Verified Implementations for Real-World Cryptographic Protocols

Karthikeyan Bhargavan

+ many co-authors at Inria, MSR, CMU, Stuttgart, ...

Collège de France, March 31 2022





## Secure Channels over Insecure Networks



- We need a secure (authentic, confidential) channel
- Security against powerful attackers who may
  - Read all data sent on the network
  - Tamper with the contents of messages
  - Impersonate a user or a server





## Secure Channels in TLS [1994-2008]

<ul> <li>C → C → monespace.lcl.fr/connexion</li> <li>Dimensions: Responsive ▼ 825 × 632</li> </ul>	BROWSER	WEB	SITE
		N <sub>c</sub>	sk <sub>s</sub>
Ma vie. Ma ville. Ma bangue.	sign	(sk <sub>s</sub> , [N <sub>c</sub> ,N <sub>s</sub> ,g <sup>y</sup> ])	
Votre identifiant         9       8       7       6       5       4       3       2       1       0         Image: Second secon		g <sup>x</sup>	
Votre code personnel		►	
8     2     3     9     4       6     1     5     7     0	$K = KDF(g^{xy}, [N_c, N_s])$	K = KDF(g	g <sup>xy</sup> ,[N <sub>c</sub> ,N <sub>s</sub> ])
Image: Sources       Sources       Security ×       >       Image: Security ×<	a	e(K, data)	
Main origin       The connection to this site is using a valid, trusted server certificate issued by Sectigo RSA Organization Validation Secure Server CA.         View certificate	4	•••	
Connection - secure connection settings The connection to this site is encrypted and authenticated using TLS 1.2, ECDHE_RSA with P-256, and AES_256_GCM.			

# Secure Channels in TLS [1994-2008]

#### Classic Two-Stage Protocol

- 1. Authenticated Key Exchange Both parties compute a shared secret key K
- 2. Authenticated Encryption Both parties exchange streams of data encrypted under K
- Many variants (IPsec, SSH, TLS)
- Many security models & proofs
- So, is this a solved problem?



# Many Attacks on TLS Deployments [2011-16]

- BEAST
- CRIME
- RC4
- Lucky 13
- 3Shake
- POODLE
- FREAK
- LOGJAM
- SLOTH
- DROWN
- SWEET32

CBC predictable IVs Compression before Encryption Keystream biases MAC-Encode-Encrypt CBC Insecure resumption SSLv3 MAC-Encode-Encrypt Export-grade 512-bit RSA Export-grade 512-bit DH **RSA-MD5** signatures SSLv2 RSA-PKCS#1v1.5 **3DES** collisions

[Sep'11] [Sep'12] [Mar'13] [May'13] [Apr'14] [Dec'14] [Mar'15] [May'15] [Jan'16] [Mar'16] [May'16]

# What goes wrong in TLS Deployments?

## Crypto Weaknesses

• RC4, 3DES, MD5, PKCS#1 v1.5

## Protocol Design Flaws

• Downgrade attacks, Transcript collisions

## Implementation Bugs

• State machine bugs, Heartbleed

## Often, a mix of all of the above!



Crypto Weaknesses

## Diffie-Hellman Key Exchange



## Diffie-Hellman Assumption



**Security Assumption:** An attacker who does not know *x* or *y* cannot compute *g*<sup>*xy*</sup> mod *p* 

## Weak Diffie-Hellman Groups

If the prime p is too small, an attacker can compute the discrete log:  $y = \log(g^y \mod p)$ 

and hence compute the session key: g<sup>xy</sup> mod p

## Current discrete log computation records:

- [Joux et al. 2005]
- [Kleinjung et al. 2007]
- [Bouvier et al. 2014]
- [Kleinjung et al. 2017]
- [Boudot et al. 2019]

- 431-bit prime
- 530-bit prime
- 596-bit prime
- 768-bit prime
- 795-bit prime

## Real-World Diffie-Hellman Groups

Internet-wide scan of HTTPS servers (2015)

- 14.3M hosts, 24% support DHE
- 70,000 distinct groups (*p*,*g*)

Many small-sized prime groups used for TLS

- 84% (2.9M) servers use 1024-bit primes
- 2.6% (90K) servers use 768-bit primes
- 0.0008% (2.6K) servers use 512-bit primes

Many servers support both strong and weak groups.

# Protecting Protocols from Weak Crypto

Many deployed crypto algorithms are now considered weak

• RC4, MD5, 3DES, RSA-PKCS#1v1.5

The need for **backwards compatibility** 

- Many systems cannot be updated frequently
- Need to continue support for legacy clients/servers

## The benefits of cryptographic agility

- Gracefully transition from one algorithm to another
- Can already start supporting Post-Quantum algorithms

# Protecting Protocols from Weak Crypto

Prove the security of protocols under weak assumptions

- Do you really need a collision-resistant hash function?
- Do you really need an IND-CCA secure encryption algorithm?

