

How to prove the security of communication protocols?

Véronique Cortier, LORIA - CNRS, Nancy

Seminar at Collège de France, 18 mai 2011

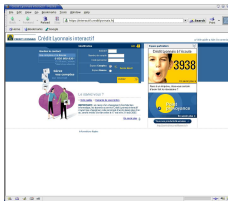
Joint work with Hubert Comon-Lundh, Stéphanie Delaune, Steve Kremer, Ben Smyth and Bogdan Warinschi.



Context : cryptographic protocols

Cryptographic protocols are widely used in everyday life.

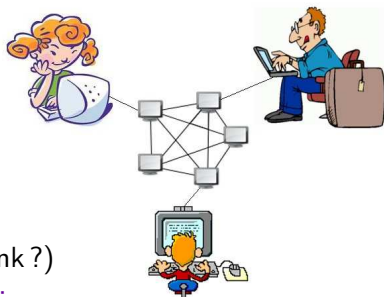
→ They aim at securing communications over public or insecure networks.



Security goals

Cryptographic protocols aim at

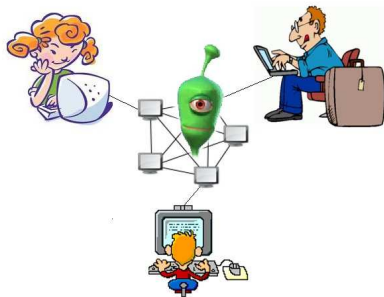
- **preserving confidentiality** of data
(e.g. pin code, medical files, ...)
- **ensuring authenticity**
(are you really talking to your bank?)
- **ensuring anonymous communications**
(for e-voting protocols, ...)
- **protecting against repudiation**
(I never sent this message!)



Difficulty : there are potential powerful attackers !

Presence of an **attacker**

- may **participate** to the protocol.
- may **forge and send** messages,
- may **read** every message sent on the net,
- may **intercept** messages,



Attacking Single Sign On Protocol

Single Sign On Protocols

- enables to log in once for several services
- used e.g. in Google App



→ A flaw discovered in 2010, now fixed (Avantssar project)

Step 1 An attacker offers an interesting or funny (but malicious) new Google App

Step 2 Some clients register to this malicious Application

Step 3 The attacker can now access all the other applications of the client, including e.g. **Gmail** or **Google Calendar**.

Designing protocols is error prone

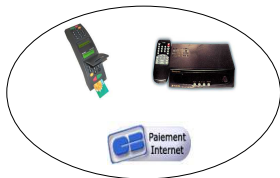
Software testing leaves **flaws** : *cf Lectures of Martín Abadi*

- Flaw in the authentication protocol used in Google Apps
- Attack on pay-per-view devices
- Man-in-the-middle attack

These flaws rely on the **design** of the protocols

- **Not on a bad implementation** (bugs)
- **Not on weaknesses of the primitives** (e.g. encryption, signatures)
- **Not on generic hacking techniques** (e.g. worms, code injection)

How to analyse security protocols?



confidentiality
authenticity
anonymity
non-repudiation
...

Methodology

- 1 Proposing accurate models
 - symbolic models
 - cryptographic/computational models
- 2 Proving security
 - decision procedures
 - transfer results

Running example : electronic voting

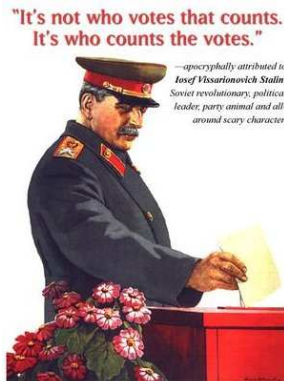
Example : Electronic voting

Elections are a **security-sensitive** process which is the cornerstone of modern democracy.

Electronic voting promises

- **Convenient, efficient** and **secure** facility for recording and tallying votes
- for a variety of **types of elections** : from small committees or on-line communities through to full-scale national elections

Already used e.g. in Estonia, Norway, USA.



Two main families for e-voting

Voting machines

- Voters have to attend a voting station
- External authentication system (e.g. ID card)



Internet voting

- Voters vote from home
- from their own computers
- Systems in use : Civitas (A. Myers *et al*),
Helios, ...



cf Seminar of Ron Rivest (March 23rd).

Running example : Helios

<http://heliosvoting.org/>

helios

Helios Demo — Voters and Ballot Tracking Center ([back to election](#))

Registration is **Open**.

search:

2 cast votes

Voters 1 - 3 (of 3)

Name	Smart Ballot Tracker
Ben Smyth	-
Michael Rusinowitch	Vo5v5Jeb0VBT1qfBwXa1xc8n5V68fWgu20guRfU6cQ4 Link
Veronique Cortier	v90pdFz23085ypcF/Byj+c8e4qIv9/UZ7eH+7/a7H5E Link

not logged in. ([log in](#))
[About Helios](#) | [Help!](#)

Done
 Voters & Ballot Trackin...

