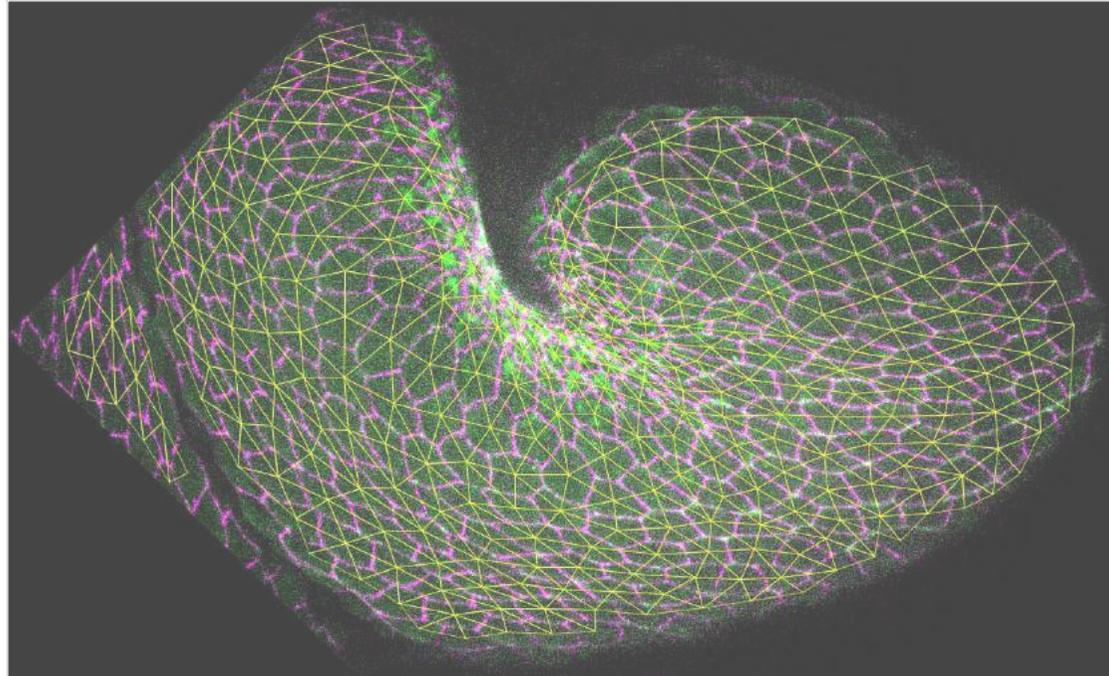


# Morphogenesis: space, time, information



Course 3: Spatial and temporal instabilities

*Thomas Lecuit*  
*chaire: Dynamiques du vivant*



COLLÈGE  
DE FRANCE  
— 1530 —

# Biological organisation in space and time

- Two modalities of information flow during morphogenesis

## Program



- hierarchical, indirect interactions
- modular
- long and short range interactions
- high-wired
- multiple parameters

## Self-organization

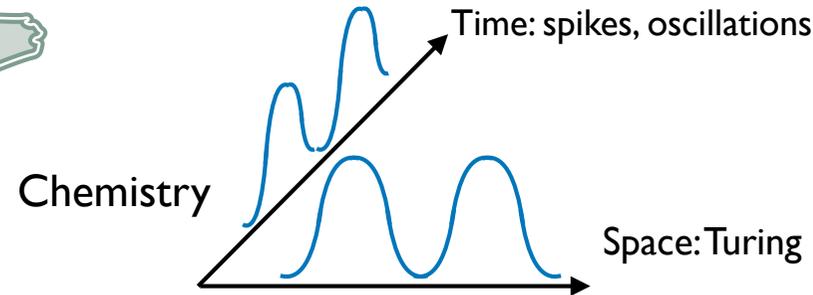
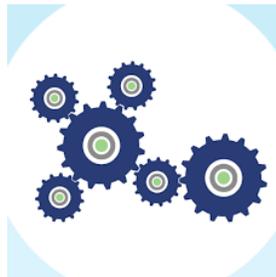
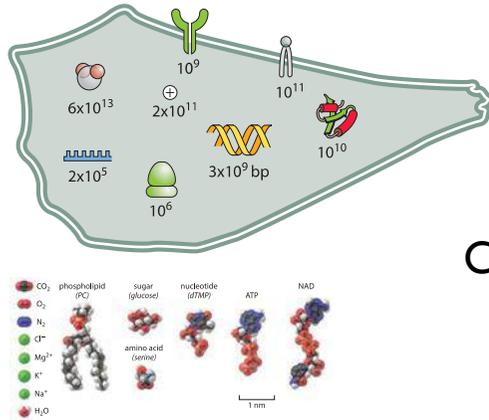


- local and direct interactions
- few rules and parameters

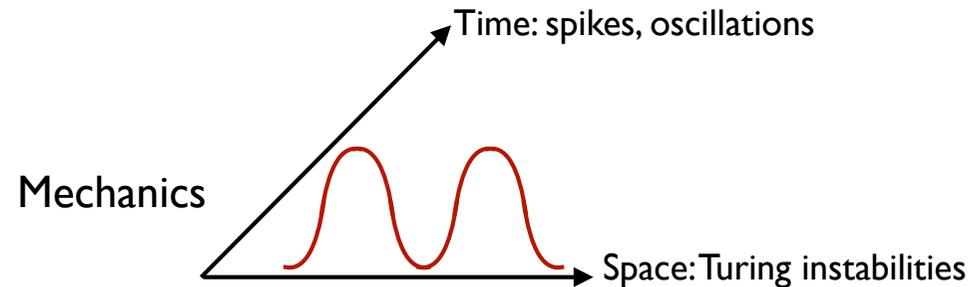


# Spatial and Temporal Instabilities

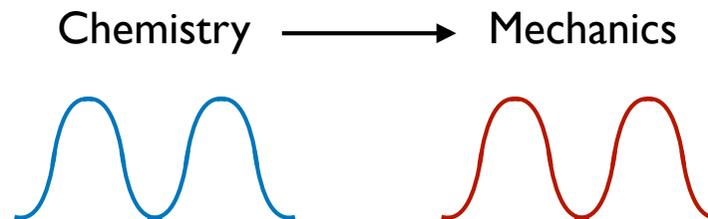
## Chemical and Mechanical Information



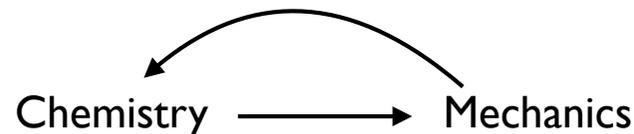
self-organization in nonequilibrium **chemical systems**



self-organization in nonequilibrium **mechanical systems**



self-organization in nonequilibrium **mechano-chemical systems**

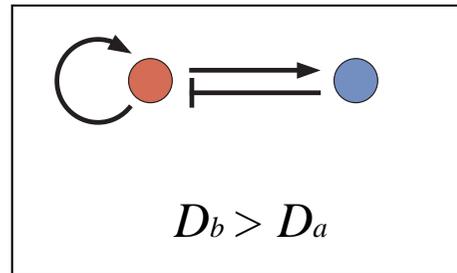


- 
1. Introduction - Program and Self-Organisation
  2. Chemical Instabilities
    21. Spatial instabilities - Turing patterns
    22. Temporal instabilities - Excitability
    23. Spatial-temporal instabilities: waves
  3. Mechanical instabilities
    31. Cellular aggregates: viscoelastic model
    32. Active gel: hydrodynamic and viscoelastic models
  4. Mechano-chemical Instabilities
    41. Mechano-chemical coupling: actomyosin dynamics
    42. Actin based trigger waves
  5. Developmental significance: impact on cellular and tissue morphogenesis



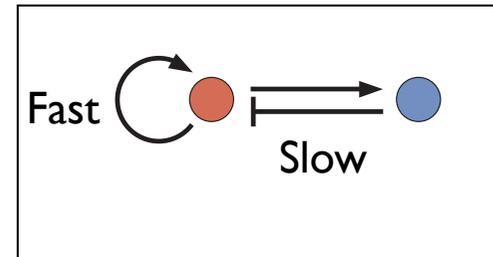
## Spatial Instabilities

- Local positive feedback
- Long range inhibition



## Temporal Instabilities

- Local positive feedback
- Negative feedback with a delay



Chemical

Mechanical

Contractility driven positive feedback  
Elasticity: « long-range inhibitor »

Turing-like patterns

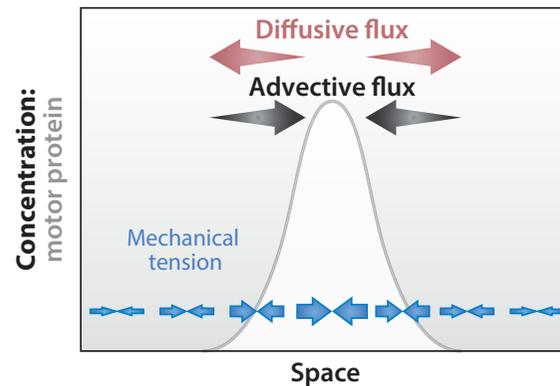
# III - Mechanical Instabilities

- Pattern formation in an **active fluid** (e.g. actomyosin gel)

$$\partial_t c = -\partial_x j, \quad j = \underbrace{-D\partial_x c}_{\text{diffusion}} + \underbrace{vc}_{\text{advection}}, \quad (1)$$

Diffusion: smoothens fluctuations

Advection: amplifies fluctuations (mechanical feedback)



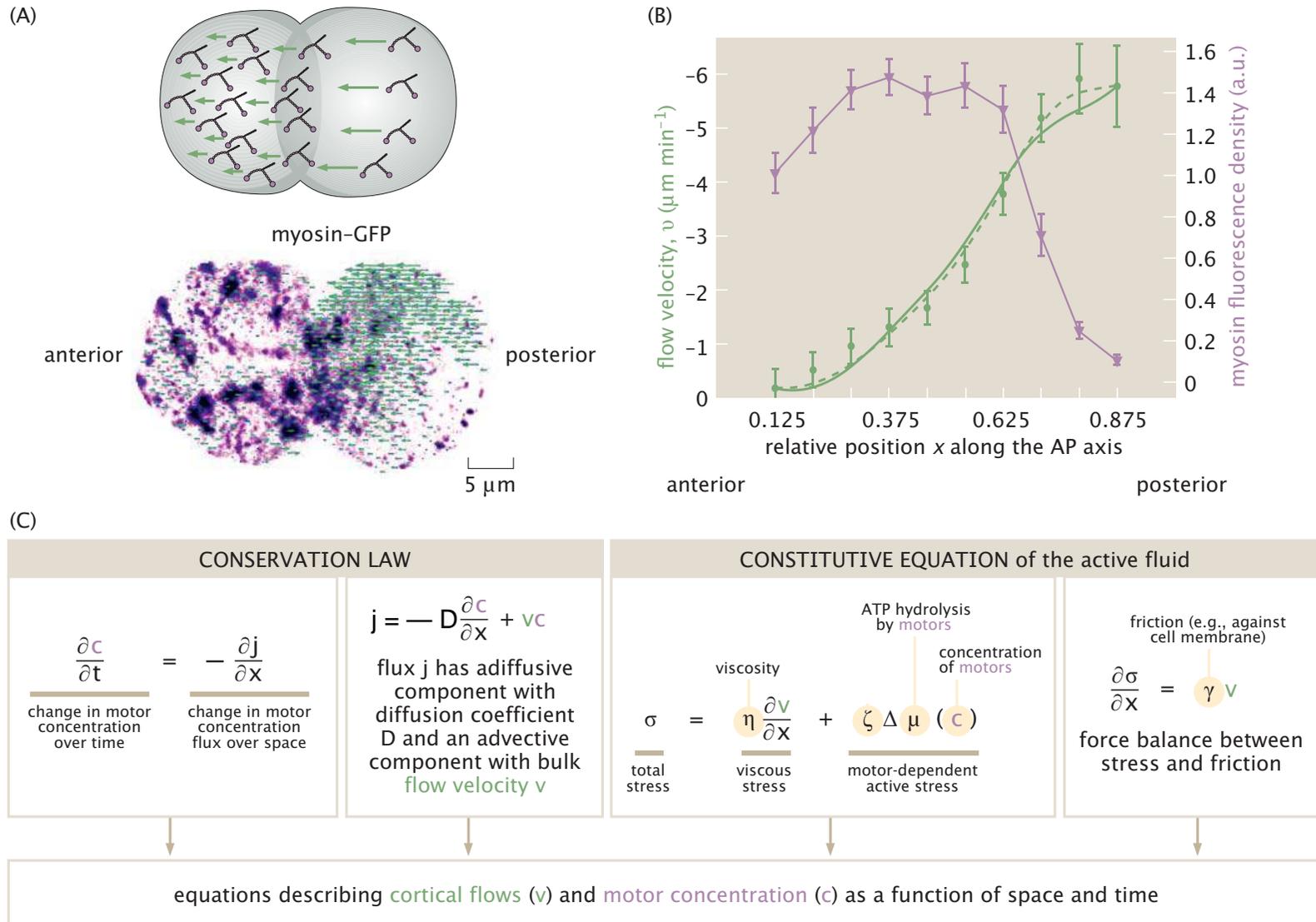
- Dimensionless parameter that considers the respective contributions of two sources of flux

Péclet number (advection rate/diffusion rate)

$$Pe = U\ell/D.$$

# III - Mechanical Instabilities

- Pattern formation in an **active fluid**: actomyosin flow



# III - Mechanical Instabilities

- Pattern formation in an **active fluid** (e.g. actomyosin gel)

Hydrodynamic flow description:

$$\partial_t c = -\partial_x j, \quad j = -D\partial_x c + v c, \quad (1) \text{ conservation law (species } c)$$

diffusion    advection

$$\sigma = \eta\partial_x v + \zeta\Delta\mu. \quad (2) \text{ constitutive equation}$$

$$\partial_x \sigma = \gamma v, \quad (3) \text{ force balance}$$

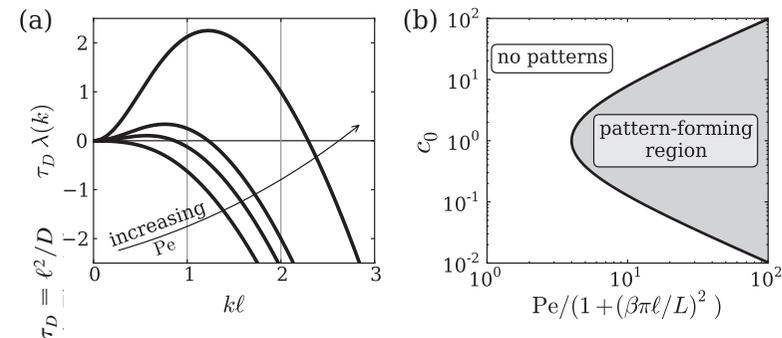
Linear stability: Eigen values  $\lambda(k) = -k^2 D \left( 1 - \frac{Pe c_0 \partial_c f(c_0)}{1 + k^2 \ell^2} \right)$ . Flow driven non-homogeneity for  $\frac{Pe c_0 \partial_c f(c_0)}{1 + (\beta \pi \ell / L)^2} > 1$ .

$\ell \equiv \sqrt{\eta/\gamma}$  hydrodynamic length scale

$Pe = U\ell/D$  Péclet number (advection rate/diffusion rate)

$\zeta\Delta\mu(c) = (\zeta\Delta\mu)_0 f(c)$  with  $\partial_c f(c_0) > 0$  (active stress increases with concentration of  $c_0$ )

- **Active stress driven flow must overcome frictional resistance and diffusive dispersion:** (requires large enough  $Pe$  and upregulation of active stress by regulator  $\partial_c f(c_0) > 1$ )

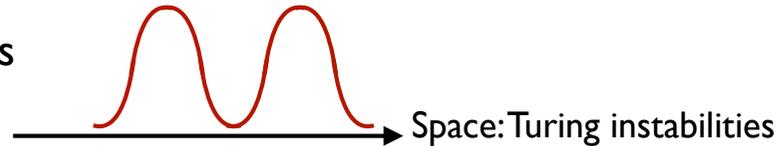


# III - Mechanical Instabilities

## Mechanical instabilities



Mechanics



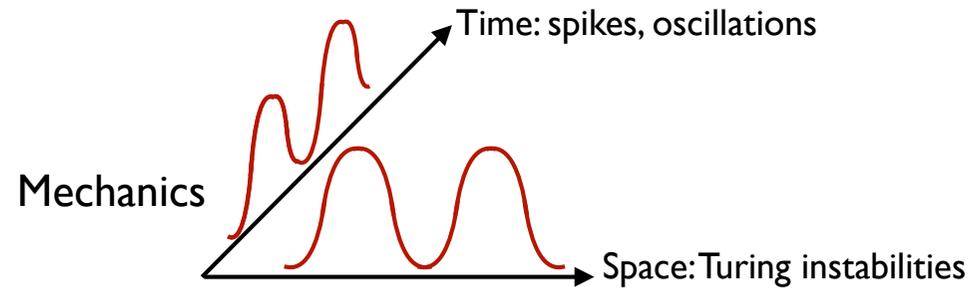
self-organization in  
nonequilibrium  
**mechanical systems**

- Turing like pattern: Activator induced active stress drives fluid flow that must overcome frictional resistance and diffusion.
- Active stress as « local activator» with autocatalysis (advective flow) Friction as « long range inhibitor ».



# III - Mechanical Instabilities

## Temporal Mechanical instabilities



self-organization in  
nonequilibrium  
**mechanical systems**



# III - Mechanical Instabilities

- Pulsatory patterns in active fluids (e.g. actomyosin gel)

Reaction-Diffusion-Advection Model:

Hydrodynamic flow description with 2 chemical species that activate or inhibit active stress

$$\partial_t A = -\nabla \cdot (\mathbf{v}A) + D\nabla^2 A, \quad (1)$$

$$\partial_t I = -\nabla \cdot (\mathbf{v}I) + \alpha D\nabla^2 I, \quad (2) \quad \alpha = D_I/D$$

$$\nabla \cdot \sigma = \gamma \mathbf{v}, \quad \sigma = \sigma_p + \zeta \Delta \mu \mathbf{1}. \quad (3)$$

passive/viscous stress      active stress

(function of A and I)

$$\zeta \Delta \mu = (\zeta \Delta \mu)_0 f(\mathbf{c}), \quad \text{with} \quad f(\mathbf{c}) = f_0 + (1 + \beta) \frac{A}{A + A_s} + (1 - \beta) \frac{I}{I + I_s},$$

$\beta$  asymmetric parameter

$\beta > 1$ : A activates and I inhibits active stress

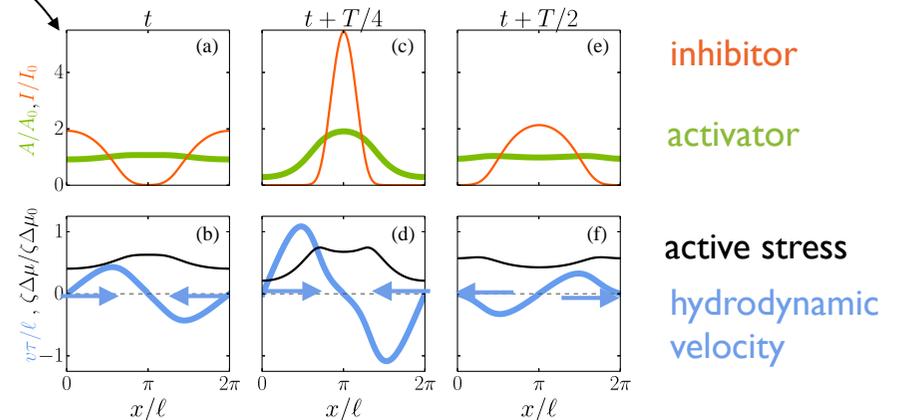
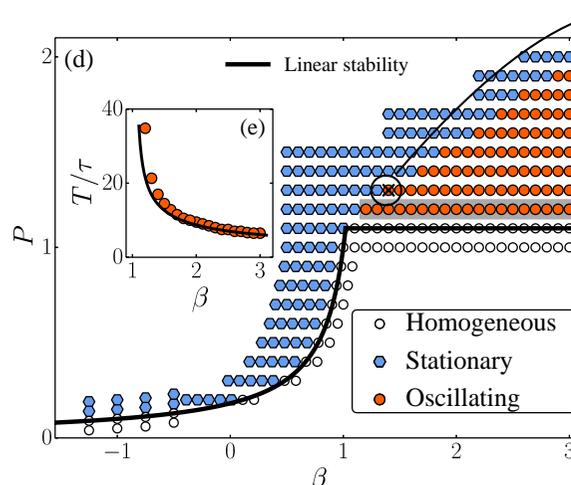
**Pulsatory dynamics emerge:**

