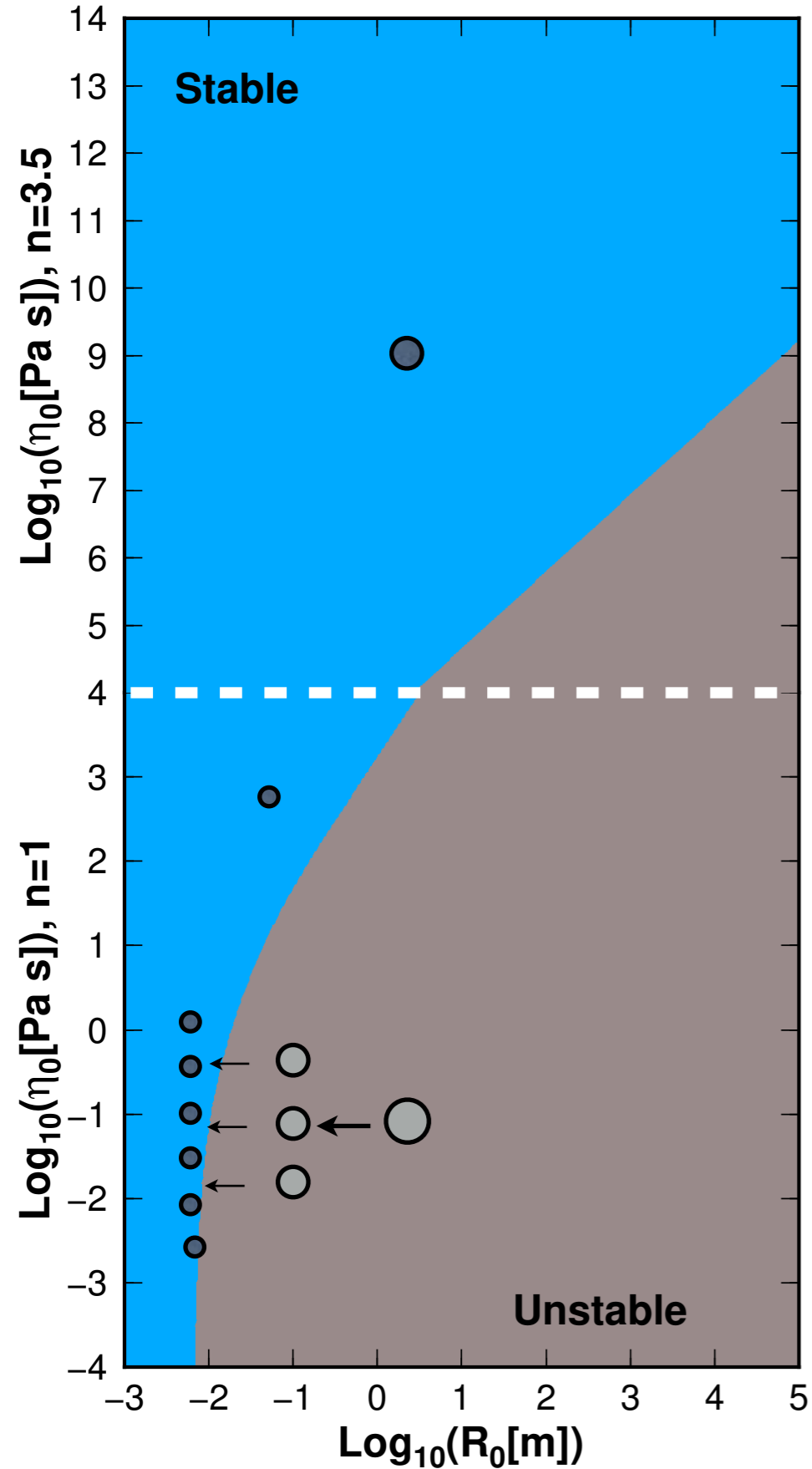
Summary: stability region

We-Re stability condition: $a_1/Re + a_2/We < C_D$



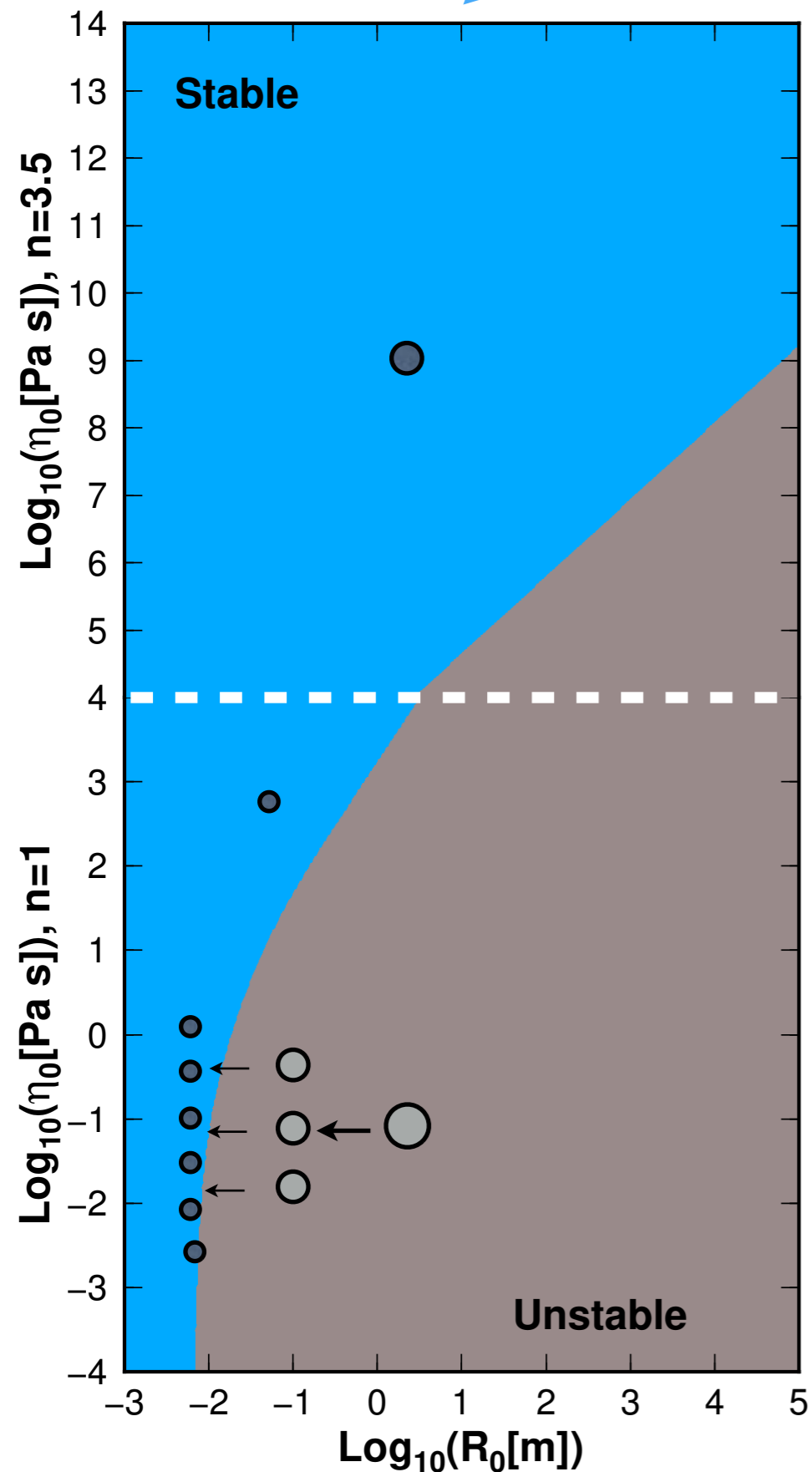
Summary: stability region

We-Re stability condition: $a_1/Re + a_2/We < C_D$

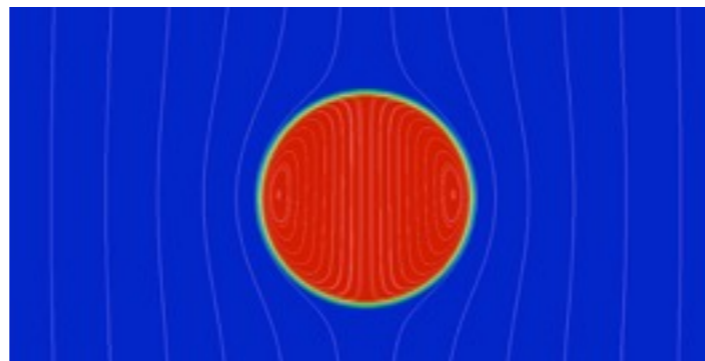


Summary: stability region

$$\text{We-Re stability condition: } a_1/\text{Re} + a_2/\text{We} < C_D$$

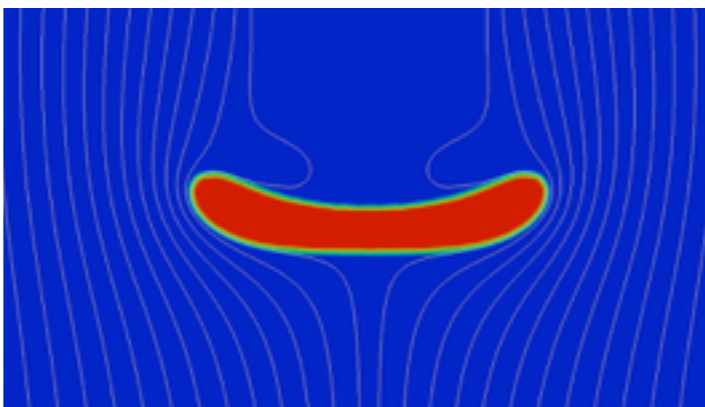


Sinking distance



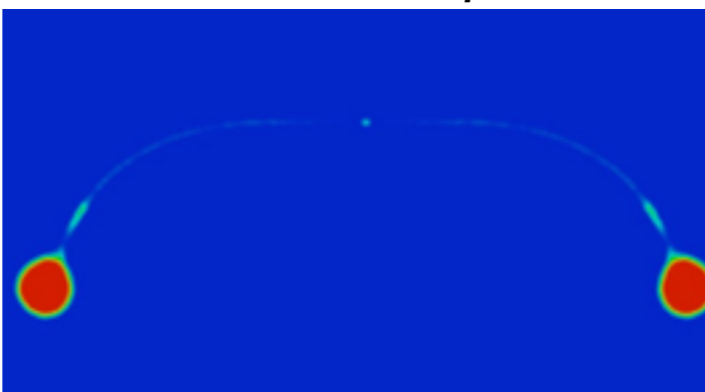
$z=0$

1. "Pancake-like" flattening



$z < R$

2. Breakup

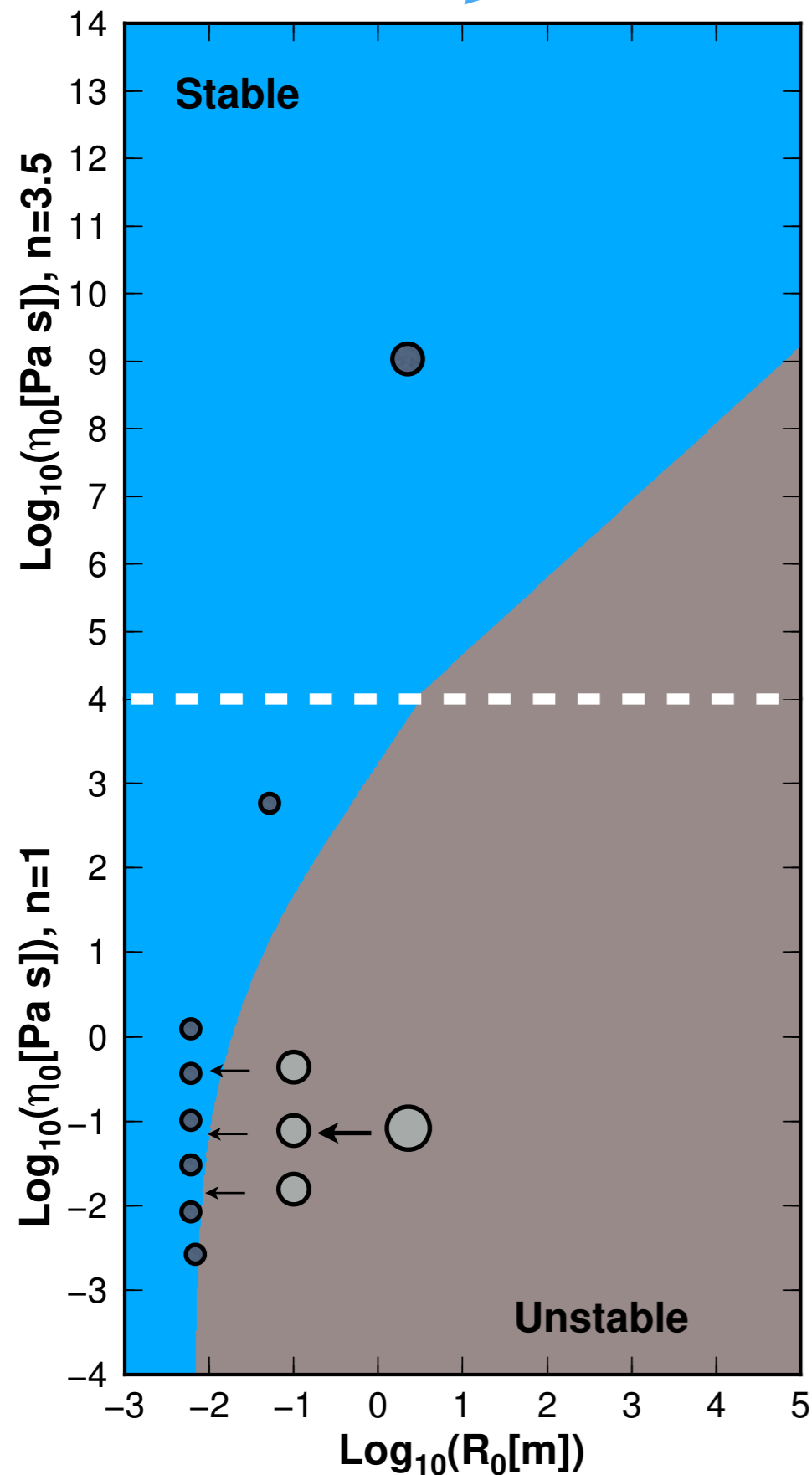


$z \sim R$

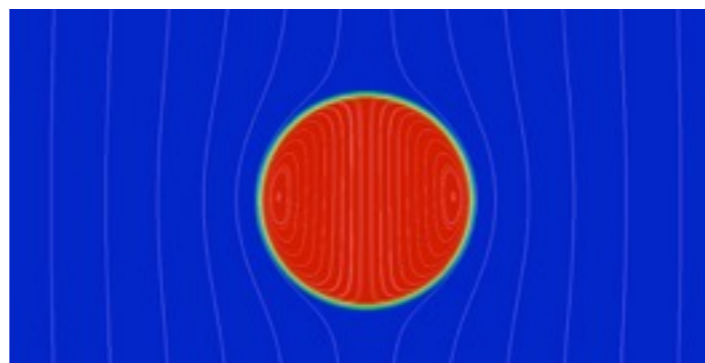
[Samuel, 2012]
+ this work

Summary: stability region

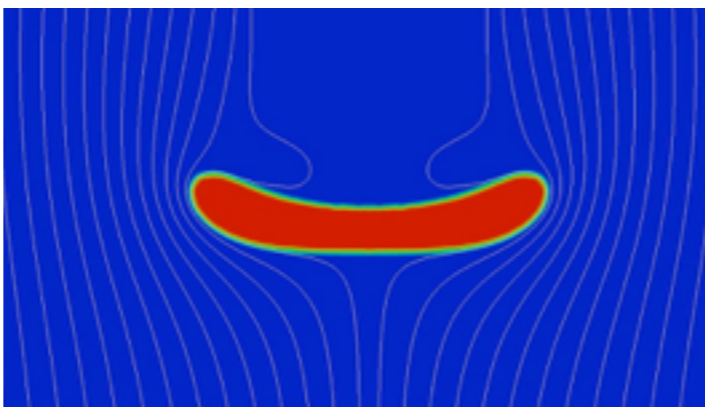
$$We-Re \text{ stability condition: } a_1/Re + a_2/We < C_D$$