Developed by B. Adida
et al, already in use :

- Election at
 Louvain University
 Princeton
- Election of the
 IACR board
 (major association
 in Cryptography)

Behavior of Helios (simplified)

Phase 1 : voting



Bulletin Board

Alice	$\{v_A\}_{pk(S)}$	$v_A = 0 \text{ or } 1$
Bob	$\{v_B\}_{pk(S)}$	$v_B = 0 \text{ or } 1$
Chris	$\{v_C\}_{pk(S)}$	$v_C = 0 \text{ or } 1$

$pk(S)$: public key, the private key being shared among trustees.

Behavior of Helios (simplified)

Phase 1 : voting



$\{v_D\}_{pk(S)}$



Bulletin Board

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...	...	

Phase 2 : Tallying using homomorphic encryption (El Gamal)

$$\prod_{i=1}^n \{v_i\}_{pk(S)} = \left\{ \sum_{i=1}^n v_i \right\}_{pk(S)} \quad \text{based on } g^a * g^b = g^{a+b}$$

→ Only the final result needs to be decrypted !

$pk(S)$: public key, the private key being shared among trustees.

This is oversimplified !


 $\{v_D\}_{pk(S)}$


Bulletin Board

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David	$\{v_D\}_{pk(S)}$	
...	...	

Result : $\{v_A + v_B + v_C + v_D + \dots\}_{pk(S)}$

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...	...	

Result : $\{v_A + v_B + v_C + 100 + \dots\}_{pk(S)}$

A malicious voter can cheat !

This is oversimplified !


 $\{v_D\}_{pk(S)}$

Bulletin Board

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~~A malicious voter can cheat!~~

In Helios : use of (Signature of) Proof of Knowledge

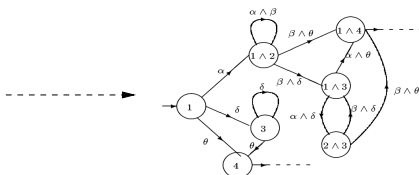
$\{v_D\}_{pk(S)}, SPK\{v_D = 0 \text{ or } 1\}$

How to analyse security protocols ?

For example, how to prove that Helios is secure ?

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Task 1 : Modeling

- 1 Modeling messages
- 2 Modeling the behavior of the protocol
- 3 Modeling “security”

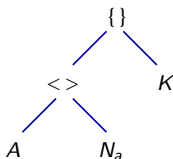
Modeling messages

Idea 1 : keeping only the structure of the messages

→ Messages are abstracted by terms.

Example :

The message $\{\langle A, N_a \rangle\}_K$ is represented by :



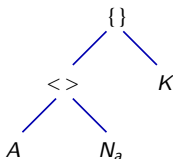
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Idea 2 : Equations for reflecting the properties of the primitives

Decryption

$$\text{dec}(\{x\}_y, y) = x$$

Homomorphic encryption

$$\{x_1\}_y * \{x_2\}_y = \{x_1 + x_2\}_y$$

Modeling protocols

Processes of the applied pi-calculus, introduced by Martín Abadi

- Voter id voting v

$$\text{Voter}(id, v) = \overline{c}_{id}(\{v\}_{pk(S)}, \text{spk}(v, \{v\}_{pk(S)}))$$

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- Bulletin board for n voters

$$\begin{aligned} \text{BulletinBoard} &= c_{id_1}(x_1). \text{ if } \text{Valid}(x_1) \text{ then } \overline{out}(x_1). \\ &\dots \\ &c_{id_n}(x_n). \text{ if } \text{Valid}(x_n) \text{ then } \overline{out}(x_n). \\ &\overline{c}_{tally}(\pi_1(x_1) * \dots * \pi_1(x_n)) \end{aligned}$$

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- Tallying phase

$$\text{Tally} = c_{tally}(y). \overline{out}(\text{dec}(y, \text{sk}(S)))$$

Modeling attackers

We assume that the network can be controlled by attackers

- may **participate** to the protocol.
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Attackers in applied pi-calculus

A protocol P satisfies some property ϕ if **for all process A**

$$A \mid P \models \phi$$

What is a secure voting protocol ?



Let's have a closer look to privacy

How to state formally :

"No one should know my vote (0 or 1)" ?



Idea 1 : An attacker should not learn the value of my vote.

Let's have a closer look to privacy

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Idea 1 : An attacker should not learn the value of my vote.
But everyone knows 0 and 1!

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Idea 2 : An attacker should not attach my vote to my identity.

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~~Idea 1 : An attacker should not learn the value of my vote.~~

Idea 2 : An attacker should not attach my vote to my identity.
But everyone can form $\langle Alice, 0 \rangle$ and $\langle Alice, 1 \rangle$!