1. if activator of active stress  $A$  diffuses faster than inhibitor  $I$

(different diffusive relaxation time scale)

$P$ : Péclet number

$$P = vL/D$$



# III - Mechanical Instabilities

- Pulsatory patterns in active fluids (e.g. actomyosin gel)

Reaction-Diffusion-Advection Model:

Hydrodynamic flow description with 2 chemical species

$$\partial_t A = -\nabla \cdot (\mathbf{v}A) + D\nabla^2 A - \kappa(A - A_0), \quad (12)$$

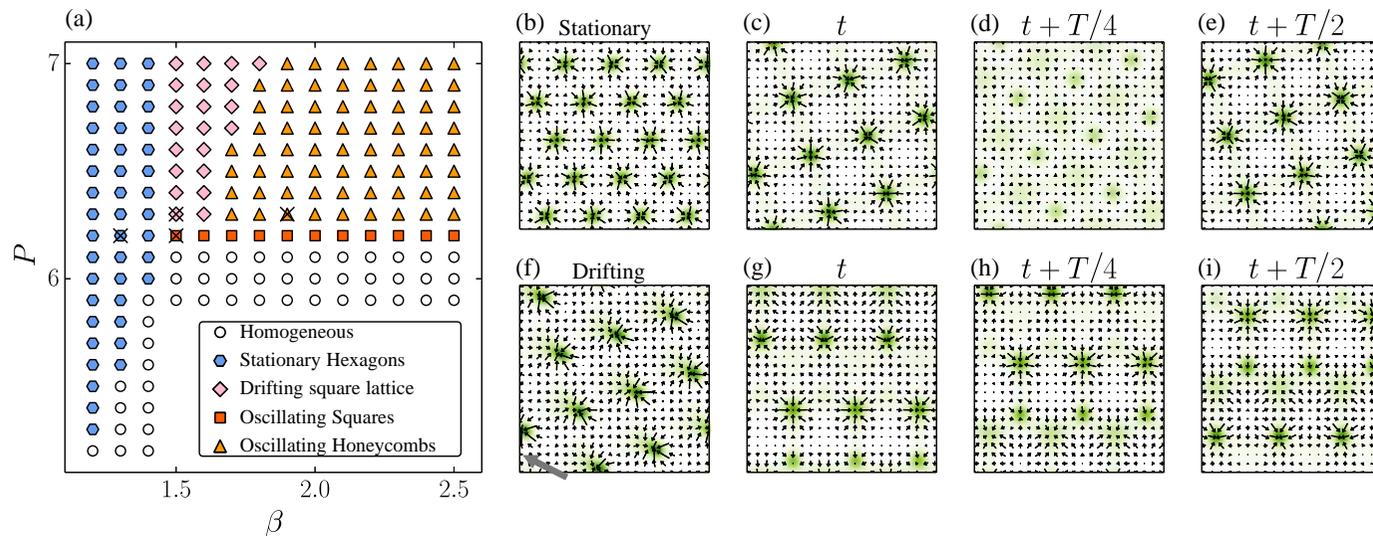
$$\partial_t I = -\nabla \cdot (\mathbf{v}I) + D\nabla^2 I - \rho\kappa(I - I_0), \quad (13)$$

$\kappa$  activator turnover rate  
 $\rho > 0$  ratio of inhibitor to activator turnover rate

**Pulsatory dynamics emerge:**

**2. if activator of active stress turns over faster than inhibitor**

(different kinetic relaxation time scales)



# III - Mechanical Instabilities

- Pulsatory patterns in active fluids (e.g. actomyosin gel)

Active stress regulated by Activator A and Inhibitor I:  $\sigma_a = \sigma_a(c_A, c_I)$

Pulsatory dynamics emerges from coupling between:

- differential effect of A and I on active stress generation
- differential relaxation modes of A and I (diffusion or turnover)

Active stress also depends on density and orientational order of actin filaments and MyosinII minifilaments: allows for more complex feedbacks and patterns of orientational order of actomyosin network



# III - Mechanical Instabilities

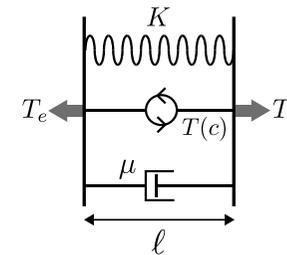
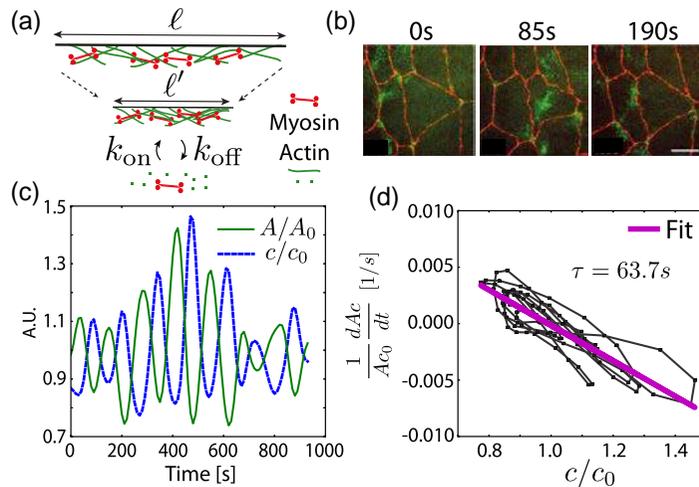
- Pulsatory patterns in **viscoelastic** contractile networks

Model: Contractile viscoelastic network with turnover :

Captures properties of actomyosin networks in cells.

$$k_{\text{on}} = c_0/\tau$$

$$k_{\text{off}}c = c/\tau$$



turnover mass conservation ( $dc/dt = 0$  if no turnover)

$$\frac{dc}{dt} = -\frac{1}{\tau}(c - c_0) - \frac{c}{l} \frac{dl}{dt}, \quad (1)$$

viscous force  $\mu \frac{dl}{dt}$  external force  $T_e$  contractile force  $T(c)$  elastic force  $K(l)$

$$\mu \frac{dl}{dt} = T_e - T(c) - K(l), \quad (2)$$

# III - Mechanical Instabilities

- Pulsatory patterns in viscoelastic contractile networks

Model: Contractile viscoelastic network with turnover : 
$$\mu \frac{dl}{dt} = T_e - T(c) - K(l), \quad (2)$$

- linear stability analysis:

steady state  $c_0, l_0$  
$$T(c) = T(c_0) + t_1(c - c_0)$$
  

$$K(l) = K(l_0) + k_1(l - l_0) + k_3(l - l_0)^3$$



Hopf bifurcation for:

$$(t_1 c_0)/(k_1 l_0) = 1 + \mu/(k_1 \tau)$$

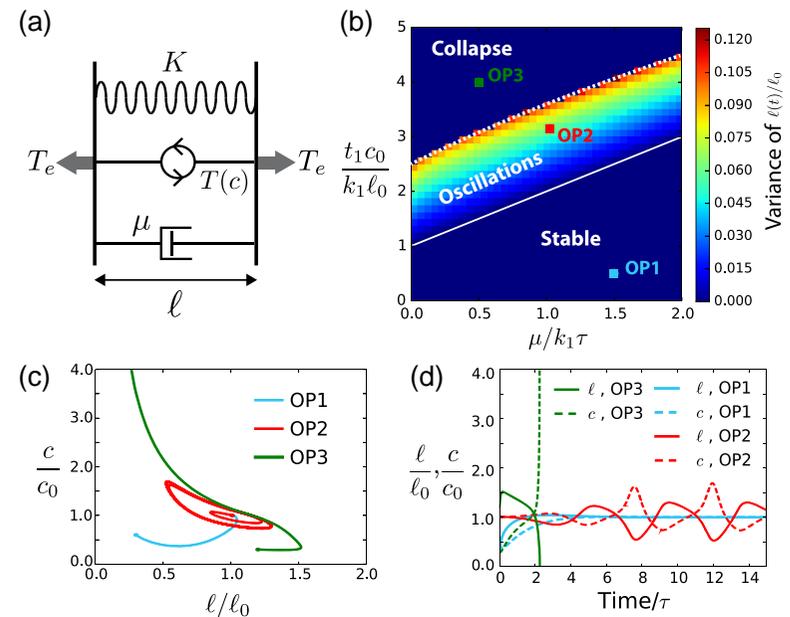
- Significance:

Contraction  $t_1$  concentrates contractile units thereby increasing contraction: **Positive Feedback**

Viscous damping opposes (and elastic tension enhances) this effect.  $\mu/k_1$ : relaxation/retardation time scale

Constant turnover tends to restore  $c$  to  $c_0$  and down regulate contraction: **Negative Feedback**

$\tau$  : turnover time scale



**Oscillatory dynamics emerges when:**

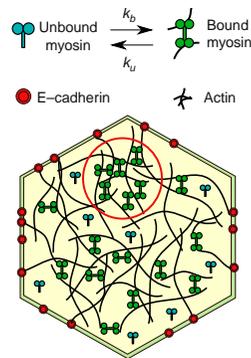
- contraction overcomes viscous resistance and motor turnover

# III - Mechanical Instabilities

- Pulses, travelling waves and contractile instabilities in viscoelastic contractile networks

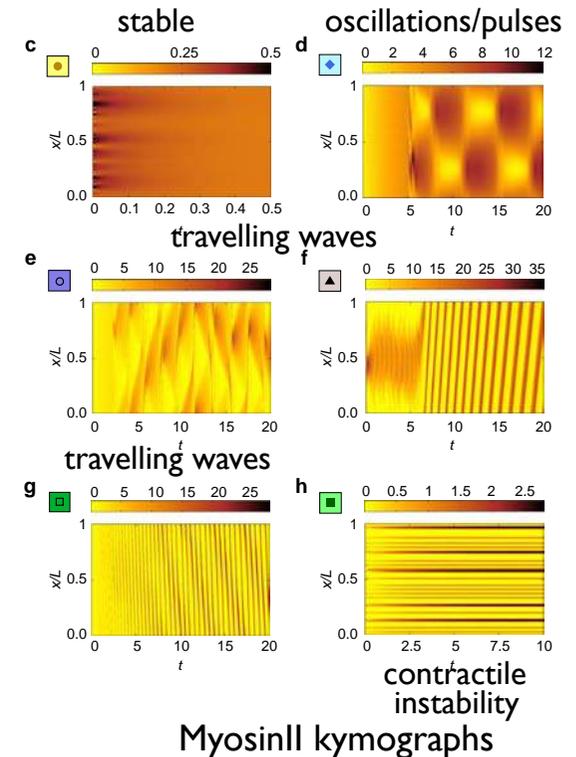
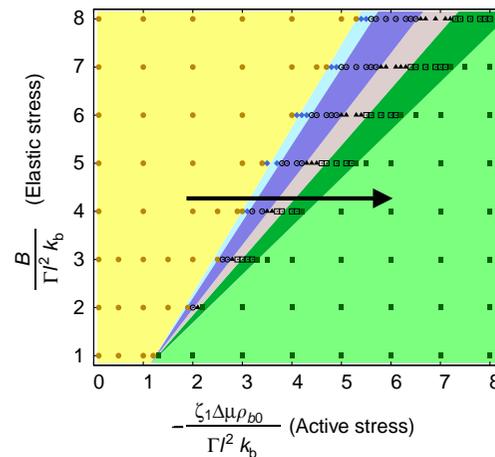
Model: Contractile viscoelastic network with turnover of actin and MyosinII:

- Study the effects of non-linearities associated with:
  - active stress (function of network density, orientational order)
  - elastic energy (function of MyoII and actin densities)
  - turnover (MyoII strain dependent unbinding)



$$\Gamma \dot{u} = \partial_x \Phi'(\epsilon) + \partial_x \sigma^a(\rho_b)$$

$$\dot{\rho}_b = -\partial_x(\rho_b \dot{u}) + D \partial_x^2 \rho_b + S_m(\epsilon, \rho_b),$$



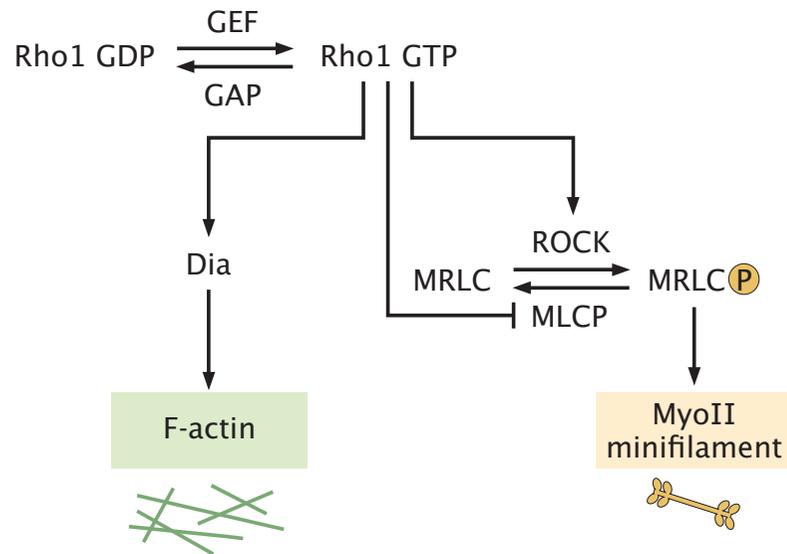
- 
1. Introduction - phenomenology
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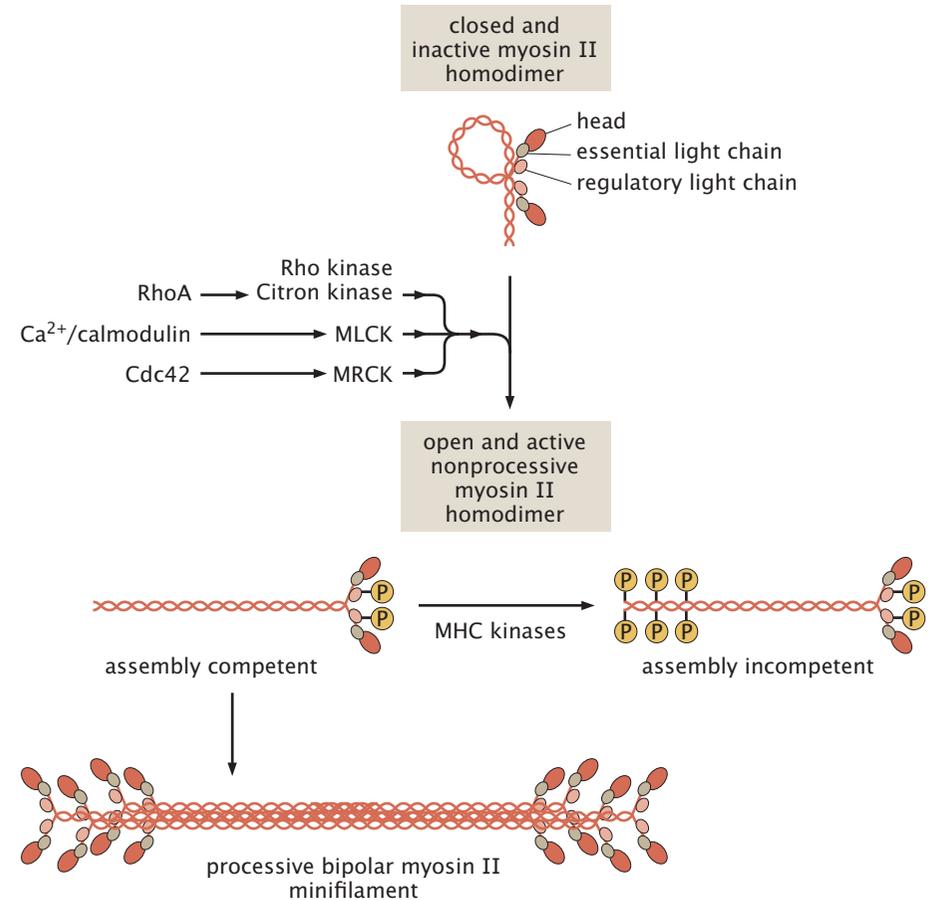
# IV - Mechano-chemical Instabilities

## Chemistry

- Rho1 pathway



- Myosin-II minifilament assembly (processive bipolar motor)



100 nm

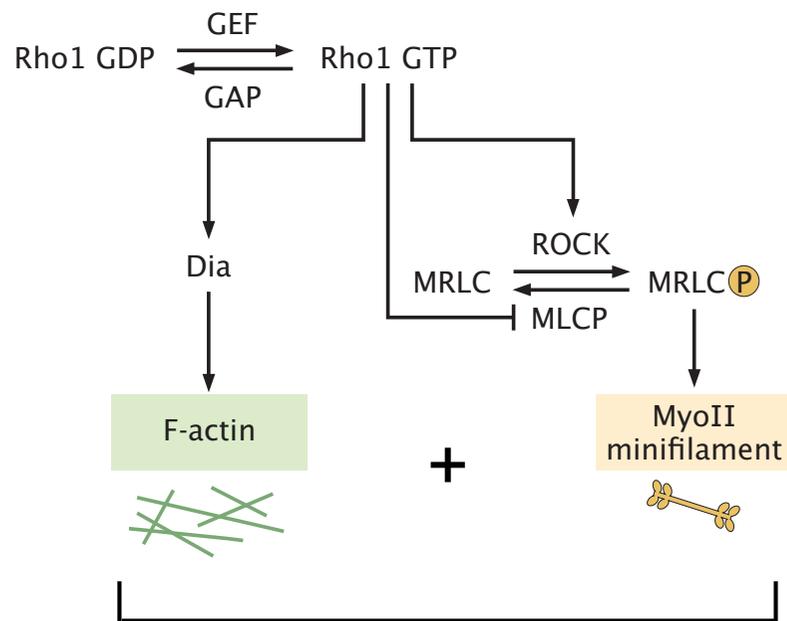
illustration: Nigel Orme.