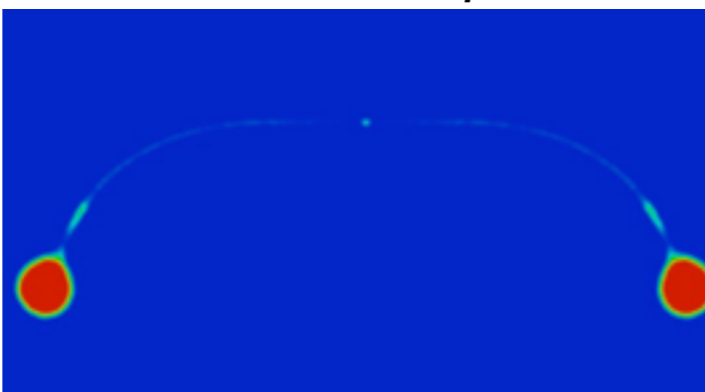
Sinking distance



1. "Pancake-like" flattening



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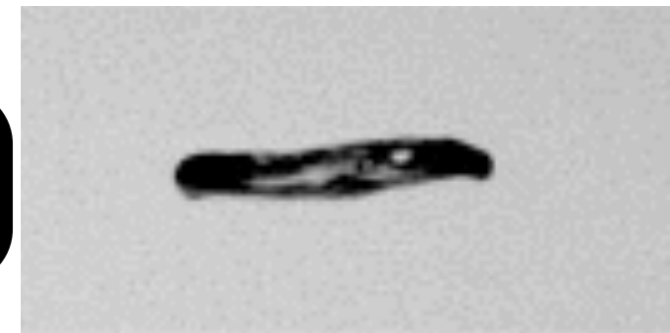


[Samuel, 2012]
+ this work

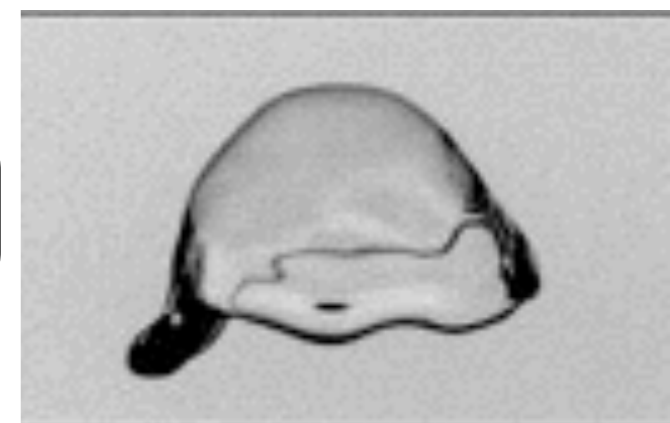
$z=0$



$z < R$



$z \sim R$



[Villermaux, 2007]

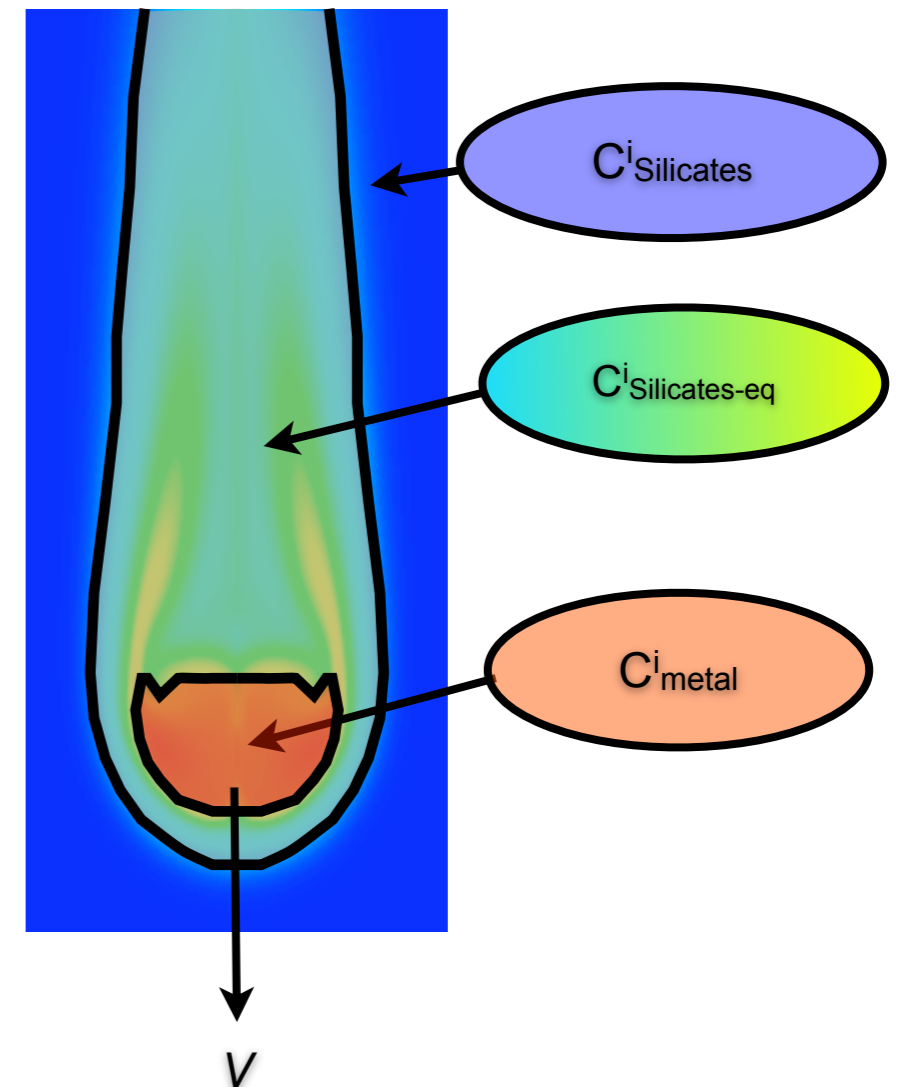
Metal-Silicate Equilibration in magma oceans

Fick's law: $\frac{dC_m}{dt} = (1 - C_m) \sqrt{\frac{9}{2} \frac{1}{Pe}}$

Chemical Péclet number: $Pe = \frac{v_\infty R_0}{\kappa_c}$

Degree of equilibration: $C_m(t) = 1 - e^{-t \sqrt{\frac{9}{2} \frac{1}{Pe}}}$

*Essentially molten, Newtonian
magma ocean*



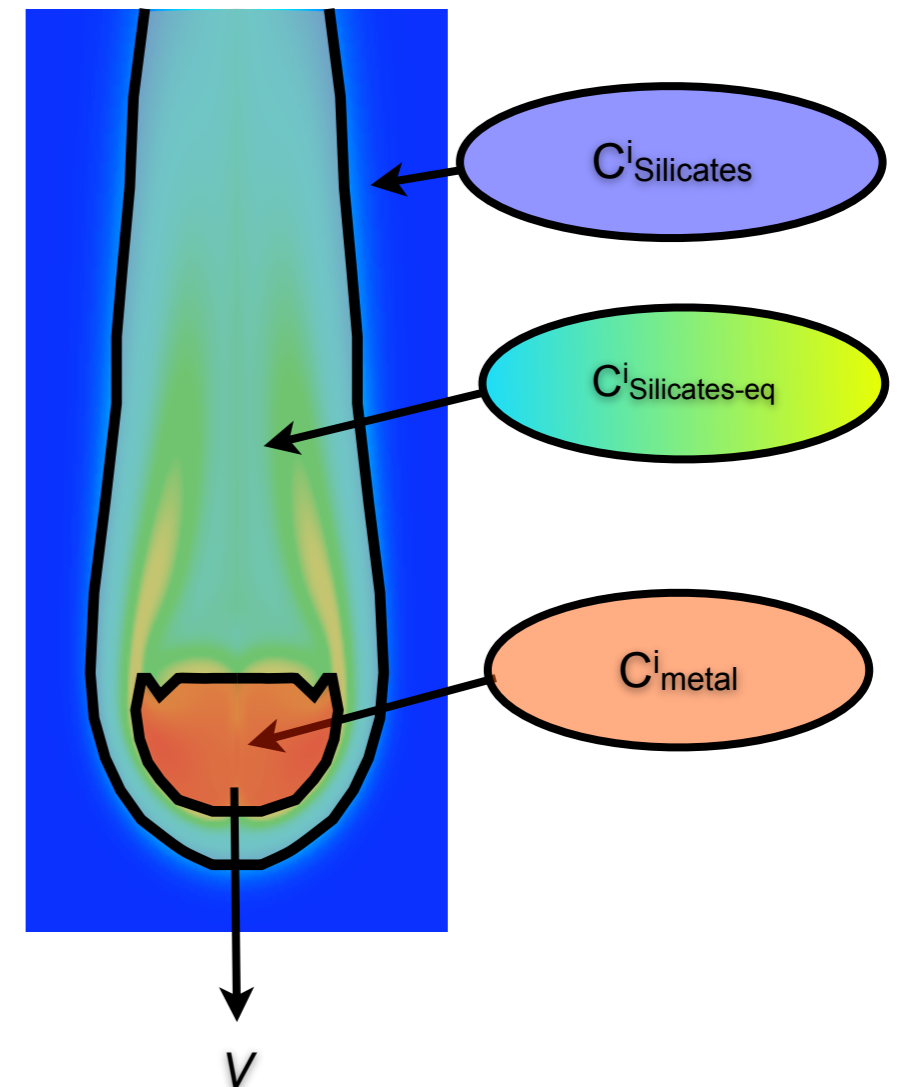
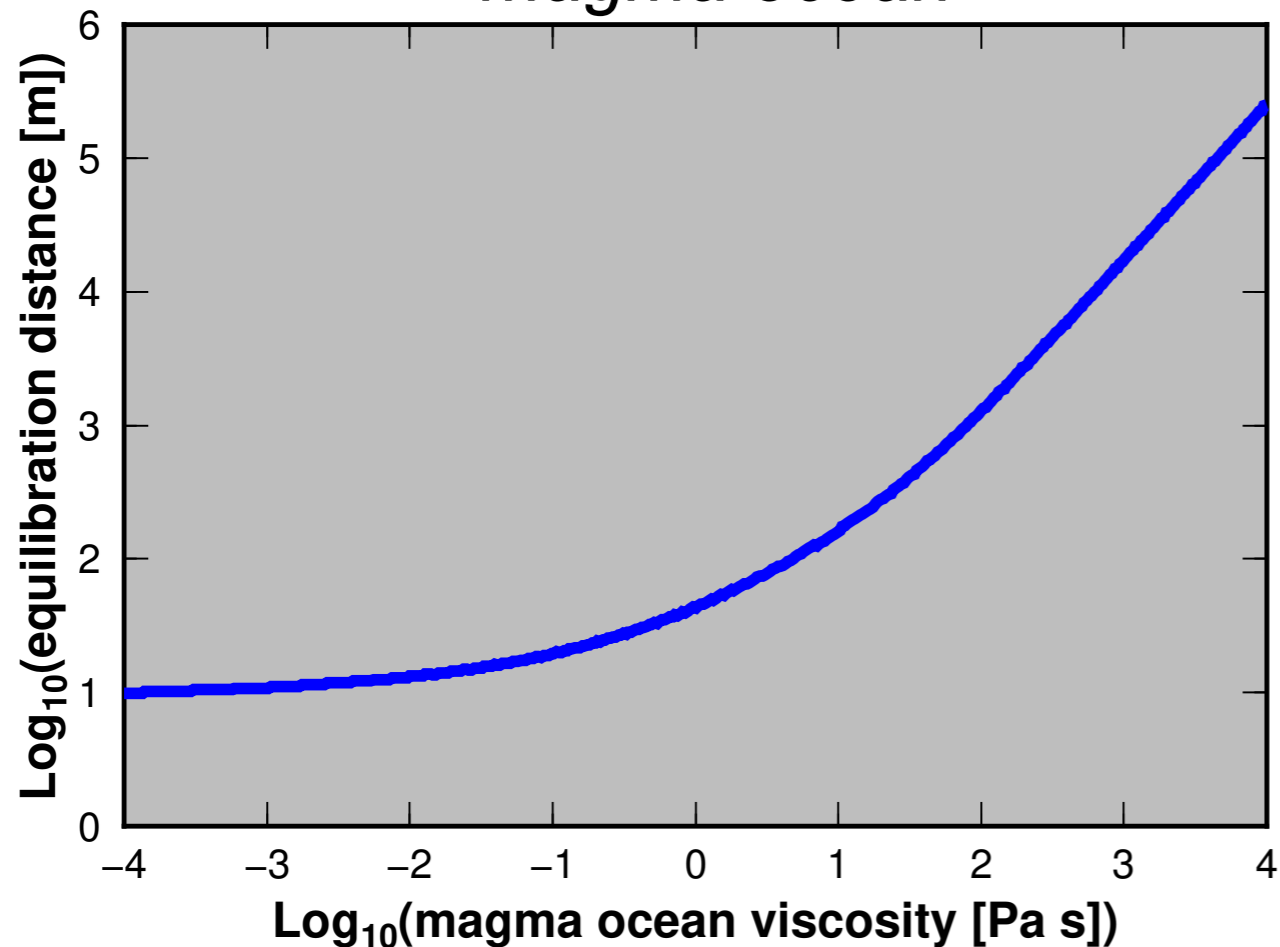
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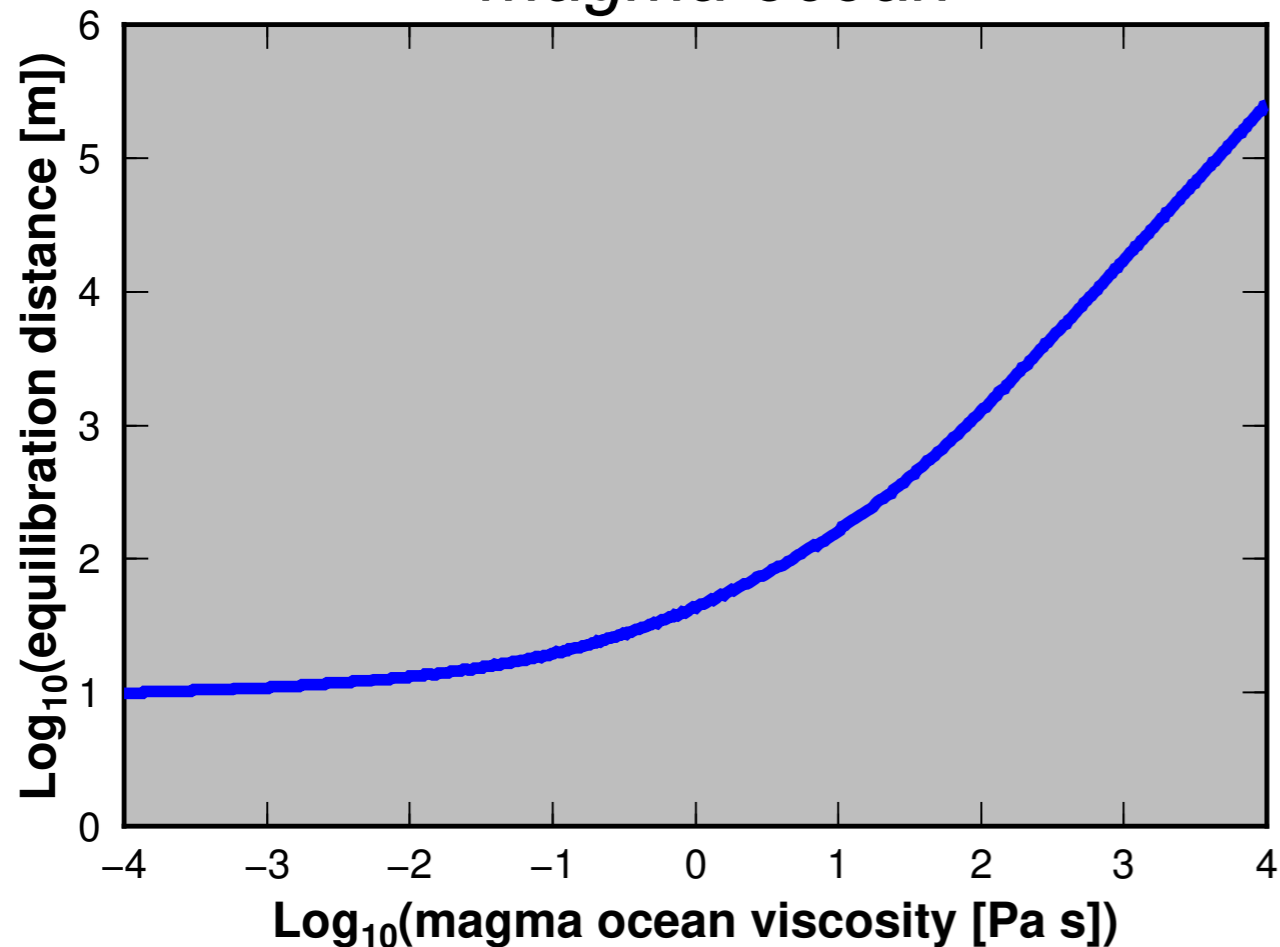
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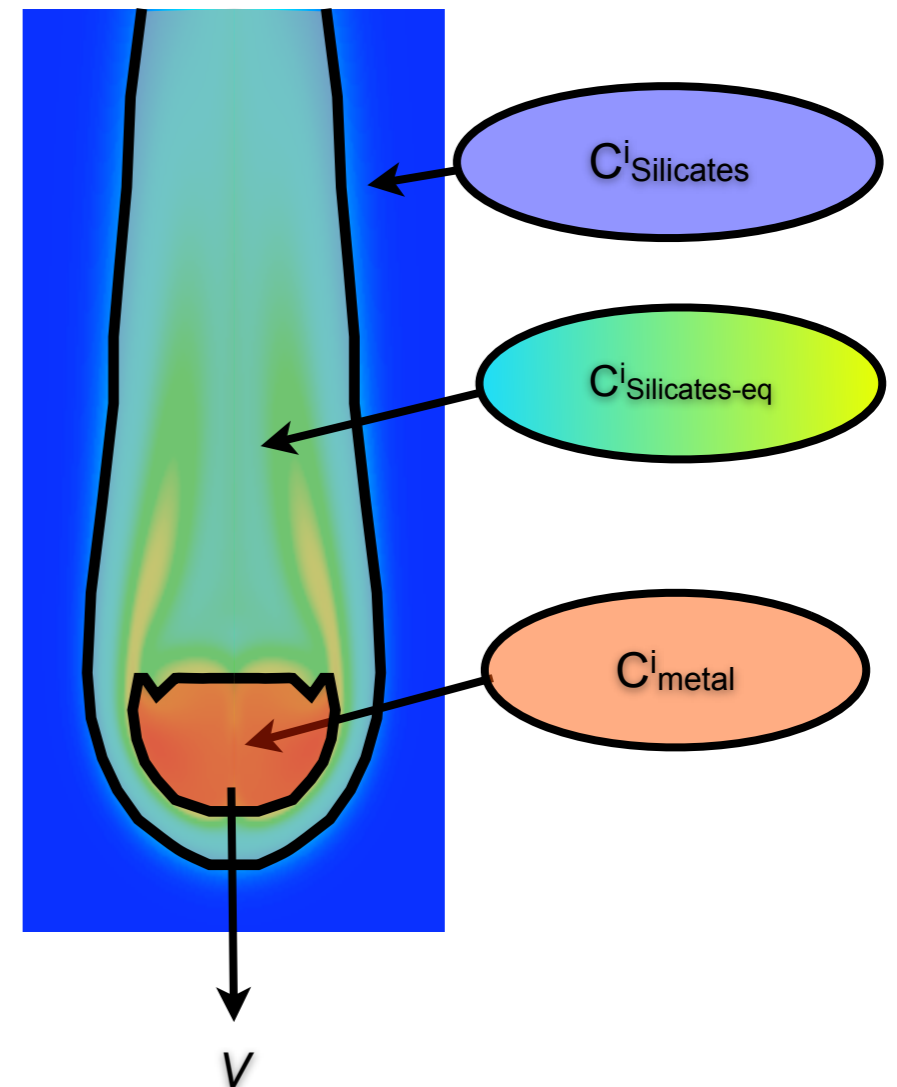
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⇒ **Complete or partial equilibration likely for plausible values of magma ocean viscosities**