## Analyze protocols that support both strong and weak crypto

- Prove security for connections that use strong crypto
- Show that strong crypto cannot be bypassed using weak crypto

## Analyzing agile protocols by hand is too hard

- Large models, subtle assumptions and goals
- Need mechanized protocol verification tools

Protocol Design Flaws

# Composing Cryptographic Constructions

Each crypto protocol composes a set of crypto constructions to achieve some target security goals

- TLS = DH + Sign + KDF + AE
- Each crypto algorithm may be individually strong, but they may not collectively achieve the desired security goal



# Composing Sub-Protocols

## Sequential or Vertical Composition

- Values generated by one protocol are used in the next
- e.g. Authenticated Key Exchange + Authenticated Encryption

## Protocols with Algorithmic Agility

- Support for multiple algorithms within a single protocol
- e.g. allow weak and strong Diffie-Hellman groups

## Parallel or Multi-mode Composition

- Many protocol flows to choose from
- Different sessions may choose a different modes

## Agility: Diffie-Hellman Group Negotiation



## Group Downgrade Attack



# What went wrong?

#### Logjam Attack [2015]

- Cryptographic weakness: Weak Diffie-Hellman Groups
- Logical protocol flaw: Downgrade from Strong to Weak Group

#### Many other examples of downgrade+crypto attacks

• FREAK, SLOTH, DROWN, ...

These attacks only appear when analyzing complex composite protocol deployments

Implementation Bugs

## Bugs in Protocol Implementations

Bugs when implementing cryptographic algorithms

- Functional correctness bugs, Side-channel leaks, ...
- e.g. Lucky13, Bleichenbacher, see OpenSSL CVEs

Bugs when parsing protocol messages and components

- Memory safety bugs (Heartbleed), Error propagation (Gotofail)
- X.509 certificate parsing errors (many CVEs)

Bugs in protocol state machine implementation (next)

• Allowing incorrect protocol flows (FREAK, SKIP)

# Many possible protocol modes of TLS

#### Protocol versions

• TLS 1.2, TLS 1.1, TLS 1.0, SSLv3, SSLv2

Key exchanges

• ECDHE, FFDHE, RSA, PSK, ...

Authentication modes

• ECDSA, RSA signatures, PSK,...

Authenticated Encryption Schemes

• AES-GCM, CBC MAC-Encode-Encrypt, RC4,...

100s of possible protocol combinations!

## State Machine for TLS-RSA Key Exchange



## State Machine for TLS-DHE Key Exchange



## Composing Protocol State Machines



# Commonly Deployed TLS State Machine

# RSA + DHE + ECDHE + Session Resumption + Client Authentication

• Covers most features used on the Web



## Full SSL/TLS State Machine

+ Fixed\_DH
+ DH\_anon
+ PSK
+ SRP
+ Kerberos
+ \*\_EXPORT
+

These are all the ones implemented in OpenSSL



# Testing TLS State Machines

#### Do popular TLS libraries conform to this state machine spec?

• Does OpenSSL? Firefox? Chrome? Safari? Java TLS? IoT devices?

## We built a fuzzing framework

- FlexTLS, based on miTLS, a verified implementation of TLS
- Generates non-conforming traces from a *formal state machine spec*
- Tests open-source libraries



# Many, Many Bugs

Unexpected state transitions in OpenSSL, NSS, Java, SecureTransport, ...

- Required messages are allowed to be skipped
- Unexpected messages are allowed to be received
- CVEs for many libraries



## Incorrectly Composing State Machines



## Incorrectly Composing State Machines

#### Follows Postel's robustness principle

 "Be conservative in what you do, be liberal in what you accept from others" (BAD for security!)