# IV - Mechano-chemical Instabilities

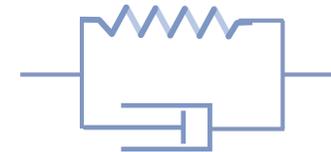
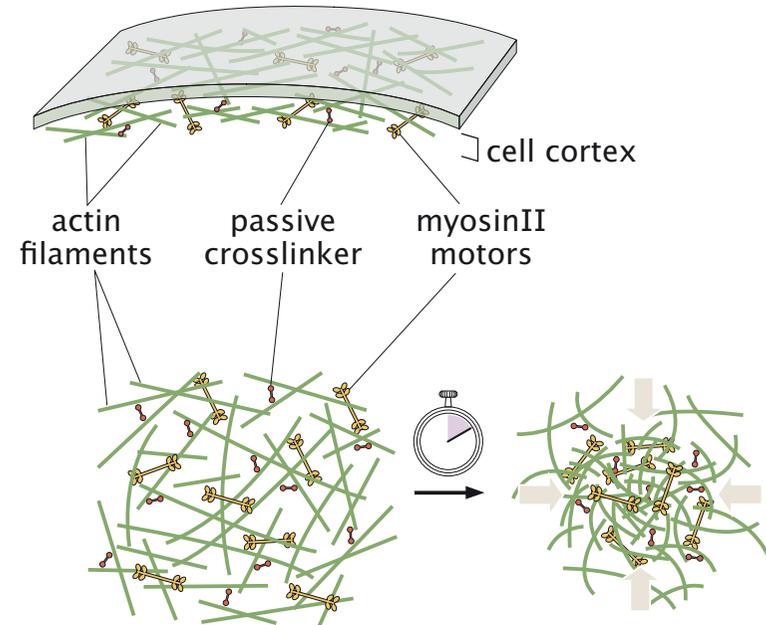
## Chemistry

- Rho1 pathway



## Mechanics

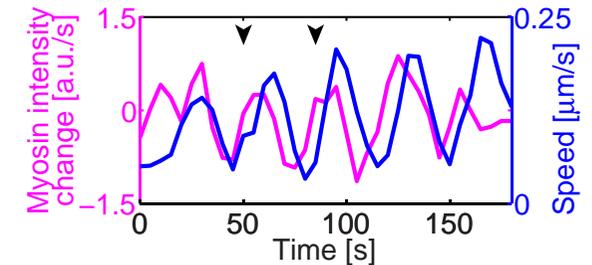
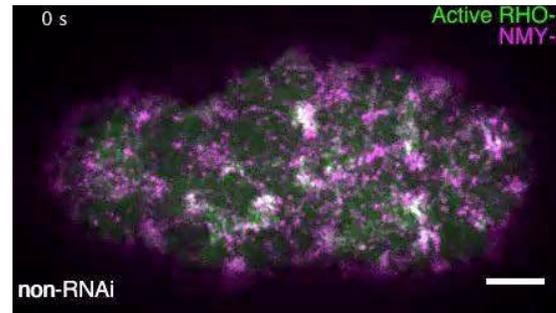
- Actomyosin contraction



# IV - Mechano-chemical Instabilities

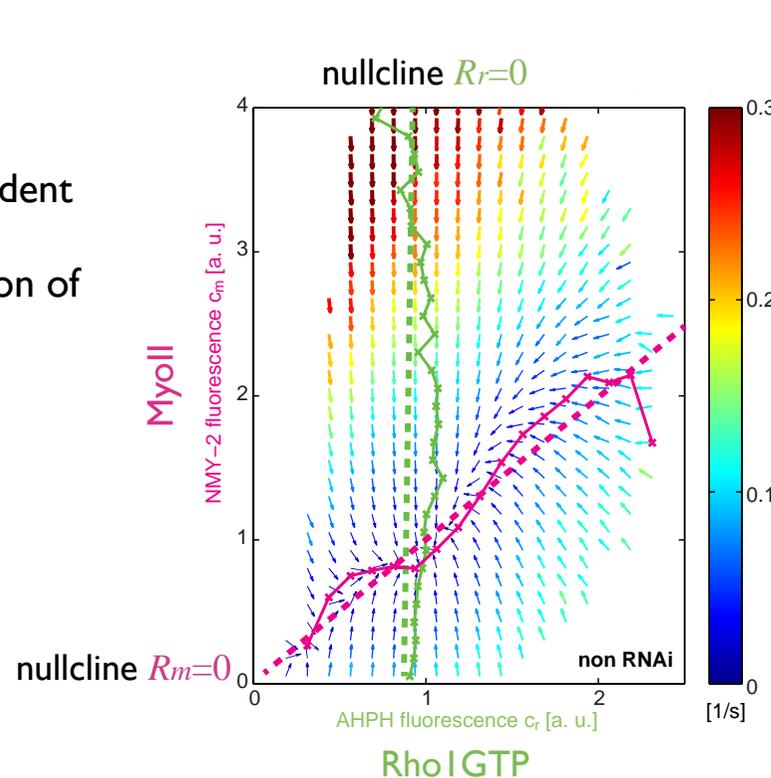
- Pulsatile contraction of actomyosin networks: a mechano-chemical model

MyoII and RhoI GTP exhibit pulsatile dynamics



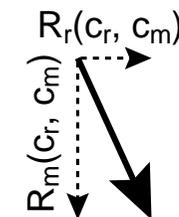
Nullcline analysis:

- RhoI activation kinetics is independent of MyoII concentration
- MyoII activation kinetics is a function of RhoI concentration



$$\underbrace{\partial_t c_i}_{\text{comoving time derivative of } c_i} + \underbrace{\mathbf{v} \cdot \nabla c_i}_{\text{compression induced enrichment}} + \underbrace{c_i \nabla \cdot \mathbf{v}}_{\text{advection}} = \underbrace{R_i(c_r, c_m)}_{\text{reaction kinetics } (i = r, m)}$$

Calculate Reaction kinetics  $R_r$  and  $R_m$  (exchange between cytosol and cortex) based on evolution of concentration and flow field



# IV - Mechano-chemical Instabilities

- Pulsatile contraction of actomyosin networks: a mechano-chemical model

Hydrodynamic mechanochemical Model:

$$\sigma^a = \zeta f(\rho_m)$$

$$\sigma = \eta \partial_x v(x, t) + \sigma^a(\rho_m)$$

$$\partial_x \sigma = \gamma v.$$

$$\lambda \partial_x^2 v + \frac{\zeta'}{\lambda} \partial_x f(\rho_m) - \frac{1}{\lambda} v = 0$$

constitutive equation  
of active gel  
 $\zeta' = \frac{\zeta}{\gamma}$

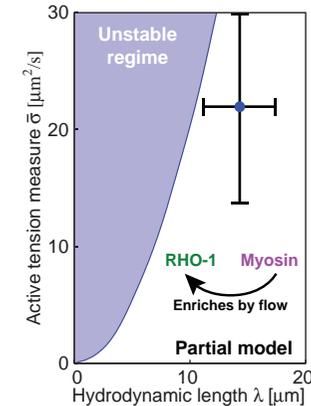
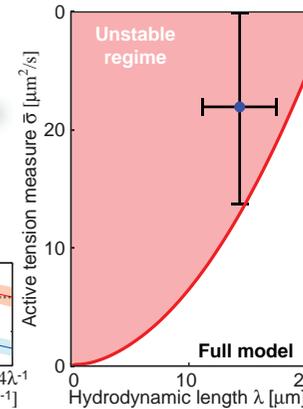
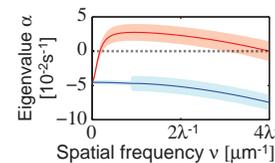
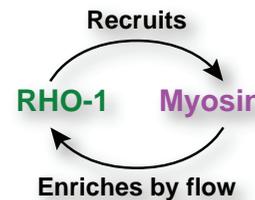
$$\partial_t \rho_i(x, t) + \partial_x j_i(x, t) = R_i(\rho(x, t))$$

$$j_i(x, t) = v(x, t) \rho_i(x, t) - D_i \partial_x \rho_i(x, t),$$

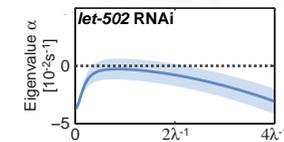
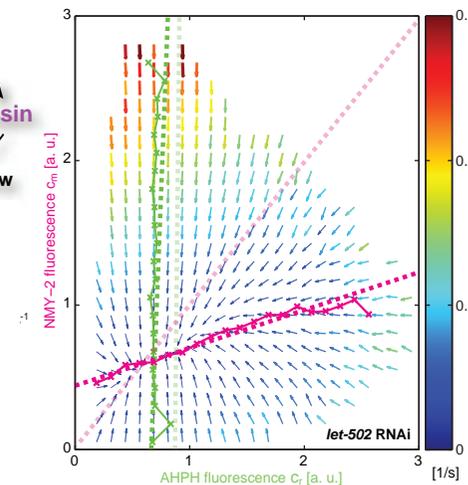
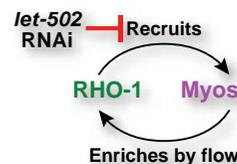
conservation law: reaction kinetics and advection

Linear stability analysis reveals that instability requires large enough active stress and explains instability of *C. elegans* cortex

Instability requires RhoI dependent activation of MyosinII



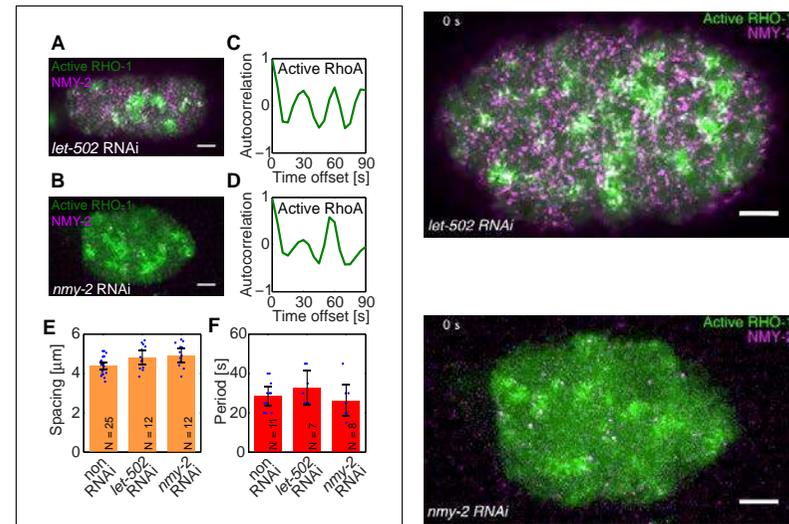
**YET: Pulsations do not emerge from the model**



# IV - Mechano-chemical Instabilities

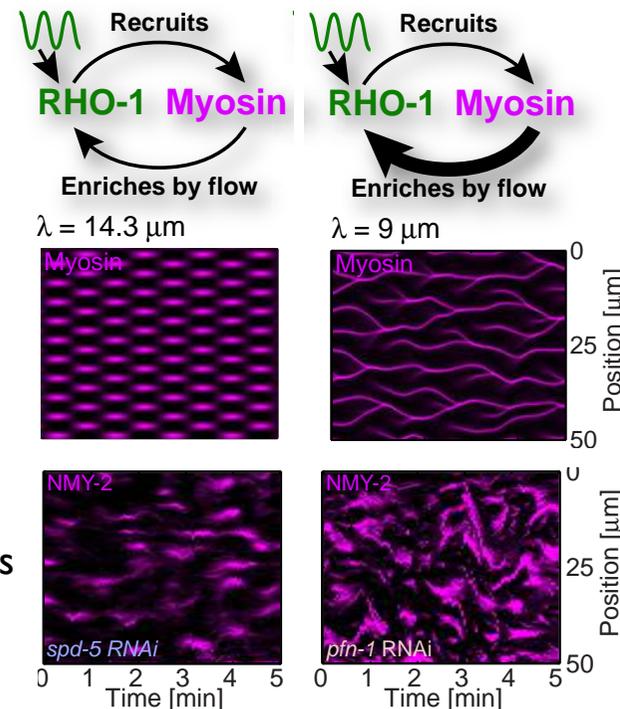
- Pulsatile contraction of actomyosin networks: a mechano-chemical model

Rho I GTP pulsations persists following inhibition of MyosinII



Pulsatile Rho I signalling can entrain pulsatile contractility

Increasing the mechanical feedback (eg. increase advective flow speed via reduction of hydrodynamic length) causes more irregular instabilities



Simulations

Experiments

# IV - Mechano-chemical Instabilities

- Pulsatile contraction of actomyosin networks: a mechano-chemical model

## Origin of Rho | GTP oscillations.

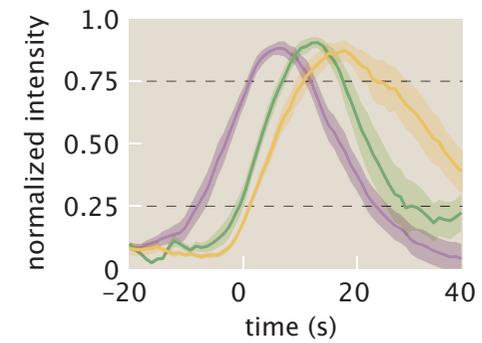
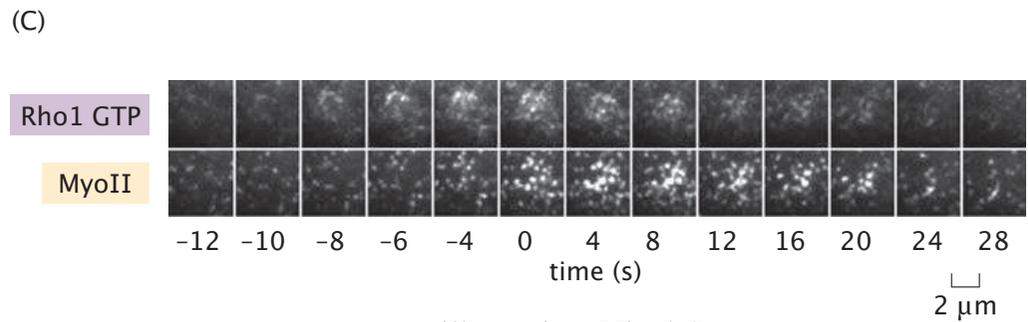
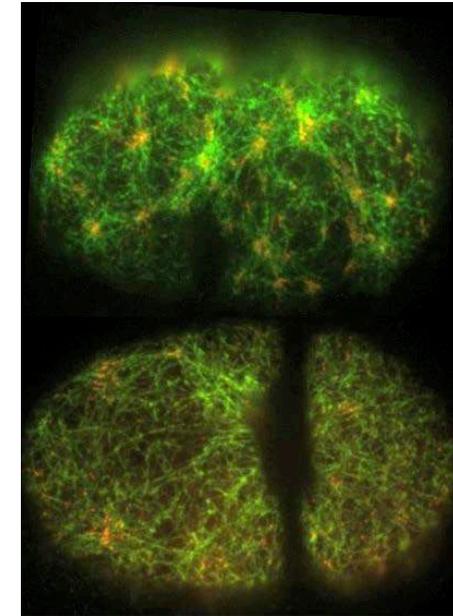
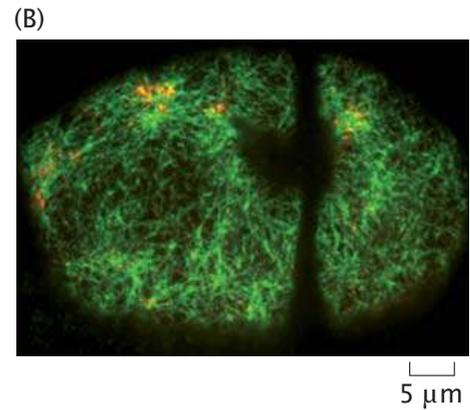
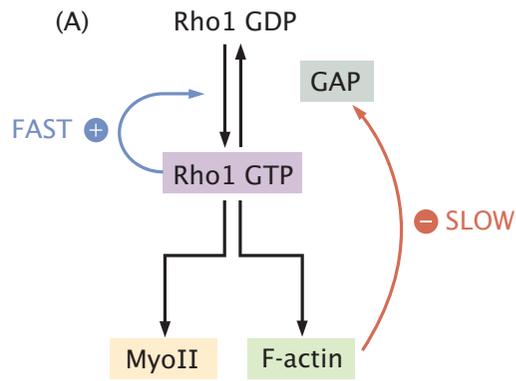


illustration: Nigel Orme.

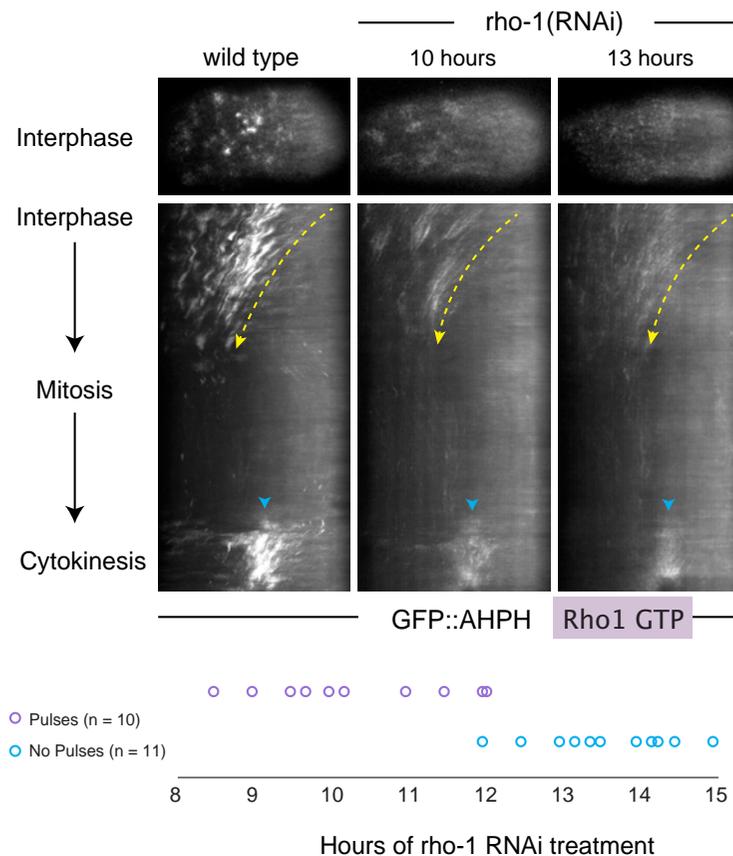
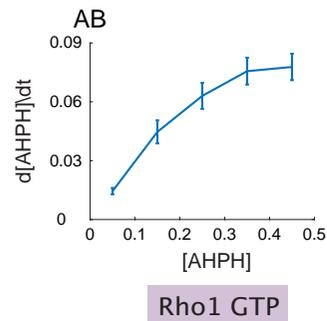
François Robin, J.B Michaux, W. McFadden and Edwin Munro. *J Cell Biol.* 2018 Oct 1. doi: 10.1083/jcb.201806161.

# IV - Mechano-chemical Instabilities

- Pulsatile contraction of actomyosin networks: a mechano-chemical model

Characteristics of an Excitable Chemical system:

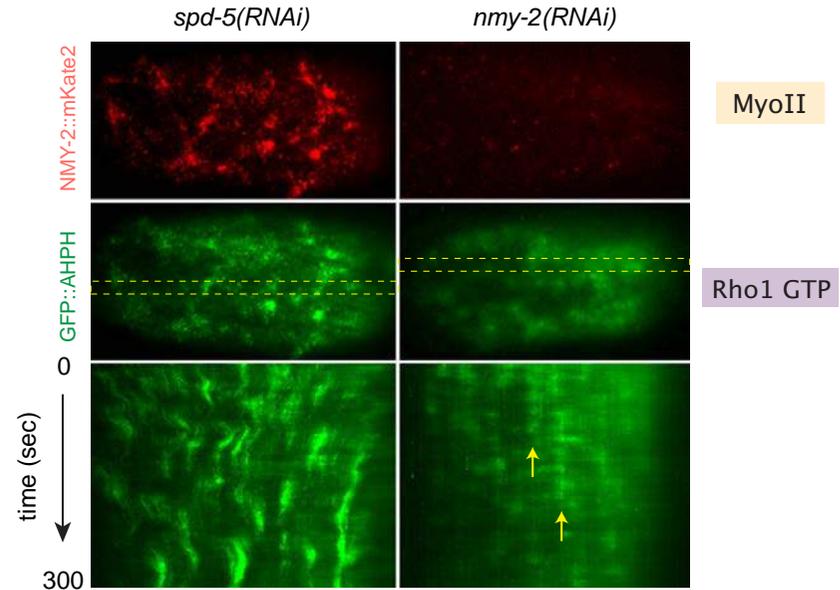
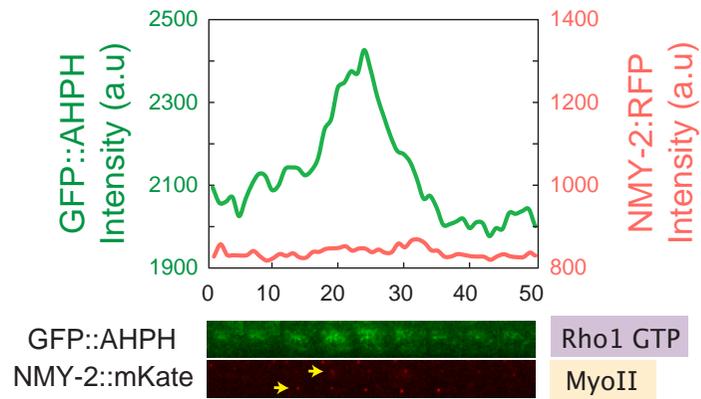
- RhoI positive Feedback and Existence of threshold



# IV - Mechano-chemical Instabilities

- Pulsatile contraction of actomyosin networks: a mechano-chemical model

Rho I positive Feedback is *Independent* of MyoII activation

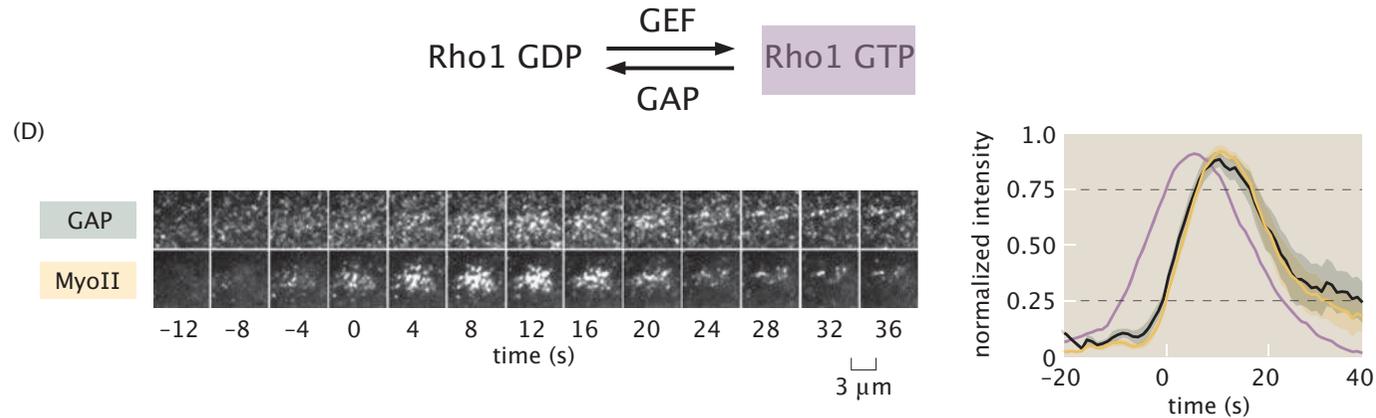


François Robin, J.B Michaux, W. McFadden and Edwin Munro. *J Cell Biol.* 2018 Oct 1. doi: 10.1083/jcb.201806161.