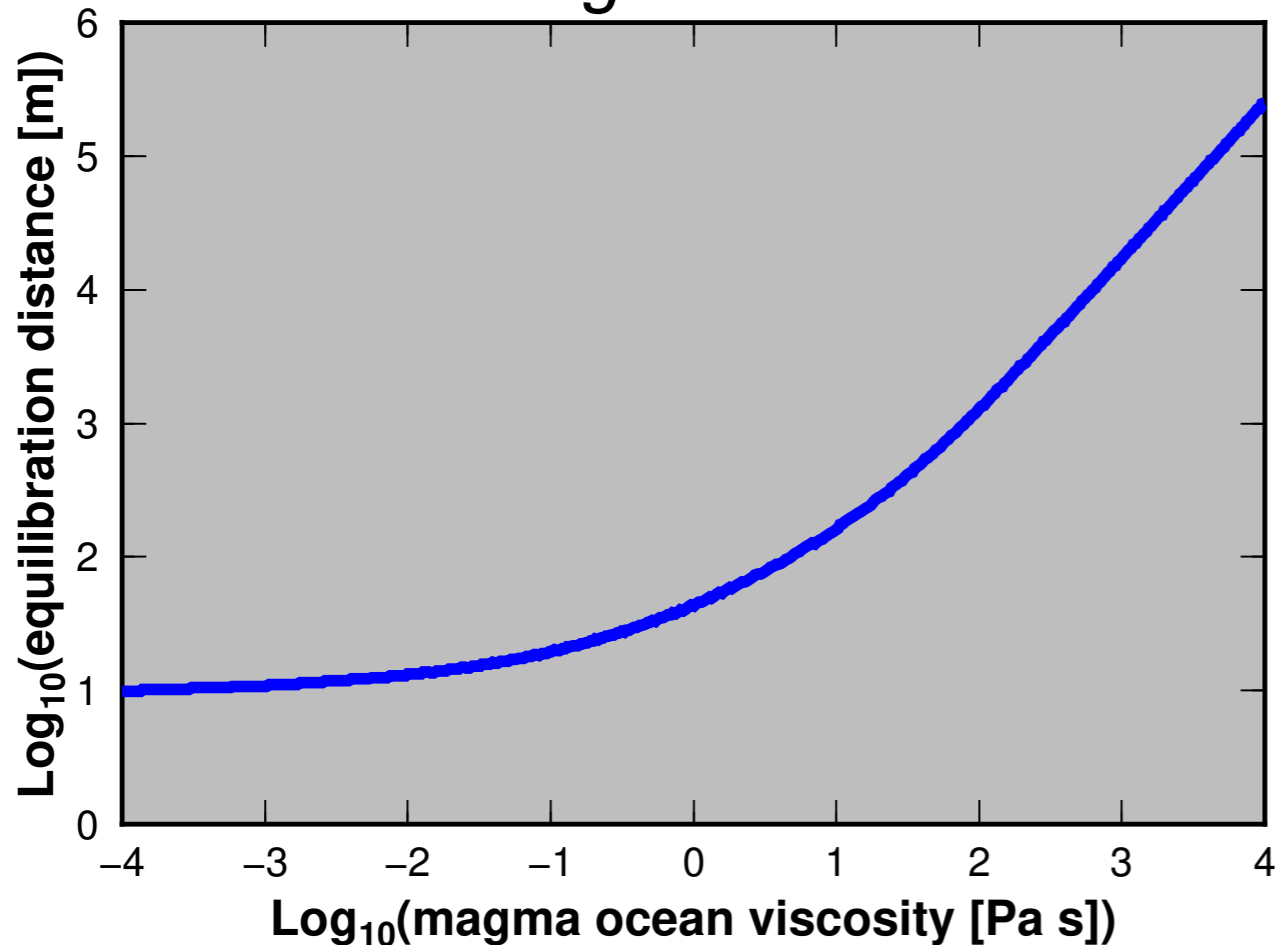
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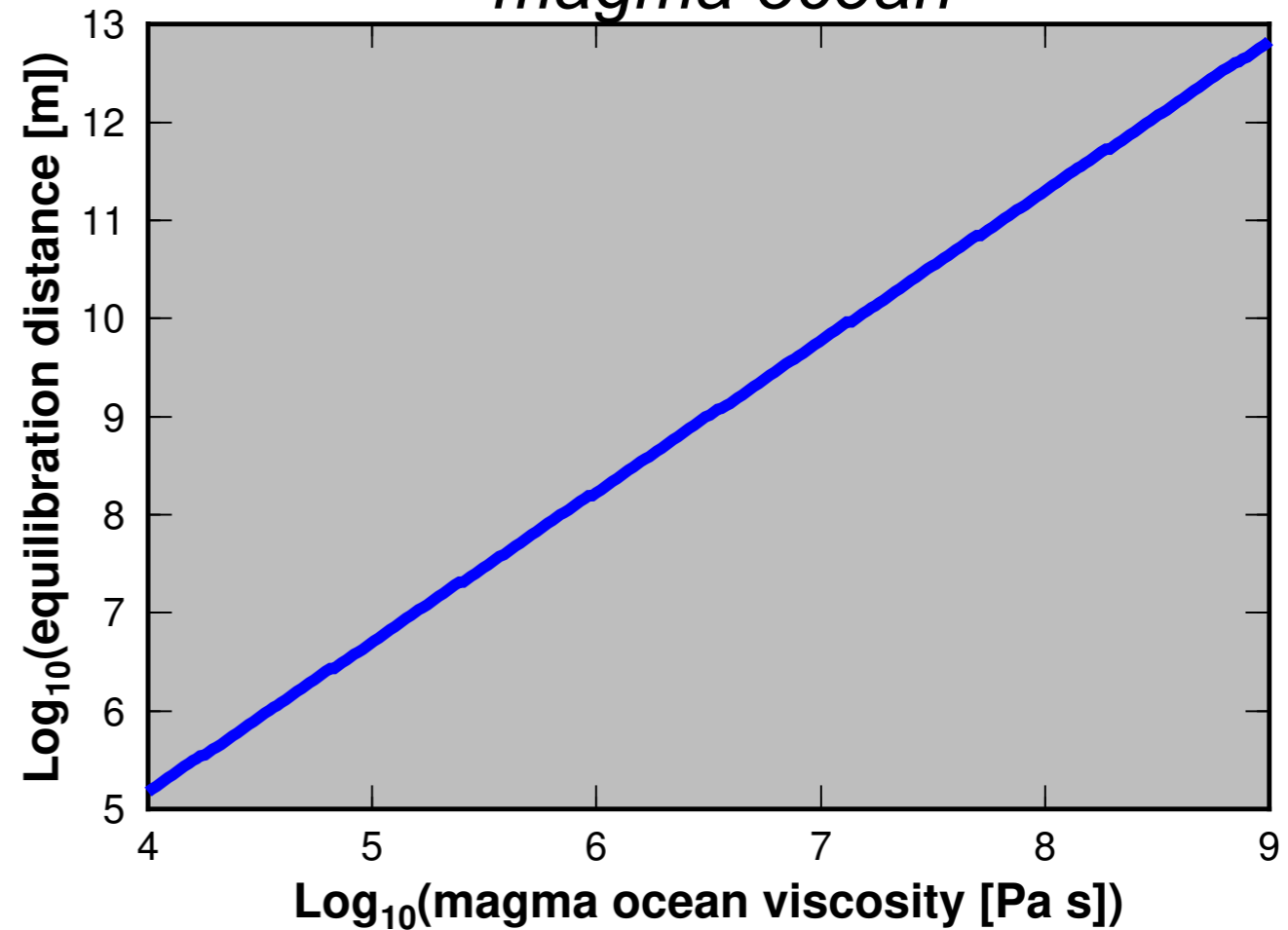
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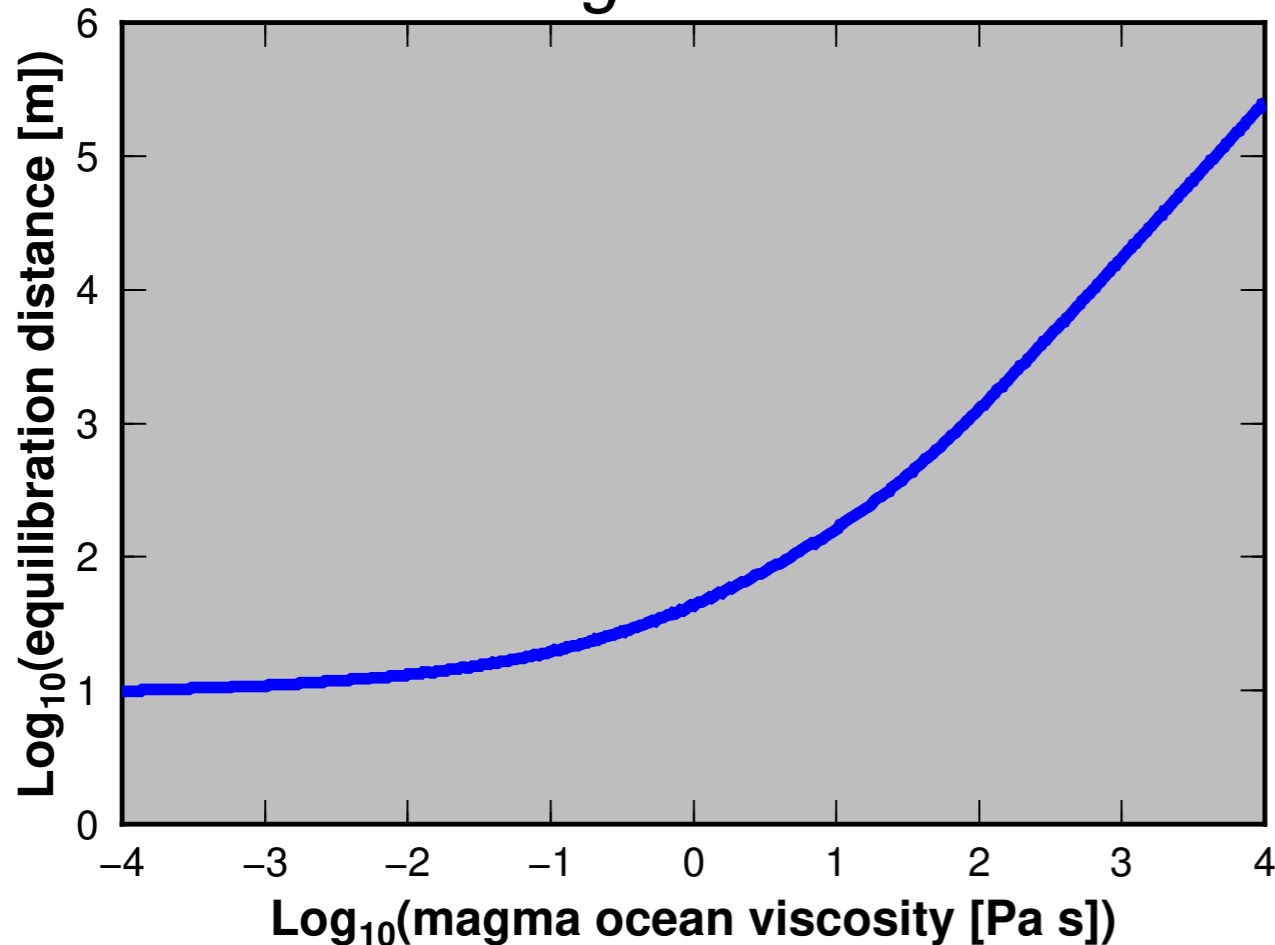
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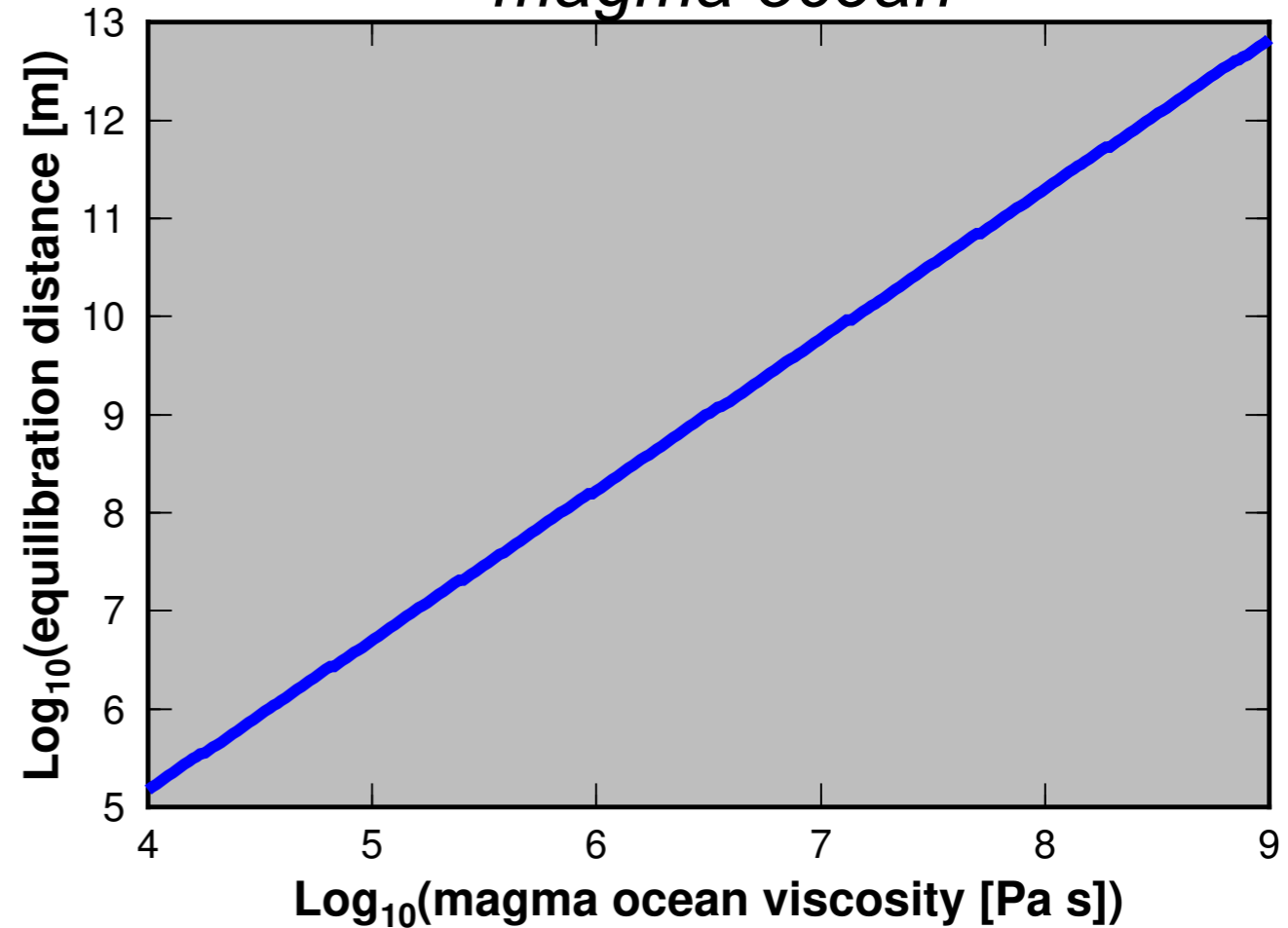
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⇒ **Complete equilibration unlikely**