#### Introduces unexpected cases at the client

- Server skips ServerKeyExchange in DHE
- Server sends ServerKeyExchange in RSA

Correct clients should reject these cases

• Otherwise, they are not executing TLS anymore, and lose all its security guarantees

 $\mathsf{ClientHello}(v, [kx_1, kx_2, \ldots])$ ServerHello(v, kx)ServerCertificate(cert<sub>s</sub>) ServerKeyExchange(···) ServerHelloDone ClientKeyExchange(...) ClientCCS ClientFinished(mac(log,...)) ServerCCS ServerFinished $(mac(log', \cdots))$ ApplicationData\*

# SKIP: skipping Messages to Java Clients

- Network attacker impersonates api.paypal.com to a JSSE client
- 1. Send PayPal's cert



# SKIP: skipping Messages to Java Clients

Network attacker impersonates api.paypal.com to a JSSE client

- 1. Send PayPal's cert
- 2. SKIP ServerKeyExchange (bypass server signature)
- 3. SKIP ServerHelloDone



# SKIP: skipping Messages to Java Clients

Network attacker impersonates api.paypal.com to a JSSE client

- 1. Send PayPal's cert
- 2. SKIP ServerKeyExchange (bypass server signature)
- 3. SKIP ServerHelloDone
- 4. SKIP ServerCCS (bypass encryption)
- Send ServerFinished using uninitialized MAC key (bypass handshake integrity)
- 6. Send ApplicationData (unencrypted) as S.com



## State Machine Attacks

Impact of SKIP on Java TLS Clients

- A network attacker can impersonate *any* server (Paypal, Amazon, Google) to *any* Java TLS client
- Affects all versions of Java until Jan 2015 CPU

Many other State Machine bugs in TLS libraries

• FREAK: combines crypto weakness, protocol flaw, and implementation bug

# Recap: What goes wrong in TLS Deployments?

## Crypto Weaknesses

• RC4, 3DES, MD5, PKCS#1 v1.5

## Protocol Design Flaws

• Downgrade attacks, Transcript collisions

## Implementation Bugs

• State machine bugs, Heartbleed

## Often, a mix of all of the above!



Idea: Implement the full TLS protocol stack in a proof-oriented programming language and formally verify its security and correctness

- Verified Crypto (correctness, memory safety, side-channel resistance)
- Verified Parsing (memory safety, correctness)
- Verified Protocol Code (state machine correctness, security proof)

# Verifying Protocol Implementations in F\*

# F\*: a security-oriented language and verification framework



- Functional programming language (« à la Ocaml »)
- Dependent type-and-effect system (« à la Coq »)
- Proof automation via the Z3 SMT solver
- Compilers to OCaml, C, WebAssembly

#### http://fstar-lang.org

Actively developed at Microsoft Research and Inria

## Refinement types

A *refinement type* is a base type qualified with a logical formula; the formula can express invariants, preconditions, postconditions, ...

Refinement types are types of the form  $x: T\{C\}$  where

- -T is the base type,
- -x refers to the result of the expression, and
- -C is a logical formula

The values of this type are the values *M* of type *T* such that  $C\{M/x\}$  holds.

# Refinement types, Pre- and Post-Conditions

```
// Sample type and value declarations in F*
type nat = n:int{ 0 <= n }
val equal: b:bytes -> b':bytes{ length(b) = length (b')} -> bool
```

# Modular Typing & Runtime Safety

#### Type safety implies that refinement formulas hold in all executions

- All invariants, pre- and post-conditions are satisfied
- Can be used to enforce a variety of correctness and security goals
- Type-checking is modular, one function at a time, so scales well

```
THEOREM 1 (Safety). If \emptyset \vdash A : T then A is safe.
```

We write  $I_0 \vdash A \rightsquigarrow I$  when, in the typing environment  $I_0$ , the module *A* is well-typed and exports the interface *I*.

If  $\emptyset \vdash A_0 \rightsquigarrow I_0$  and  $I_0 \vdash A : T$ , then  $\emptyset \vdash A_0 \cdot A : T$ .

# F\*: verification by type-checking + SMT

- 1. Write a program as an F\* module
- 2. Specify its properties in an F\* interface
- 3. Your program can call other verified user modules and trusted system libraries
- 4. Verify the module by typechecking:
  - F\* generates proof obligations, and calls Z3, an SMT solver, to discharge them
- 5. Compile the module to executable code
  - Backends for OCaml, C, and WebAssembly



# Verifying Protocol Components with F\*

## EverParse: verified zero-copy parsers in C [Usenix '19]

- Efficient parsers without memory safety bugs (i.e. no HeartBleed)
- Proofs of functional correctness for parsing
- Applied to TLS, Quic, (X.509), ...