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~~Idea 1~~ : An attacker should not learn the value of my vote.

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~~Idea 3~~ : An attacker cannot see the difference when I vote 0 or 1.

$\text{Voter}_1(0) \mid \text{Voter}_2(v_2) \mid \dots \mid \text{Voter}_n(v_n) \sim \text{Voter}_1(1) \mid \text{Voter}_2(v_2) \mid \dots \mid \text{Voter}_n(v_n)$

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- The attacker **always sees the difference** since the tally differs.
- **Unanimity does break privacy.**

Let's have a closer look to privacy

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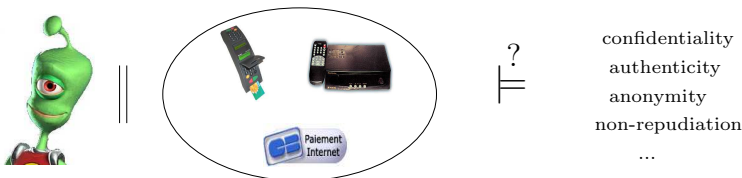
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Idea 4 : An attacker cannot see when votes are swapped.

$\text{Voter}_1(0) \mid \text{Voter}_2(1) \sim \text{Voter}_1(1) \mid \text{Voter}_2(0)$

How to analyse security protocols?



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How to analyse security protocols ?

How to prove e.g.

$$\forall A, \quad A | \text{Voter}_1(0) | \text{Voter}_2(1) \sim A | \text{Voter}_1(1) | \text{Voter}_2(0)?$$

Task 2 : Automatic verification

How to analyse security protocols ?

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Task 2 : Automatic verification

- Unfortunately, security (e.g. confidentiality) is **undecidable**.
→ No generic algorithm can work.
- Identification of **decidable fragments**
 - Analysis of a finite number of sessions
 - restriction on the class of protocols
- Semi-decision procedure : **ProVerif**

How does ProVerif work ?

Developed by Bruno Blanchet, ENS Paris, France.

- Implements a **sound semi-decision procedure** (that may not terminate).
- The applied pi-calculus is translated into **first-order logic**, more precisely into **Horn clauses**.
- Based on a resolution strategy **well adapted to protocols**.

Horn clauses for the intruder

Horn clauses perfectly reflect the attacker **symbolic manipulations** on terms.



$\forall x \forall y$	$I(x), I(y) \Rightarrow I(\langle x, y \rangle)$	pairing
$\forall x \forall y$	$I(x), I(y) \Rightarrow I(\{x\}_y)$	encryption
$\forall x \forall y$	$I(\{x\}_y), I(y) \Rightarrow I(x)$	decryption
$\forall x \forall y$	$I(\langle x, y \rangle) \Rightarrow I(x)$	projection
$\forall x \forall y$	$I(\langle x, y \rangle) \Rightarrow I(y)$	projection

Horn clauses for the protocol

Protocol WMF :

$$A \rightarrow S : \{n_a, b, k\}_{k_a}$$

$$S \rightarrow B : \{n_s, a, k\}_{k_b}$$

$$B \rightarrow A : \{m_{ab}\}_k$$

Horn clauses :

$$\Rightarrow I(\{n_a, b, k\}_{k_a})$$

$$I(\{x, b, y\}_{k_a}) \Rightarrow I(\{n_s(x, y), a, y\}_{k_b})$$

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Secrecy property is a **reachability** (accessibility) property

$$\neg I(m_{ab})$$

Checking security reduces to checking satisfiability

There exists an attack iff the set of formulas corresponding to

Intruder manipulations + protocol + property

is **NOT** satisfiable.

How to decide satisfiability ?

→ Resolution techniques : Binary resolution

$$\frac{D_1 \wedge \dots \wedge D_k \Rightarrow B \quad A_1 \wedge \dots \wedge A_n \Rightarrow C}{(D_1 \wedge \dots \wedge D_k \wedge A_2 \wedge \dots \wedge A_n \Rightarrow C)\theta} A_1\theta = B\theta$$

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→ It does not terminate.

Example :

$$I(s) \quad I(x), I(y) \Rightarrow I(\langle x, y \rangle)$$

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$$I(\langle s, s \rangle)$$

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$$I(\langle s, \langle s, \langle s, \langle s, \langle s, s \rangle \rangle \rangle \rangle \rangle) \quad \dots$$

Efficient and sound resolution strategy

Idea : Resolution is only applied on **selected literals** A_1, B that do not belong to a **forbidden set** S . Typically $S = \{I(x)\}$.

Theorem

Resolution based on selection, avoiding S , is complete w.r.t. satisfiability.

- If the fixed point does not contain the empty clause, then the corresponding protocol is secure.
- ProVerif may not terminate.