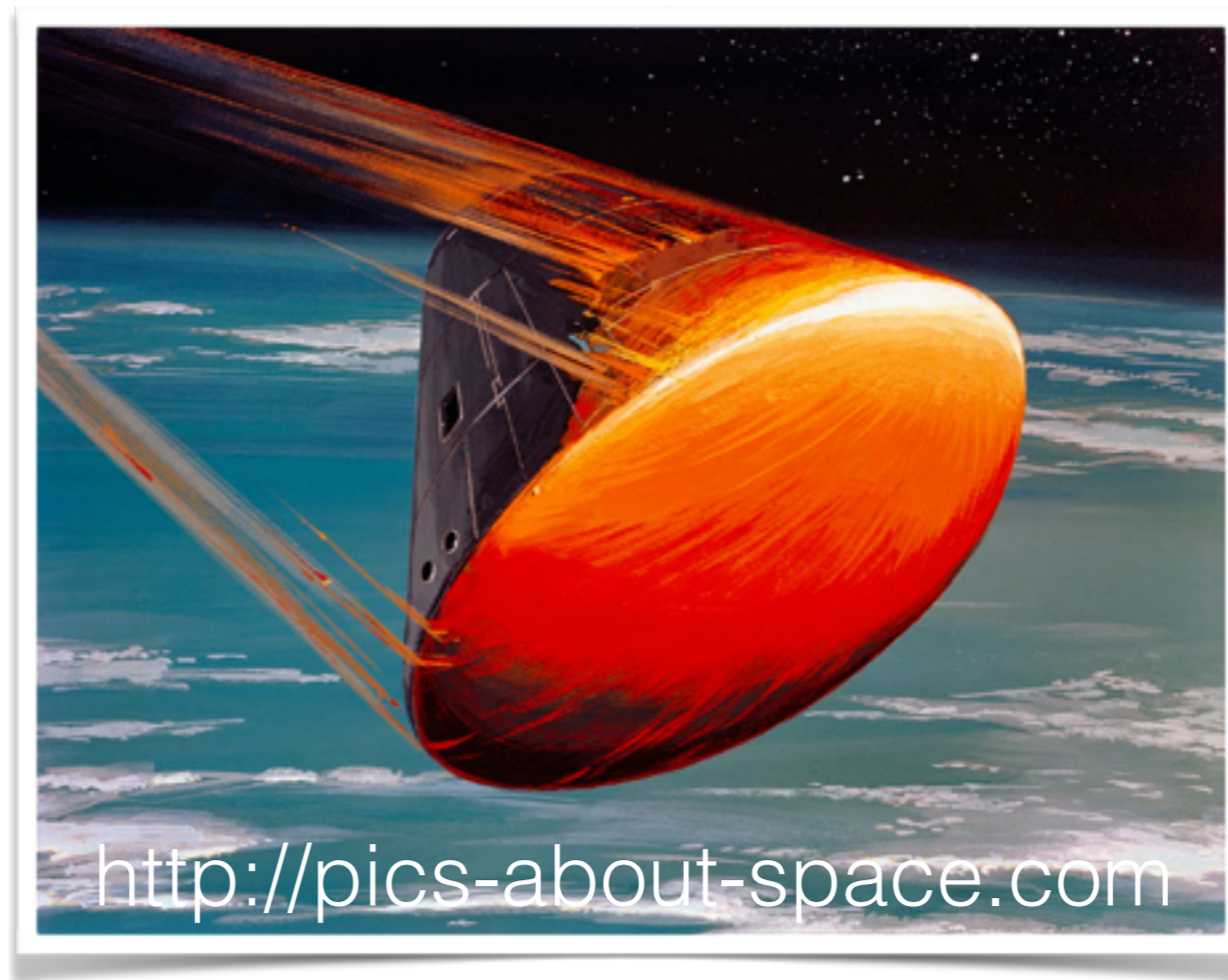
Viscous heating and heat partitioning

Gravitational potential energy \Rightarrow Kinetic Energy \Rightarrow Heat

$$E_p = (\rho_m - \rho_s) g \Delta h V_d$$

$$E_k(t, Si, Fe) = (\rho/2) V u^2 ?$$

$$E_T(t, Si, Fe) = \rho \Delta T C_p V ?$$



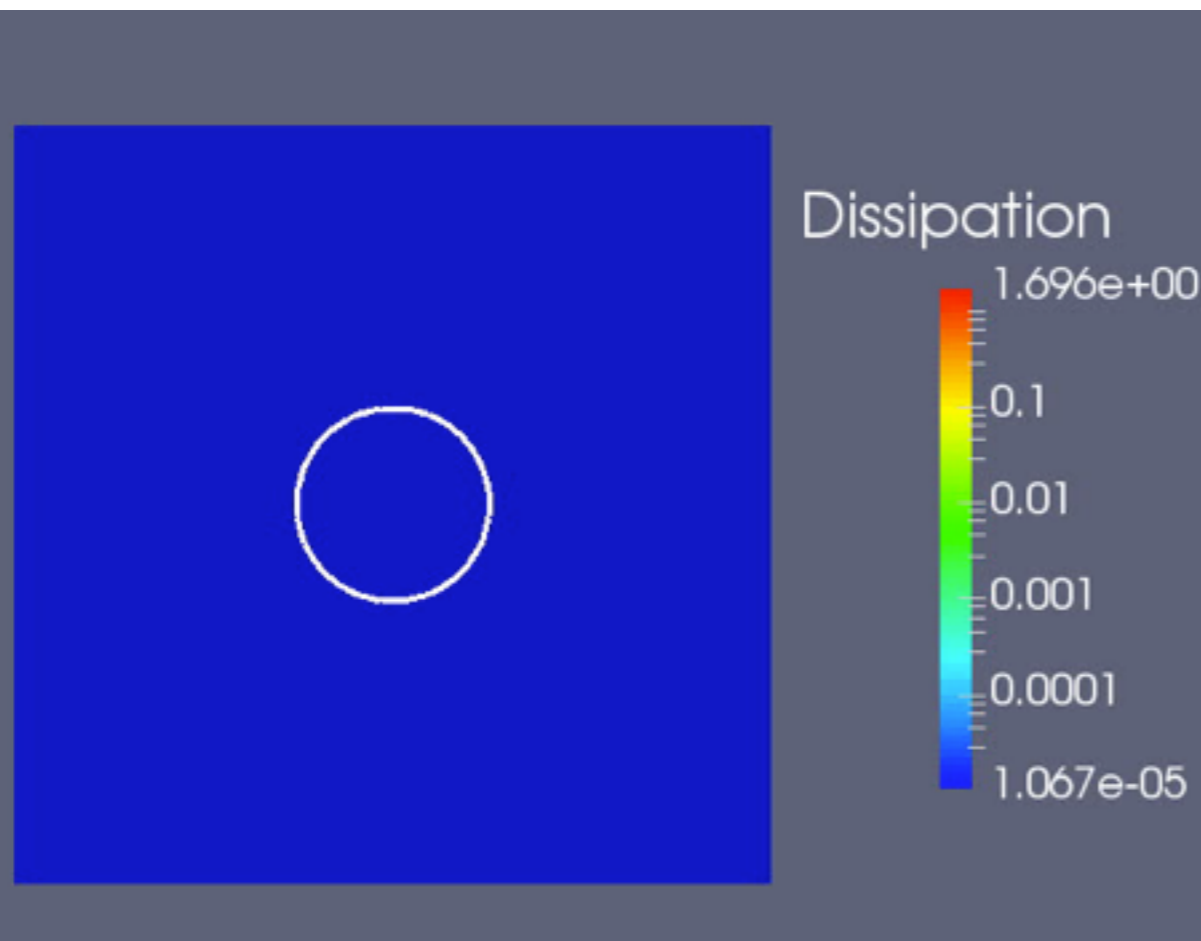
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$$\Pi_v = \frac{\eta_s V_\infty}{R \rho_s C_p \Delta T}$$