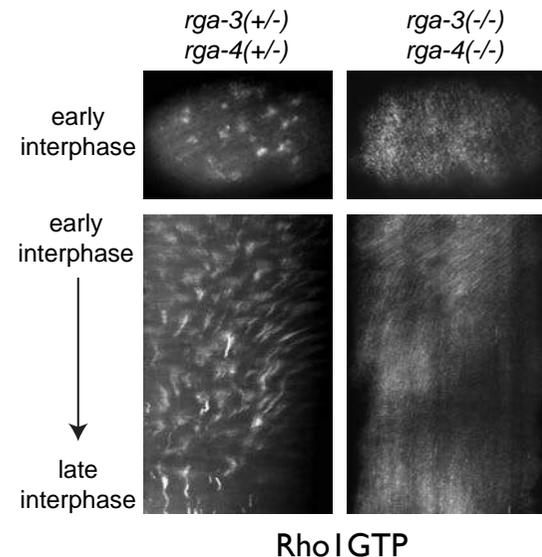
# IV - Mechano-chemical Instabilities

- Pulsatile contraction of actomyosin networks: a mechano-chemical model

Delayed Negative Feedback depends on recruitment of Rho | GAP

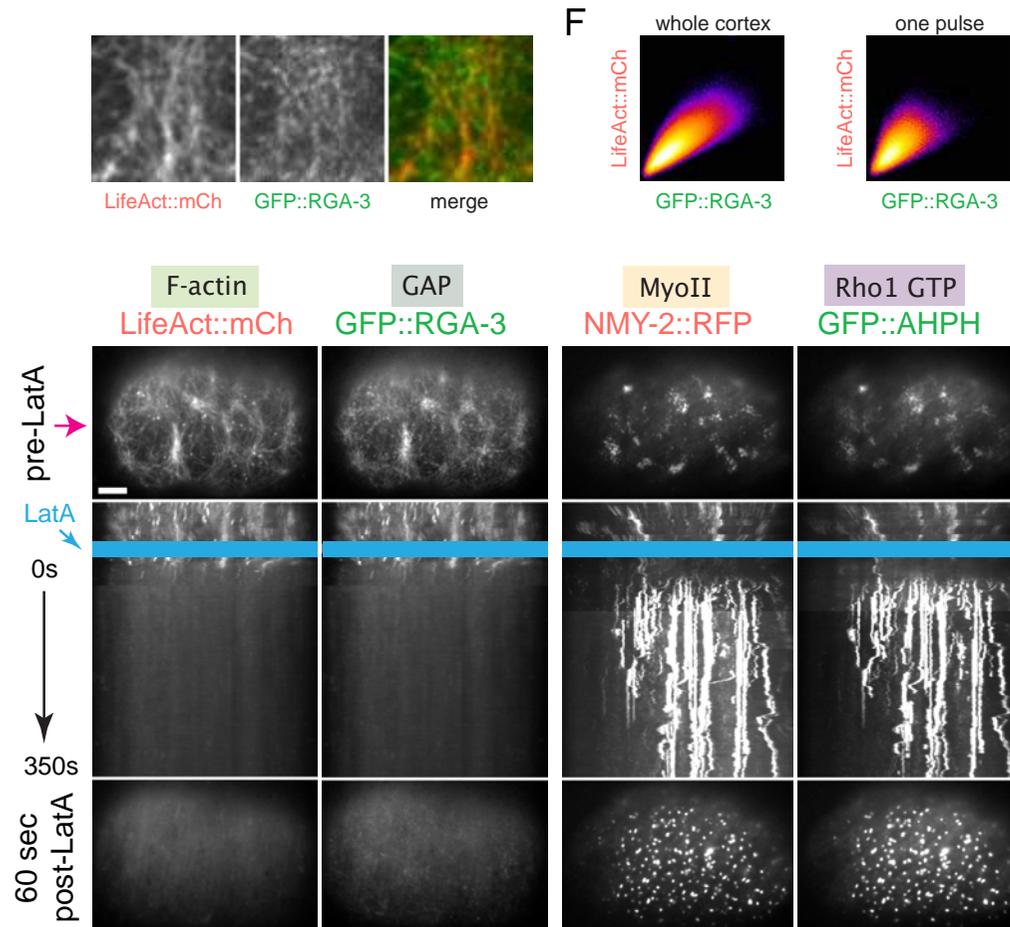


- Pulses of a RhoGAP are synchronous with MyoII pulses
- Rapid accumulation of GAP coincides with reduction and reversal in Rho | GTP concentration
- RhoGAPs (RGA) are required for pulses of Rho | GTP



# IV - Mechano-chemical Instabilities

- Pulsatile contraction of actomyosin networks: a mechano-chemical model  
Rho | GAP decorates actin filaments and is recruited to the cell cortex by actin filaments

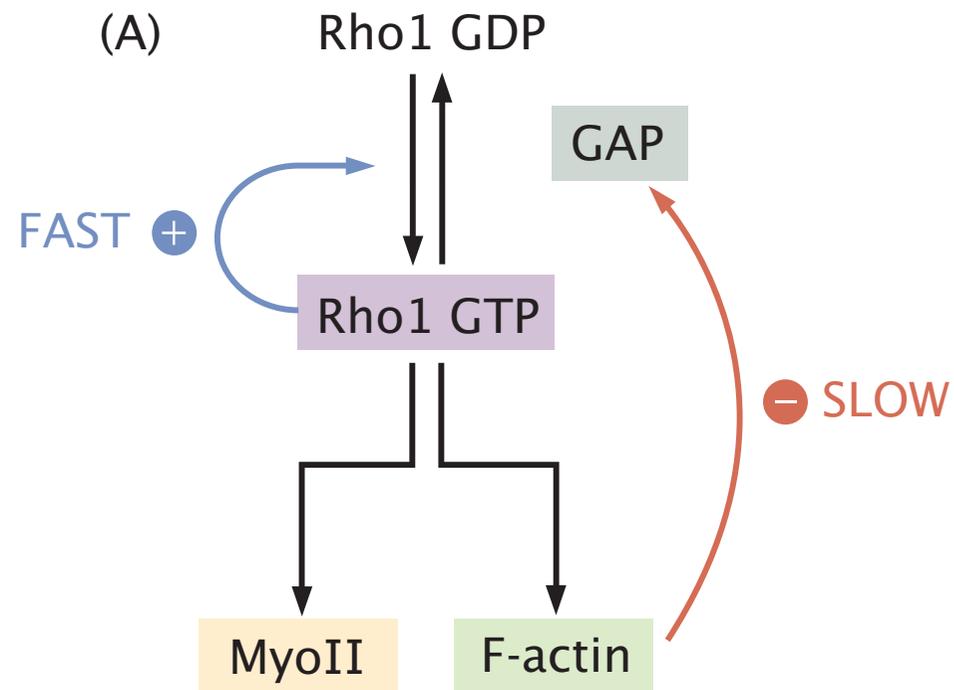


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# IV - Mechano-chemical Instabilities

- Pulsatile contraction of actomyosin networks: a mechano-chemical model

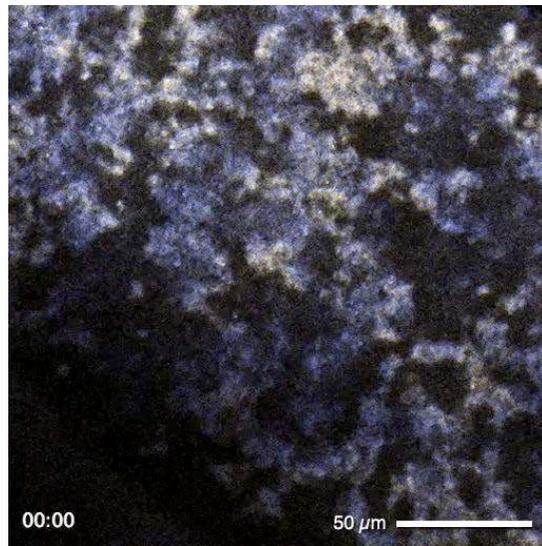
Actomyosin oscillations emerge from autocatalytic activation of RhoI and delayed negative feedback inhibition



# IV - Mechano-chemical Instabilities

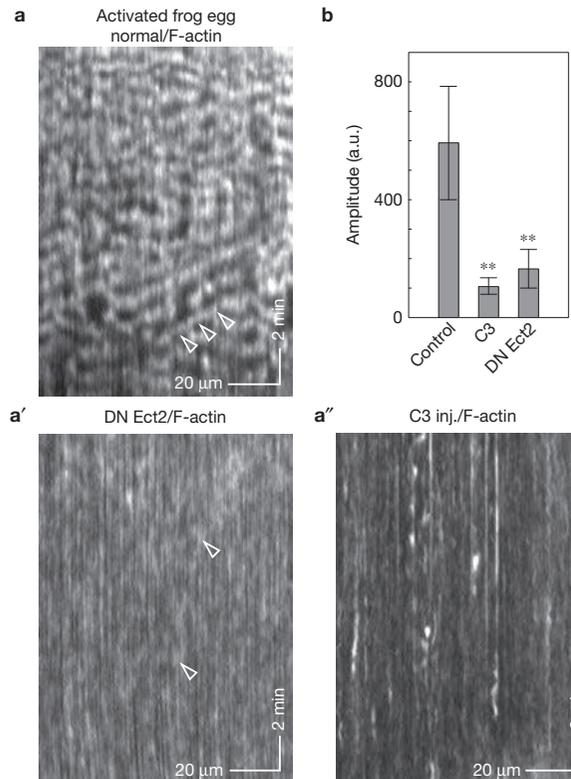
- Travelling waves in actomyosin networks: a mechano-chemical model

$\sim 0.225 \mu\text{m s}^{-1}$

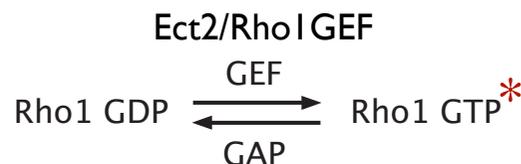
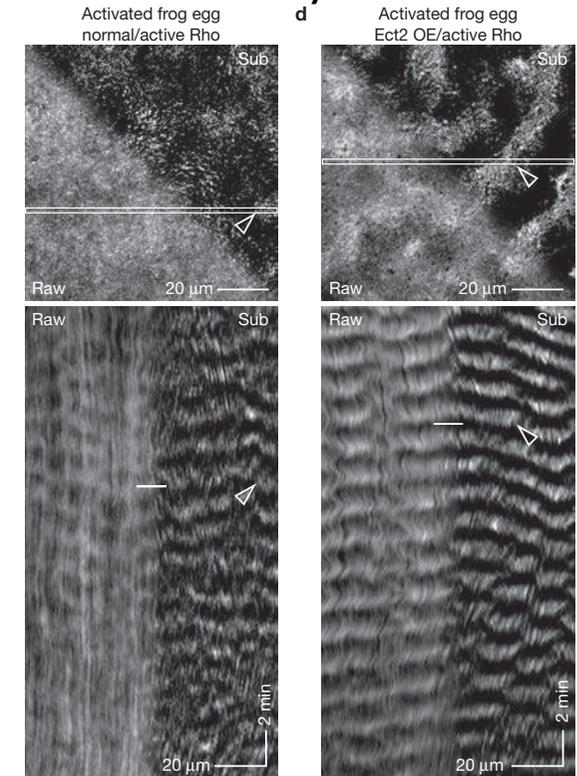


LifeAct : rapid binding — wave front  
 Utrophin: slow binding — wave back

- Rho1 is required for Actin waves



- Rho1 waves amplitude increased by RhoGEF

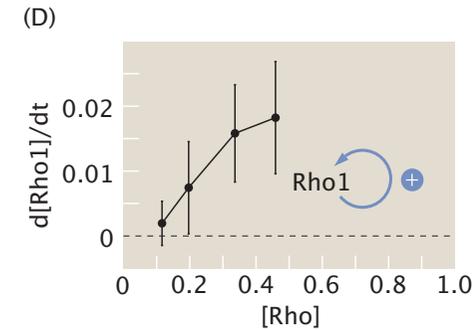
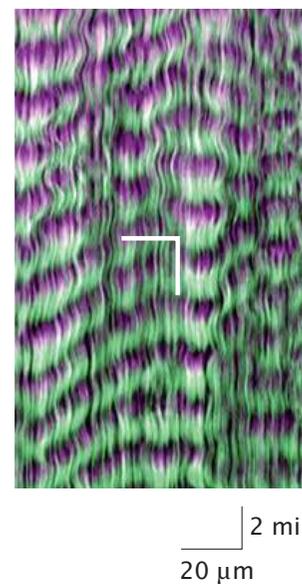
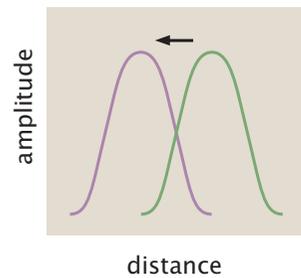
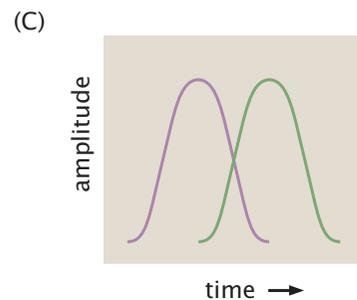
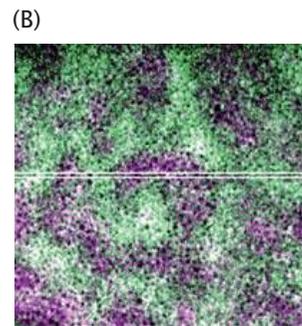
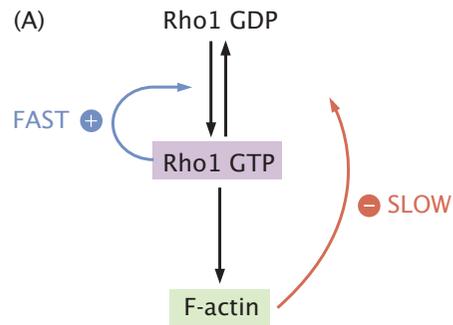


William Bement et al and George von Dassow. *Nature Cell Biology* 17(11):1471-83 (2015)

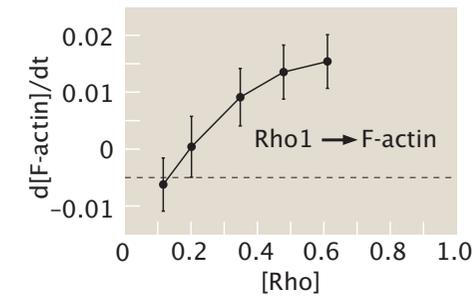
# IV - Mechano-chemical Instabilities

- Travelling waves in actomyosin networks: a mechano-chemical model

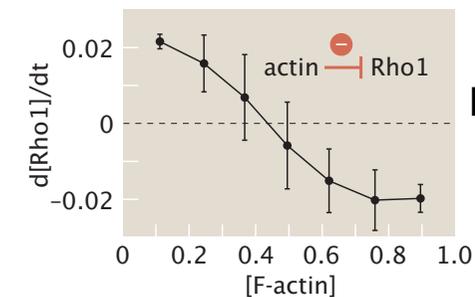
- Characteristics of an Excitable system:



Positive Feedback



Delay



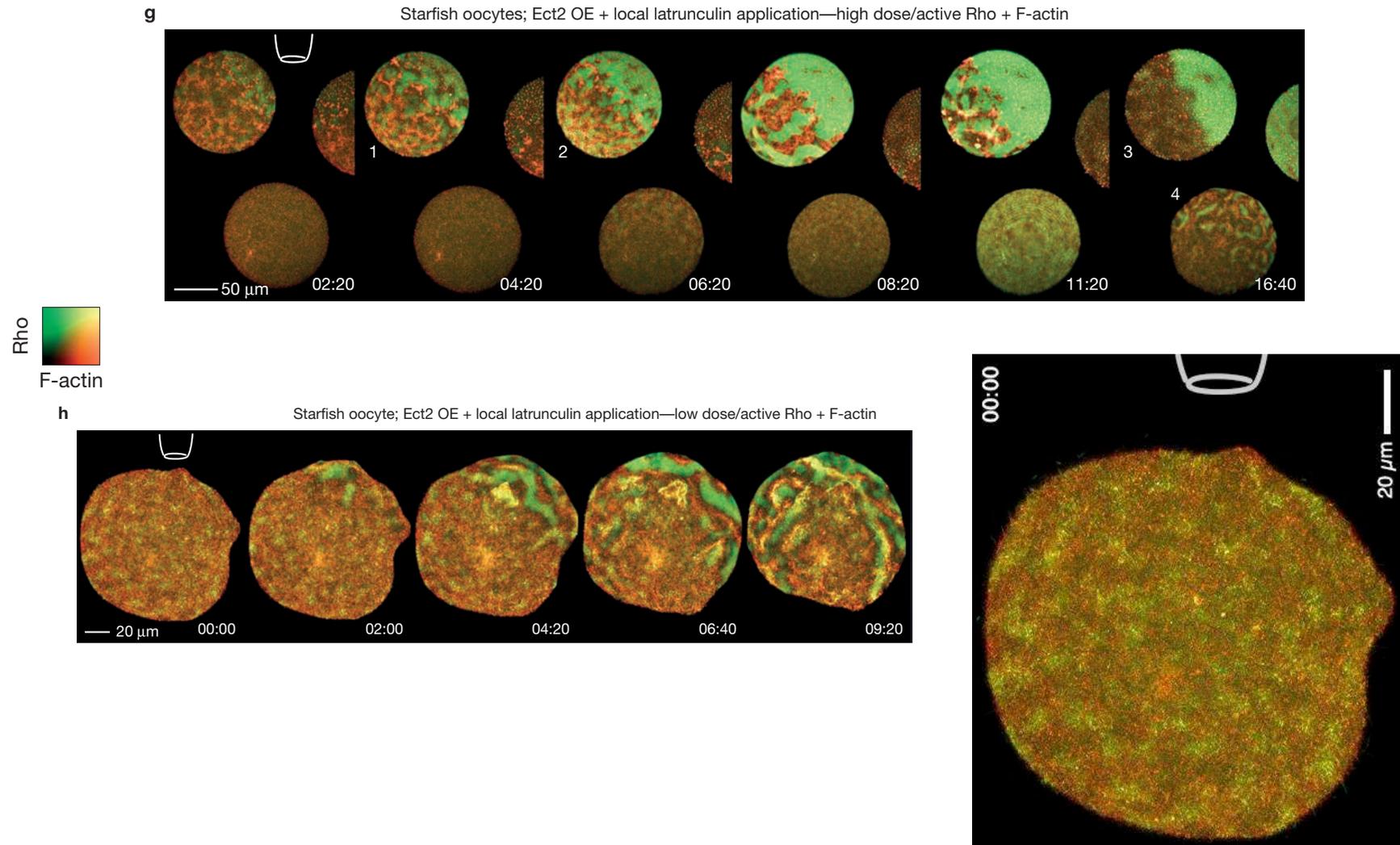
Negative Feedback

William Bement et al and George von Dassow. *Nature Cell Biology* 17(11):1471-83 (2015)

illustration: Nigel Orme.