## HACL\*: verified crypto library in C and WebAssembly [CCS'17,'20]

- A full library of modern crypto algorithms
- Verified for memory safety, functional correctness, and secret independence (e.g. no branches on secrets)

## Both written in Low\*, a C-like subset of F\* [ICFP '17]

• Verified code is compiled via KaRaMeL to C and WebAssembly

## A Low\* Spec for Stateful Crypto Code

```
// An array of secret (opaque) bytes
type block p = b:buffer uint8{ length(b)=16 }
// Stateful in-place encryption
val encrypt: k:key p -> p:block p ->
             Stack unit
              (requires (fun h0 ->
                   live h0 [k;p] /\ disjoint k p))
              (ensures (fun h0 h1 ->
                   modifies [p] h0 h1 /\
                   content h1 p ==
                   AES(content h0 k, content h0 p))
```

# Verifying Protocol Implementations with F\*

#### Verified protocol components

- EverParse: verified zero-copy parsers in C
- HACL\*: verified crypto library in C and WebAssembly

## miTLS: a cryptographically verified implementation of TLS

- Based on precise computational crypto assumptions
- Proofs require a combination of manual and F\* proofs

## **DY\***: a symbolic protocol verification framework in F\*

- Based on abstract symbolic crypto assumptions
- Proofs are fully mechanized in F\*

# Verified Security for Protocol Code: miTLS in F\*

## miTLS [2012-2015]

## A verified reference implementation of TLS

- Covers TLS 1.0-1.2
- Covers all major protocol modes and ciphersuites

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## Modular Architecture for miTLS



# miTLS Security theorem

Main crypto theorem: concrete TLS & ideal TLS are computationally indistinguishable

uses F\* typing + crypto reasoning

We then prove that ideal miTLS meets its secure channel spec uses F\* typing

We transform one module at a time based on a precise crypto assumption



## Example: Message Authentication Codes

```
module MAC
type text = bytes val macsize
type key = bytes
type mac = bytes
```

val GEN : unit -> key
val MAC : key -> text -> mac
val VERIFY: key -> text -> mac -> bool

basic F\* interface

This interface says nothing on the security of MACs.

MAC keys are abstract

module MAC
type text = bytes val macsize
type key
type mac = bytes

val GEN : unit -> key
val MAC : key -> text -> mac
val VERIFY: key -> text -> mac -> bool

MAC keys are abstract

<pre>module MAC type text = bytes val macsize type key</pre>	MACs are fixed sized
<pre>type mac = b:bytes{Length(b)=macs</pre>	ize}
<pre>val GEN : unit -&gt; key val MAC : key -&gt; text -&gt; mac val VERIFY: key -&gt; text -&gt; mac -&gt;</pre>	bool



MAC keys are abstract

<pre>module MAC type text = bytes val macsize type key</pre>	MACs are fixed sized		ideal F* interface
<pre>type mac = b:bytes{Length(b)=macs predicate Msg of key * text val GEN : unit -&gt; key</pre>	ize} Msg is protoco	spec ols us	cified by ing MACs
<pre>val MAC : k:key -&gt; t:text{Msg(k, val VERIFY: k:key -&gt; t:text -&gt; mac</pre>	t)} -> mac sg(k,t)}	"Al ha	l verified messages ave been MACed"
		т	his can't be true! (collisions)
<pre>module MAC open System.Security.Cryptography let macsize = 20 let GEN() = randomBytes 16 let MAC k t = (new HASHMACSHA1(k)) let VERIFY k t m = (MAC k t = m)</pre>	.ComputeHash	nt (	concrete F* implementation using real crypto)

Crypto Assumption: INT-CMA Resistance to Chosen-Message Existential Forgery Attacks

```
module INT CMA Game
open Mac
                             Computational Safety
Let private k = GEN()
                             a probabilistic polytime program
let private log = ref []
                             calling mac and verify forges a MAC
let mac t =
                             only with negligible probability<sup>2</sup>
  log := t::!log
  MAC k t
let verify t m =
                                                         CMA game
  let v = VERIFY k t m in
                                                        (coded in F*)
  if v && not (mem t !log) then FORGERY
  V
```

## Computational Safety for Ideal MACs



## Modular Architecture for miTLS



A High-Level Secure Channel API for TLS

- Secrecy and authenticity for application data
- Multiple ciphers (Agile)
- Multiple protocol modes
- Accounts for key compromise

Prevents large classes of attacks

- no state machine bugs
- no downgrade attacks

```
type cn // for each local instance of the protocol
// creating new client and server instances
val connect: TcpStream -> params -> (;Client) nullCn Result
val accept: TcpStream -> params -> (;Server) nullCn Result
// triggering new handshakes, and closing connections
val rehandshake: c:cn{Role(c)=Client} -> cn Result
val request:
                c:cn{Role(c)=Server} -> cn Result
val shutdown: c:cn -> TcpStream Result
// writing data
type (;c:cn,data:(;c) msg_o) ioresult_o =
 WriteComplete of c':cn
 WritePartial of c':cn * rest:(;c') msg_o
               of c':cn
 MustRead
val write: c:cn -> data:(;c) msg_o -> (;c,data) ioresult_o
// reading data
type (;c:cn) ioresult_i =
           of c':cn * data:(;c) msg_i
 Read
```