$$Pe = \frac{V_\infty R}{\kappa}$$

$\Pi_v=10$



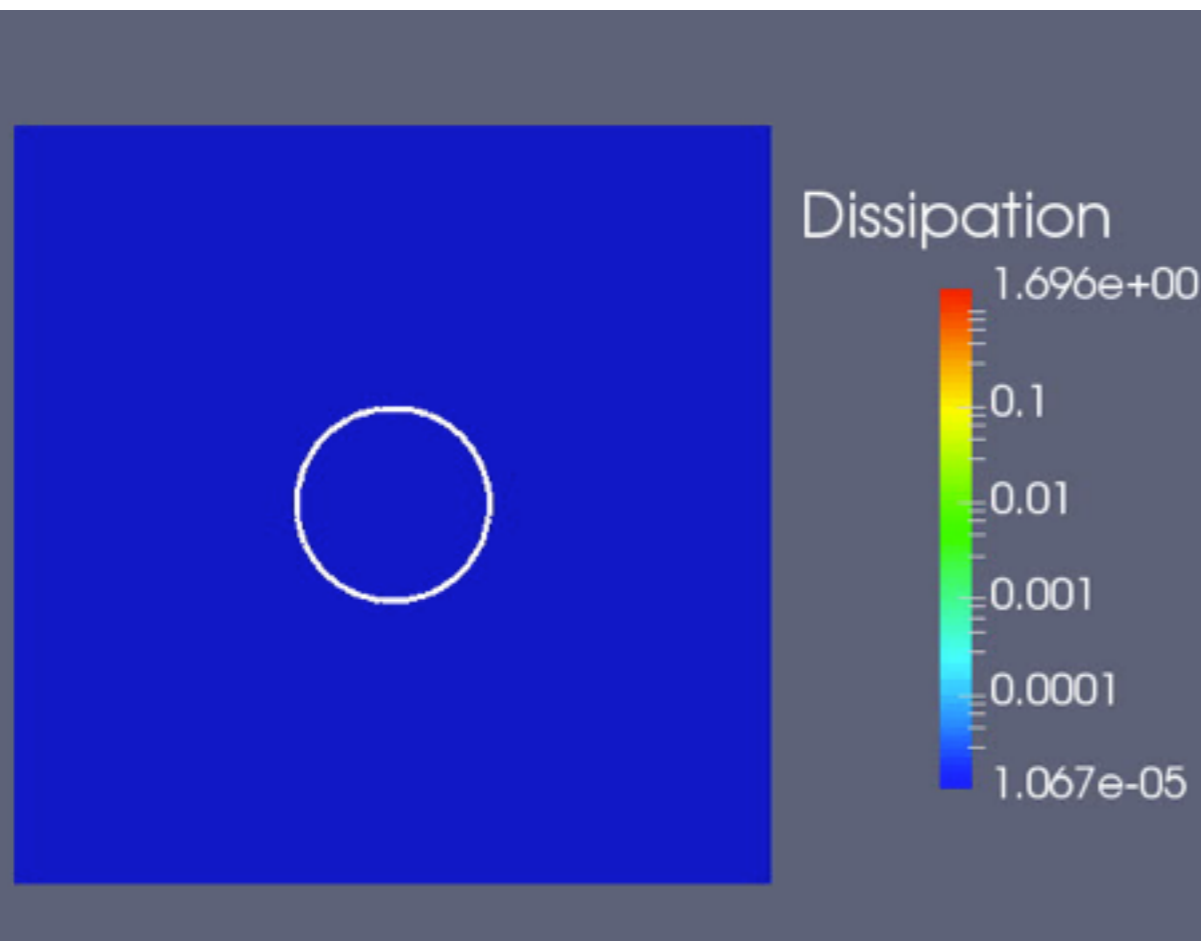
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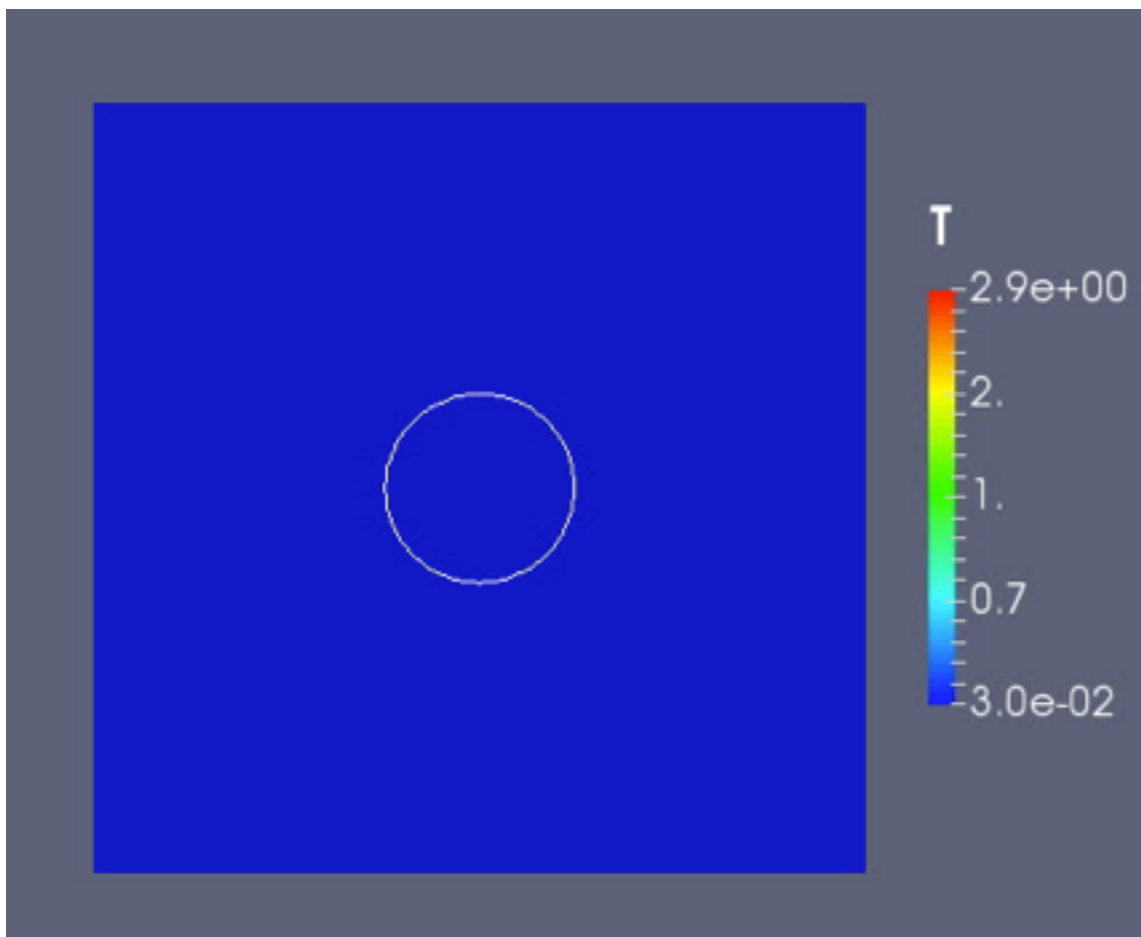
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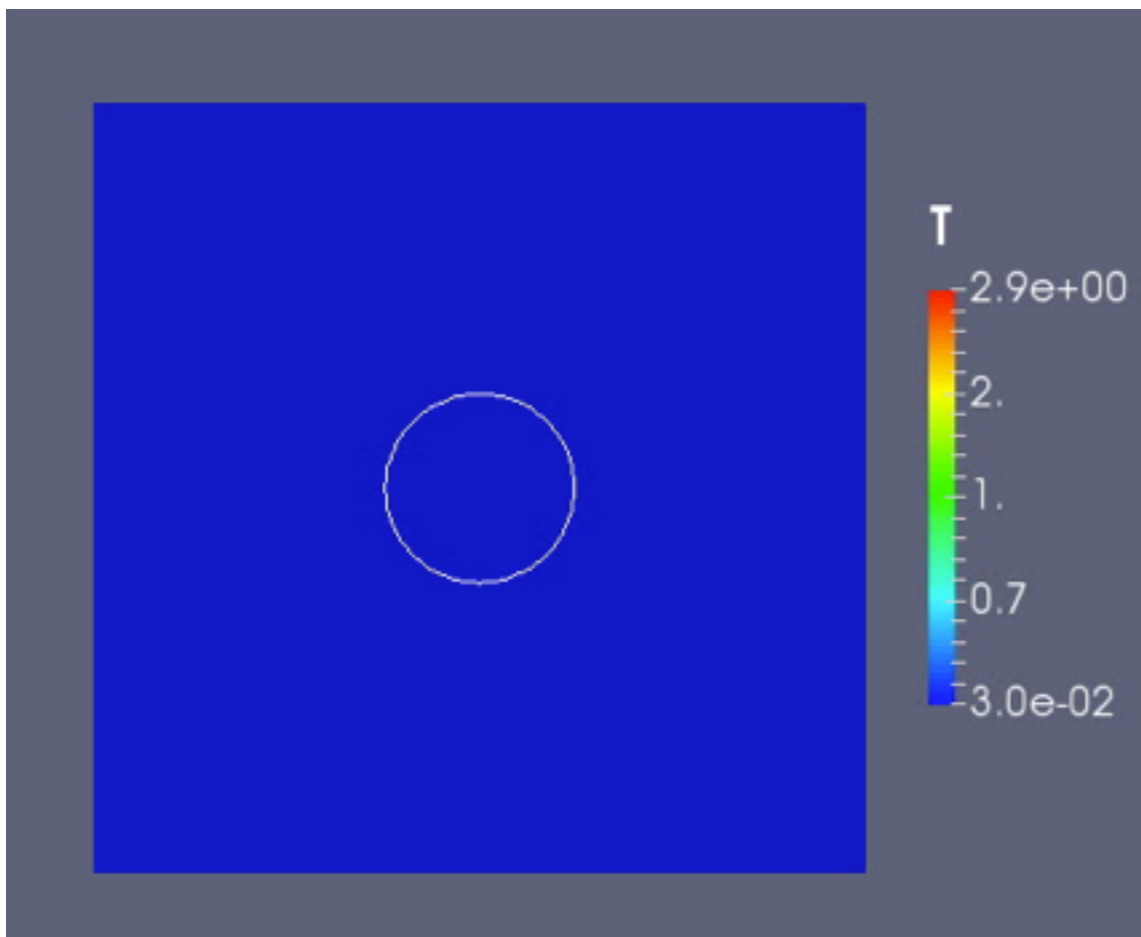
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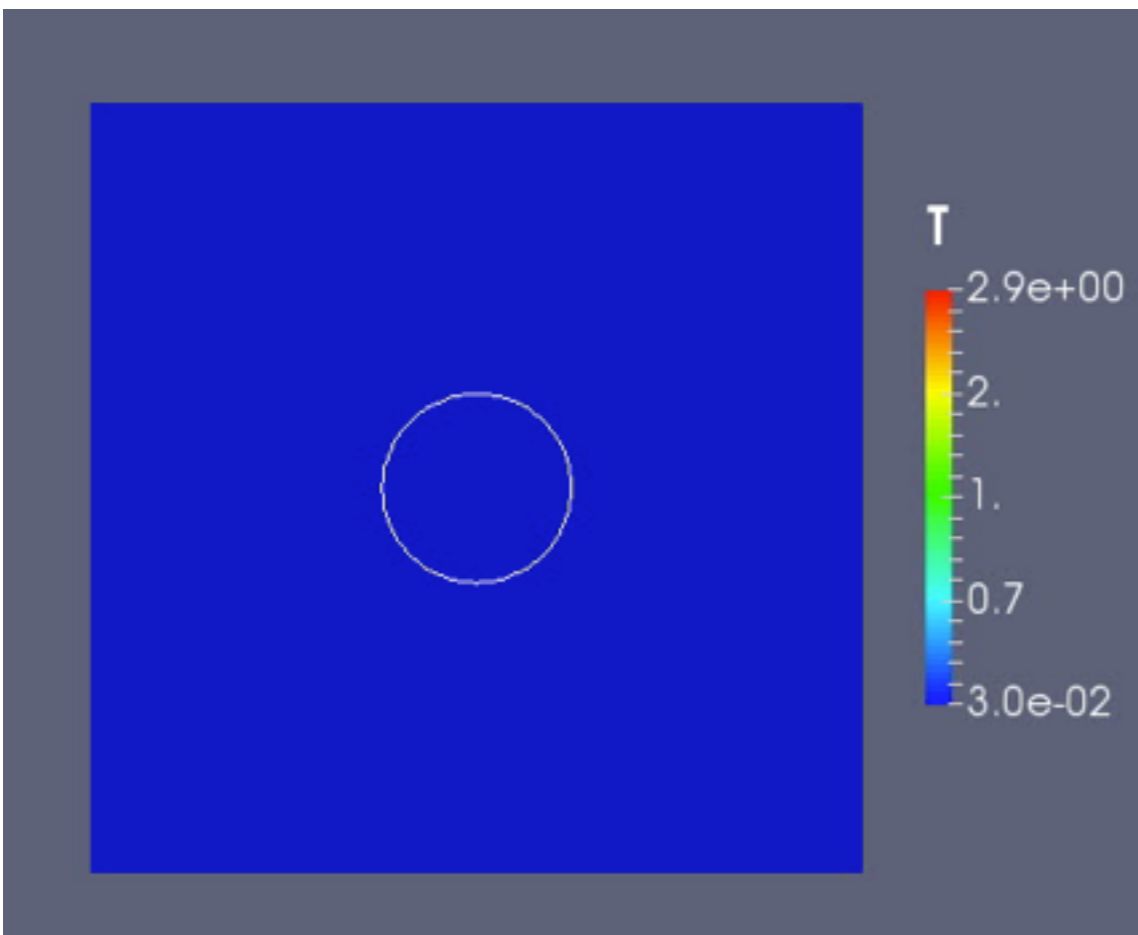
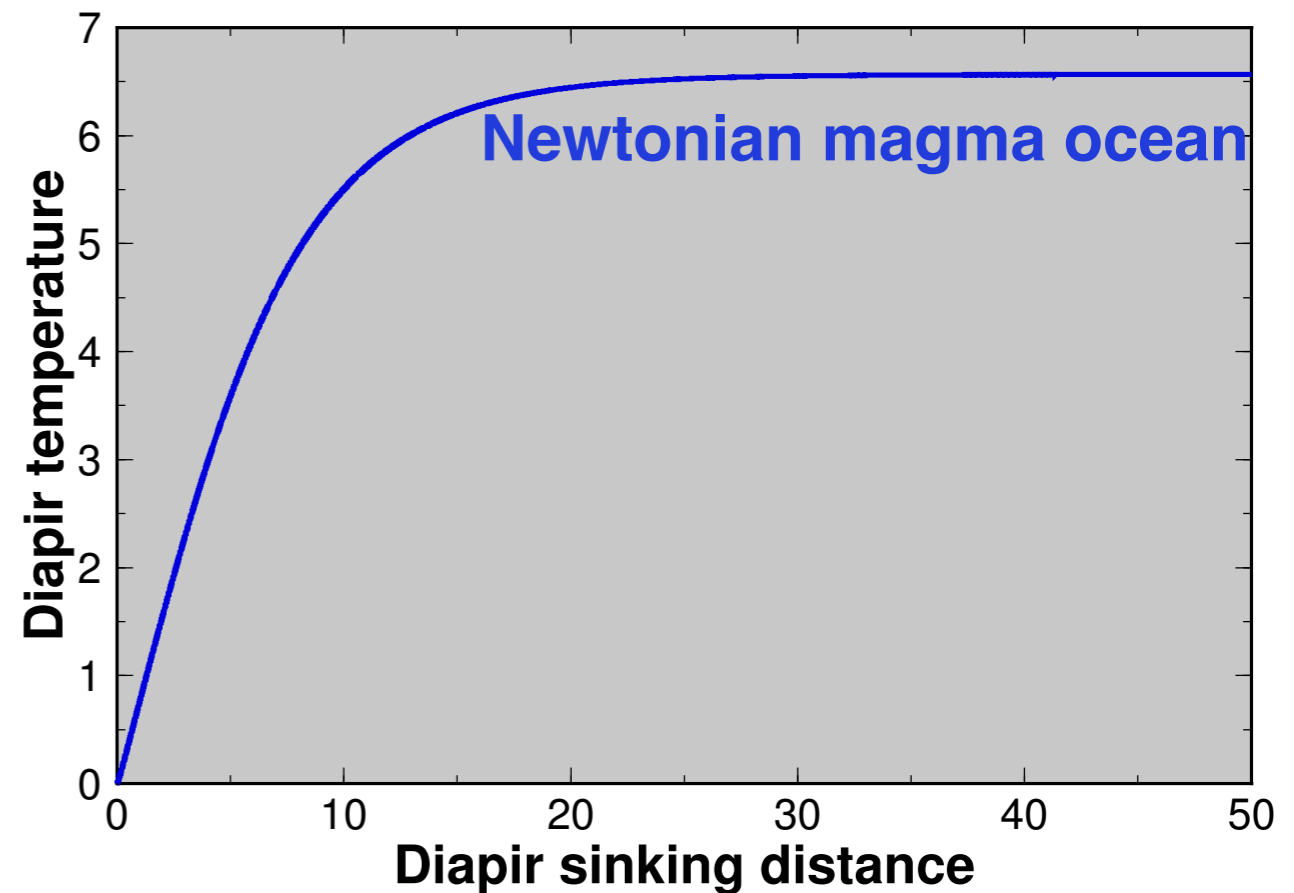
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 diffusion viscous heating