# IV - Mechano-chemical Instabilities

- Travelling waves in actomyosin networks: a mechano-chemical model  
Actin depolymerisation increases Rho I amplitude and wave length

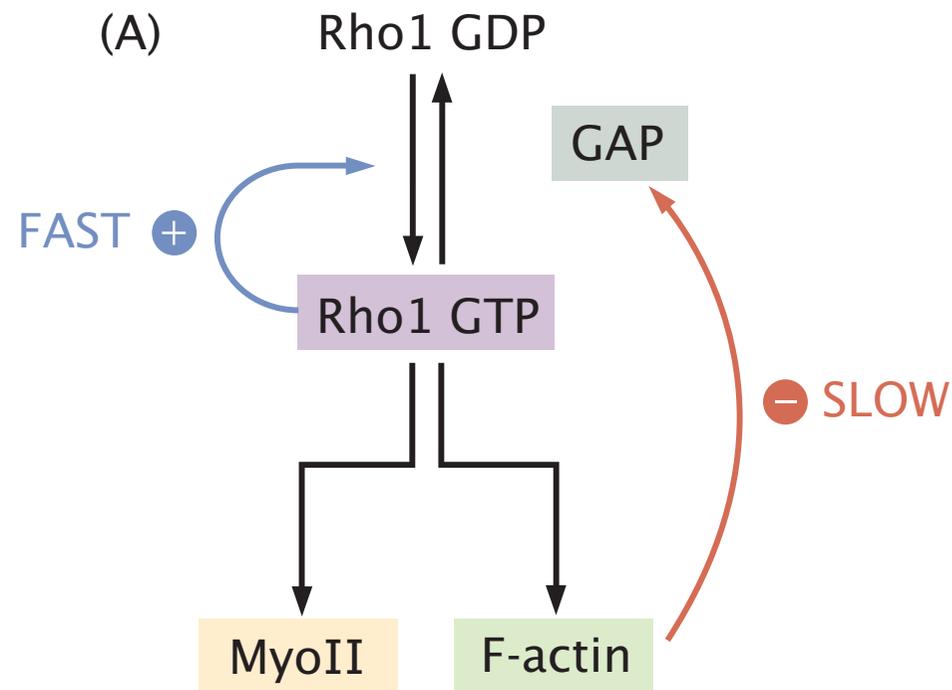


William Bement et al and George von Dassow. *Nature Cell Biology* 17(11):1471-83 (2015)

# IV - Mechano-chemical Instabilities

- Excitable dynamics of actomyosin networks: a mechano-chemical model

Actomyosin oscillations emerge from autocatalytic activation of Rho1 and delayed negative feedback inhibition



# IV - Mechano-chemical Instabilities

- **Biochemical** excitability of actomyosin networks
- **Mechanical feedbacks:**

## Mechanical Feedbacks:

- Tension dependent MyosinII unbinding kinetics (strain dependent stabilisation)

Y. Ren et al D. Robinson *Curr. Biol.* 19:1421 2009 (via actin cross linker Cortaxilin)

Effler et al D. Robinson *Curr. Biol.* 16:1962 2006

Luo et al D. Robinson *Biophys. J.* 102:238 2012

- Tension-dependent filament assembly/disassembly

K. Hayakawa et al, M. Sokabe. *JCB* 195:721 2011 ( tension suppresses Cofilin binding)

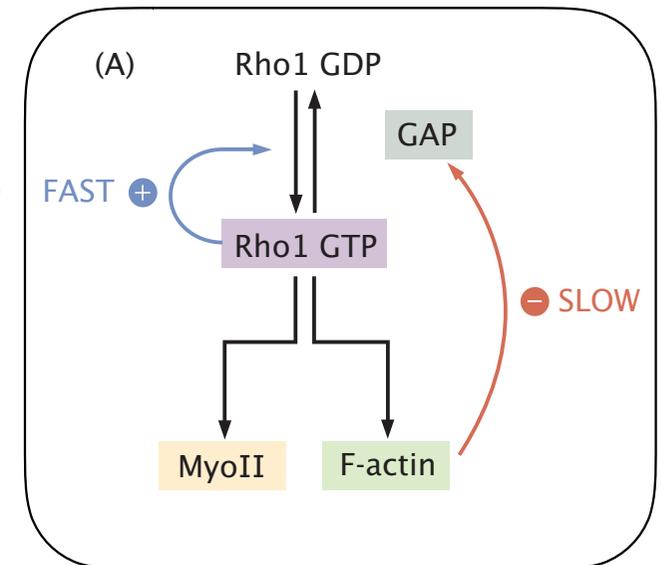
- Tension dependent activation of MyoII

- Advection driven concentration of upstream activators

K. Vijay Kumar, J. Bois, Frank Jülicher and Stephan Grill. *PRL.* (2014). 112, 208101

Munjal, A., Philippe, J.-M., Munro, E. & Lecuit, T. *Nature* 524, 351–355 (2015).

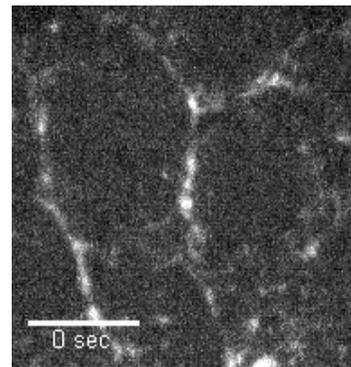
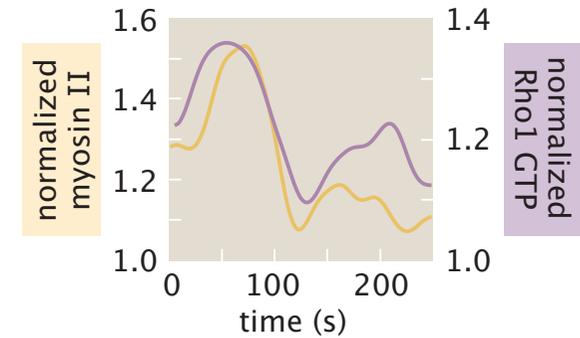
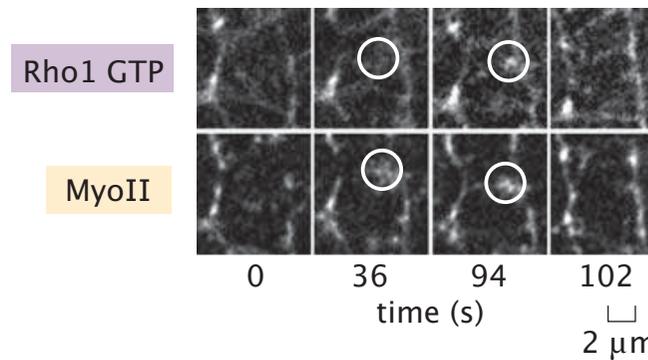
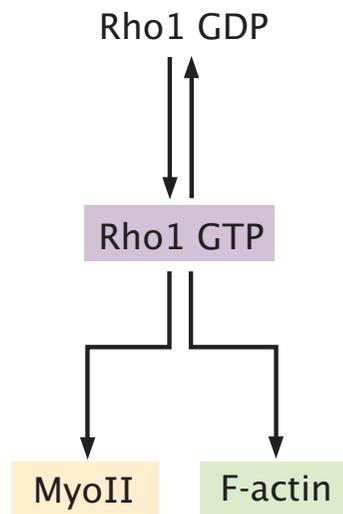
M. Nishikawa, SR Naganathan, F. Jülicher and S. Grill. *eLife* 2017;6:e19595. DOI: 10.7554/eLife.19595



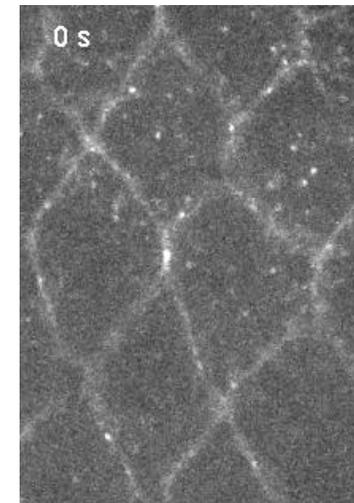
# IV - Mechano-chemical Instabilities

- **Mechanical feedback** in excitable actomyosin networks

Pulsation of Myosin-II and its activators Rho | GTP, ROK



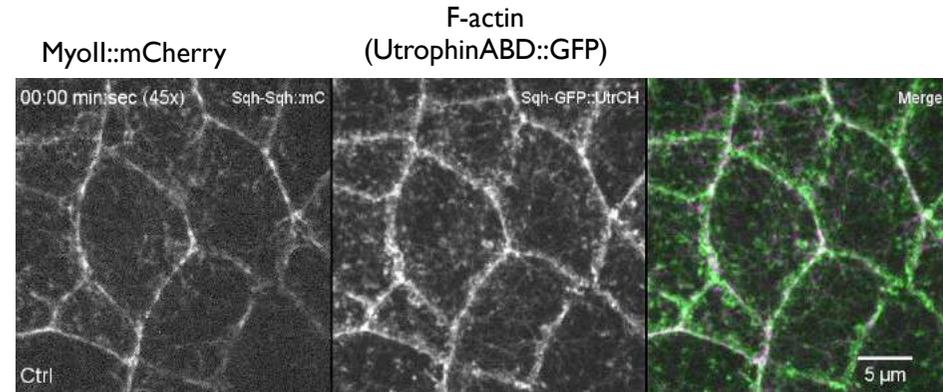
MyoII::GFP



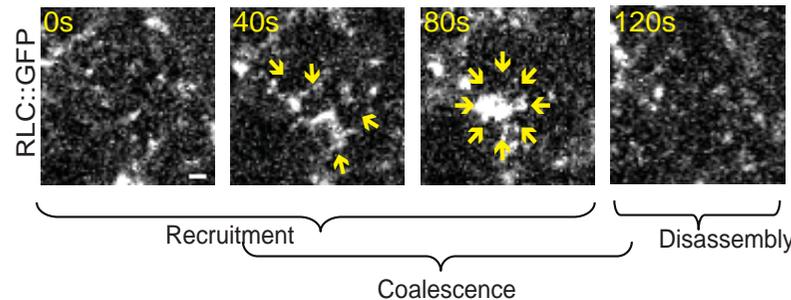
Rho1GTP::GFP

# IV - Mechano-chemical Instabilities

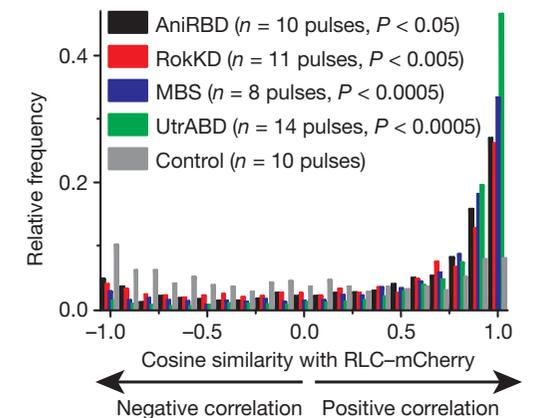
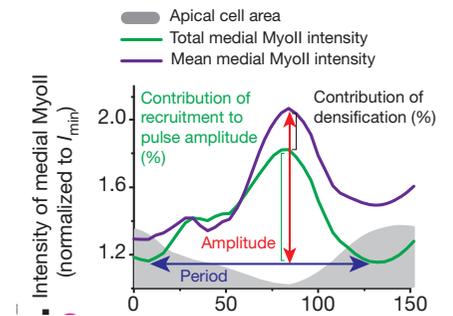
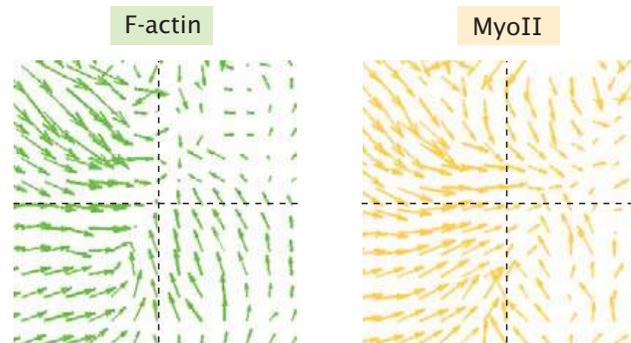
- **Mechanical feedback** in excitable actomyosin networks



Non-linear amplification of MyosinII recruitment during pulse assembly



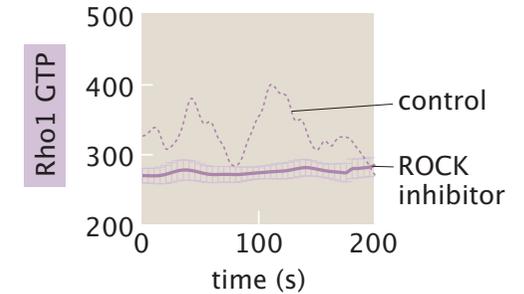
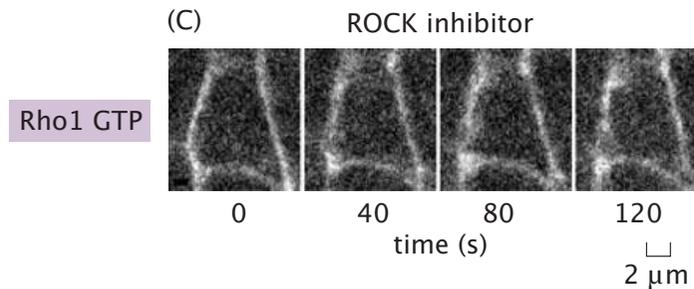
Advection of all biochemical network components



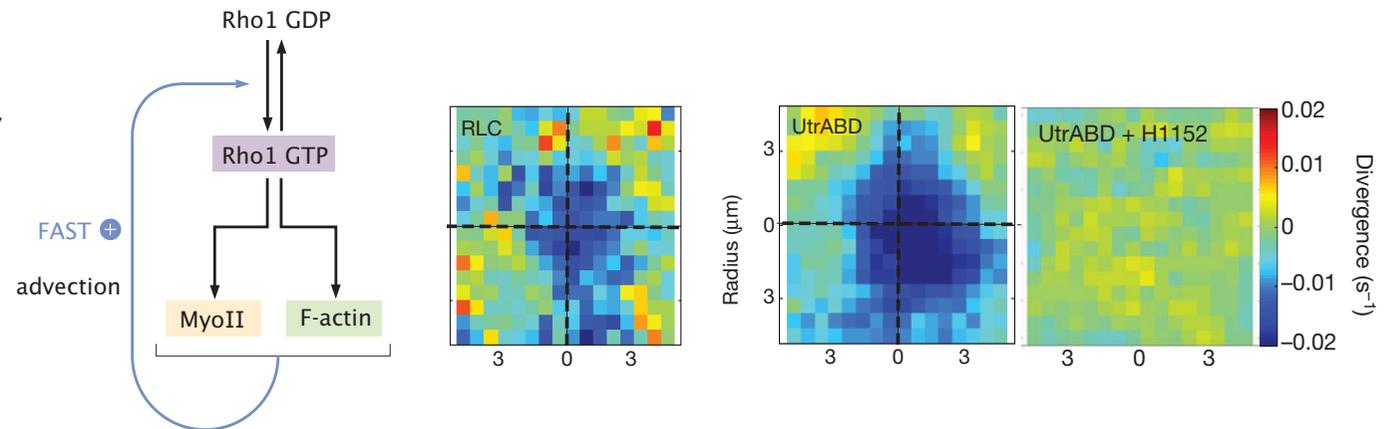
# IV - Mechano-chemical Instabilities

- **Mechanical feedback** in excitable actomyosin networks

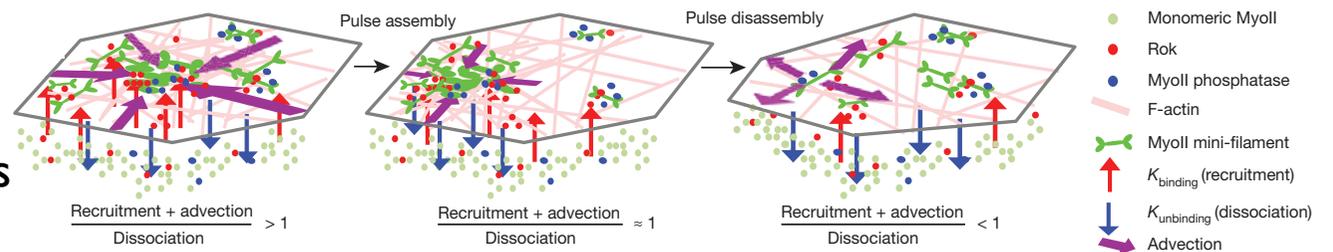
Pulsation of Rho1 GTP requires MyosinII activation



All network components show convergent advection during pulse assembly  
Advection requires MyoII



Competition between motor driven advection and turnover underlies oscillations

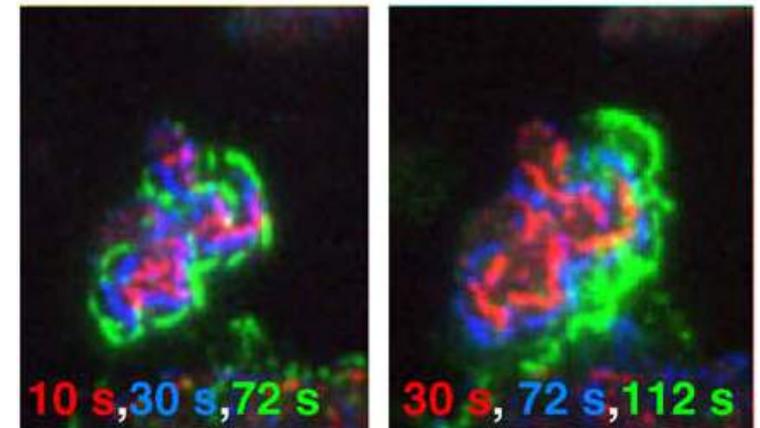
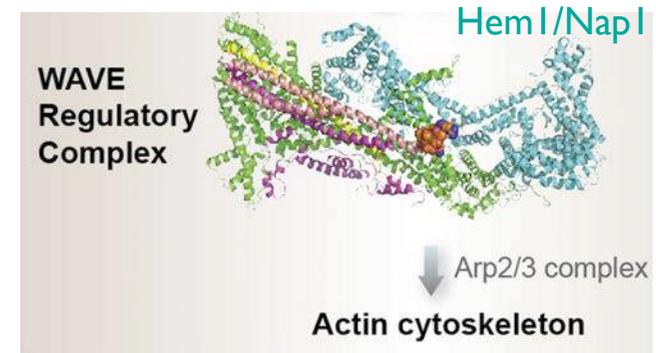
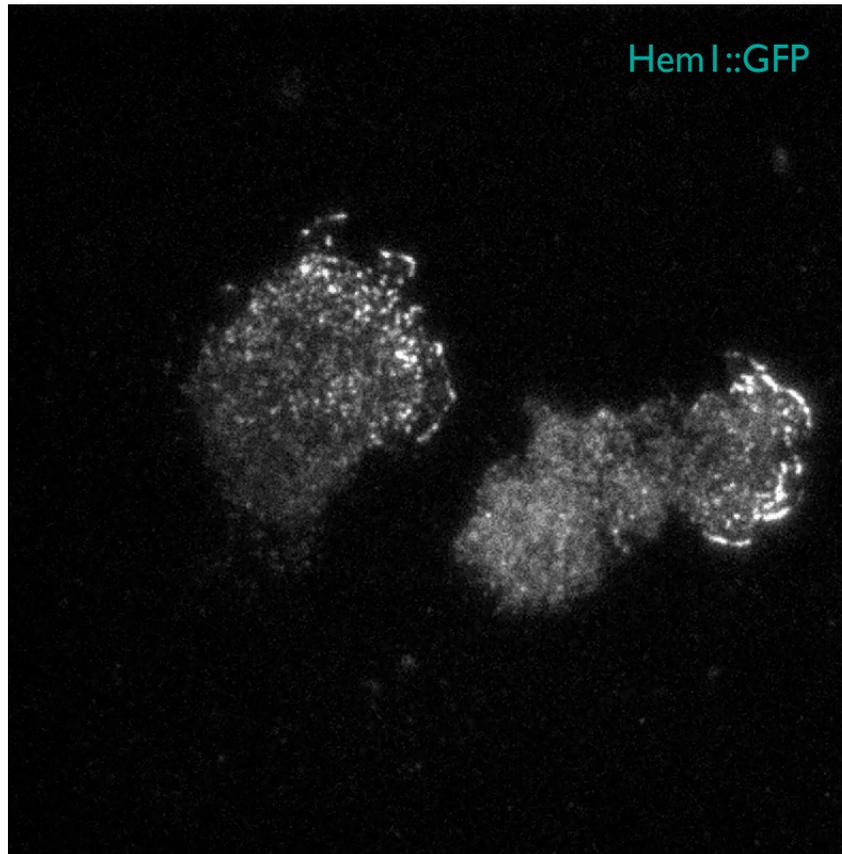