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Performs very well in practice !

- Works on **most of existing protocols** in the literature
- Is also used on **industrial protocols** (e.g. certified email protocol, JFK, Plutus filesystem)
- Can handle various cryptographic primitives (various encryption, signatures, blind signatures, hash, *etc.*)

Security of Helios

→ ProVerif cannot be applied (yet).

Privacy

$\forall A, \quad A \mid \text{Voter}_1(0) \mid \text{Voter}_2(1) \sim A \mid \text{Voter}_1(1) \mid \text{Voter}_2(0)$

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Verifiability

- **Individual verifiability** : voter can check that her own ballot is included in the election's bulletin board.
- **Universal verifiability** : anyone can check that the election outcome corresponds to the ballots published on the bulletin board.

Helios provably satisfy both verifiability properties.

Limitations of this approach ?

Are you ready to use any protocol verified with this technique ?

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Are you ready to use any protocol verified with this technique ?

→ Side channel attacks *cf* Seminar of Adi Shamir (May, 4th 2011)

→ Representing messages by a term algebra abstracts away many mathematical properties.

Setting for cryptographic/computational models

Messages : 01111001010110 ([Bitstrings](#))

Protocol :

- Message exchange program
- Use cryptographic algorithms

cf Seminar of David Pointcheval (April, 27th 2011).

Setting for cryptographic/computational models

Messages : 01111001010110 (Bitstrings)

Protocol :

- Message exchange program
- Use cryptographic algorithms

Adversary \mathcal{A} : any probabilistic polynomial Turing machine, *i.e.* any probabilistic polynomial program.

- polynomial : captures what is feasible
- probabilistic : the adversary may try to guess some information



cf Seminar of David Pointcheval (April, 27th 2011).

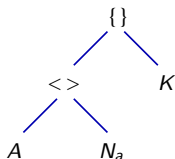
Formal and Cryptographic approaches

	Formal approach	Cryptographic approach
Messages	terms	bitstrings
Encryption	idealized	algorithm
Adversary	idealized	any polynomial algorithm
Guarantees	unclear	strong
Protocol	may be complex	usually simpler
Proof	automatic	by hand, tedious and error-prone

Link between the two approaches ?

Proving cryptographic security through symbolic models

Symbolic models

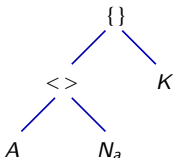


Computational models

```
0111010111010010
0101010001011101
1110010000110101
```

Proving cryptographic security through symbolic models

Symbolic models



Computational models

```

0111010111010010
0101010001011101
1110010000110101
  
```

Idea : soundness result

Show that security in symbolic models implies security in computational ones.

[Abadi Rogaway 00]

Soundness of equivalences in the applied pi-calculus

Result : Assuming a strong encryption scheme (IND-CCA2 hypothesis)

$$P_1 \sim P_2 \quad \Rightarrow \quad \llbracket P_1 \rrbracket \approx \llbracket P_2 \rrbracket$$

Symbolic equivalence of
processes P_1 and P_2

Indistinguishability of
the implementation of P_1 and P_2

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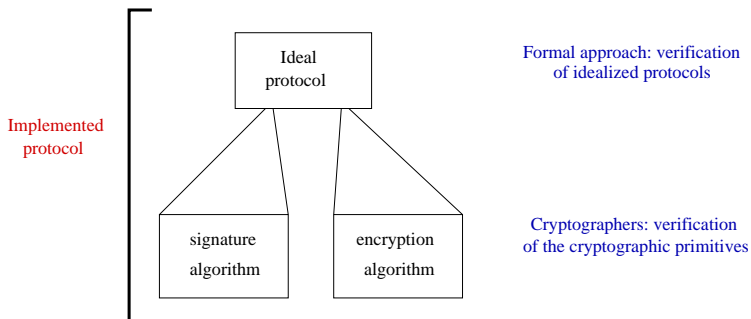
Key technique

Any attack trace from the concrete adversary is an attack against the symbolic protocol, or the adversary breaks encryption.

Consequence : Security in symbolic models directly implies security in cryptographic models, against arbitrary attackers.

Benefit : modularity

Cryptographic security guarantees can be obtained
at the symbolic level



Conclusion

Formal methods form a powerful approach
for analyzing security protocols

- **Use of existing techniques** : term algebra, equational theories, clauses and resolution techniques, tree automata, etc.
⇒ Many decision procedures
- **Several successful automatic tools**
e.g. ProVerif, Avispa/Avantssar, Scyther, NRL Protocol Analyzer
 - Detect attacks (e.g. flaw in Gmail)
 - Prove security of standard protocols (e.g. IKE, JFK, Certified email, Helios, ...)
- **Provides cryptographic guarantees** under classical assumptions on the implementation of the primitives

The end

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