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$Re=10 \quad We=1$



Viscous heating and heat partitioning

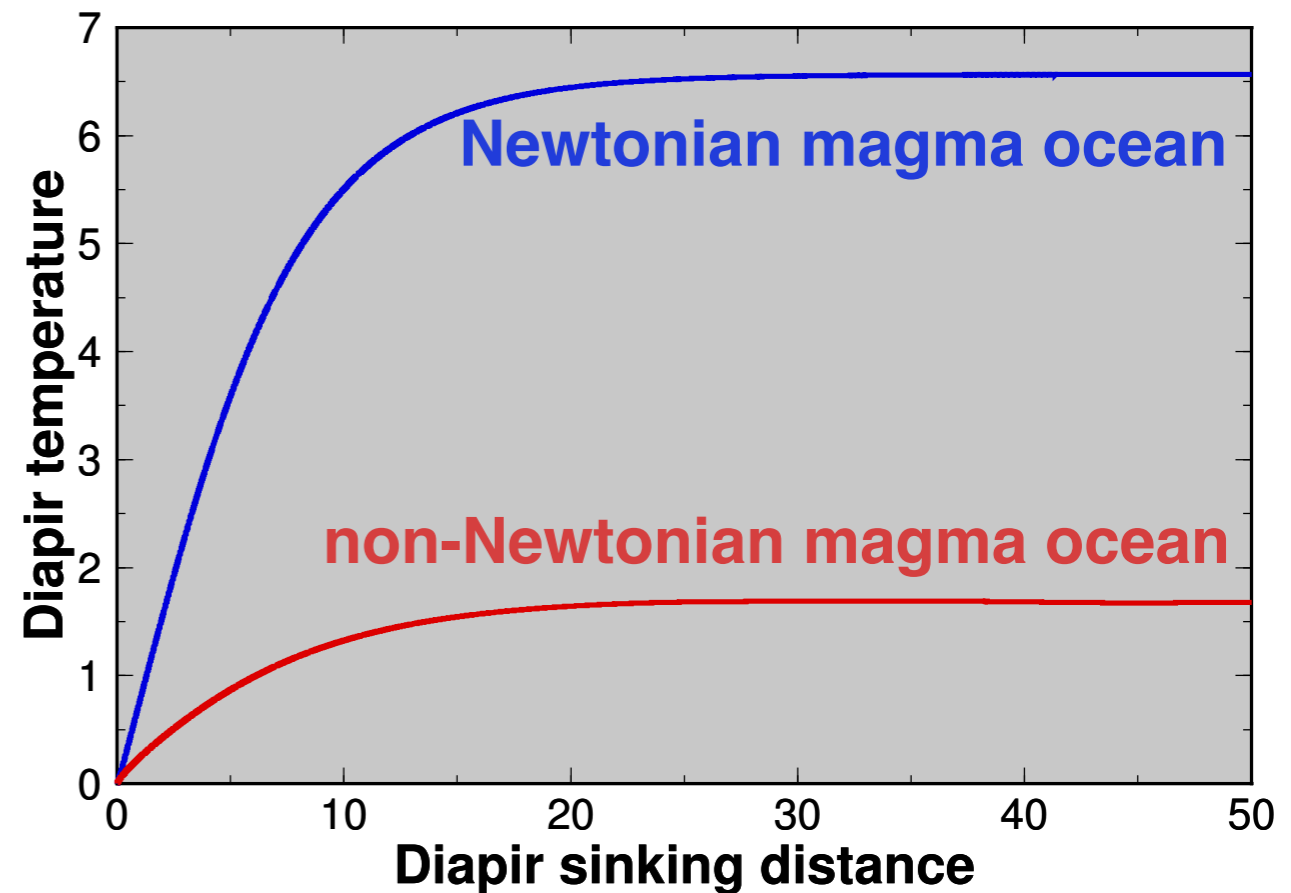
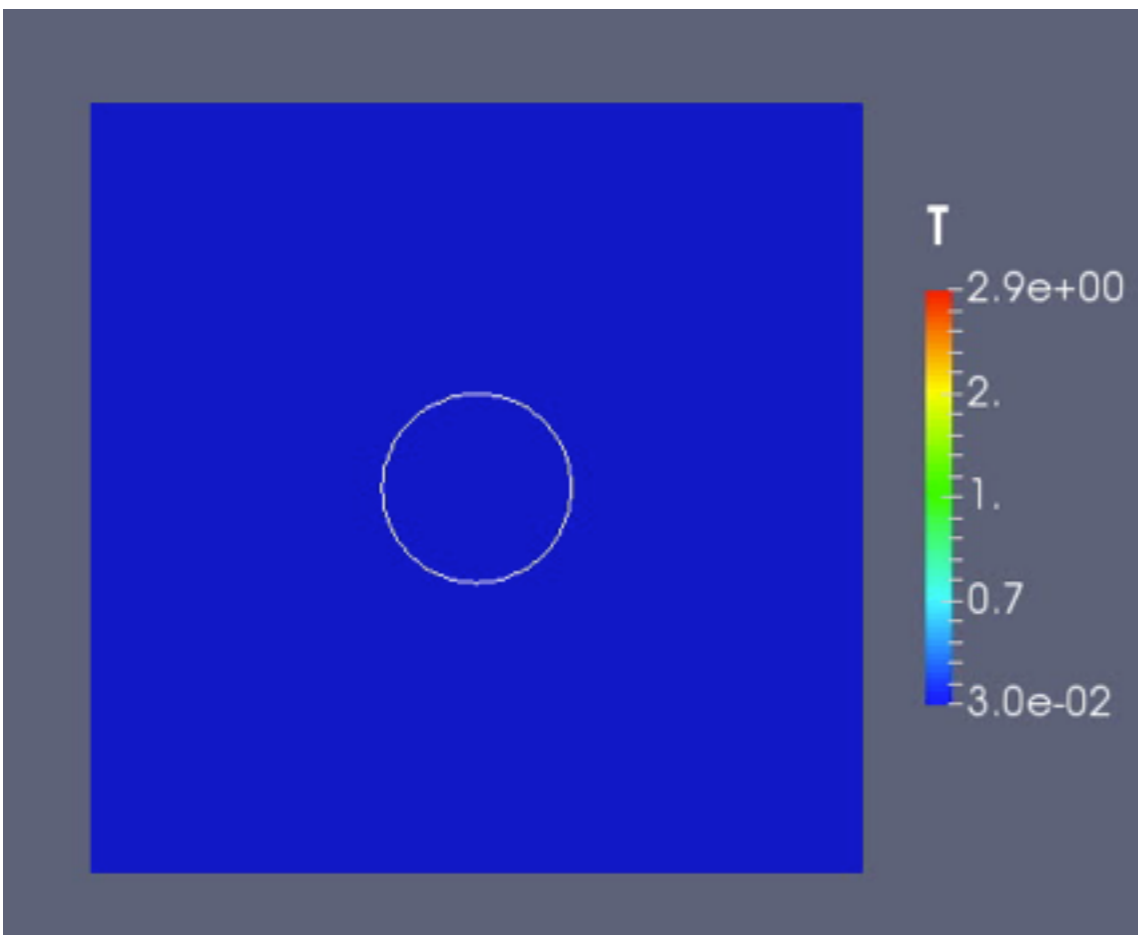
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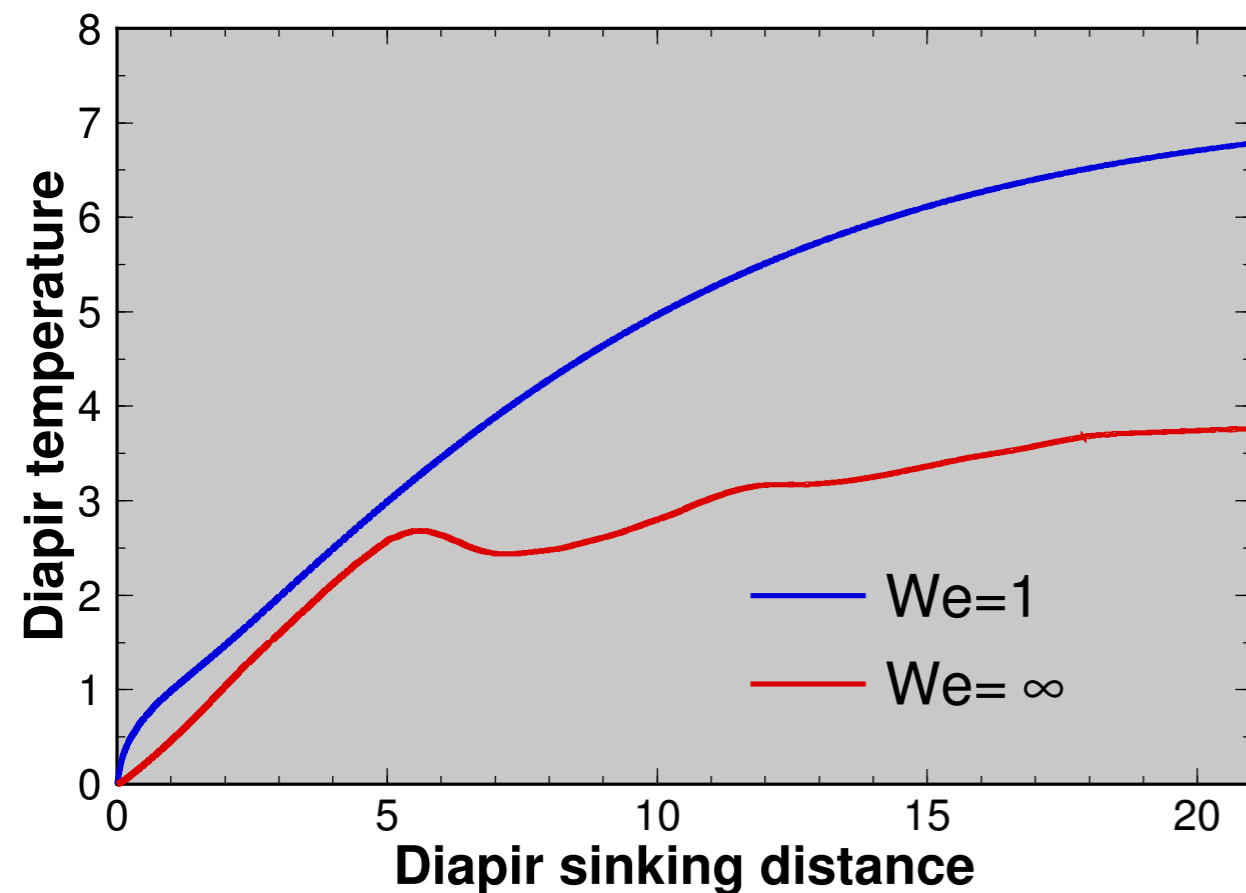
diffusion
viscous heating

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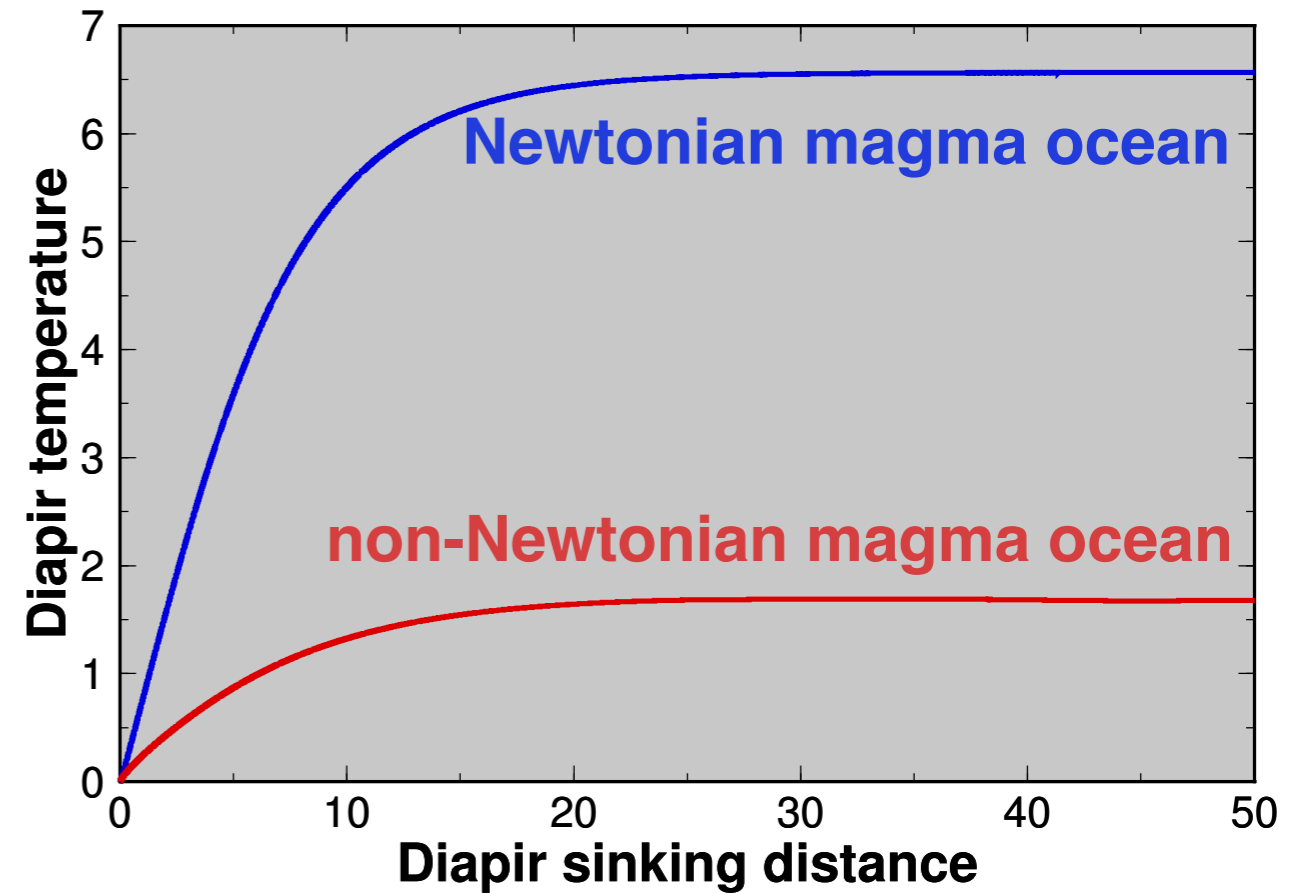
$$Pe = \frac{V_\infty R}{\kappa}$$