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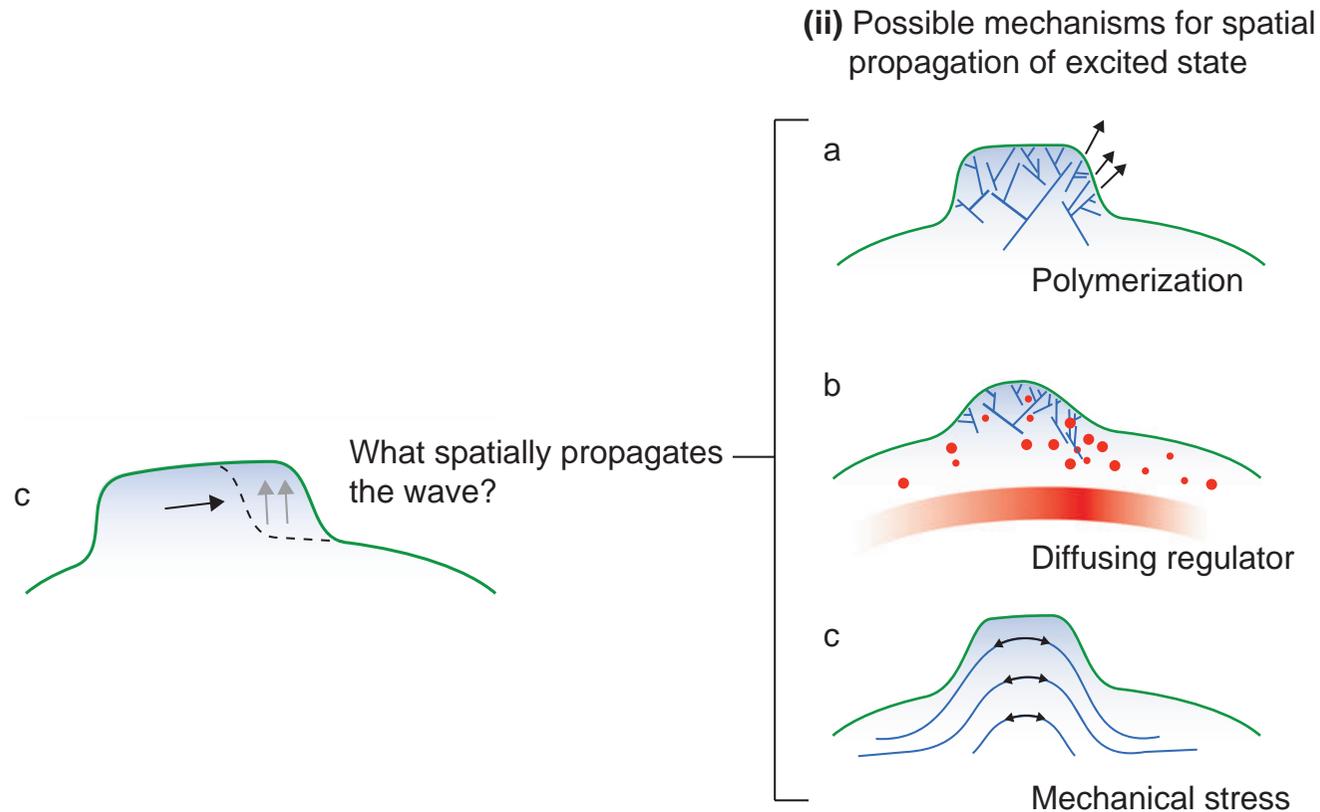
# III - Mechano-chemical Instabilities

- An actin based wave generator during cell motility



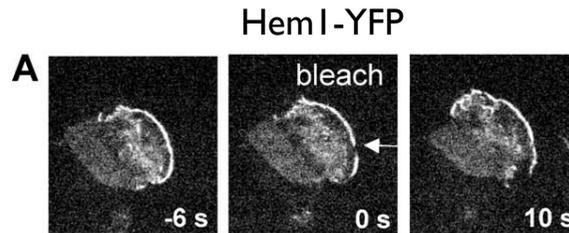
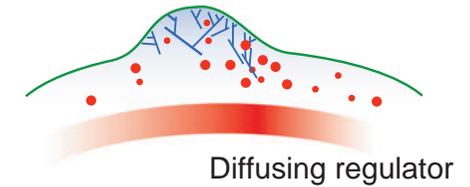
# III - Mechano-chemical Instabilities

## Mechano-chemical propagation of trigger waves

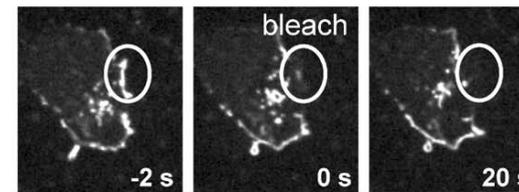
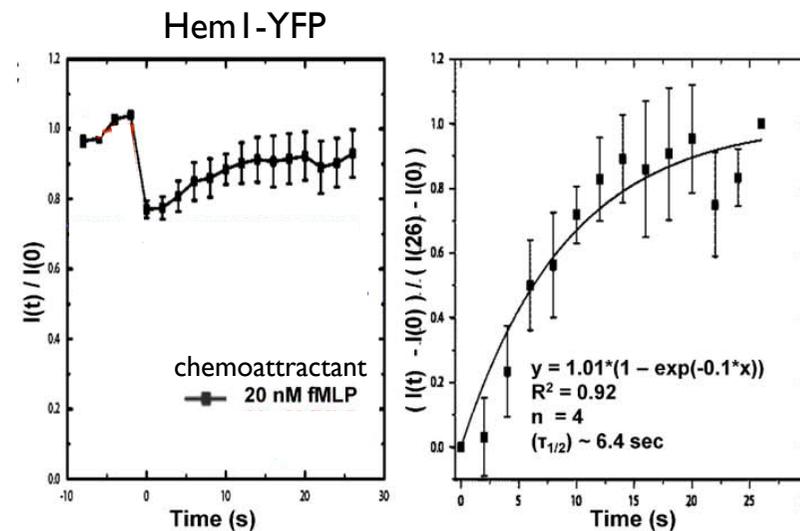


# III - Mechano-chemical Instabilities

- An actin based wave generator during cell motility



- The Wave2 complex dynamically equilibrates within a few seconds between the cytosol and the membrane
- The movement of the Wave2 front is not due to the translocation of the protein but to its dynamics recruitment in a wave-like manner



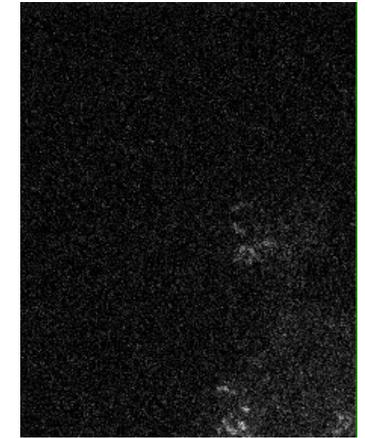
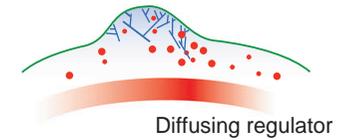
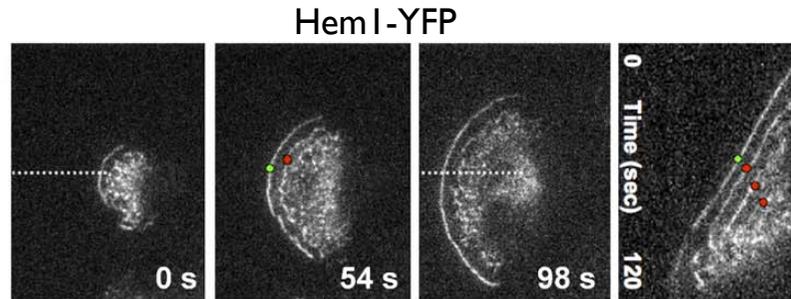
+Latrunculin A

- Rapid equilibration requires actin filaments

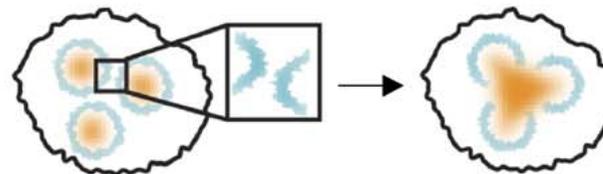
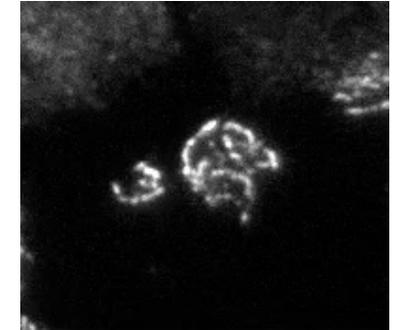
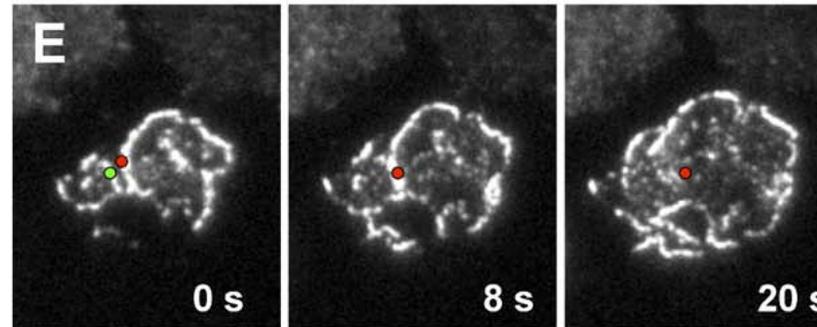
# III - Mechano-chemical Instabilities

- The Hem I wave has characteristics of a trigger wave

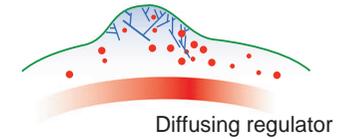
- Successive trigger waves at the cell edge with refractory period



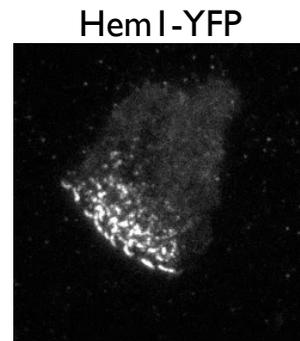
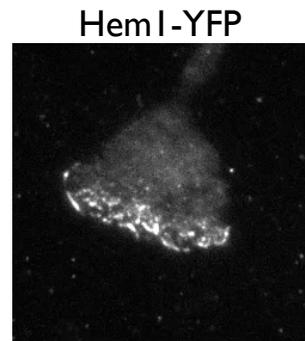
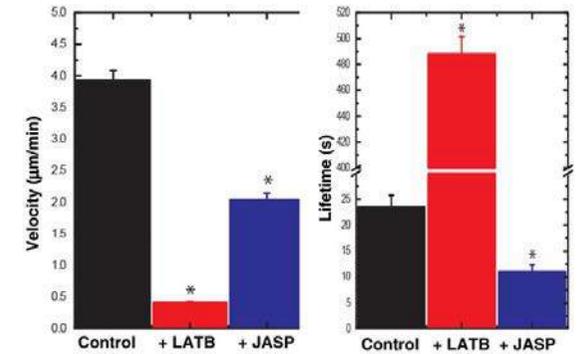
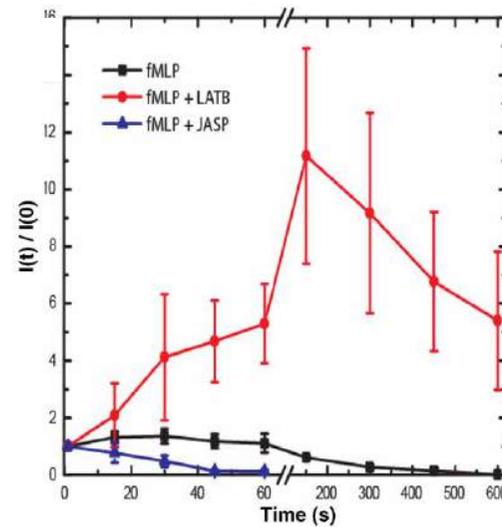
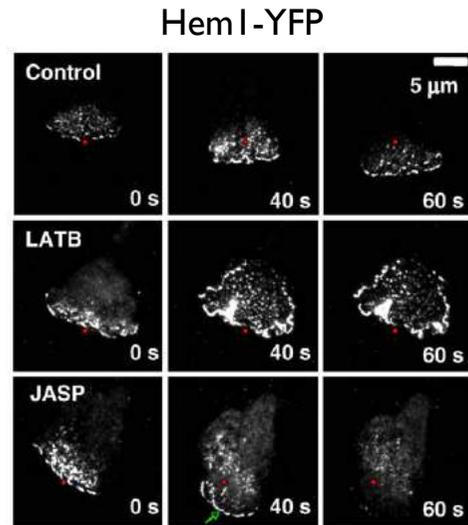
- Colliding waves annihilate (key property of trigger wave, reflecting refractory period)



# III - Mechano-chemical Instabilities



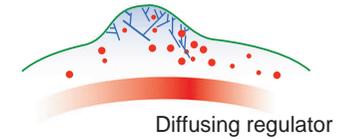
- Actin filaments provide inhibitory signal on Wave2 trigger wave dynamics.



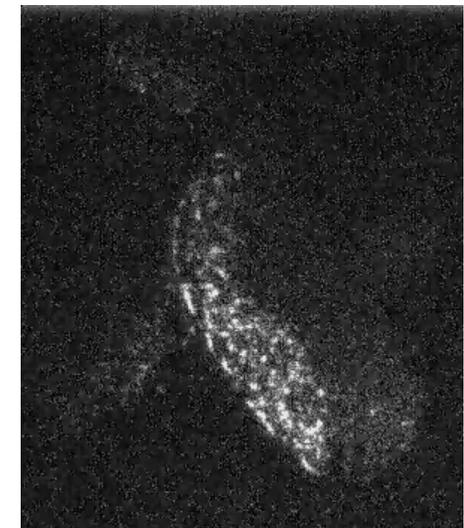
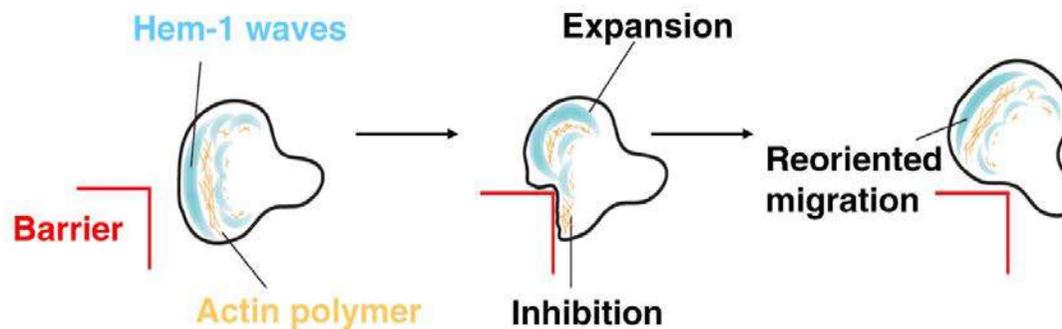
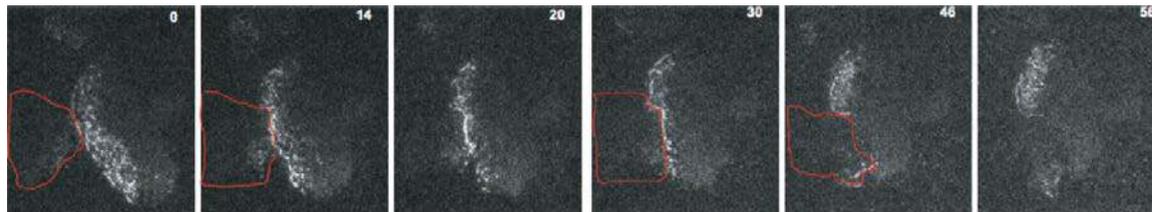
Actin destabilisation (LatA)

Actin stabilisation (Jasp)

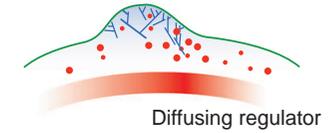
# III - Mechano-chemical Instabilities



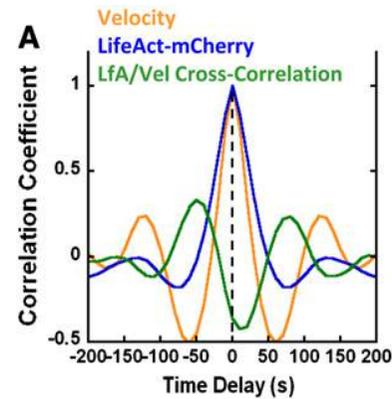
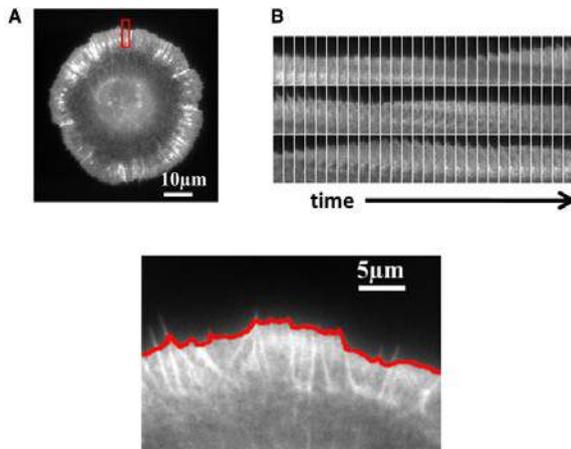
- Blocking membrane protrusion by mechanical barrier leads to wave collapse
- Induction of new wave in adjacent cell region
- Adaptive strategy for cell motility



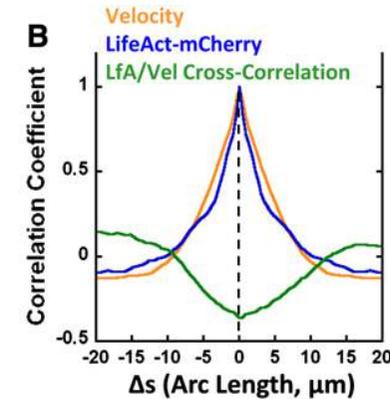
# III - Mechano-chemical Instabilities



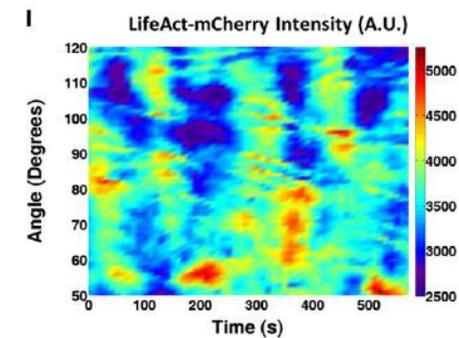
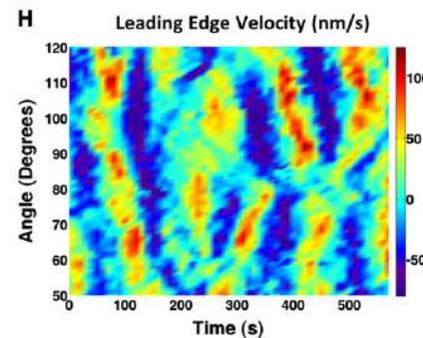
- The leading edge of plated cells shows oscillatory dynamics, and lateral waves.
  - Leading edge velocity anti-correlates with F-actin density



Space independent correlations

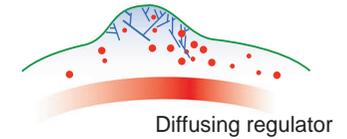


Time independent correlations



Gillian L Ryan, et al., and Dimitrios Vavylonis *Biophysical Journal* Volume 102 April 2012 1493–1502

# III - Mechano-chemical Instabilities



- Excitable dynamics driven by activator diffusion and fluctuations underlies leading edge dynamics