CertQuery of c':cn

| Handshake of c':cn

```
| Close of TcpStream
| Warning of c':cn * a:alertDescription
```

```
| warning of c :cn * a:atertDescriptio
```

```
| Fatal of a:alertDescription
```

```
val read : c:cn -> (;c) ioresult_i
```

# miTLS Impact and Verification Effort

## First verified implementation of real-world protocol

- 3600 lines of code
- 2000 lines of type annotations
- 30 pages of crypto proofs, supported by 3000 lines of EasyCrypt proof
- 3 years of concerted effort by a team of 5-10 researchers

#### Measurable impact on real-world protocol design

- Helped find attacks on TLS: Triple Handshake, SKIP, FREAK, Logjam
- Influenced design of TLS 1.3 at IETF

Can we scale up and generalize this approach to other protocols?

## DY\* Verification Architecture [Euro S&P 2021, ACM CCS 2021]



## A taste of DY\*

#### type message = I Msg1: i:principal → n\_i: bytes → message I Msg2: n\_i: bytes → n\_r:bytes → message I Msg3: n\_r: bytes → message val serialize\_message: message → bytes val parse\_message: bytes → result message val parse\_message\_correctness\_lemma: m:message → Lemma (parse\_message (serialize\_message m) == Success m)

#### **Precise Message Formats**

 serialization and parsing with correctness proofs

type session\_st = | SecretKey: secret\_key: bytes  $\rightarrow$  session\_st | PublicKey: peer:principal  $\rightarrow$  public\_key:bytes  $\rightarrow$  session\_st | ISentMsg1: r:principal  $\rightarrow$  n\_i:bytes  $\rightarrow$  session\_st | RSentMsg2: i:principal  $\rightarrow$  n\_i:bytes  $\rightarrow$  n\_r:bytes  $\rightarrow$  session\_st | ISentMsg3: r:principal  $\rightarrow$  n\_i:bytes  $\rightarrow$  n\_r:bytes  $\rightarrow$  session\_st | RReceivedMsg3: i:principal  $\rightarrow$  n\_r:bytes  $\rightarrow$  session\_st val serialize\_session\_st: session\_st  $\rightarrow$  bytes val parse\_session\_st: bytes  $\rightarrow$  result session\_st

#### **Protocol State Machine**

- Stateful protocol code
- Session state storage
- Fine-grained compromise



**Typed Crypto API encodes symbolic crypto assumptions** Using secrecy labels and authentication predicates

val pke\_enc: #i:nat → #l:label → #s:string →
 public\_enc\_key i I s →
 m:msg i l{pke\_pred m} → msg i Public
val pke\_dec: #i:nat → #l:label → #s:string →
 private\_dec\_key i I s → msg i Public →
 result (m:msg i l{is\_publishable i m ∨ pke\_pred m})

Security Label in Signal Protocol Meet (Join (Can\_Read [P i]) (Can\_Read [P r])) (Meet (Join (Can\_Read [V i *sid*<sub>i</sub> 0]) (Can\_Read [P r])) (Meet (Join (Can\_Read [V i *sid*<sub>i</sub> 0]) (Can\_Read [P r])) (Join (Can\_Read [V i *sid*<sub>i</sub> 0]) (Can\_Read [V r *sid*<sub>r</sub> 0])))

# DY\*: scalable symbolic security verification

	Modules	FLoC	PLoC	Verif. Time	Primitives
Generic DY*	9	1,536	1,344	$\approx 3.2 \text{ min}$	-
NS-PK	4	439	-	(insecure)	PKE
NSL	5	340	188	$\approx 0.5 \text{ min}$	PKE
ISO-DH	5	424	165	$\approx 0.9 \text{ min}$	DH, Sig
ISO-KEM	4	426	100	$\approx 0.7 \text{ min}$	PKE, Sig
Signal	8	836	719	$\approx 1.5 \text{ min}$	DH, Sig, KDF,
					AEAD, MAC

- Proofs require between 50% and 90% annotation overhead
- Verification time grows linearly with protocol size

# Conclusions

## End-to-End verification of protocol stacks is now feasible

- Using proof-oriented programming languages like F\*
- Crypto (HACL\*), Parsers (EverParse), Protocols (miTLS, DY\*)

## Area is still maturing and is under active research

- Verifying optimized low-level code in C and assembly
- Verifying protocols that use ZK proofs, or MPC, or FHE, or PQ

#### Many open problems for future work

- Proving the absence of side channel attacks
- Verifying code written by non-verification experts