$\Pi_v=10$

Re=100



Re=10 We=1



Viscous heating and heat partitioning

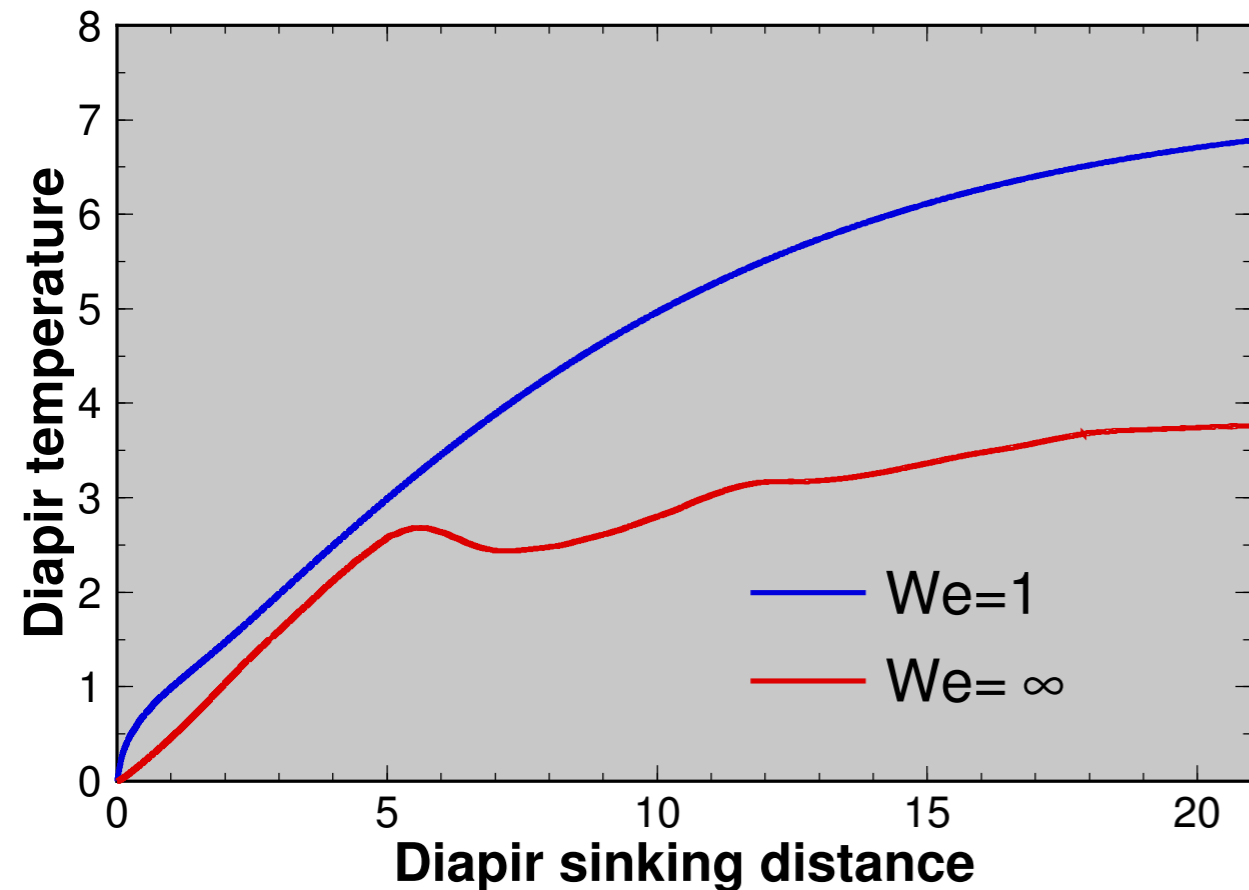
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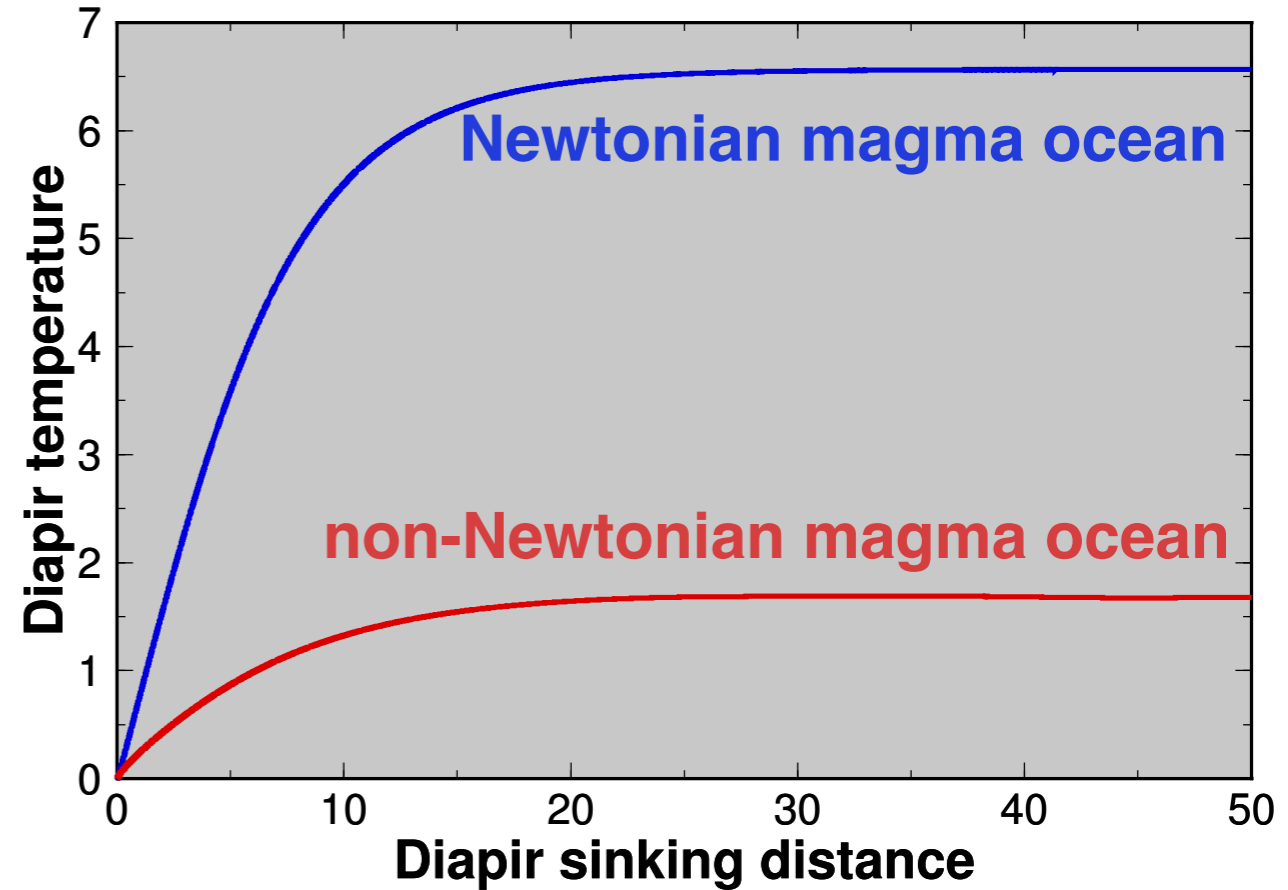
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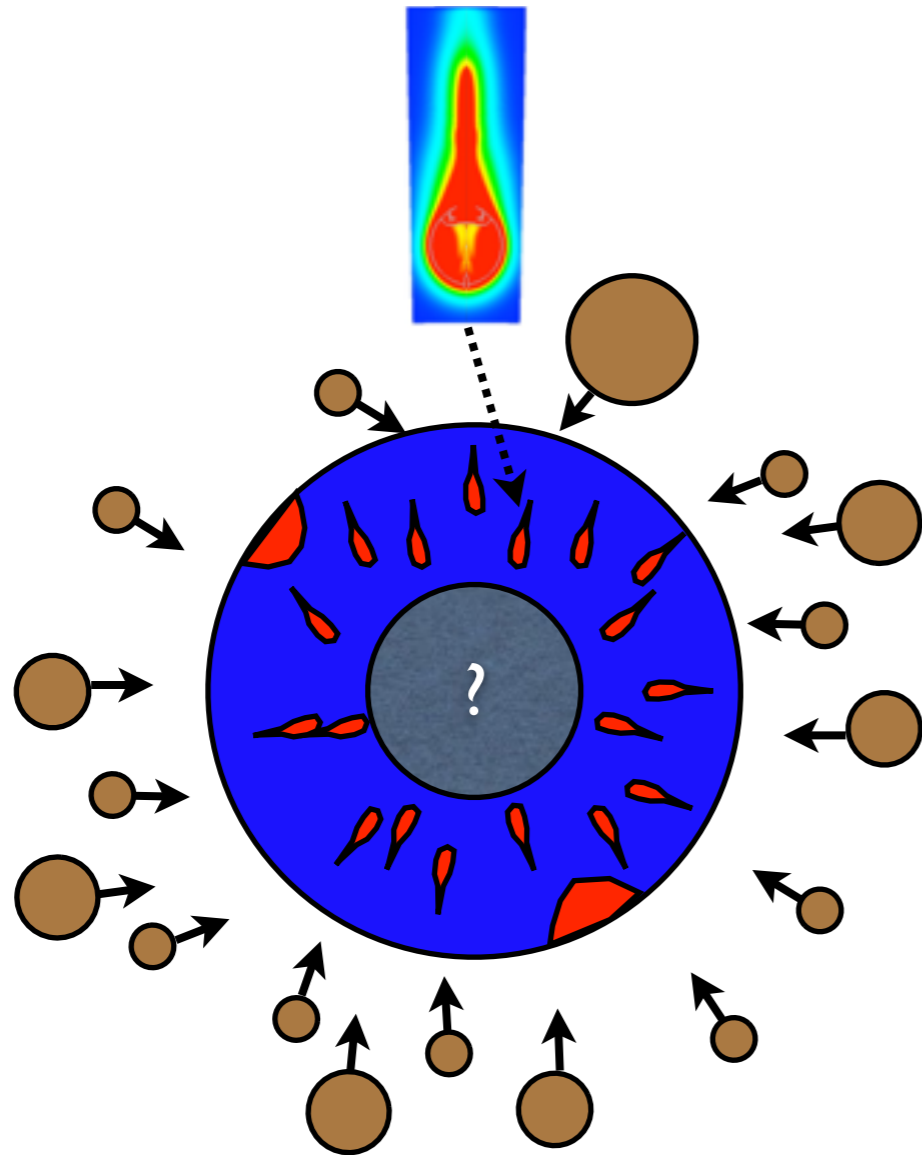


Re=10 We=1

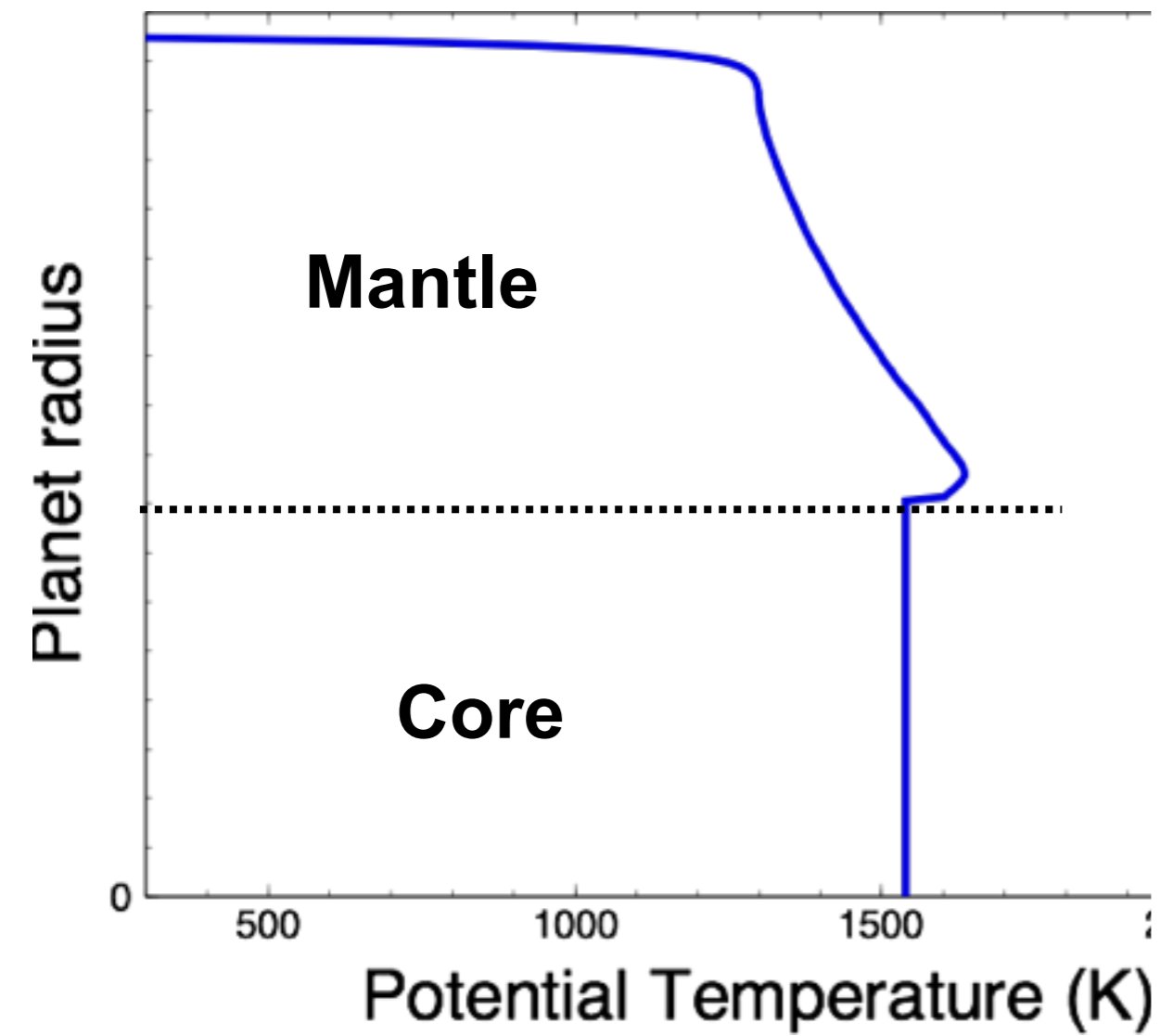


Rheology and dynamical history have a strong influence on Fe-Si heat partitioning