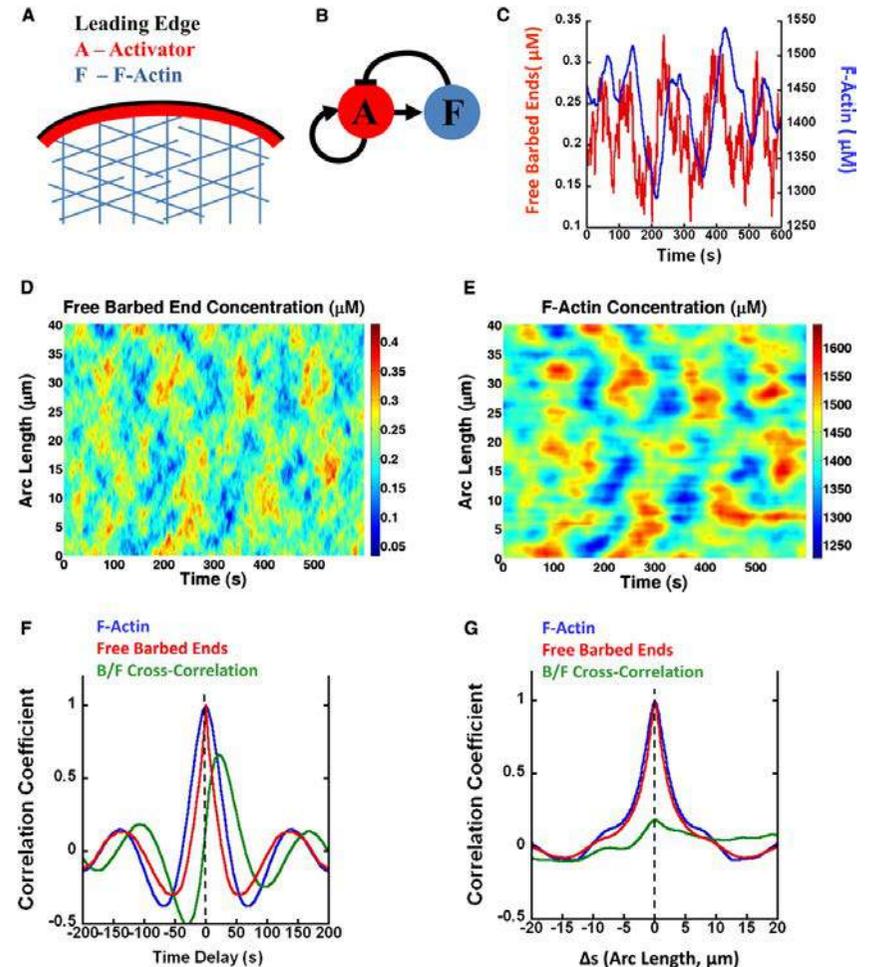
$$\frac{\partial A}{\partial t} = (\rho_0 + \rho_2 A^2) e^{-F/F_s} - k_A^- A + D_A \nabla^2 A + \sigma(x, t), \quad (1)$$

non-linear autocatalysis (points to  $\rho_2 A^2$ )  
 negative feedback (points to  $e^{-F/F_s}$ )  
 deactivation (points to  $k_A^- A$ )  
 diffusion (points to  $D_A \nabla^2 A$ )  
 noise (points to  $\sigma(x, t)$ )

A: activator  
 B: F-actin barbed ends  
 F: actin filaments

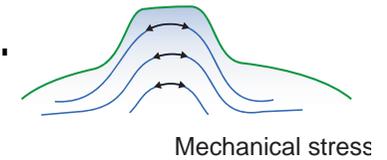
$$\frac{\partial B}{\partial t} = k_B^+ A - k_B^- B,$$

$$\frac{\partial F}{\partial t} = k_F^+ B - k_F^- F.$$

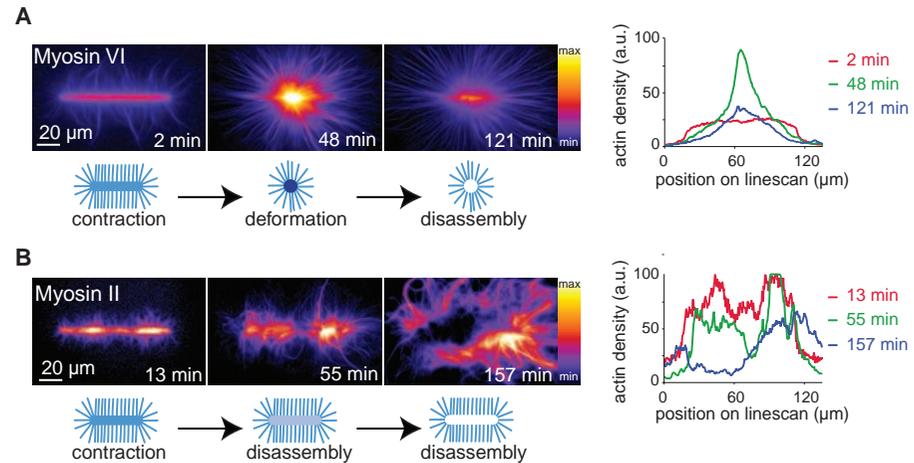


# III - Mechano-chemical Instabilities

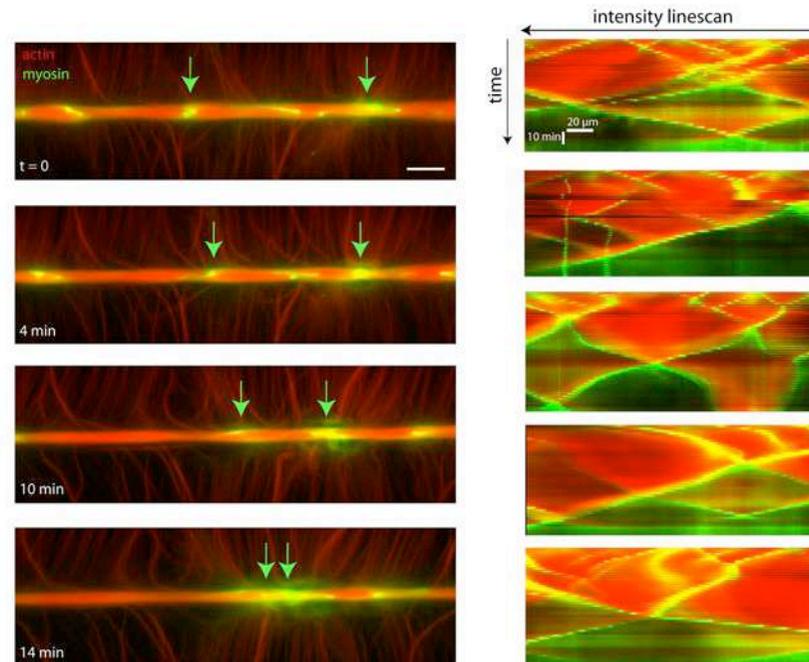
- *in vitro* evidence of tension dependent spatial coupling in wave progressio..
- Contraction (eg. Myosin) induced wave of actin disassembly



- Myosin induces sequential deformation and disassembly of anti-parallel actin filaments

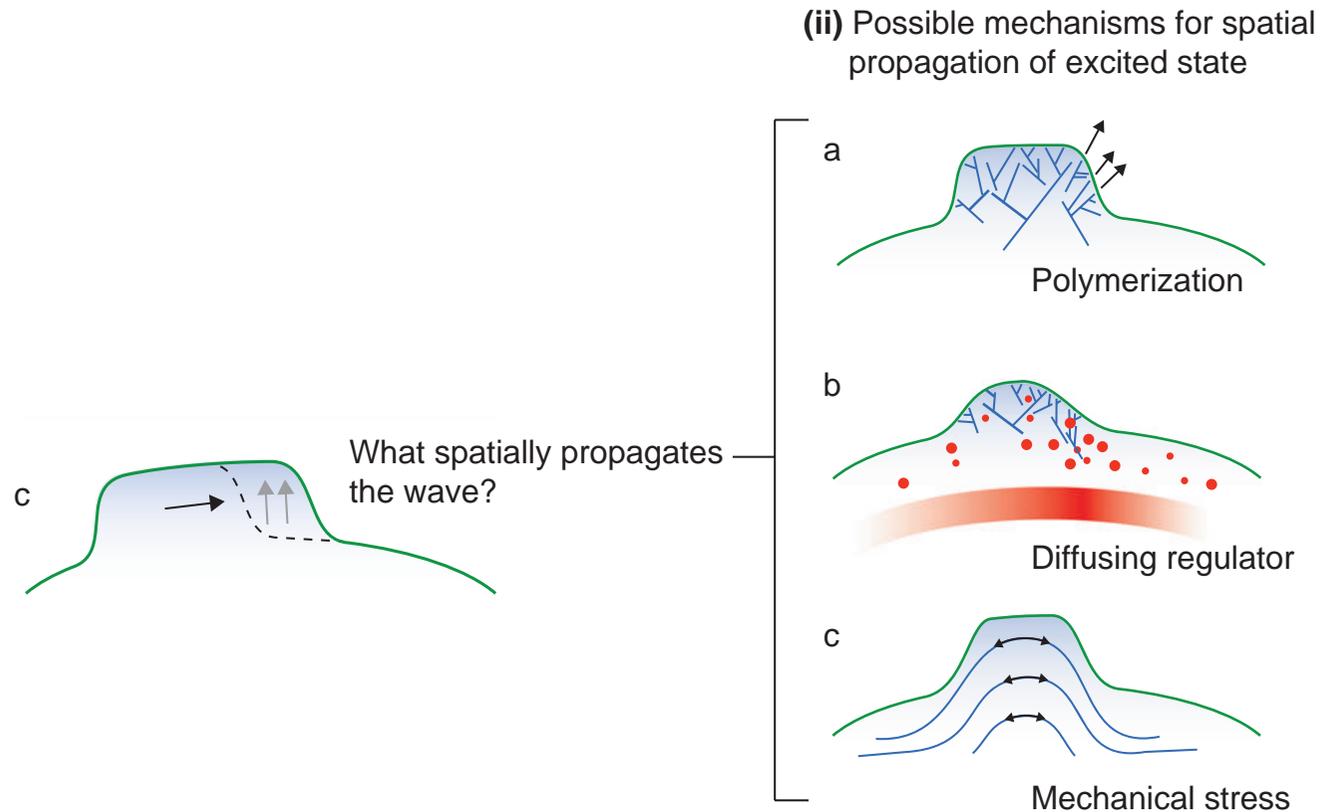


- Myosin induces actin disassembly trigger waves



# III - Mechano-chemical Instabilities

## Mechano-chemical propagation of trigger waves



# Self-organisation of mechanochemical systems: principles

---

- Mechano-chemical systems give rise to complex spatial and temporal instabilities across biological scales:
  - e.g. spatial patterns, pulsations and trigger waves in actomyosin networks
- Mechanical « Turing-like » instabilities:
  - autocatalytic amplification of active stress (advection, non linear effects due to stress/strain dependent activation of stress, effect of orientational order of actin filaments or ECM, etc)
  - long range negative feedback: elasticity, friction, diffusion etc.
- Excitability of biochemical network
  - autocatalytic amplifications of fluctuations and delayed negative feedback.
  - spatial coupling (diffusion of molecule)
  - e.g. Rho | GTP oscillations and travelling waves:
- Mechanical feedbacks in excitable systems:
  - positive feedback, and/or spatial coupling.
- Mechano-chemical coupling: advection and turnover of active stress regulators
  - ✓ **Length and time scales associated with mechano-chemical information govern these dynamics**

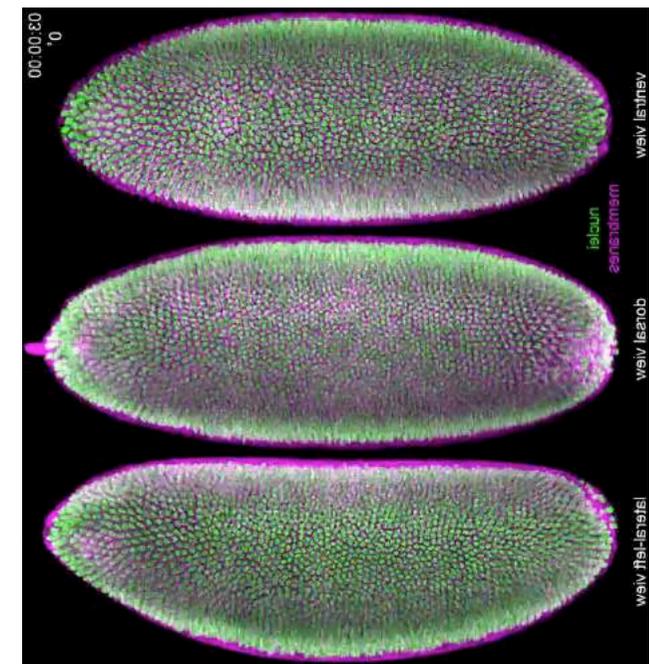
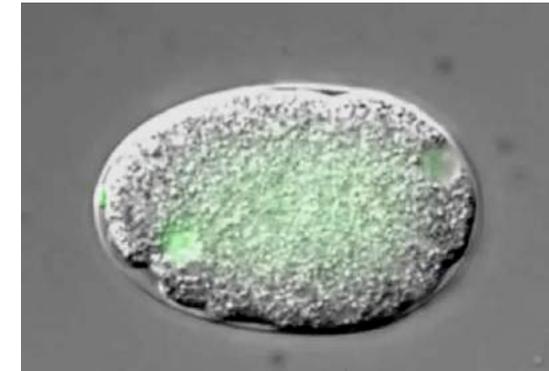
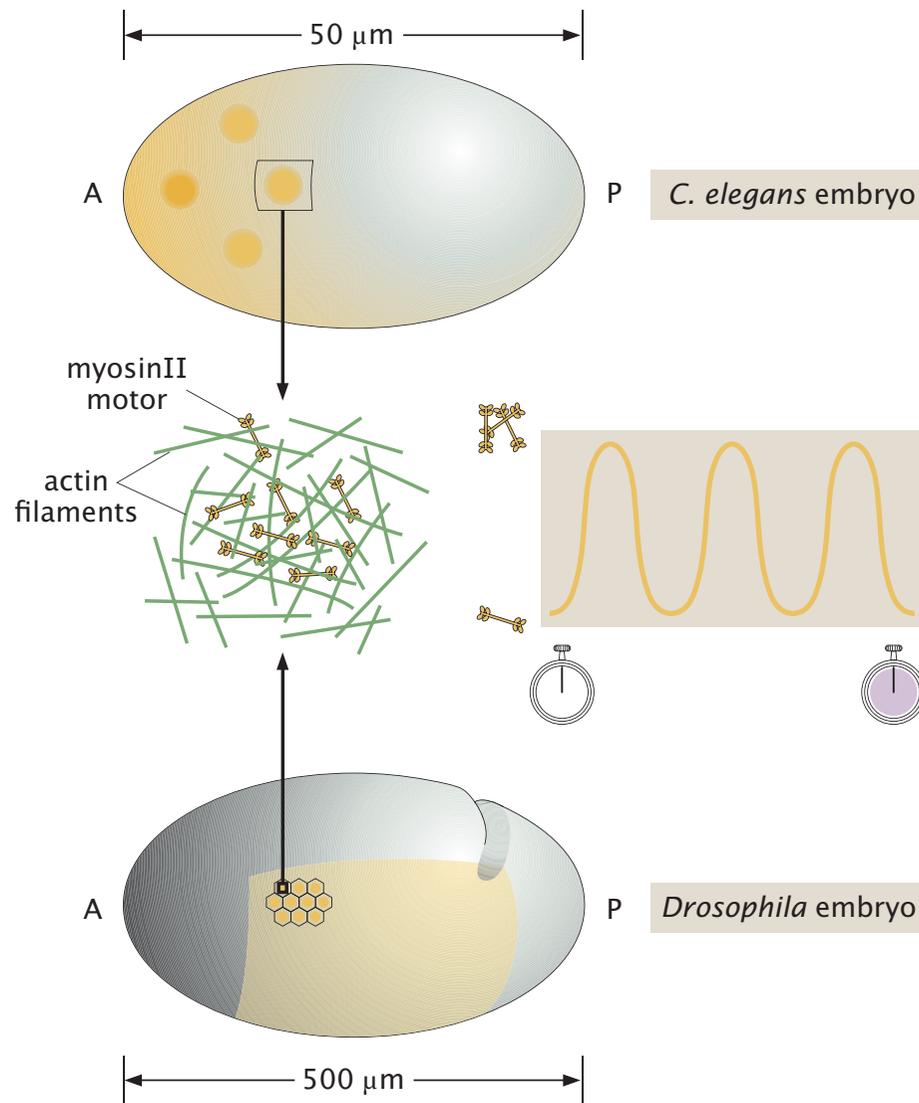


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# V - Developmental significance

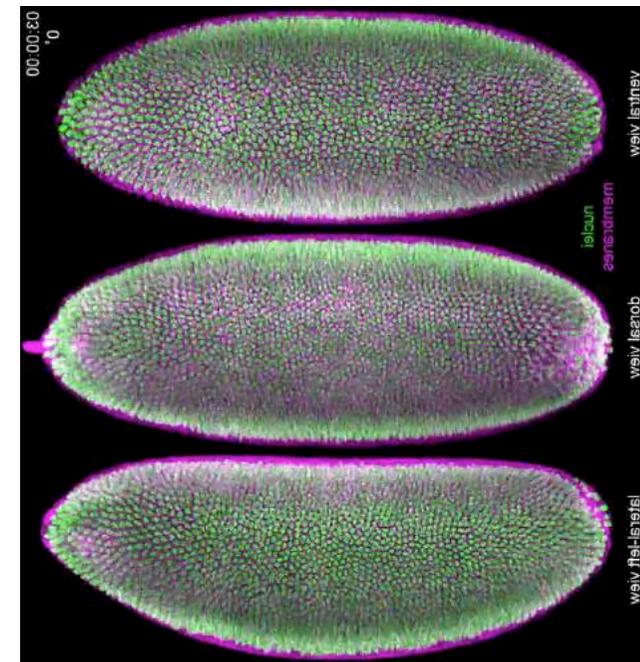
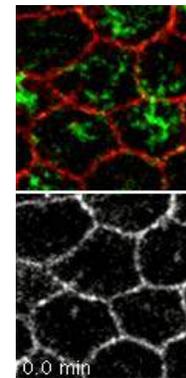
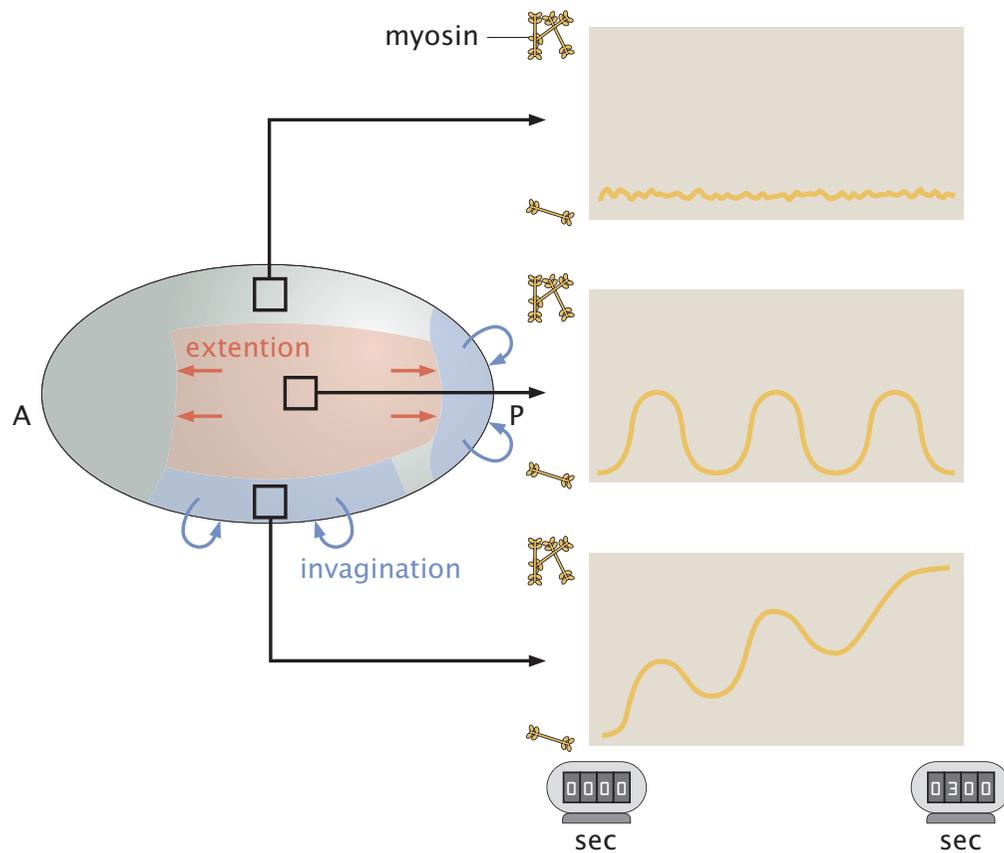
- Embryonic cells exhibit actomyosin pulsations



# V - Developmental significance

- Impact of pulsatile contractility on cellular and tissue morphogenesis: tissue invagination, tissue extension.

