Hard Processes and Partons

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Hadronic jets in e^+e^- collisions ^{and} QCD radiophysics

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• Quarks, Confinement and Hadrons

- Kogut-Susskind picture of hadronization
- Feynman plateau
- $e^+e^- \rightarrow$ two quark jets
- Gluon jets
 - Three-jet events
 - Ellis, Gaillard, Ross
 - Gluon hadronization: Lund string model
- Hadron production in-between jets
 - String effect
 - intERjet gluon radiation

• Internal structure of parton jets

- Coherence in soft gluon emission. Chudakov effect.
- intRAjet parton cascades
- Hump-backed plateau

• LPHD puzzle

 $quark \rightarrow hadrons$

Existence of Jets was envisaged from "parton models" in the late 1960's.



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Lund hadronization model

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Phenomenological realization of the Kogut-Susskind scenario



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 \Longrightarrow a "String" of hadrons

The base of the Lund Model

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The key features of the Lund hadronization model:

- Uniformity in *rapidity*: $dN_h = \text{const} \times \frac{d\omega_h}{\omega_h}$
- Limited k_{\perp} of hadrons
- Quark combinatorics at work:

Phenomenological realization of the Kogut-Susskind scenario



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The crucial step: Stress on the rôle of colour in multiple hadroproduction

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2 well-collimated jets of particles.



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HOWEVER :

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Moreover,

In 10% of e^+e^- annihilation events — striking fluctuations !

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Third jet

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By eye, can make out 3-jet structure.

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No surprise : (Kogut & Susskind, 1974)

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The first QCD analysis was done by J.Ellis, M.Gaillard & G.Ross (1976)

- Planar events with large k_{\perp} ;
- How to measure gluon spin ;
- Gluon jet softer, more populated.

How does gluon hadronize?

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QCD possesses $N_c^2 - 1$ gauge fields — vector gluons g.

At large distances, they are supposed to "glue" quarks together.

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B.Andersson, G.Gustafson & C.Peterson, Lund Univ., Sweden (1977) Gluon \simeq guark-antiguark pair:

 $3 \otimes \overline{3} = N_c^2 = 9 \simeq 8 = N_c^2 - 1.$ Relative mismatch : $\mathcal{O}(1/N_c^2) \ll 1$ (the large- N_c limit)

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> Gluon – a "kink" on the "string" (colour tube) that connects the quark with the antiquark

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Look at hadrons produced in a $q\bar{q}$ +photon e^+e^- annihilation event.



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Look at hadrons produced in a $q\bar{q}$ +photon e^+e^- annihilation event. -The hot-dog of hadrons that was "*cylindric*" in

the cms, is now *lopsided* [boosted string]



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Look at hadrons produced in a $q\bar{q}$ +photon e^+e^- annihilation event.

Now substitute a gluon for the photon in the same kinematics.



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Look at hadrons produced in a $q\bar{q}$ +photon e^+e^- annihilation event.

 The gluon carries "double" colour charge; quark pair is *repainted* into octet colour state.

Lund: hadrons = the sum of two independent (properly boosted) colorless substrings, made of $q + \frac{1}{2}g$ and $\bar{q} + \frac{1}{2}g$.

The first immediate consequence :

Double Multiplicity of hadrons in fragmentation of the gluon



Look at experimental findings



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Lessons :

N increases *faster* than ln E
 (⇒ Feynman was wrong)

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• $\frac{dN_g}{dN_q} = \frac{N_c}{C_F} = \frac{2N_c^2}{N_c^2 - 1} = \frac{9}{4} \simeq 2$ (\implies bremsstrahlung gluons add to the hadron yield; QCD respecting parton cascades)

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Now let's look at a more subtle consequence of Lund wisdom

seminar 15.03 (30/37) Radiophysics of Colour Hadrons between Jets

intERjet QCD radiation

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Lund: final hadrons are given by the sum of two independent substrings made of $q + \frac{1}{2}g$ and $\bar{q} + \frac{1}{2}g$.
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Let's look into the *inter-quark valley* and compare the hadron yield with that in the $q\bar{q}\gamma$ event.

The overlay results in a magnificent "String effect" — depletion of particle production in the $q\bar{q}$ valley !