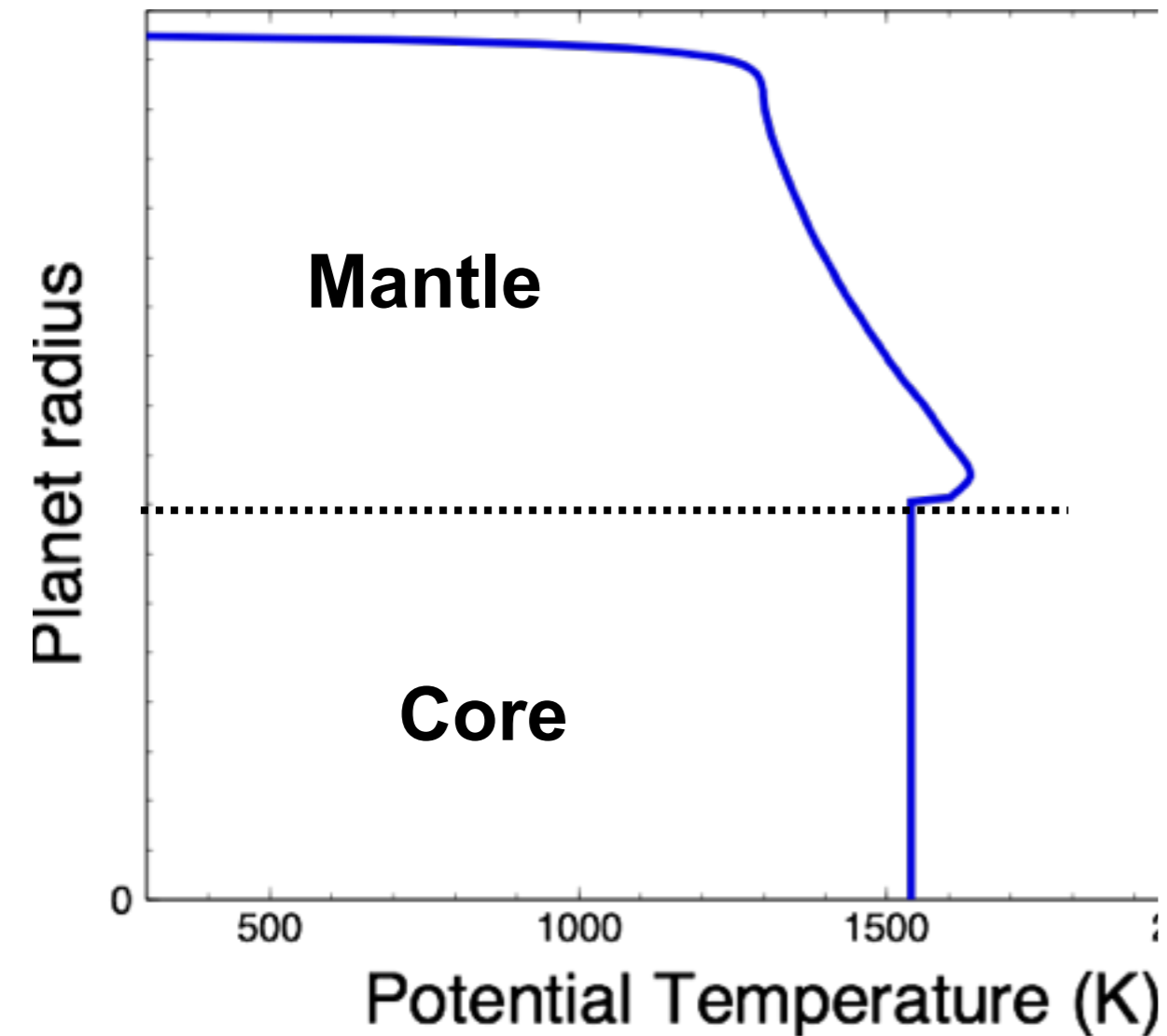
Early heat distribution



Early heat distribution

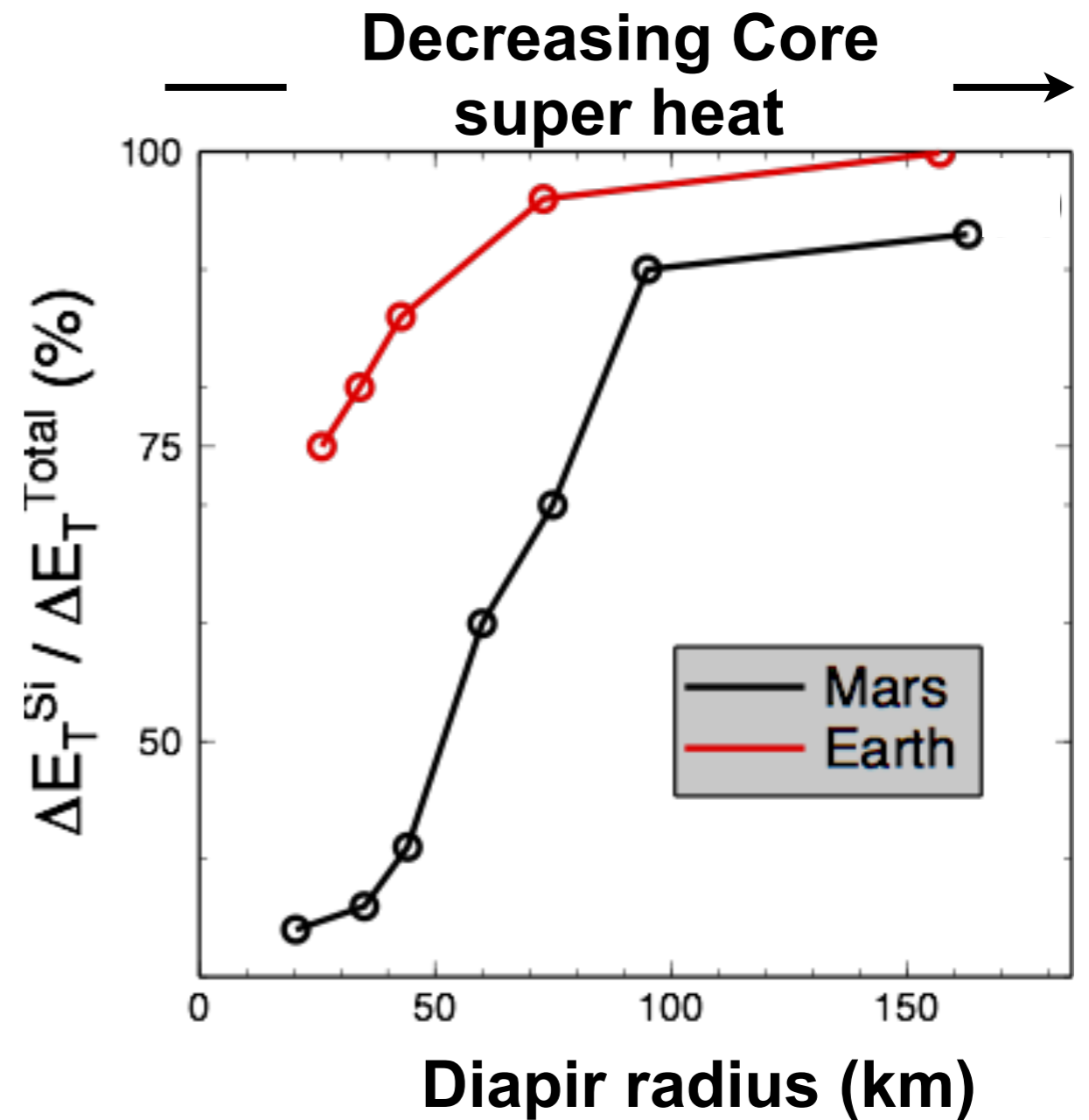
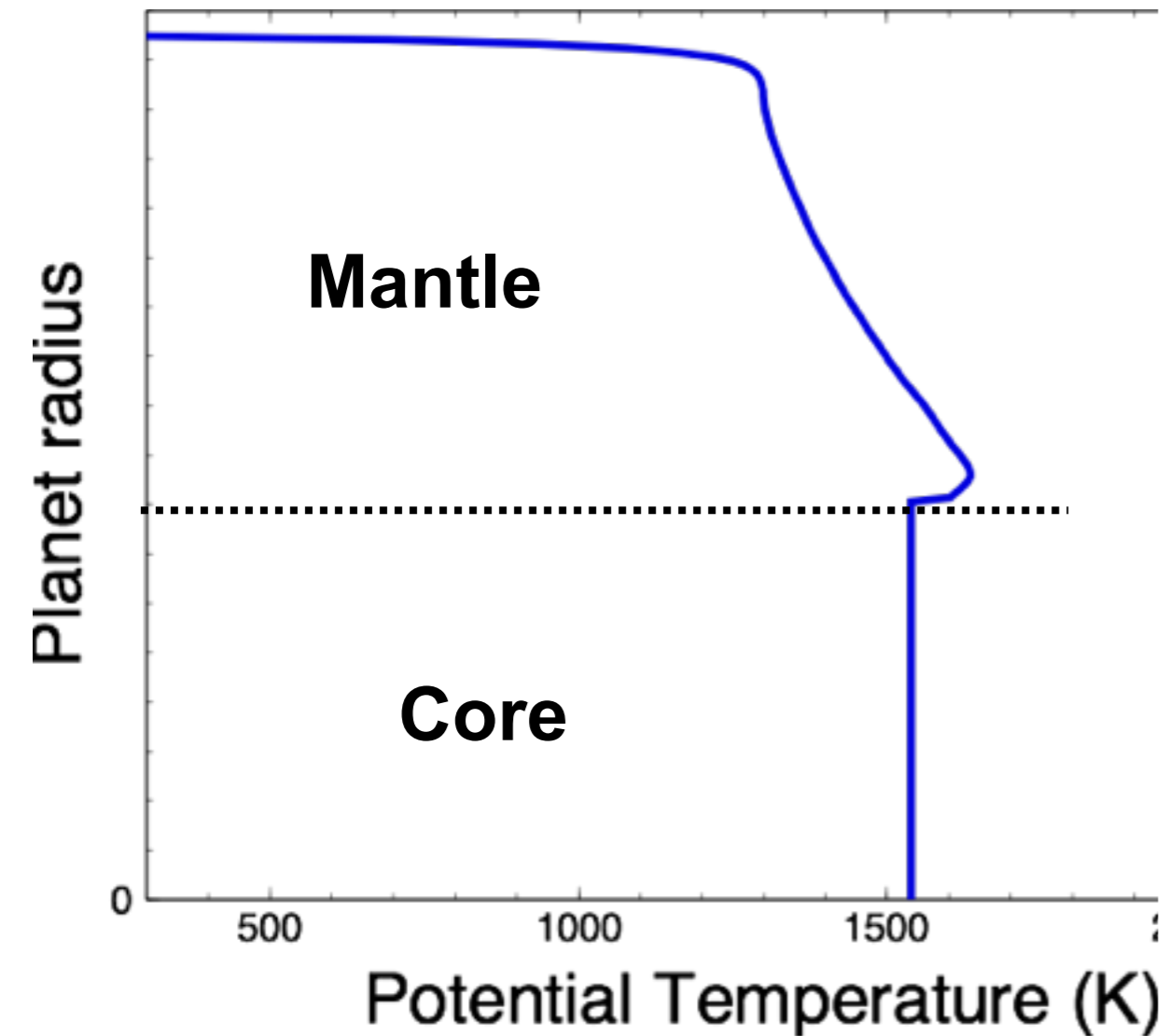


Early heat distribution



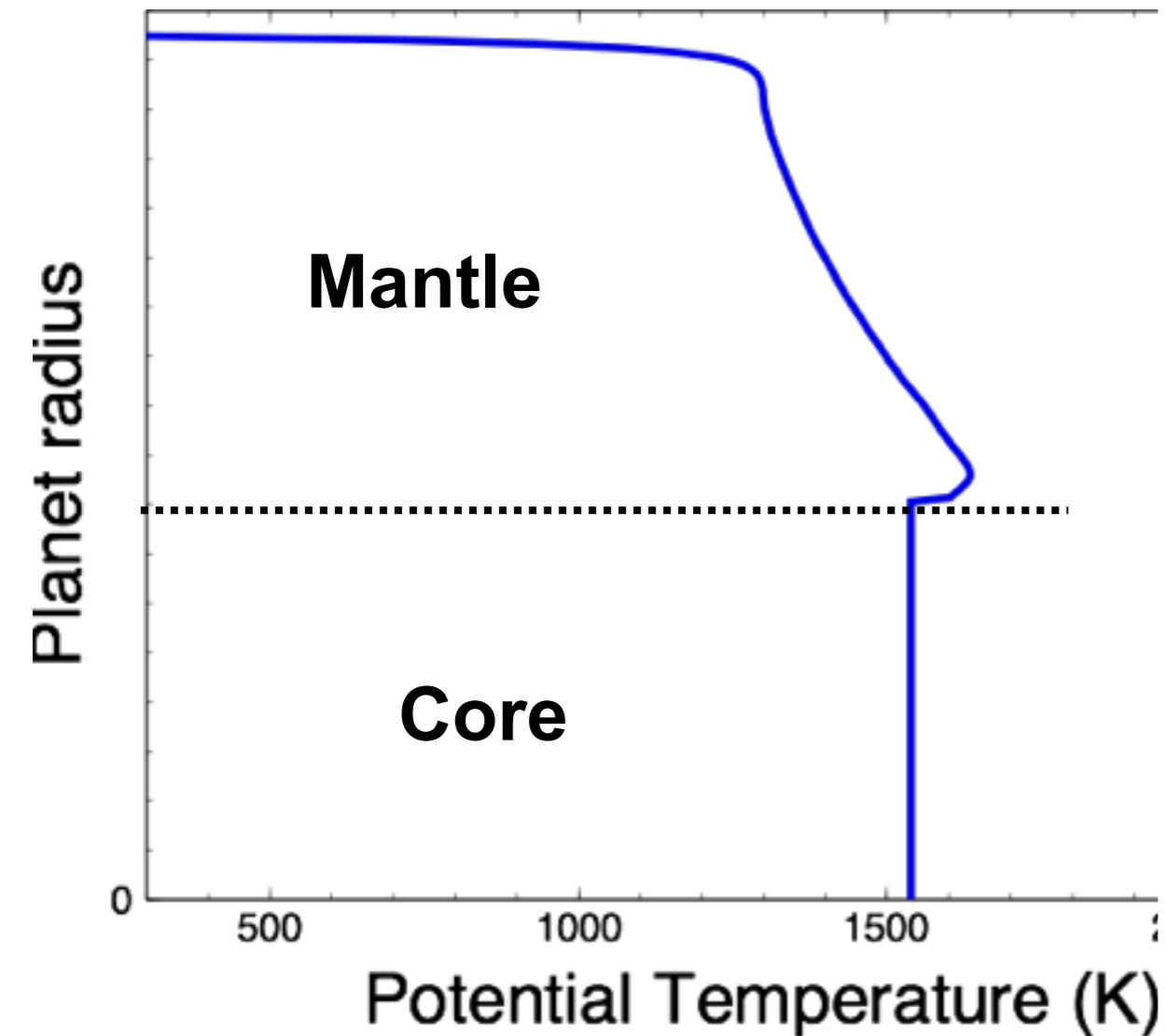
**Favours a hotter lowermost
mantle with melting (BMO?)**

Early heat distribution

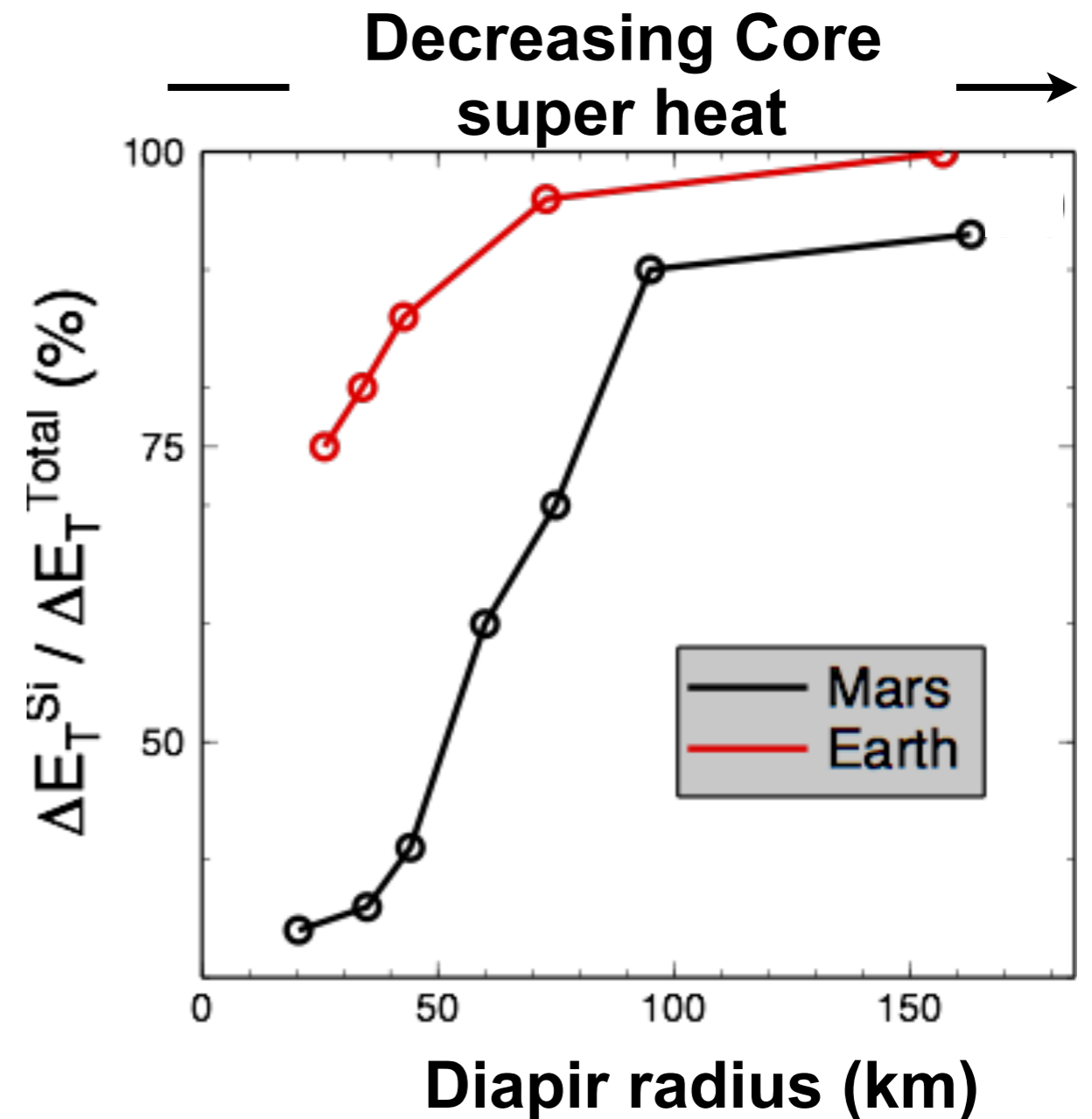


Favours a hotter lowermost mantle with melting (BMO?)

Early heat distribution



Favours a hotter lowermost mantle with melting (BMO?)



Can explain the presence and sustainability of geodynamo on Earth or Mars

Conclusions

Core formation has an huge influence on Earth evolution

1. Negative diapirism in a fully liquid or partially molten silicate magma ocean

- ✓ Stability favoured for small Re and We and Newtonian rheology
- ✓ Low viscosity diapirs favour breakup at low Re but prevents breakup at high Re
- ⇒ Characterised via scaling laws

2. Equilibration silicate magma ocean on a proto-earth

- ⇒ Fully Terrestrial magma ocean: most likely achieved
- ⇒ Partially Terrestrial magma ocean: unlikely / uncertain

3. Viscous heating and heat partitioning

- ✓ Maximum viscous dissipation (thus temperature increase) @ interface
- ✓ Negative diapirism favors higher lower mantle temperatures
- ✓ Small diapirs lead to hotter core (“stronger” dynamos)
- ✓ Silicate rheology has a strong influence on heat partitioning: non-Newtonian (partially molten) viscosity favours hotter silicates and colder metal diapirs

What next?

Need better constraints on the rheology of silicates

Partially molten case $\Rightarrow \sigma_T = f(\text{melt fraction, pressure, composition})$

Fully molten case $\Rightarrow \eta = f(\text{melt fraction, pressure, temperature, composition})$

Future/ongoing investigations

\Rightarrow Effect of turbulence on heat partitioning

... and many other things...

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... and thank you