See Courses I 1th and 18th December



Keller lab, HHMI Janelia Campus

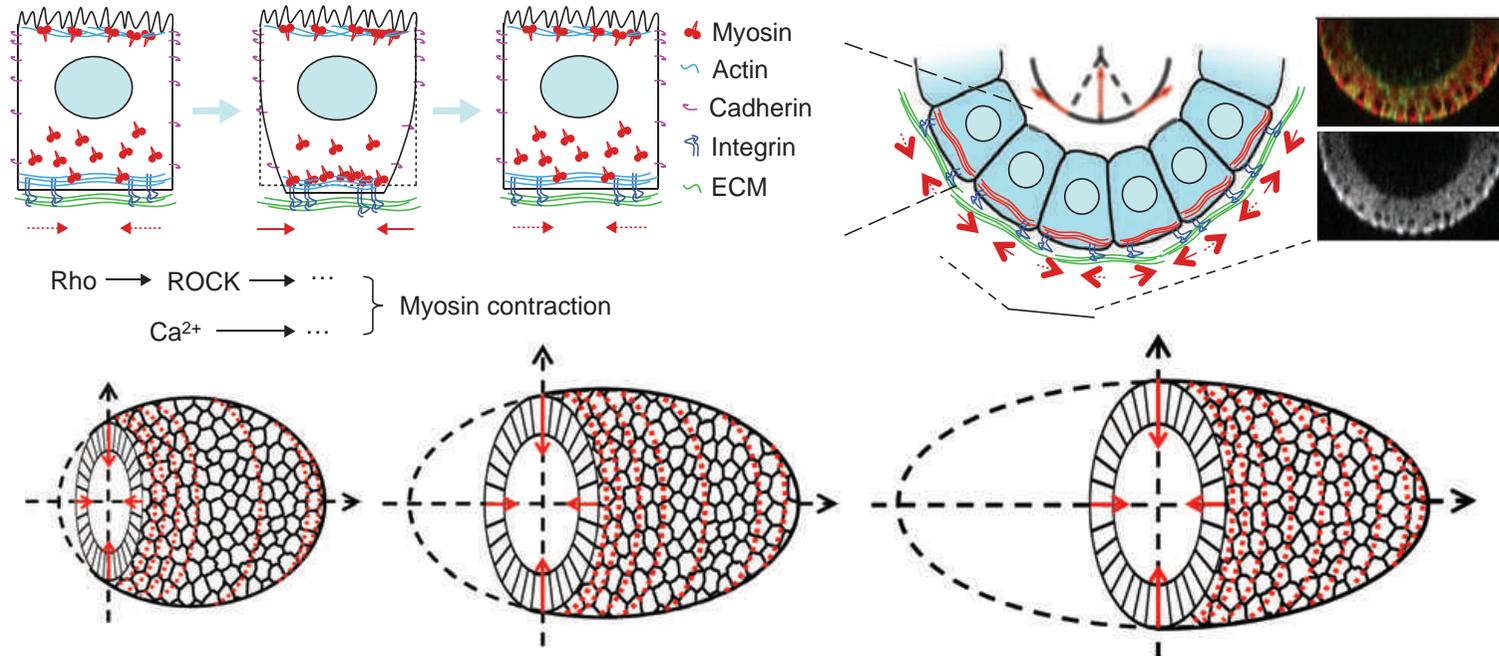
A. Martin., M. Kaschube and E. Wieschaus, *Nature* (2009) 457:495-499

M. Rauzi, PF Lenne and T. Lecuit, *Nature* (2010) 468:1110-4.

Munjal, A., Philippe, J.-M., Munro, E. & Lecuit, T. *Nature* (2015) 524, 351-355.

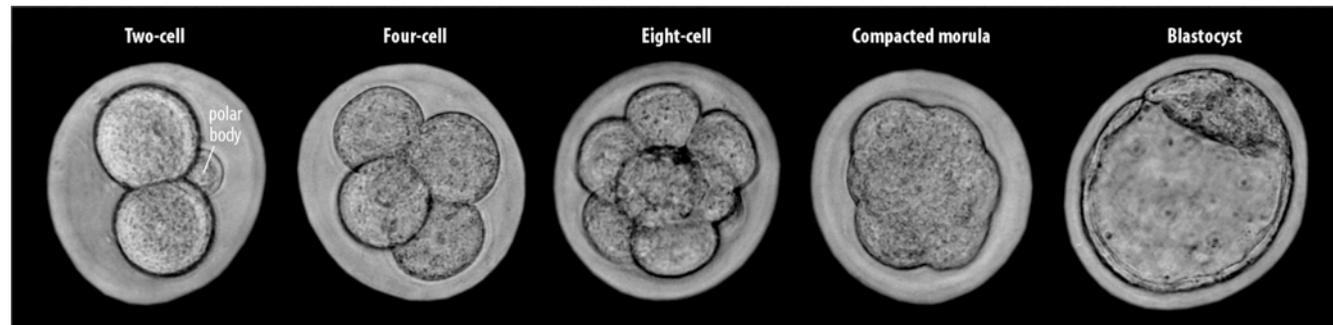
# V - Developmental significance

- Impact of pulsatile contractility on cellular and tissue morphogenesis: tissue invagination, tissue extension.

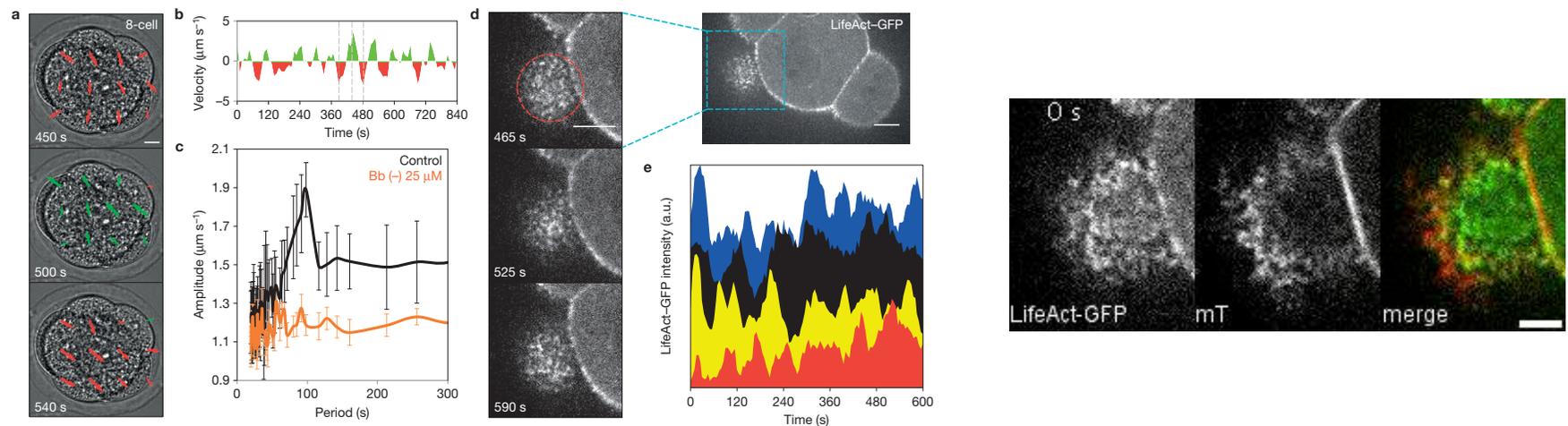


# V - Developmental significance

- Impact of pulsatile contractility on cellular and tissue morphogenesis: mouse embryo compaction



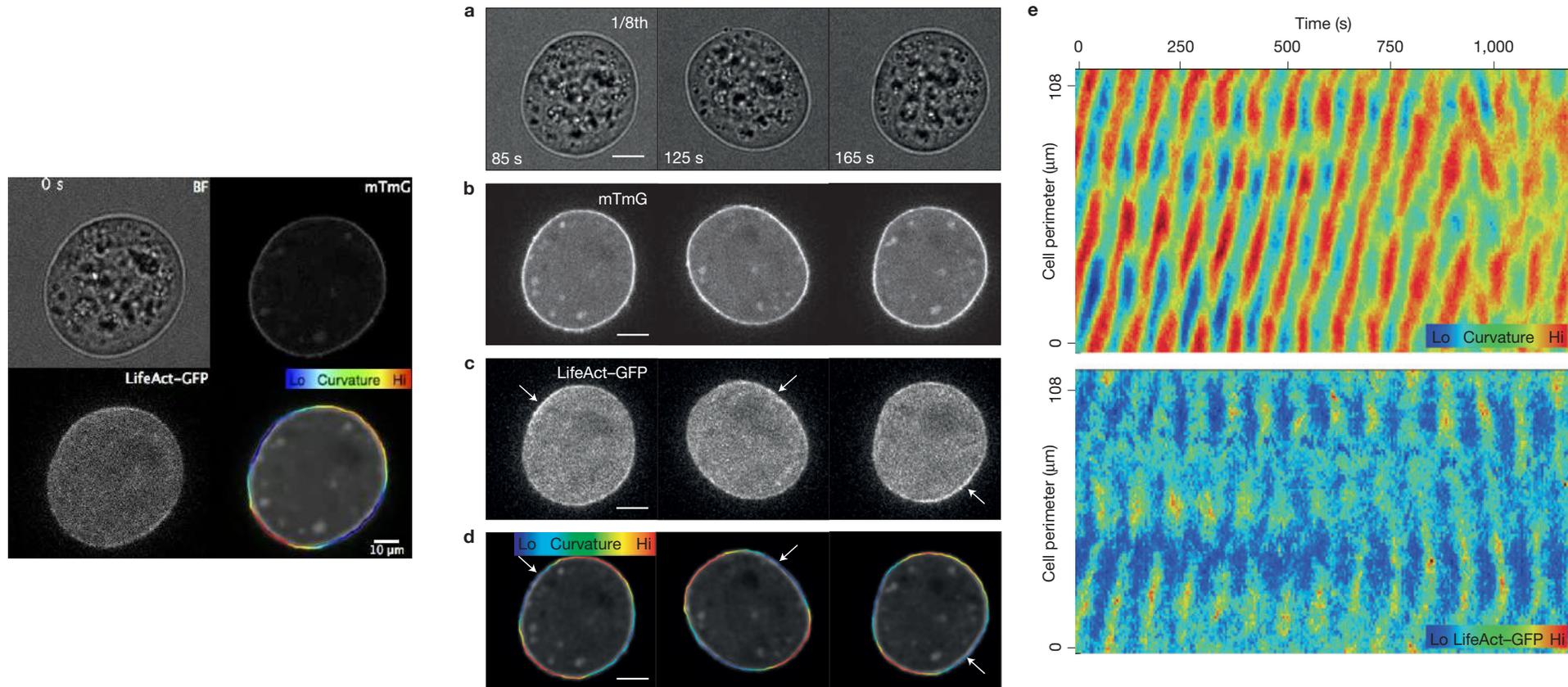
[Memorial University of Newfoundland](#)



Jean-Léon Maître, R. Niwayama, H. Turlier, F. Nédélec and, T. Hiragii. *Nature Cell Biol*, 336:1310-1314 (2015)

# V - Developmental significance

- Impact of pulsatile contractility on cellular and tissue morphogenesis: mouse embryo compaction



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# V - Developmental significance

- Spatial patterning by mechano-chemical instabilities during tubulogenesis

Viscous flow of active gel with turnover (of actin):

$$\partial_t \rho = \frac{\rho_0 - \rho}{\tau} - \partial_x(\rho v) + D \partial_{xx} \rho,$$

$$\partial_x \sigma = \xi v \quad \sigma = \chi^0 \rho / \rho_0 + \eta \partial_x v,$$

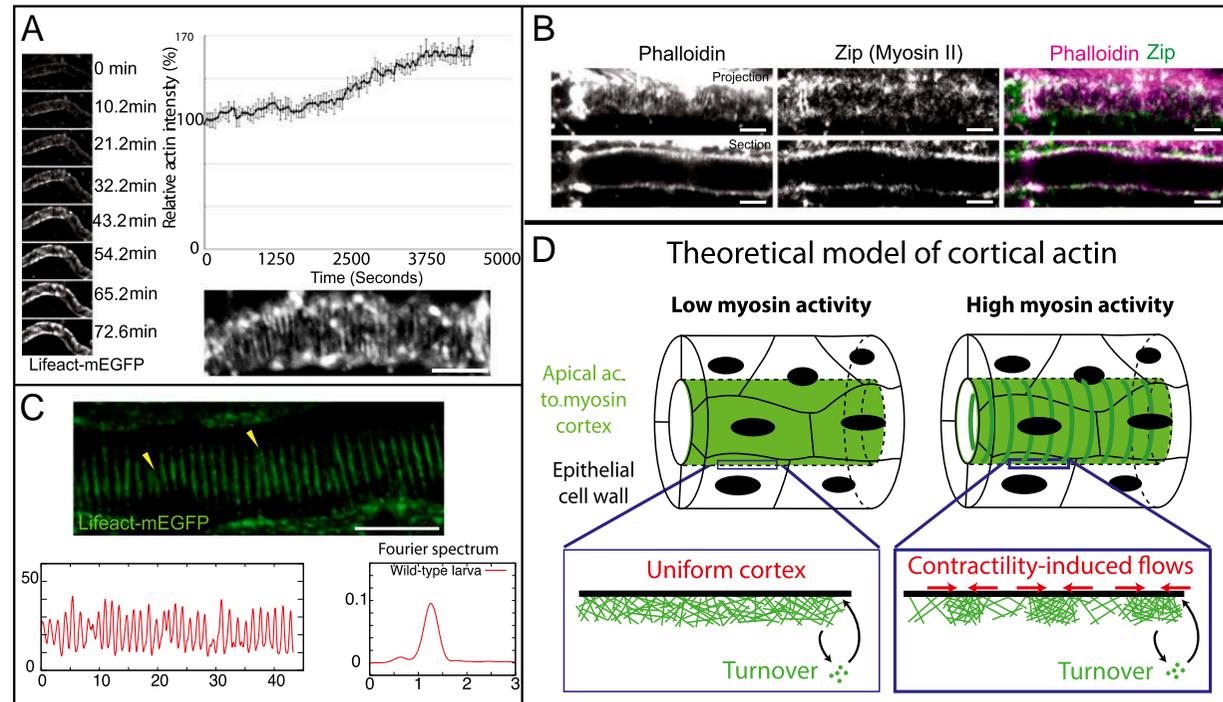
Contractility must overcome diffusion and frictional resistance to flow

Threshold for Myosin2 contractility leading to instabilities:

$$\chi_c = (\sqrt{\eta/\tau} + \sqrt{D\xi})^2$$

Wavelength of stationary pattern:

$$\lambda_c = 2\pi \left( \frac{D\tau\eta}{\xi} \right)^{1/4}.$$



E. Hannezo et al S. Hayashi and J-F. Joanny. *PNAS* 112:8620–8625 (2015)

see also: J. Bois, F. Jülicher and SW. Grill. *PRL*. 2011. 106, 028103

# V - Developmental significance

- Spatial patterning by mechano-chemical instabilities during tubulogenesis

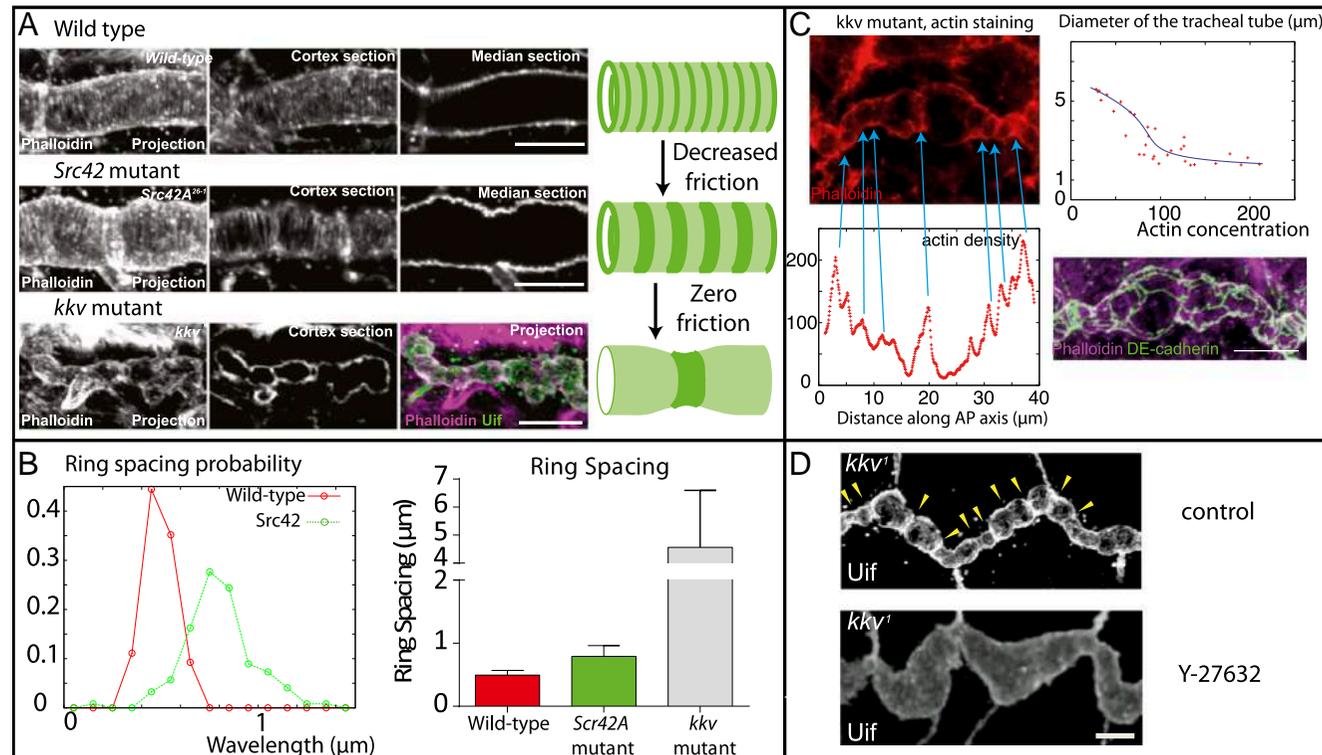
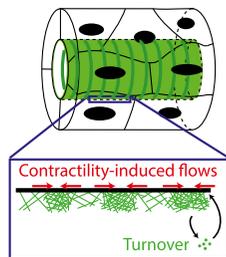
Experimental tests of the model using mutants that are expected to affect friction of the actin network with the cell boundaries:

Wavelength of stationary pattern:

$$\lambda_c = 2\pi \left( \frac{D\tau\eta}{\xi} \right)^{1/4}$$

Defects in E-cadherin  
adhesion complexes

Defects in ECM linkages:  
chitine synthase



E. Hannezo et al S. Hayashi and J-F. Joanny. *PNAS* 112:8620–8625 (2015)

# V - Developmental significance

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- Pulsatory and wave of cell contractions reveal the **out of equilibrium** nature of cell and tissue morphogenesis.

e.g. apical cell constriction during tissue internalisation and invagination.  
cell intercalation during tissue flow and extension.

- **Biological function:**

1. Pulsations prevent geometrical trap and favour exploration of cellular configurations (active noise).
2. Tissue viscoelasticity: time scale of deformations (set by pulses period) vs timescale of dissipation
3. Enables collective dynamics: non synchronous behaviour
4. Trigger waves enable rapid, long range communications
5. Trigger waves confer adaptation to environment (cell motility)

- Implication of self-organisation: high complexity of behaviours from low level developmental information.



# Self-organization



- local and direct interactions
- few rules and parameters



Complexity emerges from very simple rules  
The amount of information required to model/encode  
is very small

# Next Course



## Tissue curvature: control and self-organisation