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-Destructive interference from the QCD point of view



QCD prediction :

$$rac{dN_{qar{q}}^{(qar{q}\gamma)}}{dN_{qar{q}}^{(qar{q}gg)}}\simeqrac{2(N_c^2-1)}{N_c^2-2}=rac{16}{7}$$

(experiment: 2.3 ± 0.2)

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Destructive interference from the QCD point of view

Ratios of hadron flows between jets in various multi-jet processes — example of non-trivial CIS (collinear-and-infrared-safe) QCD observable [recall_G.V.'s lecture]

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Why "rediscovery"?

Because, under the spell of the probabilistic parton cascade picture (that we discussed last week), theorists managed to make serious mistakes in the late 70's when they indiscriminately applied it to parton multiplication in jets.

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Recall an amazing historical example: Cosmic ray physics (mid 50's); conversion of high energy photons into e^+e^- pairs in the emulsion

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Charged particle leaves a track of ionized atoms in photo-emulsion. electron track

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Angular Ordering is *more restrictive* than the fluctuation time ordering: $\vartheta \leq \vartheta_e$ versus $\vartheta \leq \vartheta_e \cdot \sqrt{\frac{p_0}{k_0}}$ that follows from

$$t_{\gamma} = \frac{p_0}{p_{\perp}^2} \simeq \frac{1}{p_0 \vartheta_e^2} < \frac{1}{k_0 \vartheta^2} \simeq \frac{k_0}{k_{\perp}^2} = t_e$$

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Coherence in large-angle gluon emission not only affected (suppressed) total parton multiplicity but had dramatic consequences for the structure of the energy distribution of secondary partons in jets.

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It was predicted that, due to coherence, "Feynman plateau" $dN/d \ln x$ must develop a *hump* at

$$(\ln k)_{\max} = \left(\frac{1}{2} - c \cdot \sqrt{\alpha_s(Q)} + \ldots\right) \cdot \ln Q, \qquad k_{\max} \simeq Q^{0.35}$$

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Angular Ordering is more restrictive than the fluctuation time ordering: $\vartheta \leq \vartheta_e$ versus $\vartheta \leq \vartheta_e \cdot \sqrt{\frac{p_0}{k_0}}$. Significant difference when $k_0/p_0 = x \ll 1$ (soft radiation).

Coherence in large-angle gluon emission not only affected (suppressed) total parton multiplicity but had dramatic consequences for the structure of the energy distribution of secondary partons in jets.

It was predicted that, due to coherence, "Feynman plateau" $dN/d \ln x$ must develop a hump at

$$\left(\ln k\right)_{\max} = \left(\frac{1}{2} - c \cdot \sqrt{\alpha_s(Q)} + \ldots\right) \cdot \ln Q, \qquad k_{\max} \simeq Q^{0.35},$$

while the softest particles (that seem to be the easiest to produce) should not multiply at all !

Hump-backed plateau

seminar 15.03 (34/37) Radiophysics of Colour Parton Cascades

CDF PRELIMINARY



First confronted with theory in $e^+e^- \rightarrow h+X$. CDF (Tevatron) $pp \rightarrow 2$ jets Charged hadron yield as a function of $\ln(1/x)$ for different values of jet hardness, versus (MLLA) QCD prediction.

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One free parameter – overall normalization (the number of final π 's per extra gluon)

Hump (continued)



Position of the Hump as a function of $Q = M_{ii} \sin \Theta_c$ (hardness of the jet)

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Position of the Hump as a function of $Q = M_{ii} \sin \Theta_c$ (hardness of the jet) is the parameter-free QCD prediction.

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Yet another calculable "IR-CO-safe" (or CIS) quantity.

Mark Universality: same behaviour seen in e^+e^- , DIS (e_p) , hadron-hadron coll.

(日)

So, the *ratios* of particle flows between jets (intERjet radiophysics), as well as the *shape* of the inclusive energy spectra of secondary particles (intRAjet cascades) turn out to be formally calculable (CIS) quantities. Moreover, these perturbative QCD predictions actually work.

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Thanks to AF and to IR-CO-safety we can compute σ_T in terms of the simplest lowest order diagram with just $q\bar{q}$ in the final state. However this is by no means the correct description of the final state ... (G.V.)

Calculation of σ_T from 1st principles – the robust example of *IR-CO-safety*.

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Calculation of σ_T from 1st principles – the robust example of *IR-CO-safety*. However, we can derive a thing or two about the structure of the *final state* — ensemble of jets stemming from primary *q*'s and *g*'s — as well.

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To describe particle multiplicities, spectra one exploits collinear and soft enhancements and must treat quark–gluon cascades in all orders in α_s (probabilistically, but not forgetting quantum mechanics — Angular Ordering).

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But this is another story ...

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